

1 **Unraveling high-pressure gas storage mechanisms in shale nanopores through SANS**

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11 **Abstract**

12 As storage rocks rather than source rocks, shale reservoirs can become a target to store
13 methane in terms of energy security and sequester CO₂ in the long-term to mitigate climate change.
14 Despite extensive studies investigating geochemical and geophysical properties of shale and gas
15 adsorption and transport in shale matrix, limited studies have been devoted to characterizing
16 nanoscale gas storage mechanisms in shale at high pressure. In this study, contrast-matching small-
17 angle neutron scattering (SANS) has been conducted to quantify the gas storage mechanisms and
18 capacity in three shale samples up to elevated high pressure. The estimated average scattering
19 length density (SLD) in pores is smaller than the SLD of bulk phase at the pressure between 100
20 bar and the contrast-matched point (~600-700 bar), indicating a lower average adsorbed phase
21 density in the pressure range for the measured shale samples. Three essential factors, including the
22 final injection pressure, total organic carbon (TOC), and the accessible porosity, have been
23 determined to screen a potential targeted shale reservoir and maximize methane storage and long-
24 term CO₂ sequestration.

25 **Keywords:** Shale; nanoscale; gas storage and sequestration; contrast-matching SANS; adsorption

26 **1. Introduction**

27 Among the energy sources, natural gas is considered an abundant, reliable, and clean
28 energy¹. Due to the technical maturity of horizontal well drilling and hydraulic fracturing², natural
29 gas exploitation and development in the United States have been heavily focused on shale
30 reservoirs in recent decades³. Although commercial development of shale gas reservoirs has been
31 conducted in the last decades, fluid transport dynamics in shale remain poorly understood with
32 many specificities left unexplained⁴. One of the critical challenges for long-term shale gas
33 production optimization is lacking reliable multi-scale and multi-mechanics gas transport model⁴.
34 Meanwhile, the increasing trend of anthropogenic greenhouse gas emissions, *e.g.*, methane and
35 CO₂, is alarming for global warming and its associated climate change⁵. One reason for the
36 increase of atmospheric CO₂ concentration is the power generation by burning fossil fuels, which
37 has adverse effects on the earth's ecological environment due to the raises of the global average
38 temperature⁵. Net emission of CO₂ must approach zero to meet the Paris Agreement's criteria of
39 limiting the increase of global temperature within 2 °C or 1.5 °C above pre-industrial levels⁶.
40 According to the Research Agenda for CO₂ removal and reliable sequestration⁶, several feasible
41 negative-emission technologies and research & development plans have been identified, including
42 (1) biological CO₂ sequestration in soils, forests, and wetlands; (2) synchronized bioenergy
43 production and CO₂ capture; (3) coupling direct-air-capture and geological sequestration; and (4)
44 enhancing geologic carbon mineralization or “weathering”. CO₂-enhanced shale gas recovery and
45 CO₂ sequestration in depleted shale gas reservoirs could be the cost-effective strategy to
46 permanently store densified CO₂ in subsurface shale formations. With various mineral and organic
47 matters, shale rock has hierarchical pore structures, including micro-fractures and macro-/meso-
48 /micro-pores⁷⁻¹¹. Methane or CO₂ is primarily stored as a free phase through the gas compression

49 in fracture voids and macropores, and as both bulk and adsorbed phases in meso-/micropores in
50 shales^{12,13}. In general, the gas sorption capacity in shale is low due to the low total organic carbon
51 (TOC) content¹²⁻¹⁵. And the adsorbed phase density is usually obtained either by using an
52 empirical value^{13,16} or curve-fitting^{16,17} or analytical/molecular simulation methods^{18,19}, which
53 could cause inaccuracy to determine the real sorption capacity for a given *in situ* pressure and
54 temperature conditions. The total gas storage capacity in shale is the sum of bulk phase and
55 adsorbed phase gases. Therefore, understanding the gas storage behaviors in shale nanopores has
56 practical applications on gas transport modeling and the estimation of the potential of methane or
57 carbon storage in shale reservoirs.²⁰ The understanding could determine the injection rate and the
58 potential of CO₂ sequestration in shale reservoirs to meet the challenge of climate change
59 mitigation²¹.

60 Numerous techniques can be successfully used to characterize pore structure in shale^{22,23},
61 specified as invasive and noninvasive methods. However, only a limited number of studies have
62 been devoted to characterizing gas storage and condensation behaviors in shale nanopores under
63 *in situ* pressure and temperature conditions. Fortunately, small-angle neutron scattering (SANS)
64 can be used to noninvasively quantify the structures of total nanopores in shale²⁴⁻²⁷. Combining
65 SANS with the contrast-matching method, or so-called contrast-matching SANS, pore
66 accessibility^{10, 28-30} and gas behaviors in pores^{31, 32} can be invasively quantified. Therefore,
67 contrast-matching SANS is an excellent choice to determine gas storage behaviors in shale
68 confined nanopores under *in situ* gas injection³³. This study focuses on the characterization of
69 nanopore structures of three shale samples and gas storage behaviors in accessible nanopores
70 through *in situ* contrast-matching SANS measurements. CD₄ injection was used in this study
71 because high-pressure CD₄ can have a relatively high scattering length density (SLD) than CO₂

72 which can reach or approach the contrast-matched condition of the shale samples with relatively
73 high SLDs. We found that the Illinois shale sample with the highest TOC has the lowest pore
74 accessibility. As the increase of injection gas pressure, adsorbed methane density in shale
75 nanopores is found to be higher than bulk phase at relatively low pressure, lower than bulk phase
76 at relatively high pressure, and again higher than bulk phase at even higher pressure. TOC could
77 be the determining factor of gas storage in micropores because of the high affinity of gas leading
78 to high adsorption. For free compression gas storage, accessible porosity of macro-/mesopores is
79 found to be the leading controlling factor of total gas storage capacity. Apparently, the total gas
80 storage will depend on the final equilibrium pressure in shale reservoirs. We believe the current
81 research will improve fundamental understandings on methane storage and long-term CO₂
82 sequestration in shale reservoirs.

83 **2. Materials and methods**

84 **2.1 Sample preparation and characterization**

85 Three shale powder samples, pulverized to 60-80 mesh sizes (0.177-0.25 mm), were
86 prepared from fresh block samples collected from different shale formations, including Marcellus
87 Formation in Pennsylvania, USA, Illinois Basin in Indiana, USA, and Longmaxi Formation in
88 Sichuan, China. Marcellus Formation describes the upper Eifelian and lower Givetian stage
89 mudrock-dominated strata lying in the Middle Devonian timescale.³⁴ The shale outcrop fresh
90 blocks were obtained in Frankstown, Pennsylvania. The collected shale in Illinois Basin is a roof
91 shale above the Coal V (Springfield Coal Member, Petersburg Formation, Pennsylvania System)
92 or so-called Springfield coal and below the Alum Cave Limestone Member, Dugger Formation.^{35,}
93 ³⁶ The roof shale is a black fissile marine shale.^{35, 36} The roof shale fresh blocks were obtained
94 from Bear Run Surface Mine in Carlisle, Indiana. Longmaxi Formation located in the Yangtze

95 area is in the Lower Silurian timescale.³⁷ The shale outcrop fresh blocks were obtained in Yibin,
96 Sichuan, China.

97 The pulverized samples were oven-dried for 24 hours at 80°C, and all the dried samples
98 were sealed in the air-tight Ziploc bags before the contrast-matching SANS and the
99 sorption/diffusion measurements. X-ray diffraction (XRD) and LECO CS230 carbon/sulfur
100 determinator were conducted to obtain the mineralogical information and the TOC of the samples,
101 respectively, as shown in Table S2 in the SI. We can find that the Marcellus shale is quartz-rich,
102 containing more than 70% quartz. The Longmaxi shale also has a relatively high amount of quartz
103 at nearly 50%, with an addition of 20% calcite. The chemical compositions were used to estimate
104 the effective scattering length density (SLD) of each shale sample. We can see that sample with a
105 relatively high TOC content has a relatively low estimated effective SLD. The estimated SLDs
106 were used for SANS data analysis to characterize the information of nanopore structures
107 quantitatively.

108 **2.2 Contrast-matching SANS measurement**

109 The contrast-matching SANS measurements were conducted using the vSANS instrument
110 at the NIST Center for Neutron Research (NCNR). Each dried powder sample was filled into an
111 aluminum capsule, and then the aluminum capsule was placed into the high-pressure cell as shown
112 in Fig. S1. The neutron wavelength λ was set at 6 Å. A small λ helps to minimize the multiple
113 scattering effect. The neutron wavelength spread $\Delta\lambda/\lambda$ was 0.12. Two configurations were used for
114 the measurements. The first configuration named as NG7 using the sample-to-detector distances
115 of 1.93 m for the Front four detectors and of 9.13 m for the Middle four detectors to cover a
116 scattering vector Q range between $\sim 4.8 \times 10^{-3}$ and $\sim 0.34 \text{ \AA}^{-1}$, corresponding to a length scale d , or
117 pore diameter, range between $\sim 1.3 \times 10^3$ and $\sim 18.6 \text{ \AA}$, where the relationship $d = 2\pi/Q$ was used.

118 The second configuration named as NG2 using the sample-to-detector distances of 4.13 m for the
119 front four detectors and of 19.13 m for the middle four detectors to cover a Q range between
120 $\sim 2.5 \times 10^{-3}$ and $\sim 0.16 \text{ \AA}^{-1}$, corresponding to a d range between $\sim 2.5 \times 10^3$ and $\sim 38.6 \text{ \AA}$. Both the
121 NG7 and NG2 configurations were used to measure the Marcellus shale and Longmaxi shale
122 samples. Only the NG7 configuration was used to measure the Illinois shale sample due to limited
123 beam time.

124 All three shale samples were dosed by deuterated methane (CD_4) with incremental gas
125 pressure for the contrast-matching SANS measurements. The maximum conducting pressure was
126 700 bar for the Marcellus shale and the Longmaxi shale samples and 600 bar for the Illinois shale
127 sample. Scattering counts were measured under vacuum condition first and then under each
128 incremental pressure with 100 bar as the pressure interval till the maximum conducting pressure
129 for each sample. Scattering counts were measured under vacuum condition again after the methane
130 injection for all the samples. After the data acquisition, obtained 2D scattering profiles were
131 radially averaged to 1D scattering profiles for each configuration using the Igor macros vSANS
132 procedures³⁸. 1D scattering profiles at two sample-to-detector distances were merged for each
133 configuration. For the Marcellus shale and Longmaxi shale samples using two configurations
134 during the measurements, 1D scattering profiles of the two configurations were further merged.

135 **3. Results and discussion**

136 In this section, we first provide the interpretation of SANS data analyses and pore structure
137 information of the measured shale samples as baseline information. Then, we estimate the average
138 SLDs in the accessible pores, which will give the information of gas condensation under
139 confinement and gas storage mechanisms. At last, we provide the implication of gas storage in
140 underground shale reservoirs.

141 3.1 SANS data analyses and pore structures of the measured shales

142 The background-subtracted scattering intensities as a function of Q and methane pressure
143 for the Marcellus shale are shown in Fig. 1, and for the Illinois shale and Longmaxi shale samples
144 are shown in Figs. S2 and S4 in the Supporting Information (SI). The flat scattering background
145 was estimated by fitting the scattering intensity in the Q range from 0.3 \AA^{-1} to the highest Q value
146 for each shale sample's scattering profile. We can see that scattering intensity decreases with
147 increasing pressure at middle and low Q regions. However, scattering intensities do not have
148 noticeable change and have higher uncertainties at the high Q region. By choosing specific Q
149 values at the middle, low, and high Q regions, scattering intensity at each Q value as a function of
150 pressure can be demonstrated in detail, and the data can be compared (Figs. 2, S3, and S5).
151 Scattering intensity at the representative middle or low Q value rapidly decreases as gas pressure
152 increases and gradually decreases with further increasing pressure for all the samples (Figs. 2ab,
153 S3ab, and S5ab). This is because the increase of SLD of CD_4 as a function of gas pressure is known
154 to be nonlinear, as shown in Table S1 and Fig. S6 in the SI. SLD of CD_4 rapidly increases with
155 increasing pressure before 300 bar, followed by a gentle and gradual increase of SLD after 300
156 bar. However, there is no clear trend between scattering intensity and gas pressure at the
157 representative high Q value for each sample (Figs. 2c, S3c, and S5c), indicating either CD_4 is
158 already highly densified at small nanopores before 100 bar or limited fine pores are accessible to
159 the guest gas or incoherent background has already surpassed the elastic intensity of fine pores
160 which was subtracted initially³⁹. We can tell that the Marcellus shale sample has reached the
161 contrast-matched condition at ~ 600 bar at low Q and ~ 400 bar at middle Q (Fig. 1ab). However,
162 the Illinois shale and Longmaxi shale samples did not reach the contrast-matched point
163 experimentally but were approaching (Figs. S3ab and S5ab). Reaching the contrast-matched point

164 at a smaller pressure at the middle Q region compared to the low Q region indicates a smaller SLD
165 of the solid matrix surrounding middle-sized pores than large-sized pores for the Marcellus shale
166 sample. Since most mineral matter have higher SLD than organic carbon, organic matter in
167 Marcellus shale could contain smaller pores than mineral matter^{9, 40}. Another possible reason
168 could be a higher degree of gas densification in smaller pores^{32, 39}.

169 Pore accessibilities of three shale samples were estimated by the previously determined
170 method using the scattering intensities under vacuum and contrast-matched conditions^{41, 42}

$$171 \quad C_{ac}(Q) = 1 - \frac{I_{cm}(Q)}{I_{va}(Q)} \quad (1)$$

172 where $I_{va}(Q)$ and $I_{cm}(Q)$ are the background-subtracted scattering intensities under vacuum and
173 contrast-matched conditions, respectively. Since we used powder samples, the estimated pore
174 accessibility should be the volumetric and statistical average pore accessibility of each shale
175 sample⁴⁰, where the results are shown in Fig. 3a. We can find that pore accessibilities of the three
176 shale samples decrease with increasing Q in general, which provides direct evidence that the
177 smaller pore is less accessible. Pore accessibilities of the Marcellus shale and Longmaxi shale
178 samples are higher than that of Illinois shale, which could be because of lower amounts of organic
179 matter in the Marcellus shale and Longmaxi shale samples in comparison with Illinois shale. The
180 Longmaxi shale has the smallest TOC and has the highest pore accessibility among the measured
181 samples.

182 Furthermore, pore volume distributions of the shale samples were estimated by the model
183 fitting method^{39, 40, 43}. The background-subtracted 1D scattering profiles under vacuum condition
184 were used to fit using the maximum entropy (MaxEnt) method in the Igor macros Irena package
185⁴⁴. Without using a statistic function of pore size distribution, the MaxEnt method can provide a

186 more accurate result in multimodal pore volume distribution for a given two-phase porous material.
187 The background-subtracted scattering intensity can be expressed as ⁴⁵

188
$$I(Q) = N(\rho_s^* - \rho_p^*)^2 \int V^2(r)f(r)P(Q, r)dr \quad (2)$$

189 where N is the pore number density; ρ_s^* and ρ_p^* are the SLDs of the solid matrix and the pores; r
190 is the spherical radius; $V(r)$ is the spherical volume; $f(r)$ is the pore size distribution; and $P(Q, r)$
191 is the spherical form factor. SLD of the pores (ρ_p^*) should be zero under vacuum condition. The
192 estimated effective SLD of each shale sample in Table S2 was used for the solid matrix SLD. The
193 upper and lower limits of the pore diameter were set as 3000 Å and 10 Å for the model-fitting of
194 the Marcellus shale and Longmaxi shale samples. However, for the Illinois shale sample, a smaller
195 upper limit of the pore diameter (1500 Å) was used because only the NG7 configuration was used
196 for the measurement due to the limited beam time. Thus, the probed pore diameter size range is 1-
197 300 nm for Marcellus and Longmaxi shale sample and 1-150 nm for the Illinois shale. The results
198 of pore volume distributions with uncertainties are shown in Fig. 3b. The unit of volume
199 distribution is $\text{cm}^3/(\text{cm}^3 \cdot \text{Å})$ i.e., $dV/(V \cdot dD)$. We can find that pore volume distributions of all the
200 shale samples are multimodal. The main peak at the pore diameter of ~ 20 Å and a small peak at
201 the pore diameter of ~ 55 Å are shown in the volume distributions of the Marcellus shale and Illinois
202 shale samples. However, a relatively lower and broader hump at the pore range around 20-300 Å
203 is shown in the volume distribution of the Longmaxi shale sample. We can see multiple peaks at
204 larger pores ranging between 100 Å and 1000 Å for the Illinois shale sample, in which the volume
205 distribution is higher than the other two shale samples due to the relatively more pore population
206 in larger sized pores. The Marcellus and Longmaxi shale samples have very similar pore volume
207 distributions at pore diameter greater than ~ 100 Å, and both have small hump at pores around 1500
208 Å.

209 Besides, cumulative porosities and surface areas of the three samples were estimated based
210 on the estimated pore volume distributions. The cumulative porosity and surface area can be
211 estimated as ^{43, 44}

$$212 \quad \varnothing = N \int f(r)V(r)dr \quad (3)$$

$$213 \quad S = N \int f(r)A(r)dr \quad (4)$$

214 where $A(r)$ is the spherical surface area. The results of cumulative porosities and surface areas are
215 shown in Fig. 3c and d. There is a three-stage porosity increase with increasing pore size for the
216 Marcellus shale and Illinois shale samples and a two-stage increase of porosity for the Longmaxi
217 shale sample as shown in Fig. 3c. A rapid increase at the pore diameter around 30 Å for the
218 Marcellus shale and Illinois shale samples is because of the major peak of volume distribution (Fig.
219 3b). And then, porosity gradually increases till ~150 Å for the Illinois shale sample and till ~1000
220 Å for the Marcellus shale sample. After that, porosity rapidly increases till the upper pore limit,
221 that the SANS instrument can measure, for these two samples. In contrast, the Longmaxi shale
222 sample has a moderate increase of porosity before 1000 Å and a rapid increase of porosity after
223 1000 Å. Overall, the Illinois shale sample has a much higher total porosity than the other two shale
224 samples at the pore size of 1500 Å, which is the maximum measured pore size of the Illinois shale
225 sample. The surface area rapidly increases at the pore around 250 Å and gradually increases further
226 for the Illinois shale sample. The surface area of the Marcellus shale sample also rapidly increases
227 at the pore with a size of ~250 Å but barely increases afterward. The Longmaxi shale sample seems
228 to have a gradual increase of surface area over the entire pore range.

229 To characterize the nanopore structure evolution under different pressure conditions for the
230 shale samples, we have applied a global scattering function integrated Guinier approximation and
231 power-law scattering, a unified scattering model, for data-fitting, in which the unified scattering

232 model is superior to differentiate multiple structures in multiscale in a hierarchical porous medium.
 233 The method has been successfully used in shale in previous studies^{25, 46}. The unified scattering
 234 equation to describe multiple interrelated structural levels over a broad range of Q without
 235 considering background can be expressed as⁴⁷

$$236 \quad I(Q) = \sum_{i=1}^n [G_i \exp(-Q^2 R_{g_i}^2/3) + B_i \exp(-Q^2 R_{g_{i+1}}^2/3) \times (Q^*)^{-P_i}] \quad (5)$$

$$237 \quad Q^* = Q [\text{erf}(QR_{g_i}/\sqrt{6})]^{-3} \quad (6)$$

238 where the first term in Eq. 5 is the Guinier's exponential form and the second term is the
 239 structurally limited power-law form. Q^* is the modified scattering vector Q containing a three-
 240 dimensional Gaussian probability function, which accounts for the finite structural effect in the
 241 power-law region. G is the classic Guinier prefactor; R_g is the radius of gyration describing the
 242 domain size; B is the power-law prefactor; P is the power-law exponent; and i is the structural
 243 level, in which $i = 1$ refers to the largest-size structural level. The fitting of each scattering profile
 244 was conducted using SasView⁴⁸. The representative model fitting profiles can be found in Fig. S7,
 245 and the fitting parameters can be found in Figs. S8-S9 and Table S3-S5. A detailed discussion can
 246 be found in the SI.

247 **3.2 The average SLD in open pores**

248 We have used the bulk phase SLD of the injected gases to estimate the changes of pore
 249 volume and surface area with increased gas pressure in our previous studies^{39, 43}. The method
 250 ignores the contribution of the SLD of adsorbed phase density in pores. To characterize the average
 251 SLD or average density fluctuation in pores under elevated pressure conditions for the shale
 252 samples, the structure-free Porod invariant method considering three-phase approximation (*i.e.*,
 253 solid matrix, open pores, and closed pores, as shown in Fig. 4) can be used. The three-phase Porod
 254 invariant equation may be expressed as

255 $Q_{\text{inv}} = \int_{Q_{\text{min}}}^{Q_{\text{max}}} Q^2 I(Q) dQ = 2\pi^2 [(\rho_s^* - \rho_o^*)^2 \phi_s \phi_o + (\rho_s^* - \rho_c^*)^2 \phi_s \phi_c + (\rho_o^* - \rho_c^*)^2 \phi_o \phi_c]$ (7)

256 $\phi_s + \phi_o + \phi_c = 1$ (8)

257 where Q_{max} and Q_{min} are the maximum and minimum Q , which can be measured by the
 258 configuration of SANS experiments; ρ_o^* and ρ_c^* are the SLDs of the open and closed pores,
 259 respectively; and ϕ_s , ϕ_o , and ϕ_c are the volume fractions of the solid matrix, open pores, and
 260 closed pores, respectively. Q_{inv} can be estimated using the experimentally obtained scattering
 261 intensity under different pressure conditions, which is shown in Fig. 5. Note that the Q range to
 262 estimate the Porod invariant was set as $2.8 \times 10^{-3} - 0.25 \text{ \AA}^{-1}$, $5.3 \times 10^{-3} - 0.25 \text{ \AA}^{-1}$, and $2.5 \times 10^{-3} - 0.21$
 263 \AA^{-1} for the Marcellus shale, Illinois shale, and Longmaxi shale samples, respectively. Then the
 264 results can be more precisely compared among different pressure conditions for each sample,
 265 although some portion of high Q was ignored. The Marcellus shale sample may already reach the
 266 contrast-matched point at the pressure around 600 bar on average over the estimated pore range
 267 (Fig. 5). The SLD of CD₄ at 600 bar in room temperature is about $3.7 \times 10^{10} \text{ cm}^{-2}$, which is slightly
 268 smaller than the estimated effective SLD ($\sim 3.9 \times 10^{10} \text{ cm}^{-2}$) from the chemical compositions of the
 269 Marcellus shale. It suggests that slightly more open nanopores accessible to CD₄ are in the matrix
 270 with a smaller SLD, which could be organic matter. In contrast, the Longmaxi shale sample may
 271 approach the contrast-matched point at the pressure around 700 bar, and the Illinois shale sample
 272 may not reach the contrast-matched point over the pressure range measured (Fig. 5). It is
 273 unexpected for the two samples because the estimated effective SLD of the Longmaxi shale sample
 274 ($\sim 4.4 \times 10^{10} \text{ cm}^{-2}$) is higher than the SLD of CD₄ at the highest pressure (700 bar), which is
 275 $\sim 3.9 \times 10^{10} \text{ cm}^{-2}$, and the estimated effective SLD of the Illinois shale sample ($\sim 3.4 \times 10^{10} \text{ cm}^{-2}$) is
 276 less than the SLD of CD₄ at the pressure of 600 bar ($\sim 3.7 \times 10^{10} \text{ cm}^{-2}$). The results suggest that more
 277 open nanopores accessible to CD₄ are in the Longmaxi shale sample matrix with a lower SLD,

278 which could be organic matter, while in the matrix of the Illinois shale sample with a higher SLD,
279 which could be clay minerals such as glauconite.

280 In order to estimate the average SLD in open pores, ρ_o^* , using Eq. 7, the volume fractions
281 of the solid matrix, open pores, and closed pores, ϕ_s , ϕ_o , and ϕ_c , need to be quantified. The
282 average SLD in closed pores, ρ_c^* is equal to zero since the guest fluid does not have access to closed
283 pores, and there may be no residual fluid inside closed pores. ρ_o^* is equal to zero under vacuum
284 condition because of empty pores and equal to ρ_s^* under contrast-matched condition. Thus, in both
285 conditions, the three-phase Porod invariant equation reduces to the two-phase one

286 Vacuum: $Q_{inv} = \int_{Q_{min}}^{Q_{max}} Q^2 I(Q) dQ = 2\pi^2 (\rho_s^*)^2 \phi_s (\phi_o + \phi_c)$ (9)

287 Contrast-matched: $Q_{inv} = \int_{Q_{min}}^{Q_{max}} Q^2 I(Q) dQ = 2\pi^2 (\rho_s^*)^2 (\phi_s + \phi_o) \phi_c$ (10)

288 where the volume fraction of total pores equals to $\phi_o + \phi_c$. Since ~600 bar could be the contrast-
289 matched pressure of the Marcellus shale sample, the SLD of CD₄ at 600 bar ($3.7 \times 10^{10} \text{ cm}^{-2}$) was
290 used as the SLD of the sample along with the Q_{inv} at that pressure to quantify volume fractions of
291 total and closed pores and the average SLD in open pores in the Marcellus shale sample. However,
292 parabolic curve-fitting using the last five data points may give the smallest Q_{inv} and the contrast-
293 matched pressure for the Illinois shale and Longmaxi shale samples. The estimated Q_{inv} and
294 pressure at the contrast-matched point could be $1.33 \times 10^{-3} \text{ cm}^{-1} \text{ \AA}^{-3}$ and 711 bar for the Illinois shale
295 sample and $3.40 \times 10^{-4} \text{ cm}^{-1} \text{ \AA}^{-3}$ and 618 bar for the Longmaxi shale sample. The approximate
296 contrast-matched SLD can be obtained, which is $3.90 \times 10^{10} \text{ cm}^{-2}$ for the Illinois shale sample and
297 $3.73 \times 10^{10} \text{ cm}^{-2}$ for the Longmaxi shale sample. The estimated contrast-matched SLDs were used
298 to estimate the volume fractions of total and closed pores and the average SLD in open pores.
299 Table S6 shows the estimated volume fractions of open and closed pores and the corresponding
300 average pore accessibility. We can find that the Longmaxi shale sample has the highest volume

301 fraction of open pores. However, the Illinois shale sample has the highest volume fraction of closed
302 pores, as expected, because of the highest amount of organic matter among the three shale samples.
303 Accordingly, the Illinois shale sample has the smallest pore accessibility on average, consistent
304 with the size-dependent result shown in Fig. 3a. Besides, Pearson correlation analysis was
305 conducted using the variables of TOC, maturity, contrast-matched SLD, the volume fraction of
306 total pores, and pore accessibility. The correlation coefficients are shown in Table S7. We can find
307 that TOC and total pores are positively correlated. A highly negative correlation is shown between
308 TOC and pore accessibility. However, since we have only measured three shale samples, those
309 correlations may be different using more samples with diverse mineral and organic components,
310 and thus further study will be needed.

311 Using the estimated volume fractions of open and closed pores and the contrast-matched
312 SLDs, the average SLD in open pores over the specified pore range as a function of pressure for
313 each sample can be quantified, as shown in Fig. 6. Here the assumption is that the volume fractions
314 of open and closed pores do not change under pressurized conditions, which may hold for shale
315 rocks. The SLD of bulk CD₄ as a function of pressure is also shown in the figure for comparison.
316 Note that the Q range for estimation of the average SLD in pores was set as $2.8 \times 10^{-3} - 0.25 \text{ \AA}^{-1}$,
317 $5.3 \times 10^{-3} - 0.25 \text{ \AA}^{-1}$, and $2.5 \times 10^{-3} - 0.21 \text{ \AA}^{-1}$ for the Marcellus shale, Illinois shale, and Longmaxi
318 shale samples, respectively. By using the relationship $d = 2\pi/Q$, the pore diameter range is
319 $2.3 \times 10^3 - 25 \text{ \AA}$, $1.2 \times 10^3 - 25 \text{ \AA}$, and $2.5 \times 10^3 - 30 \text{ \AA}$ for the Marcellus shale, Illinois shale, and
320 Longmaxi shale samples, respectively. We can find that the average SLDs of the three samples
321 over the quantified pore range are smaller than that of bulk CD₄ when the pressure is smaller than
322 the contrast-matched pressure of each sample except for the SLDs at the pressure of 100 bar for
323 the Marcellus shale and Illinois shale samples (Fig. 6). When the pressure is higher than the

324 contrast-matched pressure, the average SLD in pores becomes greater than the SLD of the bulk
325 phase for the Marcellus shale and Longmaxi shale samples. It is well known that the stored gas in
326 shale nanopores could include both bulk gas and adsorbed gas. The average SLD in open pores
327 may be expressed as

$$328 \quad \rho_{ave}^* = \phi_b \rho_b^* + \phi_a \rho_a^* \quad (11)$$

329 where ρ_b^* and ρ_a^* are the SLDs of the bulk phase and adsorbed phase, respectively; and ϕ_b and ϕ_a
330 are the volume fractions of the bulk phase and adsorbed phase, respectively, in which the sum of
331 ϕ_b and ϕ_a is equal to one. A higher ρ_{ave}^* than ρ_b^* suggests a higher ρ_a^* than ρ_b^* on average in the
332 integrated pore range, *vice versa*. The measured samples' results hypothetically indicate that the
333 adsorbed phase density, ρ_a , in shale macro-/mesopores on average could be higher than the bulk
334 phase density, ρ_b , at the low-pressure region ($< \sim 100$ bar) because of surface adsorption (Fig. 7).
335 However, the average ρ_a could become smaller than the ρ_b at a higher pressure because of the
336 increase of adsorbed phase volume, V_a , in which surface adsorption could convert to partial pore-
337 filling adsorption (Fig. 7). When the gas pressure is even higher, there could be two situations: (1)
338 the completion of pore-filling adsorption occurs, in which the V_a increased to be the pore volume;
339 (2) the decrease of V_a occurs (Fig. 7). The second situation may be more likely in shale macro-
340 /mesopores because these nanopores may not have enough overlapped energy from the pore
341 surface to provide a possible complete pore-filling adsorption. From a laboratory perspective, the
342 excess or Gibbs adsorption capacity can be directly estimated either by gravimetric or volumetric
343 methods⁴⁹. In contrast, the absolute adsorption capacity, representing the real adsorption capability,
344 can only be estimated by correcting the excess adsorption capacity through assumptions. The usual
345 assumption of constant adsorbed phase density^{13, 16} could have less error in relatively low pressure
346 than higher pressure regions. The assumption of monolayer sorption volume or pore volume as

347 constant adsorbed phase volume^{50, 51} could have higher errors for sorption capacity estimation.
348 However, since we only measured three shale samples and do not have data points at relatively
349 low-pressure (< 100 bar) and significantly high-pressure regions (> 700 bar) because of limited
350 beam time, further research, either experimental or computational approaches, need to be
351 conducted to prove the hypothetical mechanism.

352 In addition, we have used three separated Q ranges for the Marcellus and Longmaxi shale
353 samples and two separated Q ranges for the Illinois shale sample to estimate Porod invariants as
354 a function of pressure using Eq. 7 as shown in Fig. S10 and further estimate the average SLDs in
355 open pores as shown in Fig. S11. The approximate segmentation is based on the definition of
356 meso-/macropores. The determined contrast-matched pressures and corresponding SLDs are
357 shown in Table S8. We can see that mesopores have a lower average SLD than macropores for all
358 the samples when pressure is higher than 100 bar, indicating a smaller average adsorbed phase
359 density in mesopores. A possible reason could be that occupation of gas molecules or adsorbed
360 phase volume at low pressure (< 100 bar) in mesopores is relatively higher than macropores. When
361 pressure continuously increases, lesser gas molecules could be adsorbed in mesopores, in which
362 the average adsorbed phase density will be smaller in mesopores.

363 **3.3 The implication on methane storage and CO₂ sequestration in shale reservoirs**

364 For carbon storage or sequestration in subsurface formations, all the potential phases,
365 including bulk phase, chemically reacted phase(s), physically adsorbed phase, and even dissolved
366 phase(s), will contribute to the total gas storage or sequestration in shale reservoirs. In this study,
367 since we used a single-phase dry gas, the stored phases could only be the bulk and adsorbed phases.
368 From the previous section, the average SLDs in nanopores under different pressure conditions

369 were quantified. The gas density and SLD of CD₄ have an approximately linear correlation shown
370 in Table S2. The total gas storage in shale nanopores may be estimated by

$$371 \quad m = \rho_{\text{ave}} V_o / m_s = \rho_{\text{ave}} [(V_o / V_t) / (V_s / V_t)] / (m_s / V_s) \cong \rho_{\text{ave}} (\phi_o / \phi_s) / \rho_{\text{he}} \quad (12)$$

372 where ρ_{ave} is the average gas density in pores; V_o , V_s , and V_t are the volumes of open pores, solid
373 matrix, and total matrix, respectively; m_s is the mass of the solid matrix; ρ_{he} is the helium density;
374 and m is the total gas storage capacity per unit mass. The helium densities of 2.55 g/cm³, 2.07
375 g/cm³, and 2.72 g/cm³ was used for the Marcellus shale, Illinois shale, and Longmaxi shale samples,
376 respectively. The estimated methane storage capacities as a function of pressure for the measured
377 three shale samples are shown in Fig. 8. The excess adsorption capacities of the shale samples are
378 also shown for comparison, although they were measured in the low-pressure region. Detailed
379 information on the experimental operation and adsorption capacity estimation can be found in
380 paper ¹⁵, and a schematic of the experimental system is shown in Fig. S12. All the volumetric
381 adsorption capacities are higher than the methane storage capacities obtained by *in situ* SANS at
382 the low-pressure region for the samples (Fig. 8). One possible reason could be that pores with
383 overall sizes contribute to the volumetric adsorption, while only a limited pore range was used to
384 estimate methane storage capacity from *in situ* SANS data. As mentioned in the previous section,
385 the pore diameter range for the estimation is $2.3 \times 10^3 - 25 \text{ \AA}$ for the Marcellus shale sample, 1.2×10^3
386 $- 25 \text{ \AA}$ for the Illinois shale sample, and $2.5 \times 10^3 - 30 \text{ \AA}$ for the Longmaxi shale sample. We can
387 see that the micropore region was excluded entirely in the estimation because the measured high
388 Q limit of the SANS profiles is not high enough to reach the length scale of micropores. Even
389 though the high Q limit is high enough to access the length scale of micropores, the scattering
390 background could be higher than the scattering of micropores restricting the micropore information
391 to be quantified. If we assume most of the volumetric adsorption capacity is the gas storage in

392 micropores because of high specific surface area ¹¹, we can see the micropore gas storage at the
393 pressure of ~100 bar is as high as the total gas storage in macro-/mesopores at the pressure of ~600
394 bar for the Illinois shale (blue curves in Fig. 8). The sample is highly organic-rich with a TOC of
395 ~30%. The storage capacity in adsorption in micropores is approximately four times higher than
396 the storage capacity of both bulk and adsorbed gas in macro-/mesopores at the pressure of ~100
397 bar. We may conclude that adsorption could dominate total gas storage in nanopores at relatively
398 low pressure in a highly organic-rich shale sample. For the relatively less organic-rich shale
399 samples, *i.e.*, Marcellus shale and Longmaxi shale samples, the gas adsorption in micropores is
400 less dominant than the total gas storage in the low-pressure region (red and yellow curves in Fig.
401 8). At the pressure of 200 bar, the total gas capacity is slightly higher than the adsorption one for
402 the Longmaxi shale sample. The total gas capacity is very similar to the adsorption one at the
403 pressure of 300 bar for the Marcellus shale sample. It is interesting to find that the adsorption
404 capacity has a positive correlation with TOC, and the total gas storage capacity at the pressure of
405 100 bar also has a positive correlation with TOC, although only three shale samples were measured
406 here. The total gas storage capacity at the pressures of 200 bar and 300 bar are similar among these
407 samples. When the pressure is beyond 300 bar, Longmaxi shale with the highest open pores has
408 the highest total gas storage capacity. The results suggest that a target shale reservoir with a high
409 gas storage capacity either for methane storage or CO₂ sequestration could depend on three
410 essential factors: the final equilibrium pressure, TOC, and the accessible porosity. TOC seems like
411 only affecting the gas storage capacity at relatively low pressure. However, other factors such as
412 geological fault, reservoir depth, and cap rocks quality will be considered for gas storage security
413 in the long term. Indeed, the gas injection rate will depend on intrinsic permeability and diffusion
414 in fractures and pores in complex shale.

415 4. Conclusions

416 This study provides an investigation of high-pressure gas storage mechanisms of three
417 shale samples using *in situ* SANS measurements with contrast-matching method. From basic
418 characterization, the Marcellus shale and Longmaxi shale samples are quartz-rich and the Illinois
419 shale sample has the highest TOC. The Marcellus shale and Longmaxi shale samples have higher
420 pore accessibility than the Illinois shale sample. However, the Illinois shale has the highest
421 cumulative porosity and surface area among the measured samples.

422 Based on the three-phase Porod invariant method, the average SLD in accessible pores of
423 the measured shale samples can be obtained. The results indicate a lower average adsorbed phase
424 density in accessible pores of shale than bulk phase density at the pressure between 100 bar and
425 the contrast-matched point (~600-700 bar). In contrast, the average adsorbed phase density could
426 be higher than bulk when the pressure is below 100 bar and above the contrast-matched pressure.
427 Hypothetically, the average adsorbed phase volume could first increase and then decrease with
428 increasing pressure till very high-pressure region. However, further study needs to be conducted
429 at low pressure and very high-pressure regions to confirm these mechanisms and more samples
430 also need to be considered.

431 In addition, gas storage capacities of the shales were estimated. The results are compared
432 with the previously measured gas adsorption capacities of the same shale samples. TOC has
433 positive correlation with both the gas adsorption capacity and storage capacity at low pressure.
434 Longmaxi shale with the highest pore accessibility has the highest gas storage capacity at high
435 pressure. Therefore, three essential factors, including the final injection pressure, TOC, and the
436 accessible porosity, could be used for searching and maximizing methane storage and long-term
437 CO₂ sequestration in depleted shale reservoir.

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578

579 **Author contributions**

580 SL and RZ designed the research; RZ and SL performed the research; RZ, LF, TB, and GS
581 conducted the measurements; RZ analyzed and interpreted the data; RZ drafted the manuscript;
582 All authors gave feedback and contributed to the writing of the manuscript.

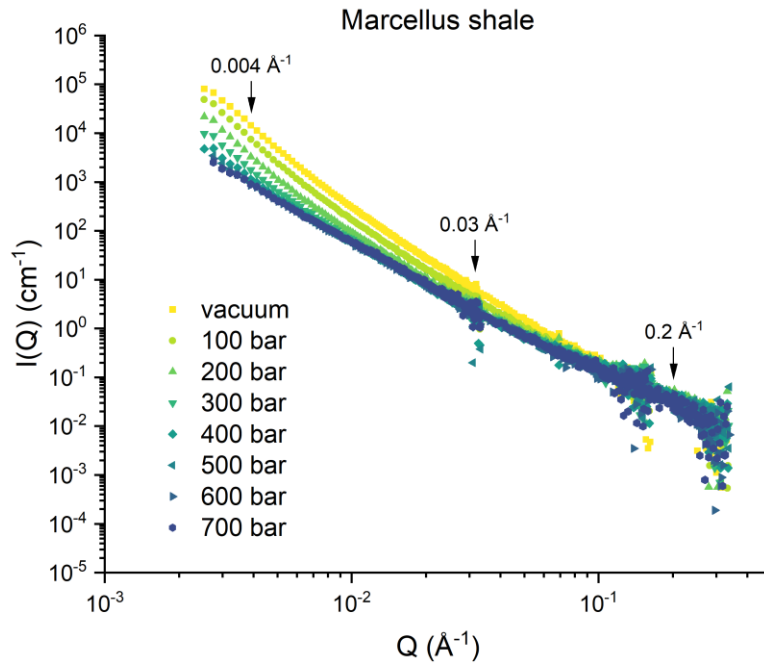
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594 **Competing interests**

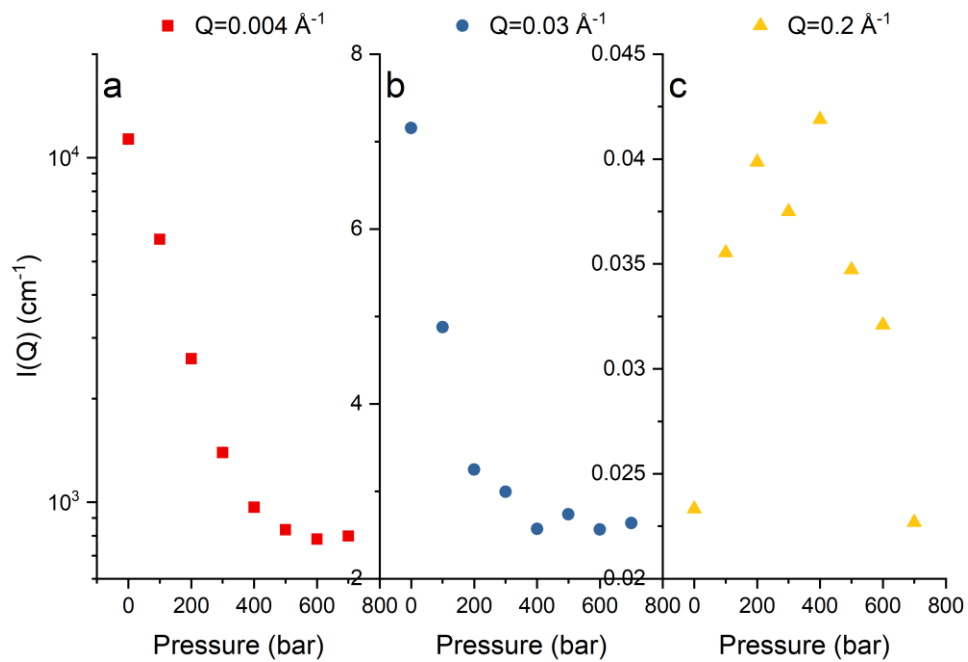
595 The authors declare no competing financial interests.

596 **Figures**



597

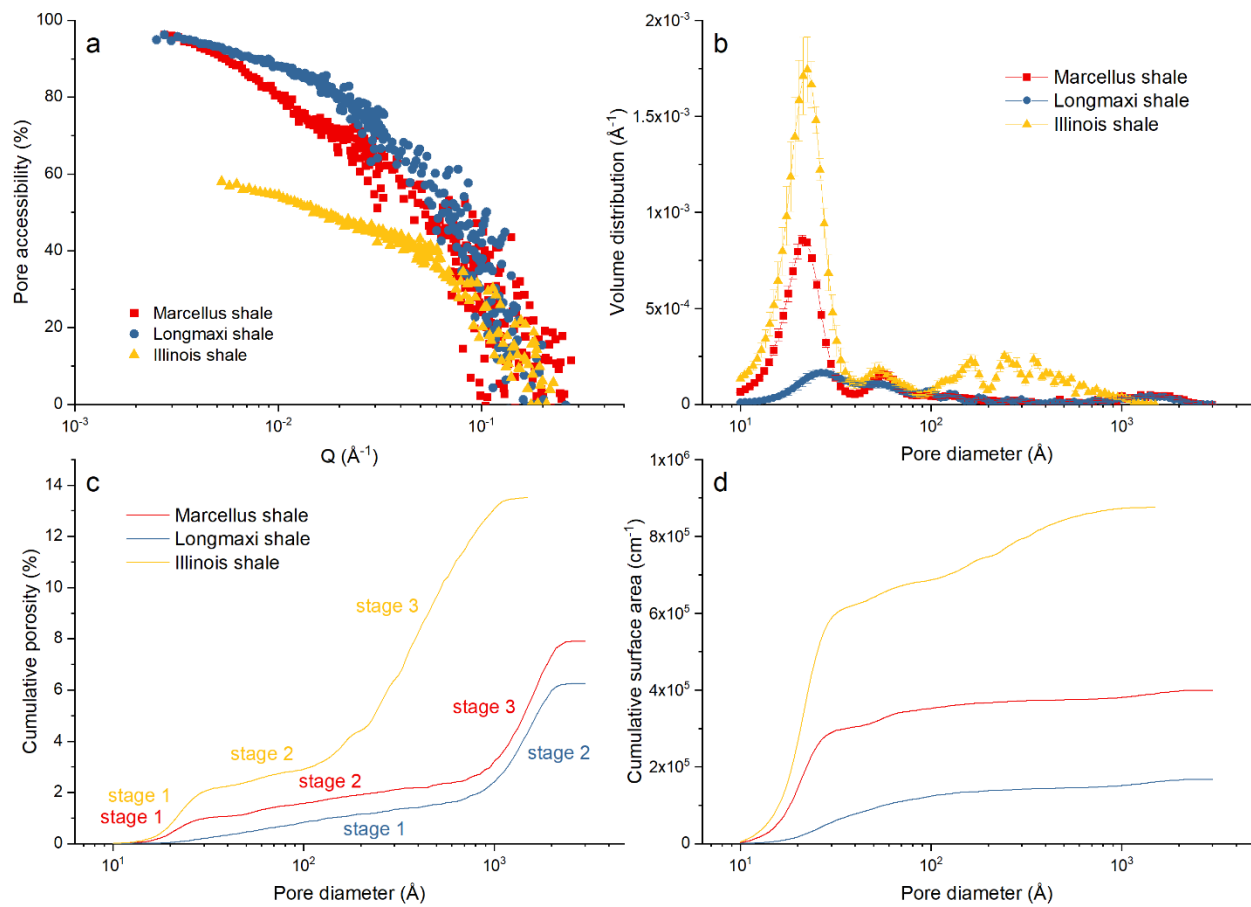
598 **Figure 1** Scattering intensity as a function of methane pressure for the Marcellus shale sample



599

600 **Figure 2** Scattering intensity as a function of methane pressure at (a) Q of 0.004 Å⁻¹, (b) Q of 0.03

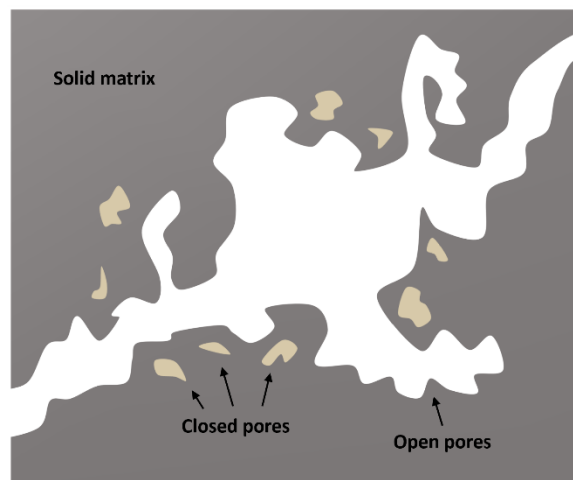
601 Å⁻¹, and (c) Q of 0.2 Å⁻¹ for the Marcellus shale sample



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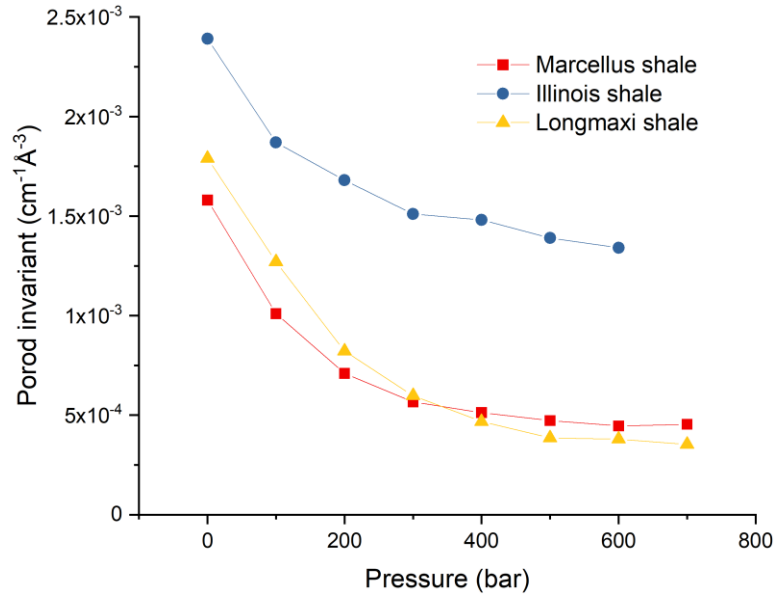
603 **Figure 3 (a)** Pore accessibility, **(b)** pore volume distribution, and cumulative **(c)** porosity and **(d)**

604 surface area of the three shale samples



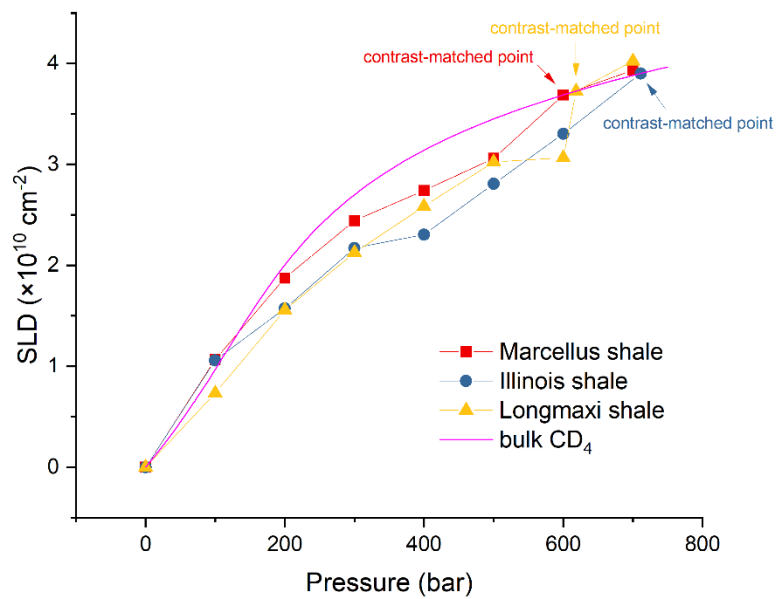
605

606 **Figure 4** A schematic of three-phase system in shale matrix



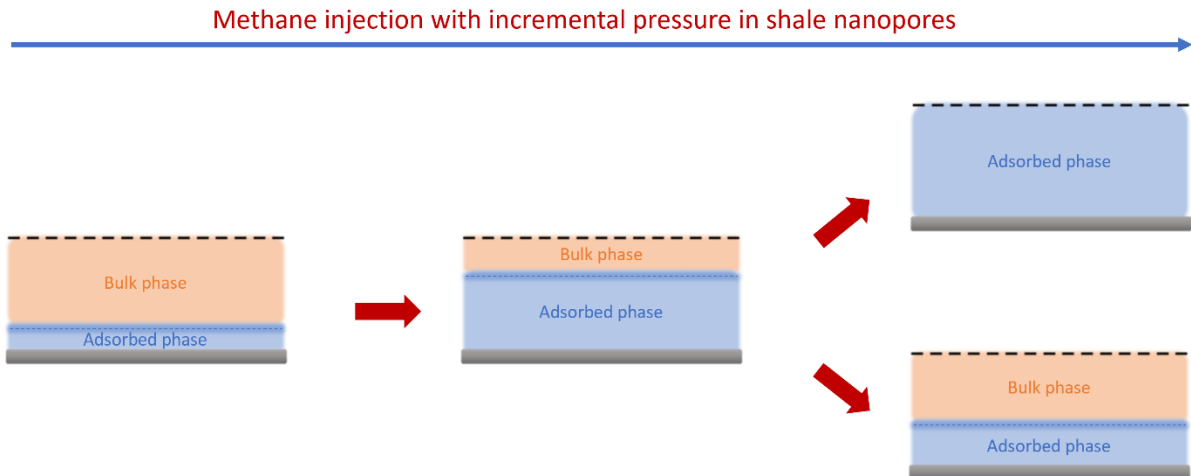
607

608 **Figure 5** Porod invariant as a function of pressure for the three shale samples

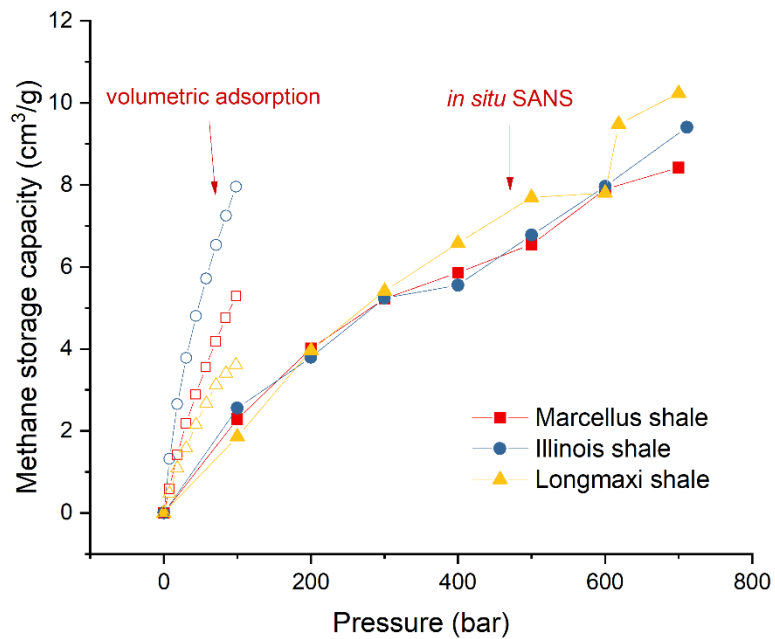


609

610 **Figure 6** Average SLD in open pores as a function of pressure for the three shale samples



611
 612 **Figure 7** Schematics of the hypothetical mechanism of methane sorption and compression as
 613 elevating pressure in idealized shale nanopores (The black dashed line is the centerline in pores;
 614 the gray area is the shale matrix)



615
 616 **Figure 8** Methane storage capacity in open pores as a function of pressure for the three shale
 617 samples