

# Experimental Study on Seawater Freeze Desalination Based on Ultrasonic Vibration

Han Yuan<sup>a,\*</sup>, Suyun Yi<sup>a</sup>, Qizhi Gao<sup>a</sup> and Haibin Wang<sup>b</sup>

*a Marine Engineering, College of Engineering, Ocean University of China,*

*238 Songling Road, Laoshan district, Qingdao, 266100, China*

*b Naval Architecture and Marine Engineering, University of Strathclyde,*

*Glasgow G4 0LZ, United Kingdom*

\* Corresponding author

Phone/Fax: +86-532-66781105,

E-mail: [hanyuan@ouc.edu.cn](mailto:hanyuan@ouc.edu.cn) (Han Yuan)

Address: 238 Songling Road, Laoshan district, Qingdao 266100, China

## Abstract

Seawater freeze desalination is a promising technology with low energy consumption; however, the presence of salt inclusions during the freezing process presents a challenge to enhancing desalination efficiency. While ultrasonic vibration has been proven effective in reducing the supercooling degree and energy consumption in pure water freezing, its impact on seawater desalination efficiency remains to be investigated. This study experimentally explores the characteristics of seawater freeze desalination under ultrasonic vibration. An ultrasonic-assisted seawater freeze crystallizer was designed, and experiments were conducted to compare and analyze the freeze desalination performance of the crystallizer with and without ultrasonic vibration. The findings reveal that ultrasonic vibration significantly enhances desalination by promoting the formation of smaller ice crystals, resulting in a substantial increase in desalination rates ranging from 18.18% to 67.86%, with an average improvement of

25 approximately 32.62%. Additionally, the application of ultrasonic vibration accelerates  
26 the icing process by approximately 8%. Notably, during continuous desalination  
27 operations, the effectiveness of ultrasonic vibration gradually diminishes as salinity  
28 decreases. Nonetheless, the ultrasonic vibration-based freeze-reverse osmosis  
29 (Ultrasonic-Freeze-RO) method offers significant advantages in terms of reduced costs  
30 and energy consumption compared to both freeze-reverse osmosis (Freeze-RO) and  
31 traditional reverse osmosis (RO) methods.

32 **Keywords:** ultrasonic vibration; freeze desalination; experimental study; energy  
33 consumption

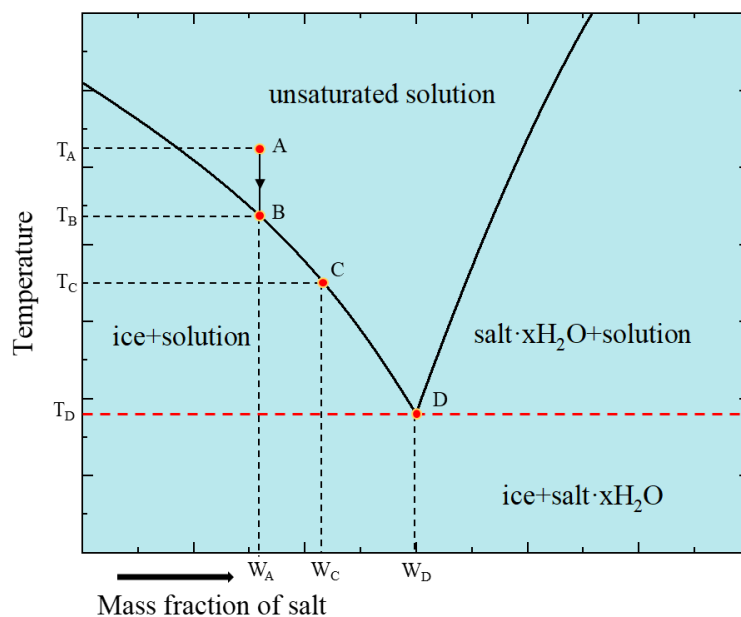
34

## 35 **1 Introduction**

36 According to statistics, seawater accounts for 97.5% of the total water on Earth,  
37 and this saline water is difficult to be directly used for irrigation, drinking, and industrial  
38 purposes. The remaining 2.5% of freshwater, of which only less than 1% is available  
39 for use[1, 2]. With the continuous growth of the world's population and industrial  
40 development, the global demand for freshwater is increasing, leading to a global  
41 freshwater shortage. The Millennium Development Goals Report pointed out that in  
42 2015, approximately 40% of the global population faced water scarcity, and this number  
43 is expected to continue to rise[3]. Therefore, utilizing and developing the abundant  
44 seawater resources into freshwater can significantly alleviate the freshwater crisis,  
45 leading to the emergence of seawater desalination technology[4, 5]. Currently, the  
46 commonly used methods for seawater desalination are reverse osmosis (RO) and  
47 thermal methods, particularly multi-stage flash distillation (MSF) and multi-effect  
48 distillation (MED) are widely applied in large-scale seawater desalination plants[6, 7].  
49 However, these seawater desalination technologies mentioned above are prone to  
50 severe scaling issues and have relatively high energy requirements[8, 9].

51 In recent years, the freezing desalination technology has been considered as one  
52 of the most promising seawater desalination technologies. The freezing desalination  
53 technology utilizes the theory of solid-liquid equilibrium to desalinate saline seawater.

54 Its advantages lie in low energy consumption and environmental, with energy  
55 consumption only about one-seventh of that of thermal desalination [10]. Generally, in  
56 the presence of inorganic salt components in a water solution, the crystallization  
57 temperature is lowered. As the temperature decreases, the water in the solution will first  
58 freeze, obtaining pure water without impurities as a solid phase separation. The  
59 inorganic salts and other impurities will continue to remain in the solution, and through  
60 solid-liquid separation, ice with lower salinity and concentrated brine with higher  
61 salinity can be obtained, achieving the purpose of desalination[11]. Figure 1 shows a  
62 schematic diagram of a binary water-salt system. Point D represents the eutectic point,  
63 where ice, salt, and saturated solution coexist. When a solution with solute mass  
64 concentration  $W_A$  at temperature  $T_A$  decreases to  $T_B$  (liquid phase line), ice phase begins  
65 to precipitate. As the temperature continues to decrease, the solution gradually enriches  
66 along line BC to the eutectic point D, during which the amount of ice increases  
67 continuously, and the remaining saline water's salinity increases. Upon reaching point  
68 D, salt crystals and ice crystals precipitate simultaneously. Below the eutectic point, salt  
69 hydrates and ice are generated simultaneously without leaving any liquid[12].



70

71

Figure 1 Binary water-salt system phase diagram

72

73

In addition, the ice crystals generated in the process of freezing desalination can also be used to store cold energy to meet the needs of refrigeration and food

74 refrigeration[13]. Some scholars have studied the application of freezing desalination  
75 in the treatment of desulfurization wastewater[11], concentrated apple juice[14], wine  
76 production[15] and cold energy utilization of LNG[16].

77 Common methods for seawater freezing desalination typically include direct  
78 contact and indirect contact methods. The direct contact method involves direct contact  
79 between the refrigerant and seawater, causing freezing on the contact surface and  
80 producing ice crystals, thereby obtaining solid freshwater with lower salinity. For  
81 example, using silicone oil, natural gas, etc., as refrigerants to obtain ice with lower  
82 salinity[17, 18]. The advantages of the direct contact method are high ice production  
83 rate and low power consumption. However, its disadvantages are also significant, as it  
84 requires additional separation methods to separate ice crystals and refrigerants, such as  
85 washing. This undoubtedly leads to certain losses. The indirect contact method uses a  
86 heat-conducting solid surface to separate the refrigerant from the saline water,  
87 eliminating the need for additional washing or treatment processes.

88 Many scholars have conducted relevant research on indirect contact seawater  
89 freezing desalination[7]. Eghtesad[19] conducted numerical studies and multi-objective  
90 optimization on indirect freezing seawater desalination, suggesting that the  
91 refrigeration capacity has a certain impact on the recovery rate and desalination rate. A  
92 larger refrigeration capacity leads to an increase in ice crystal production and recovery  
93 rate, but more salt crystals are trapped in the gaps of the ice crystals, resulting in a  
94 decrease in desalination rate. In other words, the desalination rate and recovery rate  
95 constrain each other. Jayakody[20] modeled and simulated indirect seawater freezing  
96 desalination using an ice maker to study the effects of freezing temperature and initial  
97 salinity of the saline water on ice crystal production and the final salinity of ice and  
98 brine. As the freezing temperature decreases, the low temperature increases ice  
99 production, accelerates the freezing rate of saline water, and enhances the solidification  
100 rate. It is believed that using two-stage freezing desalination can effectively obtain low  
101 salinity freshwater. Yuan and Sun[21] conducted experimental research on a ship  
102 exhaust waste heat-driven seawater freezing desalination system as a pre-desalination

103 for reverse osmosis desalination, and found that a two-stage freezing desalination  
104 system as a pre-desalination for reverse osmosis desalination has good economic  
105 benefits. In addition, some scholars have used various technological improvements to  
106 increase the desalination rate of the produced ice crystals, such as centrifugal  
107 separation[22], washing[23], sweating[24], and comprehensive methods[25]. These  
108 technologies can significantly improve the desalination rate of seawater but lead to a  
109 significant decrease in seawater recovery rate.

110 In current research, although low-temperature seawater freezing desalination  
111 technology offers advantages such as ease of operation and environmental friendliness,  
112 its desalination efficiency is relatively low, necessitating the use of additional methods  
113 for auxiliary treatment. Some scholars have explored the use of nucleating agents to  
114 accelerate the formation of ice crystals, thereby reducing the amount of salt trapped in  
115 the ice crystals and improving the desalination effectiveness[26, 27]. However, this  
116 approach can increase the operational costs of the freezing desalination system and  
117 require additional steps for removing the nucleating agents, thereby increasing the  
118 complexity of wastewater treatment.

119 Ultrasound is a high-frequency sound wave characterized by strong penetrative  
120 properties. When positive and negative pressure waves generated by ultrasound  
121 propagate in a liquid and reach a certain intensity, they create cavitation bubbles  
122 (negative pressure) and bubble collapse (positive pressure) within the liquid. After  
123 multiple cycles, the tiny cavitation nuclei inside the liquid undergo a series of oscillation,  
124 growth, collapse, and fragmentation processes. Studies have shown that the cavitation  
125 effect generated by ultrasound vibration can influence the degree of solution  
126 undercooling and saturation, effectively enhancing the cold energy diffusion in the  
127 system and providing nucleation sites, thereby improving the effectiveness of freezing  
128 desalination[28-31].

129 However, a notable research gap exists in the scarcity of studies exploring the  
130 effect of ultrasonic vibration on desalination during seawater freezing, considering the  
131 intricate mass transfer and desalination dynamics inherent in this process. To date,

132 among the few studies conducted, Phelan [32] focused exclusively on the ultrasonic  
133 freezing behavior of pure water, demonstrating that ultrasonic waves significantly  
134 decrease the supercooling required for water to freeze and shorten the freezing duration,  
135 thus reducing overall freezing energy consumption. Specifically, the application of 197  
136 J and 462 J of ultrasonic energy resulted in energy savings of 12.4% and 10.8%,  
137 respectively. This characteristic establishes a robust foundation for the potential  
138 utilization of ultrasonics in seawater desalination through freezing methods.  
139 Furthermore, Zhang [33] conducted experimental research on the desalination behavior  
140 of sea ice melting enhanced by ultrasonic vibration, verifying that it accelerates the  
141 melting speed and improves the removal efficiency of total dissolved solids (TDS) and  
142 salt from sea ice, suggesting further opportunities for exploiting ultrasonic vibration  
143 during sea ice melting processes. Nevertheless, despite these initial insights, no research  
144 has yet specifically addressed the influence of ultrasonic vibration on the desalination  
145 efficacy during the actual freezing process of seawater.

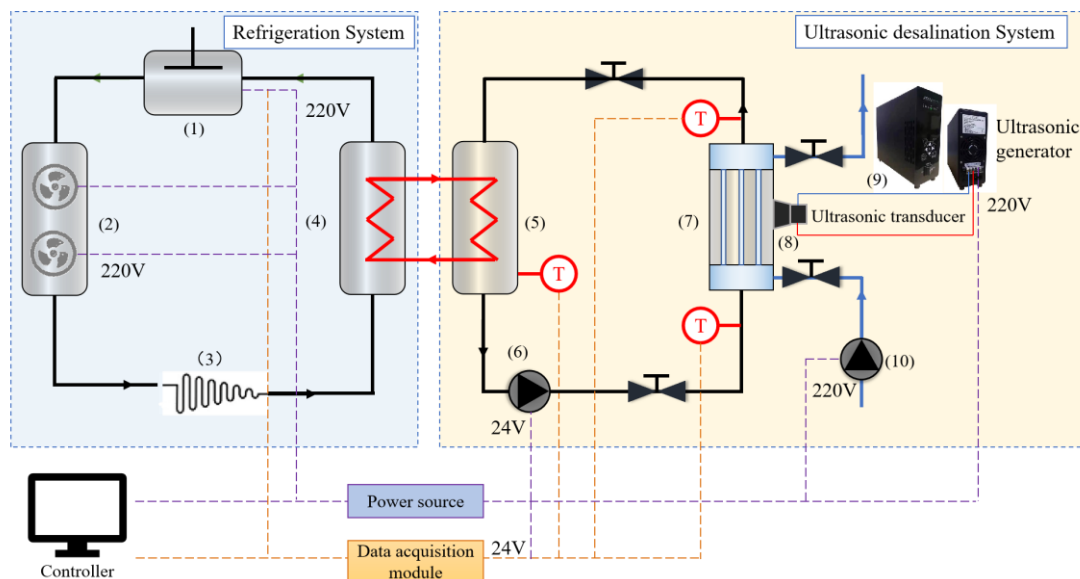
146 In this manuscript, to further investigate the relationship between ultrasound  
147 vibration and its impact on desalination rate and ice formation rate in the seawater  
148 freezing desalination process, we selected three independent variables: freezing  
149 temperature, freezing time, and seawater salinity. We constructed an experimental  
150 platform for ultrasound-assisted seawater freezing desalination and designed and  
151 conducted orthogonal experiments. To control the temperature of the freezing medium,  
152 a compression refrigeration unit was used to control the temperature of the glycerol-  
153 water solution in the storage tank. The main objective of this work is to verify the  
154 promoting effect of ultrasound vibration on the desalination efficiency of seawater  
155 inside the tube, establish relevant fitting equations, and study the economic feasibility  
156 of ultrasound-assisted secondary seawater desalination as a pre-desalination method for  
157 reverse osmosis desalination.

158 In the part 2 of this manuscript, detailed information about the experimental setup  
159 is provided. The part 3 introduces the experimental principles and analysis processes.  
160 The part 4 presents the experimental results and conducts data analysis.

161

## 162 2 Experimental setups

163 The schematic diagram of the ultrasonic freezing desalination system is shown in  
164 Figure 2. The experimental setup consists of two main sections: the refrigeration cycle  
165 system and the seawater freezing desalination experimental system. In the refrigeration  
166 cycle system, a compressed refrigeration cycle is employed to cool a glycerol-water  
167 mixture in the cold storage tank, which acts as the cold source medium for seawater  
168 freezing. The heat transfer medium in the cold storage tank is a 66.7% glycerol-water  
169 solution, which is pumped into the freezing crystallizer device through a cooling  
170 medium pump to freeze the seawater. The ultrasonic generator is used to adjust the  
171 frequency and power output of the ultrasonic oscillator. The data acquisition module  
172 monitors experimental data in real time. The controller is used to coordinate the  
173 operation of various components and record data. Further detailed information on the  
174 components of the test stand will be provided in the subsequent sections.



175

176 Figure 2 Schematic diagram of the ultrasonic freezing desalination system: (1)  
177 compressor, (2) condenser, (3) capillaries, (4) evaporator, (5) cold storage tank, (6)  
178 glycerin solution pump, (7) freezing crystallizer, (8) ultrasonic transducer, (9)  
179 ultrasonic generator, (10) seawater pump; (b) experimental setup

180

## 2.1 Seawater freezing desalination experimental system

The experimental setup of the ultrasonic freezing desalination system is shown in Figure 3. To minimize the impact of external environmental temperature on the working fluid inside the pipes and heat exchangers, adequate insulation measures were implemented using foam boards and thermal insulation materials. Additionally, low-temperature phase change materials (PCM) were placed to further reduce the internal temperature of the experimental setup. All cooling medium pipelines in the experimental setup are made of 3-inch PE pipes with corresponding quick couplings, ensuring good sealing and insulation. The connection between the cooling medium pipelines and the heat exchangers is achieved using stainless steel 304 tower heads and rubber hoses. The seawater channel employs a backflow structure, regulating the flow of seawater into the freezing desalination experimental device by adjusting the valve opening at the inlet of the heat exchanger.

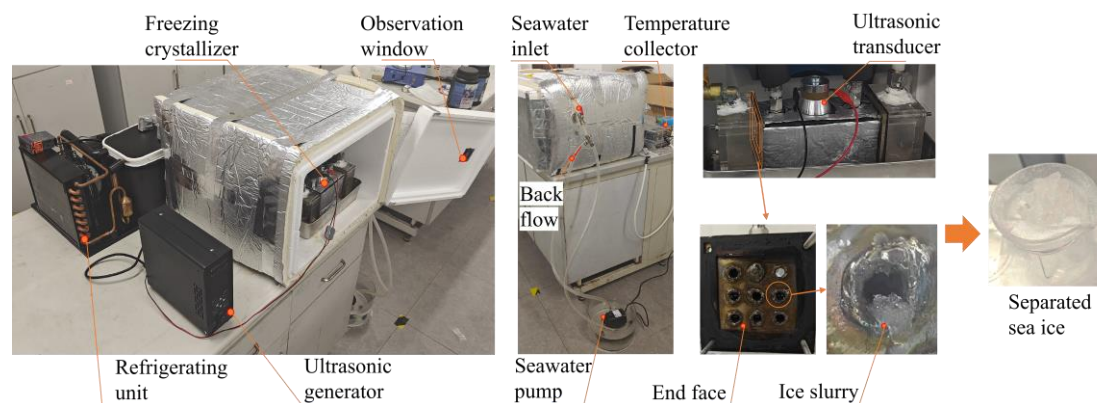


Figure 3 Experimental setup of the ultrasonic freezing desalination system

The cooling medium pump in this experimental setup is a small gear oil pump with a pure copper pump head. This gear pump operates at a rated voltage of 24V and a rated current of 3.2A, controlled by an adjustable voltage and current DC power supply, and it transports the cooling medium (glycerol-water solution) to the freezing crystallizer.

The temperature acquisition module uses the Sulinkiot 8-channel thermocouple data acquisition module, which reads the potential difference signals generated by the thermocouple due to the thermoelectric effect and converts them into temperature



204 signals. These temperature data can be transmitted to the computer system via a USB  
205 to RS486 module. A T-type ultra-fine thermocouple is used to collect the temperatures  
206 at the inlet and outlet of the heat exchanger, monitoring the temperature of the glycerol  
207 at the inlet and outlet of the freezing crystallizer. This setup aims to obtain the  
208 temperature curve of the heat exchanger when it reaches a steady state. Programming  
209 is conducted in Python to collect, output, and save the temperature signals generated by  
210 the temperature acquisition module every 2 seconds.

211 The ultrasonic generator converts electrical energy into high-frequency alternating  
212 current signals that match the ultrasonic transducer, transmitting them to the ultrasonic  
213 oscillator, and converting the input electrical power into ultrasonic waves for  
214 transmission. The ultrasonic oscillator has a specific frequency, and the ultrasonic  
215 generator must generate electrical signals of the corresponding frequency to prevent  
216 reverse electromagnetic force, which could damage the ultrasonic generator. In this  
217 experimental setup, the KMD-M3 ultrasonic generator is selected, with an adjustable  
218 frequency range of 17-120 kHz. According to reference [34], the application of high-  
219 frequency ultrasound results in an increase in heat generated by the ultrasonic thermal  
220 effect. Additionally, the rise in ultrasonic frequency during the freezing process extends  
221 the growth cycle of cavitation bubbles, introducing new physical phenomena that are  
222 detrimental to the study of desalination characteristics. Therefore, a 40 kHz ultrasonic  
223 transducer with a power of 60W was selected for the experiment.

224 The list of the main experimental equipment and data acquisition devices used in  
225 this study is shown in Table 1.

226 Table 1 List of experimental equipment and measurement device parameters

Name	Manufacturer	Model	Parameters
T-type Micro Thermocouple	Aidewin	T-type 1m Welding Pin	-200~200°C, ±0.1°C
Temperature Data Acquisition Module	Sulingke	RS20K-C	±1°C
USB to RS485 Converter	Sulingke	—	CH340 Chip
Gear Pump	Guojiang New	FP-24	24V 3.2A

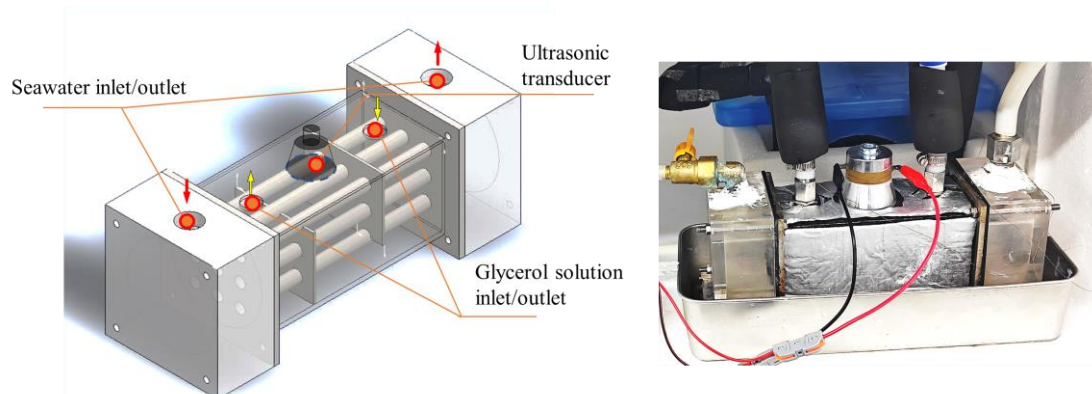
Name	Manufacturer	Model	Parameters
	Energy		
Ultrasonic Generator	KMD	KMD-M3	17-120kHz
Ultrasonic Transducer	KMD	—	40kHz 60W
Seawater Submersible Pump	SoulLi	—	35W

227

## 228 2.2 Ultrasonic freezing crystallizer

229 The schematic diagram and setup picture of the ultrasonic freezing crystallizer for  
230 seawater desalination is shown in Figure 4, which features a shell-and-tube heat  
231 exchanger structure. To ensure relatively high and consistent heat transfer efficiency, a  
232 counter-current heat exchange method is uniformly adopted in this experiment. The  
233 materials for the inner tube, baffle plate, and outer wall of the heat exchanger are all  
234 stainless steel 304. The inner tube has an inner diameter of 9 mm, a length of 16 cm,  
235 and a wall thickness of 1 mm, while the baffle plate and outer wall have a thickness of  
236 3 mm. These components are fixed and connected using argon arc welding. The outer  
237 surface of the heat exchanger is insulated with a 1 cm thick layer of thermal insulation  
238 cotton.

239 The seawater inlet and outlet are located on both sides of the device and are made  
240 of acrylic material. These parts are fixed and sealed to the heat exchanger using screws  
241 and rubber pads to prevent seawater leakage. The ultrasonic oscillator is installed at the  
242 center of the upper wall surface, as shown in the diagram, and is fixed and connected  
243 using a special adhesive designed for ultrasonic oscillators.



244

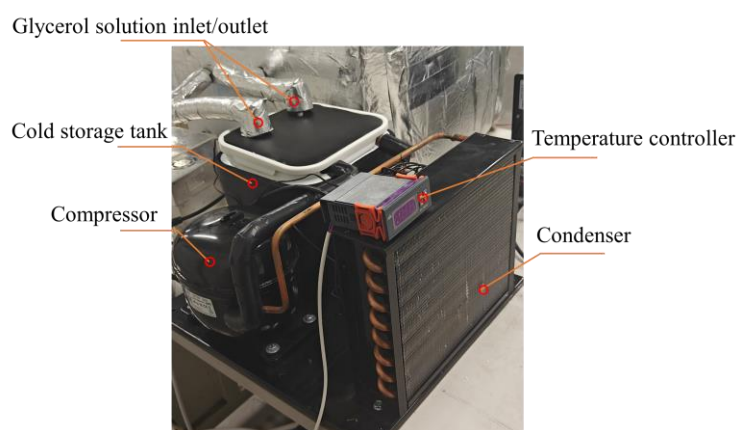
245 Figure 4 Schematic and setup picture of the ultrasonic freezing crystallizer for

246 seawater desalination

### 247 2.3 Refrigeration cycle system

248 The refrigeration cycle system in the experiment consists of a compressor,  
249 condenser, evaporator, cold storage tank, temperature control module, and associated  
250 pipelines. Its primary function is to lower the temperature of the glycerol-water solution  
251 in the cold storage tank, maintain the temperature and stability of the cooling medium,  
252 and serve as the freezing medium in the seawater crystallizer. The structure of the  
253 refrigeration unit is depicted in Figure 5. The cooling power of the refrigeration unit is  
254 165W, utilizing R134a as the refrigerant, with a minimum cooling temperature of  $-40^{\circ}\text{C}$ .

255 The condenser is an air-cooled condenser, powered by a 220V AC motor with a  
256 40W rating. The evaporator consists of a copper coil placed directly inside the reservoir,  
257 allowing for the direct cooling of the glycerol-water solution as the cooling medium.  
258 The reservoir has dimensions of  $420\text{ mm} \times 370\text{ mm} \times 240\text{ mm}$ . The refrigeration unit  
259 is equipped with a temperature control module that monitors the temperature using a  
260 probe inside the liquid reservoir. This module regulates the temperature within the  
261 reservoir by controlling the compressor power switch. The temperature control module  
262 selected for this test bench has a control range of  $-50^{\circ}\text{C}$  to  $110^{\circ}\text{C}$  ( $\pm 0.1^{\circ}\text{C}$ ), with a  
263 temperature control differential set at  $0.5^{\circ}\text{C}$ .



264

265 Figure 5 Refrigeration cycle system composition view

266 The main component of glycerol is propane-1,2,3-triol, which is easily soluble in  
267 water. Its aqueous solution has a lower freezing point, making it an excellent antifreeze

268 and refrigerant. The freezing point of glycerol-water solution can be calculated as  
269 follow:

$$270 \quad \Delta T_f = T_f^* - T_f = K_f \cdot m \quad (1)$$

271 where  $K_f$  represents the cryoscopic constant (freezing point depression constant);  
272  $m$  denotes the molal concentration.

273 Table 2 provides the freezing points of glycerol-water solutions at different mass  
274 concentrations. It can be observed that the freezing point of glycerol-water solutions  
275 shows an initial increase followed by a decrease as the concentration of glycerol  
276 increases. In this study, a glycerol-water solution with a concentration of 66.7% was  
277 selected, which exhibited the lowest freezing point of -46.5°C.

278 Table 2 Freezing point of glycerol-water solution

Glycerol mass fraction (%)	10	30	50	66.7	80	90
Freezing point (°C)	-1.6	-9.5	-23.0	-46.5	-20.3	-1.6

279

### 280 3 Experimental design and evaluation methods

281 The seawater used in the experiment was prepared by dissolving different amounts  
282 of seawater blending salt into distilled water. Table 3 shows the ion composition and  
283 physical properties of the seawater when 1 kg of seawater blending salt is dissolved in  
284 30 kg of distilled water. The mass of the salt was measured using a digital balance with  
285 a capacity of 300 g and an accuracy of 0.01 g. The salinity of the seawater was measured  
286 using a SMART SENSOR AR8012 salinity meter, which has a range of 0-100 ppt (parts  
287 per thousand) and an accuracy of  $\pm 3\%$  F.S  $\pm 1$  digit. The seawater temperature and flow  
288 rate were maintained at constant levels, with the inlet seawater temperature kept around  
289 room temperature (20°C) and the initial seawater flow rate controlled at 1 ml/s.

290 Table 3 Physical data and ionic composition of artificial seawater

Component	Values	Units	Component	Values	Units
Specific gravity	1.020-1.022(25°C)	-	Na <sup>+</sup>	9100-9300	mg/L
Salinity	30-31(25°C)	ppt	Mg <sup>2+</sup>	1150-1250	mg/L

PH	8.20-8.50(25°C)	-	Ca <sup>2+</sup>	380-420	mg/L
Total alkalinity	2.9-3.5	mmol/L	K <sup>+</sup>	240-355	mg/L
KH	8.0-10.0	dKH	Sr <sup>2+</sup>	8.2-9.0	mg/L
Cl <sup>-</sup>	17150-17980	mg/L	Br <sup>-</sup>	40-55	mg/L
SO <sub>4</sub> <sup>2-</sup>	2250-2350	mg/L	F <sup>-</sup>	0.9-1.1	mg/L
HSO <sub>4</sub> <sup>-</sup>	120-135	mg/L	B <sup>3+</sup> , B <sup>5+</sup>	5.0-6.0	mg/L

291

292 The comparative experimental study of freezing desalination with and without  
 293 ultrasonic vibration was designed. In order to optimize the relationship between various  
 294 factors during the experimental process, to systematically arrange the experimental  
 295 procedure, analyze experimental data, and achieve optimal experimental results with a  
 296 minimized number of trials, an orthogonal experimental design [35] was implemented.  
 297 This method aims to uncover the internal relationships among experimental variables  
 298 while efficiently reducing the number of experiments required.

### 299 3.1 Orthogonal experimental design

300 In this study, careful consideration was given to the impact of three key factors:  
 301 the temperature of the glycerol-water solution in the cold storage tank, the salinity of  
 302 seawater at the inlet of the crystallizer, and the freezing time, on the process of seawater  
 303 freezing desalination. Each factor was examined at five different levels, employing an  
 304  $L_{25}(5^6)$  orthogonal experimental design table. The specific values for each level of the  
 305 experimental factors are detailed in Table 4.

306 Table 4 Each level of experimental factors

Experimental factor level	L1	L2	L3	L4	L5
Inlet salinity $x$ /ppt (parts per thousand)	15	20	25	30	35
Freezing temperature $T$ /°C	-9	-12	-15	-18	-21
Freezing time $t$ /s	100	125	150	175	200

307

308 The design of the orthogonal table is presented in Appendix, where factors A to C

309 in Appendix represent the salinity of the inlet seawater in the cold storage tank, the  
310 temperature of the propylene glycerol-water solution, and the freezing time,  
311 respectively. Experiments were conducted separately without using ultrasonic vibration  
312 and with ultrasonic vibration. The experimental results were output as the desalination  
313 rate of the freezing seawater and the ice production rate inside the heat exchanger.  
314 Range analysis and variance analysis were performed on the experimental data, and the  
315 experimental data processing and analysis were validated using SPSS orthogonal  
316 analysis software.

317

### 318 **3.2 Evaluation methods**

319 The desalination rate of the freezing seawater is defined as the difference in  
320 salinity between the seawater at the inlet and the seawater after the crystalline product  
321 has melted following freezing desalination. The salinity of the inlet sea water is  $x$ , and  
322 the salinity of the frozen sea water in the pipe after melting is  $x'$ . The desalination rate  
323 of the freezing seawater is given by:

$$324 \quad w = \frac{x - x'}{x} \times 100\% \quad (2)$$

325 The seawater icing rate is defined as the ratio of the volume of the crystalline  
326 product after freezing desalination to the total volume inside the pipe. The volume of  
327 seawater in the tube after melting is  $V_{ice}$ , and the total volume in the heat exchanger  
328 tube is  $V$ , then the icing rate inside the heat exchanger is:

$$329 \quad y = \frac{V_{ice}}{V} \times 100\% \quad (3)$$

330 Range analysis is a commonly used method for handling orthogonal experimental  
331 results, which can intuitively demonstrate the extent to which different factors affect  
332 the experimental results. The principle involves analyzing the total response value  $K$   
333 and the average response value  $k$  of each factor at different levels of influence. The total  
334 response value  $K$  represents the sum of the experimental values of a factor at the  $i$ -th  
335 level, while the average response value  $k$  is the average value of  $K$  corresponding to the  
336 level number  $i$ . It is generally believed that a larger average response value  $k$  indicates

337 a better effect of the corresponding factor at that level. The range  $R$  value is the  
338 difference between the maximum and minimum values of the average response value  
339  $k$ , and a larger  $R$  value indicates a greater impact of that factor on the experimental  
340 results.

341 Range analysis can intuitively reveal the differences in experimental results  
342 corresponding to different levels of various factors. However, this analysis process  
343 cannot distinguish whether these differences are due to variations in the levels of the  
344 factors or due to errors. To analyze the magnitude of errors that inevitably exist in the  
345 experimental process, variance analysis is often employed. Variance analysis calculates  
346 the sum of squares of deviations  $S_j$  for each factor and error and the degrees of  
347 freedom  $f$ , thereby obtaining the mean square  $\hat{S}_j$  and  $F$  values for each factor and error.  
348 By consulting the  $F$ -test critical value table, the  $F_\alpha$  values for each factor are  
349 determined, ultimately establishing the significant level of the corresponding factor.  
350 These evaluation parameters are shown in Equation (4) to (8):

$$351 \quad S_j = \frac{\sum_{i=1}^m K_i^2}{m} - \frac{\left(\sum_{i=1}^n z_i\right)^2}{n} \quad (4)$$

$$352 \quad f_{total} = nm - 1 \quad (5)$$

$$353 \quad f_j = m - 1 \quad (6)$$

$$354 \quad \hat{S}_j = \frac{S_j}{f_j} \quad (7)$$

$$355 \quad F = \frac{\hat{S}_j}{\hat{S}_{error}} \quad (8)$$

356 where  $m$  is the selected factor corresponds to the number of levels,  $n$  is the number  
357 of experiments,  $z_i$  is the result of the  $i$ -th experiment.

### 358 3.3 Uncertainty analysis

359 The error transfer principle is used to analyze the uncertainty of the experimental  
360 results:

$$361 \quad \frac{\Delta_w}{w} = \sqrt{\left(\frac{\partial \ln w}{\partial x}\right)^2 (\Delta_x)^2 + \left(\frac{\partial \ln w}{\partial x'}\right)^2 (\Delta_{x'})^2} \quad (9)$$

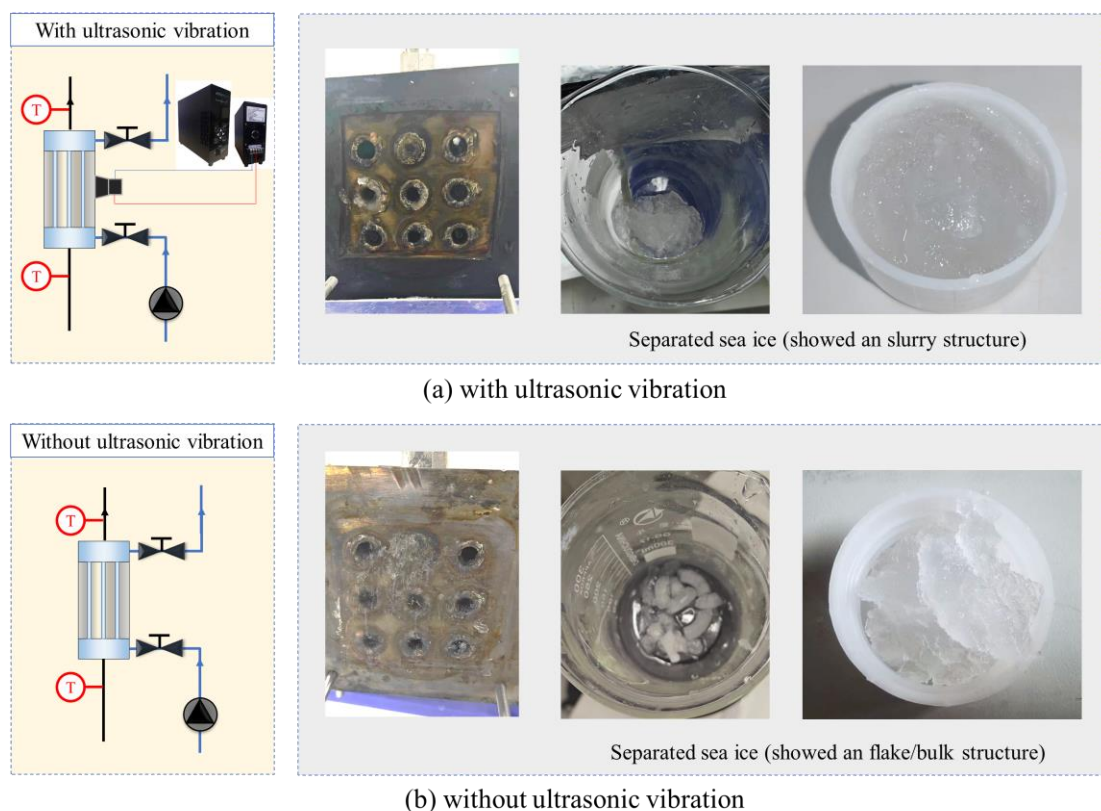
$$362 \quad \frac{\Delta_y}{y} = \sqrt{\left(\frac{\partial \ln y}{\partial V}\right)^2 (\Delta_V)^2 + \left(\frac{\partial \ln y}{\partial V_{ice}}\right)^2 (\Delta_{V_{ice}})^2} \quad (10)$$

363 Based on the accuracy of the measuring devices, the uncertainty of all  
 364 experimental data obtained is less than 3.99%, ensuring high reliability.

365

#### 366 4 Results and discussion

367 The characteristics of seawater freeze desalination with and without the  
 368 application of ultrasound were experimentally compared and investigated in this study.  
 369 Identical equipment was used in the control experiments to ensure the comparability of  
 370 the results.



371

372

Figure 6 Sea ice with and without ultrasonic vibration

373 Figure 6 shows the sea ice morphology obtained from the experiment. Overall, the  
 374 use of ultrasonic vibration can effectively fluidized sea ice without causing blockages



375 in heat exchanger tubes. When ultrasonic vibration is not applied, the freezing of  
 376 seawater will present a sheet-like or block like structure, which is prone to tube  
 377 blockage.

#### 378 4.1 Seawater freezing desalination without ultrasonic vibration

379 Table 5 to Table 8 show the experimental results and range analysis of seawater  
 380 desalination by freezing without ultrasonic vibration.

381 Table 5 Results of orthogonal experiment without ultrasonic vibration

Group	w/%	y/%	Group	w/%	y/%	Group	w/%	y/%
1	26.14	40.15	10	19.50	65.45	19	15.15	64.09
2	30.32	63.79	11	20.24	50.15	20	12.08	72.27
3	24.83	70.91	12	21.12	76.52	21	15.34	62.42
4	19.08	80.91	13	15.20	80.61	22	20.45	45.75
5	13.16	85.91	14	18.73	58.94	23	20.51	60.15
6	27.00	48.18	15	18.97	70.30	24	15.43	70.61
7	23.47	65.45	16	16.56	58.18	25	10.42	78.94
8	18.69	72.73	17	20.34	72.12			
9	14.50	84.85	18	18.67	56.67			

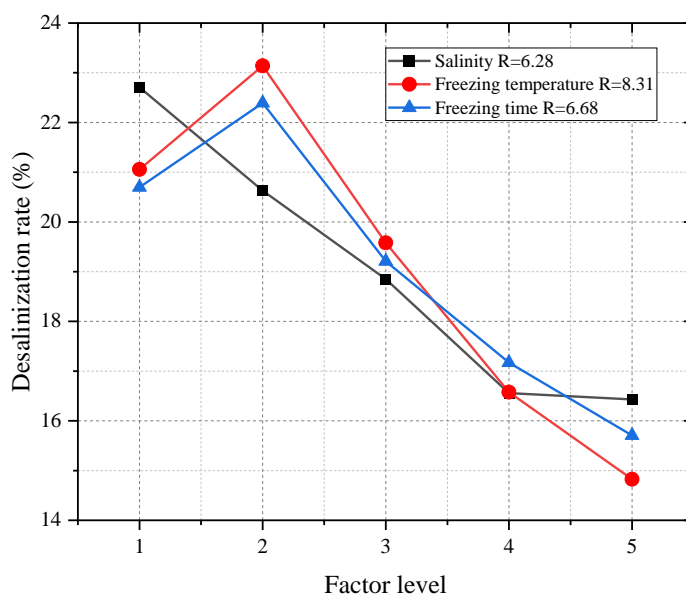
382

383 According to the range analysis in Table 6, the three influencing factors—salinity  
 384 of the inlet seawater, temperature of the glycerol-water solution in the storage tank, and  
 385 freezing time—affect both the seawater desalination rate and the icing rate of the heat  
 386 exchanger tubes to varying degrees. For the seawater desalination rate, the order of  
 387 influence from greatest to least is  $T > t > x$ , with the maximum range being 8.31 and  
 388 the minimum range being 6.28, indicating a similar level of influence among the factors.  
 389 Regarding the icing rate of the heat exchanger tubes, the order of influence is  $t > T > x$ ,  
 390 with freezing time and temperature having a significantly greater impact than seawater  
 391 salinity.

392 Table 6 Range analysis results without ultrasonic vibration

Experimental parameter	Inlet salinity/ppt		Freezing temperature/°C		Freezing time/s	
	w/%	y/%	w/%	y/%	w/%	y/%
$K_1$	113.54	341.67	105.28	259.09	103.49	266.97
$K_2$	103.16	336.67	115.70	323.64	111.96	306.52
$K_3$	94.25	336.52	97.90	341.06	96.05	329.39
$K_4$	82.79	323.33	82.88	359.39	85.86	367.27
$K_5$	82.16	317.88	74.13	372.88	78.54	385.91
$k_1$	22.71	68.33	21.06	51.82	20.70	53.39
$k_2$	20.63	67.33	23.14	64.73	22.39	61.30
$k_3$	18.85	67.30	19.58	68.21	19.21	65.88
$k_4$	16.56	64.67	16.58	71.88	17.17	73.45
$k_5$	16.43	63.58	14.83	74.58	15.71	77.18
$R$	6.28	4.76	8.31	22.76	6.68	23.79

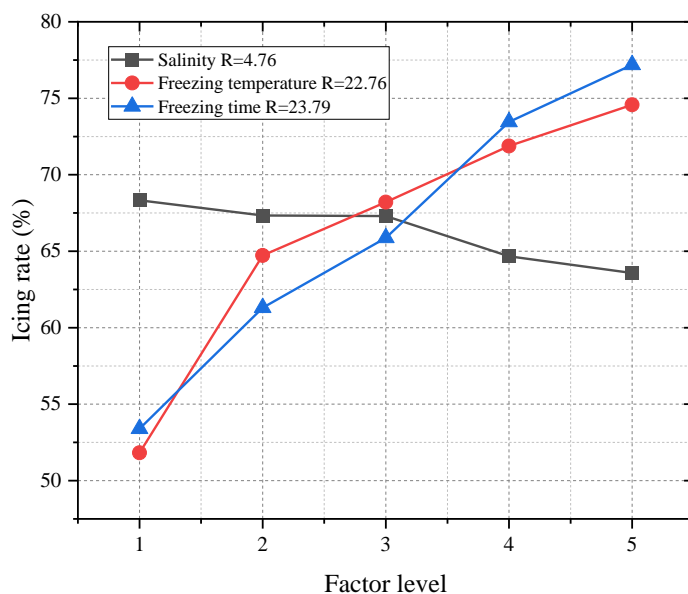
393 To visually analyze the relationship between these influences and the experimental  
 394 results, the factor levels are plotted on the horizontal axis, and the average response  
 395 values corresponding to the seawater desalination rate and tube icing rate are plotted on  
 396 the vertical axis. The results are shown in Figure 7.



397

398

(a)



(b)

Figure 7 The average response values of each factor level in the experiment without ultrasonic vibration (a) desalting rate (b) icing rate

As illustrated in Figure 7(a), the relationship between each factor and the desalination rate is detailed. Inlet seawater salinity shows the least impact on the seawater desalination rate, with an R-value of 6.28. As inlet seawater salinity increases, there is a gradual decrease in the seawater desalination rate.

The freezing time during the heat exchange process exhibits a slightly higher influence on the seawater desalination rate compared to inlet seawater salinity, with an R-value of 6.68. Initially, the desalination rate increases with longer freezing times, peaking at 125 seconds. However, at shorter freezing times, seawater tends to crystallize, resulting in a lower desalination rate due to higher seawater content remaining with the sea ice during ice-water separation. As freezing time increases, more sea ice forms, including some concentrated seawater, which diminishes the desalination rate owing to increased concentration of seawater on the ice surface.

The temperature of the glycerol-water solution exerts the greatest impact on the seawater desalination rate, with an R-value of 8.31. Initially, the desalination rate rises with decreasing temperature, achieving optimal performance at a glycerol-water solution temperature of  $-12^{\circ}\text{C}$ . However, excessively low temperatures lead to

419 increased supercooling of seawater, causing rapid freezing during crystallization. This  
 420 process results in salt pockets enclosed within ice crystals, ultimately reducing the  
 421 desalination rate.

422 In Figure 7(b), the relationship between each factor and the heat exchanger tube  
 423 icing rate is depicted. Freezing time has the most pronounced impact on the icing rate,  
 424 with an R-value of 23.79. As freezing time increases, the icing rate inside the tube also  
 425 rises. Similarly, freezing temperature significantly influences the icing rate, with an R-  
 426 value of 22.76. Lower freezing temperatures correspond to higher icing rates. This is  
 427 because longer freezing times and lower temperatures result in greater cooling of the  
 428 seawater inside the tube, leading to increased icing.

429 Inlet seawater salinity also affects the tube icing rate, albeit to a lesser extent, with  
 430 an R-value of 4.76. As seawater salinity increases, the tube icing rate decreases  
 431 gradually. This relationship arises because higher seawater salinity lowers the freezing  
 432 point of seawater, necessitating colder temperatures to initiate ice formation, thereby  
 433 reducing the icing rate.

434 Table 7 Analysis of variance of desalting rate without ultrasonic experiment

Variance source	$S_j$	$f_j$	$\hat{S}_j$	$F$	$F_\alpha$	Significant
Inlet salinity	144.87	4	36.22	12.67	$2.88 \times 10^{-4}$	Significant
Freezing temperature	224.93	4	56.23	19.67	$3.33 \times 10^{-5}$	Significant
Freezing time	143.04	4	35.76	12.51	$3.06 \times 10^{-4}$	Significant
Error	34.30	12	2.86			

Note:  $R^2 = 0.937$  (After the adjustment:  $R^2 = 0.875$ ).

435 Based on the data from Tables 7 and 8, variance analysis reveals that the inlet  
 436 seawater salinity, glycerol-water solution temperature, and freezing time significantly  
 437 impact the seawater desalination rate. Furthermore, the glycerol-water solution  
 438 temperature and freezing time also significantly affect the heat exchanger tube icing  
 439 rate, whereas the inlet seawater salinity exerts a noticeable but lesser influence on the  
 440 icing rate.

441 Table 8 Analysis of variance of icing rate without ultrasonic experiment

Variance source	$S_j$	$f_j$	$\hat{S}_j$	$F$	$F_\alpha$	Significant
Inlet salinity	81.40	4	20.35	2.86	0.0706	non-significant
Freezing temperature	1577.24	4	394.31	55.45	$1.22 \times 10^{-7}$	Significant
Freezing time	1806.49	4	451.62	63.51	$5.66 \times 10^{-8}$	Significant
Error	85.33	12	7.11			

Note:  $R^2 = 0.976$  (After the adjustment:  $R^2 = 0.952$ ).

442

## 443 4.2 Seawater freezing desalination with ultrasonic vibration

444 Table 9 to Table 12 shows the experimental results and range analysis of seawater  
445 desalination by freezing after ultrasonic vibration.

446 Table 9 Results of orthogonal experiment with ultrasonic vibration

Group	w/%	y/%	Group	w/%	y/%	Group	w/%	y/%
1	36.36	55.33	10	24.38	75.50	19	22.15	75.33
2	40.52	77.17	11	29.60	68.67	20	20.13	86.83
3	32.67	80.33	12	25.30	86.83	21	27.67	81.67
4	19.87	93.00	13	16.80	95.50	22	29.91	59.67
5	13.16	97.67	14	25.00	69.17	23	27.51	70.17
6	31.84	61.33	15	25.79	80.00	24	22.57	88.00
7	27.27	80.83	16	27.76	73.67	25	12.25	94.50
8	25.62	88.83	17	24.25	88.67			
9	18.81	95.33	18	26.32	70.50			

447

448 According to the variance analysis presented in Table 10, the impact of ultrasonic  
449 vibration on the seawater desalination rate shows that the three factors are ranked in  
450 descending order of influence as  $T > t > x$ , with a range from 11.50 to 4.53. For the heat  
451 exchanger tube icing rate, the influence of the three factors is ranked in descending

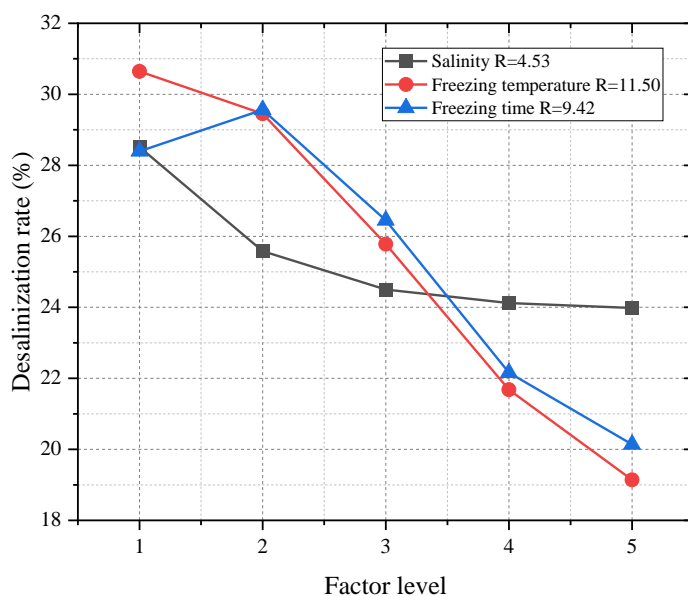
452 order as  $t > T > x$ . Specifically, freezing time and temperature significantly affect the  
 453 icing rate more than seawater salinity, with ranges from 25.73 to 1.90.

454 Table 10 Range analysis results with ultrasonic vibration

Experimental parameter	Inlet salinity/ppt		Freezing temperature/°C		Freezing time/s	
	w/%	y/%	w/%	y/%	w/%	y/%
$K_1$	142.58	403.50	153.23	340.67	141.97	330.17
$K_2$	127.92	401.83	147.26	393.17	147.81	364.00
$K_3$	122.49	400.17	128.91	405.33	132.24	404.67
$K_4$	120.61	395.00	108.40	420.83	110.79	436.83
$K_5$	119.91	394.00	95.71	434.50	100.69	458.83
$k_1$	28.52	80.70	30.65	68.13	28.39	66.03
$k_2$	25.58	80.37	29.45	78.63	29.56	72.80
$k_3$	24.50	80.03	25.78	81.07	26.45	80.93
$k_4$	24.12	79.00	21.68	84.17	22.16	87.37
$k_5$	23.98	78.80	19.14	86.90	20.14	91.77
$R$	4.53	1.90	11.50	18.77	9.42	25.73

455

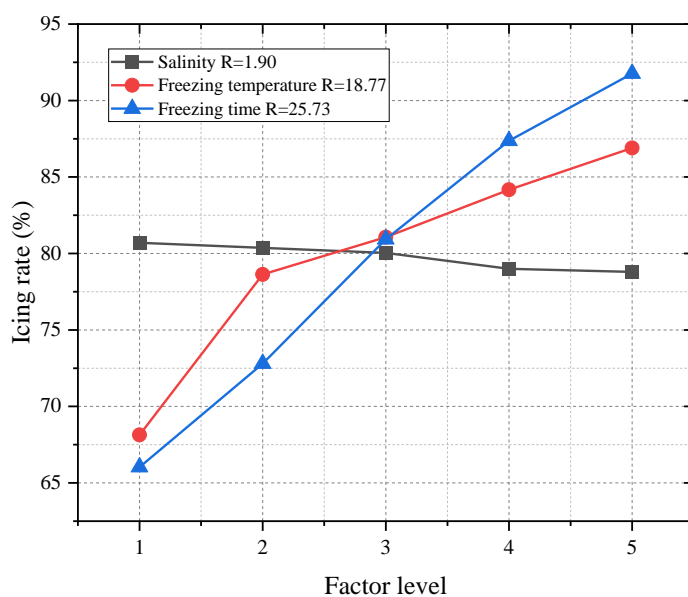
456 To visually analyze the relationship between these impacts and the experimental  
 457 results, the average response values corresponding to the factor levels are plotted on the  
 458 horizontal axis. The average response values for seawater desalination rate and tube  
 459 icing rate are plotted on the vertical axis. These results are depicted in Figure 8.



460

461

(a)



462

463

(b)

464 Figure 8 The average response values of each factor level in the experiment with  
465 ultrasonic vibration (a) desalting rate (b) icing rate

466 In Figure 8(a), the impact of inlet seawater salinity on the seawater desalination  
467 rate is minimal, indicated by an R-value of 4.53. The seawater desalination rate  
468 gradually decreases as inlet seawater salinity increases. Freezing time also affects the  
469 seawater desalination rate, with an R-value of 9.42. Initially, the desalination rate  
470 increases with freezing time, peaking at 125 seconds. The temperature of the glycerol-

471 water solution exerts the greatest influence on the seawater desalination rate, with an  
 472 R-value of 11.50. As freezing temperature decreases, the seawater desalination rate also  
 473 decreases. Comparatively, the use of ultrasonic vibration enhances the desalination  
 474 effect of seawater by generating finer ice crystals, thereby increasing the purity of  
 475 frozen sea ice and reducing salt inclusion formation.

476 In Figure 8(b), the primary factors influencing the heat exchanger tube icing rate  
 477 are freezing time and glycerol-water solution temperature, with R-values of 25.73 and  
 478 18.77, respectively. The influence of seawater salinity on the tube icing rate is minimal,  
 479 with an R-value of 1.90. Ultrasonic vibration enhances ice crystal formation and  
 480 facilitates the separation of water molecules and salt ions, significantly improving the  
 481 tube icing rate compared to experiments without ultrasonic vibration.

482 Table 11 Analysis of variance of desalting rate with ultrasonic experiment

Variance source	$S_j$	$f_j$	$\hat{S}_j$	$F$	$F_\alpha$	Significant
Inlet salinity	70.91	4	17.73	1.56	0.247	non-significant
Freezing temperature	485.34	4	121.34	10.68	$6.32 \times 10^{-4}$	Significant
Freezing time	83.23	4	20.81	7.22	$3.36 \times 10^{-3}$	Significant
Error	136.31	12	11.36			

Note:  $R^2 = 0.866$  (After the adjustment:  $R^2 = 0.733$ ).

483

484 Based on the data from Tables 11 and 12, variance analysis indicates that the  
 485 temperature of the glycerol-water solution and freezing time significantly affect both  
 486 the seawater desalination rate and the heat exchanger tube icing rate. In contrast, the  
 487 impact of inlet seawater salinity on these rates is not statistically significant.

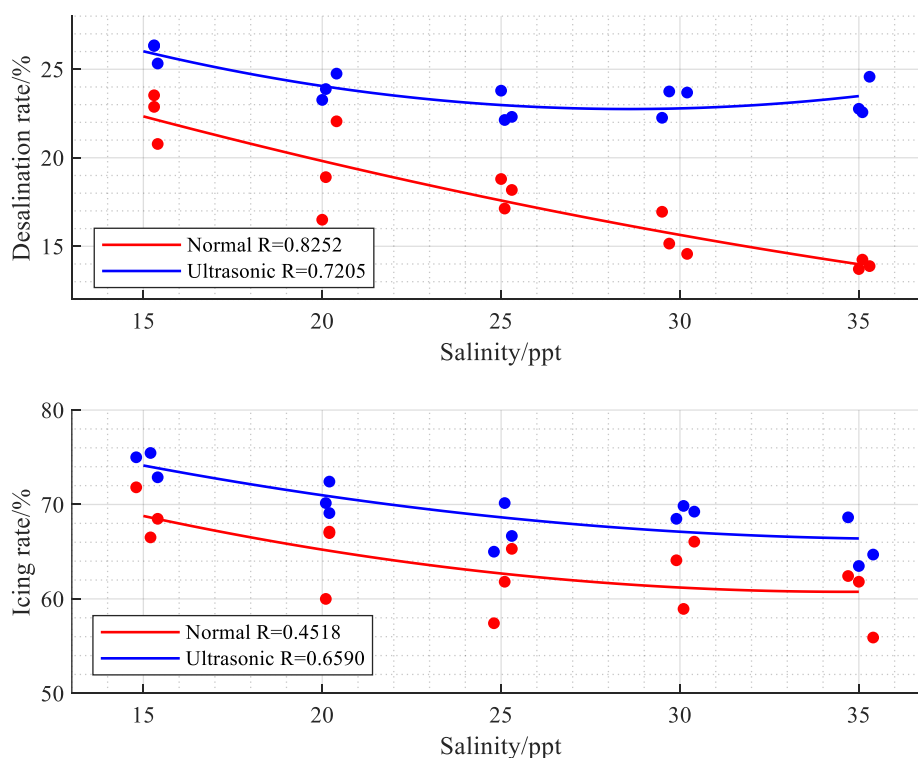
488 Table 12 Analysis of variance of icing rate with ultrasonic experiment

Variance source	$S_j$	$f_j$	$\hat{S}_j$	$F$	$F_\alpha$	Significant
Inlet salinity	14.12	4	3.53	0.37	0.826	non-significant
Freezing temperature	1042.76	4	260.69	27.27	$6.07 \times 10^{-6}$	Significant
Freezing time	2201.30	4	550.32	57.58	$9.89 \times 10^{-8}$	Significant





504 effect for the heat exchanger tube icing rate under ultrasonic experiments is moderate  
 505 and acceptable within a certain range.



506

507 Figure 9 Fitting diagram of desalting rate and icing rate

508 Based on the above experimental results, the desalination rate and icing rate were  
 509 fitted separately. The fitted equations for desalination rate and icing rate without the use  
 510 of ultrasonic vibration are as follows:

511  $w_0 = 0.005747x^2 - 0.705x + 31.62$  (11)

512  $y_0 = 0.02075x^2 - 1.439x + 85.7$  (12)

513 With ultrasonic, the fitted equations for desalting rate and icing rate are as follows:

514  $w_1 = 0.01771x^2 - 1.012x + 37.21$  (13)

515  $y_1 = 0.01625x^2 - 1.199x + 88.46$  (14)

516 According to the competitive experimental results, ultrasonic freezing desalination  
 517 substantially enhances desalination efficiency. Within the salinity range of 15-35 ppt,  
 518 the desalination rate increased by 18.18% to 67.86%, with a more pronounced effect

519 observed at higher salinity levels. The average desalination rate of ultrasonic one is  
520 23.58%, compared with the normal one of 17.78%, and the average desalination rate  
521 increased by 32.62%. The icing rate also showed an increase of 8.03% to 8.20%.  
522 Moreover, the study also suggests that the enhancement effect of ultrasound on freezing  
523 desalination diminishes with increasing stages of desalination in continuous freezing  
524 desalination processes, especially after significant reduction in salinity. These results  
525 indicate promising prospects for the application of ultrasound technology in freezing  
526 desalination.

#### 527 **4.4 Economic analysis of ultrasonic based freezing desalination**

528 The experimental research results above indicate that the use of ultrasonic freezing  
529 desalination technology can significantly enhance desalination efficiency. Since  
530 freezing desalination alone is insufficient to directly desalinate seawater to potable  
531 levels, it necessitates secondary desalination methods such as reverse osmosis (RO). In  
532 this condition, freezing desalination serves as a pretreatment process within a composite  
533 desalination system.

534 The thermodynamic and economic performance of a simple two-stage freeze  
535 desalination RO system is analyzed. After the seawater is pre-desalinated by two-stage  
536 ultrasonic freezing desalination equipment in turn, it flows into the RO system for final  
537 desalination. In order to simplify the calculation, other small component cost such as  
538 pumping and pipe are ignored, the system can be simply divided into freezing  
539 crystallization heat exchanger, ultrasonic machine and RO system. The power and cost  
540 of RO system can be calculated according to reference [36], shown in Table 14.

541 Table 14 Mathematical models of RO system.

Parameter	Equations
Recovery ratio	$RR = \frac{M_{fresh}}{M_{feed}}$
Rejected salt concentration	$X_{brine} = \frac{M_{feed} \times X_{feed} - M_{fresh} \times X_{feed} \times (1 - SR)}{M_{feed} - M_{fresh}}$

---

Temperature correction factor	$TCF = \exp(2700 \times (1/T - 1/298))$
Membrane water permeability	$k_w = \frac{6.84 \times 10^{-8} \times (18.6865 - (0.177 \times X_{brine}))}{T}$
Osmotic pressure	$P_n = 75.85 \times X_n, n = feed, brine, fresh$
Net osmotic pressure across the membrane	$\Delta P_{os} = 0.5 \times (P_{feed} + P_{brine}) - P_{fresh}$
Net pressure difference across the membrane	$\Delta P_{net} = \left( \frac{M_{fresh}}{3600 \times TCF \times FF \times A_e \times n_e \times n_v \times k_w} \right) + \Delta P_{os}$
The required power input to the RO driving pump	$\dot{W}_{RO} = \frac{1000 \times M_{feed} \times \Delta P_{net}}{3600 \times \eta_p \times \rho_{feed}}$
Purchasing cost	$C_{RO} = C_k \times n_e \times n_v + C_{pv} \times n_v$

---

542 For heat exchanger, the cost calculation function is as follow[33]:

$$543 \quad C_{hex} = 12000 \left( \frac{A_{hex}}{100} \right)^{0.6} \quad (15)$$

544 where heat transfer surface area  $A_{hex}$  can be expressed as

$$545 \quad A_{hex} = \frac{Q}{U \Delta T_{LMTD}} \quad (16)$$

$$546 \quad \Delta T_{LMTD} = \frac{\Delta T_{max} - \Delta T_{min}}{\ln \left( \frac{\Delta T_{max}}{\Delta T_{min}} \right)} \quad (17)$$

547 where  $U$  is heat transfer coefficient,  $\Delta T_{LMTD}$  is the logarithmic mean temperature difference,

548  $Q$  is heat flux,  $\Delta T_{max}$  and  $\Delta T_{min}$  are as follows:

$$549 \quad \begin{cases} \Delta T_{max} = \max(t_{hot,in} - t_{cold,out}, t_{hot,out} - t_{cold,in}) \\ \Delta T_{min} = \min(t_{hot,in} - t_{cold,out}, t_{hot,out} - t_{cold,in}) \end{cases} \quad (18)$$

550 In addition, the energy consumption of ultrasonic machines is calculated as  
551 1.8kWh based on large ultrasonic machines, and its maximum loading was 1000 kg[33].  
552 The cost consumption of ultrasound is RMB5500 (765.53\$), which is determined based  
553 on the large ultrasonic machine in actual production as an example.

554 In order to evaluate the performance of the system, the specific work consumption  
 555 (SWC) and levelized cost of water (LCOW) of the system are expressed as,

$$556 \quad SWC = \frac{W_{Ultrasound} + W_{RO}}{m_{fresh}} \quad (19)$$

$$557 \quad LCOW = \frac{CRF \cdot C_{investment} + OMC}{t_{if} \cdot m_{fresh}} \quad (20)$$

558 Where capital recovery factor (CRF) is expressed as,

$$559 \quad CRF = \frac{i(1+i)^n}{(1+i)^n - 1} \quad (21)$$

560 The Annual operation and maintenance costs (OMC) generally takes 6% of total  
 561 cost.  $i$  is the annual loan interest rate, which is set as 8%,  $n$  denotes the life cycle  
 562 time, which is set as 20 years in this study,  $t_{if}$  is the load factor, considering the  
 563 influence of disastrous weather in coastal areas, the value of 7000 hours is taken[37].

564 With the daily output fresh water of 1000m<sup>3</sup>/day as the desalination target. The  
 565 South Pacific region is selected for research. The average salinity of seawater is 35 ppt.  
 566 Desalination results of ultrasonic/no ultrasonic freezing desalination are calculated  
 567 according to formula (11)-(14). The basic operating conditions of the design system are  
 568 given according to reference [33], shown in the Table 15.

569 Table 15 Operating parameters of the proposed CCDP system

Parameter	Value
heat transfer coefficient/ kW·m <sup>-2</sup> ·K <sup>-1</sup>	1.1
Inlet Seawater salinity/ ppt	35
Recovery ratio/ %	30
Effective area of membrane/m <sup>2</sup>	37
Number of membrane elements	7
Number of pressure vessel	9
Price of each membrane/ \$	1200
Price of pressure vessel/ \$	7000

High pressure pump efficiency	90
Fouling factor	80
Price of ultrasound/ \$	765.525

570 Table 16 shows the performance of various desalination systems. Compared with  
 571 ordinary RO equipment, the LCOW of Ultrasonic-freeze-RO system is reduced by  
 572 19.62%, after adding ultrasonic vibration, the LCOW is reduced by 23.70%, to  
 573 0.486\$/m<sup>3</sup>. However, compared with the freeze desalination method with or without  
 574 ultrasonic vibration, the economic growth is not significant. This is due to the high cost  
 575 of large ultrasonic vibration equipment. The SWC of Ultrasonic-Freeze-RO system is  
 576 reduced by 11.10% compared with Freeze-RO. These results reveal that the ultrasonic  
 577 vibration-based method can effectively reduce both the desalination cost and energy  
 578 consumption of the freeze desalination method.

579 Table 16 Performance of desalination systems.

Parameter	Ultrasonic-Freeze-RO	Freeze-RO	RO[38]
SWC/ kWh/m <sup>3</sup>	2.922	3.287	/
LCOW/ \$/m <sup>3</sup>	0.486	0.512	0.637

580

## 581 **5 Conclusion**

582 An innovative ultrasonic freezing desalination method has been evaluated through  
 583 lab-scale experiments. A specially designed ultrasonic freezing crystallizer was used to  
 584 conduct experiments on ultrasonic-based seawater freezing desalination. These  
 585 experiments were then compared to traditional methods without the influence of  
 586 ultrasound. The main conclusions drawn are as follows:

587 1. Freezing time and temperature exert significant influences on the desalination  
 588 rate and icing rate of seawater. The salinity of seawater exhibits a more pronounced  
 589 impact on the experimental outcomes in the absence of ultrasonic vibration compared  
 590 to its presence.

591 2. Ultrasonic vibration results in the formation of smaller ice crystals and helps

592 reduce salt encapsulation, significantly improving the desalination rate of seawater  
593 during freezing. Within the salinity range of 15-35 ppt, the desalination rate increased  
594 by 18.18% to 67.86%, with a more pronounced effect observed at higher salinity levels.  
595 The average desalination rate increased by approximately 32.62%.

596 3. Ultrasonic vibration promotes the formation of ice crystals and enhances the  
597 separation of water molecules and salt ions, leading to an average icing rate increase of  
598 8.03% to 8.20%.

599 4. Enhancement effect of ultrasound on freezing desalination diminishes with  
600 increasing stages of desalination in continuous freezing desalination processes,  
601 especially after significant reduction in salinity.

602 5. The ultrasonic vibration-based method can effectively reduce both the  
603 desalination cost and energy consumption of the freeze desalination method. Its specific  
604 work consumption is 2.922 kWh/m<sup>3</sup>, an 11.10% reduction compared to the Freeze-RO  
605 method. The levelized cost of water for the Ultrasonic-Freeze-RO method is \$0.486/m<sup>3</sup>,  
606 5.08% lower than the Freeze-RO method and 31.07% lower than the traditional RO  
607 method.

608

## 609 Reference

- 610 1. Mishra, R.K., *Fresh water availability and its global challenge*. British Journal of  
611 Multidisciplinary Advanced Studies, 2023. 4(3): p. 1-78.
- 612 2. Kariman, H., A. Shafieian, and M. Khiadani, *Small scale desalination technologies:  
613 A comprehensive review*. Desalination, 2023. 567: p. 116985.
- 614 3. UNDESA, *The Millennium Development Goals Report 2015*. 2016. p. 55.
- 615 4. Hu, Z. and Y. Chen, *Advancements in sustainable desalination with ocean thermal  
616 energy: A review*. Desalination, 2024. 586: p. 117770.
- 617 5. Shannon, M.A., et al., *Science and technology for water purification in the coming  
618 decades*. Nature, 2008. 452(7185): p. 301-310.
- 619 6. Almasoudi, S.M. and J. Bassam, *Desalination technologies and their environmental  
620 impacts: A review*. Sustainable Chemistry One World, 2024: p. 100002.
- 621 7. Kaviani, R., et al., *Experimental and theoretical study of a novel freeze desalination  
622 system with an intermediate cooling liquid*. Desalination, 2024. 576: p. 117381.
- 623 8. Moharramzadeh, S., et al., *Parametric study of the progressive freeze concentration  
624 for desalination*. Desalination, 2021. 510: p. 115077.
- 625 9. Harby, K., et al., *Reverse osmosis hybridization with other desalination techniques:*

- 
- 626 *An overview and opportunities*. *Desalination*, 2024. **581**: p. 117600.
- 627 10. Năstase, G., et al., *Advantages of isochoric freezing for food preservation: A*  
628 *preliminary analysis*. *International Communications in Heat Mass Transfer*  
629 2016. **78**: p. 95-100.
- 630 11. Ni, N., et al., *Theoretical research on ship desulfurization wastewater freezing*  
631 *desalination system driven by waste heat*. *Desalination*, 2023. **549**.
- 632 12. Williams, P.M., et al., *Technology for freeze concentration in the desalination*  
633 *industry*. *Desalination*, 2015. **356**: p. 314-327.
- 634 13. Görgüç, A., et al., *Cryoprotective role of vacuum infused inulin on the quality of*  
635 *artichoke: Interactive effects of freezing, thawing and storage period*. *Cryobiology*, 2024. **116**:  
636 p. 104914.
- 637 14. Yoda, T., H. Miyaki, and T. Saito, *Freeze concentrated apple juice maintains its*  
638 *flavor*. *Scientific Reports*, 2021. **11**(1): p. 12679.
- 639 15. Petzold, G., et al., *Vacuum-assisted block freeze concentration applied to wine*.  
640 *Innovative Food Science & Emerging Technologies*, 2016. **36**: p. 330-335.
- 641 16. Lin, W., M. Huang, and A. Gu, *A seawater freeze desalination prototype system*  
642 *utilizing LNG cold energy*. *International Journal of Hydrogen Energy*, 2017. **42**(29): p. 18691-  
643 18698.
- 644 17. Farahat, M.A., et al., *Experimental investigation of freezing desalination using*  
645 *silicon oil for ice production*. *Desalination*, 2023. **560**: p. 116664.
- 646 18. Ong, C.W. and C.-L. Chen, *Technical and economic evaluation of seawater freezing*  
647 *desalination using liquefied natural gas*. *Energy*, 2019. **181**: p. 429-439.
- 648 19. Eghtesad, A., et al., *Numerical investigation and optimization of indirect freeze*  
649 *desalination*. *Desalination*, 2020. **481**: p. 114378.
- 650 20. Jayakody, H., R. Al-Dadah, and S. Mahmoud, *Numerical investigation of indirect*  
651 *freeze desalination using an ice maker machine*. *Energy Conversion and Management*, 2018.  
652 **168**: p. 407-420.
- 653 21. Yuan, H., et al., *Theoretical and experimental investigation of an absorption*  
654 *refrigeration and pre-desalination system for marine engine exhaust gas heat recovery*. *Applied*  
655 *Thermal Engineering*, 2019. **150**: p. 224-236.
- 656 22. Lan, W., et al., *Comprehensive thermodynamic and economic analysis of an LNG*  
657 *cold energy recovery system using organic Rankine cycle and freezing-centrifugal desalination*  
658 *for power and water cogeneration*. *Journal of Cleaner Production*, 2024. **461**: p. 142677.
- 659 23. Chang, J., et al., *Freeze desalination of seawater using LNG cold energy*. *Water*  
660 *research*, 2016. **102**: p. 282-293.
- 661 24. Mandri, Y., et al., *Parametric study of the sweating step in the seawater desalination*  
662 *process by indirect freezing*. *Desalination*, 2011. **269**(1): p. 142-147.
- 663 25. Shishiny, A.M., et al., *An investigation of a proposed freezing desalination system*  
664 *integrating sweating effect and a Centrifugal-Based brine rejection technique*. *Separation and*  
665 *Purification Technology*, 2025. **353**: p. 128390.
- 666 26. Hou, Y., et al., *Cellulose nanocrystals facilitate needle-like ice crystal growth and*  
667 *modulate molecular targeted ice crystal nucleation*. *Nano Letters*, 2021. **21**(11): p. 4868-4877.
- 668 27. Mochizuki, K., Y. Qiu, and V. Molinero, *Promotion of homogeneous ice nucleation*



- 
- 669            *by soluble molecules*. Journal of the American Chemical Society, 2017. **139**(47): p. 17003-  
670            17006.
- 671            28. Wang, Z., et al., *Research on energy saving of ultrasonic wave in the process of*  
672            *making sea-slurry ice*. Energy Conversion and Management, 2021. **247**: p. 114541.
- 673            29. Gao, P., et al., *Study on droplet freezing characteristic by ultrasonic*. Heat Mass  
674            Transfer, 2017. **53**: p. 1725-1734.
- 675            30. Gai, S., et al., *Ice nucleation of water droplet containing solid particles under weak*  
676            *ultrasonic vibration*. Ultrasonics Sonochemistry, 2021. **70**: p. 105301.
- 677            31. Tian, Y., et al., *Development of a single/dual-frequency orthogonal ultrasound-*  
678            *assisted rapid freezing technique and its effects on quality attributes of frozen potatoes*. Journal  
679            of Food Engineering, 2020. **286**: p. 110112.
- 680            32. Daghooghi-Mobarakeh, H., V. Subramanian, and P.E. Phelan, *Experimental study*  
681            *of water freezing process improvement using ultrasound*. Applied Thermal Engineering, 2022.  
682            **202**: p. 117827.
- 683            33. Zhang, Y., et al., *Promotional effects of ultrasound and oscillation on sea ice*  
684            *desalination*. Separation and Purification Technology, 2024. **347**: p. 127622.
- 685            34. Cong, J., et al., *Droplet freezing phase transition and heat transfer under the*  
686            *ultrasonic effect*. International Communications in Heat and Mass Transfer, 2021. **123**: p.  
687            105136.
- 688            35. Chen, Z., et al., *Alternating current poling conditions determination by orthogonal*  
689            *experimental design*. Ceramics International, 2024.
- 690            36. Nafey, A.S. and M.A. Sharaf, *Combined solar organic Rankine cycle with reverse*  
691            *osmosis desalination process: Energy, exergy, and cost evaluations*. Renewable Energy, 2010.  
692            **35**(11): p. 2571-2580.
- 693            37. Yi, S., et al., *Pre-expansion ejector absorption power cycle for ocean thermal*  
694            *energy conversion*. Energy Conversion and Management, 2022. **269**: p. 116151.
- 695            38. Caldera, U., D. Bogdanov, and C. Breyer, *Local cost of seawater RO desalination*  
696            *based on solar PV and wind energy: A global estimate*. Desalination, 2016. **385**: p. 207-216.
- 697
- 698

**Appendix. Orthogonal experimental design table**

Group	Factors		
	A	B	C
1	L1	L1	L1
2	L1	L2	L2
3	L1	L3	L3
4	L1	L4	L4
5	L1	L5	L5
6	L2	L1	L2
7	L2	L2	L3
8	L2	L3	L4
9	L2	L4	L5
10	L2	L5	L1
11	L3	L1	L3
12	L3	L2	L4
13	L3	L3	L5
14	L3	L4	L1
15	L3	L5	L2
16	L4	L1	L4
17	L4	L2	L5
18	L4	L3	L1
19	L4	L4	L2
20	L4	L5	L3
21	L5	L1	L5
22	L5	L2	L1
23	L5	L3	L2
24	L5	L4	L3
25	L5	L5	L4

the salinity of the inlet seawater in the cold storage tank, the temperature of the propylene glycerol-water solution, and the freezing time