

***Oxygen mass transfer and hydrodynamic behaviour in wastewater:
determination of local impact of surfactants by visualization
techniques.***

5 Authors: Mélanie Jimenez ^{a,b,c,d}, Nicolas Dietrich ^{a,b,c,d}, John R. Grace ^e, Gilles Hébrard
a,b,c,d *

* Corresponding author: Gilles Hébrard, hebrard@insa-toulouse.fr

+33 561 359 435

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a Université de Toulouse, INSA, UPS, INP, LISBP, 135 Av. de Rangueil, F-31077
Toulouse, France

b INRA UMR792, Ingénierie des Systèmes Biologiques et des Procédés, F-31400
Toulouse, France

15 c CNRS UMR 5504, Ingénierie des Systèmes Biologiques et des Procédés, F-31400
Toulouse, France

d Fédération de Recherche FERMAT, CNRS, Toulouse, France

e Department of Chemical and Biological Engineering, University Of British
Columbia, Vancouver, Canada V6T1Z3

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Abstract

Powerful techniques, based on the Planar Laser Induced Fluorescence (PLIF)
technique, are deployed to locally visualize and quantify the impact of surfactants in
25 wastewaters on hydrodynamics and oxygen mass transfer. Bubble diameter, aspect
ratio, rise velocity, contamination angle, as well as flux, flux density, liquid side mass
transfer and diffusion coefficients of transferred oxygen are determined based on
these techniques applied in the wake of rising bubbles of diameter 1 mm and through
planar gas/liquid interfaces. The initial experiments were performed in demineralized
30 water containing small amounts of surfactant. Different concentrations of surfactant
were added to finally reach the Critical Micelle Concentration (CMC). Bubbles have
classically been found to be more spherical with a reduced rise velocity in the
presence of surfactants up to the CMC. Above the CMC, these hydrodynamic

35 characteristics were found to be almost constant, although the oxygen mass transfer
decreased due to the presence of surfactants. Experimental results were markedly
lower than predicted by the well-known Frössling equation with rigid surfaces. This is
believed to be caused by a barrier of surfactants hindering the oxygen mass transfer at
the interface. Similar hindrance of oxygen mass transfer applies to waters from
sewage plants (filtered raw water and treated water), making accurate design of
40 aeration tanks difficult.

Highlights

- Gas-liquid mass transfer coefficients were found from two flow visualization methods
- 45 • Surfactants reduce mass transfer not only by retarding bubble rise velocities
- Surfactants beyond Critical Micelle Concentration congregate at gas-liquid interface
- This surfactant congregation causes further decline in interphase mass transfer
- Frössling correlation overestimates interphase mass transfer for wastewater

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Keywords: Surfactants, Wastewater, Bubbles, PLIF, Mass transfer, Interface

Introduction

55 For wastewater treatment (e.g. in activated sludge or membrane bioreactors), a
supply of dissolved oxygen, e.g. by injecting air bubbles, is required to ensure the
availability of microorganisms able to degrade specific pollutants. The path of
oxygen molecules in such processes is characterized by resistances at the gas/liquid
interface (commonly represented as gas and liquid films), in the bulk liquid and on
60 both sides of the liquid/microorganism interface (Garcia-Ochoa and Gomez, 2009).
However, due to the low solubility of oxygen in aqueous solutions ($H_e=4.05 \times 10^9$ Pa,
He being the Henry's law constant of oxygen in water at 20°C, Roustan, 2003), the
main resistance to oxygen mass transfer is usually assumed to be located in a thin film
of liquid surrounding the bubble and characterized by a liquid side mass transfer
65 coefficient k_L (m/s). Since compressors required to inject air bubbles represent almost
70% of the total energy consumption of sewage plants, accurate determination of k_L is

of prime interest to avoid over- or under-estimating of the required oxygen supply to the process.

70 Several studies have focused on characterizing oxygen mass transfer in wastewater although most of these have been limited to the evaluation of the product $k_L \times a$, considered to be the volumetric mass transfer coefficient with a the interfacial area (m^2/m^3) (Redmond et al., 1983; Gillot et al., 2005; Hébrard et al., 2000; Rosso et al., 2006; Germain et al., 2007). The standardized dynamic method for measuring $k_L \times a$ in
75 clean water is covered elsewhere (ASCE 1992). Indeed impacts on $k_L \times a$ of air flow rate, presence of suspended solids, biomass, antifoams, sludge age, bioreactor geometry, liquid viscosity, ion concentration, temperature, etc. have been investigated in detail over recent decades (e.g. Ju 1995, Gillot 2005, Rosso 2005, Germain 2006, Garcia 2009). The huge number of parameters which can influence $k_L \times a$ makes it
80 difficult to predict the optimal oxygen supply to aerated processes. Moreover, these ($k_L \times a$)-based approaches often make it impossible to determine the separate influence of specific parameters on k_L and a . A relevant example to stress this point is the influence of surfactants.

85 Surfactants are ubiquitous in wastewaters due to the widespread use of soaps and detergents. Their ability to alter oxygen mass transfer has thus been massively considered in the literature (Bel Fdhila and Duineveld, 1996; Hébrard et al., 2000; Vasconcelos et al., 2002; Vasconcelos et al., 2003; Dai et al., 2004; Loubiere and Hébrard, 2004; Alves et al., 2005; Painmanakul et al., 2005; Sardeing et al., 2006;
90 Rosso et al., 2006a; Rosso et al., 2006b; Hébrard et al., 2009; Jamnongwong et al., 2010) and can be summarized as follows:

- Surfactants are amphiphilic in nature. Near gas/liquid interfaces, their hydrophobic tails in the gas phase reduce gas renewal.
- Surfactants mainly accumulate at the bubble rear, in a stagnant cap due to
95 shear at the surface.
- This accumulation at the bubble interface increases the bubble drag coefficient, thereby decreasing the bubble rise velocity.
- Bubble diameters decrease due to presence of surfactants, and this has a positively impact on the interfacial area a .

- 100
- Liquid side mass transfer coefficients, k_L , are depressed by surfactants.
 - With increasing surfactant concentrations, bubbles tend to behave like rigid particles, and the experimental k_L values may then approach asymptotically the well-known correlation for solid spheres in steady state translation relative to a fluid (Frössling, 1938).

105 The reasons why surfactants depress k_L are still controversial. Depending on the studies, this phenomenon has been attributed to a hydrodynamic alteration by lowering the renewal rates at the gas/liquid interface or to molecular obstruction hindering the diffusion of oxygen molecules to the bulk liquid. Surfactants thus have opposite effects, positively influencing the interfacial area while negatively affecting

110 the liquid side mass transfer coefficient. Techniques able to determine both k_L and a are thus essential to evaluate the dominant effect on the global behaviour. In some studies (Painmanakul et al., 2005; Sardeing et al., 2006; Hébrard et al., 2009; Jamnongwong et al., 2010), the interfacial area is estimated by considering gas hold up and mean bubble diameter, allowing the liquid side mass transfer coefficient to be

115 evaluated. However, the global evaluation of $k_L \times a$ (by oxygen probes for instance) remains a rough approach for understanding the governing mechanisms of mass transfer at the gas/liquid interface.

The purpose of this study is to consider methodologies developed by François et al.

120 (2011), Jimenez et al. (2012), Jimenez et al. (2013a) and Jimenez et al. (2013b) to elucidate the influence of surfactants on hydrodynamics and oxygen mass transfer in wastewater. One of these novel methodologies is based on a simplified configuration, with single oxygen bubbles of diameter ~ 1 mm rising in a quiescent liquid. While this approach is far from bubble swarms encountered in aerated processes, surfactants

125 act right at the gas/liquid interface, and thus at a very local scale, so that this simplified configuration facilitates interpretation beyond the mechanisms occurring in presence of surfactants in wastewaters. The second methodology evaluates oxygen diffusion through a planar oxygen/liquid interface in a Hele-Shaw cell. For both of these configurations, the Planar Laser Induced Fluorescence (PLIF) technique

130 provides accurate and local visualization and quantification of the transferred oxygen concentration fields. Evaluation of bubble diameter d_{eq} , aspect ratio χ , rise velocity U_b , transferred oxygen flux F , liquid side mass transfer coefficient k_L , diffusion

coefficient D and oxygen solubility $[O_2]^*$ are investigated in this paper to perform a complete mapping of hydrodynamics and mass transfer in demineralized water, demineralized water plus surfactants and wastewaters from a conventional sewage treatment plant (France,

140 *Materials and methods*

The PLIF technique refers to the absorption and emission of light, at different wavelengths, by a fluorescent dye incorporated in the liquid phase of interest. The excitation light can be generated by a monochromatic laser source whose emission wavelength corresponds to the absorption spectrum of the dye. Part of this excitation light is absorbed by the dye, leading to an excited electronic state. The light that is re-emitted by the dye to return to the fundamental state has a longer wavelength than the absorbed light (Jablonski, 1933; Crimaldi, 2008). This phenomenon is called fluorescence. This process can be inhibited by the presence of quenchers, substances able to absorb (by collisions for instance) surplus energy accumulated by the dye. Oxygen molecules are known to be excellent quenchers (for specific fluorescent dyes) and have been utilized in several studies dealing with PLIF measurements (Jirka et al., 2004; Dani et al., 2007; Kück et al., 2010; François et al., 2011; Jimenez et al., 2012; Kück et al., 2012; Chen et al., 2013, Jimenez et al., 2013a; Jimenez et al., 2013b). Since oxygen molecules inhibit dye fluorescence, their presence in a liquid phase can easily be tracked and quantified based on the Stern-Volmer correlation,

$$\frac{I_0}{I} = 1 + K_{SV}[O_2], \quad (1)$$

where $[O_2]$ is the concentration of dissolved oxygen in the liquid phase (mg/L), I is the fluorescence intensity, I_0 the fluorescence intensity in the absence of oxygen and K_{SV} the Stern-Volmer constant (L/mg). The parameters I_0 and K_{SV} are experimentally determined by calibration $I=f([O_2])$ as proposed in Figure 1. Fluorescence intensities are recorded after dye excitation in a liquid of known and uniform oxygen concentration, measured by oxygen microprobes (Luminescent Dissolved Oxygen

165 Probe, Hach Lange). In a previous study, Jimenez et al. (2013b) demonstrated that
 fluorescence can be directly affected by the liquid phase composition. For instance,
 demineralized water to which small amounts of salt had been added experienced a in
 dye solubility and thus a decrease in fluorescence intensities. Such intensity decreases
 limit the accuracy of determining the corresponding oxygen concentration fields
 170 (based on Equation (1)). Moreover, a decrease in dye solubility implies a higher
 contamination rate at the gas/liquid interface that could strongly affect the measured
 oxygen mass transfer. To overcome these difficulties, a new dye, Dichlorotris (1,10-
 Phenanthroline) Ruthenium(II) hydrate (CAS: 207802-45-7, Sigma Aldrich, USA), is
 introduced in this study. This dye is directly soluble in aqueous phase, does not
 175 significantly alter the liquid phase properties as indicated in Table 1 and presents
 constant calibration parameters (I_0 and K_{SV} in Equation (1)) in the different liquids
 considered in this study (Figure 1).

180 *Table 1. Physico-chemical characteristics of demineralized water in absence and
 presence of 50 mg/L of fluorescent dye (Dichlorotris (1,10-Phenanthroline)
 Ruthenium(II) hydrate) at $20 \pm 1^\circ\text{C}$. σ_L , ρ_L and μ_L are measured respectively with a
 tensiometer (Digidrop GBX 3S®), a Ubbelohde viscometer (Schott Gerate Typ 501
 03/Oc) and a pycnometer (Brand Duran).*

Liquid phase	Surface tension σ_L (mN/m)	Liquid density ρ_L (kg/m ³)	Liquid viscosity μ_L (Pa.s)
Demineralized water	73.7	995	0.001
Demineralized water+50 mg/L of fluorescent dye	73.3	995	0.001

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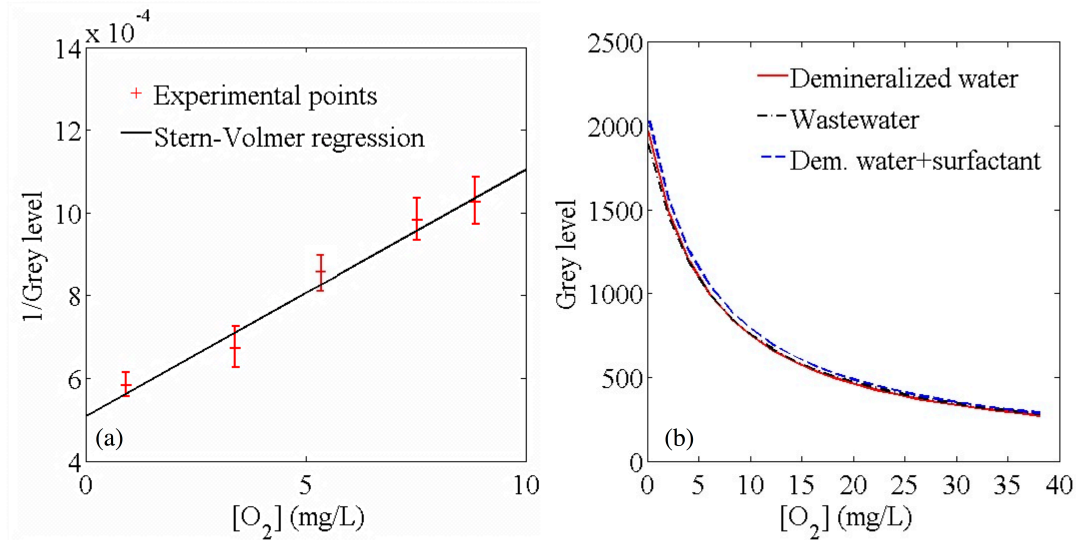


Figure 1. (a) Experimental fluorescence intensities recorded in water for different uniform oxygen concentrations measured by oxygen probes with Dichlorotris dye.

190 Straight line: corresponding linear regression based on the Stern-Volmer correlation ($I_0=1969$, $K_{SV}=0.12$ L/mg). (b) Extrapolated calibration curves (straight line in the left part of Figure 1) based on the Stern-Volmer correlation with Dichlorotris dye in demineralized water, filtered wastewater and demineralized water containing a small amount of dish soap.

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Since oxygen concentration fields are directly extrapolated from the Stern-Volmer calibration, I_0 and K_{SV} are determined for each liquid studied and only assumed valid for one day. Based on the PLIF technique, two methodologies developed by François et al. (2011), Jimenez et al. (2012), Jimenez et al. (2013a) and Jimenez et al. (2013b)

200 are used to evaluate the influence on oxygen mass transfer of surfactants and filtered waters extracted from sewage plants.

(a) Bubble experiments

205 The first technique (François et al., 2011; Jimenez et al., 2013b) aims to visualize released oxygen in the wake of small bubbles rising in a quiescent liquid (Figure 2). The optical device is composed of a laser (LaVision, Nd: Yag, 2×200 mJ) exciting at 532 nm and 10 Hz the fluorescent dye solubilized in the liquid of interest (Dichlorotris (1,10-Phenanthroline) Ruthenium(II), 50 mg/L) along a horizontal

210 plane. A CCD camera (LaVision, 12 bits, 1376×1024 pixels) is placed below the

column and focuses along the laser sheet to record synchronously the fluorescence intensities. The corresponding spatial window is about $3 \times 4 \text{ mm}^2$. A high-speed camera (APX, 8 bits, 1024×1024 pixels) placed on the column side allows the rising bubbles to be visualized and hence the determination of its diameter d_{eq} , aspect ratio χ , velocity U_b . The corresponding spatial window is $3 \times 3 \text{ cm}^2$.

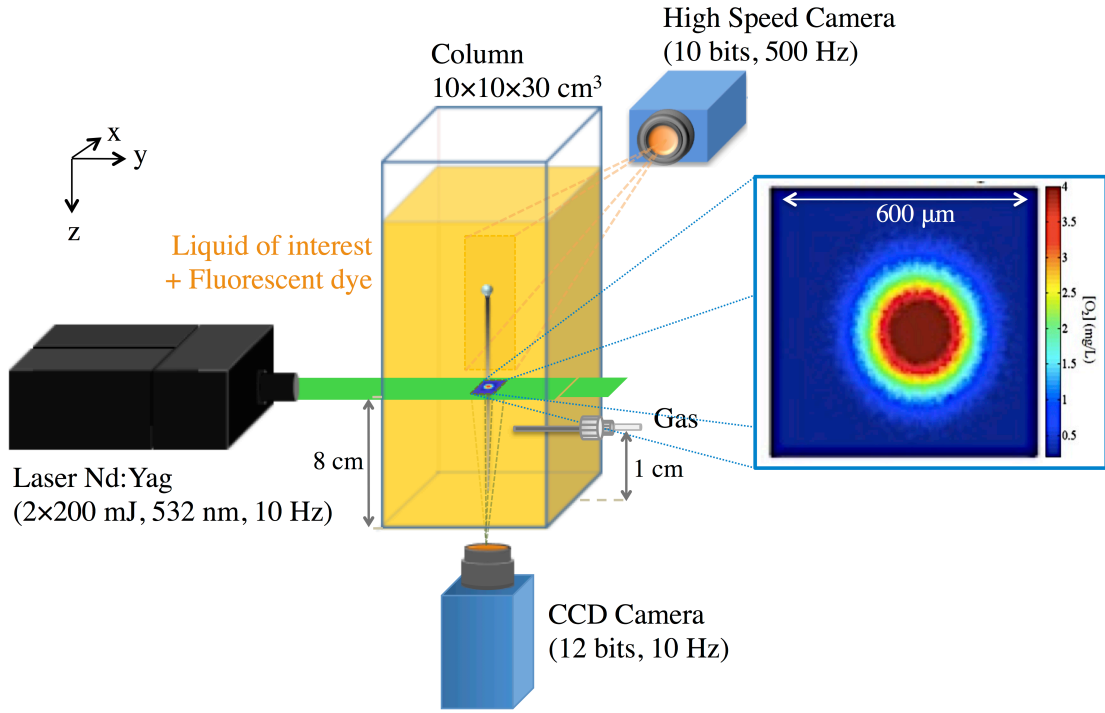


Figure 2. Experimental set-up for visualizing oxygen concentration fields in a bubble wake by PLIF and determining the bubble hydrodynamic characteristics by high-speed camera. Right part: example of experimental oxygen concentration field estimated in the wake of an oxygen bubble ($d_{eq}=1.23 \text{ mm}$, $U_b=28.1 \text{ cm/s}$, $\chi=1.1$) rising in demineralized water at about $300d_{eq}$ from the bubble.

Images are recorded by the CCD camera (as portrayed at the right part of Figure 2) at a frequency of 10 Hz, the upper limit for the optical device. This allows the evolution of the oxygen concentration field with time to be obtained. As noted by Jimenez et al. (2013b) the flux $F \text{ (mg.s}^{-1}\text{)}$ of oxygen transferred by the bubble is linked to the measured oxygen concentration field by

$$F = U_b \iint [O_2] dx dy, \quad (2)$$

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with $\iint [O_2] dx dy$ the integration of the oxygen concentration field at a given time along the recording window. Note that Equation (2) is only valid when the hydrodynamic perturbation due to the bubble passage can be neglected (diffusion of released oxygen as the dominant transport phenomenon). By displaying the flux F for all recorded images after the bubble passage as a function of time, F first increases and reaches an asymptotic region once the dominance of diffusion is reached (see François et al. (2011) and Jimenez et al. (2013b) for further details). The flux F is then estimated by averaging values in this asymptotic region. The flux density J ($\text{mg}\cdot\text{s}^{-1}\cdot\text{m}^{-2}$) can be deduced from the estimated flux F as

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$$J = \frac{F}{S_b}, \quad (3)$$

with S_b the bubble surface being a function of the bubble diameter and aspect ratio, estimated by images recorded by a high-speed camera. The liquid side mass transfer coefficient k_L ($\text{m}\cdot\text{s}^{-1}$) is then given by

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$$k_L = \frac{J}{[O_2]^* - [O_2]_0}, \quad (4)$$

with $[O_2]^*$ the oxygen solubility and $[O_2]_0$ the oxygen concentration in the bulk liquid. Experimental k_L values can classically be compared to two classical limiting cases: Higbie (1935) and Frössling (1938) equations characterizing bubbles with clean and rigid surfaces, respectively.

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$$k_{L\text{Higbie}} = \frac{D}{d_{\text{eq}}} (1.13\text{Re}^{0.5}\text{Sc}^{0.5}) \quad (5)$$

$$k_{L\text{Frössling}} = \frac{D}{d_{\text{eq}}} (2 + 0.66\text{Re}^{0.5}\text{Sc}^{0.33}) \quad (6)$$

255 with D the oxygen diffusion coefficient ($\text{m}^2.\text{s}^{-1}$), d_{eq} the equivalent bubble diameter
 (m), $\text{Re} (=d_{\text{eq}} \times U_b \times \rho_L / \mu_L)$ the Reynolds number and $\text{Sc} (= \mu_L / D \rho_L)$ the Schmidt number.
 To evaluate the contamination rate of the rising bubble, contamination angles are also
 considered based on the approach of Sadhal and Johnson (1983):

$$\frac{C_D - C_D^m}{C_D^{\text{im}} - C_D^m} = \frac{1}{2\pi} \left(2(\pi - \theta_{\text{cap}}) + \sin \theta_{\text{cap}} + \sin 2\theta_{\text{cap}} - \frac{1}{3} \sin 3\theta_{\text{cap}} \right), \quad (7)$$

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with θ_{cap} the contamination angle from the front, C_D , C_D^m and C_D^{im} are drag
 coefficients corresponding to the experimental bubble and bubbles characterized by
 mobile and immobile surfaces respectively. C_D^m and C_D^{im} are approached by
 correlations proposed by Schiller and Naumann (1933) and Mei et al. (1994),
 265 respectively.

(b) Hele-Shaw cell measurements

Based on Equations (5) and (6), the liquid side mass transfer coefficient is directly
 270 related to the oxygen diffusion coefficient D . Since diffusion coefficients in the
 literature differ drastically for oxygen-water systems at 20°C (values ranging from 0.7
 to $2.5 \times 10^{-9} \text{ m}^2.\text{s}^{-1}$), the methodology developed by Jimenez et al. (2012) and Jimenez
 et al. (2013a) using the PLIF technique is also investigated. Oxygen concentration
 fields were also visualized near a planar oxygen/liquid interface in a thin Hele-Shaw
 275 cell filled with about 10 mL of deoxygenated liquid with a 10 L/h pure oxygen flow
 rate passes over the interface (Figure 3) at a velocity too low to cause ripples on the
 surface (average gas velocity in the Hele-Shaw cell 0.07 m/s). The optical device is
 similar to the one presented previously, with a recording spatial window of about 5×6
 mm².

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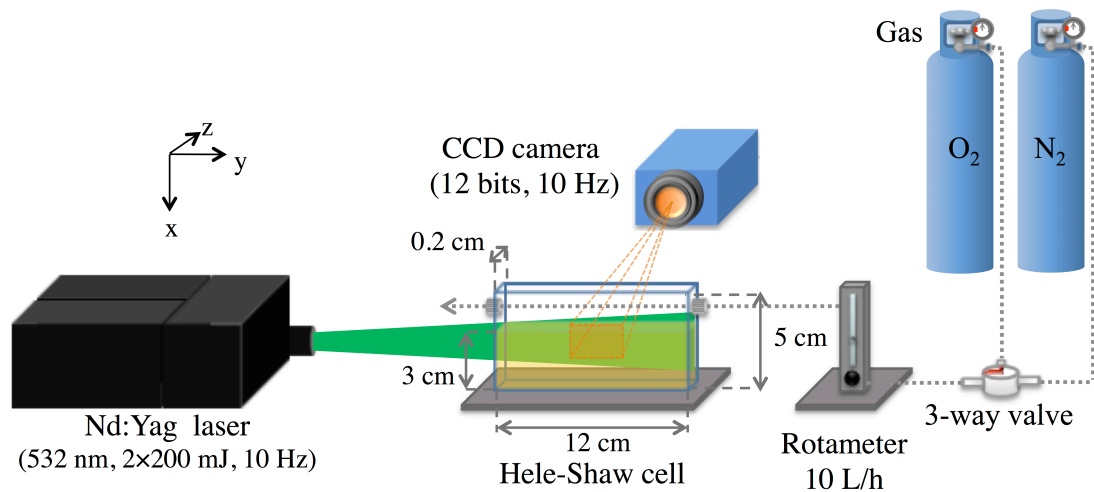


Figure 3. Experimental set-up for visualizing oxygen concentration fields near a planar gas/liquid interface by means of PLIF technique.

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Figure 4 presents an example of images recorded by considering this technique in an oxygen-water plus surfactant solution. In the top region of thickness 0.7 mm, there is no fluorescence since this corresponds to the gas phase. Then, for $0.7 \leq x' \leq 1.1$ mm, a high intensity (white area) is visualized due to the laser reflection at the gas-liquid interface. For $x' > 1.1$ mm, fluorescence intensities in the liquid phase are recorded. At the beginning (up to $t=30$ s), the liquid phase is almost deoxygenated and characterized by strong fluorescence intensities. Due to inhibition of fluorescence in the presence of oxygen molecules, the fluorescence intensity in the liquid darkens with time as oxygen diffuses into the liquid.

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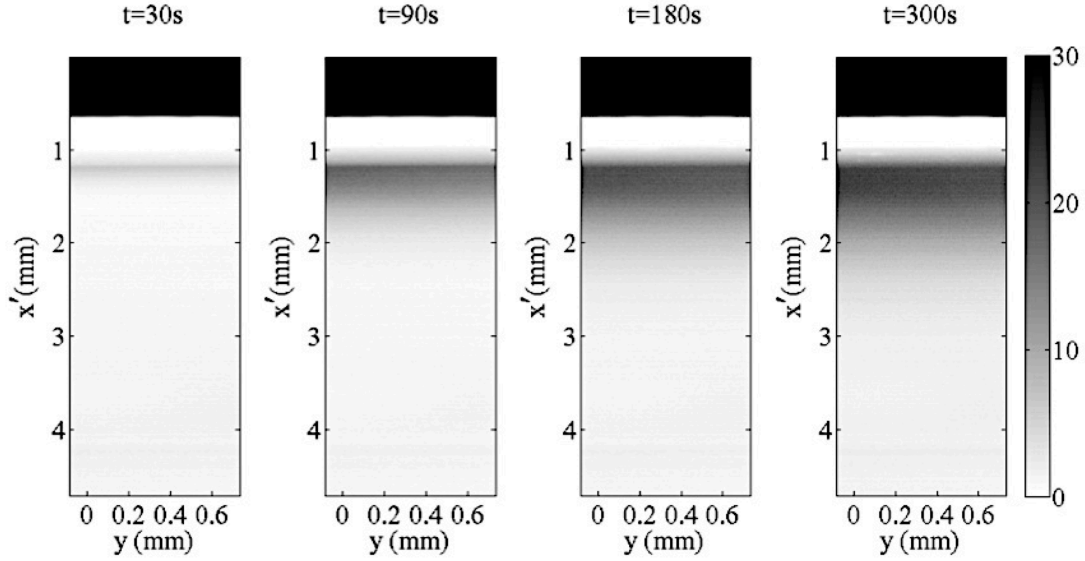


Figure 4. Example of recorded images using PLIF technique near a planar oxygen/water+surfactant (0.008 mL/L of dish soap) interface to visualize the diffusion of oxygen at different times. Colour bar represents oxygen concentrations in mg/L.

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This Hele-Shaw cell configuration allows the problem to be reduced to two dimensions (contribution along the z-axis neglected). Under well-defined gas flow rate and according to Jimenez et al. (2013a), there is no significant convection in the y-direction in the recording window and the transfer of oxygen in the liquid phase is a planar diffusive in the x-direction (Figure 4). Note that Particle Image Velocimetry measurements have been conducted to verify this assumption, with similar conclusions as in Jimenez et al. (2013a). The duration of experiments (few minutes) being short compared with the diffusion characteristic time ($t \approx L^2/D = 75$ min, with L a characteristic length (3 mm for instance, corresponding to the size of the recorded image in the liquid phase) and D the diffusion coefficient $\approx 2 \times 10^{-9}$ m²/s for an oxygen/water system at 20°C), the analytical solution of Fick's law for a semi infinite media (Fick 1855, Crank 1975) is

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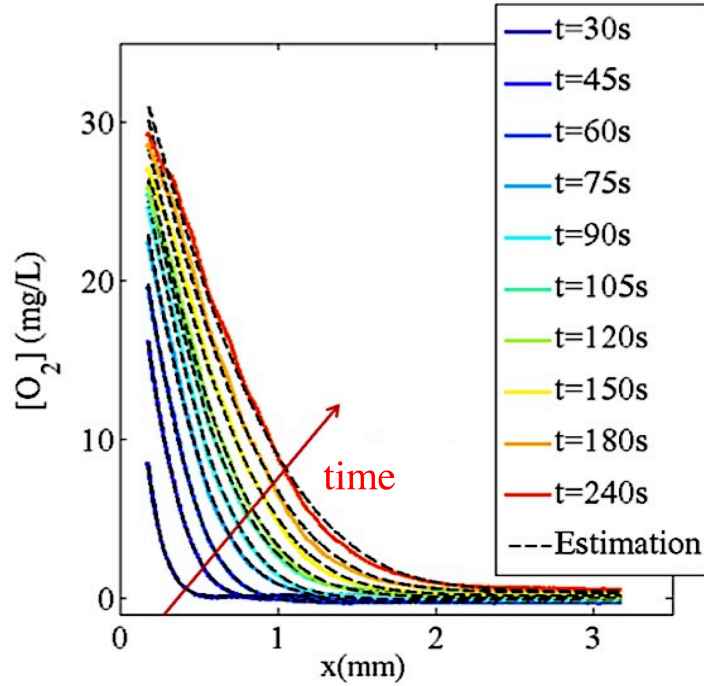
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$$\frac{[O_2](x, t) - [O_2]_0}{[O_2]^* - [O_2]_0} = 1 - \operatorname{erf}\left(\frac{x}{2\sqrt{Dt}}\right), \quad (8)$$

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with x the distance from the gas/liquid interface (m) and t the time since the beginning of the diffusive process (s). Since oxygen concentrations are constant for a fixed value of x (Figure 4), they are averaged along the y-axis to obtain an averaged oxygen

concentration profile as a function of the distance from the interface and as a function of time. Examples of experimental profiles are plotted in Figure 5.



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Figure 5. Experimental oxygen concentration profile as a function of distance from oxygen/water interface at $19 \pm 1^\circ\text{C}$ compared to analytical solution to the Fick's law in a semi-infinite medium.

325 The diffusion coefficient is then estimated by minimization of the function

$$\sum_x \sum_t \|[O_2](x, t)_{\text{exp}} - [O_2](x, t)_{\text{analytic}}\|^2 / 2, \quad (9)$$

with $[O_2](x, t)_{\text{exp}}$ the experimental oxygen concentration and $[O_2](x, t)_{\text{analytic}}$ the concentration deduced from the analytical solution (Equation 8). This minimization is performed by a Markov Chain Monte Carlo method (MCMC), a statistical method more robust than classical gradient-based solvers. Further information can be found in (Robert and Casella, 1999). The experimental oxygen concentration profile $[O_2](x, t)_{\text{exp}}$ and the corresponding distance from the interface x and time t are the required parameters for the MCMC resolution. After minimization of the function in (9), the diffusion coefficient D , oxygen saturation concentration $[O_2]^*$ and uncertainties on the position of the interface $x=0$ and time $t=0$ are estimated. Table 2 presents MCMC

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results corresponding to the experimental oxygen profile in Figure 5 for an oxygen-water system at 20°C.

340 *Table 2. Estimated oxygen solubility [O₂]*, diffusion coefficient D, uncertainties δx and δt on the experimental estimates of $x=0$ and $t=0$ for an oxygen water system at $20\pm 1^\circ\text{C}$ by the MCMC method.*

Estimated parameter	[O ₂]* (mg/L)	D ×10 ⁹ (m ² /s)	δx (μm)	δt (s)
Estimated value	39.0 ± 0.3	1.90 ± 0.01	1.0±0.5	20.8±0.3

345 Estimated values of solubility and diffusion coefficient are in good agreement (relative errors less than 10%) with values usually encountered in the literature (Scheibel, 1954; Wilke and Chang, 1955; Roustan, 2003; Jamnongwong et al., 2010). For an oxygen-water system, the experimental uncertainty of the $x=0$ position (referring to the methodology proposed by Jimenez 2013a) is negligible compared
 350 with the 21 s shift for $t=0$. The time started experimentally when the 3-way valve was switched to oxygen. However, this neglects the required time for the gas to reach the Hele-Shaw cell, which can explain this large δt value.

(c) Liquids investigated

355 To summarize, the first technique allows the oxygen mass transfer to be visualized and quantified in the wake of small oxygen bubbles rising in a quiescent liquid. The bubble diameter d_{eq} , aspect ratio χ , rise velocity U_b , contamination angle θ_{cap} as well as oxygen transfer flux F , flux density J and liquid-side mass transfer coefficient k_L
 360 are all determined. The second technique determines oxygen concentration fields near a planar oxygen/liquid interface under controlled hydrodynamic conditions in a Hele-Shaw cell. This diffusive process leads to the estimation of the oxygen solubility [O₂]* and diffusion coefficient D.

365 All of these parameters were measured for demineralized water, water plus surfactants and water extracted from a sewage plant. Surfactants tested were dish soap (0.004 mL/L and 0.008 mL/L, PAIC Citron®) and Caprylate monoglyceride C₁₁H₂₀O₅ (0.02

and 0.22 g/L). Wastewaters were extracted from a sewage plant working with activated sludge (Saint-Vrain, France, with an average wastewater flow rate of wastewaters of 2853 m³/day). Raw wastewater and treated water were investigated in this study after filtration with membranes of 0.2- μ m and 2- μ m pore diameter respectively. The relevant physico-chemical properties of these liquids, each containing 50 mg/L of fluorescent dye are presented in Table 3.

Table 3. Measured liquid surface tension σ_L , density ρ_L , viscosity μ_L , pH and conductivity λ for demineralized water and various aqueous solutions tested at atmospheric pressure and 19 \pm 2°C. All these liquids contained 50 mg/L of fluorescent dye.

Liquid phase + 50 mg/L of dye	σ_L (mN/m)	ρ_L (kg/m ³)	μ_L (mPa.s)	pH	λ (μ S/cm)
Demineralized water	73.3	995	1.0	6.2	25
+0.004 mL/L dish soap	58.6	-	1.0	6.3	17
+0.008 mL/L dish soap	33.3	-	1.0	6.5	18
+0.02 g/L C ₁₁ H ₂₀ O ₅	35.4	997	1.0	6.0	17
+0.22 g/L C ₁₁ H ₂₀ O ₅	33.3	998	1.0	6.1	16
Treated water	69.3	998	1.0	7.9	1324
Wastewater	44.1	997	1.0	8.5	1266

Table 3 shows that the presence of surfactants strongly decreases the liquid surface tension. Both caprylate monoglyceride cases are above the critical micelle concentration (CMC=0.013 g/L, Zhang et al., 2003). Discrepancies in measured surface tensions are probably related to the tensiometer accuracy (\pm 1 mN/m). As mentioned previously, surfactants are used daily and thus are largely present in sewage plants; as deduced from its measured surface tension.

Experimental results

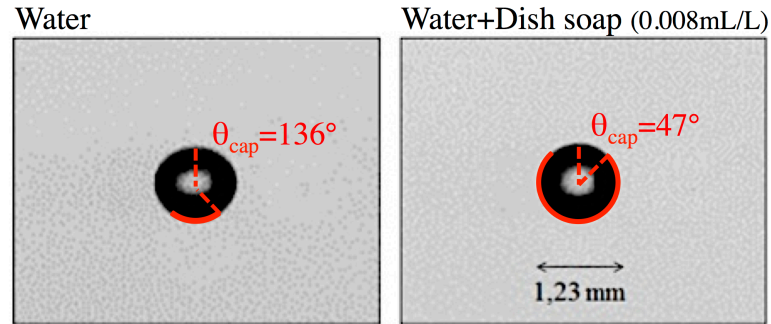
390 Table 4 presents hydrodynamic results for isolated oxygen bubbles in the different
liquids of interest whose properties appear in Table 3.

395 *Table 4. Measured bubble diameter, aspect ratio, bubble rise velocity and
contamination angle based on stagnant-cap approach for single oxygen bubbles in
different aqueous liquids including wastewater extracted from a sewage plant. ±
values correspond to repeatability errors estimated for at least five bubbles for each
liquid.*

Liquid phase + 50 mg/L of dye	d_{eq} (mm)	χ	U_b (cm/s)	θ_{cap} (°)
Demineralized water	1.23 ± 0.03	1.12 ± 0.02	28.1 ± 0.5	136.3
+0.004 mL/L dish soap	1.22 ± 0.00	1.02 ± 0.00	16.7 ± 0.1	98.0
+0.008 mL/L dish soap	1.22 ± 0.00	1.01 ± 0.00	13.6 ± 0.1	46.7
+0.02 g/L C ₁₁ H ₂₀ O ₅	1.21 ± 0.01	1.01 ± 0.02	12.9 ± 0.1	0.0
+0.22 g/L C ₁₁ H ₂₀ O ₅	1.19 ± 0.00	1.02 ± 0.01	12.7 ± 0.1	0.0
Treated water	1.23 ± 0.01	1.03 ± 0.00	20.6 ± 0.1	116.4
Wastewater	1.19 ± 0.00	1.01 ± 0.00	12.6 ± 0.1	0.0

400 As observed in the literature (e.g. Clift et al., 1978; Alves et al., 2005), bubble rise
velocities are strongly altered in presence of surfactants as a direct consequence of
larger contamination angles. Fully contaminated bubbles are obtained for caprylate
monoglyceride and filtered wastewaters. Unfortunately, it was impossible to perform
experiments with higher concentrations of dish soap due to the presence of foam.

405 Volume-equivalent bubble diameters were similar for all the cases tested, although
there was some variation in shape with aspect ratios approaching 1, corresponding to
a spherical shape, in the presence of surfactants as indicated in Figure 6. Note that the
contamination angle for demineralized water (136°) differs significantly from the
410 180° value characterizing a clean surface. This reflects the stringent measures needed
to achieve surfactant free conditions (Clift et al., 1978). The presence of the
fluorescent may itself have contributed to bubble contamination.



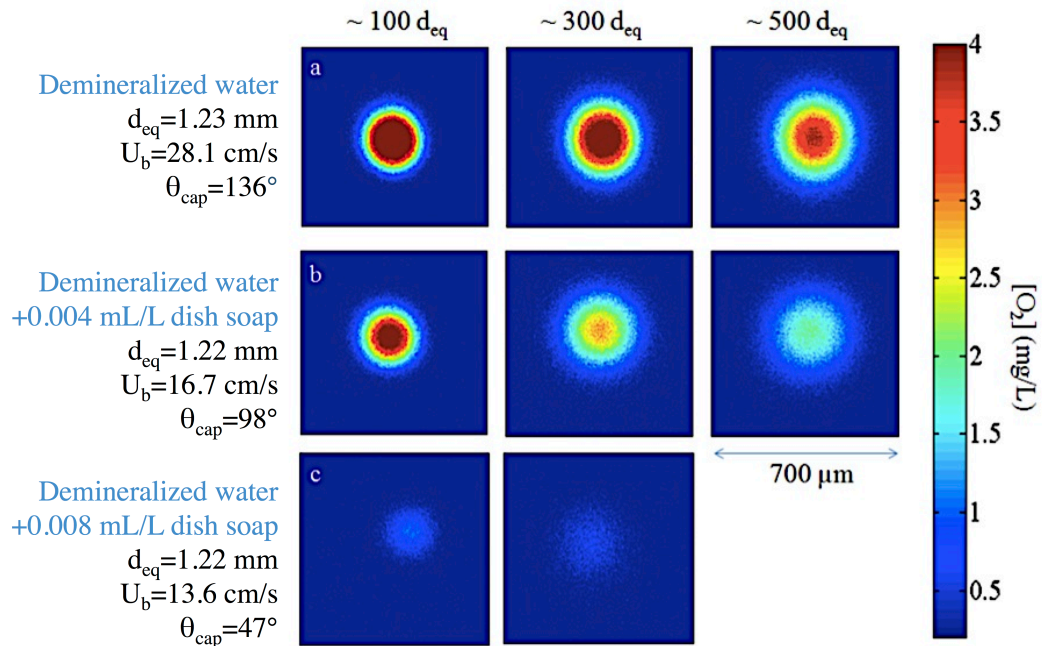
415 *Figure 6. Visualization of oxygen single bubbles in demineralized water ($d_{eq}=1.23$ mm, $\chi=1.1$, $U_b=28.1$ cm/s) and demineralized water+0.008 mL/L of dish soap ($d_{eq}=1.22$ mm, $\chi=1.0$, $U_b=13.6$ cm/s). Contact angles are based on the stagnant cap model.*

420 There were substantial differences in the oxygen released in the wake of these bubbles, based on the PLIF technique. Figures 7 and 8 display oxygen concentration fields observed in the wake of bubbles, viewed horizontally (perpendicular to the bubble ascension, see Figure 2). Distances are deduced from the time elapsed between the bubble passing through the laser sheet and the corresponding recorded image, the bubble rise velocity U_b being known. Bubbles being almost spherical for all cases tested, the visualized oxygen concentration fields were always close to circular, growing with time due to diffusion. However, the higher the surface tension and the contamination angle, the weaker the oxygen concentration field in the bubble wake. For instance, in demineralized water with 0.008 mL/L of dish soap, released oxygen is

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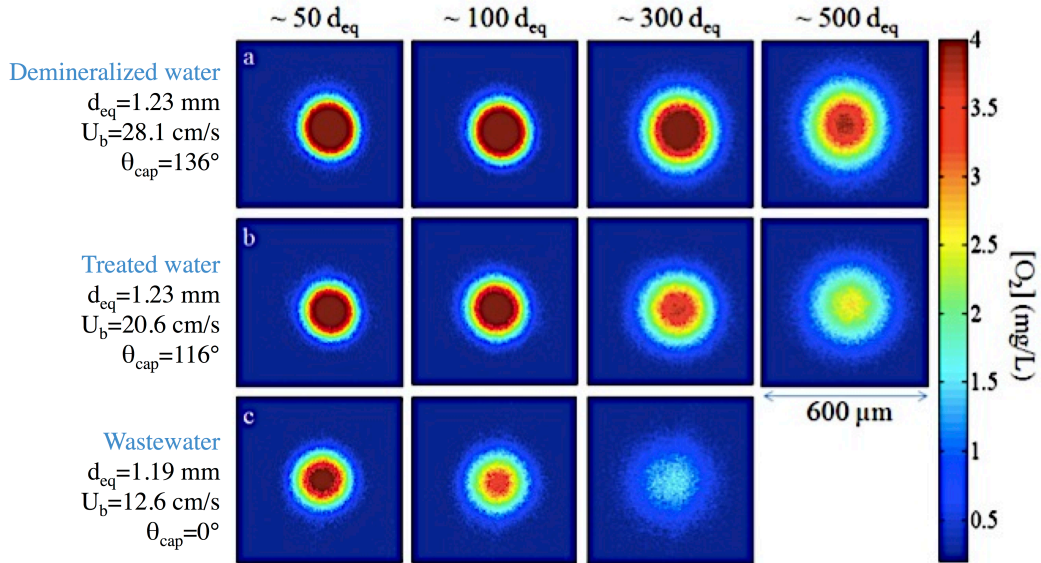
430 hardly visible (oxygen concentrations less than 1 mg/L). Similar conclusions can be obtained from the images recorded with bubbles in wastewater and treated water (Figure 8) even though a weaker depression in the oxygen concentration field is observed.

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440 *Figure 7. Oxygen concentration fields (expressed in mg/L) estimated by PLIF technique for single rising oxygen bubbles in demineralized water, demineralized water + 0.004 mL/L of dish soap and demineralized water + 0.008 mL/L of dish soap at different distances from the bubble. Hydrodynamic characteristics of the bubbles are proposed at the left.*

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450 *Figure 8. Oxygen concentration fields (expressed in mg/L) estimated by PLIF technique for single rising oxygen bubbles in demineralized water, filtered treated water and wastewater from a sewage plant based on activated sludge treatment at different distances to the bubble. Hydrodynamic characteristics of the bubbles are provided at the left.*

455 As a direct consequence of the reduction in released oxygen, parameters characterizing the mass transfer are affected also. Table 5 presents the corresponding $\iint [O_2] dx dy$ integral, flux and flux densities estimated from Equations (2) and (3).

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465 *Table 5. Measured integral $\iint [O_2] dx dy$, transferred oxygen flux F and flux density based on equations (2) and (3) and images recorded with the PLIF for isolated oxygen bubbles in liquids whose properties are presented in Table 3.. \pm values correspond to repeatability error estimated at least five bubbles for each liquid of interest.*

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Liquid phase + 50 mg/L of dye	Integral $\times 10^5$ (mg/m)	Flux F $\times 10^6$ (mg/s)	Flux density J ($\text{mg}\cdot\text{m}^{-2}\cdot\text{s}^{-1}$)
Demineralized water	27 \pm 3	73 \pm 5	15.4 \pm 0.9
+0.004 mL/L dish soap	17 \pm 1	29 \pm 1	6.3 \pm 1.0
+0.008 mL/L dish soap	4 \pm 1	5 \pm 1	1.0 \pm 0.5
+0.02 g/L C ₁₁ H ₂₀ O ₅	8 \pm 1	11 \pm 1	2.3 \pm 0.5
+0.22 g/L C ₁₁ H ₂₀ O ₅	3 \pm 1	4 \pm 1	0.7 \pm 0.2
Treated water	21 \pm 1	43 \pm 2	9.0 \pm 0.5
Wastewater	12 \pm 1	15 \pm 2	3.4 \pm 0.1

For low liquid surface tensions, the integral term is markedly less than for demineralized water. Since the bubble rise velocity tends to decrease also, strong
480 diminutions in oxygen transferred flux and flux densities are observed. Table 5 shows the impact of the contamination angle on the oxygen mass transfer. For both caprylate monoglyceride cases (concentrations > CMC), bubbles present a fully contaminated surface ($\theta_{\text{cap}}=0^\circ$), with their rising velocities reaching a constant value regardless of the surfactant concentration. However, the integral, flux and flux densities in Table 4
485 continue to decline drastically for higher surfactant concentration. This clearly indicates the presence of an interfacial phenomenon hindering oxygen mass transfer beyond the impact on the rising velocity and Reynolds number. Based on the Higbie and Frössling equations (Equations (5) and (6)), another parameter apart from the Reynolds number impacting the k_L value could be the bulk diffusion coefficient, D.
490 To test this hypothesis, oxygen diffusion coefficients and solubilities are provided in Table 6 based on measurements in the Hele-Shaw cell through a planar oxygen/liquid interface.

495 *Table 6. Measured oxygen diffusion coefficient D and solubility $[O_2]^*$ based on equation (9) and images recorded with the PLIF technique through a planar oxygen/liquid interface for different liquids. \pm values correspond to repeatability error estimated from at least three measurements for each liquid of interest.*

Liquid phase + 50 mg/L of dye	D $\times 10^9$ (m ² /s)	$[O_2]^*$ (mg/L)
Demineralized water	1.90 \pm 0.1	39.0 \pm 0.2
+0.004 mL/L dish soap	1.60 \pm 0.10	49.0 \pm 1.0
+0.008 mL/L dish soap	1.70 \pm 0.10	31.0 \pm 1.0
+0.02 g/L C ₁₁ H ₂₀ O ₅	-	-
+0.22 g/L C ₁₁ H ₂₀ O ₅	-	-
Treated water	2.02 \pm 0.10	42.0 \pm 1.0
Wastewater	2.03 \pm 0.20	46.0 \pm 2.0

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Surprisingly, experimental diffusion coefficients in the presence of surfactants and in waters extracted from sewage plant are quite similar to that of an oxygen-water system, although there was an appreciable decrease in the presence of dish soap. No tendencies can be deduced from the estimated saturation concentrations, extrapolated from experimental profiles (such as Figure 5) at the gas/liquid interface ($x=0$). However due to a thicker meniscus at the gas/liquid interface in the presence of surfactants, a higher reflection area appears in the recorded images. As is clearly visible in Figure 3, a 0.5 mm area of high reflection, characterized by the white zone at about $x' \approx 1$ mm, hinders accurate location of the gas/liquid interface and thus estimation of oxygen solubility. Note that for an oxygen-water system, this reflection zone is less than 0.1 in height facilitating estimation of the oxygen solubility. Nevertheless, oxygen concentrations measured by probes in these liquids saturated with oxygen are insensitive to the presence of surfactants. Our experimental results from the Hele-Shaw cell indicate that there is no significant difference between demineralized water, demineralized water and surfactant and waters extracted from sewage plant in term of diffusion coefficient and solubility.

This result means that, for the cases dealing with caprylate monoglyceride, there is negligible difference in the Schmidt and Reynolds numbers for the tested concentrations. Liquid-side mass transfer coefficients estimated by the Frössling correlation are thus similar for these two concentrations. However, as mentioned above, the higher the surfactant concentration, the lower the experimental oxygen transferred flux, flux density and k_L . Table 7 presents experimental liquid-side mass transfer coefficients estimated with:

- Experimental values, $k_L \text{ exp}$, based on experimental oxygen solubilities (Table 6) and on equation (4).
- Values labelled $k_L \text{ exp}'$ based on experimental solubility obtained in demineralized water (since no major difference in terms of solubility was measured by oxygen probes) and equation (4).
- Values labelled $k_L \text{ Frössling}$ from the Frössling correlation (Equation 6) applied with estimated diffusion coefficients (from Table 6).

Table 7. Comparison of experimental liquid-side mass transfer coefficients for different liquid media with ($k_{L \text{ exp}}$) experimental oxygen solubility presented in Table 5 or with the solubility of oxygen in water ($k_{L \text{ exp}}'$) and with liquid-side mass transfer coefficient estimated with the equation of Frössling (1938).

Liquid phase + 50 mg/L of dye	$k_L \text{ exp}$ $\times 10^4$ (m/s)	$k_L \text{ exp}'$ $\times 10^4$ (m/s)	$k_L \text{ Frössling}$ $\times 10^4$ (m/s)	θ_{cap} (°)
Demineralized water	3.95	3.95	1.53	136.3
+0.004 mL/L dish soap	1.29	1.62	1.06	98.0
+0.008 mL/L dish soap	0.32	0.26	0.99	46.7
+0.02 g/L $C_{11}H_{20}O_5$	0.48	0.59	1.05	0.0
+0.22 g/L $C_{11}H_{20}O_5$	0.16	0.18	1.06	0.0
Treated water	2.14	2.31	1.37	116.4
Wastewater	0.74	0.87	1.10	0.0

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For all cases involving non-zero contamination angles, higher θ_{cap} resulted in experimental k_L values tending to the Frössling correlation. However, results differ from the literature when the contamination angle is 0° . It is usually assumed that above the CMC, bubbles behave as rigid particles with liquid-side mass transfer coefficients well characterized by the Frössling correlation. In this study, this procedure markedly overestimates k_L . As mentioned above, beyond the CMC, bubble rise velocities are constant and oxygen diffusion coefficients are nearly the same as in water. However, the measured oxygen concentration fields still decreased as the surfactant concentration increased. To reach k_L values with the Frössling correlation in accordance with experimental liquid-side mass transfer coefficients, smaller diffusion coefficients would be required: $D= 8 \times 10^{-10}$, 1×10^{-10} and 1×10^{-9} m^2/s for demineralized water with 0.02 g/L and 0.22 g/L of caprylate monoglyceride and filtered wastewaters respectively. The Hele-Shaw cell methodology for determining oxygen diffusion coefficients (like other available techniques for determination of this parameter) is not relevant in the presence of surfactants, since measurements are performed hundreds of micrometers away from the interface due to laser reflection and optical resolution considerations. In the range of concentration covered in this study, surfactants tend to congregate at the gas/liquid interface, the rest of the liquid behaving like water. By measuring the diffusion coefficient “far” from the interface, experimental diffusion coefficients are similar to those for an oxygen-water system. Moreover, depending on the caprylate monoglyceride concentration, different diffusion coefficients are required to fit experimental data to the Frössling correlation. This highlights the presence of a surfactant barrier at the gas/liquid interface whose “barrier level” depends on the surfactant concentration, and probably also on the extent of multilayer congregation at the interface. Finally, the higher the surfactant concentration, the thicker the barrier and thus the lower the transfer of oxygen. Waters extracted from sewage plant are subject to the same considerations and conclusions. This highlights the high capacity of surfactants to hinder mass transfer, but also the great care needed if standard equations are to be applied for designing aerated processes in this range of bubble diameters.

Conclusions

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This paper utilizes for the first time efficient visualization techniques developed previously to better understand the mechanisms that locally govern the gas/liquid mass transfer in presence of surfactants in demineralized water and wastewaters. These techniques are focused on oxygen mass transfer (i) from single millimetre-size bubble, rising in a stagnant liquid free from solid particles (two-phase system) and (ii) through a planar oxygen/liquid interface in a Hele-Shaw cell. Results can be summarized as follows

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- There is a strong depression in bubble rise velocity in the presence of surfactants, causing higher angles of contamination.

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- Bubbles generated in filtered wastewaters and in demineralized water with surfactant concentration higher than the critical micelle concentration (CMC) are fully contaminated.

- Above the CMC, for the surfactants and concentrations tested, the bubble rise was independent of surfactant concentration.

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- Whatever the contamination angle, the higher the surfactant concentration, the lower the transfer of oxygen to the liquid phase.

- The experimental liquid-side mass transfer coefficient was lower by 80% for wastewater and by 46% for treated water than for demineralized water.

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- Diffusion coefficients estimated in the bulk liquid, i.e. away from the gas-liquid interface, were similar for all liquids tested and equal to that obtained for an oxygen-water system at 20°C.

- The Frössling correlation with experimental Reynolds and Schmidt numbers, overestimates oxygen mass transfer for fully contaminated bubbles. This overestimation was by a factor of 2 for wastewater.

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These results highlight the presence of mass transfer inhibition at the gas/liquid interface, separate from the impact of surfactants on contamination angle and reduction in rising velocity. Since this inhibition is enhanced by increasing surfactant concentration, a congregation of surfactants occurs at the gas/liquid interface providing a barrier to mass transfer. Further experiments focusing at the interface scale are required to provide further understanding of this inhibition effect. It would

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also be interesting to extend this approach to larger bubble diameters which are likely to be affected less by the presence of surfactants.

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a	Interfacial area	m^2/m^3
C_D	Drag coefficient	
C_D^m	Drag coefficient for a mobile bubble surface	
C_D^{im}	Drag coefficient for an immobile bubble surface	
D	Oxygen diffusion coefficient	m^2/s
d_{eq}	Equivalent bubble diameter	m
F	Flux of transferred oxygen	mg/s
He	Henry's law constant	Pa
I	Fluorescence intensity	-
I_0	Fluorescence intensity in absence of oxygen	-
J	Flux density of transferred oxygen	$\text{mg}\cdot\text{s}^{-1}\cdot\text{m}^{-2}$
k_L	Liquid side mass transfer coefficient	m/s
K_{SV}	Stern-Volmer constant	L/mg
$[O_2]$	Oxygen concentration	mg/L
$[O_2]^*$	Oxygen saturation concentration	mg/L
$[O_2]_0$	Oxygen concentration in the bulk liquid	mg/L
Re	Reynolds number	-
S_b	Bubble surface	m^2
Sc	Schimdt number	-
t	time	s
U_b	Bubble rise velocity	m/s
x	Distance to the gas/liquid interface	m
θ_{cap}	Contamination angle	°
μ_L	Dynamic viscosity in the liquid phase	Pa.s
ρ_L	Density of the liquid phase	kg/m^3
σ_L	Surface tension in the liquid phase	mN/m
χ	Bubble aspect ratio	-
λ	Liquid conductivity	$\mu\text{S}/\text{cm}$

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