

September 23-25, 2020, Guimarães, Portugal

A DC OPTIMAL POWER FLOW APPROACH TO QUANTIFY OPERATIONAL RESILIENCE IN POWER GRIDS

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Keywords: Power-grid, Risk, Resilience, DC-OPF, Uncertainty

Abstract

The primary objective of resilience engineering is to analyse and mitigate the risk of a system once a vulnerability has been triggered by an attack. Resilience is a multidimensional concept in the field of engineering and incorporates restoration in the form of a performance and time. Nodal restoration is a key factor in the analysis of resilience in systems, and the properties of the nodes can be analysed to assess the states on the system. The model proposed for the power grid to demonstrate the failure of the network has been used to simulate probability of contingencies on the system and applies a Sequential Monte Carlo simulation to simulate the energy supplied. Additionally, a weather model incorporating the effects of both severe winds and lightning storms has been applied to act as a trigger to the contingency. Once failure of one component has occurred, it cannot be repaired until the network's performance reaches zero. Given failure of all components, the network will immediately start its restoration phase, and using the same algorithm for optimal power flow calculations, a DC power flow approach is implemented to assess the energy supplied to the whole network in a transient model until the network's loads meet the demand criteria completely.

This is a peer-reviewed, accepted author manuscript of the following paper: Zaman, Z. A., & Patelli, E. (2021). A DC optimal power flow approach to quantify operational resilience in power grids. In J. C. Matos, P. B. Lourenço, D. V. Oliveira, J. Branco, D. Proske, R. A. Silva, & H. S. Sousa (Eds.), 18th International Probabilistic Workshop, IPW 2020 (pp. 55-65). (Lecture Notes in Civil Engineering; Vol. 153 LNCE). Springer. https://doi.org/10.1007/978-3-030-73616-3_4

1 INTRODUCTION

The power grid is an essential tool for modern society and its function is crucial for the wellbeing of people. A failure of the system can lead to major consequences, in a socio-economic scale. The assessment of reliability in power grid systems and the parameters incorporating reliability in the power grid such as availability, consequence modelling and energy not supplied has been an important field of research for the IEEE community. Past events such as the 2003 British National Power Grid Corporation outage which was responsible for the load loss of 724MW, or approximately 20 percent of London's power load have costed the UK a significant economic burden[1].

The reliability of any system can be defined as the probability of success of the system at a given period of time, and the knowledge of reliability plays a role for system engineering to enable system maintenance planning to optimize risk mitigation[2]. System reliability can be thought of as a multidimensional analysis and incorporates many parameters. The user can analyse a single metric or multiple metrics simultaneously. The constraint with complex systems is developing the most computationally inexpensive technique and producing the most accurate results, with the aim to maximise the efficiency of the simulation.

Rochetta, Zio and Patelli developed a load flow approach to calculate failure probabilities from contingencies incorporating a wind model[3]. This was further developed with an artificial neural network surrogate model to act as a metamodel for the analysis in order to minimise computational time when applied to AC optimal power flow calculations[4]. This model was developed on the basis of a severe weather model which was developed by Cadrini, Zio and Agliardi[5] which combines stochastic extreme weather model and realistic power grid fault dynamics in order to model a restoration model quantified by sequential Monte Carlo. The constraint placed when applying this model is the high computational cost for the resilience function, especially when assessing networks with large scales of nodes.

There are various definitions of resilience available, both in a scientific context and a general context. The United Nations International Strategy for Disaster Reduction defines resilience as "The capacity of a system, community or society potentially exposed to hazards to adapt, by resisting or changing to reach and maintain an acceptable level of functioning and structure."[6] However in a more specific context from that of extreme weather events, the definition of resilience can be thought of as "the network ability to withstand high impact low probability events, rapidly recovering and improving operations and structures to mitigate the impact of similar events in the future"[7]. Efforts placed on quantification of resilience analysis have been limited and have only been tested in the last 20 years. Additionally, such efforts placed into resilience analysis applied to the power grid have been performed, which includes various techniques such as transient performance modelling for the case study of typhoon Bolaven in South Korea[8]. However the authors mentioned that the limitations in their study included only computing resilience in the form of restorative and absorptive capacity without considering anticipated and adaptive capacities and also did not include a cost benefit analysis for the quantification of resilience in an economic sense. Panteli et al. developed a method to quantify resilience in the power function n with extreme weather events by developing the three phase resilience trapezoid[9]. This is an extension to the traditional resilience triangle developed in prior literature[10] which involves three stages to the disintegration, stagnation and recovery of the structure. The author divides resilience into two types, infrastructural and operational,

stating that infrastructural resilience is in a more vulnerable condition given its recovery times and damage done to the system. Kim et. al developed a novel function to analyse the South Korean power grid network using cascading failure analysis using three different node centrality metrics; degree, clustering coefficient and betweenness[11]. A high clustering coefficient of a network indicates a more resilient network as it contains a higher redundancy potential as alternative paths in the network's nodes are present. Resilience has also been portrayed in the field of structural engineering[12] by associating a structural resilience index to for both a preevent and post-event state. The arbitrary structural resilience index is conformed from certain parameters deduced by the nature of the structure as stated in the article.

1.1 Proposed approach

This paper aims to apply a DC optimal power flow approach to quantify resilience in a simple power grid system after a network failure has occurred. The novel theme of this paper is the application of resilience as an extension to the weather induced model introduced in [3]. The chosen application for modelling will be MATLAB 2020b and the application will be case 9 as obtained from MATPower.

2 **RESILIENCE MODEL**

The index of resilience chosen for the power grid system is the Expectation of Energy Not Supplied which is deemed to be the most appropriate performance and has historically been used as an indicator of reliability performance and can further be extended for resilience analysis. The equation listed below states the resilience index as a dividend of the load received and the expected load:

$$ENS = \sum_{t=1}^{T_{sim}} \sum_{i \in N} L_{cut, i, t} \cdot t$$
(1)

Where T_{sim} is the simulation time and $L_{\text{cut},I,t}$ is the load curtailed at each individual node during time t.

2.1 Optimization

In the case of optimization, the two models are the DC Optimal Power Flow approach and the AC Optimal Power Flow approach. In the real life power grid system, the electricity is generated in power plants using methods such as fossil fuels, converted fuels or geothermal steam and transfer this energy through the transmission network at high voltage using either DC or AC flow[13]. This high voltage steps down into a medium voltage range. The primary difference between the DC and AC optimal power flow models is the convexity. DC power is constantly in a steady state, and therefore is both a linear and convex optimization problem. However, AC optimal power flow calculations are non-linear and non-convex leading to much higher computational expense. It should also be noted that in high-fidelity models, DC optimal power flow are limited in terms of details for these grids as noted by [14]. This is due to DC optimal power flow models being an estimation of AC optimal power flow models and only accounts for active power, without reactive power in the model[15]. The equations for optimal power flow approach can be denoted below as obtained from [16]. The standard optimization vector is defined as:

$$\min_{x} f(x) \tag{2}$$

Subject to

$$g(x) = 0 \tag{3}$$

$$h(x) \le 0 \tag{4}$$

$$x_{min} \le x \le x_{max} \tag{5}$$

The optimization vector for DC optimal power flow neglects reactive power and voltage magnitude and is defined as;

$$x = \begin{bmatrix} \theta \\ P_g \end{bmatrix} \tag{6}$$

Equation 2 is reduced to;

$$\min_{\theta, P_g} \sum_{i=1}^{n_g} f_p^i(p_g^i) \tag{7}$$

2.2 Load contingencies

The representation of failure for this model will be in the form of contingencies. In this context, a contingency is defined as an event occurring that is not considered predictable at a given time. Contingencies when applied to the power grid network imply the network's architecture is the disruption of the load transfer from one bus to the next. This is commonly caused by a failure by extremely hot weather, system failure such as outages in loads and human errors[17].

2.3 Severe weather model

In extension to the contingencies faced in the model, a weather model has been proposed in the simulation algorithm to mimic the real-life application of an event. These events include lightning strikes, extremely high winds and natural disasters. The occurrence of normal weather conditions can be modelled as a homogeneous Poisson process. All equations for this weather model have been taken from [18].

$$P(N_f(t) = k) = \frac{[\lambda_n \cdot t]^k}{k!} e^{-\lambda_n \cdot t} \quad k = 0, 1, \dots, N$$
(8)

Where $P(N_f(t) = k)$ represents the probability that k failures happen within the network given the time (0, t) and Nf(t) is the number of failures per kilometre of grid line. However, in a more realistic perspective, the weather model is more likely to affected by uncertainty. This is why the occurrence of severe weather events is more suited to be modelled by a Nonhomogeneous Poisson process:

$$P(N_f(t) = k) = \frac{[\lambda_n \cdot t]^k}{k!} e^{-\lambda_n \cdot t} \quad k = 0, 1, \dots, N$$
(9)

In this case, Ve(t) represents the time dependent probability of the event occurring and can be obtained applying the following equation:

$$V_{e}(t) = \int_{t}^{0} v_{e}(t') dt'$$
 (10)

 $v_e(t')$ is the rate at which the disturbance occurs. Given a severe weather occurrence, the time of the event is obtained from data from previous events and will be carried out using probability distribution functions. In the case of high winds, the windstorm intensity is obtained via the following equations:

$$W_{\omega}(t) = W_{crt} + \Delta_{\omega}(t) \tag{11}$$

where $W_w(t)$ is the wind speed intensity at time t for the and W_{crt} is a datum wind speed known as the critical wind speed set at 10 m/s. $\Delta_w(t)$ is the difference between the critical wind speed and the actual wind speed during the event. In terms of the lightning severe weather model, the intensity of a the weather event is set at the lightning strike ground density N_g(t)which takes the units of ground flashes per unit time and area[occh·km²] modelled with log-normal variability.

The table below shows the shape and scale factors for the respective variables:

	Distribution	Scale (a)	Shape (b)
Dω	Weibull	9.86	1.17
D_{lg}	Weibull	0.96	0.85
$\Delta_{\omega}(t)$	Weibull	1.23	1.05
		Mean (µ _{Ng})	SD (ong)
N _g (t)	Log-normal	-5.34	1.07

Table 1: Variable attributes

Both high winds and lightning strikes are a cause of contingency and therefore it is crucial to define an equation which considers both contingencies to calculate the total failure rate:

$$\lambda(t) = \lambda_n + \lambda_\omega(W_\omega(t)) + \lambda_{lg}(N_g(t))$$
(12)

 λ_w is the total line failure contribution due to high wind measured per km and $\lambda_{(lg)}$ is the lightning storms contribution. When considering individual lines, the contribution to line failure due to high winds can be denoted in the equation;

$$\lambda_{\omega}(W_{\omega}(t)) = \lambda_n \left(\frac{W_{\omega}(t)^2}{W_{crt}^2} - 1\right) \alpha_{\omega}$$
(13)

 α_w is the regression parameter for failure data obtained from the literature. The line failure rate as a result of lightning can be denoted as:

$$\lambda_{lg} \big(N_g(t) \big) = \lambda_n \beta_{lg} N_g(t) \tag{14}$$

 β_{lg} is the regression coefficient obtained from prior data[18].

2.4 Repair speed

The model for recovery has been obtained from [5] and takes into consideration the efficiency of the repair crew as they are also affected by the adverse weather conditions. The assumptions in this model are:

- i. Repair is initiated instantly after failure
- ii. After a line is repaired, it is considered fully functional
- iii. The transitional time between failure and repair is negligible

$$v_{repair} = \begin{cases} \frac{v_{norm}}{1 + \eta \cdot (W_{\omega}(t) - W_{crt})}, & \text{if } W_{\omega}(t) \ge W_{crt}, N_g = 0\\ \frac{v_{norm}}{1 + \Psi \cdot N_g}, & \text{if } W_{\omega}(t) < W_{crt}, N_g > 0\\ \frac{v_{norm}}{[1 + \eta \cdot (W_{\omega}(t) - W_{crt})] + [1 + \Psi \cdot N_g]}, & \text{if } W_{\omega}(t) \ge W_{crt}, N_g > 0 \end{cases}$$

In this model and η are positive parameters and v_{norm} is set at 20[%/h]. The values for ψ and η are set to 40 and 0.4, respectively.

2.5 Probabilistic load uncertainty

It is important to quantify uncertainty in the model used which uses data for variability in average daily load demand. The aleatory uncertainty of the model can be considered by implementing a gaussian with parameters fitted on historical data;

$$f(L_i(t)) = \frac{1}{\sqrt{2\pi\sigma_{Li}(t)}} e^{-\frac{L_i(t) - \mu_{Li(t)}}{2\sigma L_i(t)^2}}$$
(15)

3 METHODOLOGY

The proposed approach is to apply a DC optimal power flow approach to quantify the energy not supplied during the severe weather contingency, which will then be used to quantify the resilience function of energy supplied after disaster through the same algorithm. The pseudocode below displays the steps of the proposed approach below;

Algorithm 1 DC Optimal Power Flow model 1: procedure ENS (Risk Assessment based on DC-OPF) 2: $Input = \{\lambda_{n,lg}, \alpha_w, W_{crt}, b_{Dw}, a_{Dlg}, b_{Dlg}, a_{\Delta w}, b_{\Delta w}, v_{norm}, \mu_{Ng}, \sigma_{ng}\}$ t=0, e=1, f=0 3: 4:Sample failure events for $[0, T_{sim}]$ 5: t=TTE(e) 6: if event i is a failure then 7: f=f+18: Sample X_f and L_f for tUpdate repair speed and time to repair 9: else Sample T_e and (N_g, Δ_w) 10: 11: Compute failure rates $t + TTF(f) > t + T_d$ then 12: if Compute load 13: Compute ENS(f) using $L_{cut}(f)$ and TTR(f)14: else set $t = t + T_d$ and f = f + 1Sample X_f and L_f for tUpdate repair speed and time to repair OUTPUT - Energy Not Supplied

15:

16:

17:

18: 19:

4 CASE STUDY

This paper implements case 9 as an example from MATPower's default folders [19]. It is composed of a 9 node, 9 branch network which is assumed to be equidistant in all branches.



Figure 1: Topology

Table 2: Branch failure rates

Branch	Failure rate
1-4	0.1455
4-5	0.8693
5-6	0.5797
3-6	0.5499
6-7	0.1450
7-8	0.8530
8-2	0.6221
8-9	0.3510
9-4	0.5132

4.1 Results



Figure 2: Results for DC-OPF simulation

The recovery time initiates after 1×10^{-4} dimensionless unit and continues to restore the energy supplied to the nodes are fully recovered after 4×10^{-4} , in which the system has fully recovered and therefore all the energy required for the nodes in the whole network is being supplied. The uncertainty applied from eq. 16 shows the possible ranges of the energy supplied to the recovery function which also converges in the latter stages of the simulation.

CONCLUSION

This paper demonstrates the application of a restoration function applied to a simple power network when DC optimal power flow is applied to the 9-node example provided in MATPower. The work presented has innovated the weather model applied to contingencies in the general power grid to the application of resilience for the energy supplied after disaster. Further work that could be done on this topic includes developing a cost model for resilience quantification for the respective nodes in the network, and further expanding this application into three phase resilience models for realistic and complex networks.

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