

# Variations in hazard during earthquake sequences between 1995 and 2018 in western Greece as evaluated by a Bayesian ETAS model

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Accepted 2022 May 5. Received 2022 April 16; in original form 2021 September 29

## SUMMARY

Forecasting the spatio-temporal occurrence of events is at the core of Operational Earthquake Forecasting, which is of great interest for risk management, particularly during ongoing seismic sequences. Epidemic type aftershock sequence (ETAS) models are powerful tools to estimate the occurrence of events during earthquake sequences. In this context, a robust seismicity forecasting framework based on Bayesian-inference has been adapted to the Patras and Aegio region in western Greece (one of the most seismically active parts of Mediterranean), and an incremental adaptive algorithm is introduced to train the priors for ETAS model parameters. The seismicity forecasting is capable of accounting for uncertainty in the model parameters as well as variations in the sequence of events that may happen during the forecasting interval. Six seismic sequences between 1995 and 2018 were selected with main shock moment magnitudes  $M_w \geq 6.0$ . The ETAS model was adapted for each seismic sequence. The number of forecasted events with  $M_w \geq 4.5$  and their spatial distribution was retrospectively compared with the as-recorded earthquake catalogue, confirming a good agreement between the forecasts and observations. The results show that the adapted model can be used immediately after a severe main shock to statistically predict potentially damaging earthquakes during the ongoing seismic sequence. The seismicity forecasts were translated to short-term daily exceedance rates for different thresholds of peak ground acceleration. The results reveal that the seismic hazard increased by up to 33 times in the case of the damaging 1995  $M_w$  6.5 earthquake in the city of Aegio. However, the results confirmed that in all six studied sequences, the increased seismic hazard decayed rapidly during the 2 d after the main shock, and remained relatively high in the following days (roughly ten times the long-term time-independent hazard).

**Key words:** Computational seismology; Earthquake hazards; Earthquake interaction, forecasting and prediction.

## 1 INTRODUCTION

Estimating time-dependent probabilities of occurrence of potentially damaging earthquakes are at the heart of operational earthquake forecasting (OEF, Jordan *et al.* 2014). The output of OEF is often given in terms of probability changes due to time-dependent (over the order of days to months) seismicity. These probabilities can be used by emergency managers to communicate with the public (Jordan & Jones 2010; Goltz 2015; Roeloffs & Goltz 2017; Field & Minler 2018; McBride *et al.* 2020; Azarbakht *et al.* 2021; Douglas & Azarbakht 2021). Epidemic type aftershock sequence (ETAS) is a family of spatio-temporal point process models providing estimates of the time-dependent seismicity over a predefined aftershock zone (Ogata 1988; Ogata 1998). ETAS models show promising results in forecasting aftershocks and perform quite well in prospectively forecasting the seismicity within various operational frameworks (e.g. Marzocchi & Lombardi 2009; Zhuang 2011; Marzocchi & Murru 2012; Marzocchi *et al.* 2014; Ebrahimian & Jalayer 2017; Cattania *et al.* 2018; Kourouklas *et al.* 2020). According to the study by Console *et al.* (2007), the ETAS model is the best model for describing short-term seismicity (see also Zhuang *et al.* 2011). ETAS is an epidemic stochastic point process that considers every event as a potential trigger for subsequent events, thus, generalizing the modified Omori (MO) aftershock decay model (Zhang & Shcherbakov 2016, see also Utsu 1961; Utsu & Ogata 1995). In other words, the ETAS model is capable of accounting for the triggering effects of all events in the earthquake catalogue prior to the considered forecasting

time interval. It is worth emphasizing that an ETAS model's time-dependent seismicity rate can be transformed into a time-dependent hazard model via Probabilistic Seismic Hazard Analysis (PSHA, Cornell 1968; McGuire 1995), as is discussed in the last section of this paper.

In this paper, a simulation-based framework is used for both Bayesian updating of spatio-temporal ETAS model parameters as well as to obtain robust estimates of the spatial distribution of events in a prescribed forecasting time interval after a main shock (see Ebrahimian & Jalayer 2017). The term 'robust' here relates to the concept of *robust reliability* (Papadimitriou *et al.* 2001; Beck & Au 2002), which implies both the uncertainties in ETAS model parameters and those related to the occurrence of events in the forecasting interval are considered. The Bayesian inference framework allows the model parameters to be updated with time since the main shock. In other words, the model adapts itself to the new conditions that the seismicity variations dictate. To clarify, the robust forecasting terminology implies that several sets of model parameters are used through the simulation algorithm instead of using a set of constant model parameters, as is discussed in the methodology section (see also Ebrahimian & Jalayer 2017). A Markov Chain Monte Carlo (MCMC) simulation scheme (Papadimitriou *et al.* 2001; Omi *et al.* 2015; Ebrahimian & Jalayer 2017) is used to sample directly from the conditional posterior probability distributions of the ETAS model parameters. This forecasting framework accounts for two sources of uncertainty: (1) the uncertainty in the ETAS model parameters conditioned on the available catalogue of observed events prior to the forecasting interval's origin time and (2) the uncertainty in the simulated sequence of events during the forecasting time interval. The outcomes of this framework are in terms of the spatial distribution of the forecasted events and consequently the mean and confidence interval for the estimated number of events, corresponding to a given forecasting interval. The latter results are then converted to seismic hazard estimates, here short-term (hours to weeks) probabilities of exceeding different levels of peak ground acceleration (PGA), which is chosen as the ground-motion intensity measure because of its common use in seismic hazard mapping.

This paper aims to demonstrate the feasibility of the proposed Bayesian framework and retrospectively study the aftershock seismicity and hazard forecasts in the Patras and Aegio region in western Greece. This area is chosen for this study since it is in one of Europe's highest seismicity regions with numerous recent earthquake sequences, and it is a testbed of the TURNkey project.<sup>1</sup>

The seismicity characteristics of the region and the available literature are reviewed in the next section. Following this, the input data and the selected earthquake sequences are discussed. Then, following a brief description of the used forecasting framework, the retrospective spatio-temporal forecasting of seismicity in the region is studied using this methodology. Subsequently, a daily PSHA is presented by combining the seismicity forecasts with three ground-motion models. The article ends with some brief conclusions.

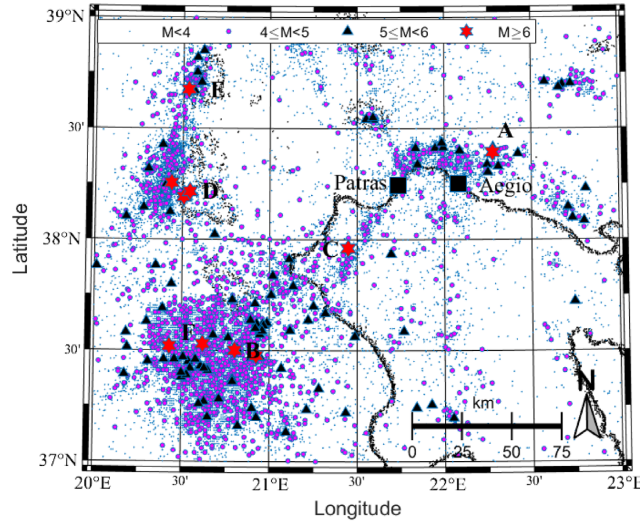
## 2 REGION OF STUDY

The geodynamic characteristics of the study region are comprehensively discussed in Karakostas *et al.* (2020). The study area in western Greece includes the third-largest (in terms of population) city in Greece, Patras, with many essential infrastructures, including a large port. There are also many public buildings, schools and heritage monuments. Additionally, the Rio–Antirrio bridge crosses the Gulf of Corinth near Patras. This is one of the world's longest multispan cable-stayed bridges and the longest of the fully suspended type. The town of Aegio is also located in the region, which is famous for a topographic plateau across a major fault (the cause of the destructive earthquake on 15 June 1995). There are also two smaller towns, Kalavryta and Lidorikion, in the region. In this section, we briefly summarize the recent literature on seismic hazard and previous earthquake forecasts for this region.

Both time-independent and time-dependent seismic hazards in Greece were investigated in terms of macroseismic intensity by Papaioannou & Papazachos (2000) for 144 cities, towns and villages. They concluded that the time-dependent seismic hazard results are in good agreement with the observed seismicity during the period 150 to 1995. A detailed areal-source seismic zonation model for shallow earthquakes in the broader Aegean area, containing 113 zones, was proposed by Vamvakaris *et al.* (2016). This model was based on seismicity and the available seismotectonic and neotectonic information to represent active faulting characteristics. A detailed investigation of catalogue completeness for the recent instrumental period was also conducted. The seismicity parameters, such as Gutenberg–Richter values for the 113 proposed zones, were calculated, and their spatial distribution was also considered. A review of the official seismic hazard maps in Greece was given by Tsapanos (2008).

Spatio-temporal earthquake clustering in the western Corinth gulf was investigated by Karagianni *et al.* (2013) by considering geological, seismological and geodetic aspects. The results reveal complicated tectonic behaviour and strong indications that seismicity in the area is not random and forms distinctive clusters. Console *et al.* (2006) applied various forecasting algorithms to the Greek catalogue for two periods: 1966–1980 and 1981–2002. The forecasting capability was statistically assessed by using the log-likelihood method. Their results revealed that short- and long-term methods performed much better than time-invariant models. Gospodinov & Rotondi (2006) and Gospodinov *et al.* (2007) studied the temporal decay in eight Greek aftershock sequences since 1975 using a Restricted ETAS model (RETAS). The RETAS model assumes that only aftershocks of magnitudes bigger than or equal to a given threshold can trigger secondary events. Karakostas *et al.* (2014) focused on forecasting, temporally and spatially, the 2013  $M_w$  5.8 north Aegean seismic sequence. They used different statistical methods to simulate the aftershock sequence, including an ETAS model with pre-calibrated parameters. Their results indicate a significant probability gain (PG) of more than 20 times the background probability during the first days of the considered aftershock sequence.

<sup>1</sup> Towards more Earthquake-resilient Urban Societies through a Multi-sensor-based Information System enabling Earthquake Forecasting, Early Warning and Rapid Response actions (<https://earthquake-turnkey.eu/>).



**Figure 1.** The spatial distribution of the earthquakes between 1995 and 2018 in the study area. The selected seismic sequences are indicated by the capital letters next to the main shock epicentre (see Table 1).

Latoussakis *et al.* (1991), Latoussakis & Drakatos (1994) and Drakatos & Latoussakis (1996) studied the possibility of forecasting large earthquakes in Greece during different sequences. They used the MO formula and noted its acceptable accuracy. Telesca *et al.* (2001) analysed the temporal properties of Greek aftershock sequences using the MO model. A physics-based and statistical earthquake forecasting approach was applied by Segou (2016) to the continental rift zone of the Corinth Gulf, by implementing a retrospective forecast of events with magnitudes greater than or equal to 3 for the time period 1995–2013. This study revealed that the joint implementation of physics-based approaches and the statistical ETAS model is beneficial for future OEF systems. Kourouklas *et al.* (2020) investigated short-term spatio-temporal clustering of Greek seismicity from 2008 to 2018. The used ETAS model used maximum-likelihood estimation through a simulated annealing approach. The discrepancies between the ETAS model forecasts and the observations were assessed by residual analysis. The model performed well except for the 2008 sequence when five  $M_w > 6$  earthquakes occurred. Finally, the short-term seismicity of the central Ionian Islands was studied by Mangira *et al.* (2020), revealing that the used ETAS clustering model provides reliable forecasts of the aftershock activity for this region.

To be complementary to the available literature, this study uses the most recent seismic data for the region from 1995 to 2018, which contains six earthquakes with  $M_w \geq 6$ , as explained in detail in the next section.

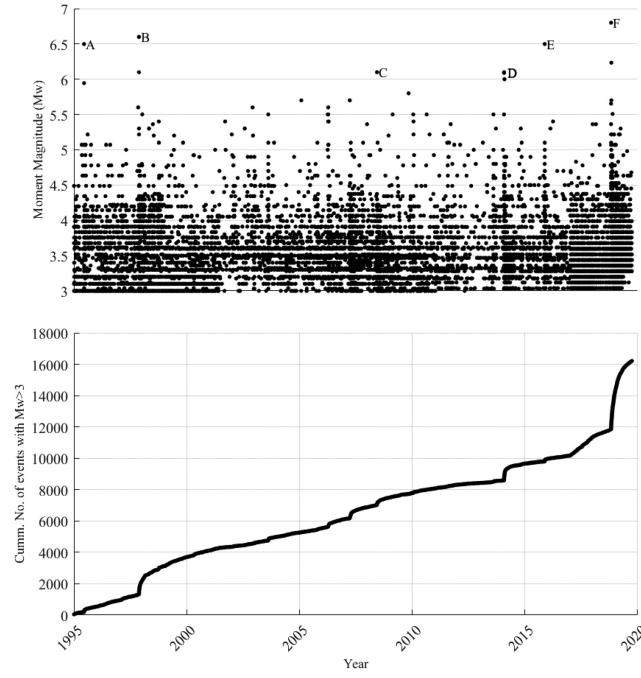
### 3 INPUT DATA AND SELECTED SEQUENCES

The International Seismological Centre (ISC, last access 2020) earthquake catalogue (Bondár & Storchak 2011; ISC 2020) was used to collect data from the previous three decades in the study region. It was concluded that six severe main shocks with their triggered aftershock sequences are distinguishable since the catastrophic 1995 Aegio event. It is assumed that these six sequences are sufficient samples to have both a set of consistent and modern instrumental data, and sufficient sequences to study the potential variation in model parameters. The spatial and temporal characteristics of the ISC catalogue for the study area between 1995 and 2018 (including the six seismic sequences A to F) are shown in Figs 1 and 2, respectively. The cumulative number of earthquakes with  $M_w \geq 3$  is also shown in Fig. 2, indicating heightened seismicity around the selected sequences. Greek national catalogues were not used here; however, they are identical with the ISC catalogue beyond the magnitude of completeness. In Greece, there are two institutions reporting phases (bulletin data) to ISC: NOA and Aristotle University of Thessaloniki (AUTH). In other words, there is no common national bulletin in Greece, although, since 2007, there is a unified network sharing waveform data with the public. NOA is the official seismic monitoring agency in Greece, which provides the majority of Greek data to ISC. Nevertheless, the ISC reports some small earthquakes (particularly in northern Greece) using AUTH data. Therefore, the ISC catalogue is the most rational choice for the current study.

The selected earthquake sequences are listed in Table 1, covering main shocks with moment magnitude  $M_w \geq 6$  between 1995 and 2018. The distances between each main shock's epicentre and the two studied cities (Patras and Aegio) are also provided in Table 1 (sequences A and C are the closest to Patras and Aegio, including sequence A, which was only 23 km from Aegio). These differences in distance will influence the seismic hazard assessed at the considered locations, as discussed later.

### 4 METHODOLOGY

Seismicity forecasts over periods of hours/days/weeks are crucial for emergency responders and decision-makers seeking to mitigate risk since there is a high chance of aftershocks during this period. It is clear that forecasting damaging earthquakes have a higher priority



**Figure 2.** Top panel: the events with  $M_w \geq 3$  versus time in the ISC earthquake catalogue between 1995 and 2018 in the study area, including the labelled sequences in Table 1. Bottom panel: the cumulative number of events with  $M_w \geq 3$  between 1995 and 2018.

**Table 1.** The selected sequences between 1995 and 2018 with main shock magnitude  $M_w \geq 6$ , main shock occurrence time and the distances to the cities of Patras and Aegio.

| Sequence Label | Lat. (N) | Lon. (E) | Main shock magnitude ( $M_w$ ) | Main shock date (dd/mm/yyyy) | Hour:minute | Distance to Patras (km) | Distance to Aegio (km) |
|----------------|----------|----------|--------------------------------|------------------------------|-------------|-------------------------|------------------------|
| A              | 38.39    | 22.28    | 6.5                            | 15/06/1995                   | 00:15       | 50                      | 23                     |
| B              | 37.50    | 20.80    | 6.6                            | 18/11/1997                   | 13:07       | 116                     | 140                    |
| C              | 37.96    | 21.45    | 6.1                            | 08/06/2008                   | 12:25       | 40                      | 64                     |
| D              | 38.19    | 20.51    | 6.1                            | 26/01/2014                   | 13:55       | 107                     | 137                    |
| E              | 38.68    | 20.53    | 6.5                            | 17/11/2015                   | 07:10       | 115                     | 143                    |
| F              | 37.53    | 20.62    | 6.8                            | 25/10/2018                   | 22:54       | 126                     | 151                    |

than forecasting small events, which is practically impossible. Therefore, this study's focus is to forecast events with magnitudes  $\geq 4.5$ , which is the cut-off magnitude often considered in European seismic hazard studies (Woessner *et al.* 2015). A robust seismicity forecasting framework (Ebrahimian & Jalayer 2017) has been implemented for this study. By pairing the Bayesian inference with an advanced simulation technique (namely, MCMC) to update the ETAS model parameters, this framework has the unique feature of considering different sources of uncertainty, i.e. the uncertainties in the ETAS model parameters and the generated sequence of events within the forecasting interval (sequences are generated based on samples of the ETAS model parameters).

#### 4.1. The epidemic-type aftershock sequence (ETAS) model

The ETAS model is a marked spatio-temporal point process (Daley & Vere-Jones 2008), where a seismic sequence is treated as a point process of interevent time and epicentres. The magnitude of each event is an additional observed variable characterizing the point process to become marked. Let the aftershock zone be defined as set  $\mathbf{A}$  in the Cartesian space. The conditional rate of occurrence of earthquakes at time  $t$  with magnitude  $\geq m$  in the cell unit centred at the Cartesian coordinate  $(x, y) \in \mathbf{A}$  based on the ETAS model is denoted as  $\lambda_{\text{ETAS}}(t, x, y, m | \theta, \text{seq}_t, M_l)$ . The rate  $\lambda_{\text{ETAS}}$  is conditioned on: (1) the vector of ETAS model parameters  $\theta$  (defined subsequently); (2) the observation history up to time  $t$ , which expresses the influence of past events  $\text{seq}_t = \{(t_j, x_j, y_j, m_j), t_j < t, M_j \geq M_l\}$ , where  $t_j$  is the arrival time for the  $j$ th event (with  $t_j < t$ ) with magnitude  $m_j$  and location  $(x_j, y_j) \in \mathbf{A}$  and (3) the lower cut-off magnitude  $M_l$ . The conditional rate  $\lambda_{\text{ETAS}}$  can be computed as follows:

$$\lambda_{\text{ETAS}}(t, x, y, m | \theta, \text{seq}_t, M_l) = e^{-\beta(m-M_l)} \sum_{t_j < t} \left[ K e^{\beta(m_j-M_l)} \frac{K_t}{(t-t_j+c)^p} \frac{K_R}{(r_j^2+d^2)^q} \right]. \quad (1)$$

In eq. (1), the background seismicity rate is not considered; this issue will be discussed in the subsequent section. The vector of ETAS model parameters is defined as  $\theta = [K, K_t, K_R, \beta, c, p, d, q]$ . Parameter  $\beta$  is related to the Gutenberg–Richter relation; parameters  $c$  and  $p$  are similar to those of the MO's Law defining the decay in time;  $d$  and  $q$  characterize the spatial distribution of the triggered events;  $r_j$  is the distance between the location  $(x, y)$  and the epicentre of the  $j$ th event  $(x_j, y_j)$ . The parameter  $K$  requires calibration for each forecasting interval and is discussed in the subsequent section. The parameter  $K_t$  is computed so that the time-dependent term  $K_t/(t - t_j + c)^p$  over infinite time will, in the limit, be equal to unity (see Ebrahimian & Jalayer 2017 and Lippiello *et al.* 2012, 2014), which results in  $K_t = (P - 1) \cdot c^{(p-1)}$ . Finally, the parameter  $K_R$  is normalized such that integrating the spatial term over infinite space will also, in the limit, be equal to unity (see Ebrahimian & Jalayer 2017; Lippiello *et al.* 2012, 2014) resulting in  $K_R = \frac{(q-1)}{\pi} \cdot d^{2(q-1)}$ . In the ETAS model (eq. 1), the term  $K e^{\alpha(M_j - M_l)}$  is called the productivity function and the coefficient  $\alpha$  shows the efficiency of an event in generating aftershock activity (dimension of magnitude<sup>-1</sup>). It is assumed herein that  $\alpha = \beta$  (for more details, see the parameter  $\alpha$  in Ogata & Zhuang 2006). Hence, in summary, only five model parameters (i.e.  $[\beta, c, p, d, q]$ ) are used in the MCMC updating framework. The other three parameters ( $[K, K_t, K_R]$ ) are calculated as described above (for more details, see Ebrahimian & Jalayer 2017). It is noted that the generated sample through the MCMC algorithm is rejected if any of the following conditions hold: (1) any value of the vector  $[\beta, c, p, d, q]$  is negative, (2)  $p \leq 1$  or (3)  $q \leq 1$  (the latter two conditions are described in Ebrahimian & Jalayer 2017). It is also worth mentioning that the focus of the current study is forecasting over a short time interval (e.g. 1 d), otherwise, the  $\beta$  coefficient in the productivity function may cause the population to explode when simulating for a relatively long time period.

To clarify, the assumption of equality between the two parameters  $\alpha$  and  $\beta$  is a commonly adopted constraint (see e.g. Seif *et al.* 2017; Zhang & Shcherbakov 2016; Papadopoulos *et al.* 2021). When  $\alpha$  is considered to be a free parameter in the ETAS model (i.e. the model parameters become  $[\alpha, \beta, c, p, d, q]$ ), past studies based on maximum-likelihood estimation (e.g. Marzocchi & Lombardi 2009) or Bayesian parameter estimation (Ebrahimian & Jalayer 2021) showed that  $\alpha < \beta$ . In particular, the parameter  $\alpha$  determines the magnitude dependence of the trigger potential, which is crucial in identifying the underlying triggering mechanism and for forecasting ongoing earthquake sequences (Hainzl *et al.* 2013). The constraint  $\alpha = \beta$  implies self-similarity of the triggering events (i.e. the number of triggered events is proportional to the rupture area of the triggering earthquake, see Papadopoulos *et al.* 2021). Moreover, it is shown that  $\alpha$  might be significantly underestimated (low value of  $\alpha$ ) due to the incompleteness of the aftershock catalogue and missing data at the early stages of an ongoing seismic sequence (Seif *et al.* 2017). This issue may be critical in terms of providing operational forecasts in the immediate aftermath of a large earthquake. Moreover, in the study region (Greece), where the recorded catalogue is not rich in low-magnitude events (see Section 4.3), this consideration might underestimate the parameter  $\alpha$ . There are also other issues that have a significant influence on the estimation of the parameter  $\alpha$  including anisotropic aftershock distribution (Hainzl *et al.* 2008), potential time-dependent (non-stationary) background rate and transient aseismic forcing (Hainzl *et al.* 2013, who show that the majority of earthquake clusters in California are compatible with  $\alpha = \beta$ ). Therefore, to avoid these potential biases, we have assumed  $\alpha = \beta$  in this study.

## 4.2. Estimation for the number of aftershocks

With reference to eq. (1), let  $\lambda_{\text{ETAS}}(t, x, y, m|\theta, \mathbf{seq}, M_l)$  be the conditional intensity representing the ETAS rate of occurrence of events in the forecasting interval  $[T_{\text{start}}, T_{\text{end}}]$  at time  $t$  (elapsed after the main event, or even any arbitrary time reference) with the time of origin at  $T_0$ . The observation history  $\mathbf{seq}$  is the sequence of  $N_0$  events (including the main shock and the sequence of aftershocks) that took place before the forecasting interval, that is in the interval  $[T_0, T_{\text{start}}]$ . This can be expressed as  $\mathbf{seq} = \{(t_i, x_i, y_i, m_i), T_0 \leq t_i < T_{\text{start}}, m_i \geq M_l, i = 1 : N_0\}$ . The number of events at the centre point of a given cell centred at  $(x, y)$  with magnitude  $\geq m$  in the forecasting interval  $[T_{\text{start}}, T_{\text{end}}]$ , denoted as  $N(x, y, m|\mathbf{seq}, M_l)$ , can be estimated by:

$$N(x, y, m|\mathbf{seq}, M_l) = N_b(x, y, m|M_l) + \int_{T_{\text{start}}}^{T_{\text{end}}} \lambda_{\text{ETAS}}(t, x, y, m|\mathbf{seq}, M_l) dt, \quad (2)$$

where  $N_b(x, y, m|M_l)$  is a constant representing the area's background seismicity. It is equal to the time-invariant background spatial seismicity rate for magnitudes  $> m$  multiplied by the time interval  $(T_{\text{end}} - T_{\text{start}})$ . To clarify, the number of events in the whole cell can be calculated by multiplying  $N$  by the area of the cell. Given a realization of  $\theta$  as the vector of ETAS model parameters, parameter  $K$  (of the vector  $\theta$ ) is calibrated such that the number of events with magnitude  $\geq M_l$  taking place in the time interval  $[T_0, T_{\text{start}}]$ , over the whole aftershock zone is equal to  $N_0$  (see Ebrahimian & Jalayer 2017 for more details). Moreover, one can calculate a plausible value for the rate of occurrence denoted as  $\lambda_{\text{ETAS}}(t, x, y, m|\theta, \mathbf{seq}, M_l)$ , as shown in eq. (1). A robust estimate (Ebrahimian & Jalayer 2017) of the average number of events in the cell centred at  $(x, y)$  with a magnitude  $\geq m$  in the forecasting interval  $[T_{\text{start}}, T_{\text{end}}]$ , denoted as  $\mathbb{E}[N(x, y, m|\mathbf{seq}, M_l)]$ , can be calculated over the domain of the model parameters  $\Omega_\theta$ :

$$\mathbb{E}[N(x, y, m|\mathbf{seq}, M_l)] = N_b(x, y, m|M_l) + \int_{\Omega_\theta} \left( \int_{T_{\text{start}}}^{T_{\text{end}}} \lambda_{\text{ETAS}}(t, x, y, m|\mathbf{seq}, M_l) dt \right) p(\theta|\mathbf{seq}, M_l) d\theta, \quad (3)$$

where  $\mathbb{E}[\cdot]$  denotes the expectation and  $p(\theta|\mathbf{seq}, M_l)$  is the conditional posterior probability density function (PDF) for  $\theta$  given the  $\mathbf{seq}$  and the lower cut-off magnitude  $M_l$ . The PDF  $p(\theta|\mathbf{seq}, M_l)$  can be estimated using Bayesian parameter estimation, which is discussed in Appendix A. Eq. (3) accounts for the events that took place before the forecasting interval  $[T_0, T_{\text{start}}]$ ; however, the triggering effect of the

events taking place during the forecasting interval  $[T_{\text{start}}, T_{\text{end}}]$  is expected to play a major role. The robust estimate for the average number of aftershocks (as noted previously) also considers all the plausible sequences of events that can happen during the forecasting time interval (see Ebrahimian & Jalayer 2017 for a comprehensive discussion). To this end, the sequence of events taking place during the forecasting interval (denoted herein as **seqg**), which is unknown at the time of forecasts, is simulated. Let us assume that a plausible **seqg** is defined as the events within the forecasting interval defined as **seqg** =  $\{(IAT_i, x_i, y_i, m_i), T_{\text{start}} \leq t_i \leq T_{\text{end}}, m_i \geq M_l\}$ , where  $IAT_i = t_i - t_{i-1}$  stands for the inter-arrival time. The robust estimate for the number of aftershocks in eq. (3) should also consider all the plausible sequences of events **seqg** (i.e. the domain  $\Omega_{\text{seqg}}$ ) that can happen during the forecasting time interval, as follows:

$$\mathbb{E}[N(x, y, m|\mathbf{seq}, M_l)] = N_b(x, y, m|M_l) + \int_{\Omega_\theta} \left[ \int_{\Omega_{\text{seqg}}} \left( \int_{T_{\text{start}}}^{T_{\text{end}}} \lambda_{\text{ETAS}}(t, x, y, m|\mathbf{seqg}, \theta, \mathbf{seq}, M_l) dt \right) p(\mathbf{seqg}|\theta, \mathbf{seq}, M_l) d\mathbf{seqg} \right] p(\theta|\mathbf{seq}, M_l) d\theta, \quad (4)$$

where  $p(\mathbf{seqg}|\theta, \mathbf{seq}, M_l)$  is the PDF for the generated sequence **seqg** given that  $\theta$  and **seq** are known and  $\lambda_{\text{ETAS}}(t, x, y, m|\mathbf{seqg}, \theta, \mathbf{seq}, M_l)$  is the space-time clustering ETAS model considering also the sequence of events taking place within the forecasting interval. The robust estimation in eq. (4) implies that a set of possible model parameters is used to estimate the conditional number of events  $N(x, y, m|\mathbf{seq}, M_l)$  rather than a single set of model parameters.

The proposed algorithm is demonstrated for six independent seismic sequences in the region (see Section 5). The used algorithm is shown to successfully forecast aftershocks in all the six considered sequences. The conditional estimation of  $N$  (see eq. 4) can be used further for short-term time-dependent PSHA. The 2013 European Seismic Hazard Model (ESHM13) (Giardini *et al.* 2013; Woessner *et al.* 2015) has been used in the current study to define the background seismicity in eqs (2)–(4). The Kernel-smoothed stochastic rate model considering seismicity and fault moment release (SEIFA-model) has been used to define each cell's background seismicity rate in the aftershock zone (Woessner *et al.* 2015).

#### 4.3. The incremental adaptive training algorithm to obtain priors for the ETAS model parameters

Defining prior values for the model parameters  $\theta$  is a challenging task. In Greece the aftershock sequences are not particularly productive and/or well-reported, that is the magnitude of completeness ( $M_c$ ) varies between 2.7 and 4.5 for different locations and catalogue lengths (see Vamvakaris *et al.* 2016). This relatively high magnitude of completeness makes defining the prior values even more challenging. It is not reasonable to wait for a long time after a main shock to obtain a satisfactory catalogue (for the period after the main shock only) to initiate the forecasting procedure (especially in the context of operational earthquake forecasting). In other words, we would need to wait a long time after a main shock (in aftershock sequences of low productivity or high magnitude of completeness) so that sufficient events occur to obtain a complete catalogue if we insist on using only the events following a main shock (sequence-specific). To clarify, as a solution, it is convenient to ‘borrow’ events from a time window before the main shock to calibrate the model parameters and consequently update it during the aftershock sequence. Therefore, an *incremental adaptive training algorithm* has been developed and proposed in this study to estimate a set of reasonable priors for the ETAS model parameters  $\theta$  to start the forecast algorithm almost immediately after a main shock (see Fig. 3). It is worth emphasizing that the proposed adaptive approach is only used for the first round of the forecasting algorithm. The sequence-specific catalogue (from the main shock's origin time) is then used for the second round (i.e. the second day in this study) of the forecasting trials and so forth. As shown in Fig. 3, the proposed algorithm starts its computations from ‘M’ months before the forecast interval and chooses several arbitrary subsets of ‘E’ events with magnitude  $\geq M_c$ . It is worth mentioning that  $M_c$  is sequence-specific and is calculated for each sequence separately. In the case of the first round, where the adaptive algorithm in Fig. 3 is used, if we face a quiescent period before the main shock, we lengthen the catalogue prior to the main shock to obtain sufficient data to calibrate the prior parameters of the ETAS model. Additionally, in the case of the second round and so forth, we may face a lack of data in the catalogue after the main shock for calculation of the magnitude of completeness. This lack of data may be due to low productivity in a specific sequence or the aftershock waves being hidden in the seismic waves of the larger events (Lippiello *et al.* 2016, 2019). In this case, we move the catalogue origin time  $T_0$  back a couple of days before the main shock, with the aim of having a catalogue that is sufficient to calculate  $M_c$ .

Normally distributed prior model parameters [mean values of  $b = 1$ ,  $c = 0.03$ ,  $p = 1$ ,  $d = 1$ ,  $q = 1.5$ , all with standard deviation ( $\sigma$ ) equal to 0.3, and  $\beta = b \cdot \ln 10$ ] used for the first subset of the adaptive incremental algorithm, and the MCMC algorithm is used to update these model parameters based on the first subset catalogue. As an example, the prior and posterior distributions of the ‘c’ model parameter are shown in Fig. 4. As seen in Fig. 4, sample posterior intervals are simulated by the MCMC algorithm, and consequently, a normal distribution is fitted to the posterior numerical histograms. In other words, an advantage of the currently used model is that the model parameters are not constant during a seismic sequence, which is in contrast with ETAS models based on the maximum-likelihood approach.

Subsequently, the previous subset's posterior distributions are used as the prior distributions for the next subset. This procedure repeats until we reach the last subset, which ends before the starting time of the forecast ( $T_{\text{start}}$ ). Each subset is also checked so that it covers at least ‘D’ days of the catalogue, that is if ‘E’ events happen in less than ‘D’ days, we increase the subset's time window to cover at least ‘D’ days.

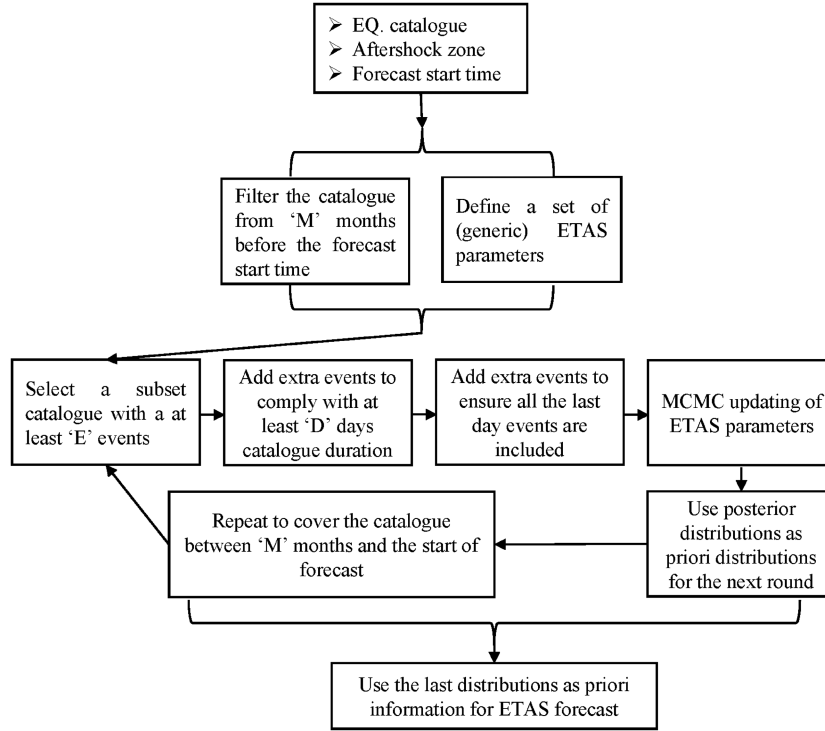


Figure 3. The flowchart of the incremental adaptive training algorithm to obtain the ETAS prior model parameters.

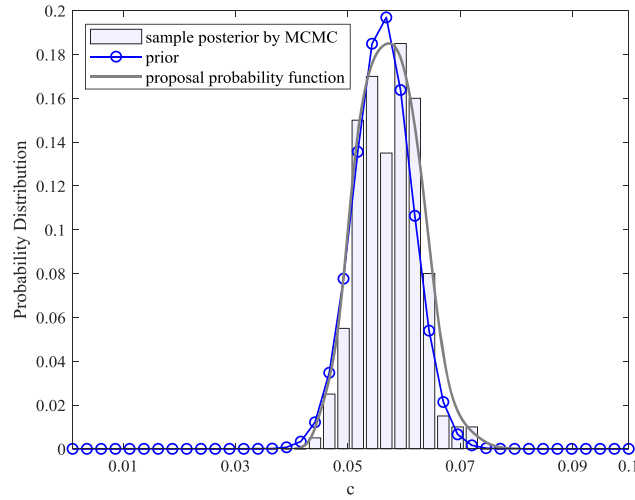


Figure 4. The MCMC updating for the example of the ‘c’ model parameter, showing the prior and posterior distributions.

**Table 2.** The incremental adaptive training of the ETAS model parameters for sequence F (see Table 1).

| Number of subsets | Start date (dd-mm-yyyy) | End date (dd-mm-yyyy) | No. of events with $M \geq M_c$ | $\beta$ | $c$   | $d$   | $p$   | $q$   |
|-------------------|-------------------------|-----------------------|---------------------------------|---------|-------|-------|-------|-------|
| 1                 | 27-01-2018              | 14-03-2018            | 71                              | 1.681   | 0.044 | 1.014 | 1.803 | 1.207 |
| 2                 | 17-03-2018              | 23-04-2018            | 70                              | 1.679   | 0.048 | 1.014 | 2.050 | 1.224 |
| 3                 | 24-04-2018              | 17-06-2018            | 70                              | 1.681   | 0.054 | 1.012 | 2.172 | 1.230 |
| 4                 | 17-06-2018              | 06-08-2018            | 70                              | 1.682   | 0.058 | 1.010 | 2.443 | 1.225 |
| 5                 | 06-08-2018              | 01-10-2018            | 70                              | 1.682   | 0.064 | 1.009 | 2.535 | 1.226 |
| 6                 | 01-10-2018              | 25-10-2018            | 68                              | 1.682   | 0.065 | 1.010 | 2.556 | 1.227 |

This proposed algorithm ensures that the final prior distributions for the ETAS model parameters have been trained based on the previous ‘M’ months catalogue. For example, for Sequence F (see Table 1), the used catalogue goes back a year before the main shock (27-1-2018 to 25-10-2018). Hence, as seen in Table 2, we start from 27 January 2018 until the date which provides subsets of at least 50 events with magnitude  $\geq M_c$  (equal to 4.1 in this case based on the approach of Wiemer 2001) and covers at least a minimum duration of 30 d. The

minimum of 50 events guarantees the proper numerical MCMC updating of the ETAS model parameters (this was empirically verified by the authors); nevertheless, considering a minimum value for  $D$  (equal to 30 d herein) will also provide a trade-off between the number of events and the time span in which they took place. The first row in Table 2 indicates that the first subset begins on 27 January 2018 and ends on 14 March 2018, which contains 71 events with  $M \geq 4.1$ . These events were primarily used in the MCMC Bayesian updating algorithm to update the prior model parameters. The updated five (mean) model parameters are also provided in the first row of Table 2. The first row of Table 2 is used as prior information (the mean value, the corresponding  $\sigma$  and the normal distribution assumption) for the second row. This procedure was repeated until the last row in Table 2, which is before the forecasting date, that is at 00:00 UTC on 26 October 2018 (almost 1 hr after the main shock of Sequence F). The proposed incremental adaptive training of the ETAS model parameters needs only the MCMC algorithm to update the ETAS model parameters (subsets 1–6 in Table 2). The seismicity forecasting is only performed for the last row in Table 2 (subset 6 in Table 2) in order to provide the spatio-temporal distribution of earthquakes in the forecasting interval of interest, as discussed in the next section.

The adaptive training of the ETAS model parameters provides the opportunity to initiate earthquake forecasting almost immediately after the occurrence of a main shock, especially in regions with aftershock sequences of low productivity. This is a key forecasting constraint in many high seismicity regions such as Greece in the first (golden) hours after a severe main shock, during which the forecasting results are of utmost importance for first responders. The possibility of earthquake forecasting immediately after a severe main shock is of great interest to researchers (e.g. Lippiello *et al.* 2016, 2019). The proposed incremental adaptive training algorithm also provides a rational framework to continuously update the prior ETAS model parameters used in an OEF engine on a regular basis. A potential OEF framework may use the last set of updated parameters, when a magnitude greater than a pre-defined threshold occurs, which can potentially define the main shock of interest. In this context, there is no need to consider a very long sequence (e.g. the whole 419 events in Table 2), which thus overcomes the burden of summing up the triggering properties of all the events when providing early forecasts. Moreover, there is no need to consider the origin time of the sequence if the main shock is not preceded by foreshocks.

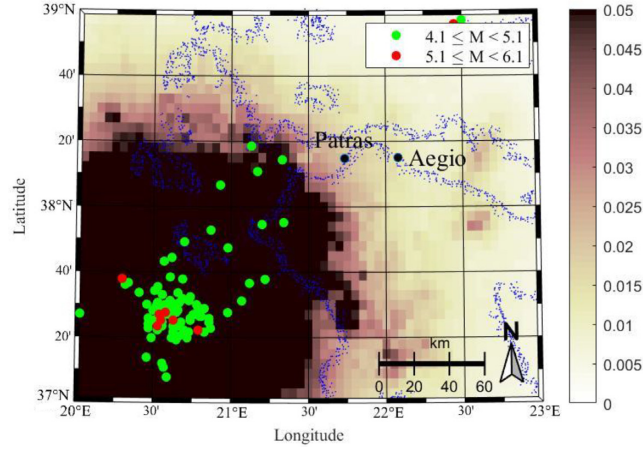
We summarize the proposed methodology's steps as follows:

1. Use the incremental adaptive training methodology to obtain prior ETAS model parameters before a main shock. This set of model parameters is used for the first forecasting attempt after a main shock.
2. Use the sequence-specific catalogue (between the main shock's origin time and the start of the forecasting interval) to obtain the ETAS model parameters for the second forecasting trial and so forth. If the catalogue is not sufficient to estimate the magnitude of completeness, then the catalogue is extended by days/months before the main shock to obtain sufficient data.
3. To estimate the ETAS model parameters conditioned on the events that have already taken place in the ongoing seismic sequence and before the beginning of the forecasting interval, an MCMC simulation scheme is used to sample directly from the conditional posterior probability distribution for ETAS model parameters. This ETAS model parameter updating is applied to the selected catalogue (from either Step 1 or Step 2 above).
4. Perform many (200 in our study) sequence simulations based on the generated plausible sequences of events that may occur during the forecasting interval (the real sequence is unknown at the time of forecasting).
5. Use eq. (4) to estimate the spatial distribution of the forecasted events and consequently the estimated number of events corresponding to a given forecasting interval with their confidence intervals. The background seismicity can also be included.
6. Use eq. (6) (see Section 6) to convert forecasted seismicity results into time-dependent seismic hazard estimates.

## 5 SEISMICITY FORECASTING RESULTS

The study area in Fig. 2 is defined between 20–23E and 37–39N and is meshed with a grid size of  $0.05^\circ \times 0.05^\circ$ , which is the same grid size as ESHM13 (Woessner *et al.* 2015). This choice facilitates the implementation of the seismicity results in the PSHA. This area is the same as in previous studies on these earthquake sequences (e.g. Karakostas *et al.* 2020). The forecast interval is defined as 1 d (24 hr), and  $T_{\text{start}}$  is set at 00:00 UTC. Starting with the most recent main shock (i.e. sequence F),  $T_{\text{start}}$  is almost 1 hr after the main shock. Sequence F's main shock had a magnitude  $M_w$  of 6.8 and occurred at 37.53N and 20.62E, which is near the southwest corner of the considered aftershock zone (Fig. 5, see also Fig. 2 and Table 1). It is worth mentioning that ESHM13 (Giardini *et al.* 2013; Woessner *et al.* 2015) has been used throughout this paper to define the background seismicity as an input to the ETAS model.

The forecasted short-term spatial distribution of seismicity in terms of the mean plus  $2\sigma$  (98 per cent confidence interval) in the study area is shown in Fig. 5, for a forecast interval of 1 d (24 hr) following  $T_{\text{start}}$  of 00:00 UTC on 26 October 2018. The observed earthquakes of interest that occurred within the corresponding forecasting interval are also illustrated as coloured dots (distinguished by magnitude). The colour bar in Fig. 5 indicates the forecasted number of occurrences (per forecast time interval and per  $\text{km}^2$ ) of events with a magnitude  $\geq M_l$  (we set  $M_l = M_c = 4.1$  in this case).  $M_c$  is calculated (Wiemer 2001) based on the sequence of events (see *seq* in eq. 2), which contains 68 observed data from 1-10-2018 to 25-10-2018 (see the last row in Table 2), and eight aftershocks occurred during the 66 min between the main shock time (22:54 UTC) and  $T_{\text{start}}$  (00:00 UTC). Only eight aftershocks with  $M \geq M_c$  took place after the main shock up to  $T_{\text{start}}$ ; hence, as explained in the previous section, we used the catalogue before the main shock origin time (see the last row in Table 2) to overcome this shortcoming and to incrementally obtain the model parameters' prior values.



**Figure 5.** The spatial distribution of the seismicity (the map reports the mean  $+2\sigma$  confidence interval, that is 98th percentile, for the number of events per  $\text{km}^2$ ) in the aftershock zone for 26 October 2018 (sequence F in Table 1). The forecast interval is 24 hr, starting from 00:00 UTC. The probability of having a magnitude greater than or equal to a given magnitude is shown in the figure's bottom-left-hand corner. The forecasted numbers of events with  $M \geq 4.5$  are shown in the bottom-right-hand corner. The first, second and third numbers indicate the 50th, 84th and 98th percentiles. The fourth number (in the parenthesis) indicates the observed number of events.

**Table 3.** Comparison between the forecasted number of events (and the corresponding statistical distribution) with  $M \geq 4.5$  and the observed data in the case of all sequences for the first day after the main shock. The probabilities of exceeding different magnitude thresholds (from 4.5 to 7.5) over the whole aftershock zone are also shown.

| Sequence label | Number of forecasted events with $M \geq 4.5$ |                 |                 | Observed | P( $M \geq m$ ) over the aftershock zone |           |           |           |
|----------------|-----------------------------------------------|-----------------|-----------------|----------|------------------------------------------|-----------|-----------|-----------|
|                | 50th percentile                               | 84th percentile | 98th percentile |          | $m = 4.5$                                | $m = 5.5$ | $m = 6.5$ | $m = 7.5$ |
| A              | 2                                             | 2               | 2               | 2        | 0.9                                      | 0.2       | 0.03      | 0.003     |
| B              | 3                                             | 4               | 4               | 4        | 1                                        | 0.3       | 0.04      | 0.005     |
| C              | 3                                             | 3               | 4               | 0        | 0.9                                      | 0.2       | 0.03      | 0.003     |
| D              | 1                                             | 1               | 1               | 4        | 0.6                                      | 0.1       | 0.01      | 0.001     |
| E              | 4                                             | 5               | 7               | 3        | 1                                        | 0.5       | 0.1       | 0.02      |
| F              | 20                                            | 24              | 35              | 32       | 1                                        | 1         | 0.5       | 0.1       |

As shown in Fig. 5, higher seismicity is forecasted at the closest distances to the main shock's epicentre. The probabilities of exceeding different magnitude thresholds (from 4.5 to 7.5) are shown in Table 3 for all sequences (A to F in Table 1) and the first forecasting day following the given main shocks. The upper limit for the magnitude is assumed to be 7.5 since the maximum magnitude in ESHM13 (Giardini *et al.* 2013; Woessner *et al.* 2015) for all the 14 SEIFA area sources in the study area are between 7.2 and 8.1. It is worth noting that the probabilities shown in Table 3 refer to an event occurring anywhere inside the study area and cannot be interpreted as a forecast of a specific event at a particular location. These probabilities are the integration of forecasted numbers over all cells (covering the whole study region). For example, the probability of having  $M_w \geq 4.5$  during the first day following a main shock anywhere in the whole study area is equal to 0.999 ( $= 1.00$ ) in the case of sequence F. This forecast is reasonable since there are 32 observed events with  $M_w \geq 4.5$  in this forecasting time interval (Fig. 5 and Table 3).

The forecasted number of events, within the aftershock zone, with  $M_w \geq 4.5$  (which is the minimum magnitude assumed in ESHM13 for seismic hazard calculation) is also shown in Table 3, indicate the forecasted 50th percentile (the median value, equivalent to the logarithmic mean in an arithmetic scale), the 84th percentile (logarithmic mean plus one logarithmic  $\sigma$  in an arithmetic scale), and the 98th percentile (logarithmic mean plus two logarithmic  $\sigma$  in an arithmetic scale), respectively. The observed number of events with a magnitude greater than 4.5 is also shown in Table 3 for the purpose of comparison. As seen in Table 3, the forecasted numbers of events are in good agreement with the observed data. This is an inherent criterion to intuitively assess the quality of the forecasting algorithm. To study this agreement more, we estimated the seismicity for different forecasting time intervals. Besides, as seen in Table 4, the results (including statistical percentiles) are provided by repeating the current forecasting algorithm for nine different forecasting time intervals, all with the same  $T_{\text{start}}$  (i.e. 00:00 UTC on 26 October 2018). The distribution of the forecasted number of events shows good agreement with the observed catalogue, as reported in Table 4. Therefore, the 24-hr forecasting time interval is chosen for further investigations; this is also a reasonable time interval for risk management purposes (see also Ebrahimian *et al.* 2013, 2014). It is worth mentioning that the forecasted number of events is calculated as a real number, but is shown in Table 4 after rounding to the closest integer value. Therefore, some percentiles for a given time interval become identical in Table 4.

**Table 4.** Comparison between the forecasted number of events (and the corresponding statistical distribution) with  $M \geq 4.5$  and the observed data in the case of sequence F for different forecasting intervals. The forecasting start time,  $T_{\text{start}}$ , is 00:00 UTC on 26 October 2018.

| Forecasting interval | Number of forecasted events with $M \geq 4.5$ |                 |                 |                 |                 | Observed | N-test       |
|----------------------|-----------------------------------------------|-----------------|-----------------|-----------------|-----------------|----------|--------------|
|                      | 2nd percentile                                | 16th percentile | 50th percentile | 84th percentile | 98th percentile |          |              |
| 6 hr                 | 6                                             | 7               | 7               | 9               | 12              | 11       | 0.946, 0.098 |
| 12 hr                | 9                                             | 10              | 12              | 15              | 20              | 19       | 0.978, 0.037 |
| 1 d                  | 13                                            | 16              | 20              | 24              | 35              | 32       | 0.983, 0.026 |
| 2 d                  | 19                                            | 23              | 30              | 42              | 83              | 39       | 0.953, 0.064 |
| 3 d                  | 23                                            | 30              | 39              | 57              | 92              | 45       | 0.850, 0.187 |
| 4 d                  | 28                                            | 36              | 48              | 68              | 109             | 50       | 0.648, 0.405 |
| 5 d                  | 35                                            | 43              | 61              | 82              | 149             | 61       | 0.483, 0.567 |
| 6 d                  | 39                                            | 49              | 66              | 93              | 181             | 63       | 0.386, 0.660 |
| 7 d                  | 44                                            | 54              | 76              | 111             | 189             | 67       | 0.227, 0.807 |

In addition, the N-test (Zechar *et al.* 2010) was used to assess the quality of the forecasts. The N-test is intended to measure (in a probabilistic manner) how well the forecasted number of earthquakes matches the observed number of events. According to this test, we fit a Poisson distribution to the forecasted number of events ( $N_{\text{fore}}$ ) with a magnitude greater than a threshold, which is actually the expected number of events in the forecasting interval that we have estimated. Then, we measure if the observed number of events ( $N_{\text{obs}}$ ) with a magnitude greater than a threshold is not located in the tails of the Poisson distribution. To this end, we estimate two probability terms that should be greater than a pre-defined value  $P_{\text{eff}}$ : as written in eq. (5).

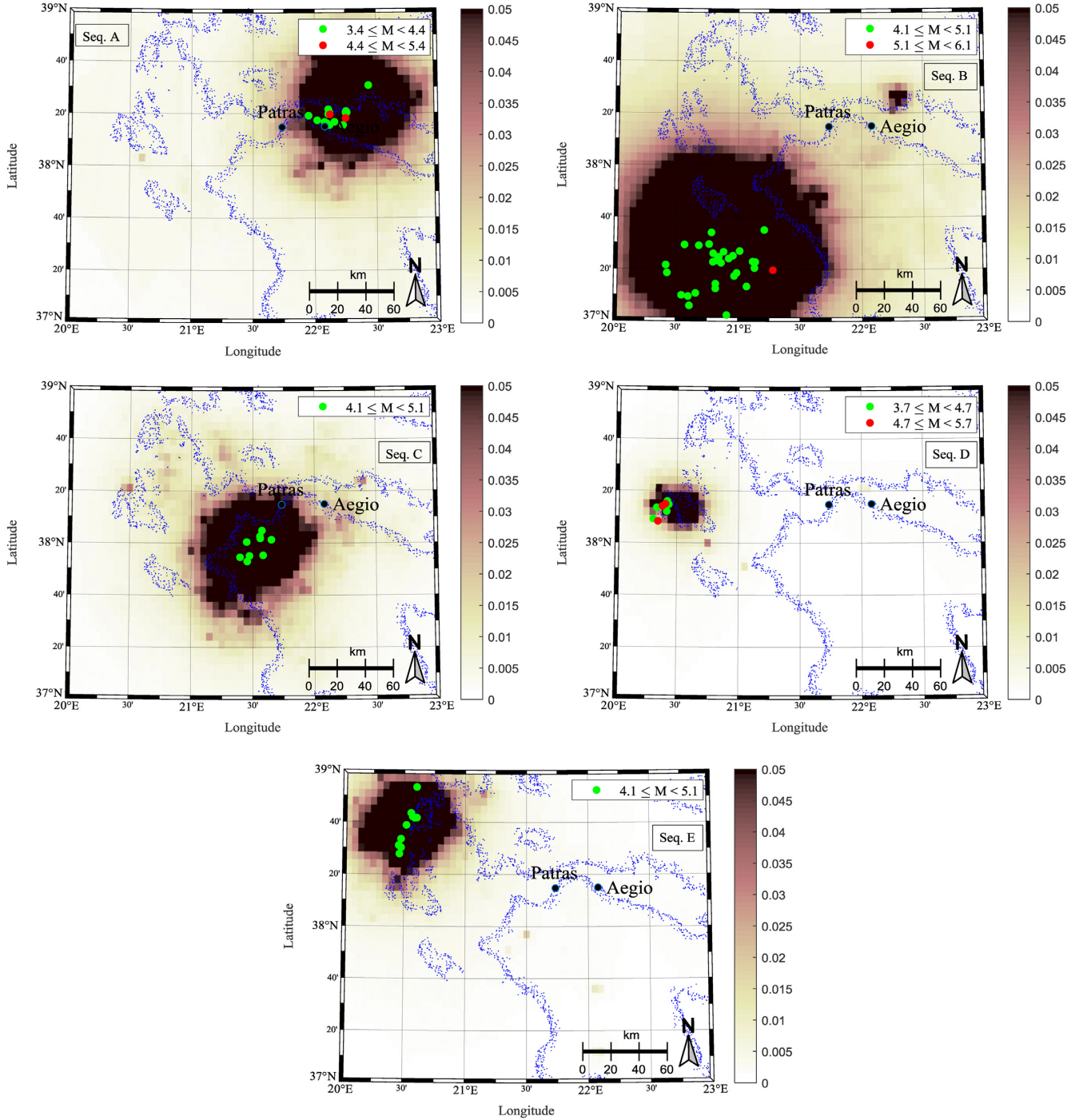
$$P(n \leq N_{\text{obs}} | N_{\text{fore}}) = \sum_{n=0}^{N_{\text{obs}}} \frac{(N_{\text{fore}})^n e^{-N_{\text{fore}}}}{n!} > P_{\text{eff}}$$

$$P(n \geq N_{\text{obs}} | N_{\text{fore}}) = 1 - P(n \leq N_{\text{obs}} - 1 | N_{\text{fore}}) = 1 - \sum_{n=0}^{(N_{\text{obs}}-1)} \frac{(N_{\text{fore}})^n e^{-N_{\text{fore}}}}{n!} > P_{\text{eff}}. \quad (5)$$

The above expression guaranties that the real case of  $N_{\text{obs}}$  will not be within the tails of our forecast. It is worth mentioning that the value for  $P_{\text{eff}}$  is set to 0.025 to reflect the 95 per cent confidence interval. As seen in Table 4, the N-test column has two numbers in each cell, representing the first and second integrals in eq. (5), respectively. The used N-test confirms that, in all forecast cases, the  $N_{\text{obs}}$  is not located within the tails of our forecast. However, providing the statistical distribution of  $N_{\text{fore}}$  (see Table 4) is more feasible in the sense that instead of assigning a Poisson distribution to the forecasted number of events, it estimates directly the distribution of the forecast and computes its percentiles (i.e. 50th, 16th, 84th, 2nd and 98th). In this way, one can judge how well the forecasted number of earthquakes matches  $N_{\text{obs}}$ . Besides, as seen in Fig. 5 and Fig. 6, the spatial distribution of forecasted events are in very good agreement with the observed events, which again demonstrates the accuracy of the used algorithm.

Another advantage of the seismicity forecasting model is its ability to forecast repeatedly during the short duration of most aftershock sequences within an operational framework. Hence, the forecasting model has been run repeatedly every day until 7 d following the main shock (see Table 5). To clarify, we only used the incremental adaptive training of the parameters in the case of forecasting for 26 October (the first row in Table 5), for which **seq** contained 68 events and was defined previously in this section (see the last row of Table 2). However, for the second-day forecast (second row in Table 5) and for subsequent forecasts, we only used the previous day's posterior distribution (the mean value, the corresponding  $\sigma$  and the normal distribution) as prior values for the next day. Additionally, we only used the catalogue starting from the main shock up to the  $T_{\text{start}}$ , in the case of forecasting for 27 October and beyond (i.e. the **seq** includes the main shock and the sequence of the events up to  $T_{\text{start}}$  of the corresponding date). This change is a rational (as well as an operational) choice; for example for daily forecasting starting from 00.00 UTC on 27 October, 25 hr have passed since the main shock, and we have sufficient events (according to the second column of Table 5, **seq** contains 101 events including the main shock and the sequence of aftershocks with  $M > M_c$ ). Thus, there is no longer a need to use the catalogue before the main shock. However, if we face a lack of data in the catalogue after the main shock, then, we would move the catalogue's start time back a couple of days before the main shock, in order to have sufficient data to perform the Bayesian updating. This was not necessary for Sequence 'F', but, this assumption is necessary to make the algorithm versatile. The magnitude of completeness,  $M_c$ , in Table 5 is equal to 4.1 (see the third column). The retrospective forecasting results for the number of events with  $M > 4.5$  are shown in Table 5, which confirms that the forecasted number of events is in good agreement with the observed data (see the last four columns in Table 5). However, an event with a magnitude ( $M_w$ ) of 6.2 occurred on 30 October at 02:59 UTC. The ETAS model cannot directly forecast such a severe doublet event. Nevertheless, the forecasted number of earthquakes above the threshold of 4.5 is between 4 and 7, which confirms that the seismicity is still high based on this forecasting model. As seen in Table 5, the used N-test results also confirm that, in all cases, the  $N_{\text{obs}}$  is not located within the tails of our forecast.

In addition, the forecasting model is applied to the other sequences in Table 1(A) to (E), starting about 1–2 hr following their main shocks. The forecasting results for the first 24 hr are shown in Fig. 6 for sequences A to E. As seen in Fig. 6, it is confirmed that the numbers of



**Figure 6.** The spatial distribution of seismicity (the maps report the mean +  $2\sigma$  confidence interval, that is 98th percentile, for the number of events per  $\text{km}^2$ ) in the aftershock zone for sequences A to E (Table 1) during 1 d following the main shock. See the caption of Fig. 5 for an explanation of the information.

forecasted events are in good agreement with the observed data. Additionally, in all the six considered sequences the forecasted events' spatial distribution is also in good agreement with the observed data. This is evidence that the proposed model can reproduce seismic sequences surrounding a main shock in the study area.

As discussed earlier, one concern in the ETAS forecasting approach is how to select reasonable prior values for  $\theta$ . The posterior distributions of  $\theta$ , in the day following the main shock, and for the six seismic sequences in Table 1, are shown in Table 6. The forecasting origin time,  $T_{\text{start}}$ , for each seismic sequence in Table 6 is identical to that shown in Fig. 5 and Fig. 6. The median of the five model parameters of ETAS and their uncertainties are also provided in Table 6. Furthermore, the minimum and maximum values for each model parameter (in terms of the median and  $\sigma$ ) are shown in the last row in Table 6, which we propose to be used as a reasonable set of prior  $\theta$  for further implementation in the study area. As seen in Table 6, parameters  $c$  and  $p$  do not change significantly,

**Table 5.** The variation of the model parameters  $\theta$  and seismicity forecasting results for 7 d following the main shock for sequence F (Table 1). The forecasting time interval is equal to 24 hr (1 d) for all 7 d with  $T_{\text{start}} = 00:00$  UTC at the corresponding date.

| Forecast date<br>(dd-mm) | No. of events<br>after the<br>main shock<br>( $M \geq M_c$ ) | Number of forecasted<br>events with<br>$M \geq 4.5$ |          |         |          |        |          |        |          |        |          |        |          |           |          |           |          | Observed     | N-test |
|--------------------------|--------------------------------------------------------------|-----------------------------------------------------|----------|---------|----------|--------|----------|--------|----------|--------|----------|--------|----------|-----------|----------|-----------|----------|--------------|--------|
|                          |                                                              | $M_c$                                               |          | $\beta$ |          | $c$    |          | $p$    |          | $d$    |          | $q$    |          | $1\sigma$ |          | $2\sigma$ |          |              |        |
|                          |                                                              | Median                                              | $\sigma$ | Median  | $\sigma$ | Median | $\sigma$ | Median | $\sigma$ | Median | $\sigma$ | Median | $\sigma$ | Median    | $\sigma$ | Median    | $\sigma$ |              |        |
| 26-10                    | 8 (+68)                                                      | 4.1                                                 | 1.682    | 0.002   | 0.064    | 0.007  | 1.008    | 0.005  | 2.556    | 0.151  | 1.226    | 0.012  | 0.012    | 20        | 24       | 35        | 32       | 0.983, 0.026 |        |
| 27-10                    | 101                                                          | 4.1                                                 | 1.872    | 0.102   | 0.042    | 0.007  | 1.558    | 0.135  | 2.241    | 0.266  | 1.338    | 0.042  | 0.042    | 2         | 3        | 5         | 7        | 0.988, 0.033 |        |
| 28-10                    | 138                                                          | 4.1                                                 | 1.966    | 0.112   | 0.041    | 0.008  | 1.273    | 0.095  | 2.315    | 0.224  | 1.330    | 0.031  | 0.031    | 4         | 5        | 9         | 6        | 0.889, 0.214 |        |
| 29-10                    | 210                                                          | 4.1                                                 | 2.056    | 0.091   | 0.042    | 0.007  | 1.180    | 0.075  | 2.480    | 0.228  | 1.354    | 0.035  | 0.035    | 4         | 6        | 7         | 5        | 0.785, 0.371 |        |
| 30-10                    | 247                                                          | 4.1                                                 | 2.078    | 0.099   | 0.042    | 0.007  | 1.109    | 0.055  | 2.534    | 0.196  | 1.373    | 0.028  | 0.028    | 4         | 5        | 7         | 11       | 0.989, 0.025 |        |
| 31-10                    | 286                                                          | 4.1                                                 | 2.067    | 0.068   | 0.041    | 0.007  | 1.079    | 0.040  | 2.730    | 0.221  | 1.383    | 0.035  | 0.035    | 5         | 6        | 9         | 2        | 0.238, 0.908 |        |
| 01-11                    | 303                                                          | 4.1                                                 | 2.089    | 0.079   | 0.045    | 0.008  | 1.110    | 0.053  | 2.684    | 0.194  | 1.381    | 0.034  | 0.034    | 4         | 5        | 6         | 4        | 0.628, 0.566 |        |

**Table 6.** The posterior distributions of ETAS parameters for six sequences in Table 1. All the parameters are assumed normally distributed.

| Sequence ID          | $\beta$ |          | $c$    |          | $p$    |          | $d$    |          | $q$    |          |
|----------------------|---------|----------|--------|----------|--------|----------|--------|----------|--------|----------|
|                      | Median  | $\sigma$ | Median | $\sigma$ | Median | $\sigma$ | Median | $\sigma$ | Median | $\sigma$ |
| A                    | 2.049   | 0.001    | 0.062  | 0.008    | 1.010  | 0.004    | 2.669  | 0.221    | 1.195  | 0.010    |
| B                    | 2.148   | 0.016    | 0.042  | 0.008    | 1.018  | 0.009    | 2.153  | 0.216    | 1.187  | 0.018    |
| C                    | 2.270   | 0.012    | 0.055  | 0.007    | 1.010  | 0.006    | 2.457  | 0.212    | 1.217  | 0.015    |
| D                    | 2.151   | 0.091    | 0.031  | 0.008    | 1.033  | 0.024    | 1.172  | 0.199    | 1.182  | 0.032    |
| E                    | 1.759   | 0.069    | 0.046  | 0.007    | 1.012  | 0.007    | 1.654  | 0.193    | 1.216  | 0.023    |
| F                    | 1.682   | 0.002    | 0.064  | 0.007    | 1.008  | 0.005    | 2.556  | 0.151    | 1.226  | 0.012    |
| Bounds of parameters | 1.682–  | 0.001–   | 0.031– | 0.007–   | 1.008– | 0.004–   | 1.172– | 0.151–   | 1.182– | 0.010–   |
|                      | 2.270   | 0.091    | 0.064  | 0.008    | 1.033  | 0.024    | 2.669  | 0.221    | 1.226  | 0.032    |

confirming that the temporal decay follows the MO's law in all the sequences. However, parameters  $\beta$  and  $d$  vary significantly among the different sequences, which indicates that the spatial characteristics and the Gutenberg–Richter relation are sequence-specific. Additionally, it is worth emphasizing that, as seen in Table 6, the ETAS posterior parameters are quite sequence-specific. Hence, using the proposed *incremental adaptive training algorithm* is a superior approach to using the model parameters from previous sequences in the study area.

## 6 SEISMIC HAZARD MODEL

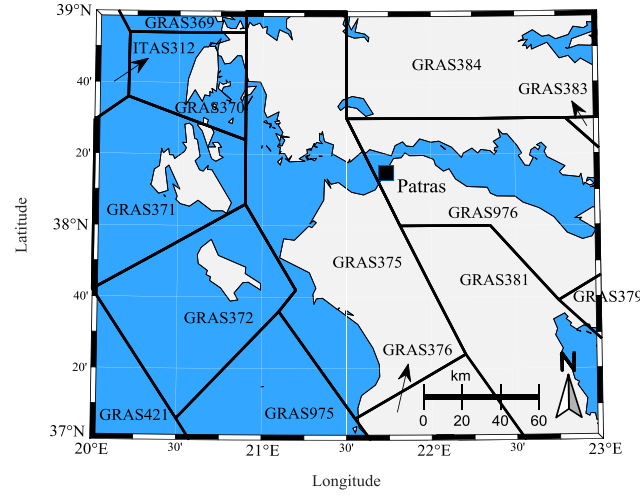
The short-term changes in seismicity revealed by the ETAS model, reflected by the time-variant conditional rate in eq. (1), are superimposed on the background seismicity (see eq. 2) to forecast the number of events over the aftershock zone within the considered time interval. The seismicity output in terms of the forecasted number of events in the forecasting time interval can be used as the short-term seismicity rate within a short-term time-dependent PSHA. Therefore, firstly, a conventional PSHA has been performed using eq. (6) (adapted from Cornell 1968; McGuire 1995; Ebrahimian *et al.* 2014; Baker 2015; Ebrahimian *et al.* 2019; and numerically integrated over the aftershock zone):

$$\lambda(PGA > pga) = \lambda(M > M_{\min}) \int_{M_{\min}}^{M_{\max}} \int_{x_{\min}}^{x_{\max}} \int_{y_{\min}}^{y_{\max}} P(PGA > pga|m, d\{(x, y), (x_s, y_s)\}) \cdot f_M(m) \cdot f_{X,Y}(x, y) dy dx dm, \quad (6)$$

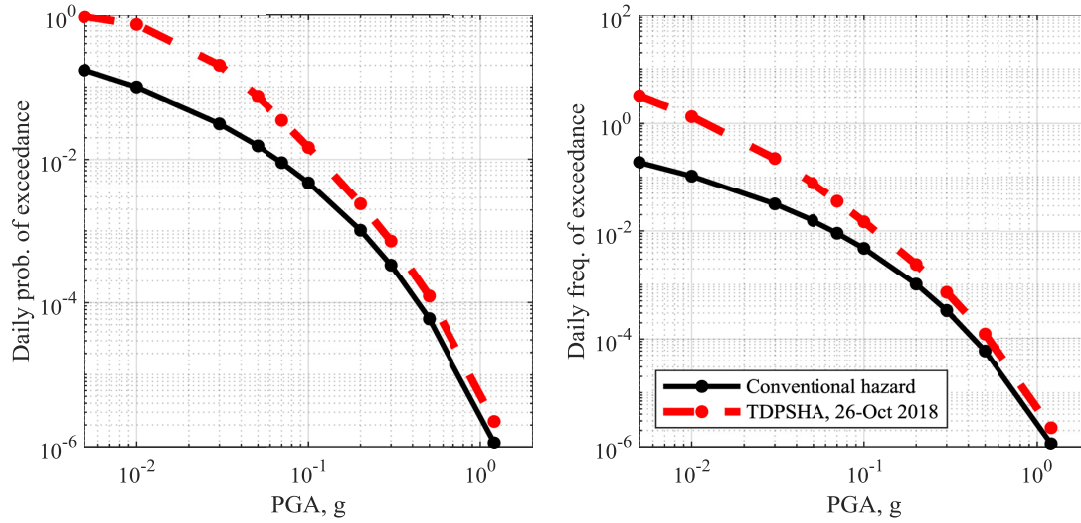
where  $\lambda(PGA > pga)$  is the annual rate of exceedance of  $PGA$  above a threshold  $pga$ ;  $M_{\min}$  is equal to 4.5 (the same assumption as in ESHM13);  $M_{\max}$  is the maximum magnitude obtained from the ESHM13 results for each area source;  $\lambda(M > M_{\min})$  is the annual rate of exceedance of earthquakes greater than  $M_{\min}$ , which is numerically defined for each grid cell based on the ESHM13 SEIFA model;  $d\{(x, y), (x_s, y_s)\}$  is the epicentral distance between the desired site ( $x_s$  and  $y_s$  coordinates where the hazard computation is of interest) and an arbitrary point ( $x$  and  $y$  coordinates  $\in \mathbf{A}$ ) inside the aftershock zone (see also Ebrahimian *et al.* 2019);  $P(PGA > pga|m, d\{(x, y), (x_s, y_s)\})$  is the conditional probability of  $PGA$  exceeding a threshold  $pga$ , given a magnitude  $m$  and an epicentral distance  $d$  at the  $(x, y \in \mathbf{A})$  coordinate which can be estimated using a Ground Motion Prediction Equation (GMPE);  $f_M(m)$  is the probability density function of magnitude, which follows the Gutenberg–Richter relationship based on the ESHM13 for each area source;  $f_{X,Y}(x, y)$  is the joint probability density function of the distance distribution at an arbitrary point with  $(x, y \in \mathbf{A})$  from the site  $(x_s, y_s)$  coordinate, which has a uniform distribution, that is assuming equiprobable occurrence of earthquakes in the area source;  $X_{\min}$  and  $X_{\max}$  are, respectively, the lower and upper bound values in the  $x$ -axis direction in Cartesian coordinates inside the study area ( $\in \mathbf{A}$ );  $Y_{\min}$  and  $Y_{\max}$  are, respectively, the lower and upper bound values in the  $y$ -axis direction in Cartesian coordinates inside the study area ( $\in \mathbf{A}$ ).

Choosing GMPEs for seismic hazard analysis has always been a challenging task (see also Danciu & Tselentis 2007; Segou *et al.* 2010; Delavaud *et al.* 2012; Skarlatoudis *et al.* 2013). On the other hand, a sophisticated logic tree including several GMPEs makes the forecasting algorithm time consuming, thereby limiting its potential real-time use for OEF. Therefore, only three GMPEs are used in this study to approximately match the ESHM13 assumptions as well as recent GMPE developments for Greece: Chiou & Youngs (2014), with a weight of 25 per cent, Zhao *et al.* (2006), with a weight of 25 per cent and Boore *et al.* (2021), with a weight of 50 per cent. The 2008 version of Chiou and Youngs' GMPE has been used in ESHM13; however, we decided to use the newer version (Chiou & Youngs 2014). The Chiou & Youngs (2014) GMPE is also justified by this model's high stability (Bommer & Stafford 2020). However, Zhao *et al.* (2006) GMPE was also chosen to account for epistemic uncertainty since it has the simplest functional form among the GMPEs used in the ESHM13. The Boore *et al.* (2021) GMPE was also taken into consideration since it has recently been developed specifically for Greece. Therefore, we allocate a higher, 50 per cent, weight to this regional model. We also acknowledge that the influence of GMPE selection on the final short-term time-dependent PSHA is an interesting topic for future research but it is beyond the scope of this study.

The short-term (daily) time-dependent PSHA is performed by substituting the rate  $\lambda(M > M_{\min})$  in eq. (6) by the forecasted number of events obtained from the robust seismicity framework (herein, corresponding to sequence F for 26 October 2018) and over the forecasting time interval (see eq. 4). The rest of the parameters have the same definition and values as used for the background (time-independent)



**Figure 7.** 14 area sources in the study area from ESHM13 (Giardini *et al.* 2013; Woessner *et al.* 2015).

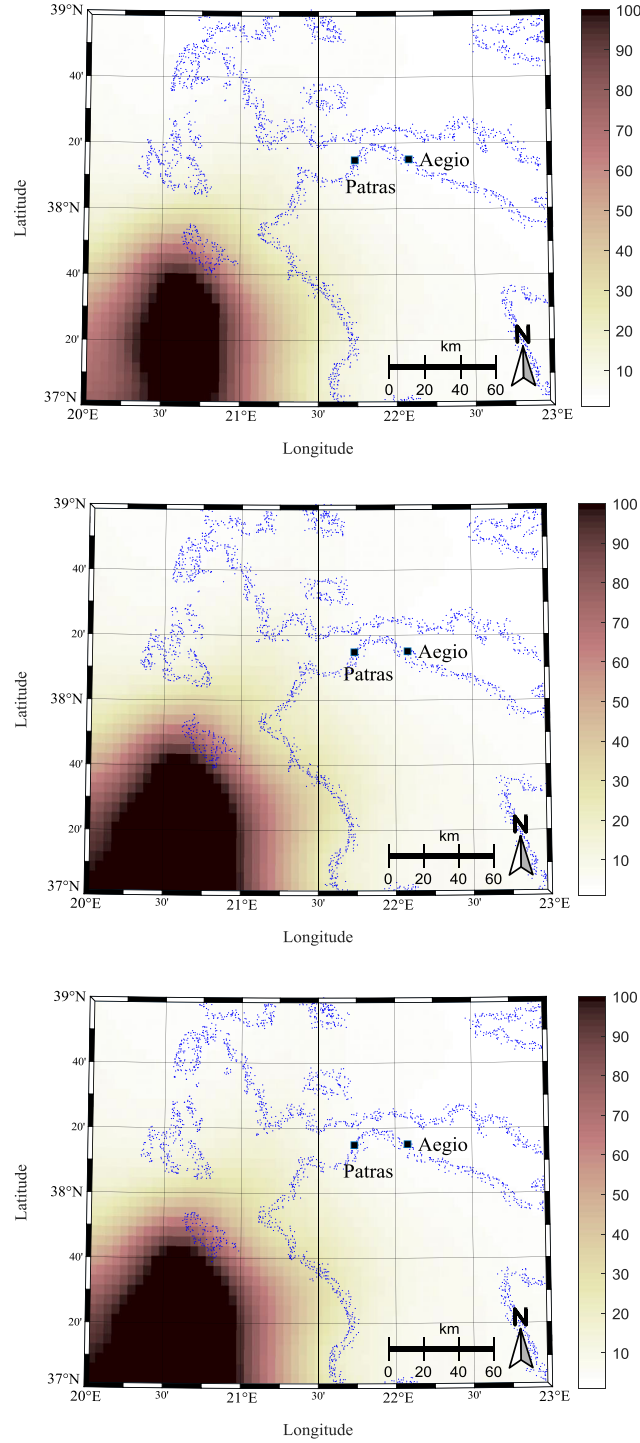


**Figure 8.** Short-term PSHA for Patras, left-hand panel: the short-term time-dependent daily probability of exceedance versus  $PGA$  and comparison with the conventional daily hazard curve and right-hand panel: short-term time-dependent daily rate of exceedance versus  $PGA$  and comparison with the conventional daily hazard curve.

hazard calculations. The aftershock zone is subdivided into 14 area sources as defined in ESHM13 and shown in Fig. 7. The results of the conventional and time-dependent PSHA are shown in Fig. 8 for Patras city. The left graph in Fig. 8 is for the daily probability of exceedance, and the right graph is for the daily rate of exceedance. It is assumed that a Poisson process models the occurrence of earthquakes of interest. It is worth mentioning that a complex logic-tree is not recommended for OEF, since the computational effort should be kept to a minimum level to obtain the forecasts as rapidly as possible.

In the next step,  $\lambda(M > M_{\min})$  is altered with the expected number of events within the forecasting interval (herein, 1-d) resulting from the implemented seismicity forecasting framework to account for the summation of background seismicity (from conventional PSHA) and short-term seismicity (see eq. 4). The hazard integral (eq. 5) is computed again based on this increased short-term seismicity. The results of this time-dependent PSHA are shown in the left (daily probability of exceedance) and the right (daily rate of exceedance) panels in Fig. 8 for Patras on 26 October 2018. For the purpose of comparison with the conventional PSHA, the annual frequency of exceedance derived from the long-term (time-independent) hazard is converted to the daily rate (dividing by 365) and consequently transformed into the daily probability of exceedance using the Poisson distribution. It is worth mentioning that the conventional hazard curve represents a lower bound for this short-term hazard curve, since we assume that the short-term seismicity can only increase the long-term hazard.

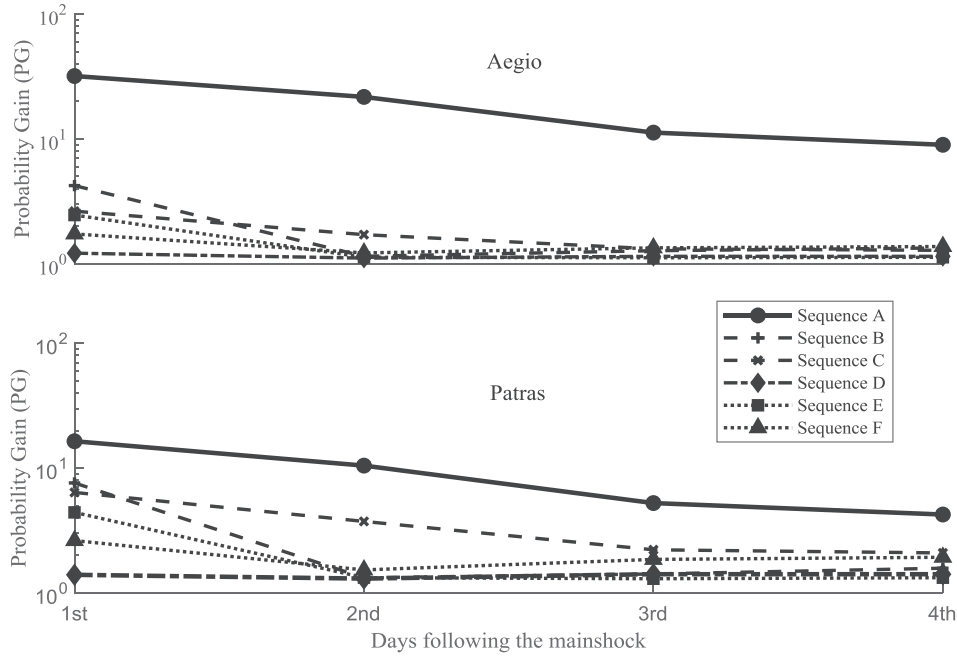
The short-term hazard ratio to the median conventional hazard is defined as the *Probability Gain* (PG), which is a function of the considered  $PGA$ . As can be seen in Fig. 8, the PG parameter decreases as  $PGA$  increases. The PG parameter, corresponding to a  $PGA$  equal to 0.05 g, is calculated for all the cells inside the study area and the results are shown in Fig. 9 in terms of 2nd, 50th and 98th percentiles.



**Figure 9.** The spatial distribution of the PG parameter (the ratio of short-term hazard to the long-term time-independent hazard corresponding to a  $PGA$  equal to 0.05 g) for sequence F (Table 1). The forecast starts at 00:00UTC on 26 October 2018 and for the next 24 hr. top panel: 2nd percentile, middle panel: 50th percentile and bottom panel: 98th percentile.

These percentiles are based on the dispersion of the forecasted number of events obtained from the robust seismicity framework. It is worth mentioning that the background seismicity is kept to the median value for all three cases. The maximum PG values occur around the main shock's epicentre, and equal 321, 385 and 448, respectively, in the cases of 2nd (Fig. 9-top), 50th (Fig. 9-middle) and 98th percentiles (Fig. 9-bottom). However, the colour bar in Fig. 9 is limited to 100 to better distinguish the differences amongst the cells.

PG can also be considered for a given site with respect to time since the main shock. The variation of the 50th percentile PG for the cities of Patras and Aegio is shown in Fig. 10 for all the sequences in Table 1 during the 4 d following each sequence's main shock. The



**Figure 10.** The median probability gain PG (the ratio of the median short-term time-dependent to the median long-term time-independent hazard corresponding to a  $PGA$  equal to 0.05 g) versus days since the main shock at Patras and Aegio for the different seismic sequences in Table 1.

results reveal that the heightened seismicity decays rapidly during the first 2 d (the so-called ‘golden hours’ for first responders) following the main shock. The 50th percentile PG is as high as 33 in Aegio (23 km from the epicentre of the main shock of sequence A, see Table 1) during the first hours following the main shock whereas, the 50th percentile PG equals 17 in Patras (50 km from the epicentre) in this time period. As seen in Fig. 10, the same trend is seen for sequence C (see Table 1), the second closest event to the studied cities among the six selected sequences. The other seismic sequences show lower PG values (mostly less than 10) since their main shock epicentres are far from the studied cities. For example, the 50th percentile PG value is about 3 in the case of sequence F (starting on 26 October 2018), which can also be seen in Fig. 8 for a  $PGA$  equal to 0.05 g.

## 7 CONCLUSIONS

A robust seismicity forecasting framework has been applied using the ISC earthquake catalogue for western Greece, one of the most seismically active regions in Europe. The chosen catalogue was used to identify six aftershock sequences between 1995 and 2018 with at least one main shock with moment magnitude  $M_w \geq 6$ . A new approach has been introduced for incrementally adaptive training of the ETAS model parameters prior to the main shock, which can be further used to start forecasting quickly after the main shock. The developed algorithm facilitates the concept of operational earthquake forecasting, which aims at forecasting damaging earthquakes during the first golden hours after a severe main shock. It is worth emphasizing that the used algorithm takes advantage of Bayesian inference, in contrast to the majority of the available studies which use constant ETAS coefficients. The forecasting algorithm is applied for the next 24 hr to forecast the spatial distribution of the seismicity rate and the number of potentially damaging earthquakes (here defined as an event with a moment magnitude  $M_w \geq 4.5$ ). In addition, the proposed algorithm has been tested to demonstrate its usability for operational forecasting on the basis of intervals of 6 hr to 7 d. The results show that the adapted ETAS model within the seismicity framework can retrospectively forecast the number of damaging earthquakes and that the forecasts are generally in good agreement with the observed data. The spatial distribution of the heightened seismicity zone is also in good agreement with the spatial propagation of observed events. This seismicity forecasting framework has been applied to the six selected seismic sequences, and posterior distributions of the model parameters were obtained by using Bayesian inference. These distributions and their relative bounds are proposed as prior values for future forecasting of new aftershock sequences in the region. The results of the current study reveal that the temporal decay of events follows almost the same MO’s law for all sequences; however, the spatial and magnitude–frequency (Gutenberg–Richter) characteristics are sequence-specific.

The forecasted occurrence rates were implemented within a time-dependent seismic hazard framework using inputs on the long-term seismicity from ESHM13. The daily seismic hazard was computed for the study area as well as for the two major cities of the study region, Patras and Aegio. The results revealed that the daily probability of exceeding a threshold  $PGA$  equal to 0.05 g is, on average, increased by up to 33 times the long-term (time-independent) hazard in Aegio, during the first hours following the 1995  $M_w$  6.5 main shock. This PG parameter decays to under 10 after 3 d. Additionally, the PG parameter varies between 1 and 10 for the four seismic sequences (B, D, E and F)

that are relatively far from the considered cities. It is important to note that multiple types of uncertainty have been addressed in the proposed forecasting framework, such as Bayesian inference and MCMC simulations in the ETAS forecasting model, and GMPE and logic-tree in the hazard model. However, the optimum choice of GMPE and associated logic-tree weights for this region, and more generally for operational earthquake forecasting globally, remains an interesting topic for future research. Also, considering uncertainties from different sources such as the PSHA and forecasting algorithms is an area to be explored in future.

The current study has demonstrated the applicability of the proposed forecasting algorithm for short-time intervals (by emphasizing medium-to-large events), which is of great interest for first responders during an aftershock sequence. The forecasted distribution was in good agreement with the observed events in all retrospectively studied earthquake sequences. Besides, the spatial distribution of forecasted events was close to the distribution of observed events. Therefore, at least within the assumption and limitations of this study, it is concluded that the used Bayesian inference has the ability to be adapted to the specific characteristics of earthquakes in this region.

## ACKNOWLEDGMENTS

This study was supported by the European Union's Horizon 2020 research and innovation programme under grant agreement No 821046, project TURNkey (Towards more Earthquake-resilient Urban Societies through a Multi-sensor-based Information System enabling Earthquake Forecasting, Early Warning and Rapid Response actions). We thank the partners of Workpackage 3 of TURNkey and the project management team for their comments on these analyses. Finally, we thank two anonymous reviewers and the journal editor (Dr Margarita Segou) for their detailed and constructive comments on earlier versions of this manuscript in which substantially enhanced the paper's quality.

## DATA AVAILABILITY

Earthquake catalogue data were provided by ISC (last accessed 2020). The data regarding this paper can be found online at <https://earthquake-turnkey.eu/> or by contacting the corresponding author.

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## APPENDIX A: SAMPLING $\theta$ FROM THE DISTRIBUTION $p(\theta|\text{seq}, M_l)$

The probability distribution  $p(\theta|\text{seq}, M_l)$  in eq. (3) can be calculated using Bayesian parameter estimation as follows (see also Ebrahimian & Jalayer 2017):

$$p(\theta|\text{seq}, M_l) = C^{-1} p(\text{seq}|\theta, M_l) \cdot p(\theta|M_l) \quad (\text{A1})$$

where  $p(\text{seq}|\theta, M_l)$  denotes the likelihood of the observed sequence given the vector of model parameters  $\theta$  and lower cut-off magnitude  $M_l$ ,  $p(\theta|M_l)$  is the prior distribution for the vector  $\theta$ , and the term  $C^{-1}$  is a normalizing constant. In lieu of additional information (e.g. statistics of regional model parameters), the prior joint distribution  $p(\theta|M_l)$  can be estimated as the product of marginal uniform probability distributions for each model parameter. The calculation of the likelihood  $p(\text{seq}|\theta, M_l)$  is discussed in detail in Ebrahimian & Jalayer (2017).

In order to sample from  $p(\theta|\text{seq}, M_l)$ , a MCMC simulation routine is used, which is particularly useful for cases where the sampling needs to be done from a probability distribution that is known up to a constant value, that is  $C^{-1}$  herein (see Beck & Au 2002). The MCMC routine uses the Metropolis–Hastings (MH) algorithm (Metropolis *et al.* 1953; Hasting 1970) in order to generate samples as a Markov Chain sequence used first to sample from the target probability distribution  $p(\theta|\text{seq}, M_l)$ , and later to estimate the robust seismicity forecasting in eqs (3) and (4). The MH routine generates a Markov chain that produces a sequence of samples  $[\theta_1 \rightarrow \theta_2 \rightarrow \dots \rightarrow \theta_n \rightarrow \dots]$ , where  $\theta_n$  represents the state of Markov Chain at  $n$ th iteration. It can be shown that the samples from the chain after the initial transient ones (the first few samples are often discarded to reduce the initial transient effect) reflect samples from the target distribution  $p(\theta|\text{seq}, M_l)$ . To generate the  $(n+1)$ th sample  $\theta_{n+1}$  given that the  $n$ th sample  $\theta_n$  is already known, the following procedure is performed:

- Generate a candidate sample  $\theta^*$  from a proposal (candidate) distribution  $q(\theta|\theta_n)$ . It is important to note that there are no specific restrictions about the choice of  $q(\cdot)$  apart from the fact that it should be possible to calculate both  $q(\theta_{i+1}|\theta_i)$  and  $q(\theta_i|\theta_{i+1})$ .
- Accept the candidate sample with the probability  $\min(1, r)$  (where  $r$  is defined in eq. (A2) as follows) and set  $\theta_{n+1} = \theta^*$ ; otherwise,  $\theta_{n+1} = \theta_n$ :

$$r = \frac{p(\theta^*|\text{seq}, M_l)}{p(\theta_n|\text{seq}, M_l)} \cdot \frac{q(\theta_n|\theta^*)}{q(\theta^*|\theta_n)} = \left( \frac{p(\text{seq}|\theta^*, M_l)}{p(\text{seq}|\theta_n, M_l)} \cdot \frac{p(\theta^*|M_l)}{p(\theta_n|M_l)} \right) \cdot \frac{q(\theta_n|\theta^*)}{q(\theta^*|\theta_n)}, \quad (\text{A2})$$

where  $\frac{p(\text{seq}|\theta^*, M_l)}{p(\text{seq}|\theta_n, M_l)}$  is the likelihood ratio;  $\frac{p(\theta^*|M_l)}{p(\theta_n|M_l)}$  is the prior ratio;  $\frac{q(\theta_n|\theta^*)}{q(\theta^*|\theta_n)}$  is the proposal ratio.

It can be shown, see Beck & Au (2002); Ebrahimian & Jalayer (2017), using the Total Probability Theorem that, if the current sample  $\theta_n$  is distributed as  $p(\cdot|\text{seq}, M_l)$ , the  $(n+1)$ th sample  $\theta_{n+1}$  is also distributed as  $p(\cdot|\text{seq}, M_l)$ . In order to improve the rate of convergence of the simulation process, we have used an adaptive MH algorithm, as proposed by Beck & Au (2002), that introduces a sequence of intermediate evolutionary candidate PDF's that resemble more and more the target PDF.

## APPENDIX B: LIST OF SYMBOLS

| Symbol                               | Meaning                                                                                                                                                               | Symbol                                       | Meaning                                                                                                                                                                   |
|--------------------------------------|-----------------------------------------------------------------------------------------------------------------------------------------------------------------------|----------------------------------------------|---------------------------------------------------------------------------------------------------------------------------------------------------------------------------|
| Mw                                   | Moment magnitude                                                                                                                                                      | $N_b(x, y, m M_I)$                           | a constant representing the area's background seismicity                                                                                                                  |
| A                                    | Aftershock zone                                                                                                                                                       | $\mathbb{E}[N(x, y, m \mathbf{seq}, M_I)]$   | the average number of events in the cell centred at $(x, y)$ with a magnitude $\geq m$ in the forecasting interval $[T_{\text{start}}, T_{\text{end}}]$                   |
| $\lambda_{\text{ETAS}}$              | The conditional rate of occurrence of earthquakes                                                                                                                     | $\Omega_\theta$                              | the domain of the model parameters                                                                                                                                        |
| $\theta$                             | Model parameters                                                                                                                                                      | $p(\theta \mathbf{seq}, M_I)$                | conditional posterior probability density function (PDF) for $\theta$ given the $\mathbf{seq}$ and the lower cut-off magnitude $M_I$                                      |
| $\mathbf{seq}_t$                     | past events                                                                                                                                                           | $\mathbf{seqg}$                              | the events within the forecasting interval                                                                                                                                |
| $M_I$                                | lower cut-off magnitude                                                                                                                                               | $p(\mathbf{seqg} \theta, \mathbf{seq}, M_I)$ | the PDF for the generated sequence $\mathbf{seqg}$ given that $\theta$ and $\mathbf{seq}$ are known                                                                       |
| $M_c$                                | Magnitude of completeness                                                                                                                                             | 'M'                                          | Number of months before the forecast interval when applying the <i>incremental adaptive training algorithm</i>                                                            |
| $\beta$                              | related to the Gutenberg–Richter relation                                                                                                                             | 'E'                                          | arbitrary subsets of events with magnitude $\geq M_c$ when applying the <i>incremental adaptive training algorithm</i>                                                    |
| $c$ and $p$                          | MO's Law parameter                                                                                                                                                    | 'D'                                          | Each 'E' subset covers at least 'D' days of the catalogue when applying the <i>incremental adaptive training algorithm</i>                                                |
| $d$ and $q$                          | spatial distribution of the triggered events                                                                                                                          | $\sigma$                                     | Standard deviation                                                                                                                                                        |
| $K$                                  | calibration for each forecasting interval                                                                                                                             | $\lambda(PGA > pga)$                         | the annual rate of exceedance of <i>PGA</i> above a threshold <i>pga</i>                                                                                                  |
| $K_t$                                | Unifies the time-dependent term over infinite time                                                                                                                    | $M_{\min}$                                   | The minimum magnitude in PSHA                                                                                                                                             |
| $K_R$                                | Unifies the spatial term over infinite space                                                                                                                          | $M_{\max}$                                   | The maximum magnitude in PSHA                                                                                                                                             |
| $\alpha$                             | efficiency of an event in generating aftershock activity                                                                                                              | $\lambda(M > M_{\min})$                      | the annual rate of exceedance of earthquakes greater than $M_{\min}$                                                                                                      |
| $[T_{\text{start}}, T_{\text{end}}]$ | forecasting interval                                                                                                                                                  | $P(PGA > pga m, d\{(x, y), (x_s, y_s)\})$    | the conditional probability of <i>PGA</i> exceeding a threshold <i>pga</i> , given a magnitude <i>m</i> and a epicentral distance <i>d</i> at the $(x, y \in \mathbf{A})$ |
| $T_o$                                | time of origin                                                                                                                                                        | $f_M(m)$                                     | probability density function of magnitude                                                                                                                                 |
| $\mathbf{seq}$                       | The observation history of $N_o$ events that took place before the forecasting interval $[T_o, T_{\text{start}}]$                                                     | $f_{X,Y}(x, y)$                              | the joint probability density function of the distance distribution                                                                                                       |
| $N(x, y, m \mathbf{seq}, M_I)$       | The number of events at the centre point of a given cell centred at $(x, y)$ with magnitude $\geq m$ in the forecasting interval $[T_{\text{start}}, T_{\text{end}}]$ |                                              |                                                                                                                                                                           |