

1 **Processing outcomes of atomic force microscope tip-based**
2 **nanomilling with different trajectories on single-crystal silicon**

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12

13 **Abstract**

14 Atomic force microscope (AFM) tip-based nanomilling is an emerging
15 technology for machining nanostructures with a high rate of material removal and
16 slight tip wear. However, subsurface damage induced by nanomilling is poorly
17 understood. In this study, we investigated nanomilling-induced subsurface damage of
18 single-crystal silicon experimentally and with molecular dynamics simulations. We
19 studied the effect of clockwise and anticlockwise trajectories on the nanochannel
20 morphology. The clockwise trajectory resulted in a ‘U’-shaped nanochannel at a
21 relatively low normal load. Transmission electron microscopy and Raman
22 spectroscopy analysis of the nanochannel subsurface revealed atomic-scale defects,

1 including dislocations, stacking faults, and amorphous silicon. Molecular dynamics
2 simulations described the evolution of the phase transformation and subsurface
3 damage. This work reveals the mechanism of subsurface damage of single-crystal
4 silicon in nanomilling, which will facilitate the machining of nanostructures with
5 minimal subsurface damage.

6

7 **Keywords:** Atomic force microscope, nanomilling, single-crystal silicon, subsurface
8 damage, phase transformation

9 **1. Introduction**

10 Single-crystal silicon is one of the most important semiconductors in the
11 semiconductor industry, and is used in applications such as micro-electronics,
12 photovoltaic solar panels, micro-electro-mechanical systems (MEMS), and micro- and
13 nanofluidic fields [1-3]. Nanostructures, such as nanochannels, fabricated on single-
14 crystal silicon using mechanical machining are fundamental for such applications.
15 However, because of tool–workpiece contact in the machining process, subsurface
16 damage invariably occurs just beneath the workpiece surface [4,5], which affects the
17 mechanical, electronic, and optical performance of silicon devices. Another key
18 determinant of performance is the surface integrity of the machined nanostructure.
19 Thus, it is important to study the subsurface damage and surface integrity of
20 nanostructures fabricated by mechanical machining.

21 Ultra-precision machining approaches, including single-point diamond turning
22 (SPDT), polishing, and grinding, are commonly used to machine single-crystal silicon

1 in the ductile regime [6-9]. However, it is difficult to machine a nanostructure using
2 SPDT to below 100 nm because of the kinematic accuracy of the rigid machining
3 system. Machining systems for grinding and polishing are more flexible than those of
4 SPDT, making it easy to obtain a surface with higher surface integrity. However, there
5 are several drawbacks of these methods, including low machining efficiency,
6 unpredictable machined depth, and their inability to form single nanostructures (such
7 as nanochannels). Atomic force microscope (AFM) tip-based direct mechanical
8 nanoscratching is a powerful approach to machine nanostructures. This approach has
9 many merits, such as ease of use, low requirements for the processing environment,
10 and high machining flexibility [10-12]. The dimensions — especially the machined
11 depth of the nanostructures — can be predicted precisely by considering the
12 machining parameters and material properties of the specimen [13]. Furthermore, it is
13 easy to machine nanochannels with this machining system. Nevertheless, for the tip-
14 based single-scratch method, the channel shape can only be determined by the tip
15 geometry and the material removal rate needs to be improved.

16 The AFM tip-based nanomilling method was proposed to overcome the
17 aforementioned drawbacks of the single-scratch nanofabrication approach. The ratio
18 of the depth to width of the channel can be controlled by the driving voltage of the
19 piezoelectric actuator and the normal load. Moreover, the material removal rate at
20 large machined depths is much greater than that of the single-scratch method for the
21 same applied normal load [14]. The nanomilling approach has been used to fabricate
22 nanostructures on polymers, metals, and photoresists [15-17]. However, for brittle

1 materials, such as single-crystal silicon, mechanical machining inevitably induces
2 damage and microstructural change of the sample under the machined surface [18]. In
3 our previous study, we investigated the mechanism of nanomilling and subsurface
4 damage caused by a non-circular nanomilling trajectory [19]. However, the effect of
5 clockwise and anticlockwise nanomilling trajectories on the machining outcomes such
6 as the shape of the nanochannel and the formation process of chips were not studied.
7 Furthermore, the subsurface damage caused by a circular nanomilling trajectory was
8 not investigated. Thus, the aforementioned concerns should be further explored.
9 Molecular dynamics (MD) simulations are effective for studying the nanomachining
10 process, and can even reveal the dynamic evolution process of the generated atomic
11 defects [20]. Nevertheless, to our knowledge, MD simulations for nanomilling on
12 single-crystal silicon have been not reported.

13 The objective of the present study was to understand the effect of clockwise and
14 anticlockwise tip-based nanomilling on the subsurface damage and morphology of
15 nanochannels fabricated on single-crystal silicon. Furthermore, we compared the
16 material removal rate for machining using nanomilling and the single -scratch
17 method. Raman spectroscopy and TEM were used to study the subsurface structure of
18 the nanostructures machined using nanomilling with a circular trajectory. The
19 dynamic evolution of the subsurface damage and morphology were further studied
20 using MD simulations. The obtained results can be used to understand the
21 morphology of machined nanostructures and the subsurface damage mechanism
22 caused by nanomilling.

1 **2. Experimental details**

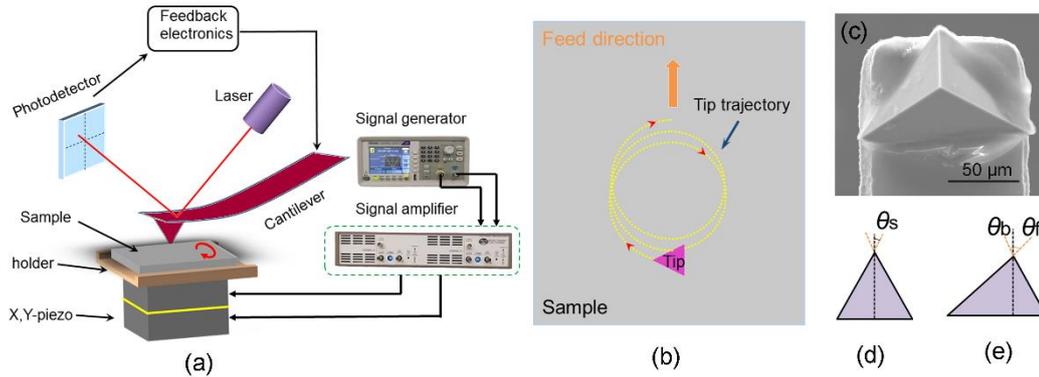
2 **2.1 AFM-based nanomilling set-up and methods**

3 As shown in Fig. 1(a), an AFM tip-based nanomilling set-up consisted of a
4 piezoelectric actuator (P-122.01, PI Company, Germany) and a commercial AFM
5 system (Dimension Icon, Bruker, Karlsruhe, Germany). The two-dimensional
6 piezoelectric actuator was driven by a sinusoidal signal and moved in the horizontal
7 plane. To obtain the driving sinusoid signals, a commercial signal generator
8 (AFG1022, Tektronix, USA) and signal amplifier (PZD350A, TREK, USA) were
9 used. The maximum travel ranges in both the x and y directions for the piezoelectric
10 actuator were 1 μm . The specimen was fixed on the piezoelectric actuator. A
11 revolving translational movement of the specimen could be obtained when the
12 piezoelectric actuator was driven by a sinusoid signal with 90° phase difference in x -
13 and y -directions. Thus, as illustrated in Fig. 1(b), the nanomilling process was
14 achieved with the aid of the relative movement between the tip and specimen. Figure
15 1(c) shows a scanning electron microscopy (SEM) image of the triangular pyramidal
16 diamond tip (PDNISP, Bruker, Germany) used in this study. The tip cantilever was
17 made of stainless steel with a normal spring constant (K_N) of 286 N/m provided by the
18 manufacturer. The front angle (θ_f), back angle (θ_b), and side angle (θ_s) of the tip, as
19 illustrated in Fig. 1(d) and (e), were 55° , 35° , and 51° , respectively. The specimen was
20 a single-side-polished single-crystal silicon (100) wafer, which was purchased from
21 Suzhou Research Semiconductor Co., Ltd., China. The surface root-mean-square
22 roughness of the specimen was measured to be about 0.1 nm by scanning a $1 \mu\text{m} \times$

1 1 μm area using the AFM. Five normal loads in the range of 60–180 μN with steps of
2 30 μN (Fig. 1(a)) were used to perform the machining process; the load was constant
3 during nanomilling. Furthermore, the driving voltage and frequency (f) of the
4 sinusoidal signals in both the x and y directions were 125 V and 500 Hz, respectively.
5 The driving amplitude (A) of the piezoelectric actuator was measured to be 370 nm.
6 Thus, the linear velocity of the tip can be obtained by $V=\pi fA$, which is calculated to be
7 580 $\mu\text{m/s}$. The feed direction of the tip was selected as side-forward and the
8 nanomilling process was along the in-plane Si $[\bar{1}\bar{1}0]$ orientation.

9 SEM (Quanta 200FEG, FEI, USA) and AFM (Dimension Icon, Bruker,
10 Karlsruhe, Germany) were used to investigate the morphologies of the nanochannels.
11 The obtained nanochannels were analyzed immediately using SEM and were then
12 ultrasonically cleaned in alcohol solution for approximately 10 minutes to remove the
13 generated chips. The AFM measurements were performed using a new silicon tip
14 (radius of 10 nm, TESPA, Bruker, Germany) in tapping mode. The phase structure of
15 the machined nanochannels and subsurface characteristics were investigated using a
16 commercial Renishaw Raman system (InVia-Reflex, Renishaw, UK) and TEM (FEI
17 Tecnai F20, USA), respectively. The laser wavelength of the Raman system was 633
18 nm and the power of the laser beam was 1.7 mW. A 100 \times objective lens was selected
19 such that the spot of the laser was approximately 0.8 μm . A focused-ion-beam (FIB,
20 FEI Helios NanolabG3 UC, USA) system was used to prepare the cross-sectional
21 TEM samples. The TEM samples were cut perpendicularly to the nanochannels. To
22 enable electron transmission, the samples were thinned to approximately 90 nm using

1 the FIB technique.



2

3 Fig. 1. (a) Schematic diagram of the tip-based nanomilling set-up. (b) Schematic diagram of

4 the nanomilling process. (c–e) SEM micrograph and schematic diagrams of the side and

5 views of the diamond AFM tip.

6 2.2 MD simulation model

7 A three-dimensional (3D) MD nanomilling model was constructed as shown in

8 Fig. 2. The model consisted of a rigid diamond tool and a single-crystal silicon

9 workpiece. The size of the crystal silicon workpiece was $59 \text{ nm} \times 37 \text{ nm} \times 28 \text{ nm}$, and

10 the crystal orientations for x , y , and z direction were $[110]$, $[\bar{1}\bar{1}0]$, and $[002]$,

11 respectively. The silicon atoms were categorized as either Newtonian or boundary

12 atoms. The boundary atoms were used to reduce the boundary effect and to maintain

13 the proper symmetry of the lattice. To reduce the effect of simulation scale, periodic

14 boundaries were applied in the x and y directions. Nanomilling was simulated on the

15 (100) surface along the $[\bar{1}\bar{1}0]$ direction of the single-crystal-silicon workpiece. The

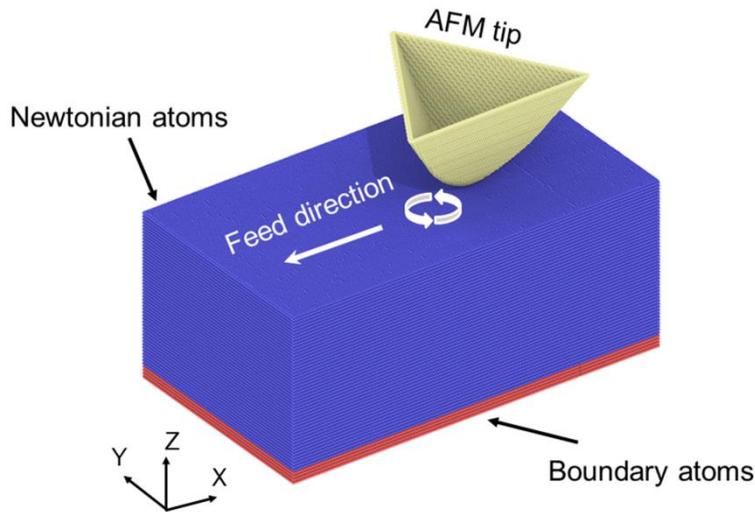
16 analytical bond order potential (ABOP), which is an appropriate potential for

17 simulating covalently bonding materials [21], was used to calculate the interatomic

18 forces between Si atoms. The interaction between tip-workpiece (C–Si) atoms was

19 expressed as the Morse potential [22]. The simulation model was equilibrated to 300

1 K under the canonical (NVT) ensemble in 50 ps, and the initial velocities of the
 2 workpiece atoms were assigned in accordance with the Maxwell–Boltzmann
 3 distribution. The tip was pressed into the workpiece under a normal load of 3.4 μN
 4 and moved with a feed rate of 80 m/s. Furthermore, for tip rotation, the maximum
 5 displacement in the x and y directions was 0.4 nm. The moving period was 10 ps. The
 6 other simulation parameters are listed in Table 1. The MD simulation was performed
 7 with the software Large-scale Atomic/Molecular Massively Parallel Simulator
 8 (LAMMPS) [23]. The software OVITO was used to visualize the simulation results
 9 [24].



10
 11 Fig. 2. Three-dimensional MD simulation model.

12 **Table 1 MD simulation parameters**

Parameters	Value
Workpiece size	58 nm \times 37 nm \times 28 nm
Atoms in workpiece	3035857
Atoms in Tool	106614
Feed velocity	80 m/s
Machining distance	26 nm
Tip rotation period	10 ps

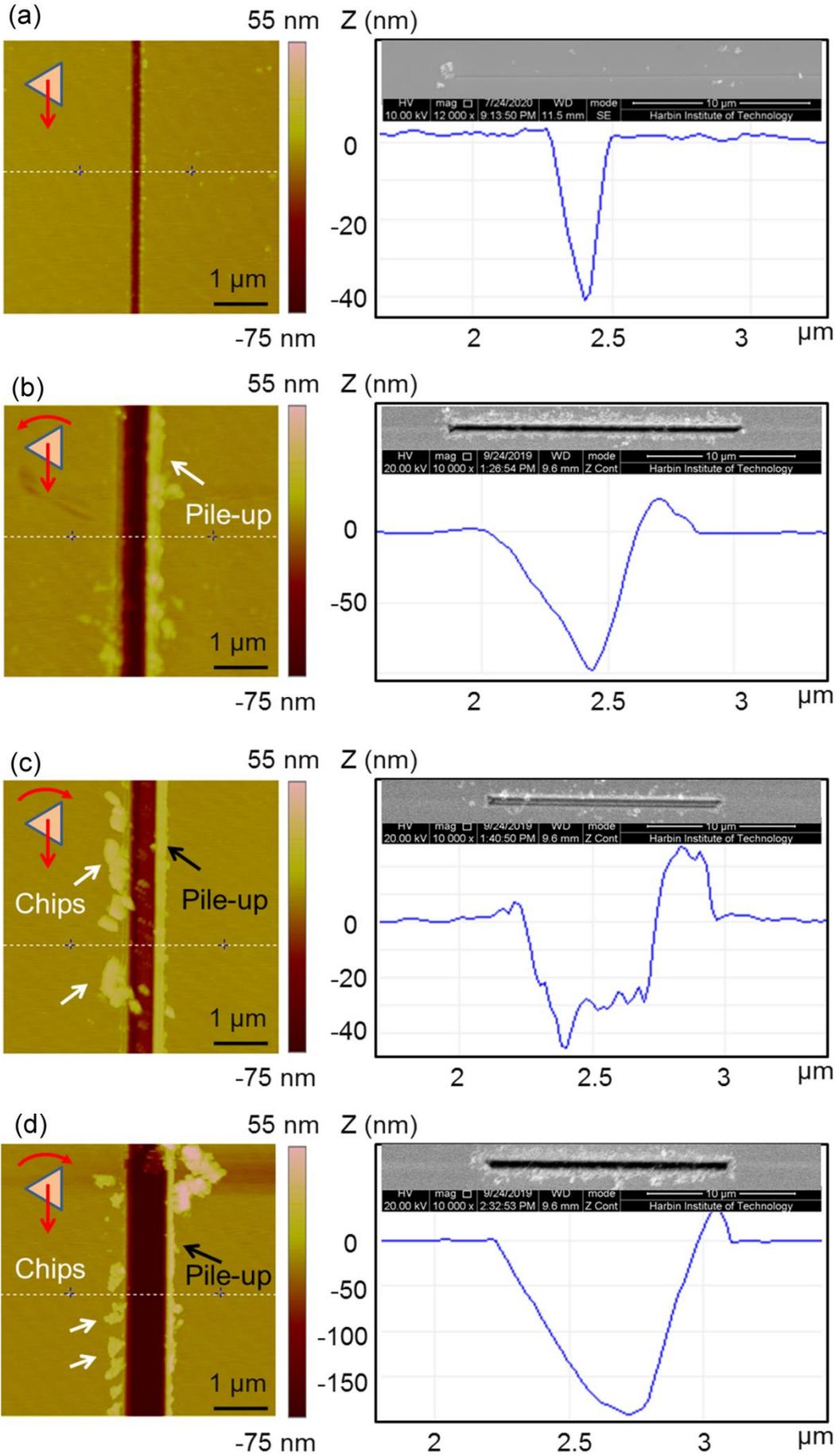
1 **3. Results and discussion**

2 **3.1 Nanochannel morphology**

3 The effect of different tip trajectories (i.e. single-scratch, anticlockwise, and
4 clockwise) on the nanochannel morphology was investigated using SEM and AFM.
5 Figure 3(a) shows the AFM image and corresponding cross-section of the
6 nanochannel fabricated using the single-scratch approach with a normal load of 180
7 μN . The inset is an SEM image of the nanochannel. In the AFM image, there are no
8 pile-ups on either side of the channel. The cross-section of the nanochannel displays a
9 'V' shape, which depends on the shape of the tip. In the SEM image, several small
10 chips can be observed.

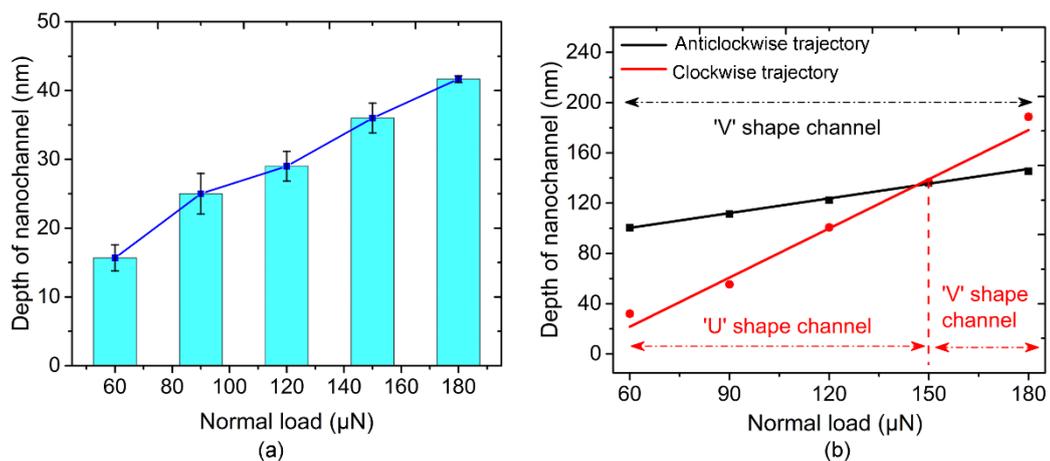
11 Figure 3(b) shows the AFM image of the nanochannel machined using an
12 anticlockwise trajectory with a normal load of 60 μN . The tip trajectory and feed
13 direction are marked in the AFM image. This image reveals the generation of pile-ups
14 during nanomilling, which were distributed on the left side of the tip feed direction.
15 Moreover, chips can also be found in the SEM image of the channel (inset in the right
16 panel). The cross-section corresponding to the nanochannel has a 'V' shape that is
17 much wider than that of the nanochannel machined with a single scratch. Figure 3(c)
18 and (d) show the AFM images of the nanochannels machined using a clockwise
19 trajectory with normal loads of 60 and 180 μN , respectively. In this case, the chips
20 were distributed on the right side and pile-ups were generated on the left side of the
21 tip feed direction. The inset SEM images also reveal the generation of pile-ups and
22 chips. The width of the 'V'-shaped cross-section of the nanochannel machined with a

1 normal load of 180 μN (Fig. 3(d)) was similar to that obtained with an anticlockwise
2 trajectory at the same load (Fig. 3(b)). By contrast, the cross-section of the
3 nanochannel fabricated with a normal load of 60 μN had a ‘U’ shape. From the
4 different cross-sections of the nanochannels, we estimate that the volume of material
5 removal for clockwise nanomilling was approximately 10 times greater than that for
6 the single-scratch approach for a normal load of 180 μN . Thus, our results show that
7 the rate of material removal is substantially improved using this nanomilling
8 approach.



1 Fig. 3. (a–d) Typical AFM images and corresponding cross-sections of the nanochannels
 2 fabricated with a single-scratch, an anticlockwise trajectory, a clockwise trajectory with a load of
 3 60 μN , and a clockwise trajectory with a load of 180 μN , respectively.

4 Figure. 4(a) illustrates the relationship between the machined depth and the
 5 applied normal load when machining using the single-scratch approach, which
 6 indicates the depth of the nanochannel is almost linearly proportional to the applied
 7 normal load. Figure 4(b) shows that the machined depth increased with increasing
 8 applied normal load for both the anticlockwise and clockwise trajectories. The
 9 machined depths were smaller with the clockwise trajectory than with the
 10 anticlockwise trajectory for normal loads lower than 150 μN . The morphology of the
 11 nanochannels fabricated using anticlockwise trajectory always had a ‘V’ shape.
 12 However, for nanochannels machined using the clockwise trajectory, there was a
 13 critical normal load that determined whether the channel had a ‘V’ or ‘U’ shape.
 14 These nanochannels were ‘U’-shaped for normal loads smaller than 150 μN and ‘V’-
 15 shaped for loads larger than 150 μN .



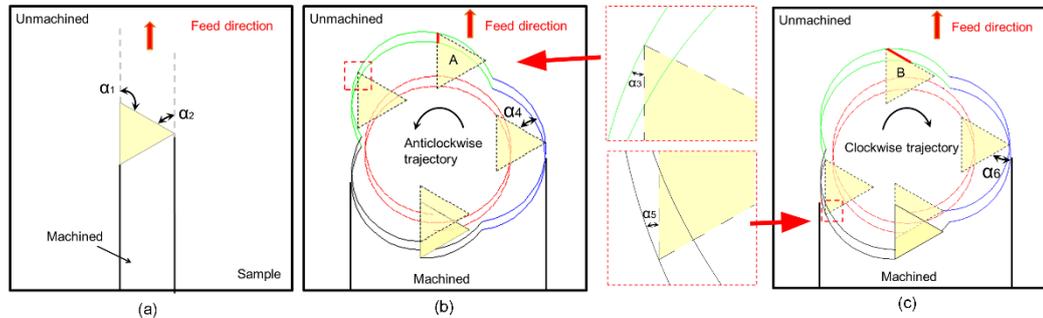
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 17 Fig. 4. Relationship between the nanochannel depth and the applied normal load. (a)

1 Fabrication with a single scratch. (b) Nanomilling with anticlockwise and clockwise trajectories.

2 Figure 5(a–c) shows schematic diagrams of the tip-edge trajectories when
3 fabricated with a single scratch, and with anticlockwise and clockwise trajectories,
4 respectively. Previous studies have demonstrated that the removal mechanisms of
5 materials are determined by the attack angle (α) between the tip and sample surface
6 [25,13]. Three removal mechanisms — plowing, wedge formation, and cutting —
7 have been proposed to increase the attack angle [26]. Cutting is considered to be the
8 dominant mechanism for material removal when the attack angle exceeds a critical
9 value, which is approximately 70° [25,13]. As shown in Fig. 5(a), the attack angles
10 for the left (α_1) and right (α_2) cutting edge were approximately 120° and 60° ,
11 respectively, which results in material being removed by cutting and chip formation.
12 Hence, there was almost no pile-up on either side of the channel (Fig. 3(a)).

13 For the nanomilling process, the channel morphology mainly depended on the
14 edge of the tip trajectory. Figure 5(b) illustrates the tip-edge trajectory in one
15 anticlockwise nanomilling period. The enlarged images are of the area marked in the
16 red dashed rectangle. The left attack angle (α_3) was far smaller than the critical value
17 for cutting ($\sim 70^\circ$). Thus, the materials were expelled by ploughing and accumulated
18 on the side of the machined nanochannel, resulting in pile-ups on the left side of the
19 tip feed direction (Fig. 3(b)). However, the right attack angle (α_4) was relatively close
20 to the critical value for the cutting mode. In this case, the materials were removed by
21 cutting and no pile-up can be found at the right side of the tip feed direction (Fig.
22 3(b)). The undeformed chip thickness during nanomilling reached the nanometer

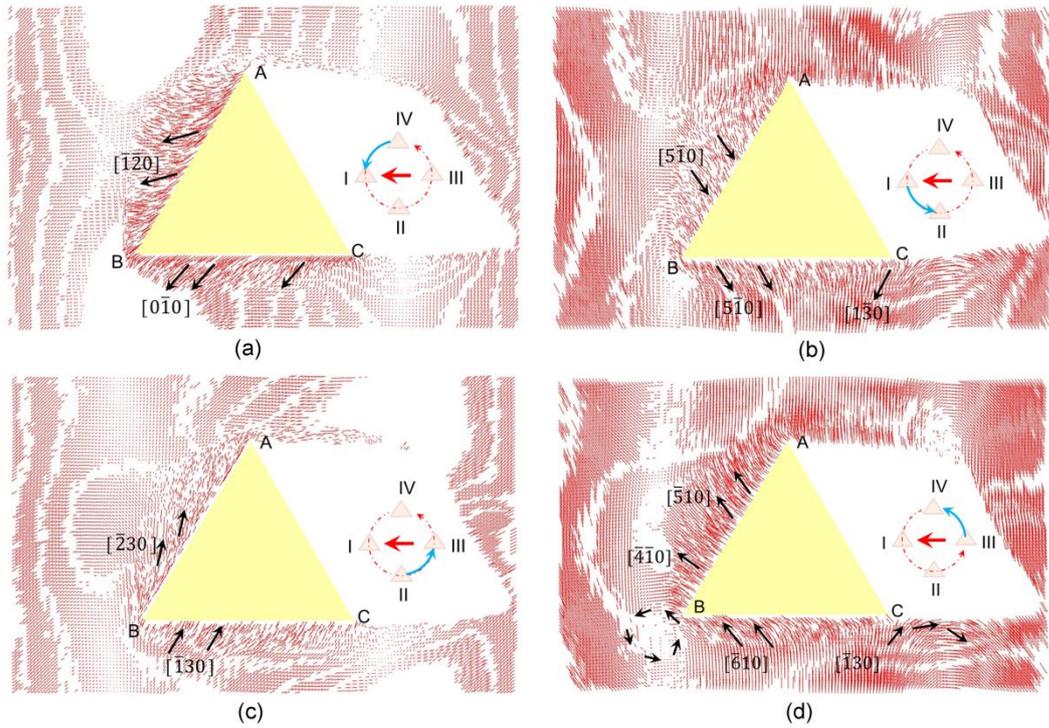
1 scale, which is comparable with the radius of the tip edge. According to the reports of
 2 Fang et al. [27,28], in contrast with conventional micro-cutting, material removal for
 3 nanoscale-cutting occurs by extrusion rather than by a shearing mechanism. Thus, in
 4 the cutting mode of the nanomilling process, materials were expelled by extrusion.
 5 The tip-edge trajectory in one clockwise nanomilling period is depicted in Fig. 5(c),
 6 where the enlarged schematic shows the region marked in red dashed rectangle. As
 7 was the case for anticlockwise nanomilling, pile-ups were generated on the left side of
 8 the tip feed direction (Fig. 3(c) and (d)) owing to the small attack angle (α_5).



9 (a) (b) (c)
 10 Fig. 5. (a–c) Schematic diagrams of the tip-edge trajectories when fabricated using a single
 11 scratch, and with anticlockwise and clockwise trajectories, respectively.

12 To better understand the material-removal process during nanomilling, the
 13 displacement vectors of the silicon atoms in a nanomilling period were revealed using
 14 MD simulations. Figure 6 shows snapshots of the atomic flow fields in the workpieces
 15 when the tip rotates in one period with the anticlockwise trajectory. As depicted in
 16 Fig. 6(a), the tip moves from position IV to I and the atomic flows mainly moves in
 17 the $[\bar{1}\bar{2}0]$ and $[0\bar{1}0]$ directions because of the material extrusion by the tip. When
 18 the tip moves from position I to II (Fig. 6(b)), the atoms adjacent to the edge ‘AB’
 19 move in the $[5\bar{1}0]$ direction because of the elastic recovery of the specimen. Atoms

1 near the edge ‘BC’ move in the $[\bar{5}10]$ and $[1\bar{3}0]$ directions, which contributes to the
 2 formation of pile-up on the left side of the tip feed direction. Figure 6(c) and (d)
 3 illustrate the atomic flows for the tip moving from position II to III and III to IV,
 4 respectively. In Fig. 6(c), the atoms move in the $[\bar{2}30]$ and $[\bar{1}30]$ directions. In Fig.
 5 6(d), the atoms are pushed forward in the $[\bar{5}10]$ and $[\bar{4}\bar{1}0]$ directions by the edge
 6 ‘AB’, which leads to chip formation. Furthermore, the atoms flowing in the $[\bar{6}10]$
 7 direction contribute to the generation of pile-ups.



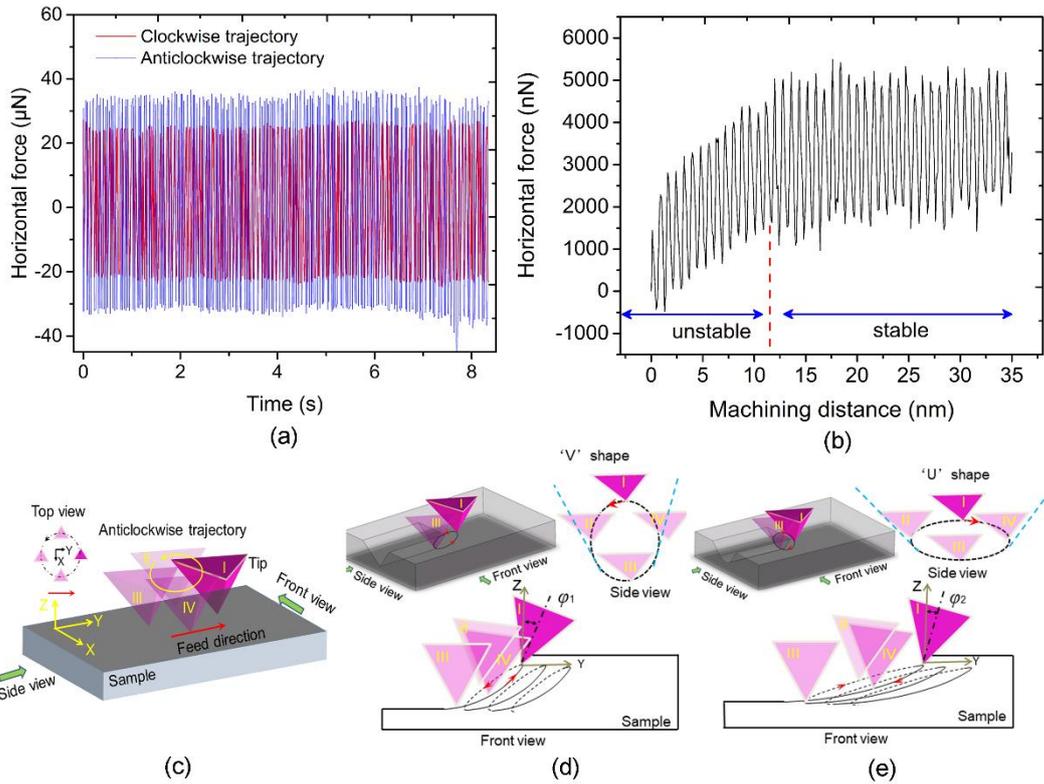
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 9 Fig. 6. (a–d) Snapshots of the atomic flow fields in the workpieces when tip moves from position
 10 IV to I, I to II, II to III, and III to IV, respectively.

11 The machined depth of the nanochannel is inversely proportional to the
 12 horizontal projection of the contact area between the tip and sample when the applied
 13 normal load is constant [29]. The red lines in Fig. 5(b) and (c) represent the contact
 14 area between the tip and sample when the tip is at positions A and B, respectively.
 15 The contact area for the clockwise trajectory is larger than for the anticlockwise

1 trajectory. Thus, depth of the nanochannel fabricated using a clockwise trajectory is
2 smaller than that machined by anticlockwise trajectory when the normal load is
3 smaller than $150\ \mu\text{N}$ (Fig. 4(b)).

4 Using the method proposed by Varenberg et al, the horizontal force in the
5 nanomilling process was calibrated and measured [30,31]. Figure 7(a) shows the
6 recorded experimental horizontal forces for anticlockwise and clockwise nanomilling
7 with a normal load of $180\ \mu\text{N}$. The horizontal force is smaller for clockwise
8 nanomilling than for anticlockwise nanomilling. Figure 7(b) illustrates the horizontal
9 force obtained from MD simulations for machining with an anticlockwise trajectory.
10 The force becomes stable after machining for a distance of approximately $11.5\ \text{nm}$.
11 The tip torsion during machining is proportional to the horizontal force [30]. A large
12 tip torsion due to a large horizontal force enlarges the contact area between the tip and
13 sample. Hence, for a normal load of $180\ \mu\text{N}$, the nanochannel depth was greater under
14 clockwise than anticlockwise milling. A schematic diagram of the nanomilling
15 process is shown in Fig. 7(c). Because the applied normal load is constant in
16 nanomilling, the tip can scratch the specimen at all times. The real tip trajectory for
17 anticlockwise nanomilling is depicted as Fig. 7(d), which is an inclined ellipse in
18 space. As shown in the side view of Fig. 7(d), the inclined ellipse trajectory
19 contributes to the 'V' shape of nanochannels fabricated using the anticlockwise
20 trajectory. For nanomilling with a clockwise trajectory (Fig. 7(e)), the real tip
21 trajectory is closer to a circle than to an inclined ellipse owing to the shallower
22 machined depth at applied normal loads smaller than $150\ \mu\text{N}$. The machined

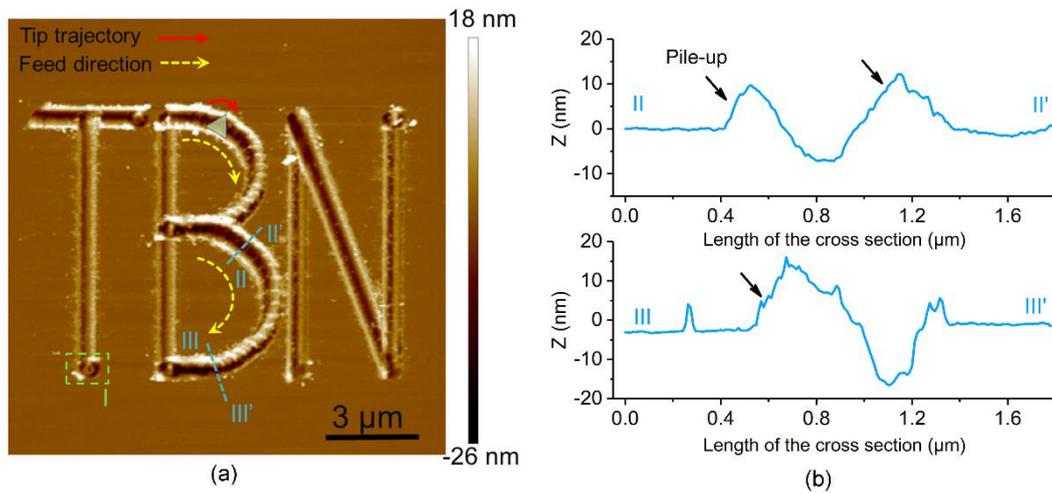
1 nanochannels display a ‘U’ shape in this case. However, when the normal load
 2 exceeds 150 μN , because of the large machined depth, the real tip trajectory
 3 approaches an inclined ellipse trajectory similar to that for anticlockwise nanomilling.
 4 Hence, a ‘V’-shaped nanochannel is obtained.



5
 6 Fig. 7. (a) Experimental horizontal forces recorded for anticlockwise and clockwise
 7 trajectories with a normal load of 180 μN . (b) MD-simulated horizontal force for the anticlockwise
 8 trajectory. (c–e) Schematic diagrams of the nanomilling process, and the anticlockwise and
 9 clockwise nanomilling trajectories, respectively.

10 To further reveal the influence of the trajectory shape on the processing outcomes,
 11 as shown in Fig. 8(a), the acronym of ‘tib-based nanomilling’, which includes curved
 12 trajectories, was fabricated using clockwise nanomilling. A circle (indicated by I in
 13 Fig. 8(a)) machined by the circle trajectory can be observed. Fig. 8(b) shows the

1 cross-sections corresponding to the curved channels in Fig. 8(a). It is obvious that the
 2 curved channels demonstrate a ‘U’ shape, which is constant with the result of the
 3 aforementioned clockwise nanomilling. Furthermore, from the cross-section II-II’,
 4 one can see that the pile-ups almost distribute uniformly on both sides of the channel.
 5 However, the pile-ups mainly distribute on the left side of the channel for the cross-
 6 section III-III’. The variation of the feed direction during nanomilling the curved
 7 channel contributes to the variation of the pile-ups.

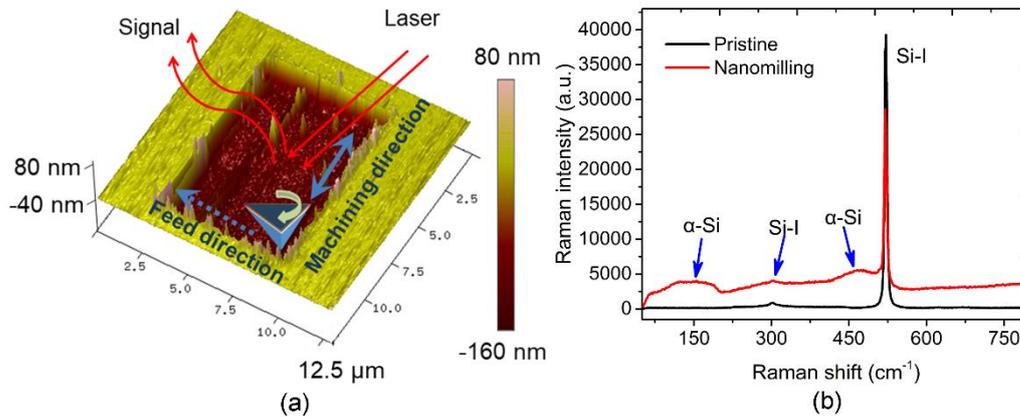


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 9 Fig. 8. (a) AFM image of TBN fabricated using nanomilling approach. The ‘TBN’ is the
 10 acronym of tib-based nanomilling. (b) Cross-section of the channels that marked in (a).

11 3.2 Phase transformation

12 Mechanical machining induces a series of phase transformations in single-crystal
 13 silicon because the hydrostatic pressure exceeds the pressure limit [32,33].
 14 Specifically, a new phase, labeled Si-II, forms under the tip. This phase transforms
 15 from Si-I and is not stable at ambient pressure [33, 34]. The Si-II phase further
 16 transforms during unloading depending on the pressure release rate, transforming into
 17 α -Si at high unloading rates, and into Si-III and Si-XII at low unloading rates [35]. We

1 performed Raman spectroscopy on a rectangular area ($10\ \mu\text{m} \times 7\ \mu\text{m}$) with a depth of
 2 120 nm that was machined using nanomilling. The Raman spectrum from the
 3 nanomilling region indicated in Fig. 9(a) is shown in Fig. 9(b); a spectrum for a
 4 pristine sample is provided for comparison. Three characteristic peaks (150 , 470 , and
 5 $521\ \text{cm}^{-1}$) of the nanomilling spectrum can be observed. We identify the sharp peak at
 6 $521\ \text{cm}^{-1}$ as the Si-I phase, and the two broadband peaks at 150 and $470\ \text{cm}^{-1}$ as the α -
 7 Si phase [36]. Thus, the α -Si phase is induced under the high unloading rate of the
 8 nanomilling process.



9
 10 Fig. 9. (a) Annotated AFM image illustrating the process of Raman detection. (b) Raman
 11 spectra acquired from the nanomilling region and of a pristine sample.

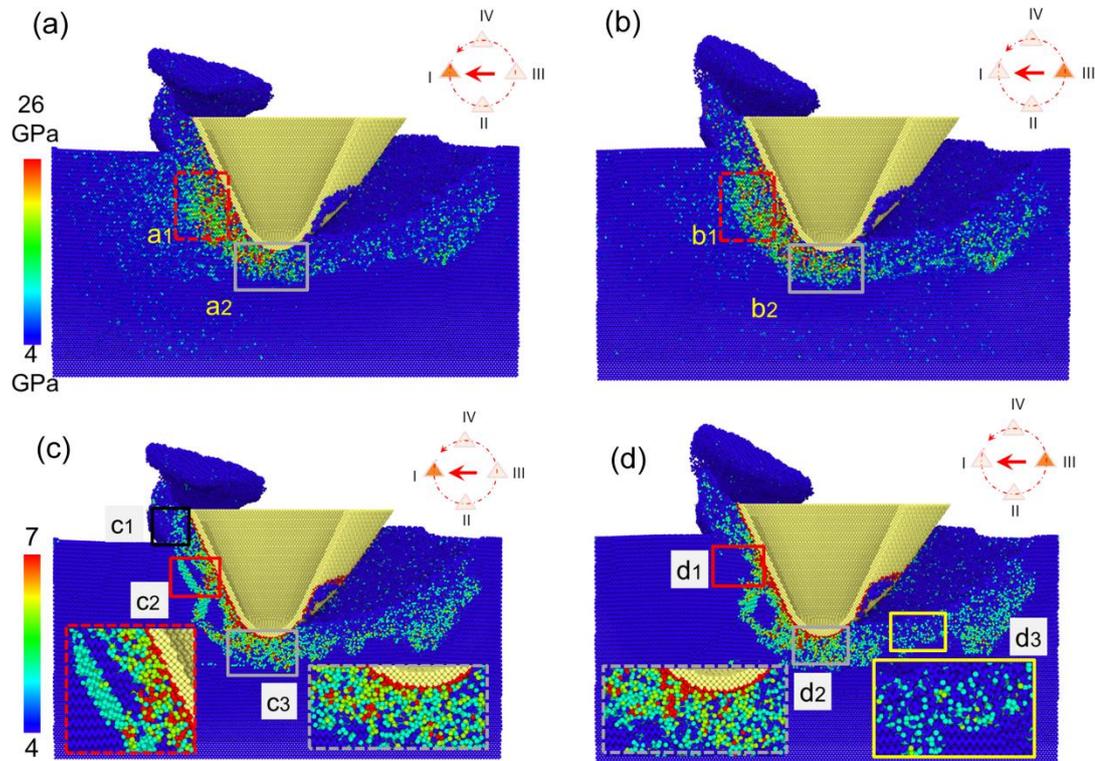
12 We carried out MD simulations to further investigate the phase transformation of
 13 the single-crystal silicon during nanomilling. The evolution of the crystalline phases is
 14 consistent with the distribution of the hydrostatic stress [37,38]. The hydrostatic stress
 15 can be calculated using a method proposed by Goel et al. [39]. Figure 10(a) and (b)
 16 show the hydrostatic stress distributions when machining at positions I and III. High-
 17 pressure zones can be observed in front of the tip (areas a_1 and b_1) and beneath the tip
 18 (areas a_2 and b_2). The sample undergoes a phase transformation from Si-I to Si-II

1 under high pressure, which contributes to plastic deformation in these zones. The tip
2 extrudes the sample material more severely at position I than position II, which leads
3 to a larger hydrostatic stress zone in area a_1 . The coordination numbers (n) in the
4 workpiece were used to identify the different phases forms, such as the diamond
5 crystal phase, bct-silicon, and β -silicon.

6 Figure 10(c) and (d) show the cross-sections of the phase transformation of the
7 single silicon atoms corresponding to the hydrostatic stress distributions shown in Fig.
8 10(a) and (b). The pile-up indicated by the black rectangle (area c_1) in Fig. 10(c)
9 includes bct-silicon ($n = 5$). Furthermore, the regions in front of the tip (area c_2) and
10 under the tip (area c_3), which are indicated by the red and gray rectangles,
11 respectively, are composed of amorphous silicon atoms mixed with bct-silicon ($n = 5$),
12 β -silicon ($n = 6$), and metastable atoms ($n = 7$). When the tip moves back to position
13 III, as illustrated in Fig. 10(d), the number of bct-silicon atoms in the pile-ups and the
14 tip - sample contact area (area d_1) become smaller than at position I because of the
15 unloading process. However, there are more metastable atoms in the region under the
16 tip (area d_2) than in area c_3 , as shown in Fig. 10(c).

17 Based on these simulation results, the phase transformation during nanomilling
18 can be described as follows. At position I, owing to the effect of tip extrusion, the
19 atoms in the contact area between the tip and sample (area c_2) transform from
20 diamond cubic four-coordinated α -silicon to bct-silicon, β -silicon, and metastable
21 atoms. The pile-up is generated by the extrusion and is mainly composed of bct-
22 silicon. The diamond cubic four-coordinated α -silicon atoms under the tip (area c_3)

1 also transform to bct-silicon, β -silicon, and metastable atoms, which induces
 2 subsurface damage. As the tip passes and moves to position III, the stress of the
 3 silicon atoms in front of the tip is released and the number of bct-silicon atoms
 4 decreases. However, more metastable atoms ($n = 7$) are generated by the pressing of
 5 the tip in area c_2 , which further contributes to the subsurface damage. The final
 6 subsurface of the nanochannel is shown in the enlarged image of area d_3 in Fig. 10(d),
 7 which includes bct-silicon ($n = 5$) and several β -silicon atoms.

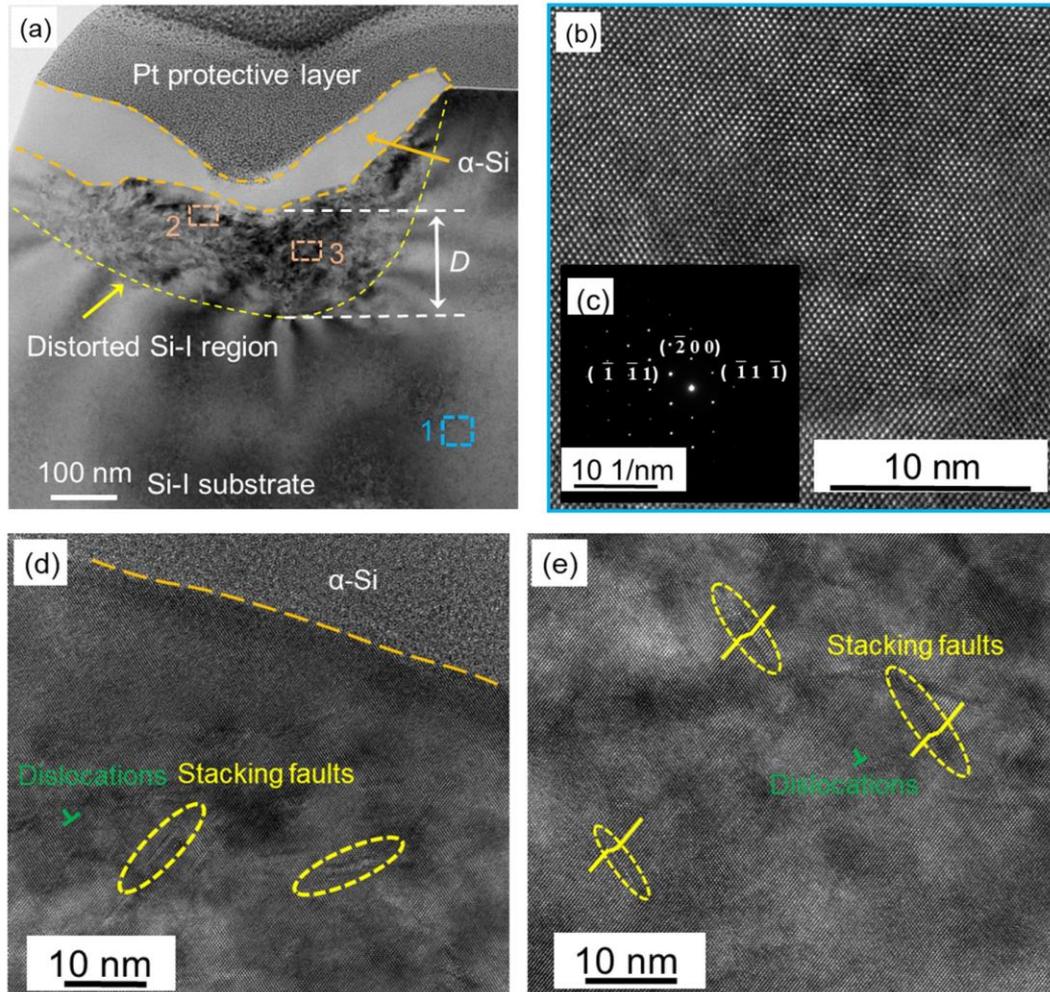


8
 9 Fig. 10. (a,b) Stress distributions at points I and III, respectively, of the nanochannel. (c,d)
 10 Phase transformation at points I and III, respectively, of the nanochannel simulated via MD.

11 3.3 Subsurface damage

12 The subsurface of the nanochannel fabricated with a circular trajectory was
 13 investigated using TEM. As shown in Fig. 11(a), a protective Pt layer was deposited
 14 on the nanochannel surface during the preparation of the TEM sample to avoid the

1 subsurface damage caused by the FIB. A grey layer beneath the Pt protective layer can
2 be observed in Fig. 11(a), which was identify as α -Si [36,40]. This observation agrees
3 with the Raman results. The maximum depth (D) of the distorted Si-I region is
4 approximately 150 nm. The enlarged image (Fig. 11(b)) of the region 1 marked in Fig.
5 11(a) shows that there are no atomic defects in the area far from the distorted region.
6 Furthermore, the diffraction pattern (Fig. 11(c)) corresponding to the area is indicative
7 of a single crystal structure [41]. Thus, these results indicate the pristine sample
8 material is a single crystal without defects before machining. High-resolution TEM
9 (HRTEM) was used to better understand the subsurface damage of the nanochannel. A
10 region adjacent to the α -Si layer (indicated as 2 in Fig. 11(a)) was selected. As shown
11 in Fig. 11(d), it is evident that dislocations and stacking faults were induced in the
12 adjacent area between the α -Si layer and the distorted Si-I region. Figure 11(e)
13 demonstrates the HRTEM image of region 3 in Fig. 11(a). Dislocations and stacking
14 faults also can be observed. These atomic-scale defects are generated by the high
15 pressure and shear stress during nanomilling [42]. Wu et al conducted nanoscratching
16 on monocrystalline silicon using a diamond tip and only α -Si, dislocations, and
17 stacking faults were observed in the subsurface [43], which indicates the subsurface
18 damages are almost identical for nanoscratching and nanomilling.

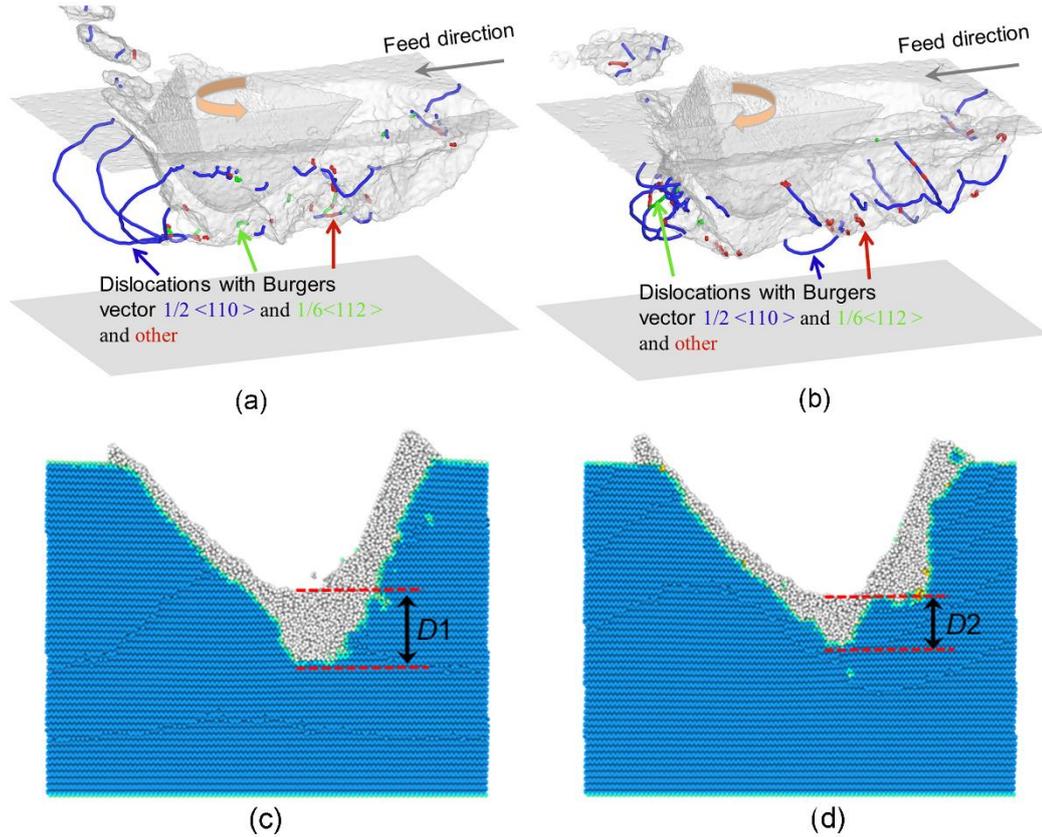


1

2 Fig. 11. (a) TEM image of the subsurface of the cross-section for a nanochannel machined by
 3 nanomilling with circular trajectory. (b,c) HRTEM image and diffraction of the region 1 marked in
 4 (a), respectively. (d,e) HRTEM images of the regions 2 and 3 that marked in (a), respectively.

5 We summarized the dislocation networks generated by anticlockwise and
 6 clockwise nanomilling trajectories using dislocation analysis based on MD
 7 simulations. As shown in Figs. 12(a) and (b), dislocations and their Burgers vectors
 8 were identified using the dislocation extraction algorithm, where the Burgers vectors
 9 $1/2 [110]$, $1/6 [112]$, and unidentified dislocations are colored blue, green, and red,
 10 respectively. For anticlockwise nanomilling (Fig. 12(a)), the dislocation loops with
 11 Burgers vector $1/2 [110]$ were distributed in front of the tip because of the extrusion

1 of the tip. For clockwise nanomilling (Fig. 12(b)), dislocations with Burgers vector
2 $1/2[110]$ also formed in front of the tip. However, the length of these dislocations
3 was much smaller than that generated in anticlockwise nanomilling. Furthermore,
4 more dislocations were generated on the right side of the nanochannel. The full length
5 of the induced dislocations for anticlockwise and clockwise nanomilling were 263 nm
6 and 204 nm, respectively, which indicates anticlockwise nanomilling contributing to
7 longer dislocations compared with clockwise nanomilling. Figs. 12(c) and (d)
8 illustrate the cross-section views of the nanochannel at the machining distance of 26
9 nm when nanomilling with an anticlockwise and a clockwise trajectory, respectively.
10 It is observable that the depth of the subsurface damage (D_1) induced by
11 anticlockwise nanomilling is much deeper than that induced by clockwise nanomilling
12 (D_2). The MD simulation reveals the tip trajectory has a strong influence on the
13 plastic deformation of the material. Furthermore, clockwise nanomilling could
14 facilitate a shallower subsurface damage compared with anticlockwise nanomilling.



1

2 Fig. 12. Distribution of the dislocations obtained by MD simulations in single-crystal silicon
 3 for nanomilling with (a) an anticlockwise and (b) a clockwise trajectory. (c,d) The cross-section
 4 view of the nanochannel at the machining distance of 26 nm when nanomilling with an
 5 anticlockwise and a clockwise trajectory, respectively.

6 4. Conclusions

7 Using an AFM tip-based nanomilling set-up, nanochannels were fabricated on
 8 single-crystal silicon with a single scratch, and with anticlockwise and clockwise
 9 nanomilling trajectories. The morphology of the obtained nanochannels, phase
 10 transformations, and subsurface characteristics were investigated. The main findings
 11 are summarized as follows:

- 12 (1) Experimental observation and analysis of the atomic flow fields using MD
 13 simulations revealed that the channel shape depends on the tip trajectory and applied

1 normal load. For an anticlockwise nanomilling trajectory, the nanochannel had a ‘V’
2 shape at all loads. However, for normal loads smaller than 150 μN , the nanochannel
3 fabricated using a clockwise nanomilling trajectory had a ‘U’ shape, which is caused
4 by the real trajectory that is closer to a circle than to an inclined ellipse. The volume
5 of material removed by nanomilling was about 10 times larger than that machined by
6 a single scratch.

7 (2) The atomic structure of the fabricated nanostructures was investigated by
8 Raman spectroscopy, which demonstrated that the α -Si phase was generated because
9 of the high unloading rate. The dynamic evolution of phase transformation was
10 revealed by MD simulations, which showed that the final subsurface of the
11 nanochannel included β -silicon and β -silicon atoms.

12 (3) TEM observations showed that many atomic-scale defects, such as
13 dislocations and stacking faults, were induced in the subsurface of the nanochannels.
14 MD simulations revealed that the length of the dislocations with Burgers vector
15 $1/2 [110]$ was smaller for clockwise than anticlockwise nanomilling. In addition,
16 more dislocations were generated on the right side of the channel for clockwise
17 nanomilling.

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