

Article Smart Dimmable LED Lighting Systems

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Abstract: This paper proposes energy-efficient solutions for the smart light-emitting diode (LED) 1 lighting system, which provides minimal energy consumption while simultaneously satisfies il-2 luminance requirements of the users' in typical office space. Besides artificial light received from dimmable LED lamps, natural daylight coming from external sources, such as windows, is considered as a source of illumination in indoor environment. In order to reduce total energy consumption, the smart LED system has the possibility to dim LED lamps resulting in reduced LED output power. Additionally, various LED lamps functionality, such as semi-angle of the half illuminance and LED 7 tilting, are introduced as an additional parameter to be optimized to achieve greater energy saving of 8 the designed system. In order to properly exploit external lighting, the idea to reduce overall daylight intensity at users' location is realized by option to dim the windows by a shading factor. Based on the 10 users' requirements for minimal and desired level of illumination, proposed optimization problems 11 can be solved by implementing different optimization algorithms. Obtained solutions are in charge 12 to give instructions to smart LED system to manage and control system parameters (LEDs dimming 13 levels, semi-angles of the half illuminance, orientation of LEDs, the shading factor) in order to design 14 total illumination which ensures minimal energy consumption and users' satisfaction related to 15 illuminance requirements. 16

Keywords: Daylight, dimming, energy saving, illuminance design, users' requirements, smart LED lighting systems.

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1. Introduction

Based on recent studies on modern society and nowadays lifestyle, people spend 20 more than 70 % of the daytime in indoor environments, especially in developed countries 21 [2–4]. In indoor environments, such as offices and homes, the illumination is mostly 22 provided by lighting systems based on light-emitting diodes (LEDs) due to long lifetime 23 and good quality of light. According to many analysis and statistics, about 20 % of global 24 electric energy usage is used for lighting, with tendency to be increased to 40 % in the 25 future [5–7]. As modern commercial and industry markets aim to achieve energy savings as much as possible, the smart LED lighting systems have received attention in both 27 research communities and industry as an efficient way of energy conservation. Offering a 28 modern, persistent, and energy-efficient method of illumination, the smart lighting market 29 is predicted to exceed 47 billion \$ in next 10 years [8].

Besides minimal energy consumption, the smart LED systems aim to improve the comfort of users and satisfy their requirements related to level of illumination at a certain 32

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Copyright: © 2022 by the authors. Submitted to *Journal Not Specified* for possible open access publication under the terms and conditions of the Creative Commons Attribution (CC BY) license (https://creativecommons.org/licenses/by/4.0/). locations. For example, since people spend large part of the daytime in the offices, it is 33 beneficial to ensure a comfort environment during the working hours in order to avoid 34 poor performance as a result of an inappropriate level of light [9]. In practice, the design 35 of overall illumination in indoor environments can be quite complicated and challenging 36 since users' demands for certain level of light are very personal, subjective and frequently 37 changing. With development of different indoor wireless technologies, modern Internet of 38 Things (IoT) applications are able to provide the information about occupant preferences, 39 presence and current illumination levels, which can be beneficial for a smart LED systems 40 architecture to perform illumination optimization and reduce energy consumption. 41

Many recent studies analyzed low energy efficiency and high user comfort within 42 smart LED systems in different scenarios [10–20]. More precisely, [10–13] considered 43 the smart LED systems with optimal dimming feature, capable of controlling optical 44 LED output power, with the aim to achieve maximal energy savings while satisfying 45 users' comfort at the same time. Furthermore, besides artificial LED light, the indoor environments are also illuminated by external sources of light from different objects, e.g., 47 windows, resulting in daylight illumination. Since daylight represents an important part of the total illumination in most of the indoor spaces, it should also be taken into account 49 during the design of the smart LED systems. Optimization problems of reducing total energy consumption of smart LED systems with daylight taken into account were analyzed 51 in [14–18]. 52

Complete surveys of the smart lighting systems were presented in [19,20]. A detailed 53 state-of-the-art of the smart lighting systems is given in [19], but mostly focusing on 54 industrial area. Besides detailed literature overview of the same topic, [20] introduced a 55 new machine learning application within smart lighting to improve user comfort. 56

Inspired by aforementioned, the aim of this paper is to establish an efficient strat-57 egy to reduce total energy consumption of the smart user-centric LED lighting system 58 implemented in indoor office space. The possibility to dim each LED lamp is introduced 59 in order to control the artificial illumination and to provide energy savings. This way, 60 illuminance contribution in the room can be managed by determined, optimized dimming 61 levels of LEDs, while minimizing total energy consumption of the smart LED system, 62 simultaneously satisfying users' requirements for illumination. Furthermore, different 63 functionalities of the LED lamp are identified as a potential parameter to be optimized 64 in order to minimize energy consumption of the designed smart LED system and/or to 65 satisfy users' requirements for illumination. To the best of authors' knowledge, for the first 66 time, the possibility to optimize the semi-angle at the half-illuminance of LED, and later the LED tilting in terms of LED orientation, are included. The expanded optimization problem 68 results in more efficient managing of the total illuminance in the room, while providing 69 better energy performance of the smart LED system. Additionally, the system model is 70 augmented by considering daylight contribution from the windows. Since commercial 71 tintable smart windows can be employed as a way to reduce and manage the daylight 72 contribution in indoor space [21–23], the optimization problem is expanded with respect to 73 shading factor, which is related to shading the windows and reducing the daylight contri-74 bution. Finally, after taking into account all optimization parameters, the total illuminance 75 contribution can be managed and controlled by smart LED system in the most effective 76 way to ensure the most convenient system performances. 77

The rest of the paper is organized as follows. Section II presents the system model 78 together with the LED illumination model. Problem formulation is established in Section 79 III, together with numerical results. Section IV considers a more general case when daylight 80 is taken into account. Section V gives some concluding remarks.

2. Smart Dimmable LED Lighting System Model

The considered scenario assumes an indoor office environment with rectangular-83 shaped floor area of dimensions $L_x \times L_y$ meters and height L_z meters. A smart LED lighting 84 system with N ceiling-mounted LED lamps is employed to illuminate the indoor floor 85

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plane. In order to provide energy saving, dimmable LED lamps are implemented, resulting in an artificial LED illumination in the room that is controlled by adjusting dimming levels 87 of each LED lamp. Dimmable ceiling-mounted LED lights are placed on a rectangular grid 88 $(N = N_x \times N_y)$ to illuminate the space, and their positions are considered to be fixed, and 89 known to the smart LED system. Each LED lamp consists of *l* LEDs photodiodes [24], thus the maximum transmitted optical power of a LED lamp equals to $P_t = lP_l$, where P_l is 91 transmitted optical power of a single LED lamp. Each LED covers certain circular coverage 92 area on a floor plane. An overlapping beam scenario is considered where users can be 93 covered by multiple LED beams. The floor plane is considered to be a horizontal plane 94 divided into $M(M = M_x \times M_y)$ grid points, each representing possible users' locations. 95 Figure 1a represents an example of the considered room model with LED lamps and grid 96 points positions, while Figure 1b depicts the considered 3D indoor office environment with 97 LEDs and possible users' locations. 98



Figure 1. Considered system model: (a) the grid model of the ceiling with the LED lamp positions (red dots); (b) 3D indoor office environment.

Since dimmable LED lamps are employed within the smart lighting system, the LED output power is related to the dimming vector **s** defined as

$$\mathbf{s} = [s_1, s_2, \dots, s_N]^T, \quad 0 \le s_i \le 1, \quad i = 1, 2, \dots, N,$$
(1)

where s_i represents the dimming level of the *i*-th LED lamp. The value $s_i = 0$ results in turning off the *i*-th LED, while the value $s_i = 1$ indicates that the *i*-th LED radiates at its maximum power P_t . Based on former, it follows that the output power of the *i*-th LED source is $P_i = s_i P_t$, where P_t is the maximum LED power assumed to be the same for all LEDs in the considered system.

The illumination vector \mathbf{z} , representing the illumination at the M points on the workspace plane, can be defined as as

$$\mathbf{z} = \begin{bmatrix} z_1, \dots, z_j, \dots, z_M \end{bmatrix}^T, \quad j = 1, 2, \dots, M,$$
(2)

where z_i is the illuminance at the *j*-th grid point.

First, it is assumed that the dimmable LED lighting system is the only source of light in the room, which leads to a simple linear model which relates the dimming vector \mathbf{s} and the resulting illumination on the task plane points \mathbf{z} as [10]

$$\mathbf{z} = \mathbf{H} \cdot \mathbf{s},\tag{3}$$

where **H** represents the illuminance $M \times N$ matrix with element h_{ji} (j = 1, 2, ..., M), i = 1051,2,..., N) that determines the illuminance at the *j*-th point when the *i*-th LED is fully 106 turned on $(s_i = 1)$, while all other LEDs are turned off $(s_j = 0 \text{ for } j \neq i, j = 1, 2, ..., N)$. 107



Figure 2. A LED illumination model.

Table 1. Values of *m* and I(0) based on semi-angle at the half-illuminance, $\Phi = 107.16$ lm

$\Phi_{1/2}[^0]$	т	I(0) [cd]
10	45.27	789.3
20	11.14	207.11
30	4.81	99.24
40	2.6	61.41
50	1.56	43.81
60	1	34.11
70	0.64	28.07
80	0.39	23.81

Clearly, the dimming vector **s** affects both illumination and energy consumption of the LED system.

LED illumination model: The illuminance at the *j*-th point when the *i*-th LED is set to maximum output power, while all other LEDs are turned off, is defined as [25–27]

$$h_{ji} = \frac{I(0)\cos^{m_i}(\theta_{ji})}{d_{ii}^2}\cos(\psi_{ji}),$$
(4)

where I(0) is the centre luminous intensity of the LED, θ_{ji} represents the angle of irradiance with respect to the axis normal to the ceiling, ψ_{ji} is the angle of incidence with respect to the axis normal to the working plane surface, and d_{ji} denotes the distance between the *i*-th LED and the *j*-th user position, as presented in Figure 2. The assumption that the LED and user plane surface are parallel is adopted, thus $\theta_{ji} = \psi_{ji}$. A LED lighting is described by a Lambertian radiation pattern with the order m_i defined as

$$m_i = -\frac{\ln 2}{\ln(\cos \Phi_{1/2,i})},\tag{5}$$

where $\Phi_{1/2,i}$ represents the semi-angle at the half-illuminance of the *i*-th LED. We consider that all LED lamps are characterized by the same semi-angle at the half-illuminance (i.e., $\Phi_{1/2,i} = \Phi_{1/2}$ and $m_i = m$ for all $i = , 1, \dots, N$).

Overall illumination in the room: Figures 3 and 4 present graphical examples of considered smart LED system applied to a typical office space with dimensions $L_x \times L_y \times L_z = 10 \times 10 \times 3$ meters with N = 25 dimmable ceiling-mounted LED lamps arranged as an $N_x \times N_y = 5 \times 5$ array. Each LED lamp consists of l = 100 LEDs, arranged as an 10×10 array. The number of grid points on the horizontal floor plane is adopted to be



(a) $\Phi_{1/2} = 20^0$ (b) $\Phi_{1/2} = 60^0$ Figure 3. Overall illumination of the system without LEDs dimming, $s_i = 1, i = 1, ..., N$.



(a) $\Phi_{1/2} = 20^0$ (b) $\Phi_{1/2} = 60^0$ Figure 4. Overall illumination a randomly selected dimming vector, $0 \le s_i \le 1, i = 1, ..., N$.

 $M = 100 \times 100 = 10000$. Moreover, we adopted the following model for LED output power, derived from the example presented in [25]. Input voltage of LED and input current are 6.42 V and 700 mA, respectively, resulting in the electrical power $P_e = 4.494$ W. The electrical/optical conversion efficiency is 0.101, the optical output power of each LED is $P_l = 0.452$ W, and the total luminous flux is $\Phi = 107.16$ lm. The values of LED system parameters defined above are adopted in the rest of the paper if otherwise is not stated.

The centre luminous intensity of LED, I(0), can be determined for different values of the semi-angle at the half-illuminance based on definition of the total luminous flux Φ [25]

$$\Phi = \frac{2\pi I(0)}{(1+m)}.$$
(6)

For constant total luminous flux ($\Phi = 107.16$ lm), based on (6), the centre luminous intensity of LED will be different for varios values of *m*, i.e., the semi-angle at the half-illuminance. The values of the parameter *I*(0) and parameter *m* for different values of semi-angle at the half-illuminance are given in Table I.

Taking all definitions and values of LED system parameters into account, overall 128 illumination in the room is simulated and presented in Figures 3 and 4. Figure 3 presents 129 scenario when all LED lamps are set to the maximum output power ($s_i = 1, i = 1, ..., N$), 130 which results in maximal energy consumption. Additionally, adopted values of the semi-131 angle at the half-illuminance are $\Phi_{1/2} = 20^0$ and $\Phi_{1/2} = 60^0$ in 3a and 3b, respectively. The 132 semi-angle determines the wideness of the optical beam at the LED lamp output. Lower 133 values of $\Phi_{1/2}$ results in narrower output optical beam. Figure 4 depicts the same system 134 scenario, but for randomly selected dimming levels of LED sources. It is obvious that the 135 dimming vector has significant impact on the overall distribution of the illumination in the 136 indoor environment. 137

3. Problem Formulation and Results

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The main aim of our work is to design the smart LED illumination system for *K* users residing in the horizontal workspace plane parallel to the ceiling. User devices are located at some of the previously defined grid points, thus their positions are known, based on an earlier estimation with any indoor positioning technique [28,29]. We tend to design an optimal LED illumination configuration which provides minimal energy consumption. In other words, the main purpose of our smart LED system is to design illumination vector **z** based on users' requirements by selecting optimized dimming vector **s**.

Problem 1 formulation: Find an optimal energy consumption by dimming vector s that satisfies users' illumination requirements at their locations.

The adopted scenario considers two types of users' illumination requirements: desired and minimal level of illumination. This means that the *j*-th user tends to be illuminated by a desired level of illumination r_j (i.e., $z_j \approx r_j$), as well as that it requires that the level of illumination at its position is not lower than minimal requirement l_j (i.e., $z_j \ge l_j$).

The vector of desired illuminance requirements for *K* users is defined as

$$\mathbf{r} = \begin{bmatrix} r_1, \dots, r_j, \dots, r_K \end{bmatrix}^T, \quad j = 1, 2, \dots, K,$$
(7)

while the vector of minimal illuminance requirements for K users is defined as

$$\mathbf{l} = \begin{bmatrix} l_1, \dots, l_j, \dots, l_K \end{bmatrix}^T, \quad j = 1, 2, \dots, K.$$
(8)

The optimal illumination vector $\mathbf{z} = \mathbf{H} \cdot \mathbf{s}$ will clearly depend on definition of user requirements, which should be satisfied. Note that for considered scenario with *K* users, the size of vector \mathbf{z} is now *K*, while the size of the illuminance matrix \mathbf{H} is $K \times N$.

Energy consumption of the smart LED system is related to the total system output power determined as $P_t \cdot \sum_{i=1}^{N} s_i$, where P_t is the maximum transmitted optical power of a LED lamp previously defined as $P_t = lP_l$. Dimming vector **s** affects both illumination configuration and energy consumption, which means that the energy consumption of designed smart LED system is directly and linearly related to the ℓ_1 -norm of vector **s**, i.e., $||\mathbf{s}||_1 = \sum_{i=1}^{N} s_i$.

In order to have insight of the energy saving contribution, the energy saving factor *G* is defined as a ratio between the total consumed power of designed system and the total system output power when all LEDs are fully turned on, i.e.,

$$G = \frac{P_t ||\mathbf{s}||_1}{P_t N} = \frac{||\mathbf{s}||_1}{N}.$$
(9)

Favouring solutions with lower G, i.e., smaller $||\mathbf{s}||_1$, leads to reduced energy consumption. 161

In order to optimize dimming vector **s**, the optimization problem for considered smart LED scenario is formulated as

$$\begin{array}{ll} \underset{\mathbf{s}}{\text{minimize}} & \|\mathbf{s}\|_{1} + \lambda \|\mathbf{H} \cdot \mathbf{s} - \mathbf{r}\| \\ \text{subject to} & \mathbf{H} \cdot \mathbf{s} \ge \mathbf{l} \\ & 0 \le \mathbf{s} \le 1, \ \mathbf{s} \in \mathbb{R}^{N} \end{array}$$
(10)

where parameter λ ($0 \le \lambda \le 1$) sets the priority by tuning the relative importance of the minimizing energy consumption and satisfying users' requirements, and **H** represents the illuminance $K \times N$ matrix with elements h_{ji} (j = 1, 2, ..., K, i = 1, 2, ..., N) defined in (4). The optimization proposed problem in (10) can be efficiently solved in software package MATLAB.

Results: Figure 5 depicts the illumination distribution when K = 10 users with known positions are placed randomly in the office. The semi-angle at half-illuminance is $\Phi_{1/2} = 60^0$, and smart LED system employs $N = 3 \times 3$ LED lamps. Desired and minimal illuminance requirements are the same for all users and equal to $r_i = 600$ and $l_i = 300$ lux for j = 1, 2, ..., K, respectively. In Fig. 5a, the priority parameter is $\lambda = 0.01$ meaning that 171 the primary task is to reduce total energy consumption. Two of nine LEDs are turned off, 172 while seven LEDs are turned on and dimmed to give a certain level of illumination with 173 maximal possible energy savings. The energy saving factor is G = 0.44 for this scenario. 174 The illumination distribution of the same system with $\lambda = 0.5$ is presented in Fig. 5b, 175 pointing that the satisfaction of the users' requirements has priority over energy savings. 176 In this case, even five of nine LEDs are fully turned on and the energy saving factor is 177 G = 0.92.178

Based on the results presented in Figs. 5a and 5b, it can be concluded that *G* is significantly higher in Fig. 5b resulting in more power consumption. Still, the level of illumination on users' position is close to the desired level, so the users' illumination requirements will be fulfilled to great extent. By tuning the priority parameter λ , the compromise between energy saving and satisfaction of illumination requirements can be achieved.



(a) $\lambda = 0.01, G = 0.44, \Phi_{1/2} = 60^0$ (b) $\lambda =$ **Figure 5.** Solution of the Problem 1 defined in (10).

3.1. Effect of the Optical Signals Reflections

The previous illumination model is based on the direct Line of Sight (LoS) propagation model between LEDs and users' devices. Still, optical signals will be reflected from surrounding surfaces in indoor environments, which will have an impact on the overall illumination in the room. From the *i*-th LED lamp, light can reach the *j*-th grid point after number of reflections. In order to apply a more general illumination model that takes into account both LoS and diffuse reflection components, we adopt a recursive method presented in [30].

After multiple reflections, the illumination at the *j*-th grid point from the fully turned on *i*-th LED lamp (while all other LEDs are turned off) can be expressed as [30]

$$a_{ji} = \sum_{k=0}^{\infty} h_{ji}^{(k)},$$
 (11)

where $h_{ii}^{(k)}$ is the illumination component after exactly *k* reflections.

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When k = 0, i.e., for direct LoS component at the *j*-th grid point from the *i*-th LED lamp, the illuminance component was previously defined in (4) as

$$h_{ji}^{(0)} = \frac{I(0)\cos^{m}(\theta_{ji})}{\rho_{ji}^{2}}\cos(\psi_{ji}).$$
(12)

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For k > 0, the illumination component $h_{ii}^{(k)}$ can be determined recursively as

$$h_{ji}^{(k)} = \int_{i} \rho_{ref} h_{ji}^{(0)} * h_{ji}^{(k-1)},$$
(13)

where the symbol * represents convolution and ρ_{ref} is the reflection coefficient dependent on the surface material. Note that, for the *k*-th reflection, the lighting source is the receiving point of the previous (k - 1)-th reflection, and so on.

Based on the presented recursive method [30], we simulated the overall illumination 197 in the room by taking into account the direct LoS component (k = 0) and the first reflected 198 component (k = 1) from the walls, i.e., only the first two terms of the summation in (11). 199 Other reflections are ignored. The reflection coefficient takes a value $\rho_{ref} = 0.8$. For the 200 same system configuration as in Figure 3, the overall illumination in the room considering 201 k = 0 and k = 1 components, as well as the illumination only from k = 1 component, 202 is presented in Figures 6 and 7, when the semi-angle is $\Phi_{1/2} = 20^0$ and $\Phi_{1/2} = 60^0$, 203 respectively. From the presented results, it can be concluded that that the first reflection has 204 important impact only near the walls in the indoor environments, and for higher values of 205 the semi-angle. 206



(a) Joint illumination for k = 0 and k = 1. (b) Illumination only for k = 1. Figure 6. Overall illumination when $s_i = 1 \forall i, \Phi_{1/2} = 20^0$.



(a) Joint illumination for k = 0 and k = 1. (b) Illumination only for k = 1. Figure 7. Overall illumination when $s_i = 1 \forall i, \Phi_{1/2} = 60^0$.

Next, the same problem defined in (10) is solved, but the illuminance matrix H is 207 determined by the elements h_{ii} (j = 1, 2, ..., K, i = 1, 2, ..., N) defined in (11) while 208 taking only the first two terms of the summations into account (direct (k = 0) and the first 209 reflected component (k = 1). Comparing results from Figures 5 and 8, it can be concluded 210 that the first reflection reduces the energy saving factor G and that contributes to the energy 211 consumption to a some extent. Still, the main conclusion is not changed if the illumination 212 model is based only on the direct LoS components; thus in the following analysis, we will 213 ignore the reflections. 214



(a) $\lambda = 0.01$, G = 0.36, $\Phi_{1/2} = 60^0$ (b) $\lambda = 0.5$, G = 0.75, $\Phi_{1/2} = 60^0$ **Figure 8.** The solution of the Problem 1 defined in (10) while taking into account the direct LoS and the first reflection.

3.2. The semi-angle at the half-illuminance of optimization problem

In order to minimize energy consumption and satisfy illuminance requirements, optimization problem in (10) can be expanded by considering the semi-angle at the halfilluminance of LEDs. Using beam-shaping lenses or different co-centric LEDs, the smart lightning system can implement the LEDs with tunable semi-angles.

With the assumption that lenses implemented at each LED transmitter can be managed, the semi-angle at the half-illuminance can take several discrete values (e.g., 20° , 40° , 60° or 80°), i.e.,

$$\Phi_{1/2} = [\phi_1, \phi_2, \dots, \phi_N], \quad \phi_i \in \{20^\circ, 40^\circ, 60^\circ, 80^\circ\}, \quad i = 1, 2, \dots, N.$$
(14)

Recall that the semi-angle at the half-illuminance affects the order *m* of a Lambertian radiation pattern and the centre luminous intensity of LED, I(0) (see (5 and (6)). For constant total luminous flux $\Phi = 107.16$ lm, the values of the parameters I(0) and *m* for different values of semi-angle can be found in Table I.

Problem 2 formulation: Minimise energy consumption by dimming vector s and the224semi-angle $\Phi_{1/2}$ while satisfying users' illumination requirements at their locations.224

If we consider the illumination propagation model in (4), the value of the semi-angle affects both the order *m* and the centre luminous intensity and thus has impact on the illuminance matrix **H**. In order to optimize both dimming vector **s** and semi-angle $\Phi_{1/2}$, the optimization problem becomes discrete and non-convex:

$$\begin{array}{ll} \underset{\mathbf{s}, \Phi_{1/2}}{\text{minimize}} & \|\mathbf{s}\|_1 + \lambda \|\mathbf{H} \cdot \mathbf{s} - \mathbf{r}\| \\ \text{subject to} & \mathbf{H} \cdot \mathbf{s} \ge \mathbf{l} \\ & 0 \le \mathbf{s} \le 1, \ \mathbf{s} \in \mathbb{R}^N \\ & 0 \le \Phi_{1/2} \le \pi/2 \end{array}$$
(15)

For a limited number of discrete semi-angles, the optimization problem in (15) can be solved in MATLAB.

Results: Figure 9 shows the illumination distribution when K = 10 and the smart LED system employs $N = 3 \times 3$ LED lamps, of the optimisation solution of (15), i.e., when the 229 discrete semi-angle values for each LED are $\phi_i \in \{20^\circ, 40^\circ, 60^\circ\}$. In order to see if there is 230 a benefit in expanding the optimization problem, we compare Figures 5 and 9. Note that 231 both figures show the results with the same scenario, only with and without possibility to optimze the semi-angle is added. Comparing results in Figures 5a and 9a, when $\lambda = 0.01$ 233 meaning that the primary task is energy saving, it can be concluded that energy saving 234 factor *G* is reduced from G = 0.44 to G = 0.31. From Figures 5b and 9b it can be observed 235 that a greater reduction of energy consumption is achieved when the priority parameter 236 $\lambda = 0.5$ since the energy saving factor *G* is reduced from G = 0.92 to G = 0.61. 237



(a) $\lambda = 0.01$, G= 0.31. (b) $\lambda = 0.5$, G = 0.61. Figure 9. Solution of the Problem 2 defined in (15).



Figure 10. LED rotation coordinates

Based on the results presented in Figures 5 and 9, it can be concluded that a significant energy saving can be achieved by introducing the option of multiple semi-angle choices, at the expense of the system complexity due to employment of the beam-shaping lenses or different co-centric LEDs.

3.3. LED tilting

With aim to further reduce energy consumption and/or to satisfy illuminance re-243 quirements, the optimization problem can be posed in terms of LED lamps tilting. It is 244 assumed that each LED can be tilted by a certain angle in the room coordinate system. The 245 orientation of the LED tilt in 3D is determined by two angles: the zenith angle, ρ , and the 246 azimuth angle, ε . The zenith angle ρ ($-\pi/2 \le \rho \le \pi/2$) corresponds to LED deviation in 247 relation to the z-plane. The azimuth angle ($0 \le \varepsilon \le 2\pi$) represents the deviation in relation 248 to the x-plane, i.e., it is the angle between the positive part of the x-axis and the projection 249 on the x-y plane. 250

If the LED lamp coordinates¹ are LED(x, y, z) (note that $z = L_z$ is the height), the projection of the LED on x-y plane is given as LED(x, y, 0). If it is assumed that the LED is tilted by the angles $-\pi/2 \le \rho \le \pi/2$ and $0 \le \varepsilon \le 2\pi$, the projection of the rotated LED 253

¹ The indexes *i* and *j* are omitted since the presented analysis is general and valid for all pairs of LED and grid points.



(c) $\rho = 30^{0}$, $\varepsilon = 180^{0}$ (d) $\rho = 30^{0}$, $\varepsilon = 270^{0}$ Figure 11. Overall illumination with LEDs tilting for $s_{i} = 1 \forall i, \Phi_{1/2} = 20^{0}, \rho = 30^{0}$.

axis (the height of the cone of LED lighting) on x-y plane is $\text{LED}'(x_1, y_1, 0)$. The distance 254 between LED and LED' on x-y plane is determined as $r = L_z \tan(\rho)$ (see Figure 10). 255

Since the coordinates of LED locations (x, y, 0) are known, the coordinates $LED'(x_1, y_1, 0)$ can be determined as

$$x_1 = x + L_z \tan(\rho) \cos(\varepsilon),$$

$$y_1 = y + L_z \tan(\rho) \sin(\varepsilon).$$
(16)

Note that the grid point coordinate $GP(x_g, y_g, 0)$ are also known. Finally, based on the geometry of the system setup presented in Figure 10, the angle of irradiance can be determined as

$$cos(\theta) = \frac{d^2 + b^2 - c^2}{2db}, \quad \text{for} \quad c^2 > d^2 + b^2 \ (\theta \le \pi/2), \\
d = \sqrt{L_z^2 + (x_g - x)^2 + (y_g - y)^2}, \\
b = \sqrt{L_z^2 + (x_1 - x)^2 + (y_1 - y)^2}, \\
c = \sqrt{(x_1 - x_g)^2 + (y_1 - y_g)^2}.$$
(17)

If the LEDs tilting is implemented within the smart lighting system, then the elements h_{ji} of the illuminance matrix **H** are defined in (4), but the cosine of the angle of irradiance, $\cos(\theta_{ji})$, is determined by (17), while the angle of incidence, ψ_{ji} , is related to the receiver characteristics and can be determined as

$$\cos(\psi_{ji}) = \frac{L_z}{d_{ji}},\tag{18}$$



Figure 12. Overall illumination with LEDs tilting for $s_i = 1 \ \forall i, \Phi_{1/2} = 20^0, \varepsilon = 0^0$.

where d_{ii} is defined in (17).

The overall illumination for the systems with the same configuration as in Figure 257 3a (without LEDs dimming, the semi-angle is $\Phi_{1/2} = 20^{\circ}$) is presented in Figures 11 258 and 12, considering different zenith and azimuth angels. Figure 11 represents the overall 259 illumination in the room, for constant zenith angle, $\rho = 30^{0}$, while the azimuth angle is 260 $\varepsilon = 0^0$, $\varepsilon = 90^0$, $\varepsilon = 180^0$ and $\varepsilon = 270^0$. On the other hand, Figure 12 shows the overall 261 illumination for constant azimuth angle, $\varepsilon = 90^{\circ}$, while the zenith angle is $\rho = 20^{\circ}$, $\rho = 40^{\circ}$, 262 $\rho = 60^{\circ}$ and $\rho = 80^{\circ}$. Based on the presented results, it is proved that the geometric analysis 263 of tilted LED system is correct and affects overall illumination in the indoor space. 264

Problem 3 formulation: Minimise energy consumption by dimming vector **s** and the tilting angles of LEDs, while satisfying user illumination requirements. 265

By introducing the possibility to tilt the LEDs, the optimization problem in (10) can be expanded by considering different LED orientations. Since the orientation of the LEDs will affect the illuminace matrix **H**, the optimization problem is now updated as

$$\begin{array}{ll} \underset{\mathbf{s},(\rho,\varepsilon)}{\text{minimize}} & \|\mathbf{s}\|_{1} + \lambda \|\mathbf{H} \cdot \mathbf{s} - \mathbf{r}\| \\ \text{subject to} & \mathbf{H} \cdot \mathbf{s} \geq \mathbf{l} \\ & 0 \leq \mathbf{s} \leq 1, \ \mathbf{s} \in \mathbb{R}^{N} & \cdot \\ & -\pi/2 \leq \rho \leq \pi/2 \\ & 0/2 \leq \varepsilon \leq 2\pi \end{array}$$
(19)

(19) can be solved using MATLAB.

Results: Figure 13 presents the illumination distribution obtained by the solution of (19) for the same system configuration as in Figure 5. In the presented example, we considered three possible orientations of LEDs, defined by the pairs of the zenith and



(a) $\lambda = 0.01$, G= 0.42. (b) $\lambda = 0.5$, G Figure 13. Solution of the Problem 3 defined in (19).

azimuth angles as $(\rho_i, \varepsilon_i) \in \{(0,0), (30,0), (30,180)\}$. Based on the results in Figure 5a for 271 the system without LED tilting, and results in Figure 9a for the system when LED tilting 272 is employed, it can be concluded that energy saving can be achieved by introducing the 273 possibility of different LEDs orientations. The energy saving is greater when $\lambda = 0.5$, which 274 means that the LEDs tilting can provide energy saving while satisfying users' requirements. 275 Note that the significant energy savings can be obtained with adding more options for 276 LEDs orientation (this example considered only 3 options due to implemented optimization 277 algorithm complexity), but at the expense of the system design complexity. 278

4. Effects of External Daylight in Smart Dimmable LED Lighting Systems

The model analysed above includes only artificial light in the indoor environment since dimmable LED system is the only source of light. Still, the external sources of light (e.g., windows) usually cannot be ignored since natural daylight can significantly contribute to overall illumination in the room. If there are K users in the room located at some of the previously defined M grid points, illumination due to external sources at the users' positions on the workspace plane, usually called daylight, is defined as

$$\mathbf{w} = \begin{bmatrix} w_1, \dots, w_j, \dots, w_K \end{bmatrix}^T, \quad j = 1, 2, \dots, K,$$
(20)

where w_i represents the total daylight intensity received at the *j*-th user device's position. 280 Note that daylight contribution is independent of the dimming LED vector **s**. With the 281 aim to minimise energy consumption and to ensure satisfaction of the users' requirements, 282 smart home can employ a smart LED system by exploiting both artificial light and daylight. Smart home environment usually employs "smart windows" [21], which can manage the 284 level of daylight intensity in the room. The windows can be uniformly shaded by a constant 285 factor denoted by $a (0 \le a \le 1)$ [22,23], e.g., via controllable blinds. When the shading 286 factor is a = 1, the windows are completely 'open' (blinds are off) and overall daylight 287 intensity is present at the users' location. On the contrary, when a = 0, windows are totally 288 shaded, and the daylight will be absent (w = 0). 289

Considering the general case when both artificial light and daylight are exploited, the illumination model in (3) can be easily updated with daylight distribution, resulting in the illumination at the users' being

$$\mathbf{z} = \mathbf{H} \cdot \mathbf{s} + a \cdot \mathbf{w}. \tag{21}$$

Problem 4 formulation: Find the minimum energy consumption by dimming vector **s** and shading factor *a* that satisfies users' illumination requirements at their locations. 200

Besides dimming vector **s**, the shading coefficient *a* can be also optimized in order to reduce the daylight distribution density over the room. In this way it is possible to manage



Figure 14. Daylight intensity in the considered office. The windows are positioned at the bottom of the figure.

overall illumination through the open office space in order to reduce energy consumption in larger extent and/or to satisfy users' demands. The ewly formulated optimization problem is defined as

minimize
$$\|\mathbf{s}\|_{1} + \lambda \|\mathbf{H} \cdot \mathbf{s} + a \cdot \mathbf{w} - \mathbf{r}\|$$

subject to $\mathbf{H} \cdot \mathbf{s} + a \cdot \mathbf{w} \ge \mathbf{l}$
 $0 \le \mathbf{s} \le 1, \ \mathbf{s} \in \mathbb{R}^{N}$, (22)
 $0 \le a \le 1, \ a \in \mathbb{R}$

where **H** is the illuminance matrix of size $K \times N$, with elements given by (4). Priority parameter λ ($0 \le \lambda \le 1$) is previously defined as a way to manage a relative importance of the minimizing energy consumption and satisfying users' requirements. To solve the optimization problem in (22), we can employ CVX, a MATLAB package for specifying and solving convex programs [31].

Results: Simulation results are obtained for the example of a typical office with four windows, each with dimensions 1 × 2 meters. While all LEDs are turned off, i.e., artificial lights are absent, measurements can be performed during different periods of the day in order to collect data about the level of daylight illuminance at the horizontal plane. This kind of measurements can be performed by employing different light sensor devices. Figure 14 presents the level of the daylight intensity which are obtained by measurements in June, at noon, in Glasgow UK.

For the same system setup as in Figure 5 (K = 10, $N = 3 \times 3$, $\Phi_{1/2} = 60^{\circ}$, $r_i = 600$ lux 304 and $l_i = 300$ lux for j = 1, 2, ..., K), Figure 15 presents the illumination distribution based 305 on the solution of the problem defined in (22). Figures 15a-15b show the scenario when 306 $\lambda = 0.01$ and the priority is to achieve the energy savings. Figure 15a presents the system 307 when the windows shading is not possible (a = 1), while Figure 15b corresponds to the 308 case when smart windows are employed. Although greater energy consumption is present in Figure 15b, users near the windows are illuminated with lower light intensity when the 310 shading of the windows is available. For example, when a = 1, a complete contribution of 311 the light from the windows will affect users near windows, i.e., 2110 lux, 1402 lux, etc., due 312 to strong component of daylight illumination close to windows. Similar conclusion can be 313 taken from Figures 15c-15d when $\lambda = 0.5$. In both cases the window shading is beneficial 314 since it can achieve better level of users' satisfaction while maintaining energy savings. 315



Figure 15. Solution of the Problem 4 defined in (22), K = 10 users randomly located, $\Phi_{1/2} = 60^0$.

A similar situation is presented in Figure 16, but for K = 5 users located near the 316 windows, for $\lambda = 0.1$ and $\lambda = 0.5$. If there is no possibility to shade the windows, users near 317 the window will be illuminated with significant level of light, which can be undesirable 318 resulting in the inadequate positions for sitting. Contrary, a situation when K = 5 users 319 are placed opposite of the windows is shown in Figure 17. Note that for the position of the 320 users' devices in Figure 17, after solving the optimization problem in (22), it is obtained that 321 a = 1, which is justified with the daylight distribution in Figure 14, as the daylight from 322 the windows will have a minor effect in that part of the room. It is obvious that daylight 323 from the windows should be exploited in order to reduce artificial LED lighting, but also it 324 is important to take into consideration both minimal and desired users' requirements for 325 illumination. 326

Figure 18 observes the same problem, but in the context of the semi-angle of the half illuminance. As it can be noticed, different semi-angle will have impact on the overall illumination and energy saving, thus should be considered as an important part of the smart LED systems, which is the topic of the next optimization problem.



Figure 16. Solution of the Problem 4 defined in (22), K = 5 users located near windows, $\Phi_{1/2} = 60^0$.



Figure 17. Solution of the Problem 4 defined in (22), K = 5 users located opposite of the windows, $\Phi_{1/2} = 60^0$.



Figure 18. Solution of the Problem 4 defined in (22) for different semi-angles, $\lambda = 0.01$.

4.1. Simultaneously optimising shading window factor and semi-angle at the half-illuminance

Similarly to Section 3.2, we will extend the optimization problem presented in (22) 332 by introducing a possibility to optimize the semi-angle at the half-illuminance in order to 333 minimize energy consumption.

Problem 5 formulation: Minimise energy consumption by dimming vector s, shading factor *a* and the semi-angle $\Phi_{1/2}$ that satisfy users' illumination requirements at their 336 locations.

Considering the problem posed in Section 3.2 (i.e., (15)), the optimization problem in (22) can be updated as follows

$$\begin{array}{ll} \underset{\mathbf{s},a,\Phi_{1/2}}{\text{minimize}} & \|\mathbf{s}\|_{1} + \lambda \|\mathbf{H} \cdot \mathbf{s} + a \cdot \mathbf{w} - \mathbf{r}\| \\ \text{subject to} & \mathbf{H} \cdot \mathbf{s} + a \cdot \mathbf{w} \ge \mathbf{l} \\ & 0 \le \mathbf{s} \le 1, \ \mathbf{s} \in \mathbb{R}^{N} \\ & 0 \le a \le 1, \ a \in \mathbb{R} \\ & 0 \le \Phi_{1/2} \le \pi/2 \end{array}$$

$$(23)$$

where different values of $\Phi_{1/2}$ result in different order *m* and in different centre luminous intensity, i.e., different illuminace matrix H. This optimization problem is solved in 339 MATLAB with a help of a package CVX [31]. 340



Figure 19. Solution of the Problem 5 defined in (23).

Results: The system configuration from analysis in Section 3.2 (Figure 9) is extended 341 by considering daylight sources as it was previously discussed, i.e., daylight contribution 342

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is defined by Figure 14. Recall that the discrete semi-angle values for each LED are 343 $\phi_i \in \{20^\circ, 40^\circ, 60^\circ\}$. Comparison of Figures 15b and 19a for $\lambda = 0.01$, i.e., Figures 15d and 344 19b for $\lambda = 0.5$, leads to a conclusion that introducing the extra component for optimization 345 results in greater energy saving while satisfying users' requirements. For example, when 346 the achieved energy saving factor in Figure 15b is G = 0.26, it is G = 0.19 in Figure 19a. 347 Introducing the selection of an optimal value of $\Phi_{1/2}$ results in important minimization of 348 energy consumption. This will be more pronounced if the smart LED system has a larger 349 set of discrete values of semi-angles as a choice. 350

4.2. Simultaneously optimising shading window factor and LED tilting

As additional component, the orientation of LED lamps is added as optimization parameter to the problem defined in (22). Based on analysis presented in Section 3.3, the optimization problem is defined as follows. 354

Problem 6 formulation: Find dimming vector s, shading factor a and tilting angles of
LEDs that simultaneously minimise energy consumption and satisfies users' illumination
requirements at their locations.355357357

Based on the problem observed in Section 3.3 (i.e., (19)), the optimization problem in (22) is now defined as

$$\begin{array}{ll} \underset{\mathbf{s},a,(\rho,\varepsilon)}{\text{minimize}} & \|\mathbf{s}\|_{1} + \lambda \|\mathbf{H} \cdot \mathbf{s} + a \cdot \mathbf{w} - \mathbf{r}\| \\ \text{subject to} & \mathbf{H} \cdot \mathbf{s} + a \cdot \mathbf{w} \geq \mathbf{l} \\ & 0 \leq \mathbf{s} \leq 1, \ \mathbf{s} \in \mathbb{R}^{N} \\ & 0 \leq a \leq 1, \ a \in \mathbb{R} \\ & -\pi/2 \leq \rho \leq \pi/2 \\ & 0/2 \leq \varepsilon \leq 2\pi \end{array}$$

where previously defined azimuth and zenith angles, i.e., (ε) and (ρ), respectively, have ³⁵⁸ impact on the illumination matrix **H**.

Results: After adding the daylight contribution presented in Figure 14 to the system 360 configuration from Section 3.3 (Figure 13), problem defined in (24) is solved using MATLAB 361 and CVX package [31]. Three possible orientations of LEDs, defined by the pairs of the 362 zenith and azimuth angles as $(\rho_i, \varepsilon_i) \in \{(0,0), (30,0), (30,180)\}$, are considered. Results 363 are presented in Figure 20. In order to observe benefits of possible LEDs orientations, we 364 will compare 15b and 20a for $\lambda = 0.01$, and Figures 15d and 20b for $\lambda = 0.5$. Greater energy 365 saving is noticed with introducing the LED tilting in the smart LED system, which further 366 can be improved with a greater number of options for LEDs orientation, but at the expense 367 of the system complexity and costs. 368



(a) $\lambda = 0.01$, a = 0.2, G= 0.2; (b) $\lambda = 0.5$, a = 0.16, G = 0.73; Figure 20. Solution of the Problem 6 defined in (24).

5. Conclusions

In this paper, we have proposed an energy-efficient strategy for the smart lighting 370 system. In order to provide minimal energy consumption and/or satisfy users' require-371 ments for illumination level, the smart LED system can control and manage the overall 372 illumination in the indoor space by considering that the LED lamps have possibility to 373 be dimmed. Furthermore, besides artificial LED light, external sources of light have been 374 also included. With the aim to properly exploit external lighting while providing minimal 375 energy consumption, we have proposed that the level of daylight are managed by win-376 dows shading. As an additional parameter to be optimized to improve performance of the 377 designed smart lighting system, we have observed both semi-angle of the half illuminance 378 and LED orientations. After solving the optimization problems by implementing algo-379 rithm in MATLAB software, it has been proved by a sequence of illustrative examples that 380 significant energy savings can be achieved while simultaneously satisfying users' demands. 381

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