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Javier Contreras, Athanasios Kolios

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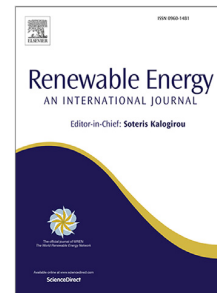
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# An autonomous decision-making agent for offshore wind turbine blades under leading edge erosion

Javier Contreras<sup>a,\*</sup>, Athanasios Kolios<sup>b</sup>

<sup>a</sup>*Naval Architecture, Ocean and Marine Engineering, University of Strathclyde, 16 Richmond St, Glasgow – G1 1XQ, Scotland, UK*

<sup>b</sup>*Department of Wind and Energy Systems Structural Integrity and Loads Assessment, Technical University of Denmark, Risø Campus Frederiksborgvej 399, Roskilde 4000, Denmark*

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## Abstract

The increasing pressure of offshore wind developments is leading to projects being located in areas with more difficult access and greater weather barriers. As these constraints increase, O&M costs also grow in importance. Therefore, the current scenario requires a careful planning to avoid unnecessary costly maintenance decisions or unexpected failures. To overcome the problem of increasing O&M costs and difficult access, this manuscript presents an autonomous decision-making Reinforcement Learning (RL) agent to improve O&M planning for the Leading Edge Erosion (LEE) problem. The method developed in this work makes use of a linear degradation model to account for the damage progression dynamics and site-specific weather models. The RL-based agent proposed in this manuscript is able to reduce expected O&M costs in the range of 12-21% when compared with condition-based policies.

## List of Abbreviations

<b>ANN</b>	Artificial Neural Network
<b>CFD</b>	Computational Fluid Dynamics
<b>CfD</b>	Contracts for Difference
<b>CTV</b>	Crew Transfer Vessel
<b>DQN</b>	Deep Q Networks
<b>HLV</b>	Heavy Lift Vessel
<b>LEE</b>	Leading Edge Erosion
<b>MIP</b>	Mixed Integer Programming
<b>MDP</b>	Markov Decision Process
<b>NLP</b>	Non-linear programming

## Highlights

- A decision-support framework for LEE maintenance is presented.
- Weather, material and repair success uncertainties are considered in the framework.
- An autonomous RL-based agent is trained considering site-specific conditions.
- The agent improves expected O&M costs against condition-based baseline policies.

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The increasing pressure of offshore wind developments is leading to projects being located in areas with more difficult access and greater weather barriers. As these constraints increase, O&M costs also grow in importance. Therefore, the current scenario requires a careful planning to avoid unnecessary costly maintenance decisions or unexpected failures. To overcome the problem of increasing O&M costs and difficult access, this manuscript presents an autonomous decision-making Reinforcement Learning (RL) agent to improve O&M planning for the Leading Edge Erosion (LEE) problem. The method developed in this work makes use of a linear degradation model to account for the damage progression dynamics and site-specific weather models. The RL-based agent proposed in this manuscript is able to reduce expected O&M costs in the range of 12-21% when compared with condition-based policies.

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<b>OWTs</b>	Offshore Wind Turbines
<b>O&amp;M</b>	Operation and maintenance
<b>PN</b>	Petri Nets
<b>RL</b>	Reinforcement learning
<b>WARER</b>	Whirling Arm Rain Erosion test Rig

### Keywords

Leading edge erosion; Wind turbine blade O&M; Blade erosion degradation; Wind turbine O&M optimisation.

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## 1. Introduction

The rise of renewable energies and the challenging carbon-emission reduction goals set for the upcoming years have driven the exploration of offshore energy opportunities. In this context, offshore wind turbines (OWTs) are one of the most promising offshore energy sources. With the knowledge and expertise gained from the bottom-fixed sites, the development of floating wind technologies unlocked a large range of potential sites. Despite the knowledge of OWTs being much more premature than that of onshore ones (64.3 GW vs 841.9 GW capacity installed worldwide) the potential benefits of its large-scale deployment, such as the potential to install larger turbines or the reduction of the environmental impact of wind farms are propelling its growth. According to the Global Wind Energy Report 2023 produced by the Global Wind Energy Council (GWEC), the wind energy market is expected to grow by 15% on average per year and the compound annual growth rate of offshore wind reach 32% in the next five years.

Despite the promising outlook for the offshore wind industry, several issues still need to be addressed to make this technology as competitive as its onshore counterpart. The O&M costs of OWTs are estimated to account for 25-30% of the total lifecycle costs [1]. Offshore maintenance activities are estimated to be five to ten times more expensive than those performed onshore [2, 3]. When combined with the required weather

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\*Corresponding author  
Email addresses: javier.contreras-lopez@strath.ac.uk (Javier Contreras), atko@dtu.dk (Athanasios Kolios)

16 windows for maintenance activities, this can result in O&M costs that are double those of onshore turbines  
17 [4]. The combination of accessibility challenges and the lower reliability of large rotor turbines offshore  
18 turbines [5] creates a challenging scenario leading the operators to use preventive or reactive maintenance  
19 resulting in unnecessary O&M costs [6].

20 Given the challenges of maintenance planning, the use of decision support tools is vital for offshore wind  
21 farm operators. Many efforts have recently been made to develop different tools to optimise one or many of  
22 the different existing maintenance methods: routine inspections, corrective maintenance, preventive maintenance,  
23 condition-based maintenance, predictive maintenance or opportunistic maintenance. Several different  
24 approaches have been used. These include methods such as Mixed Integer Programming (MIP), Non-linear  
25 Programming (NLP), stochastic models, Markov models, Petri Nets (PN) models, analytical models, fuzzy  
26 models, intelligent algorithmic models, and multi-objective models, to name a few. Regardless of the method  
27 used, scholars have targeted different levels for optimisation, ranging from individual components such as  
28 the tower, foundation, or drivetrain, to the entire turbine or wind farm. The objectives for optimisation  
29 include O&M costs, logistics costs, availability, reliability, and environmental impact. Some of the most  
30 recent publications are summarised here. Saleh et al. [7] proposed a PN model combined with RL for the  
31 O&M of wind turbines. Elusakin et al. [8] developed a stochastic PN model for O&M planning of floating  
32 offshore wind turbines. Yan and Dunnet [9] studied the maintenance of OWTs under the PN paradigm and  
33 considering periodic maintenance, condition-based maintenance and reactive maintenance policies. Ge et al.  
34 [10] designed a maintenance planning optimisation algorithm based on MIP to minimise power generation  
35 losses on maintenance activities. Li et al. [11] proposed a multi-objective maintenance strategy optimisation  
36 framework at wind-farm level considering uncertainty in the maintenance performance. In [12], Schouten et  
37 al. introduce a single-component model for maintenance optimisation under time-varying costs that is ap-  
38 plicable to offshore wind turbine maintenance. Aafif et al. [13] provides an optimal preventive maintenance  
39 strategy for a wind turbine gearbox based on its temperature. In [14], Yong and Qirong propose an optimi-  
40 sation maintenance scheme for the maintenance missions considering the time windows based on a hybrid  
41 ant colony algorithm. In [15], Zou and Kolios propose a framework to improve maintenance decision-making  
42 by quantifying the value of information of condition monitoring.

43 The modelling of the O&M of OWTs at turbine level or wind farm level requires a deep knowledge  
44 about the failure modes of the components that carry the highest weights in the maintenance activities.  
45 Damage is usually discretised in states and its progression represented with a probabilistic description of the  
46 transition between them. The calibration of these require the possession of considerable amounts of failure  
47 and maintenance data of the same or similar equipment in sites with similar weather conditions to provide  
48 good results. Alternatively, the use of detailed models, can provide with a numerical testing environment to  
49 obtain synthetic data. Higher level models require more computationally affordable damage descriptions that  
50 can mimic the real behaviour of damage degradation. Being the rotor one of the most critical components

[16, 17] and LEE one of the failure modes carrying the higher criticality [17–20], its O&M planning requires a careful analysis. The unattended evolution of LEE can have aerodynamic, environmental and structural implications increasing in importance and finally being able to produce the catastrophic failure of the blade. Lifetime assessments of erosion protection systems can be found in the literature, such as the works performed by Hasager et al. [21, 22] and [23]. In [21], the lifetime assessment of leading edge protection systems of Vestas V52 turbines for sites in the Danish Seas was performed, finding expected lifetimes between 2 and 13 years. Also, in [22], for sites in the North and Baltic Sea, the expected lifetime of coatings was in the range of 1 to 25 years. There have been many efforts to estimate the life of protective coatings but, to the best knowledge of the authors, there are no studies focusing on the predictive maintenance of this failure mode. Under this high uncertainty in coating lifetime and weather effects, there is a need for a decision support tool to improve the decision-making capability of wind farm operators. The potential benefits of its application increase with its application in harsher environment. In this sense, the current study presents a novel autonomous decision-making RL agent to optimise OWT LEE O&M costs. The uncertainties in weather scenarios, maintenance performance and LEE protective coating behaviour are considered in this paper. The proposed agent, once trained, can provide an action suggestion at any stage of the turbine service life. Also, the proposed agent can be retrained once real operation data becomes available improving its accuracy and providing further O&M cost reduction.

The remainder of this paper is structured as follows: Section 2 presents the methodology used for the optimisation of the O&M planning. Section 3 provides the assumptions and considerations of the O&M model used in this study. Section 4 presents two case studies to evaluate the performance of the proposed decision-support agent. Section 5 offers a discussion about the benefits and limitations of the framework presented as well as some follow-up opportunities. Finally, Section 6 summarises the conclusions of the application of the proposed methodology.

## 2. Methodology

This section delineates the methodology employed in this study, which is divided into two subsections. The first subsection elucidates the computational framework for LEE degradation and turbine operation simulation, while the second one delves into the decision-making framework for the optimisation of O&M costs.

### 2.1. Computational framework

This subsection provides a description of the *environment* and the computational framework that defines the dynamics of the degradation of the system.

LEE is a degradation phenomenon that affects wind turbine blades in several aspects (acoustic, aerodynamic and structural). The relations between the parameters affecting this problem is shown in Figure 1.

84 This phenomenon is caused by fatigue degradation through a repeated number of impacts of airborne parti-  
 85 cles (rain, insects and other airborne particles) onto the outermost layers of the blade. The dynamics of this  
 86 process are affected by a number of parameters such as the impact energy, coating material parameters and  
 87 weather conditions. The present computational framework provides a method to consider uncertainty in the  
 88 abovementioned parameters. This computational framework is presented in [24] and depicted in Figure 2.  
 89 To account for the uncertainty in climatic, material and aerodynamic parameters, the techniques described  
 90 below can be used.

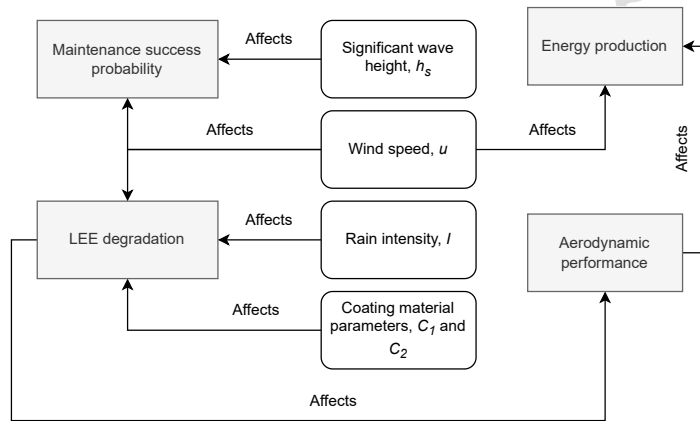


Figure 1: Relations between parameters



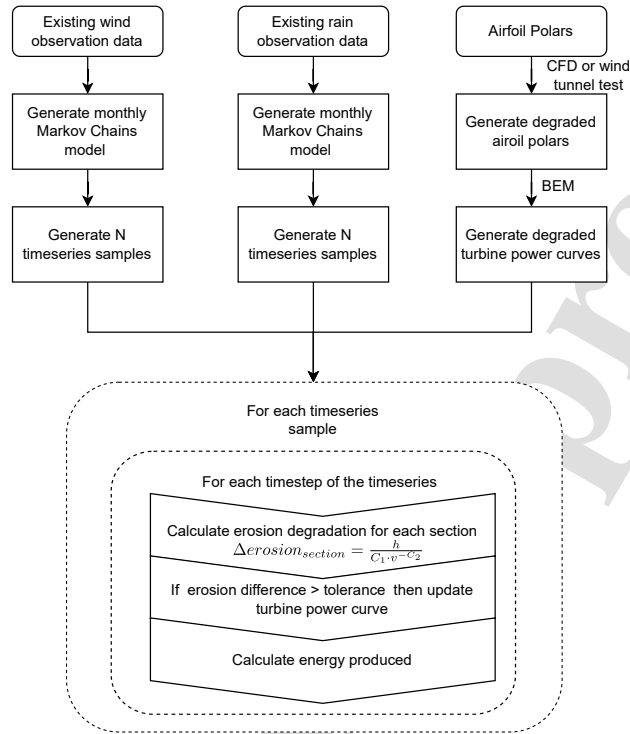


Figure 2: LEE calculation framework. Source: [24]

91 First, synthetic weather data needs to be generated for the location of the turbine. Rain intensity, wind  
 92 speed and significant wave height time series should be generated in order to compute damage degradation  
 93 and maintenance success rates. Depending on the availability of data for the project's location, various  
 94 approaches can be considered. If a considerable amount of observations is not available, data can then be  
 95 obtained from the ERA5 reanalysis data [25]. A Markov chains model [26] can then be used to generate  
 96 synthetic wind series as shown in [24]. Significant wave height is an important parameter to account for the  
 97 limitations in the logistics for offshore wind turbine maintenance activities. The generation of significant  
 98 wave height series should be dependent on wind speed. Different approaches can be used to achieve this  
 99 conditioned on data availability. In this case, an Artificial Neural Network (ANN) was used to mimic  
 100 the significant wave height,  $h_s$ , patterns registered by the FINO1 platform. The parameters of the neural  
 101 network used are the significant wave height of the two previous time steps, the wind speed of the current  
 102 and two previous time steps and the calendar month (to account for seasonality). The proposed ANN is  
 103 composed of a hidden layer of 4 neurons using the sigmoid activation function and an output layer with the  
 104 significant wave height value.

LEE is known to cause effects on the aerodynamic performance of wind turbine blades [18, 27–29], resulting in reduced lift and increased drag forces. These effects lead to a decrease in the power generated by the turbine. The estimated annual energy production losses can range from 1.5% to 10%, depending on the turbine’s characteristics and site-specific climatic conditions [27, 30–33]. Estimating changes in aerodynamic performance is a non-trivial task, often requiring the application of 2D and 3D Computational Fluid Dynamics (CFD) numerical models due to the limited availability of observational data [29, 34–36]. Once the blade’s performance at various levels of LEE degradation is determined, the degraded power curves of the turbine can be constructed. These curves are used to assess the energy losses of the turbine. The energy produced at each time step,  $\Delta E_i$ , is calculated using Equation 1, where  $P(u, d)$  represents the power obtained from the degraded power curves, and  $\Delta t$  is the computational time step. Energy losses due to LEE degradation are then estimated as the difference between the pristine and degraded power curves.

$$\Delta E_i = P(u, d) \cdot \Delta t \quad (1)$$

Considering the high uncertainty in the behaviour of various coating materials is essential because the agent needs to account for uncertain degradation dynamics. To address this, the proposed method leverages the inherent uncertainty found in the Whirling Arm Rain Erosion test Rig (WARER) results, as shown in Figure 3. In these tests, leading edge protection coatings are subjected to water droplet impacts until they reach their final degradation. By analysing the evolution of the coating’s degradation, the accumulated volume of water impacting the blade, and the velocity of the section being tested, curves showing the coating’s failure can be obtained, as illustrated in Figure 3. The curve fitting used in this case follows Equation 2.

$$H = C_1 \cdot v(r)^{-C_2} \quad (2)$$

being  $H$ , the accumulated rain impingement to erosion failure and  $C_1, C_2$  material parameters calibrated using experimental WARER test data for a specific protection system and  $v(r)$  the local rotor speed. For this study, damage evolution is assumed to be linear, as assumed in other relevant works related to LEE in the literature [20] and following the experimental behaviour reported by [37], and damage accumulation calculated using the Palmgren-Miner rule, Equation 3. In this work, damage has been accumulated using average 10-min wind speed and rain data. The study of the influence of more granular data has not been part of this study, but the authors believe that the granularity used in this study can be considered representative for the lifetime analysis of the turbines.

$$\Delta d = \frac{h_i}{C_1 \cdot v(r)^{-C_2}} \quad (3)$$

with  $h_i$  being the accumulated rain impingement during time-step  $i$ .

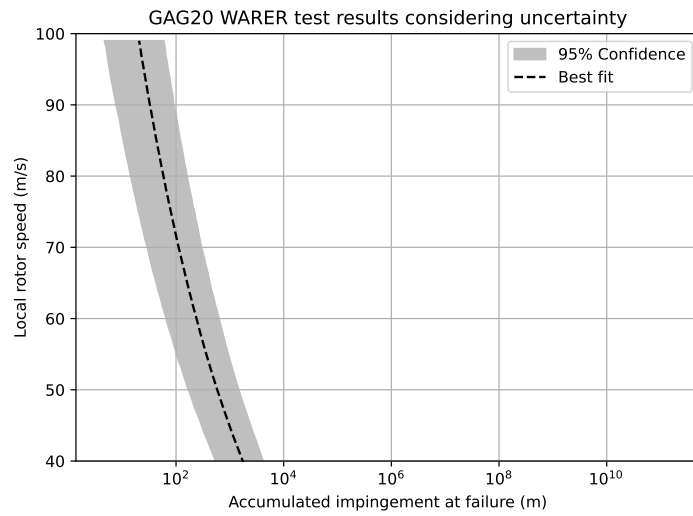
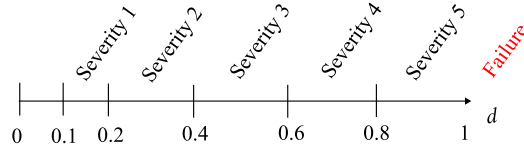


Figure 3: Accumulated impingement at failure for the GAG20 coating

133 In the literature, the evolution of LEE damage is typically described using a five-stage framework, which  
 134 is described in Table 1. In this study, a continuous damage parameter, denoted as  $d$ , is defined within the  
 135 interval  $[0,1]$ , allowing for the representation of the damage severity across these stages. Figure 4 illustrates  
 136 the mapping of these stages to the damage levels within the  $[0,1]$  range, providing a clear visualisation of  
 137 how different damage severity levels are associated with the stages of LEE damage evolution.

Table 1: LEE stages

Stage	Description
0	Incubation stage
1	Formation of minor pits
2	Growth of pits
3	Partial removal of topcoat
4	Total removal of topcoat and initiation of delaminations

Figure 4: Damage,  $d$ , assigned to different damage severity categories

138 The proposed framework operates on two different timescales: one for computational modelling (compu-  
 139 tational time step) and another for decision-making (decision time step). In this study, the computational  
 140 time step is set to 10 minutes, while the decision time-step is 1 calendar month. To mimic real-world condi-  
 141 tions, the agent operates without prior knowledge of the model but relies on observations. The agent's state  
 142 representation at each time step includes the parameters presented in Table 2.

Table 2: RL Agent state parameters

Parameter	Description	Range
Time from last maintenance, $t_{lm}$	Represents the last time a successful maintenance was performed	$\geq 0$
Time until decommissioning, $t_{td}$	Remaining time of the life of the turbine	$[0, 300]$
Estimated maximum damage, $D_{max}$	Maximum level of damage of the turbine as estimated through the model and updated through inspection data when available	$[0, 1]$
Current calendar month	Calendar month	$[1, 12]$
Average annual erosion rate, $a_d$	Prognostic feature for the agent representing the average annual erosion rate expected the turbine given the information available	$\geq 0$

143 At each decision step, the RL agent is presented with three possible actions: continue operating normally  
 144 with no maintenance activities, attempt inspection, and attempt repair. The variable  $D_{max}$  is updated  
 145 at each decision time step using the average annual erosion rate, unless new maintenance information is  
 146 acquired. When new maintenance data, denoted as  $D_{ins}$ , becomes available,  $D_{max}$  is updated using the  
 147 equation below:

$$D_{max} \rightarrow \frac{D_{max} + D_{ins}}{2} \quad (4)$$

148 The average annual erosion rate is initially set at 0.3, representing the average rate for the coating and  
 149 the specific study site. Whenever new inspection data becomes available,  $a_d$  is updated using a weighted

150 average, where the weights are proportional to the time between inspections. Greater weight is assigned to  
 151 inspection data collected over longer intervals.

## 152 2.2. Decision-making framework

153 The decision-making process is executed by an agent trained using Reinforcement Learning. In this con-  
 154 text, the agent is trained by interacting with the *environment*, receiving rewards and penalties to maximise  
 155 a *reward* signal  $R$ . The problem is framed as a Markov Decision Process (MDP). Using this formalism, at  
 156 each time step  $t$ , the agent receives some representation of the environment's *state*,  $S_t \in \mathcal{S}$ , and selects an  
 157 *action*,  $A_t \in \mathcal{A}(s)$ . In the subsequent time step, the agent receives a numerical *reward*,  $R_{t+1} \in \mathcal{R} \subset \mathbb{R}$  and  
 158 receives the representation of the new state of the environment,  $S_{t+1}$ . In an MDP, the dynamics of the  
 159 *environment* ( $S_t, R_t$ ) are entirely characterised by the dynamics function  $p(S, A)$  that depends only on the  
 160 immediately preceding state and action ( $S_{t-1}, A_{t-1}$ ).

$$161 \quad p(s', r | s, a) \doteq \Pr\{S_t = s', R_t = r | S_{t-1} = s, A_{t-1} = a\} \quad (5)$$

162 Therefore, the interaction between agent and environment in a finite MDP gives rise to a trajectory  
 163  $\{S_0, A_0\}, \{R_1, S_1, A_1\}, \dots, \{R_T, S_T, A_T\}$  being  $T$  the termination state. The flexibility of the MDP frame-  
 164 work makes it ideal for modelling O&M tasks, including the one addressed in this work. The final goal of  
 165 the agent in RL is the maximisation of the cumulative sum of rewards, referred to as *return*  $G_t$ , following  
 166 an action:

$$167 \quad G_t = R_{t+1} + \gamma R_{t+2} + \gamma^2 R_{t+3} + \dots = \sum_{k=t+1}^T \gamma^{k-t-1} R_k \quad (6)$$

168 being  $\gamma \in [0, 1]$  the discount factor used in continuous task problems, where  $T = \infty$ , to avoid the potential  
 169 issue of  $G_t$  approaching infinity. For finite episodic tasks,  $\gamma$  shall be taken as 1 to avoid suboptimal solutions  
 170 in the optimisation of  $G$ . However, reducing  $\gamma$  can aid in stabilising the training process and encourage riskier  
 171 decision-making [38]. By doing this, the agent increases the importance of the rewards and shorter time  
 172 horizons and can have a target with a lower variance. This can be of great importance in high uncertainty  
 173 scenarios such as the problem analysed in this work. To assess the preference for different actions in a given  
 174 state, the agent utilises *value functions* or *action-value functions*. The *action-value function* of a state  $s$   
 175 under a policy  $\pi$ , denoted  $q_\pi(s, a)$ , is defined as follows:

$$176 \quad q_\pi(s, a) \doteq \mathbb{E}_\pi[G_t | S_t = s, A_t = a] \quad (7)$$

177 The optimal value function  $q^*(s, a)$  provides the maximum values in all states and can be determined by  
 178 solving the Bellman equation:

$$179 \quad q^*(s, a) = \mathbb{E}[R(s, a) + \gamma \sum_{s'} P(s' | s, a) \max_{a'} q^*(s', a')] \quad (8)$$

180 the optimal policy  $\pi^*$  is then constructed by following:

$$181 \quad \pi^*(s) = \arg \max_a q^*(s, a) \quad (9)$$

182 To achieve the optimal policy, one of the strategies is to make use of the  $\varepsilon$ -greedy policy, which can be  
183 expressed as follows:

$$184 \quad A_t = \begin{cases} \arg \max_a q^*(s, a) & \text{with probability } 1 - \varepsilon \\ A \in \mathcal{A}(S_t) & \text{with probability } \varepsilon \end{cases} \quad (10)$$

185 where the agent balances the exploration,  $\arg \max_a q^*(s, a)$  with the exploration, *random* action, by utilising  
186 the exploration rate,  $\varepsilon \in [0, 1]$ . Typical approaches consider a decaying exploration rate over time to explore  
187 more intensively the state space frequented by the best-known policy to the agent. In this case, the update  
188 rule for the exploration is as follows:

$$189 \quad \varepsilon_i = \varepsilon_0 + (\varepsilon_f - \varepsilon_0) \cdot \frac{\min(i, f)}{f} \quad (11)$$

190 where  $i$  is the step,  $\varepsilon_0$  the initial learning rate, and  $\varepsilon_f$  the final learning rate. The values used were 0.6, 0.03  
191 and  $10^5$  for  $\varepsilon_0$ ,  $\varepsilon_f$  and  $f$ , respectively.

192 Given the nature of the problem at hand, Temporal Difference (TD) learning methods, in which the  
193 values are updated online based on the difference of temporally successive estimates, can be beneficial.  
194 In this case, the method chosen to solve the problem is *Q-learning* [39]. *Q-learning* is an off-policy TD  
195 method used to find the action-value function of the states to find the optimal or nearly optimal policy. To  
196 address this problem, Deep Q Networks (DQN) are used for function approximation. The value  $q(s, a)$  is  
197 approximated as  $\hat{q}_\pi(s, a, w) \approx q_\pi(s, a)$ , where  $w$  represents the set of weights for the DQN. This approach  
198 was chosen to improve the generalisation of the agent and better approach different regions of the state space  
199 given the continuous value of the damage state and the large state-action space of the problem. To use this  
200 method, two separate networks need to be kept, one called the online or behaviour network with weights  
201  $w$ , which is the one being updated every step, and the target network, which shares architecture with the  
202 first but has a different weight vector  $w^-$  that is updated less frequently. In the agent's design, the weight  
203 vector update frequency  $C$  is set to  $10^4$  steps (months). The adoption of this approach, along with the use  
204 of the experience replay buffer  $M$ , help break the correlation of the sequence and stabilise the training of  
205 the agent. Throughout the learning process, Q-learning updates are applied to minibatches extracted from  
206 the experience replay, following the equation below:

$$207 \quad w_{t+1} \leftarrow w_t + \alpha \frac{1}{N} \sum_{i=1}^N [R_i + \gamma \arg \max_{a_i} \hat{q}(s'_i, a'_i; w_t^-) - \hat{q}(s_i, a_i; w_t)] \cdot \nabla w \cdot \hat{q}(s_i, a_i; w_t) \quad (12)$$

208 where the subindex  $i$  is used to denote the sample in the batch,  $t$  is the time index at which the weights are  
209 updated and  $\nabla w$  the gradient of the weights. Here,  $\alpha$  represents the learning rate, and  $N$  is the number of

210 samples in the minibatch. The chosen size of the minibatch for the RL agent solving the LEE degradation  
 211 O&M optimisation problem is 128. The weights learnt by the agent approximate the optimal state-action  
 212 function  $q^*(s, a)$  regardless of the followed policy. Then, the agent can approximate the optimal policy  $\pi^*$   
 213 by choosing the action with the greatest state-action value:

$$214 \quad \widehat{\pi}^* = \arg \max_a \hat{q}^*(s, a; w) \approx \pi^* \quad (13)$$

215 The experiences from the replay buffer are not sampled uniformly but by a priority,  $P$ , assigned on its  
 216 importance, using what is termed as prioritised replay buffer [40]. When stored in the replay buffer, each  
 217 experience is assigned a priority based on its TD-error, creating what is termed a *prioritised replay buffer*  
 218 [40]. These priorities are then used to calculate a probability distribution for sampling, which has been  
 219 calculated as:

$$220 \quad p_k = \frac{P(k)^\alpha}{\sum_{j=1}^N P(j)^\alpha} \quad (14)$$

221 With  $\alpha$  as a parameter emphasising higher probabilities,  $p_k$  as the sampling probability of experience  $k$ ,  
 222 and  $N$  as the size of the experience replay buffer, sampling weights, denoted as  $w_s$ , are used to compensate  
 223 for the bias introduced by the sampling probability distribution. These weights are calculated using the  
 224 following expression:

$$225 \quad w_{s_k} = \left( \frac{1}{N} \cdot \frac{1}{P(k)} \right)^\beta \quad (15)$$

226 During the training of the agent, the loss calculated for each experience is weighted by  $w_s$  to increase  
 227 the importance of experiences with higher priorities. In this case, values of 0.6 and 0.4 were used for the  
 228 parameters  $\alpha$  and  $\beta$ , respectively.

229 The Deep Neural Network used is a fully connected network composed of three hidden layers with 300,  
 230 600, and 150 units, respectively, and it employs the *ReLU* activation function. The output layer provides  
 231 the state-action value,  $\hat{q}(s, a; w)$ , for each of the actions available for the agent. The activation function for  
 232 the output layer is linear, allowing the network to provide negative q-values, as expected for the rewards  
 233 of the environment. The optimisation algorithm chosen for training the network is ADAM [41], using a  
 234 fixed learning rate,  $\alpha$ , of 0.0001. The reward function defined for this problem is shown in Equation 16.  
 235 The reward is composed of 3 terms, the aerodynamic losses,  $C_{aero}$ , the maintenance costs,  $C_{om}$ , and the  
 236 downtime costs,  $C_{dt}$ .  $C_{aero}$  is computed as the difference in production between the original and the eroded  
 237 power curves of the turbine,  $C_{om}$  using the costs provided in Table 3 and  $C_{dt}$  as energy lost during downtime.  
 238 Maintenance costs are obtained following the procedure depicted in Figure 5. This function is defined to  
 239 produce rewards  $\leq 0$  for which a zero initialisation of Q-values will encourage exploration. The algorithm  
 240 outlining the training of the RL agent is depicted in Figure 6 and outlined in Algorithm 1.

$$241 \quad R_i = C_{aero} - C_{om} - C_{dt} \quad (16)$$

Table 3: Repair costs per damage severity - 3 blades. Data obtained from [42] and [43].  $m_b$ ,  $m_a$  and  $m_e$  are the booking, access and execution costs, respectively.

Damage severity	$m_b$ (£)	$m_a$ (£)	$m_e$ (£)
0 (Inspection)	1,600	1,000	3,200
1	2,000	1,000	4,000
2	2,000	1,000	4,000
3	3,000	1,000	6,000
4	5,000	1,000	36,000
5	0	250,000	3,500,000
6	0	250,000	5,000,000

Table 4: Weather repair constraints.

Damage category	Logistic requirements	Duration (h)	Max. significant wave height (m)	Max 10-min avg. wind speed (m/s)
1: LE discoloration, paint or bugs	CTV, rope access	6	1.5	11
2: Coat/paint damage, surface: Missing less than 10 cm <sup>2</sup>	CTV, rope access	15	1.5	11
3: Coat/paint damage, surface: Missing more than 10 cm <sup>2</sup>				
Damaged leading edge protection	CTV, rope access	18	1.5	11
Damaged leading edge tape				
LE erosion, down to laminate				
4: LE erosion, down to laminate and first layer laminate	CTV, crawler platform	40	1.5	12
5: LE erosion, through laminate / Open LE	HLV, blade disassembly	72	1.8	10
6: LE erosion, blade failure	HLV, blade disassembly	72	1.8	10



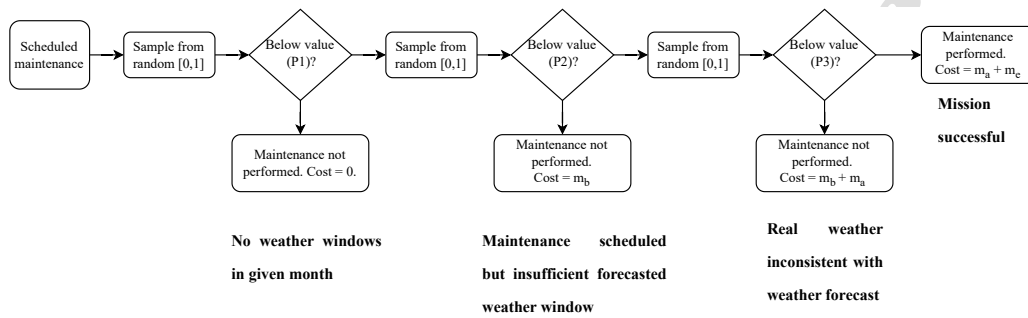


Figure 5: Repair modelling.

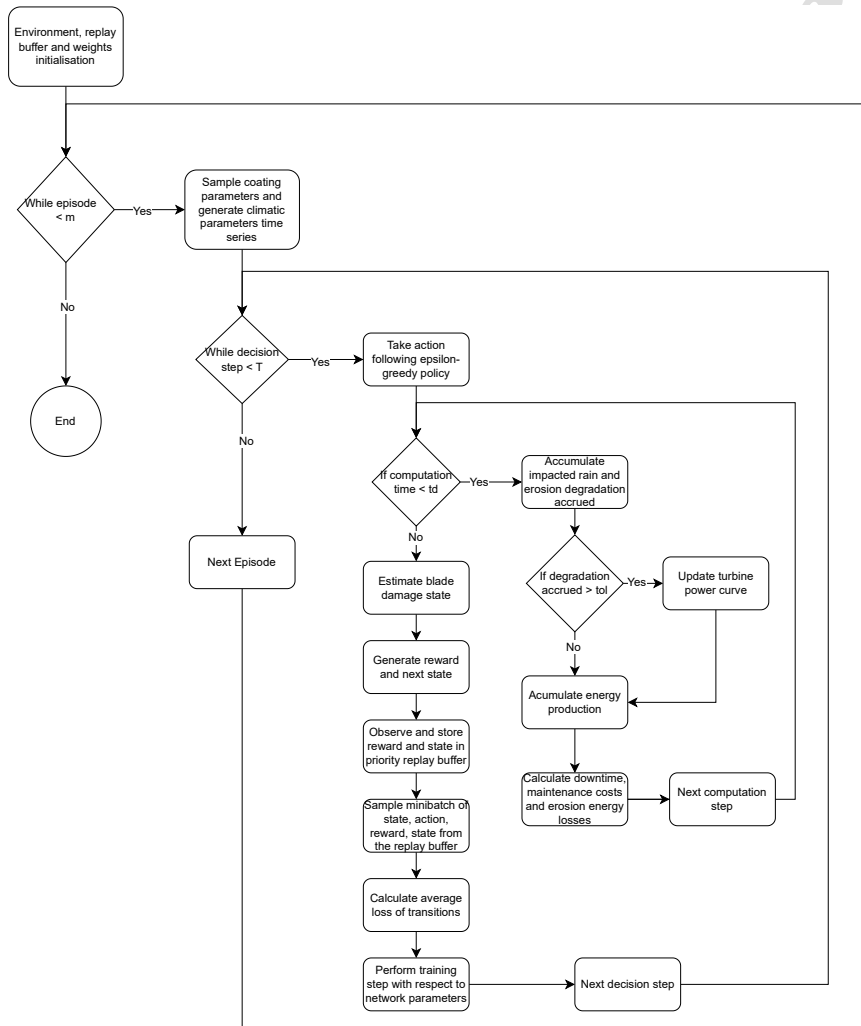


Figure 6: Leading edge erosion RL algorithm flowchart

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**Algorithm 1** Deep Q-learning for wind turbine blade LEE O&M optimisation with experience replay buffer

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- 1: Initialise priority replay buffer  $M$  to capacity  $N$
  - 2: Initialise action-value function  $\hat{q}$  with random weights  $w$
  - 3: Initialise action-value function  $\hat{q}$  for target network with weights  $w^- = w$
  - 4: Environment initialisation  $\triangleright$  Wind turbine definition, Blade degradation power curves, weather data, maintenance success probabilities
  - 5: Generate  $k$  transitions to pre-fill  $M$  using a random policy
  - 6: **for** episode = 1,  $m$  **do**
  - 7:   Reset environment,  $s = s_0$
  - 8:   Generate random material coating parameters  $C_1, C_2$  and weather scenarios  $I(t), u(t)$ .
  - 9:   **for** decision step  $t_d = 1, T$  **do**
  - 10:     With probability  $\varepsilon$  select a random action  $a_t$
  - 11:     otherwise select  $a_{t_d} = \arg \max_a \hat{q}^*(s, a; w)$
  - 12:     execute action  $a_{t_d}$
  - 13:     **while** computation time  $t_c \leq t_d$  **do**
  - 14:       Accumulate impacted rain.
  - 15:       Calculate real erosion degradation accrued,  $\Delta d$ .
  - 16:       **if**  $\Delta d \geq tol$  **then**
  - 17:         Update turbine power curve due to erosion degradation.
  - 18:         Accumulate energy production,  $\Delta E$ .
  - 19:         Calculate downtime and maintenance costs  $C_{dt}$  and  $C_{om}$ .
  - 20:         Calculate erosion energy losses.
  - 21:     Estimate blade damage state,  $D_{max}$
  - 22:     Generate reward  $r_{t_d+1}$  and next state  $s_{t_d+1}$
  - 23:     Observe  $r_{t_d+1}$  and  $s_{t_d+1}$
  - 24:     Store transition  $(s_{t_d}, a_{t_d}, r_{t_d+1}, s_{t_d+1})$  in  $M$
  - 25:     Sample minibatch of transitions  $(s_j, a_j, r_{j+1}, s_{j+1})$  from  $M$
  - 26:     Calculate average loss of transitions
  - 27:     Perform training step with respect to network parameters  $w$
  - 28:     Every  $C$  steps reset  $w^- = w$
- 

242 **3. O&M considerations**

243 For the O&M simulations, the following assumptions were considered:

- 244 • Only the O&M costs related to blade damage due to LEE are considered in this study; no other failure  
245 modes are taken into account.
- 246 • Turbine operation is assumed to commence at the beginning of January.
- 247 • Imperfect repairs are considered, where the true damage state of each calculation point, denoted as  $d$ ,  
248 is set to a value drawn from a Gaussian distribution with  $d \sim \mathcal{N}(\mu, \sigma^2)$ , where  $\mu = 0.05$  and  $\sigma = 0.001$ ,  
249 and truncated at the interval  $[0, 1]$ .
- 250 • Imperfect inspections are also considered, with inspected damage denoted as  $D_{ins}$ . Inspected damage  
251 follows a Gaussian distribution with parameters  $\mu = d$  and  $\sigma = 0.1$ , truncated within the interval  
252  $[0, 1]$ .
- 253 • If any real damage calculation point on the blade reaches  $d = 1$ , the turbine will be preventively  
254 stopped until it undergoes repair or replacement. This study assumes that when the blade reaches this  
255 degradation level, alarms from other systems such as SCADA will trigger the preventive shutdown.
- 256 • An energy cost of 50 GBP/MWh is considered, in line with the Contracts for Difference (CfD) strike  
257 price signed for CfD4 in the UK in 2022.
- 258 • Probabilistic definitions of repair success are discredited by month to mimic real O&M scheduling. The  
259 associated cost of a repair is a function of the damage and the month when the repair is attempted.
- 260 • For condition-based maintenance strategies, referred to as  $AC$ , repairs are attempted upon reaching  
261 an estimated damage,  $D$ , above a specified damage threshold.
- 262 • Energy production losses resulting from reduced aerodynamic performance of the blade due to erosion  
263 are considered, following the calculation framework outlined in [24] and summarised in this study.
- 264 • Energy production losses stemming from downtime and preventive stops are also taken into account.
- 265 • Maintenance costs are as specified in Table 3.
- 266 • Inspections are mandated for all maintenance strategies during the early operation phase of the turbine,  
267 specifically during months 3 to 6, to ensure more stable results that closely resemble real-life operations.
- 268 • For this study, inspection costs used were assumed as a deterministic values. Notwithstanding, the  
269 proposed framework can accommodate a probabilistic description of inspection costs for different  
270 damage levels or inspection techniques.

271 This study models the maintenance success rate for a maintenance mission in three sequential steps as  
272 shown in Figure 5. First, it considers the probability of a given month to have wind and significant wave

273 height values below the threshold, denoted as  $P_1$ . Second, it evaluates the probability of the forecasted  
274 weather complying with a required weather window, known as  $P_2$ . Finally, it assesses the probability of  
275 the actual weather matching the weather predictions, labelled as  $P_3$ . The weather constraints for different  
276 maintenance methods and the required weather windows are provided in Tables 4 and 3. Synthetic weather  
277 data generation techniques, as described earlier, are used to obtain values for  $P_1$  and  $P_2$ . In the absence of  
278 data, real weather is assumed to deviate from the forecast with increasing uncertainty. For the calculation  
279 of  $P_3$  values, a Gaussian distribution is employed, centred on the forecast value, with a standard deviation  
280 increasing by 4% daily.

#### 281 4. Case studies

282 To assess the effectiveness of the proposed framework, two case studies were conducted. Both cases share  
283 the same location and turbine model but differ in terms of maintenance success probabilities. In Case 2,  
284 there is a lower maintenance success rate and a more pronounced seasonal influence, resulting in a higher  
285 difference between the success rates during spring-summer and autumn-winter months. These probabilities  
286 are presented in Appendix A.

287 For these cases, the O&M costs related to leading-edge erosion were analysed under condition-based  
288 maintenance policies,  $AC$ , and the policies generated by the RL agents. Two  $AC$  policies were selected as  
289 baselines for comparison with the performance of RL agents:  $AC\ 0.4$  and  $AC\ 0.3$ . These  $AC$  policies initiate  
290 maintenance when the blade reaches 0.4 and 0.3  $D_{max}$ , respectively. The results are analysed and compared  
291 in terms of several aspects, including the average estimated damage throughout the turbine's lifetime, the  
292 estimated damage when maintenance is attempted, the evolution of the frequency of maintenance activities  
293 over time, the average time between maintenance actions in relation to the estimated annual damage rate,  
294 repair frequency per calendar month and the percentage of O&M actions taken. Finally, a thorough cost  
295 analysis based on a number of cost metrics is shown to compare the analysed policies.

296 Both case studies are situated at the FINO1 platform, located 45 km off the coast of Germany. The  
297 5MW NREL offshore wind turbine serves as the model for simulating these scenarios, with its characteristics  
298 detailed in Table 5.

Table 5: 5 MW NREL Turbine data. Data extracted from [44]

Property	Value
Rated power	5 MW
Control	Variable speed, collective pitch
Drivetrain	High speed, multiple-stage gearbox
Rotor diameter	126 m
Hub height	90 m
Cut-In / Rated / Cut-out wind speed	3 m/s / 11.4 m/s / 25 m/s
Cut-in / Rated rotor speed	6.9 rpm, 12.1 rpm
Rated tip speed	80 m/s

299 For these case studies, a training period of  $10^6$  months was employed for training the RL agents. Simu-  
 300 lations were conducted using  $\gamma$  values ranging from 0.95 to 1 at intervals of 0.01. The two best-performing  
 301 agents are compared with condition-based maintenance strategies featuring damage repair thresholds of 0.3  
 302 and 0.4.

303 Both condition-based and RL maintenance strategies utilised updates in the estimated maximum damage,  
 304  $D_{max}$ , and the average annual erosion rate,  $a_d$ , to estimate the blade's condition. To evaluate the results of  
 305 the various O&M strategies, 5,000 simulations spanning 25 years each were performed.

306 When assessing risk, the expected O&M cost value must be supplemented with additional metrics. There-  
 307 fore, the policies will be compared based on the following metrics: Conditional Value at Risk ( $CVaR_{0.95}$ ),  
 308 which represents the average of values above the 95th percentile; the median; the expected cost (mean); and  
 309 Value at Risk ( $VaR_{0.95}$ ).

#### 310 4.1. Case study 1

311 In this case, the maintenance success probabilities shown in were derived from direct simulation con-  
 312 sidering the weather repair constraints shown in Tables A.1 to A.3 and the synthetic weather generation  
 313 explained under section 2.1.

314 In this subsection, we present and analyse the results of Case Study 1. Figure 7 provides a summary of the  
 315 most relevant aspects of the different policies. Figure 7a illustrates the evolution of the average maximum  
 316 blade LEE damage over time. At the start of the operation, the 90<sup>th</sup> percentile damage approaches the  
 317 damage threshold of AC strategies. The periodic waviness in the data series is attributed to the seasonality  
 318 of maintenance success probability, with a period of 12 months, and the distinct strategies employed for  
 319 maintenance scheduling. AC strategies exhibit a more regular damage pattern compared to RL strategies.

320 It's worth noting that RL strategies tend to utilise most of the LEE's lifespan before decommissioning. This  
 321 tendency is more pronounced in the case of the *RL CS1*  $\gamma = 0.98$  RL agent.

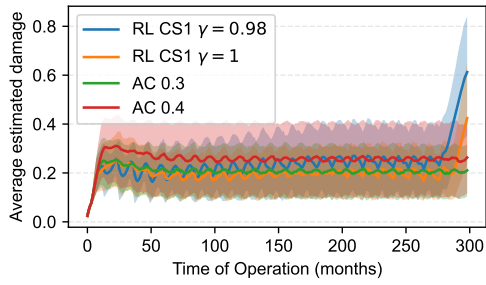
322 Figure 7b displays the distribution of  $D_{max}$  for the maintenance attempts of the different strategies. *AC*  
 323 strategies follow an exponential-like distribution with peaks at their respective damage thresholds (0.3 and  
 324 0.4), which decrease with the success of maintenance activities. Conversely, the RL agents employ different  
 325 strategies. *RL CS1*  $\gamma = 1$  demonstrates a Gaussian distribution with a mean of 0.3, while *RL CS1*  $\gamma = 0.98$   
 326 shows a wider Gaussian-like distribution with a mean around 0.35.

327 The frequency of attempted repair activities over the turbine's service life is presented in Figure 7c.  
 328 *AC* strategies maintain a constant maintenance rate throughout the turbine's life, whereas *RL* strategies  
 329 tend to accumulate more maintenance activities at the beginning of their service life and reduce them as  
 330 decommissioning approaches. This trend is more pronounced in the *RL CS1*  $\gamma = 0.98$  policy but is also  
 331 evident in the *RL CS1*  $\gamma = 1$  policy.

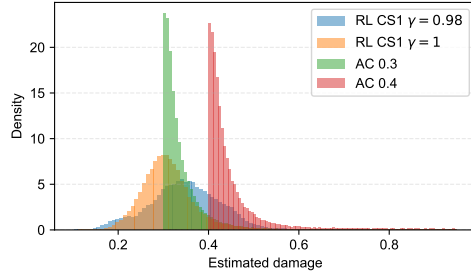
332 Figure 7d illustrates the average time between maintenance actions for the different policies analysed.  
 333 *AC 0.4* shows the longest time between maintenance actions for all values of  $a_d$ . As expected, the time  
 334 between maintenance actions for this policy is greater than *AC 0.3*. RL agents adopt different approaches,  
 335 with *RL CS1*  $\gamma = 0.98$  being closer to *AC 0.3*, while *RL CS1*  $\gamma = 1$  follows a safer strategy for  $a_d \leq 0.4$ .

336 Figure 7e provides insights into the planning of maintenance activities by calendar month. It's important  
 337 to note that this graph displays all maintenance attempts, not just the successful ones. *AC* policies show a  
 338 curve with lower values in the months of April to October, with similar shapes and values. This is because  
 339 maintenance success probabilities are higher during those months, reducing the need for maintenance actions  
 340 in the coming months. In contrast, *RL* policies exhibit a different behavior, with a significant increase in  
 341 maintenance planning intentions for the period from October to February. RL agents have learned the  
 342 benefit of anticipating maintenance, as failure to do so would lead to an increase in the blade's damage state  
 343 and higher maintenance costs. RL policies adopt a more conservative approach in this regard compared to  
 344 *AC* policies.

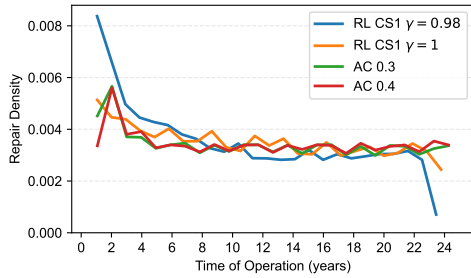
345 Finally, Figure 7f presents the percentage of different actions taken. Given that *AC 0.4* has a higher  
 346 damage repair threshold, it's expected that the 'operate' action is more frequent (85.29% of months) com-  
 347 pared to *AC 0.3* (82.77%). The fixed inspections scheduled for all policies remain at 1.34%, with RL agents  
 348 showing a marginal increase in the use of inspections (2.00% and 2.22% for *RL CS1*  $\gamma = 1$  and *RL CS1*  
 349  $\gamma = 0.98$ , respectively). *RL CS1*  $\gamma = 1$  employs the highest maintenance intention rate (16.98%), while *RL*  
 350 *CS1*  $\gamma = 0.98$  adopts a rate of 14.98%, falling between *AC 0.3* and *AC 0.4*.



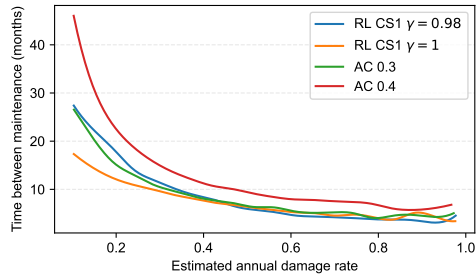
(a) Evolution of maximum estimated damage,  $D_{max}$  vs time of operation. The shadowed regions represent the 10-90 percentile band



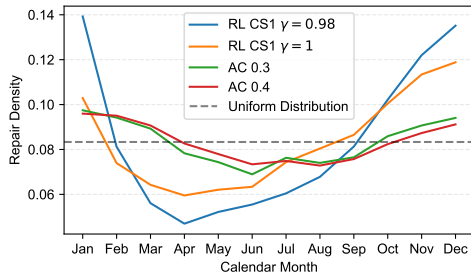
(b) Distribution of attempted repairs by estimated damage. *AC* policies have a fixed threshold while *RL* policies are left free to modify it to optimise expected O&M costs



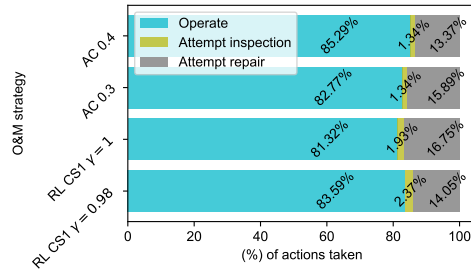
(c) Evolution of attempted repairs over the years of operation. *AC* policies have a fixed policy with forced inspections at the beginning of operation



(d) Average time between maintenance actions vs estimated annual damage rate,  $a_d$



(e) Repair attempt frequency over calendar months. The dashed line represents the uniform maintenance planning distribution



(f) O&M actions taken by the policies

Figure 7: Case study 1 O&M policy analysis

351 Figures 8 and 9 display the distribution of the O&M cost for the evaluated O&M maintenance policies,  
 352 while Table 6 presents various cost metrics compared to the baseline policy *AC 0.3*. Concerning cost  
 353 distribution, *AC 0.4* exhibits a higher number of values at the lower end of the cost spectrum. This can be



354 attributed to the fixed policy of *AC 0.4*, which entails some risk to the blade's condition but proves effective  
 355 for scenarios involving slow damage growth.

356 In contrast, both *AC 0.3* and *RL CS1*  $\gamma = 0.98$  show similar cost distributions, with a slight advantage  
 357 in median values observed for *RL CS1*  $\gamma = 0.98$ . On the other hand, *RL CS1*  $\gamma = 1$  outperforms in terms of  
 358 the average,  $CVaR_{0.95}$ , and  $VaR_{0.95}$  values. It presents reductions of 21.4%, 46.1%, and 8.7%, respectively,  
 359 when compared to the *AC 0.3* policy, along with a marginal increase in the median value (8.5%).

360 *RL CS1*  $\gamma = 0.98$  closely resembles the behavior of *AC 0.3* by achieving a 5% reduction in median cost,  
 361 with slight increases observed in the  $CVaR_{0.95}$  and  $VaR_{0.95}$  values. Conversely, *AC 0.4* displays a 12.1%  
 362 reduction in the median value but experiences significant increases in the remaining metrics.

Table 6: Cost metrics for Case study 1

Label	Median	Average	$CVaR_{0.95}$	$VaR_{0.95}$
<i>RL CS1</i> $\gamma = 0.98$	95.0%	100.7%	102.4%	105.4%
<i>RL CS1</i> $\gamma = 1$	108.5%	78.6%	53.9%	91.3%
<i>AC 0.3</i>	100.0%	100.0%	100.0%	100.0%
<i>AC 0.4</i>	87.9%	192.0%	273.2%	432.8%

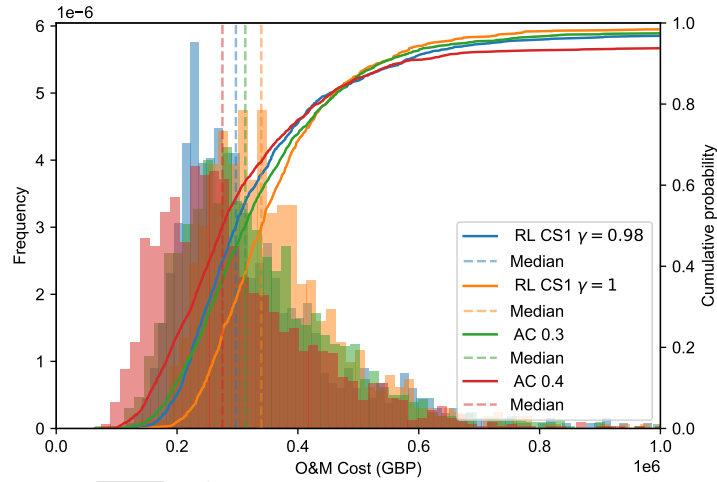


Figure 8: O&M cost distribution of the CS1 policies analysed. The dashed lines represent the median of the distribution. The right axis shows the cumulative probability of the distribution

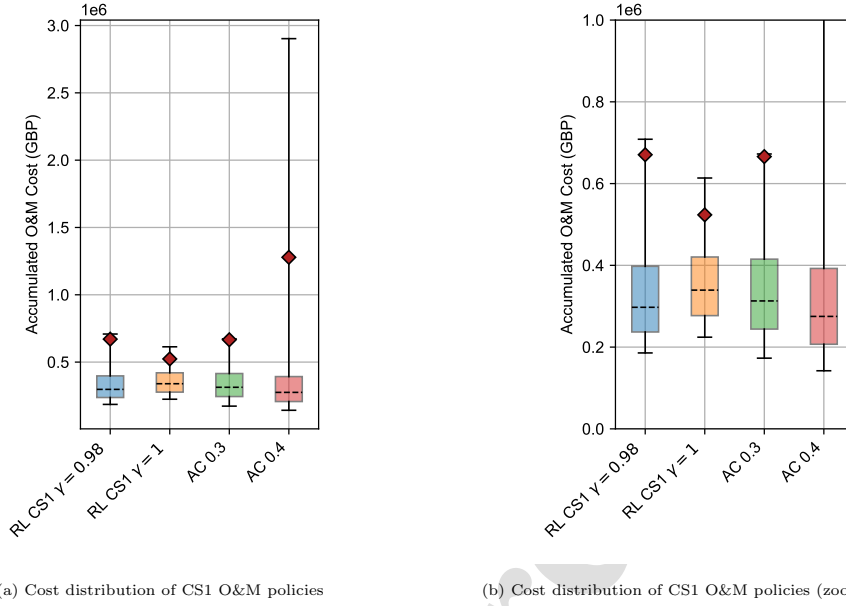


Figure 9: Cost distribution of CS1 O&M policies. The minimum and maximum values of the whiskers represent P5 and P95, respectively and the red marker the average cost. The right plot is a zoomed in version of the one on the left.

#### 363 4.2. Case study 2

364 In this case, the same location, turbine and costs are assumed with the main difference being the  
 365 maintenance success probabilities which have been modified to show a greater seasonal influence and a lower  
 366 maintenance success rate to assess the robustness of the proposed agent under more difficult conditions.  
 367 The probabilities used are shown in Tables A.4 to A.6.

368 In this subsection, we present and analyse the results of case study 2. Figure 10 summarises the most  
 369 relevant aspects of the different policies. Figure 10a illustrates the evolution of the average maximum blade  
 370 LEE damage over the turbine's operational period. During the turbine's operation, the 90th percentile  
 371 damage increases above the thresholds of the AC strategies, reaching 0.47 for AC 0.4 and 0.39 for AC  
 372 0.3. The wavy pattern in the data series is attributed to the seasonality of maintenance success probability,  
 373 exhibiting a periodic behaviour with a 12-month cycle, and the distinct strategies in maintenance scheduling.  
 374 While AC strategies demonstrate a similar regularity in the damage pattern compared to RL strategies, the  
 375 last 50 months of operation show a noticeable difference. RL strategies tend to make more extensive use  
 376 of the blade's leading-edge erosion resistance before decommissioning. This trend is managed differently by  
 377 RL CS2  $\gamma = 0.98$  and RL CS2  $\gamma = 0.99$ , with the agent having  $\gamma = 0.98$  progressively reducing the average  
 378 damage.

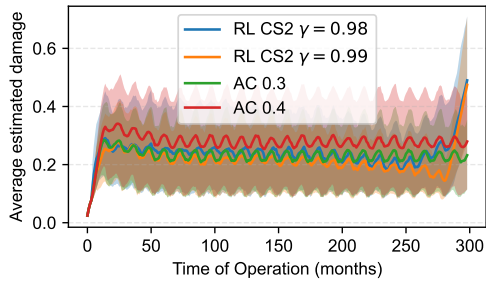
379 Figure 10b presents the distribution of  $D_{max}$  for the maintenance attempts of various strategies. *AC*  
 380 strategies exhibit an exponential-like distribution with peaks at their respective damage thresholds (0.3 and  
 381 0.4), which decrease with the success of maintenance activities. In contrast, the RL agents adopt different  
 382 strategies. *RL CS2*  $\gamma = 0.99$  showcases a Gaussian-shaped distribution with a mean around 0.3, while *RL*  
 383 *CS2*  $\gamma = 0.98$  displays a more skewed distribution, peaking around 0.4.

384 The frequency of attempted repair activities over the turbine's service life is shown in Figure 10c. *AC*  
 385 strategies maintain a consistent maintenance rate throughout the turbine's life, whereas RL strategies aim  
 386 to reduce repair activities as the turbine approaches the end of its operational life. Both RL strategies  
 387 exhibit a peak in maintenance activities during the final years, with year 23 for *RL CS2*  $\gamma = 0.99$  and years  
 388 20-21 for *RL CS2*  $\gamma = 0.98$ .

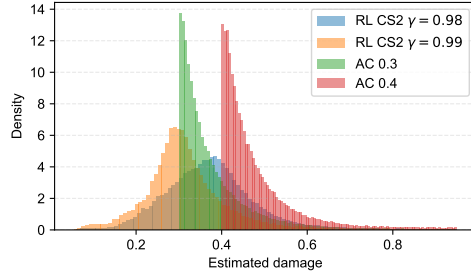
389 Figure 10d displays the average time between maintenance actions for the different policies analysed.  
 390 *AC 0.4* shows the longest intervals between maintenance actions for all  $a_d$ . As expected, the time between  
 391 maintenance actions in this policy is greater than that of *AC 0.3*. RL agents follow distinct policies, with *RL*  
 392 *CS2*  $\gamma = 0.98$  resembling the approach of *AC 0.3*, while *RL CS2*  $\gamma = 0.99$  adopts a more cautious strategy  
 393 for  $a_d \leq 0.4$ . However, *RL CS2*  $\gamma = 0.99$  appears to face generalisation issues for  $0.8 \leq a_d \leq 1.0$ .

394 Figure 10e provides insight into maintenance planning by calendar month. Notably, this graph illustrates  
 395 all maintenance attempts, not just the successful ones. *AC* policies and *RL CS2*  $\gamma = 0.99$  exhibit a similar  
 396 curve with lower values during the months from April to October. This behaviour aligns with higher  
 397 maintenance success probabilities in those months, reducing the need for maintenance actions in the coming  
 398 months. In contrast, the *RL CS2*  $\gamma = 0.98$  policy deviates from this pattern, displaying a pronounced  
 399 increase in maintenance planning from October to December.

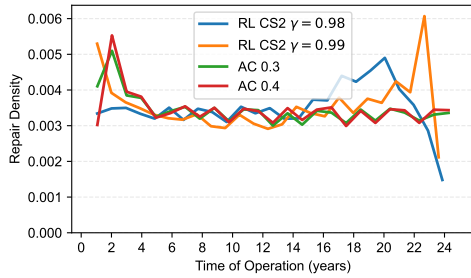
400 Lastly, Figure 10f presents the percentage of different actions taken. As *AC 0.4* has a higher damage  
 401 repair threshold, it is unsurprising that the "operate" action is more prevalent (77.37% of months) compared  
 402 to *AC 0.3* (73.23%). Fixed inspections are scheduled for all policies at a rate of 1.34%, with RL agents  
 403 demonstrating an increase in inspection usage, particularly *RL CS2*  $\gamma = 0.98$  (13.3%) compared to *RL CS2*  
 404  $\gamma = 0.99$  (5.61%). Furthermore, *RL CS2*  $\gamma = 0.99$  exhibits a slightly higher repair intention rate than *AC*  
 405 *0.3* (25.95% vs. 25.44%), and *RL CS2*  $\gamma = 0.98$  adopts a repair attempt rate of 23.12%, positioning it  
 406 between *AC 0.3* and *AC 0.4*.



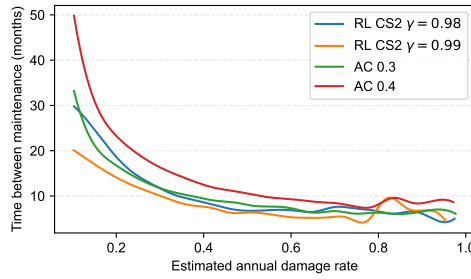
(a) Evolution of maximum estimated damage,  $D_{max}$  vs time of operation. The shadowed regions represent the 10-90 percentile band



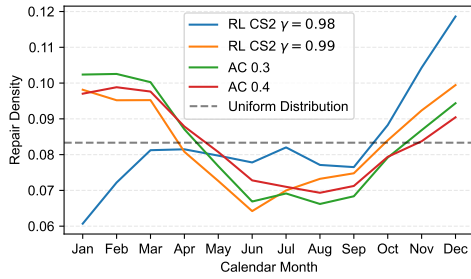
(b) Distribution of attempted repairs by estimated damage. *AC* policies have a fixed threshold while *RL* policies are left free to modify it to optimise expected O&M costs



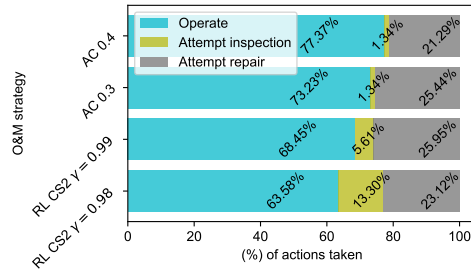
(c) Evolution of attempted repairs over the years of operation. *AC* policies have a fixed policy with forced inspections at the beginning of operation



(d) Average time between maintenance actions vs estimated annual damage rate,  $a_d$



(e) Repair attempt frequency over calendar months. The dashed line represents the uniform maintenance planning distribution



(f) O&M actions taken by the policies

Figure 10: Case study 2 O&M policy analysis

407 Figures 11 and 12 display the distribution of O&M costs for the evaluated O&M maintenance policies, and  
 408 Table 7 presents various cost metrics compared to the baseline policy, *AC 0.3*. Regarding cost distribution,  
 409 *AC 0.4* has more values in the lower end, which can be attributed to the fixed policy of *AC 0.4* taking

risks with the blade's condition and being successful for slowly growing damage cases. *AC 0.3* reaches a higher cumulative probability (0.91) at £1.5 million than *AC 0.4* (0.88), while higher values are achieved by RL policies, specifically *RL CS2*  $\gamma = 0.98$  (0.948) and  $\gamma = 0.99$  (0.95). In terms of cost metrics, *RL CS2*  $\gamma = 0.98$  and  $\gamma = 0.99$  outperform *AC 0.3*, with reductions in the range of 12-13%, 16-19%, and 73-78% for Average,  $CVaR_{0.95}$ , and  $VaR_{0.95}$ , respectively. They also exhibit a slight increase in the median value (11.5% and 6.2%, respectively). In contrast, *AC 0.4* shows a 6.2% reduction in the median value but experiences significant increases in the other metrics.

Table 7: Cost metrics for Case study 2

Label	Median	Average	$CVaR_{0.95}$	$VaR_{0.95}$
<i>RL CS2</i> $\gamma = 0.98$	111.5%	86.8%	80.9%	26.9%
<i>RL CS2</i> $\gamma = 0.99$	106.2%	87.3%	84.0%	21.7%
<i>AC 0.3</i>	100.0%	100.0%	100.0%	100.0%
<i>AC 0.4</i>	93.8%	159.4%	154.4%	308.5%

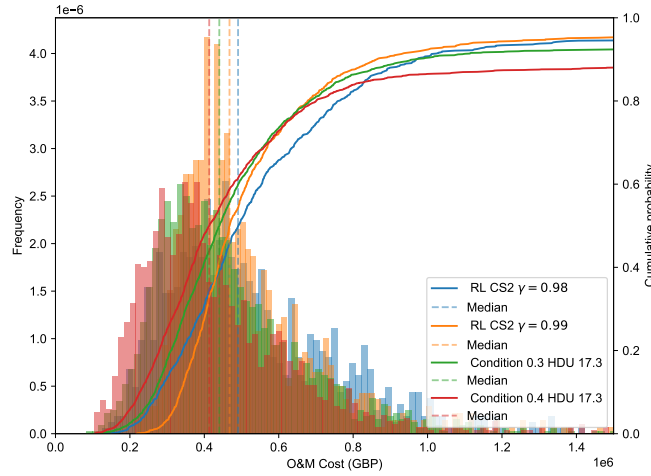


Figure 11: O&M cost distribution of the CS2 policies analysed. The dashed lines represent the median of the distribution. The right axis shows the cumulative probability of the distribution

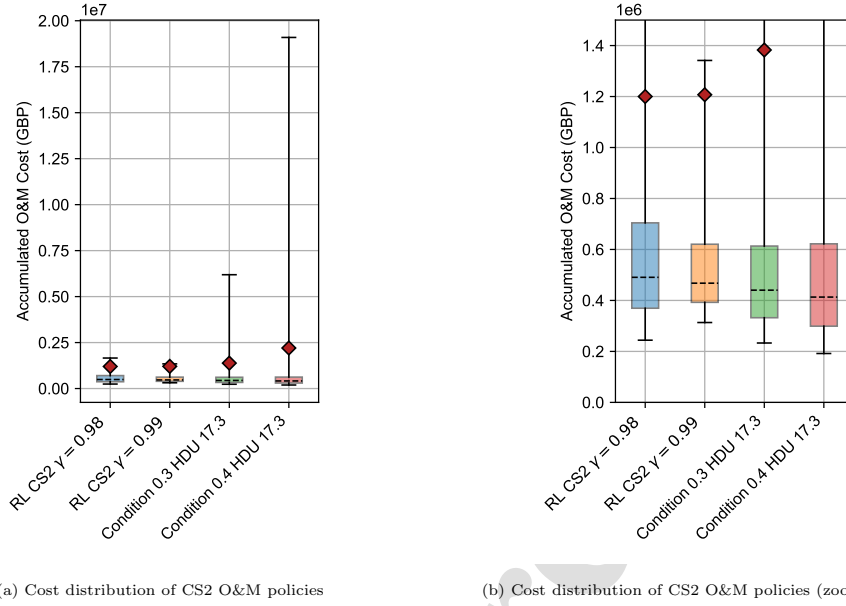


Figure 12: Cost distribution of CS2 O&M policies. The minimum and maximum values of the whiskers represent P5 and P95, respectively and the red marker the average cost. The right plot is a zoomed in version of the one on the left.

## 417 5. Discussion

418 The analysis of both case studies has led us to the conclusion that RL agents have been able to improve  
 419 the target metric of the optimisation, which is the expected value of the O&M cost, within a certain range.  
 420 In the case of CS1, with maintenance probabilities based on site-specific weather constraints, the reduction in  
 421 expected (average) O&M costs was 21.4% when compared with the baseline AC 0.3 condition-based policy.  
 422 Alongside the reduction in average costs, there was also a decrease in several relevant cost metrics related to  
 423 risk-based decision-making, such as  $CVaR_{0.95}$  and  $VaR_{0.95}$  with values of 46.1% and 8.7%, respectively. The  
 424 same trend was observed in CS2, an environment that has a greater uncertainty in the repair success derived  
 425 from harsher climatic conditions, with reductions of 13.2%, 19.1% and 73.1% for the average,  $CVaR_{0.95}$  and  
 426  $VaR_{0.95}$  O&M costs. A considerable  $VaR_{0.95}$  reduction is provided by the RL agent for CS2, highlighting  
 427 the importance of predictive maintenance in cases of reduced maintenance accessibility of offshore assets.  
 428 This expected cost reduction comes with an increase in the median cost, making the condition-based policies  
 429 (AC) more cost-efficient in some cases. Additionally,  $\gamma$  values between 0.98 and 1.0 have proven to be the  
 430 most effective in achieving this reduction. Overall, RL agents have successfully identified a cost advantage  
 431 by reducing maintenance activities towards the end of the turbines' operational life. The use of inspections

432 by RL agents has increased as maintenance success rates decreased; the inspection intention rate grew from  
 433 2.0% in CS1 to a range of 5-13% in CS2, explaining the importance of a reduced uncertainty of the damage  
 434 state for low accessibility sites. Regarding maintenance planning by calendar month, RL agents did not  
 435 provide a clear indication of a single planning strategy, which would require further investigation towards  
 436 potential convergence issues.

437 The presented framework has proven to be effective in high-uncertainty scenarios, with the material pa-  
 438 rameters  $C_1$  and  $C_2$  having the greatest influence on the degradation dynamics. This information is valuable  
 439 for the initial planning of the O&M of the turbine. To reduce the uncertainty in the degradation dynamics,  
 440 the probabilistic description of the abovementioned parameters can be modified once real operation data be-  
 441 comes available to improve the performance of the agent. Unfortunately, the modification of the description  
 442 of the stochastic variables requires the retraining of the agent, which can be time-consuming.

443 This framework can be used by operators at the early O&M design stage at the wind farm level. By  
 444 analysing the behaviour of the best agents, important qualitative metrics can be extracted to define global  
 445 policies such as the damage threshold for optimal maintenance scheduling for a particular failure mode if  
 446 considered alone. If combined with additional components and failure modes, this framework can provide  
 447 O&M policies at the wind turbine level. In this study, only the leading-edge erosion failure mode of the  
 448 blade was considered. Nevertheless, it can be extended to accommodate different failure modes as long as  
 449 a degradation function can be defined. This would require the inclusion of, at least, two parameters for the  
 450 DQN per failure mode. One of the parameters would be the estimation of the state of the component and  
 451 failure mode, and the other a prognostic parameter to improve the O&M planning of the agent. The selection  
 452 of the failure modes to consider should be based on risk priority to provide efficiency to the framework.

453 In this study, material parameters  $C_1$  and  $C_2$  have been assumed to remain constant throughout the life of  
 454 the turbine. It is important to note that there are many types of repair available (protection tapes, protective  
 455 coatings, and epoxy or polyurethane fillers) the durability of which is not well known yet. An interesting  
 456 opportunity to overcome this issue would be the inclusion of SHM in the turbine to provide timely inspection  
 457 data. Moreover, this would reduce the cost of inspection data for low-accessibility sites, which has proven to  
 458 be determinant for O&M for cost reduction. Also, there is potential for improvement in the quantification  
 459 of uncertainty in the damage state and prognostic features of the agent. In the proposed definition of the  
 460 RL agent, there is no quantification of the uncertainty about  $D_{\max}$  and  $a_d$  made by the agent, which can be  
 461 bypassed by the usage of the parameters  $t_{tm}$  and  $t_{td}$ . Another interesting direction of providing additional  
 462 functionality to this framework would be the inclusion of opportunistic maintenance as an action for the  
 463 agent. It would be interesting to explore the damage level at which opportunistic maintenance becomes  
 464 attractive, as this is sometimes the case when unexpected failures of different components of the turbines  
 465 occur.

## 466 6. Conclusion and further remarks

467 The proposed O&M blade LEE maintenance optimisation based on RL is able to produce an improvement  
468 in average costs in the range 12-21%, a reduction in risk of failure of the blades and reductions in  $CVaR_{0.95}$   
469 and  $Var_{0.95}$  O&M costs under this failure mode against condition-based policies. In contrast, condition-  
470 based policies can show lower median costs, and be more cost-effective in some low degradation cases. The  
471 proposed agent has highlighted the importance of a reduced uncertainty in the known condition of the blade  
472 when the opportunities for repair are fewer, with a growth from 2.0% (CS1) to 13.0% (CS2) in the scheduling  
473 of inspections. This framework has proven to be robust as to produce consistent improvements in different  
474 settings. Besides, the provided framework has the option to be re-trained with real data of different turbines  
475 of a site during operation to reduce the uncertainty in the material parameters and approximate better the  
476 degradation dynamics of this failure mode.

477 Notwithstanding, the high uncertainty underlying this problem sets a difficult scenario for decision-  
478 making in which the interpretability of the recommendations and the models used is key for practitioners  
479 to modify their current way of operating. Also, the need to incorporate the risk-critical failure modes  
480 to produce a common maintenance strategy calls for computationally efficient frameworks in which the  
481 logistics of the whole wind farm is considered and the opportunities for maintenance actions when not  
482 strictly required can be studied. In order to reduce the complexity of the models, a thorough understanding  
483 of the problem at hand is required, and this is why frameworks such as the proposed are required. Once  
484 there is a more profound knowledge about the dynamics of the failure mode and the relevance of different  
485 parameters modifying them, computationally efficient reduced-order models can be built for strategic wind  
486 farm decision-making. Techniques such as intelligent PN [7, 45] are promising for this last step in which the  
487 maintenance optimisation of assets in similar conditions can be jointly considered.

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495 WeSt High Performance Computer ([www.archie-west.ac.uk](http://www.archie-west.ac.uk)) based at the University of Strathclyde.



496 **Data availability**

497 The datasets generated during and/or analysed during the current study are available from the corre-  
 498 sponding author on reasonable request.

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## 588 Appendix A. Repair success probabilities

Table A.1: CS1  $P_1$  probabilities. The first row represents the damage severity

	0 (Inspection)	1	2	3	4	5	6
Jan	0.6614	0.6614	0.6614	0.6614	0.6614	0.3665	0.3665
Feb	0.7075	0.7075	0.7075	0.7075	0.7075	0.4052	0.4052
Mar	0.7194	0.7194	0.7194	0.7194	0.7194	0.4138	0.4138
Apr	0.8004	0.8004	0.8004	0.8004	0.8004	0.4807	0.4807
May	0.8138	0.8138	0.8138	0.8138	0.8138	0.4812	0.4812
Jun	0.8533	0.8533	0.8533	0.8533	0.8533	0.5326	0.5326
Jul	0.8663	0.8663	0.8663	0.8663	0.8663	0.5356	0.5356
Aug	0.8388	0.8388	0.8388	0.8388	0.8388	0.5083	0.5083
Sep	0.7908	0.7908	0.7908	0.7908	0.7908	0.4722	0.4722
Oct	0.7169	0.7169	0.7169	0.7169	0.7169	0.3162	0.3162
Nov	0.6880	0.6880	0.6880	0.6880	0.6880	0.3813	0.3813
Dec	0.6605	0.6605	0.6605	0.6605	0.6605	0.3841	0.3841

Table A.2: CS1  $P_2$  probabilities. The first row represents the damage severity

	0 (Inspection)	1	2	3	4	5	6
Jan	0.8444	0.7615	0.7243	0.6891	0.4624	0.1000	0.1000
Feb	0.8653	0.7925	0.7595	0.7281	0.5264	0.1000	0.1000
Mar	0.8832	0.8186	0.7892	0.7611	0.5715	0.1000	0.1000
Apr	0.9071	0.8544	0.8298	0.8062	0.6418	0.1000	0.1000
May	0.9070	0.8556	0.8317	0.8088	0.6483	0.1000	0.1000
Jun	0.9191	0.8728	0.8514	0.8307	0.6846	0.1000	0.1000
Jul	0.9221	0.8772	0.8514	0.8356	0.6921	0.1000	0.1000
Aug	0.8945	0.8369	0.8103	0.7849	0.6118	0.1000	0.1000
Sep	0.8912	0.8314	0.8037	0.7772	0.5964	0.1000	0.1000
Oct	0.8442	0.7597	0.7216	0.6856	0.4571	0.1000	0.1000
Nov	0.8303	0.7409	0.7006	0.6624	0.4264	0.1000	0.1000
Dec	0.8412	0.7576	0.7198	0.6840	0.4567	0.1000	0.1000

Table A.3: CS1  $P_3$  probabilities. The first row represents the damage severity

	0 (Inspection)	1	2	3	4	5	6
Jan	0.9614	0.9414	0.9309	0.9191	0.8066	0.1000	0.1000
Feb	0.9613	0.9409	0.9302	0.9196	0.8124	0.3930	0.3779
Mar	0.9680	0.9510	0.9417	0.9321	0.8387	0.1000	0.1000
Apr	0.9703	0.9538	0.9449	0.9352	0.8432	0.4560	0.4560
May	0.9708	0.9550	0.9463	0.9374	0.8502	0.4124	0.4124
Jun	0.9666	0.9481	0.9383	0.9281	0.8320	0.2432	0.2571
Jul	0.9751	0.9606	0.9383	0.9446	0.8645	0.3236	0.2991
Aug	0.9689	0.9521	0.9433	0.9342	0.8447	0.6747	0.6898
Sep	0.9703	0.9545	0.9459	0.9369	0.8510	0.2917	0.2917
Oct	0.9590	0.9353	0.9223	0.9095	0.7857	0.1000	0.1000
Nov	0.9630	0.9425	0.9316	0.9199	0.8057	0.1000	0.1000
Dec	0.9690	0.9534	0.9447	0.9359	0.8492	0.1000	0.1000

Table A.4: CS2  $P_1$  probabilities. The first row represents the damage severity

	0 (Inspection)	1	2	3	4	5	6
Jan	0.4374	0.4374	0.4374	0.4374	0.6614	0.3665	0.3665
Feb	0.5006	0.5006	0.5006	0.5006	0.7075	0.4052	0.4052
Mar	0.5175	0.5175	0.5175	0.5175	0.7194	0.4138	0.4138
Apr	0.6406	0.6406	0.6406	0.6406	0.8004	0.4807	0.4807
May	0.6622	0.6622	0.6622	0.6622	0.8138	0.4812	0.4812
Jun	0.7282	0.7282	0.7282	0.7282	0.8533	0.5326	0.5326
Jul	0.7504	0.7504	0.7504	0.7504	0.8663	0.5356	0.5356
Aug	0.7036	0.7036	0.7036	0.7036	0.8388	0.5083	0.5083
Sep	0.6253	0.6253	0.6253	0.6253	0.7908	0.4722	0.4722
Oct	0.5140	0.5140	0.5140	0.5140	0.7169	0.3162	0.3162
Nov	0.4733	0.4733	0.4733	0.4733	0.6880	0.3813	0.3813
Dec	0.4362	0.4362	0.4362	0.4362	0.6605	0.3841	0.3841

Table A.5: CS2  $P_2$  probabilities. The first row represents the damage severity

	0 (Inspection)	1	2	3	4	5	6
Jan	0.7130	0.5799	0.5246	0.4748	0.4624	0.1000	0.1000
Feb	0.7488	0.6280	0.5768	0.5302	0.5264	0.1000	0.1000
Mar	0.7800	0.6701	0.6228	0.5793	0.5715	0.1000	0.1000
Apr	0.8229	0.7300	0.6885	0.6500	0.6418	0.1000	0.1000
May	0.8226	0.7320	0.6917	0.6541	0.6483	0.1000	0.1000
Jun	0.8448	0.7618	0.7248	0.6900	0.6846	0.1000	0.1000
Jul	0.8502	0.7694	0.4790	0.6983	0.6921	0.1000	0.1000
Aug	0.8001	0.7004	0.6566	0.6160	0.6118	0.1000	0.1000
Sep	0.7943	0.6912	0.6459	0.6041	0.5964	0.1000	0.1000
Oct	0.7126	0.5771	0.5207	0.4700	0.4571	0.1000	0.1000
Nov	0.6894	0.5489	0.4908	0.4388	0.4264	0.1000	0.1000
Dec	0.7077	0.5740	0.5181	0.4678	0.4567	0.1000	0.1000

Table A.6: CS2  $P_3$  probabilities. The first row represents the damage severity

	0 (Inspection)	1	2	3	4	5	6
Jan	0.9243	0.8862	0.8666	0.8447	0.8066	0.1000	0.1000
Feb	0.9241	0.8853	0.8653	0.8457	0.8124	0.3930	0.3779
Mar	0.9370	0.9044	0.8868	0.8688	0.8387	0.0940	0.0880
Apr	0.9415	0.9097	0.8928	0.8746	0.8432	0.4560	0.4560
May	0.9425	0.9120	0.8955	0.8787	0.8502	0.4124	0.4124
Jun	0.9343	0.8989	0.8804	0.8614	0.8320	0.2432	0.2571
Jul	0.9508	0.9228	0.7474	0.8923	0.8645	0.3236	0.2991
Aug	0.9388	0.9065	0.8898	0.8727	0.8447	0.6747	0.6898
Sep	0.9415	0.9111	0.8947	0.8778	0.8510	0.2917	0.2917
Oct	0.9197	0.8748	0.8506	0.8272	0.7857	0.1000	0.1000
Nov	0.9274	0.8883	0.8679	0.8462	0.8057	0.1000	0.1000
Dec	0.9390	0.9090	0.8925	0.8759	0.8492	0.1000	0.1000

**Declaration of interests**

The authors declare that they have no known competing financial interests or personal relationships that could have appeared to influence the work reported in this paper.

The authors declare the following financial interests/personal relationships which may be considered as potential competing interests:

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