

Density functional theory study on biodiesel production from yeast lipid catalyzed by imidazolium ionic liquid

Yuwei Chen^{a,b,d}, Xiaolei Zhang^c, Yunwu Zheng^d, Jianchun Jiang^b, Feng Long^b, Wei Liu^{a*},
Junming Xu^{b*}, Xiaoan Nie^{b*}

^a School of Automotive Engineering, Jiangsu Provincial Key Laboratory of Eco-Environmental Materials, Yancheng Institute of Technology, Yancheng 224051, China

^b Institute of Chemical Industry of Forest Products, Chinese Academy of Forestry, Nanjing 210042, China

^c Department of Chemical and Process Engineering, University of Strathclyde, UK

^d National Joint Engineering Research Center for Highly-Efficient Utilization Technology of Forest Biomass Resources, International Joint Research Center for Bioenergy, Southwest Forestry University, Kunming, 650224, PR China

* Corresponding authors: liuwei@ycit.edu.cn (W. Liu), xujunming@icifp.cn (J. Xu), niexiaoan@icifp.cn (X. Nie)

Abstract

Imidazolium ionic liquid is a novel and efficient catalyst for biodiesel production from oleaginous yeast. However, the catalytic mechanism of how imidazolium ionic liquid works in the reaction is not clear. Herein, Density functional theory (DFT) was employed to investigate the catalytic mechanism of three imidazolium ionic liquids in esterification and transesterification reactions. Pathways containing three intermediates and two transition states were proposed for the two reactions. In the subsequent DFT calculation, PBE0-D3BJ functional and 6-31G* basis set were used to optimize the intermediates and transition states. Then the Gibbs free energy of the intermediates and transition states in each reaction step was calculated to obtain the energy barrier for each reaction. The calculation results showed that 1-butyl-3-methylimidazolium hydrogen sulfate ([Bmim][HSO₄]) had the minimum energy barrier of 37.77 kcal/mol in esterification, and 1-sulfobutyl-3-methylimidazolium hydrosulfate ([HSO₃-Bmim][HSO₄]) had the minimum energy barrier of 20.80 kcal/mol in transesterification, which were consistent with previous experimental results. The catalytic mechanism validated in this study provides a new idea for subsequent optimization of imidazolium ionic liquid structure to improve their catalytic efficiency in biodiesel production from oleaginous yeast.

33

34 **Key words**

35 Biodiesel, yeast lipid, imidazolium ionic liquid, DFT calculations

36 **1.Introduction**

37 Energy consumption and environment protection are two hot issues in recent decades[1,
38 2]. The fast population explosion, continuous industrialization and irreversible
39 metropolitan expansion consumes fossil fuels excessively[3, 4]. To deal with the
40 drawbacks of excessive use of fossil, China has taken the lead in promising of “peak
41 carbon dioxide emissions” and “carbon neutral”[5]. In order to achieve the goals, the
42 renewable biodiesel is a promising candidate to replace fossil fuels[6, 7]. Biodiesel
43 (long-chain monoalkyl fatty acid esters) has many sources, such as agricultural wastes,
44 waste cooking oil and non-edible oils[8, 9]. In recent years, oleaginous yeast has been
45 a new kind source of biodiesel, for it has advantages of high lipid content, wide varieties
46 of substrates and short cultivation cycles[10, 11]. Among all the oleaginous yeast,
47 *Rhodosporidium toruloides* (*R. toruloides*) is a bright candidate. *R. toruloides* can
48 accumulate more than 70% lipid in dry cells[12]. The lipid from *R. toruloides* consist
49 of triacylglycerol (TAG), fatty acid (FFA), diacylglycerol (DAG) and
50 monoacylglycerol (MAG)[13]. Because of these properties, *R. toruloides* is suitable for
51 biodiesel production. In previous work, hydrothermal liquefaction showed to be a novel
52 method to disrupt cell wall of *R. toruloides* and extract the lipid from the yeast[14].

53 In order to obtain biodiesel, the lipid extracted from *R. toruloides* needs to take
54 transesterification or esterification reactions with methanol in the presence of catalyst.
55 As there exists considerable fatty acid in the lipid, acid catalyst is suitable for the
56 reaction in order to obtain biodiesel in one step. Sulfuric acid or p-Toluenesulfonic acid
57 is often used as catalyst in the reactions. However, both of these acids are strong acids
58 and they can be corrosive to equipment. Besides, the catalyst can not be recycled.
59 Considering these drawbacks of traditional catalyst, acidic ionic liquid was introduced
60 in converting yeast lipid to biodiesel[15-17]. In previous study, acidic ionic liquid

61 showed the similar catalytic effect with the strong acid, and they can be recycled with
62 proper processes[18]. Hu et al. used acidic ionic liquid 1-sulfobutyl-3-
63 methylimidazolium hydrosulfate ($[\text{HSO}_3\text{-Bmim}][\text{HSO}_4]$) as catalyst to convert waste
64 oils containing 72% of free fatty acids to biodiesel, the yield of biodiesel achieved as
65 high as 94.9% at the optimum conditions. Besides, the catalytic activity of the ionic
66 liquid $[\text{HSO}_3\text{-Bmim}][\text{HSO}_4]$ remained around 97% after re-use of 5 times[19]. Sun et
67 al. used 1-butyl-3-methylimidazolium hydrogen sulfate ($[\text{Bmim}][\text{HSO}_4]$) as a solvent
68 and acid catalyst for in-situ extractive transesterification of wet *Nannochloropsis* with
69 methanol, the results showed that at optimum conditions, the biodiesel yield achieved
70 as high as 95.28%, and the catalytic efficiency remained as 81.23% after the ionic liquid
71 $[\text{Bmim}][\text{HSO}_4]$ recycled 4 times. In previous work, $[\text{Bmim}][\text{HSO}_4]$, $[\text{HSO}_3\text{-}$
72 $\text{Bmim}][\text{HSO}_4]$ and 1-butyl-3-methylimidazolium dihydrogen phosphate
73 ($[\text{Bmim}][\text{H}_2\text{PO}_4]$) were used as catalysts in model compound experiments, which were
74 designed to identify the catalytic effect of three AILs in biodiesel production.[8] The
75 results showed $[\text{Bmim}][\text{HSO}_4]$ had better catalytic effects on esterification reaction and
76 $[\text{HSO}_3\text{-Bmim}][\text{HSO}_4]$ had better catalytic effects on transesterification reaction. The
77 research only gave the experimental results, further investigation on the interaction
78 between catalysts and reactant weren't discussed. The catalytic processes were also not
79 inferred. So the reason why the specific catalyst has the best or worst catalytic effect
80 was not clear.

81 Density functional theory (DFT) is a reliable method in studying the mechanisms and
82 kinetics of reactions. Many catalytic processes involved ionic liquid have been
83 investigated by DFT[20, 21]. Silva et al. used DFT to study the solvent effects on the
84 acid-catalyzed ethanolysis of butyric acid monoglyceride[22]. It was found that the
85 reaction proceeded through a concerted mechanism with a single transition state
86 without the formation of a tetrahedral intermediate. Ma et al. used DFT to calculate the
87 effects of hydrogen bond between three ionic liquids and cellulose before the
88 transesterification of algae lipid[23]. However, the most calculations only primarily

89 focused on the solvent effect of ionic liquids, the catalytic effect and the catalytic
90 process were not investigated. Li et al. used DFT to investigate a three-step
91 transesterification catalyzed by a pyridinium-based Brønsted acidic ionic liquid[24].
92 The results showed that hydrogen bond was existed throughout the process. Based on
93 this founding, the catalytic mechanism involving hydrogen bond was established. To
94 best of our knowledge, the catalytic mechanism of esterification or transesterification
95 by acid imidazolium ionic liquid [Bmim][HSO₄], [HSO₃-Bmim][HSO₄] and
96 [Bmim][H₂PO₄] hasn't been studied.
97 In this work, the plausible mechanism of esterification and transesterification catalyzed
98 by [Bmim][HSO₄], [HSO₃-Bmim][HSO₄] and [Bmim][H₂PO₄] was proposed. Based
99 on the mechanism, the reaction processes were then designed. The structures of reactant,
100 intermediate (IM) and products were optimized before the transition states (TS) were
101 obtained. After all the basic work was completed, the energy barriers of each reaction
102 catalyzed by three different acidic ionic liquids were obtained. As a result, the catalytic
103 effects of the three different acidic ionic liquids were obtained eight. In comparison
104 with the previous experiments results, the correction of the DFT calculation was
105 validated. The validated catalytic mechanism will provide a new idea for subsequent
106 optimization of imidazolium ionic liquid structure to improve their catalytic efficiency
107 in biodiesel production from oleaginous yeast.

108 **2.Methods**

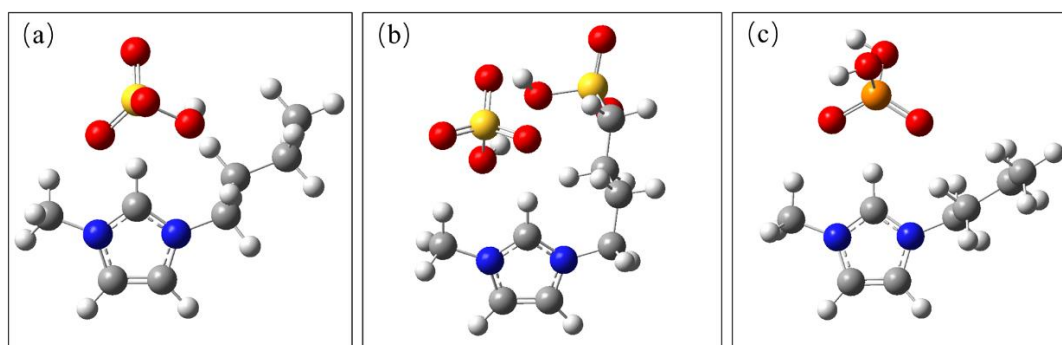
109 All calculations have been performed using the DFT method implemented in the
110 commercial Gaussian 16 program package[25]. Molecular geometries of the model
111 complexes were optimized applying the PBE0-D3BJ functional[26, 27]. For all atoms
112 the 6-31G* basis set was used. As soon as the convergences of optimizations were
113 obtained, the frequency calculations at the same level have been performed to identify
114 all the stationary points as minima or transition states, which has the unique imaginary
115 frequencies. The intrinsic reaction coordinate (IRC) calculations have been carried out
116 to confirm that the transition structures can indeed connect the related reactant and

117 product[28]. All of the optimized geometries mentioned were built by GaussView
118 6.0[29].

119 The main component of fatty acid in yeast lipid was oleic acid, which accounted about
120 half in the lipid[14]. Synthetically considering the calculation accuracy and efficiency,
121 the reactant of fatty acid in esterification was modelled as 4-Hexenoic acid with a linear
122 carbon chain length of six carbon atoms containing an ethylenic bond
123 ($\text{CH}_3\text{CH}=\text{CHCH}_2\text{CH}_2\text{COOH}$), and the monoacylglycerol was modelled as 2,3-
124 dihydroxypropyl (4E)-hexenoate ($\text{CH}_3\text{CH}=\text{CHCH}_2\text{CH}_2\text{COOCHOHCH}_2\text{OH}$).

125 3.Results and discussion

126 With the functional and the basis set, the molecular geometries of the three acidic ionic
127 liquid were firstly optimized. The results are shown in Fig. 1.



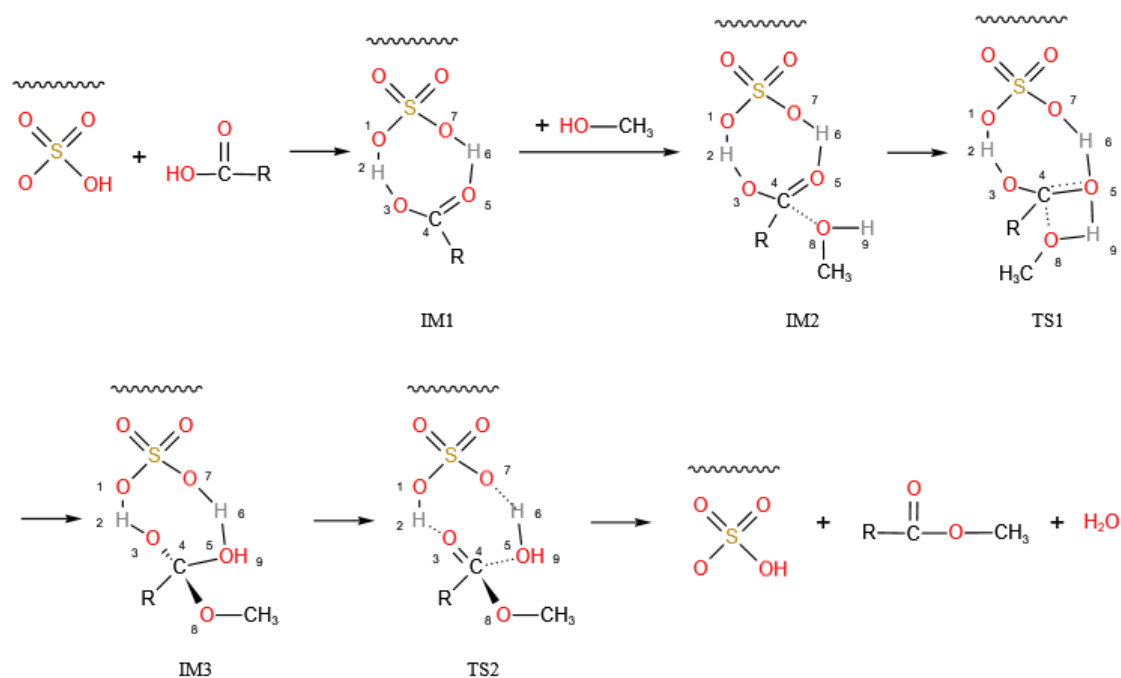
128
129 Fig. 1. Molecular Geometries of three acidic ionic liquid

130 (a) $[\text{Bmim}][\text{HSO}_4]$ (b) $[\text{HSO}_3\text{-Bmim}][\text{HSO}_4]$ (c) $[\text{Bmim}][\text{H}_2\text{PO}_4]$

131 3.1 Esterification

132 3.1.1 Reaction pathway

133 Taking other acidic ionic liquid catalyzed reaction pathways as reference[30], the
134 reaction pathway of esterification catalyzed by $[\text{Bmim}][\text{HSO}_4]$, $[\text{HSO}_3\text{-Bmim}][\text{HSO}_4]$
135 and $[\text{Bmim}][\text{H}_2\text{PO}_4]$ was proposed. Taking $[\text{Bmim}][\text{HSO}_4]$ as the catalyst as example,
136 the reaction pathway of esterification is shown in Fig. 2.



137

138

Fig. 2. Reaction pathway of esterification catalyzed by [Bmim][HSO₄]

139 As Fig. 2 shows, the total reaction contains two transition states (TS) and three

140 intermediates (IM). Firstly, the acidic ionic liquid has effect on the FFA, and the

141 carbonylic moiety of FFA was protonated, and it was activated to form IM1. Then the

142 carbon atom (C4, the number means the number besides the atom in Fig. 2) of activated

143 carbonyl combines with the oxygen (O8) of methanol and forms IM2. Due to the

144 attraction between the hydrogen (H9) of hydroxyl from methanol and the oxygen (O5)

145 of carbonyl from FFA, the bond between the two atoms establishes and thus IM2

146 transforms to TS1. TS1 is not stable, the oxygen (O5) of carbonyl from FFA has more

147 attraction than the oxygen (O8) from methanol, so the hydrogen atom (H9) removes

148 closely to the oxygen (O5) of carbonyl from FFA and forms hydroxyl. Due to the

149 formation of hydroxyl, the attraction between the carbon atom (C4) and the oxygen

150 atom (O5) from carbonyl decreases, so the double bond between the two atoms is

151 broken and it becomes a single bond, so a tetrahedral structure is formed with the

152 transformation of TS1 to IM3. With the increasing departure of the oxygen atom (O5)

153 from the carbon atom (C4), the attraction between the two atoms decreases, and the

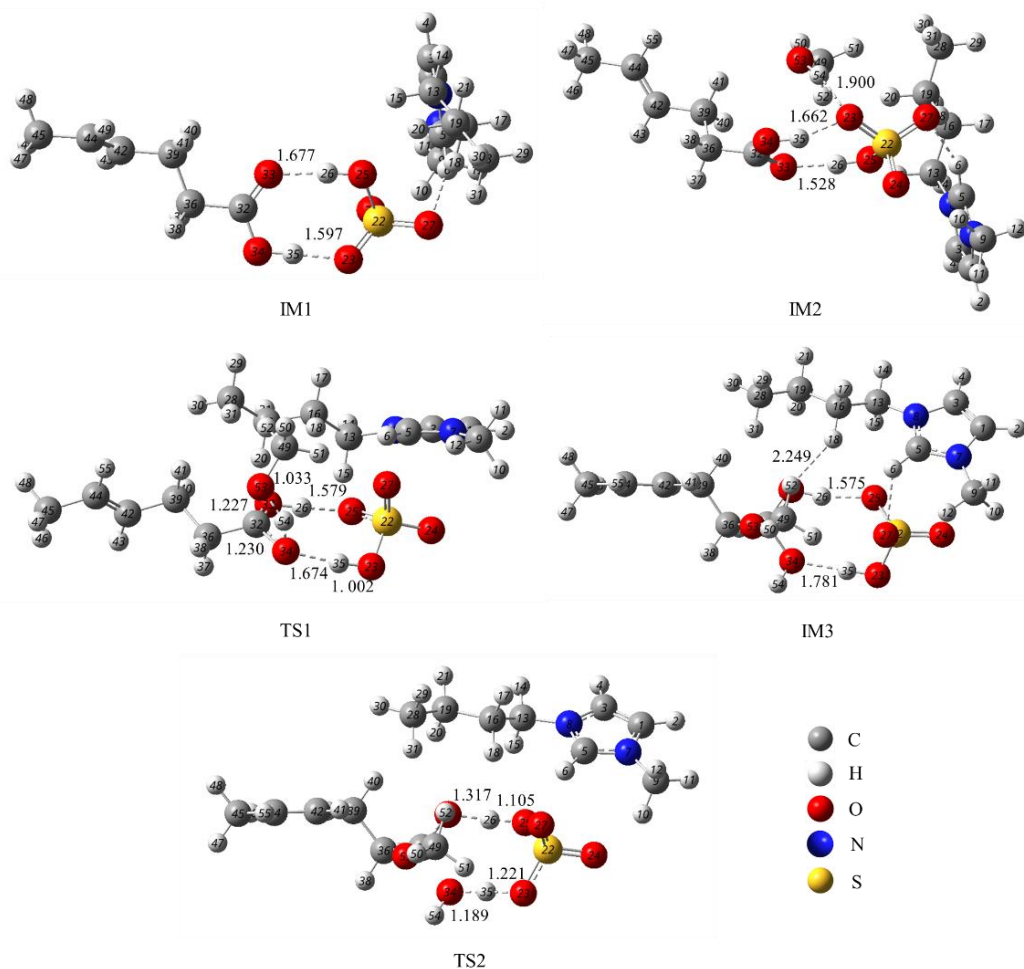
154 single bond between the two atoms becomes an imaginary bond. Due to the attraction

155 between the oxygen atom (O5) and the hydrogen atom (H6) from acidic ionic liquid

156 increases, so the single bond between the hydrogen atom (H6) and the oxygen atom
157 (O7) from the acidic ionic liquid becomes an imaginary bond. At the same time, the
158 attraction between the carbon atom (C4) and the oxygen atom (O3) increases, so the
159 single bond between the two atoms becomes a double bond. The attraction between the
160 hydrogen atom (H2) and oxygen atom (O3) of hydroxyl from FFA decreases, the single
161 bond between the two atoms becomes an imaginary bond. The process is the
162 transformation of IM3 to TS2. After the TS2 forms, all the imaginary bonds breaks,
163 thus the fatty acid methyl ester and water forms. The reaction pathways catalyzed by
164 the other two acidic catalytic liquid $[\text{HSO}_3\text{-Bmim}][\text{HSO}_4]$ and $[\text{Bmim}][\text{H}_2\text{PO}_4]$ are the
165 same with that catalyzed by $[\text{Bmim}][\text{HSO}_4]$.

166 3.1.2 Optimization of IMs and TSs

167 Based on the reaction pathway above, the structures of IMs and TSs in esterification
168 catalyzed by $[\text{Bmim}][\text{HSO}_4]$, $[\text{HSO}_3\text{-Bmim}][\text{HSO}_4]$ and $[\text{Bmim}][\text{H}_2\text{PO}_4]$ were
169 optimized. The results are shown in Fig. 3, Fig. 4 and Fig. 5. As Fig. 3 shows, in IM1,
170 there exists hydrogen bond between the oxygen atom (O33) of carbonyl from FFA and
171 the hydrogen atom (H26) from the acidic ionic liquid, there also exists hydrogen bond
172 between the oxygen atom (O23) from ionic liquid and the hydrogen atom (H35). The
173 bond lengths of hydrogen bonds are 1.677\AA and 1.597\AA respectively, and the bond
174 orders are both 0.1. The results reveal that these hydrogen bonds are weak. In IM2,
175 when methanol participates in the reaction, there exists hydrogen bond between the
176 hydrogen atom (H54) of hydroxyl from methanol and the oxygen (O23) from the ionic
177 liquid, the bond length is 1.900\AA , and the bond order is 0.1, indicating that the hydrogen
178 bond is weak. Due to the influence of hydrogen atom (H54), the bond length between
179 H35 and O23 increases to 1.662\AA , at the same time, the bond length between H26 and
180 O33 decreases to 1.528\AA . The results show the distance between H26 and O33 is
181 decreasing, the interaction between the two atoms is strengthening.



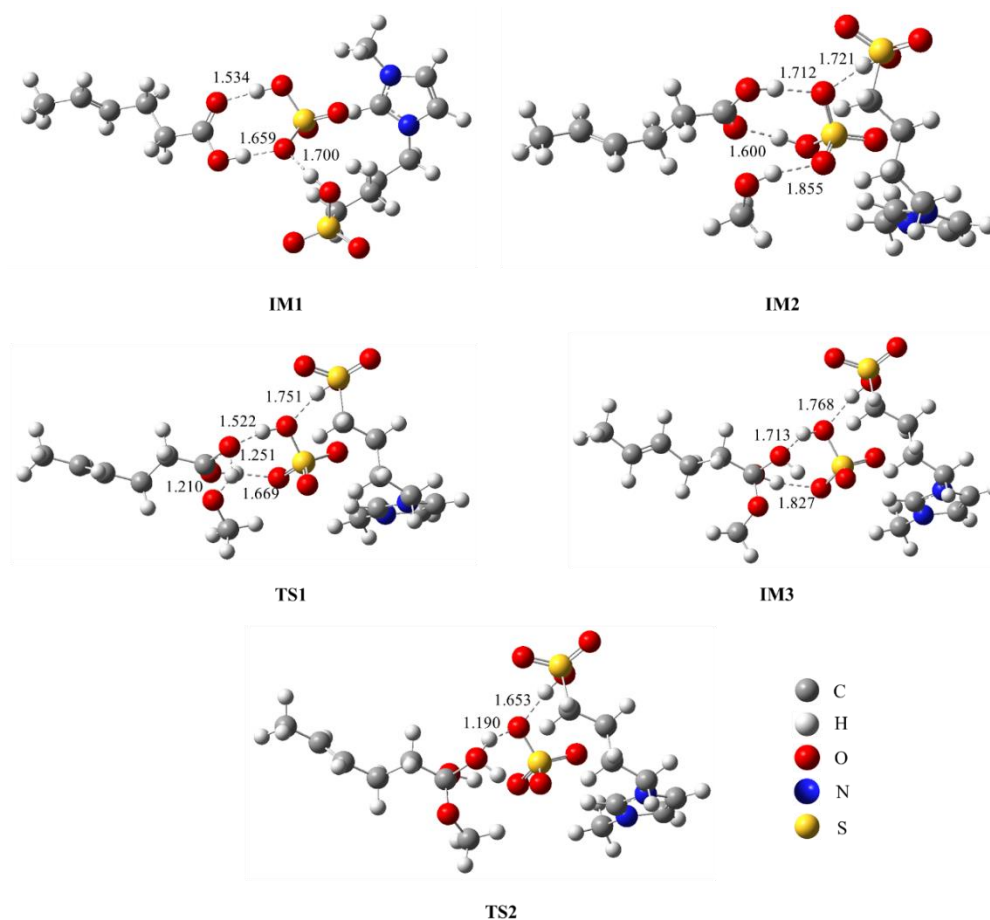
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Fig. 3 IMs and TSs in esterification catalyzed by [Bmim][HSO₄]

184 In TS1, the bond length between H26 and O23 decreases to 1.013 Å and the bond order
 185 increases to 1.0, this means there has formed a stable bond between the hydrogen atom
 186 H26 and oxygen atom O33. There is a hydrogen bond between H54 and O34, the bond
 187 length is 1.230 Å and the bond order is 0.5, which means the hydrogen bond is forming
 188 but it is not stable enough. At the same time, the bond between O53 and C32 is forming,
 189 the bond length is 1.401 Å and the bond order is 1.0, the results demonstrate that the
 190 tetrahedral structure has established. After the geometry of TS1 was optimized, an
 191 imaginary frequency of 1597.38 icm^{-1} was obtained. The frequency is corresponding
 192 with vibration of the movement of H54 from O53 to O34. In IM3, the hydrogen bond
 193 between H54 and O53 disappears, while there forms a bond between H54 and O34, the
 194 bond length and bond order are 0.968 Å and 1.0 respectively, which means the bond
 195 between H54 and O34 is stable. The length of hydrogen bond between H35 and O33 is

196 1.781 Å, and the bond order is 0.1. The length of hydrogen bond between H26 and O25
 197 is 1.575 Å, and the bond order is 0.1. The results indicate the two hydrogen bonds are
 198 weak. In TS2, the bond between O34 and C32 breaks. The bond length between H35
 199 and O34 decreases to 1.189 Å, and the bond order is 0.5. The bond length between H35
 200 and O21 increases to 1.221 Å, and the bond order is 0.5. These phenomena demonstrate
 201 that the H35 has a tendency of transferring from O21 to O34. At the same time, the
 202 bond length between H26 and O25 decreases to 1.105 Å, and the bond length between
 203 H26 and O33 increases to 1.317 Å. This indicates that H26 has a tendency of
 204 transferring from O33 to O25. When the TS2 is optimized, an imaginary frequency of
 205 873.96 cm^{-1} is obtained. The frequency is corresponding with vibration of the
 206 movement of H35 from O21 to O34, H26 from O33 to O25 and the departure of O34
 207 from C32. The vibration is exactly the generation path of fatty acid methyl ester and
 208 water.



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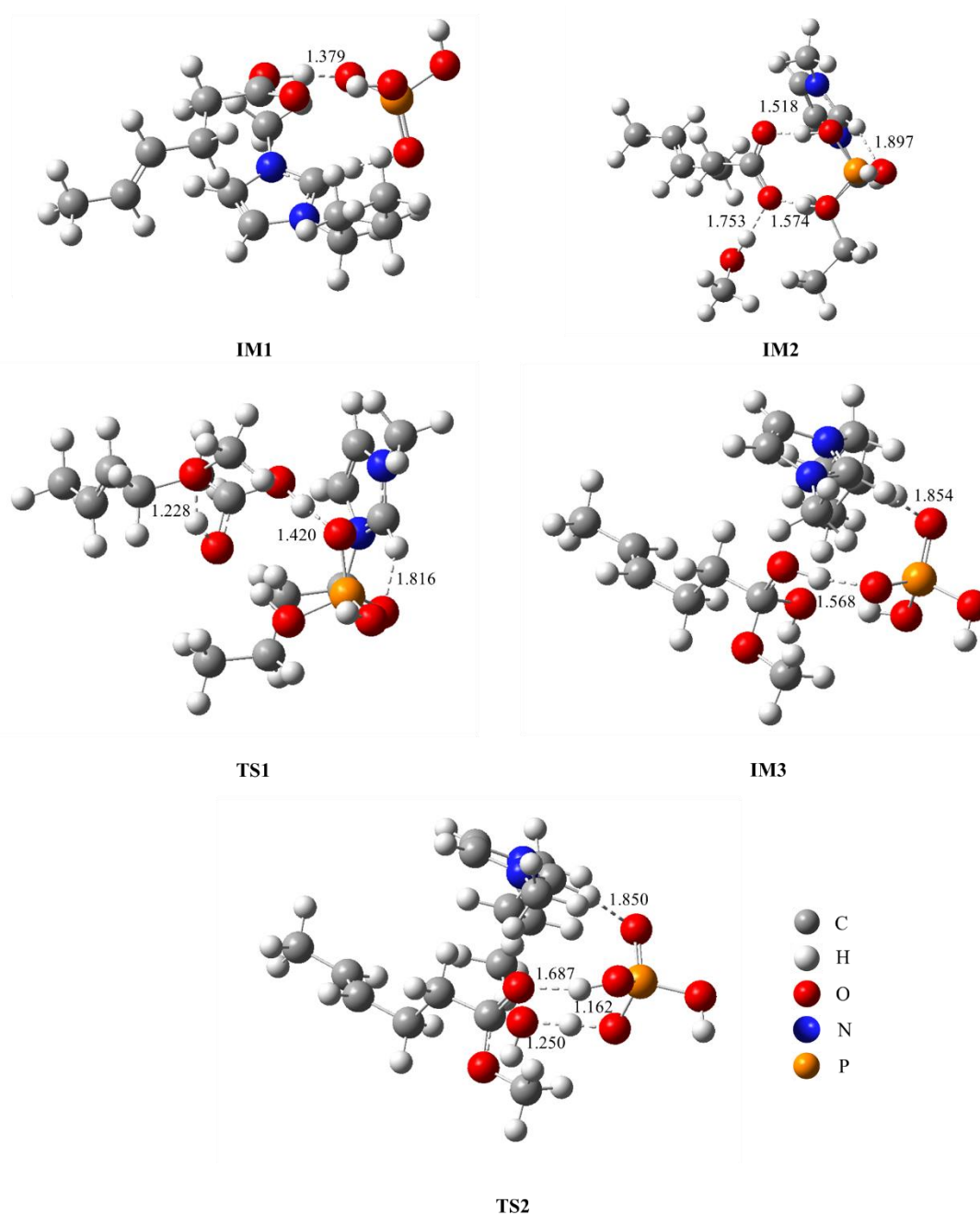
Fig. 4 IMs and TSs in esterification catalyzed by [HSO₃-Bmim][HSO₄]

211 Fig. 4 and Fig. 5 are the structures of IMs and TSs in esterification catalyzed by [HSO₃-
 212 Bmim][HSO₄] and [Bmim][H₂PO₄]. The reaction processes are similar with that
 213 catalyzed by [Bmim][HSO₄]. The imaginary frequency of TS1 and TS2 catalyzed by
 214 the three ionic liquids is shown in Table 1.

215 Table 1 Imaginary frequency of TS1 and TS2 catalyzed by the three ionic liquids (icm⁻¹)

	[Bmim][HSO ₄]	[HSO ₃ -Bmim][HSO ₄]	[Bmim][H ₂ PO ₄]
TS1	1597.38	1579.39	1591.98
TS2	873.96	201.35	616.80

216



217

218 Fig. 5 IMs and TSs in esterification catalyzed by [Bmim][H₂PO₄]

219 3.1.3 Analysis of Gibbs free energy

220 After all the geometry of IMs and TSs was optimized, the frequency of each IMs and
 221 TSs was calculated. Then the Gibbs free energy was obtained. The results are shown in
 222 Table 2.

223 Table 2 Gibbs free energy of each phase in esterification catalyzed by three ionic liquids (Hartree)

	[Bmim][HSO ₄]	[HSO ₃ -Bmim][HSO ₄]	[Bmim][H ₂ PO ₄]
R1	-384.56	-384.56	-384.56
R2	-115.55	-115.55	-115.55
Ionic Liquid	-1121.88	-1745.32	-1065.78
IM1	-1506.45	-2129.89	-1450.36
IM2	-1622.00	-2245.44	-1565.92
TS1	-1621.94	-2245.38	-1565.85
IM3	-1621.98	-2245.42	-1565.89
TS2	-1621.96	-2245.40	-1565.88
Product	-423.79	-423.79	-423.79
H ₂ O	-76.32	-76.32	-76.32

R1: CH₃CH=CHCH₂CH₂COOH

R2: CH₃OH

Product: CH₃-CH=CH-CH₂-CH₂-COOCH₃

224 Based on the calculation results in Table 2, taking the Gibbs free energy of ionic liquid
 225 as zero, then calculate the difference of the Gibbs free energy (ΔG) of each IMs and
 226 TSs relative to ionic liquid. The calculation results are shown in Fig. 6. From Fig. 6, it
 227 is easy to obtain the energy barrier (ΔG_{\max}) in the esterification reactions catalyzed by
 228 different ionic liquids. By comparing the difference of ΔG_{\max} , the reason why the three
 229 ionic liquids have different catalytic effects can be easily concluded.

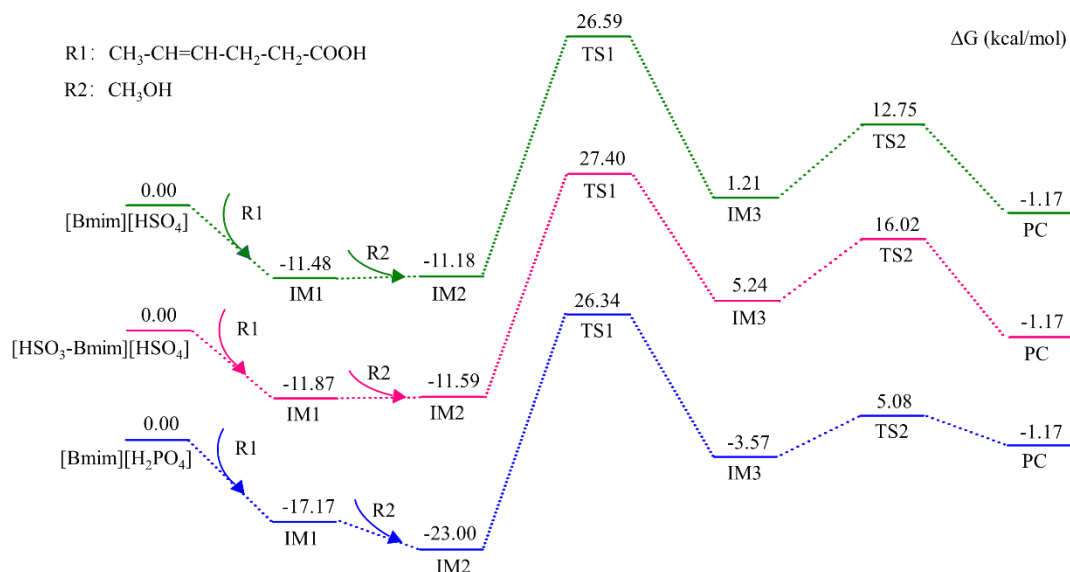


Fig. 6 Gibbs free energy in each phase of esterification catalyzed by three ionic liquids

In Fig. 6, it is obvious IM1 is a combination of ionic liquid and fatty acid, and IM2 is the combination of all reactant and catalyst, so the reactions begin from IM2. According to rate-limiting step theory suggested by Murdoch[31], the reaction can be divided into one period, i.e., from the ionic liquid to PC. The reaction contains two energy barriers, which are from IM2 to TS1 and IM3 to TS2 respectively. It is not difficult to be concluded that the energy barrier of IM2 to TS1 is higher than that of IM3 to TS2. So the rate-limiting step is IM2 to TS1. The ΔG_{\max} of esterification catalyzed by [Bmim][HSO₄], [HSO₃-Bmim][HSO₄] and [Bmim][H₂PO₄] are 37.77 kcal/mol, 38.99 kcal/mol and 49.34 kcal/mol, respectively. The results demonstrate that the ΔG_{\max} of esterification catalyzed by [Bmim][HSO₄] is the lowest, and [Bmim][H₂PO₄] is the highest. And of course [Bmim][HSO₄] and [Bmim][H₂PO₄] had the best and the worst catalytic effects respectively. The DFT results are consistent with the experimental results[8].

3.2 Transesterification

3.2.1 Reaction pathway

Taking transesterification pathway catalyzed by pyridinium based ionic liquid as reference[24, 32], the reaction pathway catalyzed by [Bmim][HSO₄], [HSO₃-

250 Bmim][HSO₄] and [Bmim][H₂PO₄] was proposed. Taking [Bmim][HSO₄] as the
 251 catalyst as example, the reaction pathway of transesterification is shown in Fig. 7.

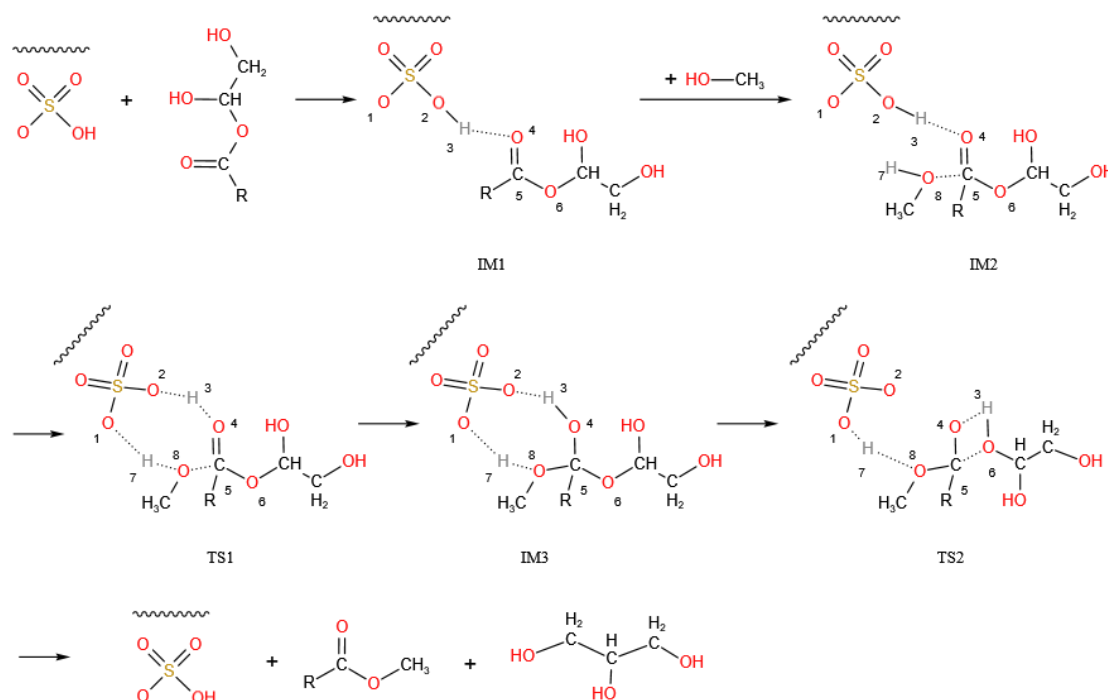


Fig. 7 Reaction pathway of transesterification catalyzed by [Bmim][HSO₄]

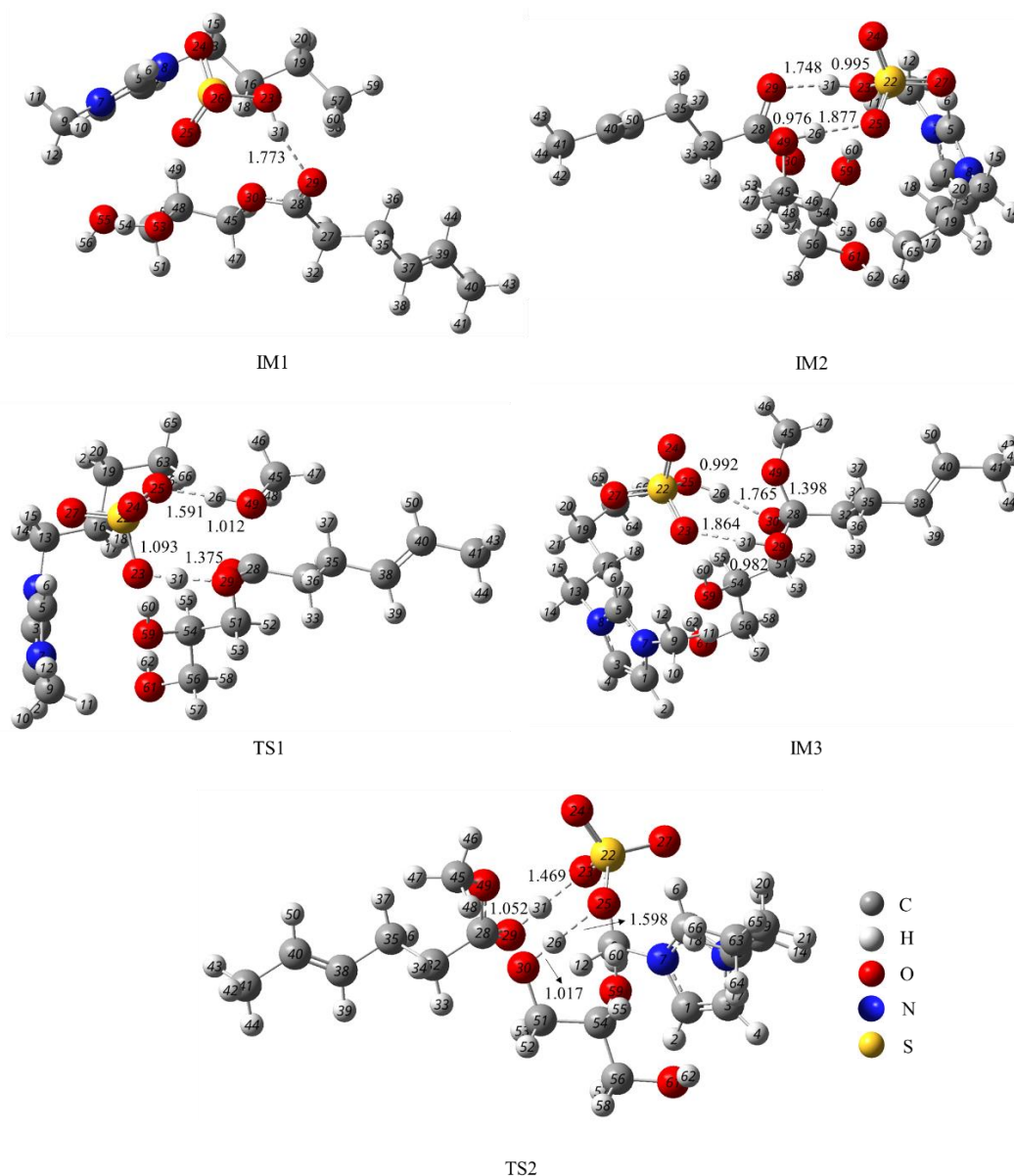
254 In Fig. 7, the hydrogen atom (H3) from [Bmim][HSO₄] was attracted by the oxygen
 255 atom (O4) of carbonyl from MAG, and a hydrogen bond is formed between the two
 256 atoms. This process is also the formation of IM1. After the combination of IM1 with
 257 methanol, the carbon atom (C5) from carbonyl has attraction on the oxygen atom (O8)
 258 of methanol, and an imaginary bond is formed between the two atoms. During this
 259 process, IM2 is also formed. As there exists attraction between the oxygen atom (O1)
 260 of the ionic liquid and the hydrogen atom (H7) of methanol, a hydrogen bond is formed
 261 between the two atoms. During this process, IM2 transforms to TS1. After TS1
 262 formed, the attraction between the oxygen atom (O1) and hydrogen atom (H7) is
 263 strengthened, the hydrogen atom (H7) has the trend of movement from O8 to O1, so
 264 the bond between the hydrogen atom (H7) and the oxygen atom (O8) becomes an
 265 imaginary bond. At the same time, the attraction between the oxygen atom (O4) and
 266 hydrogen atom (H3) is strengthened, the hydrogen atom (H3) has the trend of
 267 movement from O2 to O4, so the bond between the hydrogen atom (H3) and the oxygen
 268 atom (O2) becomes an imaginary bond. With the continuous movement of hydrogen

269 atom (H3) from O2 to O4, the interaction between H3 and O4 becomes stronger, which
270 makes the interaction between O4 and C5 becomes weaker, so the double bond between
271 O4 and C5 becomes a single bond. As a result, the interaction between C5 and O8
272 becomes stronger, so the imaginary bond between the two atoms becomes a single bond.
273 These processes lead the transformation of the structure from TS1 to IM3, and the
274 tetrahedral structure centered on carbon atom (C5) is also formed. With the movement
275 of hydrogen atom (H3) in space, the atom H3 has interaction with the oxygen atom
276 (O8), and there exists a hydrogen bond between the two atoms. This is also the
277 transformation of IM3 to TS2. Due to the attraction of O6 is strengthened, the
278 interaction between O2 and H3 is disappeared, and the bond between the two atoms is
279 broken. Besides, the bond between H3 and O4 becomes an imaginary bond. At the same
280 time, the bond between O6 and C5 becomes an imaginary bond. After the imaginary
281 bonds are broken in TS2, the fatty acid methyl ester and glycerol are produced. The
282 reaction pathway catalyzed by the other two ionic liquid [HSO₃-Bmim][HSO₄] and
283 [Bmim][H₂PO₄] is similar with that of [Bmim][HSO₄].

284 3.2.2 Optimization of IMs and TSs

285 Based on the reaction pathway above, the structures of IMs and TSs in
286 transesterification catalyzed by [Bmim][HSO₄], [HSO₃-Bmim][HSO₄] and
287 [Bmim][H₂PO₄] were optimized. The results are shown in Fig. 8, Fig. 9 and Fig. 10. As
288 Fig. 8 shows, in IM1, there exists a hydrogen bond between the hydrogen atom (H31)
289 from the ionic liquid and oxygen atom (O29) of carbonyl from MAG. The bond length
290 of hydrogen bonds is 1.773 Å, and the bond order is 0.1. The results reveal that the
291 hydrogen bond is weak. In IM2, after the methanol participates in the action, a hydrogen
292 bond appears between the hydrogen atom (H26) from methanol and the oxygen atom
293 (O25) from the ionic liquid. The bond length is 1.877 Å, and the bond order is 0.5,
294 which means the bond is weak. Due to the influence of methanol, the hydrogen bond
295 between H31 and O29 decrease to 1.748 Å, and the bond order increases to 0.5. The
296 phenomenon shows that the distance between H31 and O29 is shorten, and the

297 interaction between the two atoms is strengthening.
298 After the geometry changes to TS1, the length of hydrogen bond between H31 and O29
299 decreases to 1.375 Å, and the bond order is 0.5. The length of bond between H31 and
300 O23 increases from 0.995 Å to 1.093 Å. The phenomena demonstrate the hydrogen
301 atom H31 is transforming from O23 to O29, but the hydrogen bond between H31 and
302 O29 is not strong enough. Apart from this, the length of hydrogen bond between H26
303 and O25 decreases to 1.591 Å, and the bond between H26 and O49 increases from
304 0.995 Å to 1.012 Å. The bond orders of the two bonds are 1.0 and 0.5 respectively. This
305 indicates the hydrogen atom H26 is transforming from O49 to O25. After the geometry
306 of TS1 was optimized, a frequency of 238.68 cm^{-1} was obtained. The frequency is
307 corresponding with vibration of the movement of H31 from O23 to O29.



308
309

Fig. 8 IMs and TSs in transesterification catalyzed by [Bmim][HSO₄]

310 With the further movement of H31 from O31 to O29, and H26 from O49 to O25, the
311 geometry changes to IM3. In IM3, the length of hydrogen bond between hydrogen atom
312 H31 and oxygen atom O23 is 1.864 Å, and the bond order is 0.5. The length of bond
313 between H31 and O29 is 0.982, and the bond order is 1.0. This shows the bond between
314 H31 and O29 is strong, and the atom H31 has escaped the attraction of O23. Apart from
315 this, the distance between hydrogen atom H26 and oxygen atom O49 increases to 2.475
316 Å, while the bond between H26 and O25 is 0.992 Å, and the bond order is 1.0. This
317 demonstrates the hydrogen atom H26 has escaped the attraction of O49, and has formed
318 a strong bond with O25. Besides, a hydrogen bond between H26 and O30 appears. The

319 length of bond between the two atoms is 1.765 Å, and the bond order is 0.5, which
320 means the hydrogen bond is weak. At the same time, a bond between oxygen atom O49
321 and carbon atom C28 formed. The length of the bond is 1.398 Å, and the bond order is
322 1.0. This indicates the bond is strong enough, and the tetrahedral structure has
323 established.

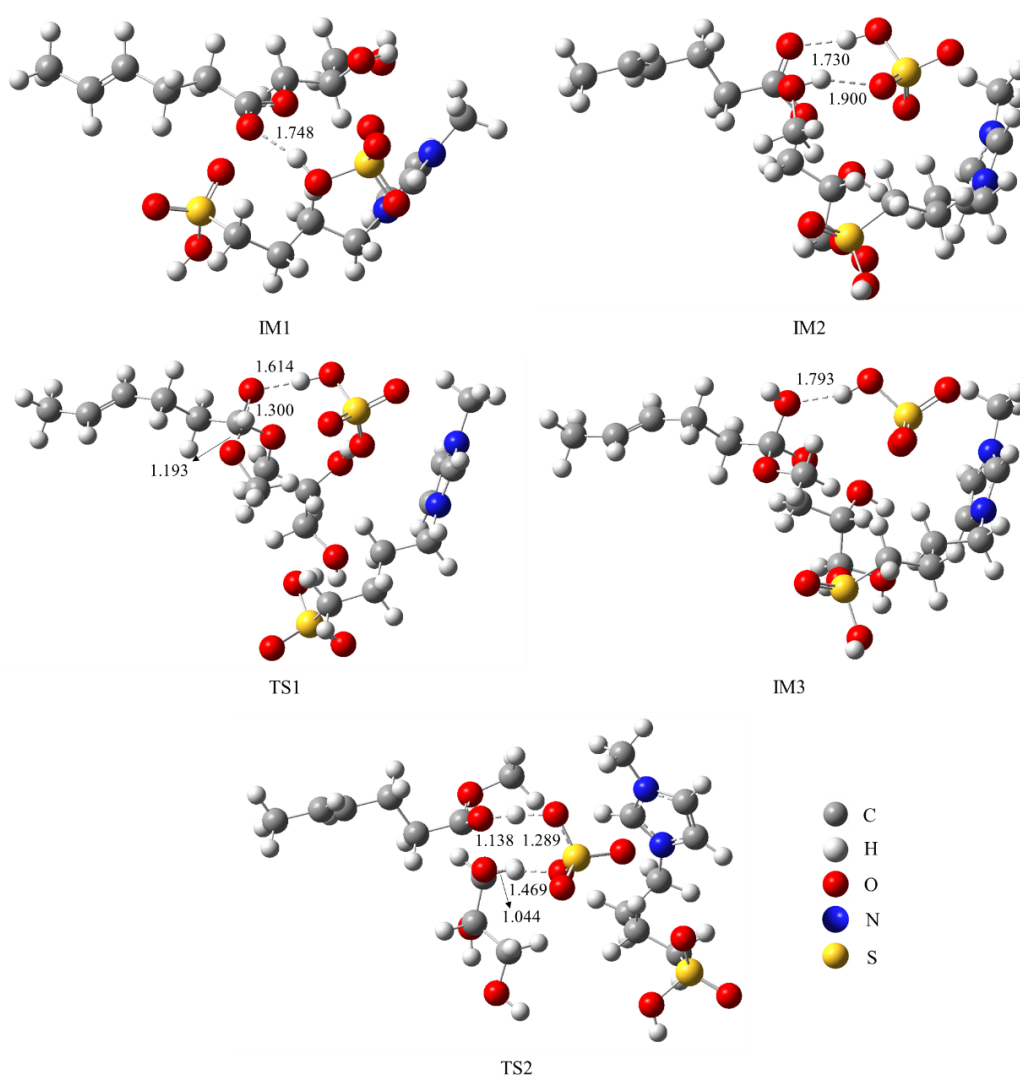


Fig. 9 IMs and TSs in transesterification catalyzed by [HSO₃-Bmim][HSO₄]

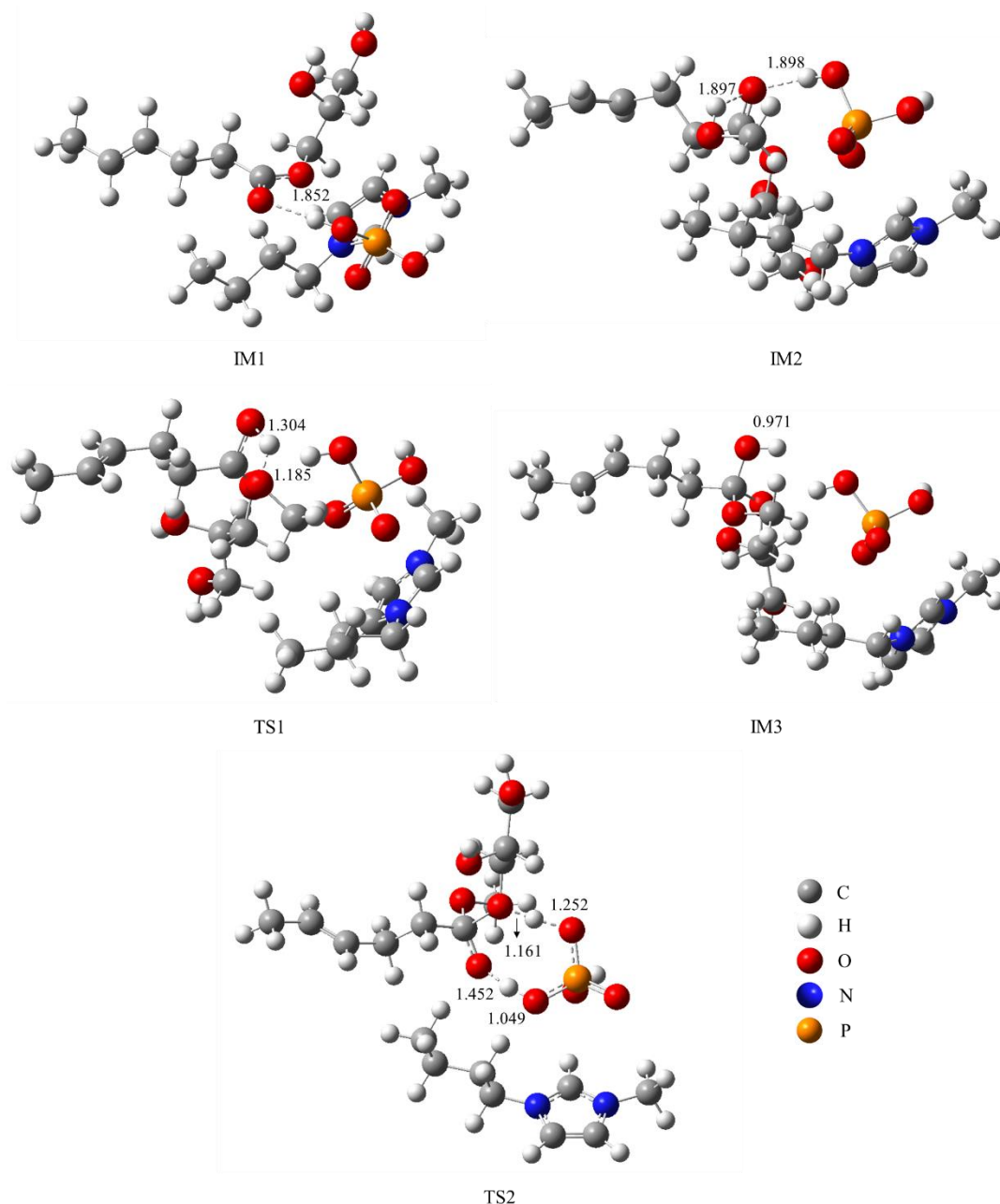


Fig. 10 IMs and TSs in transesterification catalyzed by [Bmim][H₂PO₄]

326
 327
 328 In TS2, the length of hydrogen bond between hydrogen atom H31 and oxygen O23 is
 329 1.469 Å, and the length of hydrogen bond between hydrogen atom H31 and oxygen
 330 O29 is 1.052 Å. The bond orders of the two bonds are both 0.5. The results mean the
 331 bonds are not strong enough, and the hydrogen atom H31 has the trend of movement
 332 from O29 to O23. Apart from this, the length of hydrogen bond between the hydrogen
 333 atom H26 and oxygen atom O25 increases to 1.598 Å, and the length of hydrogen bond
 334 between the H26 and O30 decreases to 1.017 Å. The bond orders of the two bonds are
 335 both 0.5. This indicates the hydrogen atom H26 has the trend of movement from O25

336 to O30. Besides, the bond between O30 and C28 is broken. When the TS2 is optimized,
 337 a frequency of 202.46 icm^{-1} is obtained. The frequency is corresponding with vibration
 338 of the movement of H31 from O29 to O23, H26 from O25 to O30 and the departure of
 339 O30 from C28. The vibration is exactly the generation path of fatty acid methyl ester
 340 and glycerol.

341 Fig. 9 and Fig. 10 are the structures of IMs and TSs in transesterification catalyzed by
 342 $[\text{HSO}_3\text{-Bmim}][\text{HSO}_4]$ and $[\text{Bmim}][\text{H}_2\text{PO}_4]$, the reaction processes are similar with that
 343 catalyzed by $[\text{Bmim}][\text{HSO}_4]$. The imaginary frequency of TS1 and TS2 catalyzed by
 344 the three ionic liquids is shown in Table 3.

345 Table 3 Imaginary frequency of TS1 and TS2 catalyzed by the three ionic liquids (icm^{-1})

	$[\text{Bmim}][\text{HSO}_4]$	$[\text{HSO}_3\text{-Bmim}][\text{HSO}_4]$	$[\text{Bmim}][\text{H}_2\text{PO}_4]$
TS1	238.68	256.43	194.84
TS2	202.46	435.76	521.16

346

347 3.2.3 Analysis of Gibbs free energy

348 After all the geometry of IMs and TSs was optimized, the frequency of each IMs and
 349 TSs was calculated. Then the Gibbs free energy was obtained. The results are shown in
 350 Table 4.

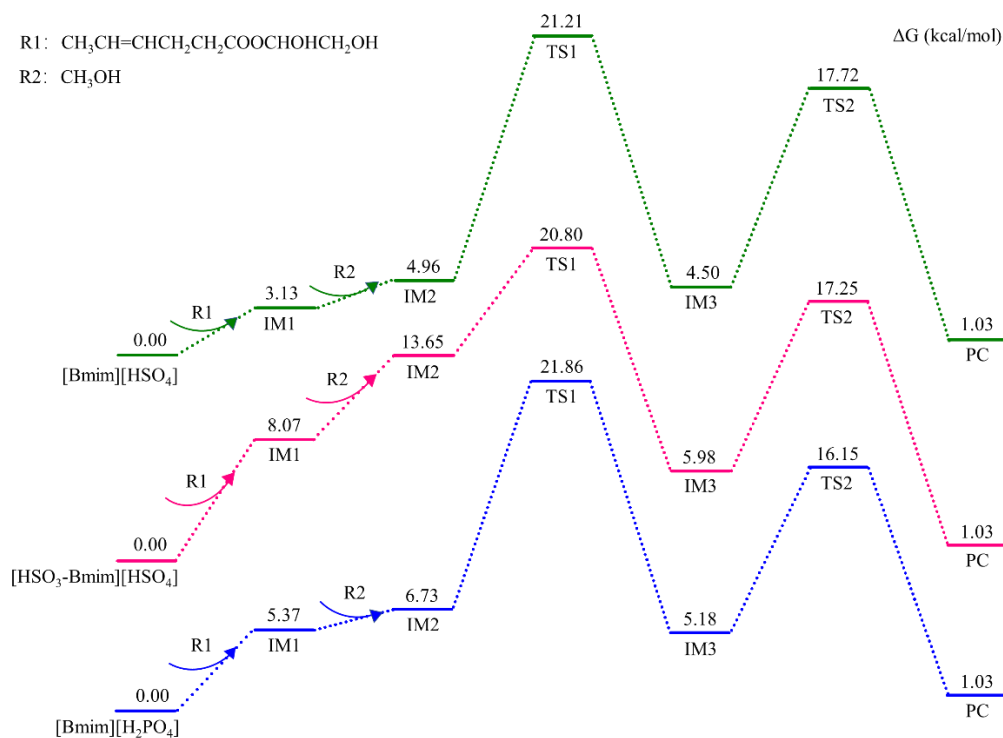
351 Table 4 Gibbs free energy of each phase in transesterification catalyzed by three ionic liquids (Hartree)

	$[\text{Bmim}][\text{HSO}_4]$	$[\text{HSO}_3\text{-Bmim}][\text{HSO}_4]$	$[\text{Bmim}][\text{H}_2\text{PO}_4]$
R1	-653.19	-653.19	-653.19
R2	-115.67	-115.67	-115.67
IM1	-1775.92	-2399.69	-1719.83
IM2	-1891.58	-2515.35	-1835.50
TS1	-1891.56	-2515.33	-1835.48
IM3	-1891.59	-2515.36	-1835.51
TS2	-1891.57	-2515.32	-1835.49
Product	-424.21	-424.21	-424.21
$\text{CH}_2\text{OHCHOHCH}_2\text{OH}$	-344.65	-344.65	-344.65

R1: $\text{CH}_3\text{CH}=\text{CHCH}_2\text{CH}_2\text{COOCHOHCH}_2\text{OH}$

R2: CH₃OHProduct: CH₃CH=CHCH₂CH₂COOCH₃

352 Based on the calculation results in Table 4, use the same treatment as in section 3.1.3
 353 for Gibbs free energy of each IMs and TSs. The calculation results are shown in Fig.
 354 11.



355

356 Fig. 11 Gibbs free energy in each phase of transesterification catalyzed by three ionic liquids

357 According to Murdoch[31], it is obvious that the processes of transesterification can be
 358 divided into two period, one is ionic liquid to IM3, and another is IM3 to PC. The two
 359 periods contain two energy barriers, one is ionic liquid to TS1 and another is IM3 to
 360 TS2. It can be easily found that the energy barrier of ionic liquid to TS1 is much higher
 361 than that of IM3 to TS2, so the process of ionic liquid to TS1 is the rate-limiting step.
 362 After calculation, the ΔG_{\max} of transesterification catalyzed by [Bmim][HSO₄], [HSO₃-
 363 Bmim][HSO₄] and [Bmim][H₂PO₄] are 21.21 kcal/mol, 20.80 kcal/mol and 21.86
 364 kcal/mol, respectively. The results indicate that the ΔG_{\max} of transesterification
 365 catalyzed by [HSO₃-Bmim][HSO₄] is the lowest, and [Bmim][H₂PO₄] is the highest.
 366 The calculation results reveals [HSO₃-Bmim][HSO₄] and [Bmim][H₂PO₄] has the best
 367 the worst catalytic effects in transesterification reactions. The DFT results consistent

368 with the experimental results and other DFT research[8, 32].

369 **4.Conclusions**

370 Based on DFT calculations, the catalytic mechanism of esterification and
371 transesterification by acidic imidazolium ionic liquid [Bmim][HSO₄], [HSO₃-
372 Bmim][HSO₄] and [Bmim][H₂PO₄] was discussed. The reaction pathways of
373 transesterification and transesterification catalyzed by three acidic ionic liquids were
374 proposed. Three intermediates and two transition states were found to be contained in
375 both of the pathways. The intermediates and transition states in each reaction phase
376 were optimized and verified by frequency calculations and intrinsic reaction coordinate
377 (IRC) calculations. The Gibbs free energy of the intermediates and transition states in
378 each reaction phase was then calculated. By analyzing the variation of Gibbs free
379 energy along the reaction pathway, it was found that the esterification contained one
380 period, and the rate-limiting step was IM2 to TS1. The transesterification contained two
381 periods, and the rate-limiting step was ionic liquid to TS1. Based on the results above,
382 the energy barrier of each reaction was obtained. It showed that the esterification
383 reaction catalyzed by [Bmim][HSO₄] had the minimum energy barrier of 37.77
384 kcal/mol, and the reaction catalyzed by [Bmim][H₂PO₄] had the maximum energy
385 barrier of 49.34 kcal/mol. The energy barrier results revealed [Bmim][HSO₄] had the
386 best catalytic effect in esterification. As for transesterification reactions, the reaction
387 catalyzed by [HSO₃-Bmim][HSO₄] had the minimum energy barrier of 20.80 kcal/mol,
388 and the reaction catalyzed by [Bmim][H₂PO₄] had the maximum energy barrier of 21.86
389 kcal/mol, indicating [HSO₃-Bmim][HSO₄] had the best catalytic effect in
390 transesterification. All the calculation conclusion were consistent with previous
391 experimental results. On the other hand, the results also validate the correction of the
392 proposed reaction pathways. The validated catalytic mechanism will provide a new idea
393 for subsequent optimization of imidazolium ionic liquid structure to improve their
394 catalytic efficiency in biodiesel production from oleaginous yeast.

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