

# Electrostatic Precipitation Efficiency for a Multi-needle Plane Electrode Topology under DC Excitation



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## Objectives

- Demonstrate the Integration of a Particle Charging Model along with existing FEA Analysis to Simulate Particle Dynamics under divergent Electric Field conditions.
- Simulate and Predict Electrostatic Precipitation (ESP) Efficiency of a novel 4-needle-plane electrode test cell.
- Compare simulated trend to practical testing through the use of Laser Aerosol Spectrometry in laboratory air under dry and wet conditions.

## Charging Model

Governing Differential Equation [1]:

$$m \frac{d^2x}{dt^2} = mg + E(x) \left[ q_c(t) + q_p(t) + q_d(t) \right] - \frac{F_d}{C_0}$$

$$\text{Conduction Charge: } q_c(t) = 6\pi R_p^2 E(x) \epsilon_0 \frac{\epsilon_m \sigma_p - \sigma_m \epsilon_p}{2\sigma_m + \epsilon_p} \left( 1 - e^{-\frac{t}{\tau_{mw}}} \right)$$

$$\text{Polarisation Charge: } q_p(t) = 6\pi R_p^2 E(x) \epsilon_0 \epsilon_p \left( 1 - \frac{\epsilon_p + \epsilon_m}{2\sigma_m + \sigma_p} e^{-\frac{t}{\tau_{mw}}} \right)$$

$$\text{Diffusion Charge: } q_d(t) = \frac{2\pi\epsilon_0 k T d}{e} \ln \left( 1 + \frac{e^2 N t d}{2\epsilon_0 \sqrt{2\pi m k T}} \right)$$

$$\text{Viscous Drag Force: } F_d = 6\pi\eta R_p \frac{dx}{dt}$$

Considers spherical particles Diameter, Conductivity, Permittivity and surrounding medium in any field E(x)

[1] I. Timoshkin et al. "Analysis of Particle Charging Mechanism for Optimisation of Precipitation Efficiency"

## Electrode & Test-Cell Configuration

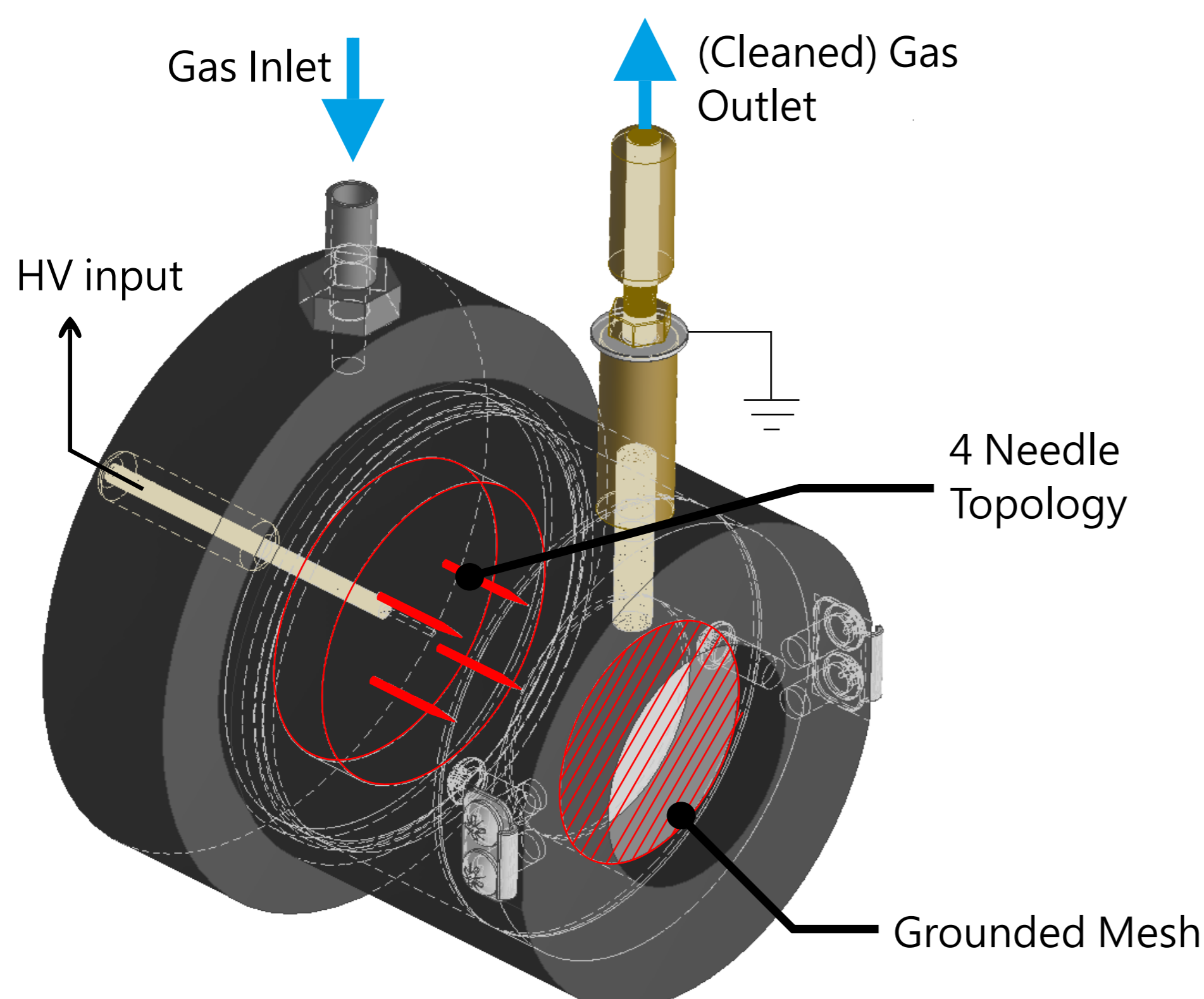


Figure 1: CAD Model of test-cell, with electrodes highlighted

## Particle Dynamics Solver

Electric Field Topology solved using QuickField FEA solver

Custom MATLAB variable-step solver written to take Field solution output and solve for Particle Dynamics and Trajectory using above Charging Model.

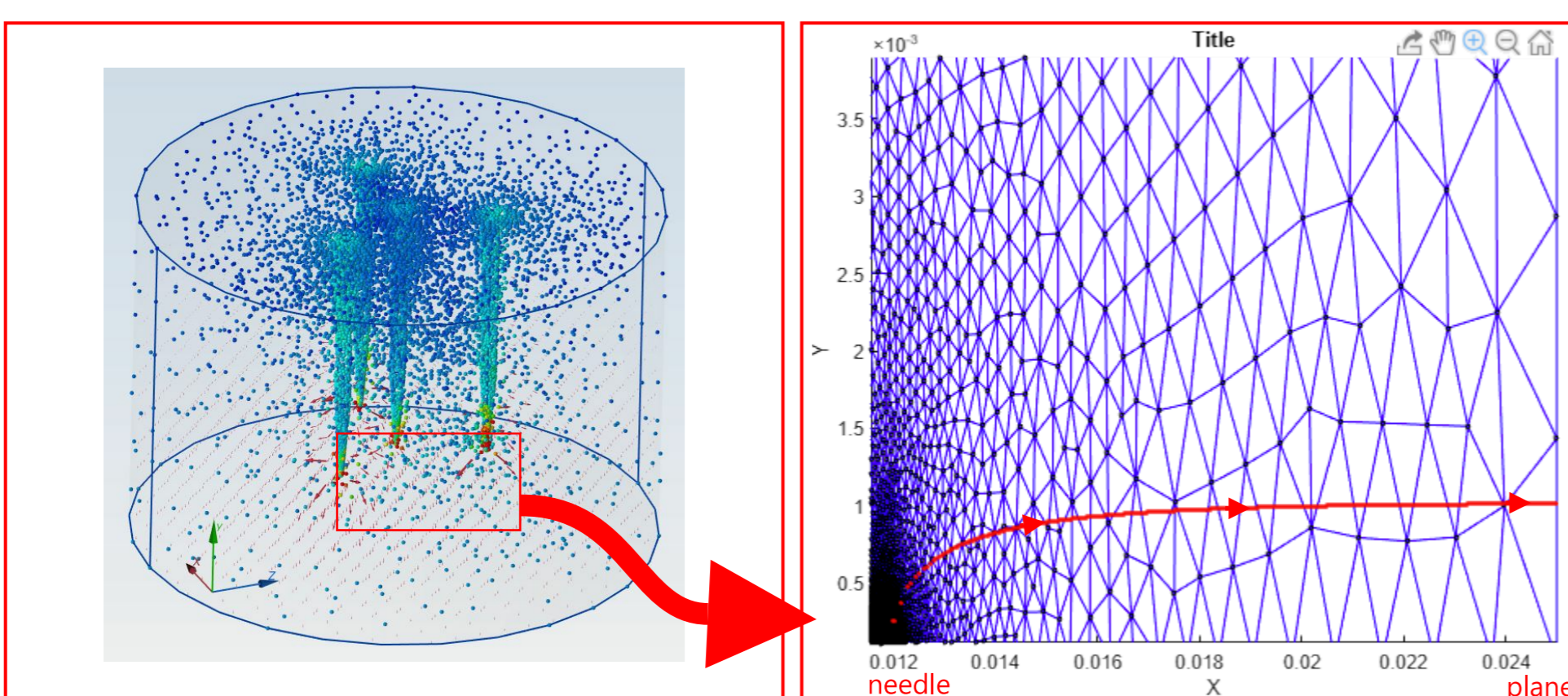


Figure 2: QuickField FEA Solution Visualisation

Figure 3: MATLAB Solver Particle Trajectory (Water)

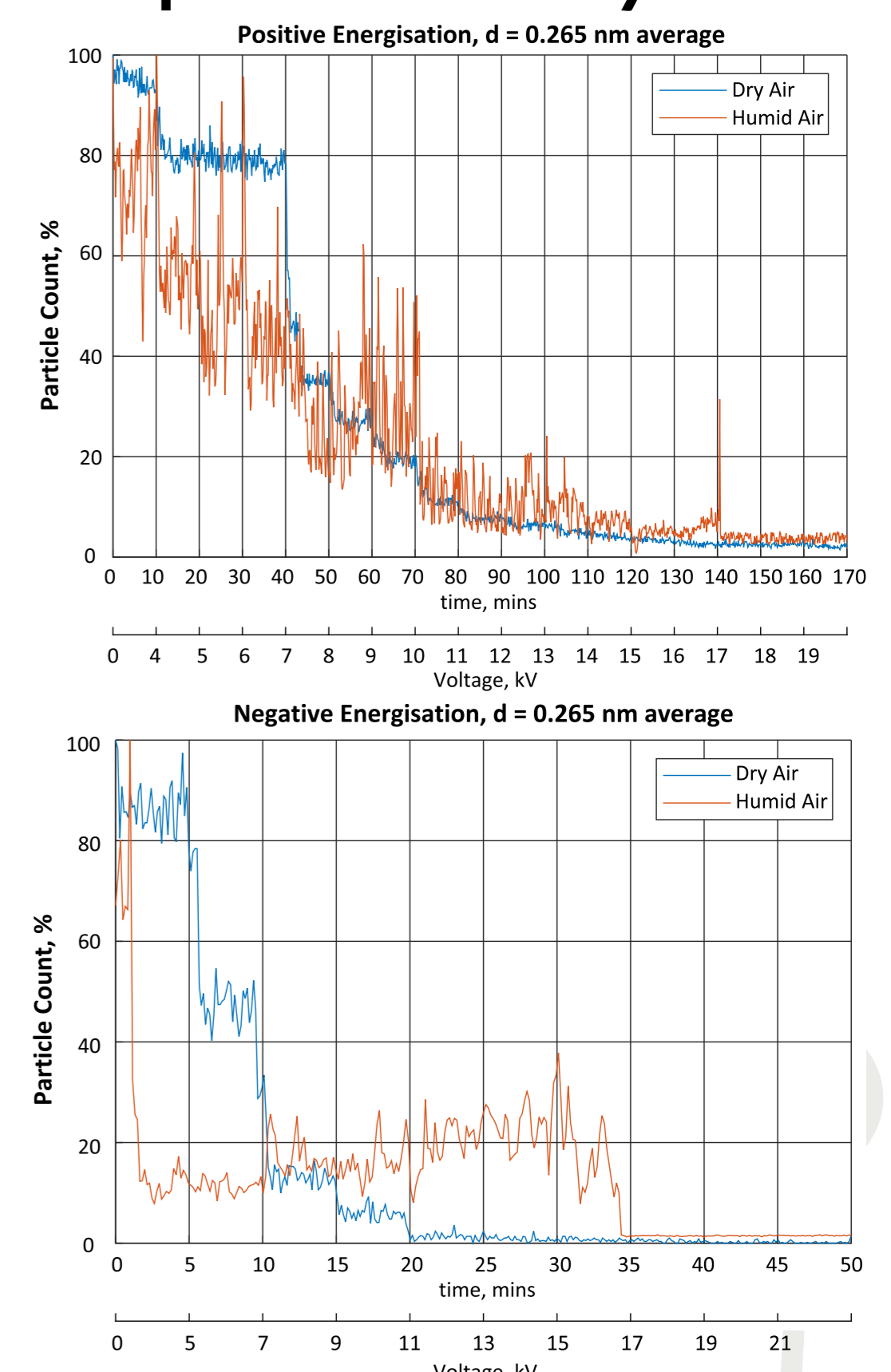
Used to predict Electrostatic Precipitation Efficiency

## Laser Aerosol Spectrometry

Using the GRIMM Laser Aerosol Spectrometer

Concentrations of PM 0.265 nm and above in laboratory air were measured for a DC voltage range of 0 to 21 kV, for both dry and humid air. Both positive and negative energisation was tested.

All tests ultimately achieved over 95% Precipitation Efficiency, with dry air exhibiting higher stability in recorded PM count. Negative energisation sees better precipitation performance overall.



## Discussion and Further Work

- Measured relationship between precipitation efficiency and voltage was found to closely match predicted behaviour from numerical solvers.
- Future line of investigation to repeat study under pulsed regime to compare performance to single point-plane topology.
- Potential interest with regards to the precipitation of contaminants on HVDC power lines under various atmospheric conditions.