

# A Cost-Function Driven Adaptive Welding Framework for Multi-Pass Robotic Welding

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## Abstract

Manual teaching of robot paths and welding parameters for multi-pass robotic welding is a cumbersome and time-consuming task, which decreases the flexibility, adaptability, and potential of such systems. This paper introduces and presents a new automated weld parameter and pass deposition sequencing framework, which builds on the current state of the art developments and enables automatic planning of multi-pass welding for single-sided V-groove geometries. By integrating a novel cost-function concept that permutes and identifies the welding parameters for each layer through a user-driven weighting, the framework delivers the minimum number of passes, filler material and welding arc time based on application requirements. A mathematical model relating the cross-section area of beads with the pose of the torch and weaving width was built upon to allow full-process automated welding parameter generation and adaption for different geometric characteristics of the groove. The concept methodology and framework were then developed and verified experimentally, through robotically deployed Metal Active Gas (MAG) welding. For a given representative joint, the arc welding time and amount of filler wire were found to be 32.9% and 26.18% lower respectively, than the worst-case available welding parameter combination, delivering a corresponding decrease in direct automated welding manufacturing costs. Lastly, an ultrasonic inspection was undertaken to verify the consistent quality of the weldments validating the framework outcome and enabling welding pass automation through robotic systems.

31 **Keywords:** Robotic Arc Welding, Multi-pass, Weld Sequence Planning, V-groove, MAG

## 32 **1. Introduction**

33 The need to automate processes in manufacturing lies in the desire for high productivity,  
34 reduction of production costs and increase of profits through reduced labour cost [1]. Fusion  
35 welding is the process of joining two materials together, typically employing heat through  
36 solidification with or without the use of filler consumable material. Over the past decades,  
37 welding has made a considerable impact in different sectors of our world including, aviation,  
38 automotive, defence and marine through the fabrication of tanks, frigates and submarines [2].

### 39 **1.1. Arc Welding Technology and Joint Designs**

40 Among the different types of welding, arc welding has evolved for over 100 years [3]. The  
41 different types of arc welding can be categorized based on the electrode method used, which is  
42 consumable or non-consumable [4]. Among the most common techniques, Gas Metal Arc  
43 Welding (GMAW) widely known as Metal Inert Gas (MIG) and Metal Active Gas (MAG)  
44 utilize a consumable filler wire. The distinction originates from the shielding gas that is  
45 employed, and this technique is suitable for both thin and thick sections resulting in high  
46 deposition rates and increased productivity [3–5]. The power source of these welders can be  
47 synergically controlled for a given wire material and diameter and in absolute wire feed speed  
48 or current mode, depending on which parameter the welder will control. A different variety of  
49 metals can be welded, which range from carbon steels, low alloy steels, stainless steels,  
50 aluminium alloys, copper, and nickel alloys.

51 In welded structures, loads are distributed between the welds of the joints. The type of joint  
52 geometry is determined through the geometric requirements of the assembly and the type of  
53 loading [4]. As can be seen in Figure 1 [6], the basic joint designs are summarized as butt,  
54 corner, edge, lap and tee joints. The selection of the joint type also aligns with the requirement  
55 for the least amount of deposited weld metal to meet the strength requirements for load  
56 distribution [4]. For thick butt joints, the edges are mechanically prepared (machined, water-  
57 jet cutting etc.) to a particular geometry to provide adequate access for the weld torch and  
58 achieve even heat input flow and penetration between filler and parent metal [3,4]. These  
59 mechanically prepared geometries, which are shown in Figure 2 [4], can be single sided or  
60 double sided for example with double V's, and single or double U's.

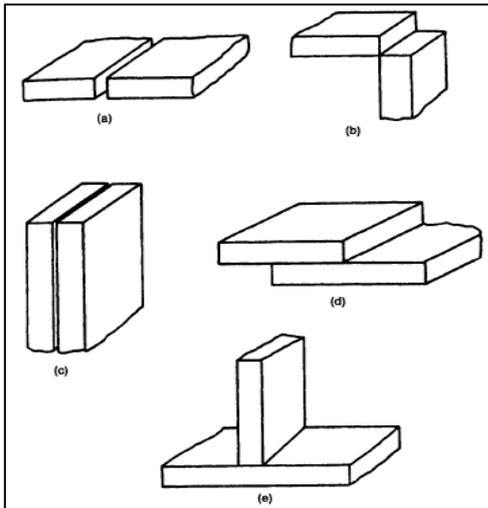


Figure 1. Five basic types of weld joint geometries. (a) butt joint, (b) corner joint, (c) edge joint, (d) lap joint and (e) tee joint

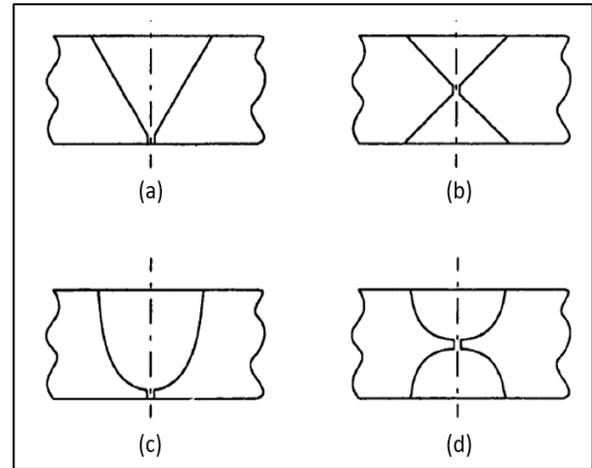


Figure 2. Butt joint geometries processed for welding. (a) single sided -V, (b) double -V, (c) single-U, (d) double-U

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62 **1.2. Multi-Pass Welding Notation**

63 In the maritime, oil and offshore industries, the thickness of the single or double V-groove  
 64 joints requires more than a single pass, usually manually or semi-autonomously deposited,  
 65 resulting in low efficiency and productivity [7]. Although manual welding allows selecting  
 66 different welding parameters per layer or even per pass if that is required, this depends on the  
 67 experience of the welder and the limits and window of the approved Welding Procedure  
 68 Specification (WPS) produced from a weld procedure qualification record.

69 Figure 3 describes the terminology of multi-pass welding for a single sided V-groove open root  
 70 gap assembly. The root pass refers to the initial welding pass used to join parent metals  
 71 together, where a non-metallic backing strip can be used to support the root surface [3]. The  
 72 hot pass is the second welding pass used to reshape the root pass, achieve sidewall fusion and  
 73 fill any inconsistencies caused by improper penetration of the root pass [8]. Filler passes serve  
 74 the remaining weld groove area until the cap passes are deposited to reinforce the weld groove

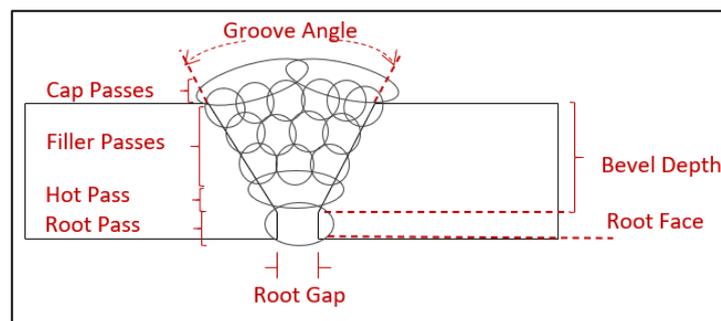


Figure 3. V-Groove joint characteristics and passes notation

75 and provide a clean finish to the top weld face. Welding passes deposited at the same height  
76 offset relative to the root face belong to the same layer. The vertical root face is used for to  
77 achieve proper fusion with the root sides.

### 78 ***1.3. Welding Environment and Challenges***

79 Despite the massive utilisation of welding technology in manufacturing, the welding  
80 environment still imposes difficulties for the welders. During welding, high concentrations of  
81 fumes, gases, dust, infra-red and ultra-violet radiation are produced along with substances, such  
82 as nickel and chromium, which have an adverse effect in the human respiratory system and can  
83 lead to lung cancer and asthma [9].

84 Lack of space during welding can amplify the exposure to toxic fumes and increase the ambient  
85 temperature. Those unpleasant conditions can be met in enclosed spaces, as it happens in the  
86 pre-fabrication of double hull structures [10]. Nonetheless, during the maintenance of such  
87 structures, there is limited space for work. Fixed infrastructure that cannot be moved and other  
88 manufacturing processes taking place in parallel also increases the possibilities for injuries  
89 while working in a confined area.

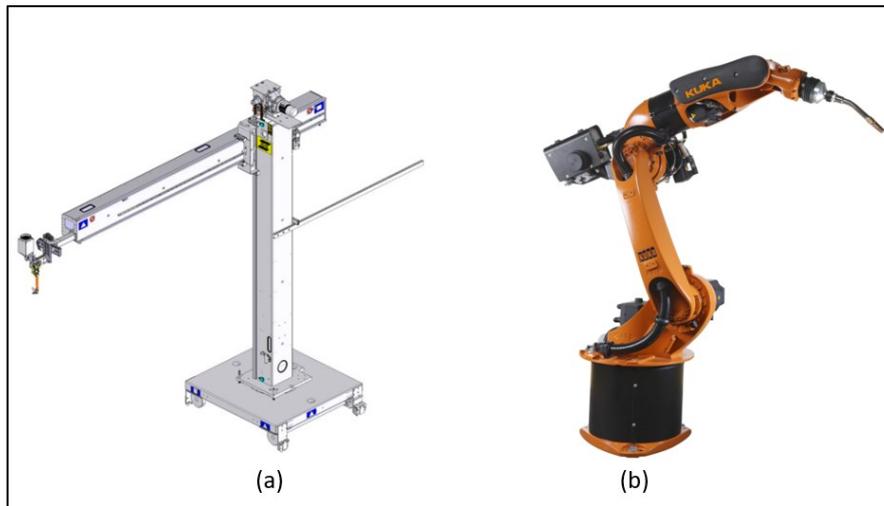
### 90 ***1.4. Welding Automation***

91 A complex dynamic process such as welding, which is challenging to parameterize and to  
92 control [11–14], must meet the demand for high production rates, precision, and consistent  
93 quality. However, labour turnover due to harsh environmental conditions further increase the  
94 shortage of skilled welders to fulfil the needs of manufacturing in the 21<sup>st</sup> century [15],  
95 affecting production and consistency of quality. Consequently, the life span of future assets can  
96 be reduced, and the amount of rework increased [16]. Automating welding can alleviate issues  
97 of repeatability, quality, and increased production demand. The bulk production of repeatable  
98 welds in multi-pass welding of known joint geometries can be delivered through robotic  
99 welding systems. Therefore, freeing welders to be utilized in more complex and creative tasks  
100 where a high degree of customisation is required.

101 When considering automated welding deployment, based on the Degrees of Freedom (DoF)  
102 that the welding systems exhibit, these can be commonly classified into either rectilinear  
103 (Figure 4(a)-[17]) or articulated robotic solutions (Figure 4(b)-[18]) [19]. Rectilinear robots  
104 (gantry systems) can demonstrate a constrained boxed working envelope, moving multiple axes  
105 to allow flexibility and volume coverage. Alternatively, articulated robots mimic human arms

106 with six DoF, utilizing revolving wrists connected through joints and controlled by motors to  
107 cover the working volume with flexibility and speed.

108 These articulated robotic manipulators exploit interest for specific automation applications, due  
109 to their capabilities and multiple DoFs, increased pose repeatability and duty cycles. However,  
110 the realisation of fully automated robotic arc welding systems is not yet achieved, as the  
111 welding procedure, operating environment, welding joint geometry and preparation can vary  
112 significantly [20].



**Figure 4. Welding robotic systems classified based on the degrees of freedom  
(a) Rectilinear robotic system and (b) Articulated robotic arm**

### 113 **1.5. Automated Robotic Welding**

114 Considering this progress, and the conditions of common industrial welding environments, the  
115 call for flexible automated arc welding can be realized through decisional autonomy [21]. A  
116 closed-loop robotic system can alter the trajectory of the motion based on sensory feedback  
117 information (camera, laser scanner, touch-sensing). In that way, it can sense the local  
118 environment and superposes pre-programmed moves adapting to changes encountered in the  
119 environment.

120 The realization of a fully automated robotic welding system demands the development of a  
121 welding framework which combines sensor-driven robotic motion along with multi-pass  
122 sequence planning for the weld joint geometry. Sequence planning of multi-pass welding is  
123 imperative for automation of welding in the shipbuilding and offshore sector due to the  
124 requirement of the thickness of the joints. Moreover, this welding process is repetitive and  
125 monotonous, while manual welders can be utilized in more complex tasks.

126 This paper presents a new welding framework that enables automatic planning of the complete  
127 multi-pass welding sequence with different welding parameters per layer. Moreover, this  
128 approach adapts to varying single sided V-groove geometries, without human intervention,  
129 populating the number of layers and passes to minimise a desired cost function. These  
130 developments are demonstrated alongside a flexible 6-DoF sensor-driven robotic welding  
131 system. The rest of this paper is organised as follows. Section 2 introduces a multi-pass welding  
132 sequence review for V-groove joint configurations. Section 3 presents the welding framework  
133 and the developed algorithms for automated multi-pass weld planning based on the  
134 minimization of a cost function. Section 4 demonstrates the experimental setup, utilizing  
135 different butt joint geometries for a proof-of-concept validation along with inspection of the  
136 completed joints. The subsequent proof-of-concept demonstration characterization results are  
137 discussed in Section 5. Section 6 discusses future work with Section 7 concluding the paper.

## 138 **2. Automated Multi-Pass Welding**

### 139 ***2.1. The Current State-of-The-Art in Multi-Pass Sequence Planning***

140 Mathematically describing and approximating the shape geometry of the deposited welding  
141 beads requires developing algorithms to generate the sequence of welding parameters and as a  
142 result, the robotic motion path. In the relevant works, welding beads are represented as  
143 parallelograms and trapeziums since often the cross-section shapes of weld beads match these  
144 shapes visually. Using the same welding parameters for all the deposited weld beads, the  
145 authors in [7,22,23] simplified the welding sequence generation. Adopting the same welding  
146 parameters for every welding pass, for all the layers, the method of equal height was used in  
147 [7,22]. The method assumed that every layer had the same height, which could be argued as  
148 partially true since the width of the groove increases between the bottom and the top surface  
149 of the specimen. Similarly, in [23], the welding sequence schedule was generated utilizing the  
150 same welding bead for all the filling layers. This assumption was held since the cross-section  
151 area of the weld bead remains constant under the same welding parameters, resulting in the  
152 equal area method.

153 The number of passes per layer can be minimised by selecting different welding parameters for  
154 every layer, and the groove can be filled faster than using the same weld bead for each weld  
155 pass. In [24], authors related the cross-section area of the weld bead with the value of the wire  
156 feed speed, robot speed and diameter of the wire. Depending on where the weld bead was  
157 deposited in the groove it was approximated as a trapezium or a parallelogram. This method

158 prompted the user to enter the desired welding parameters per layer and number of passes, and  
 159 outputted the robot pose trajectory and position of weld bead in the groove to aid automation,  
 160 while mimicking manual welding approaches. The approximation of weld beads as a parabola  
 161 is discussed in [25]. The welding schedule algorithm assumed that the width of every weld pass  
 162 in the same layer remains constant and the bead selected maximizes the occupied cross-section  
 163 area to result in the minimum number of passes. However, no action is taken on the maximum  
 164 allowed height of every new welding layer, where the user decides as the groove is filled with  
 165 passes. This call for user action makes the multi-pass welding sequence planning a semi-  
 166 automatic procedure. In all the relevant works [7,22–25], the user input is required at multiple  
 167 stages. In the proposed approach documented herein, the user is asked only once to assign  
 168 welding parameters. Then they will not be prompted to make decisions, as welding parameters  
 169 can adapt for varying butt joint configurations. Table 1 depicts the current advancements on  
 170 the state-of-the-art in multi-pass sequence planning along with their limitations.

171 **Table 1. Relevant works in multi-pass weld sequence planning and limitations**

Relevant works	Different welding parameters per layer	Adapting different welding parameters to varying V-groove geometries	Cap passes planning	Post-Trial Inspection Verification
C.D. Yang et al.[7]	✗	✗	✗	✗
C. Yang et al. [22]	✗	✗	✗	✗
T.-Y.Huang et al.[23]	✗	✗	✓	✓
H. Zhang [24]	✓*	✓*	✗	✗
S.J. Yan et al.[25]	✓**	✓**	✗	✗
<b>This Body of work</b>	✓	✓	✓	✓

172 \* The user prompts to enter the welding parameters per layer. In that way, it can select different welding parameters for  
 173 different V-groove geometries.

174 \*\*Welding parameters are provided from a bank of parameters where the user decides for the initial number of passes and  
 175 layer height. The chosen dimensions of the bead must satisfy the stored configurations in the database

### 176 2.1.1. Research Gap and Opportunity

177 The research gap based on prior literature, indicated the lack of an automated technique to  
 178 identify the combination of the welding parameters per layer and the number of welding layers  
 179 to fill the V-groove geometries without user intervention. Zhang et al. in [24] prompted the  
 180 user to decide for the welding parameters per layer, while in [7,22,23] the same welding bead  
 181 was deployed in every pass of each layer, which is not always efficient in terms of welding  
 182 time and heat input required. The maximum height and width of the planned passes were not

183 discussed, and as a result, the chosen weld passes could have an irregular cross-section area  
184 relative to the size of the whole groove. Two common points of the above approaches was the  
185 use of backing to deposit the root pass, and the fact that the hot pass was treated as a regular  
186 filling pass when more heat is required than the first pass to fill any inconsistencies caused by  
187 improper penetration of the root pass [8]. Moreover, cap planning and inspection for defects  
188 were only performed in [23] where the micrograph analysis revealed a lack of sidewall fusion.

189 Building and adapting on the work reported in [24] the following advancements and work  
190 packages are developed in this body of work, where Figure 5 summarizes and illustrates the  
191 developed contribution of the automated multi-pass weld sequence framework:

- 192 • The opportunity from the research gap is realized by developing an algorithm to  
193 automate the sequence path planning with different welding parameters per layer and  
194 identifying the number of passes per layer and number of layers irrespective of the butt  
195 joint geometric characteristics.
- 196 • A logic is integrated to allow the adaption of the sequence of welding parameters for  
197 varying single sided V-groove geometries (groove angle, gap size, bevel height)  
198 enabling the automated robotic weld path planning. This advancement can eliminate  
199 additional time to re-program, from scratch, the robot motion when the joint geometry  
200 changes due to design or operational requirements.
- 201 • Additional work is performed to formalize the need for cap planning in the final  
202 welding layer for varying V-groove geometries.
- 203 • The optimized solution of the sequence of welding parameters per layer is shaped  
204 further by introducing the dynamic concept of the cost function. This delivers the  
205 combination of welding parameters that will produce the minimum number of passes  
206 in the minimum arc welding time, with the minimum spent filler material while taking  
207 care of the restrictions on allowed height and weaving width of the weld bead. The size

208 of the bead can increase the residual stress between weld passes, leading to cracks and  
209 increased distortion of the weldment [26,27].

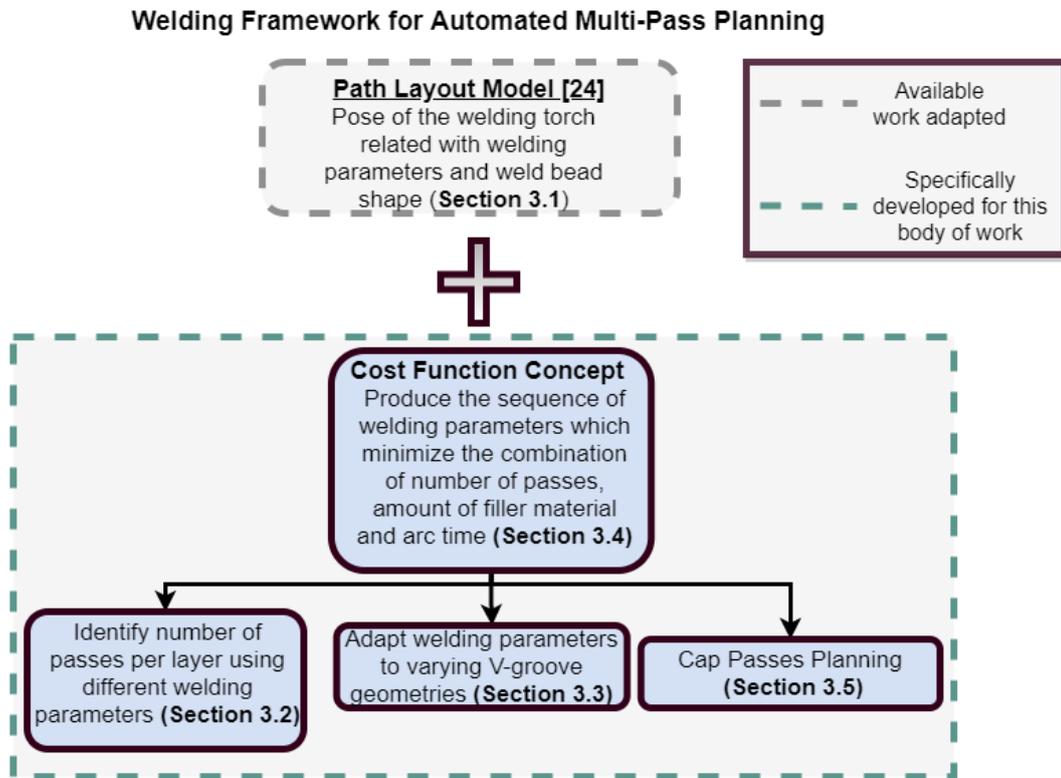


Figure 5. Highlighted is the available adapted and newly developed work for this paper with direct reference to their corresponding section in the paper

210

### 211 3. Proposed Automated Welding Framework

212 A mathematical model, relating the cross-section area of beads with the welding parameters,  
213 pose of the torch and weaving width, was adopted from [24] and built upon to allow full-  
214 process automated welding parameter generation, optimization and robotic path planning. The  
215 flowchart in Figure 6 describes each step of the welding framework as well as the required user  
216 input. The following sections explains in detail the implementation of the different steps along  
217 with the notation used in the diagram.

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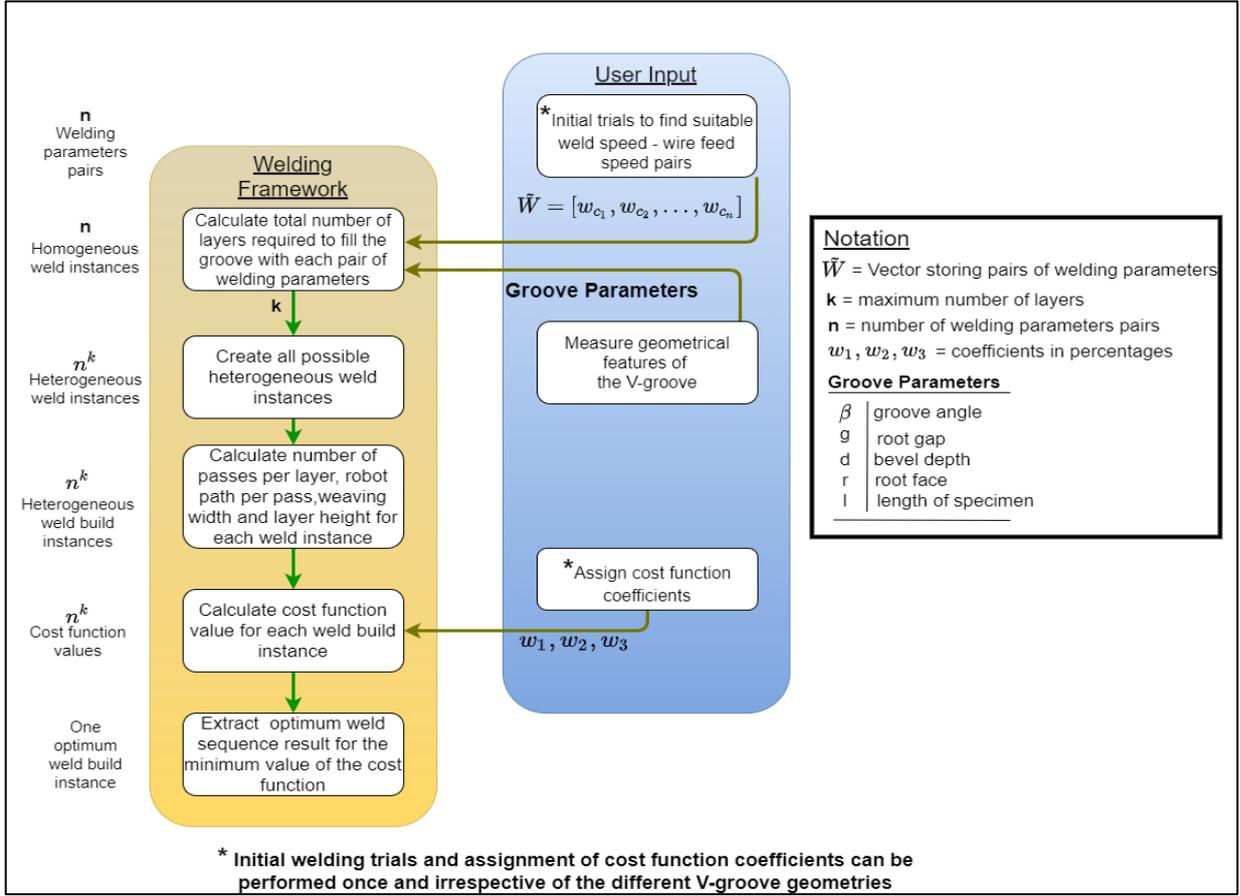


Figure 6. Flowchart presenting the welding framework process and the required user input

222

223 **3.1. Cross-section Area and Efficiency Coefficient**

224 An integral part of the welding framework is the prediction and approximation of the cross-  
 225 section area of a deposited weld bead based on the welding parameters. The cross-section area  
 226 defined with variable  $S$  ( $\text{mm}^2$ ) is represented by a trapezium or parallelogram shape depending  
 227 on where it is deposited within the groove [24] and is given by Eq:3:1

$$S = \frac{\pi \cdot u \cdot D^2}{2 \cdot v} \quad \text{Eq:3:1}$$

228 where  $u$  = wire feed speed ( $\text{mm}/s$ ),  $D$  = diameter of the wire (mm) and  $v$  = robot welding  
 229 speed ( $\text{mm}/s$ ). Every pair of robot and wire feed speed is provided as a welding configuration  
 230 vector,  $w_c = [v, u]$ . To reflect the material loss during welding, due to the efficiency of the  
 231 filler wire, spatter and heat transfer, the coefficient  $a_H$  was introduced, to give Eq:3:2 based on  
 232 [7,22]. The coefficient  $a_H$  was determined through experiments and subsequent welding trials.

$$S = \frac{a_H \cdot \pi \cdot u \cdot D^2}{4 \cdot v} \quad \text{Eq:3:2}$$

### 234 3.2. Assess the Number of Layers and Passes

235 The automatic generation of the number of layers and passes required was obtained by building  
 236 on [24] where the user was prompted to provide the total number of layers and passes. The root  
 237 and hot pass were not part of this routine, as they each constitute one welding pass. The number  
 238 of welding passes for every new layer is now automatically calculated based on the parameters  
 239 shown in Table 2, and driven by restrictions on the maximum weaving width and the range of  
 240 allowed height of every weld bead on the layer. This is core of the developed algorithm,  
 241 highlighted in the flowchart of Figure 7 with the green dotted lines.

242 **Table 2. Inputs of the algorithm that produce the number of passes per layer**

Parameter	Description
$w_c$	Generated vector of welding parameters (see Sec. 3.1 above)
$S$	Array of values of cross-section areas of already deposited weld beads
$m_i$	Number of already deposited passes per layer
$i$	Current layer number
$a_H$	Deposition coefficient (see Sec. 4.2)
$\delta$	Weaving factor used to restrict weaving width (see Sec. 4.2)
$\beta$	Groove angle of V-groove
$g$	Root gap length
$D$	Diameter of filler wire

243

244 The range of accepted height and maximum weaving width of a weld pass are not defined  
 245 explicitly in welding standards but is guided mainly from the requirements of the application  
 246 and is recorded as part of the WPS. However, the narrower and taller the bead is, the more  
 247 challenging it is to perform subsequent weld passes and to achieve proper fusion with the sides  
 248 of the weld bead. On the other hand, weld beads with a smaller height lead to more passes to  
 249 fill the remaining groove, which is not efficient in terms of manufacturing time.

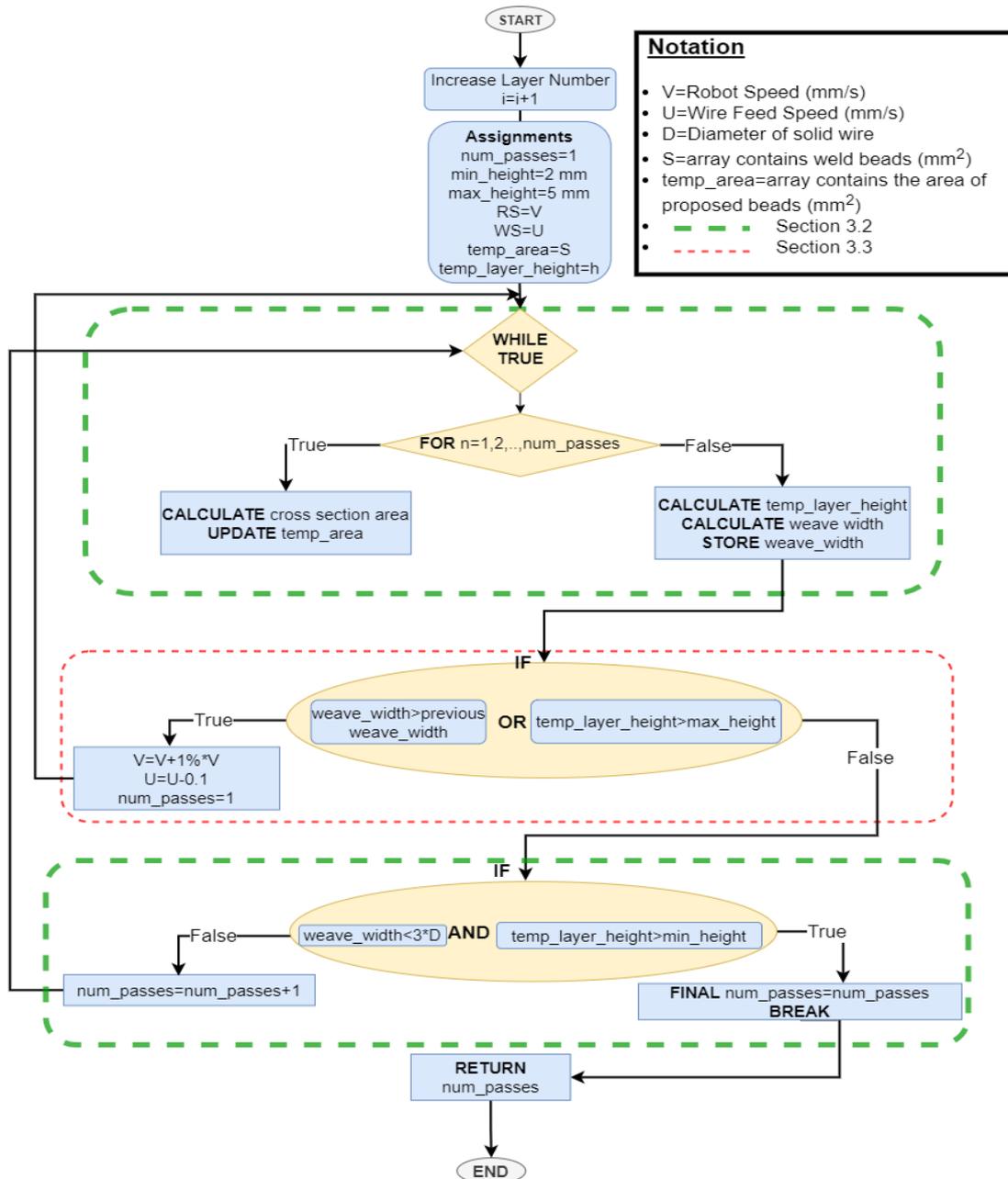


Figure 7. Process flowchart of the developed algorithm. The algorithm also adjusts the welding parameters based on the imposed restrictions of bead height and weave width

250 Preliminary experimental trials deployed with the robotic setup presented in Section 4 showed  
 251 that the acceptable range of height of each layer could be between 2 mm and 5 mm. Moreover,  
 252 the maximum weaving width was limited to three times the diameter of the welding wire ( $3 \cdot$   
 253  $D$ ) used. Excessive weave width increases heat input towards inline cracking and the chance  
 254 for lack of fusion with the sidewalls.

### 255 3.3. Adapting Welding Parameters to Varying V-groove Geometries

256 Lastly, the process marked with red dotted lines in Figure 7, assists in generating the number  
 257 of passes per layer for varying groove geometries, irrespective of the characteristics of the butt

258 joint (bevel angle, height, root gap). As operator input is not required for each layer, to  
259 guarantee that the restrictions on height and weave width are satisfied, a logic is encapsulated  
260 to adapt the given welding parameters.

261 Investigating the variation on the geometric characteristics on the V-groove joint, there is a  
262 possibility that the cross-section areas of the produced welding beads based on the given  
263 welding parameters will never satisfy the restrictions on height and weave width of the welding  
264 beads. These variations which were validated from experimental procedures consist of a groove  
265 angle further of  $95^\circ$ , root gap length more than 2 mm and the total height of 15 mm.

266 Violating the restrictions, stems from the rise of the width groove from bottom to top and in  
267 which height previous deposited layers were within the groove. More particularly equations  
268 from [24] were used to calculate the height of the layer and required weaving width of passes.  
269 Both depend on the previous layers' height and covered area from already deposited weld  
270 beads. For every new layer, the algorithm initially picks a welding parameters pair and assigns  
271 one pass which will have large weaving width and very small height to occupy the whole layer.  
272 In the next iteration a new pass will be added, so the weaving width will decrease and because  
273 more passes stack together the height of the layer will increase. But in some circumstances, by  
274 adding more passes in that layer may never satisfy the restrictions as the initial cross section  
275 area of the pass was too big and the height of the layer will keep increasing. To counteract this  
276 action and always satisfy the imposed size limits the cross-section area formed from the  
277 existing welding parameters must decrease. Hence, once there is a violation, the provided  
278 welding configurations are adjusted in every iteration, by 1% of the robot speed and 0.1 m/min  
279 the wire feed speed. These incremental proportional changes (1%, 0.1 m/min) were selected,  
280 as are the minimum allowed increments in the robotic and welder equipment setup used for the  
281 experimental proof of concept (Section 4). If larger increments were selected, the restrictions  
282 would be satisfied in fewer iterations. Still, the cross-section area of the welding passes would  
283 be much different from the welding parameters that the user initialized at the start of the  
284 framework and at the end may not be accepted if the deviation is outside of the accepted  
285 window of the WPS document. It must be stressed also that large cross-section area beads  
286 produced from increased wire feed speed, may fill faster the area and volume of the groove,  
287 but will require more iterations to adjust the welding parameters if the restrictions are violated.

### 288 ***3.4. Cost Function and Sequence of Welding Parameters***

289 In manual welding, the sequence of welding parameters per layer is not always known  
 290 beforehand. Therefore, when considering automated welding, the total number of layers,  
 291 welding passes, arc time and the amount of filler wire material that will be required are often  
 292 unknown variables in the multi-pass weld planning procedure. As these parameters drive the  
 293 actual costs of welding, they can be used to form a cost function. Such a cost function can be  
 294 assigned by the operator and could be minimised, leading to the most optimum welding  
 295 procedure.

296 For a given V-groove geometry and a produced sequence of welding parameters, the cost  
 297 function proposed is the weighting summation of the number of passes, the amount of filler  
 298 material and total arc time required. It takes the form of Eq:3:3 where  $w_1, w_2, w_3$  are the

$$C(w_1, w_2, w_3) = w_1 \cdot \text{passes} + w_2 \cdot \text{material} + w_3 \cdot \text{time} \quad \text{Eq:3:3}$$

299 weighting coefficients which must add up to 100% in total. These weighting coefficients are  
 300 set by the operator, based on which parameter they would like to minimise the most.

301 The value of number of passes per layer are given from the algorithm described in Section 3.2.  
 302 Regarding the arc time and amount of filler material per layer is given by Eq:3:4 and Eq:3:5  
 303 respectively.

304

$$\text{Arc time/layer} = \sum \text{arc time/pass} \quad \text{Eq:3:4}$$

$$\text{arc time/pass} = \text{Length specimen}/v$$

305

$$\text{Filler material / layer} = \sum \text{material/pass}$$

$$\text{material/pass} = (\text{wire weight/mm}) * \text{length of wire} \quad \text{Eq:3:5}$$

$$\text{length of wire} = (\text{arc time /pass}) * u$$

306 To automate this process, the user initially defines the welding parameters that will be used in  
 307 the welding framework providing in pairs of  $w_c$  vectors, as mentioned in section 3.1, and are  
 308 feasible from the welder equipment regarding heat input and welding speed. It must be noted  
 309 that utilizing beads with increased cross-section area by increasing the wire feed speed  $u$  and  
 310 keeping constant the robot speed  $v$ , will result in a decreased number of passes to fill the V-  
 311 groove volume. However, the welding parameters must be approved from the relevant WPS  
 312 document regarding the properties of the joint material. Increased wire feed speed and as a  
 313 result increased current can result to excessive heat input, damaging the internal structure of  
 314 the material and generating defects.

315 These welding configurations are stored as a vector  $\tilde{W} = [w_{c_1}, w_{c_2}, \dots, w_{c_n}]$  where  $n \in Z^+$  is  
 316 the length of the vector and shows the number of different welding parameters. The vector  $\tilde{W}$   
 317 remains constant for all the varying V-groove geometries that welding is scheduled.

318 **3.4.1. Homogeneous Weld Instances**

319 Firstly, the total number of layers that can fit in a provided V-groove geometry has to be  
 320 estimated based on the assigned vector  $\tilde{W}$ . Following the root and hot pass which are not  
 321 generated from the developed welding framework, the number of welding layers for the  
 322 remaining volume of the groove can be found by iterating through  $\tilde{W}$ , and creating instances  
 323 of the same geometry where each layer is assigned the same welding configuration.

324 This is illustrated in Figure 8, where the generated samples of the V-groove geometry can be  
 325 seen. The number of passes per layer is found, utilizing the algorithm described in sections 3.2  
 326 and 3.3.

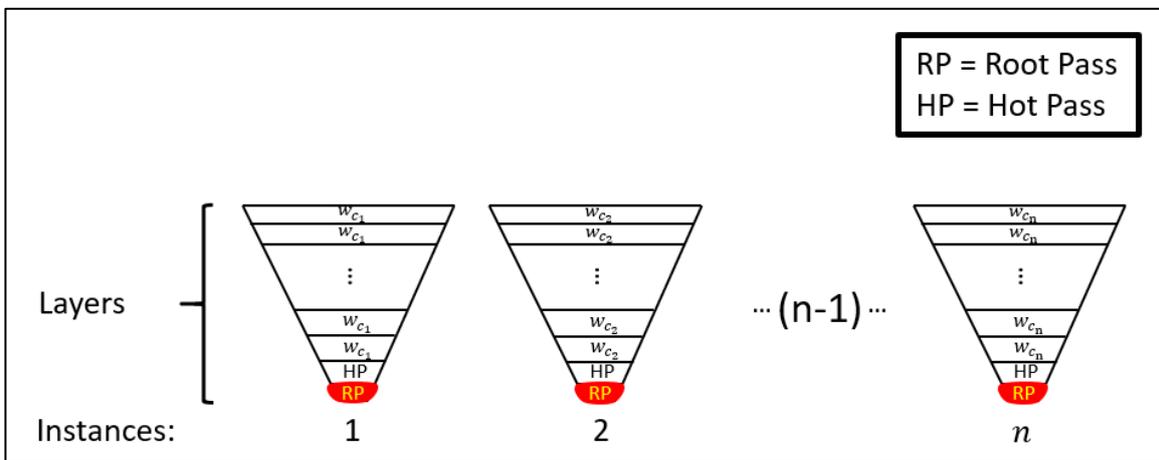


Figure 8. Highlighted are the initial generated instances which investigate the maximum number of layers that fitted among all the  $n$  different welding configurations in  $\tilde{W}$  vector

327 The  $w_c$  welding configuration per layer is adjusted if the restrictions of height and weaving  
 328 criteria are violated. Therefore,  $n$  different instances are created for the same geometry and the  
 329 maximum number of layers that found from this iterative process is recorded and defined as  
 330  $k \in Z^+$ .

331 **3.4.2. Heterogeneous Weld Instances**

332 Permutations within iterations are utilized to determine all the different ways that the welding  
 333 parameters can be assigned for the maximum number of layers found, while addressing the  
 334 need for varying welding parameters as the layers are generated. The number of permutations  
 335 can be found using Eq:3:6, and these are populated schematically in array  $P$  of Figure 9.

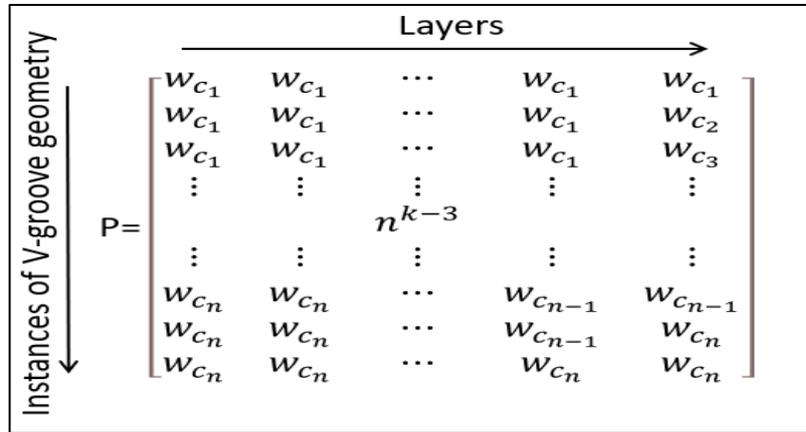


Figure 9. Array  $P$  is generated from populating the welding parameters per layer for  $n$  different welding configurations  $w_c$  using permutations within iterations

336 Iteration is used since every new layer can have the ability to get assigned the same welding  
 337 configuration  $w_c$  as the previous layer.

$$P_n^k = n^k \text{ where } k, n \in Z^+ \quad \text{Eq:3:6}$$

338 For example, if  $n = 4$  different welding configurations of  $w_c$ , assigned in the framework as  
 339 vector  $\tilde{W}$  and  $k = 6$ , found from the process described in Section 3.4.1, then  $4^6 = 4096$   
 340 different sequences of welding parameters, for the same groove geometry, can be generated,  
 341 utilizing only four other welding parameters. However, not all the generated welding sequences  
 342 are unique, since the value  $k$  that was found is a rough estimation of how many layers can fit  
 343 in the V-groove when all the layers have the same welding parameters. The restrictions on  
 344 height and weaving width that are imposed when a new pass is added to the layer affect the  
 345 height where every layer will reach within the V-groove. The algorithm reported in [24] that

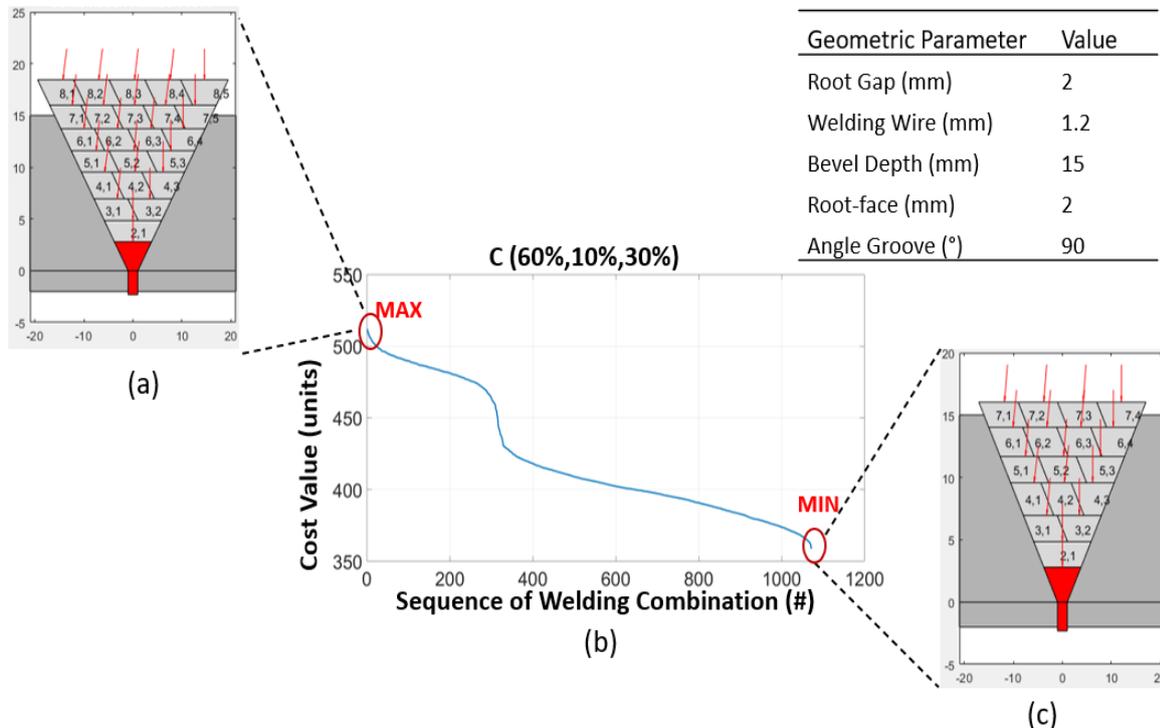
346 calculates the weaving width of a pass is guided from the summation of the cross-section areas  
347 of previous beads and the height where the last layer reached. Combining this fact with the V-  
348 groove shape, where by definition the width of the groove increases from bottom to top and  
349 more passes can fit per layer, the number of total layers at the end may not be equal to the  
350 estimated value  $k$  (see Section 3.4.1). Besides, layers with welding parameters that follow a  
351 swapped order result from the permutations (i.e.  $[w_{c_1} - w_{c_2} - w_{c_1}]$ ,  $[w_{c_1} - w_{c_1} - w_{c_2}]$ ,  $[w_{c_2} -$   
352  $w_{c_1} - w_{c_1}]$ ) and have different cross section area, may not reach the same height as they can  
353 be deposited in a different height offset from the root face. As a result, the restrictions can  
354 generate different number of passes in these instances. The existence of these cases requires  
355 one additional layer, and this depends on the sequence of welding parameters that were  
356 populated until reaching the formation of these layers. For that reason, permutations within  
357 iterations are investigated for  $k + 1$  possible welding layers with  $n$  pairs  $w_c$  of welding  
358 configurations to compensate for these cases.

### 359 **3.4.3. Weld Build Instances and Cost Function Calculation**

360 Populating the array  $P$  with dimensions  $n^k \times k$ , as shown above in Figure 9 which stores the  
361 permutations of different welding sequences for a given V-groove geometry, is essential to find  
362 all the values of the cost function. A V-groove instance filled by layers is created, where each  
363 layer following the root and hot pass, gets assigned the welding parameters per column of the  
364 array  $P$ . For every generated layer the algorithm analysed in section 3.2, is used to generate the  
365 number of passes where the amount of filler wire, the arc welding time and the number of  
366 passes is recorded based on Eq:3:4 and Eq:3:5. New layers are added until the top surface of  
367 the V-groove is reached and the robotic path per pass is generated based on [24] and welding  
368 parameters assigned per layer. Regarding the arc welding time, optional time of 10 seconds  
369 should be added after depositing each pass to avoid contamination with following passes.  
370 Eq:3:3 is used to calculate the value of the assigned cost function. This process is repeated for  
371 all the rows of array  $P$ , until  $n^k$  weld build instances are populated and those that resulted in  
372 the same cost value are rejected.

373 For example, assuming the annotated geometry in Figure 10, the proposed solution for the  
374 sequence of the welding parameters derives from the minimum value of the cost function  
375  $C(60\%, 10\%, 30\%)$ . Schematics in Figure 10(a), (b) represents the number of layers, along with  
376 the generated passes and pose of the weld torch. The values of the cost function for all 1071  
377 generated unique instances highlight the extreme maximum and minimum values and all the

378 different ways that the geometry can be welded utilizing four different welding configurations  
 379  $w_c$ . The aim was to minimize the number of passes; thus, the first weighting coefficient was  
 380 selected to be 60%. Comparing the results from the maximum cost value relative to the



**Figure 10. Highlighted cost function built from 1071 unique instances using 4 different welding configurations for 7 possible layers: (a) Solution from maximum cost value showing additional required six passes and increased welding time of 44.49%, (b) Cost function along the sequences of welding combinations, (c) Solution from minimum cost value showing a decrease of 34.24% in filler wire and six welding passes less than the maximum result**

381 minimum requires 6 more passes, the welding time is increased by 44.49% and filler wire is  
 382 34.24% higher. This result validates the benefits linked to the cost function concept, which  
 383 decreases the actual costs of automated welding, through reduced welding time, material and  
 384 passes deposited. Moreover, when the geometry under consideration increases in depth and  
 385 groove angle, more instances can be built and investigated, exploiting the advantages of the  
 386 cost function concept, and delivering crucial savings on large scale projects in terms of cost  
 387 and time planning.

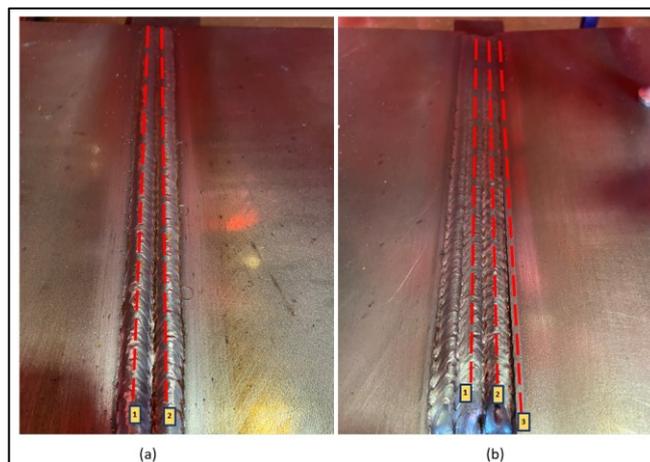
388 This process can be accelerated if instead of populating all the instances for every sequence of  
 389 welding parameters, to reject every new incompatible instance when a new layer is added.  
 390 However, the benefits of investigating the welding sequence from the minimum value of  
 391 different cost functions, recommends the generation of all the possible instances for every row  
 392 of array  $P$ . Therefore, the series of welding configurations that minimize at the most one of the  
 393 three parameters (welding time, number of passes, filler material) can be found.

394 **3.5. Formalizing the Deposition of Additional Cap Passes**

395 The need to formalize the input of additional weld cap passes in the path layout model of [24],  
396 originates from initial welding trials, where the schematic of the proposed and actual welding  
397 solution did not match the expected result. The reasons behind this can be summarized as  
398 follows:

- 399 • According to the model of the welding torch pose and generated weld pass on [24], the  
400 shape of each bead (trapezium/parallelogram) is an approximation of the actual result  
401 and the space that will be allocated. However, as the molten weld pool solidifies, gravity  
402 and residual stress forces alter the approximated shapes in the cap layer to be more  
403 convex, circling the toes of the edges.
- 404 • Based on [24], all weld passes are deposited from side to side, and the increased angle  
405 of the torch on the first pass of the cap layer relative to the working angle of the root  
406 pass leads to overlap a part of the toes of the top surface. Additional passes with the  
407 same angle overlap again part of the previous cap passes, resulting in the formation of  
408 hollow spaces as can be seen in Figure 11 (a) and (b).

409 Therefore, the additional cost related to the necessary cap passes is required to be  
410 incorporated into the cost function calculation in order for the total minimum solution to  
411 be found.



**Figure 11. Highlighted formed concave spaces: (a) Between dotted lines 1 and 2 (b) Between dotted lines 1 and 2, 2 and 3**

412 Formalizing these passes depends on the welding parameters of the previous passes in the cap  
413 layer. If the total number of weld beads deposited in the cap layer is denoted with letter  $m$ ,  $p_m$   
414 is the offset of the last pass from the middle of the seam and  $w_m$  is the weaving width then:

- 415 • When  $m = 2$ , only one additional cap pass is required. The pass is deposited in the  
 416 middle of the V-groove (zero-offset from root gap) utilizing the same pose as the root  
 417 pass with wire feed speed 10% less, based on experimental analysis, than what was  
 418 used for the other passes at the same layer. Moreover, the required weaving width was  
 419 set to be 3 mm from the experimental trials.
- 420 • For the case where  $m > 2$  two additional cap passes are required. The first one is  
 421 deposited between one pass before the last one and the last one with the position offset  
 422 from the middle of the seam, is given by Eq: 3:7.

$$p_{m+1} = \frac{(p_{m-2} + w_{m-2}) + (p_{m-1} - w_{m-1})}{2} \quad \text{Eq: 3:7}$$

424 The second pass is deposited with an offset from the middle of the seam based on Eq:  
 425 3:8.

$$p_{m+2} = p_{m-1} + w_{m-1} \quad \text{Eq: 3:8}$$

426 As before the required wire feed speeds for both passes are 10% less than what is  
 427 assigned in the other passes on the cap layer and the weaving width is 3 mm. Moreover,  
 428 the angle of the welding torch for the second cap pass was set to be  $-5^\circ$  relative to the  
 429 root pass angle. Consequently, proper fusion is managed with the already deposited  
 430 pass and the toes of the bevel.

431 It must be noted that the bevel depth input to the framework should be increased by 1 mm  
 432 relative to the actual. This action assists in forming a cap layer, where new layers are generated  
 433 until the total height of the last layer exceeds the groove depth by 1 mm.

434 The proposed additional cap passes in the welding framework result can be seen schematically  
 435 with the red dotted lines on the top layers in Figure 12. The selected welding parameters for  
 436 both cases, were guided from the experimental trials and provided suitable fusion of the two  
 437 toes of the bevel groove and a clean finish of the cap layer. Formalizing the additional cap  
 438 passes requirement, allows the generalization of this process in varying V-groove geometries.

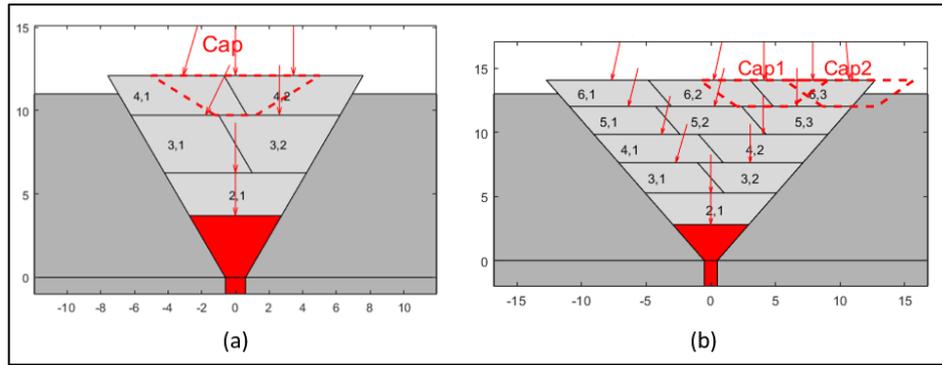


Figure 12. Additional cap passes added to the welding framework solution to compensate between the model and actual welding result: (a) One more cap pass is required in the middle of the seam since the total deposited passes in the top layer were  $m=2$ , (b) Two additional cap passes are proposed when  $m>2$  and the deposition position is formalized based on the previous existing passes in the same layer

439

## 440 4. Proof-of-Concept Experimental Verification

### 441 4.1. Experimental Setup

442 A series of experiments were undertaken to prove the feasibility of the proposed welding  
 443 framework for multi-pass welding, aiming to automate the generation of the robotic motion  
 444 path, welding parameters allocation and optimisation per layer based on the cost function  
 445 concept. A 6 DoF articulated robotic welding system was deployed, and two different types of  
 446 steel of three samples were bevelled under different V-groove geometries as can be seen in  
 447 Table 7. The robotic setup is shown in Figure 13 and recorded in Table 3.

Table 3. Robotic and welding equipment layout

#	Equipment
1	KUKA KR3-R540
2	Scan-Control 2910-100/BL
3	TBI Weld Torch 22°
4	XIRIS XVC 1000
5	Blackfly PGE50S5C
6	TBI Weld Torch Hose 1.2m
7	Jackle Propuls 400 V wire feeder

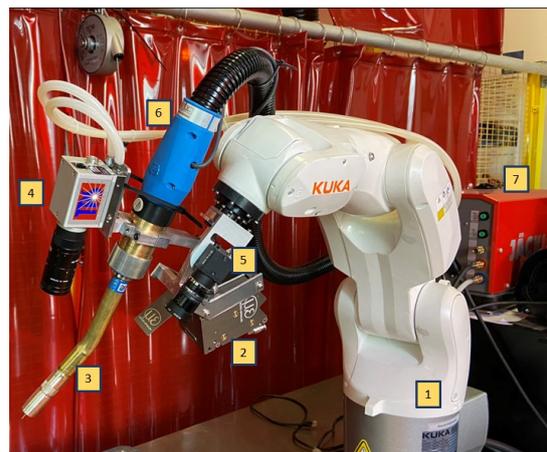


Figure 13. KUKA-KR3 Transformed into a compact welding robot

448 A laser scanner (2) [28] extracts the geometric characteristics of the V-groove geometry such  
 449 as the root gap, groove angle, bevel depth, height of root face, length of specimen and height  
 450 offset of the root pass from the root-face, which are the inputs to the framework. The welding

451 process was MAG using pulsed current to reduce the welding spatter in absolute wire-feed  
 452 speed synergic mode [29–31]. Shielding gas ArCO<sub>2</sub>-(80% Ar + 20% CO<sub>2</sub>) with a constant flow  
 453 of 15 l/min and filler solid wire of 1.2 mm diameter was used with characteristics shown in  
 454 Table 4.

455 The working angle of the welding torch selected was 65.5° and the wire stick-out was 8.5 mm.  
 456 A XIRIS high dynamic range weld camera (4) [32] provides visual feedback of the weld pool  
 457 during welding, and the colour camera (5) [33] locates the weld joint in the scene relative to  
 458 the reference frame of the welding torch [22]. Robot motion happens through real-time  
 459 communication provided from the Robot Sensor Interface (RSI) [34] of KUKA at real-time  
 460 intervals of 4ms. Control of welding dynamics is facilitated from a compact embedded  
 461 reconfigurable input/output (cRIO 9035) controller of National Instruments (NI) [35], using  
 462 analogue and digital connections and software developed in LabVIEW environment.

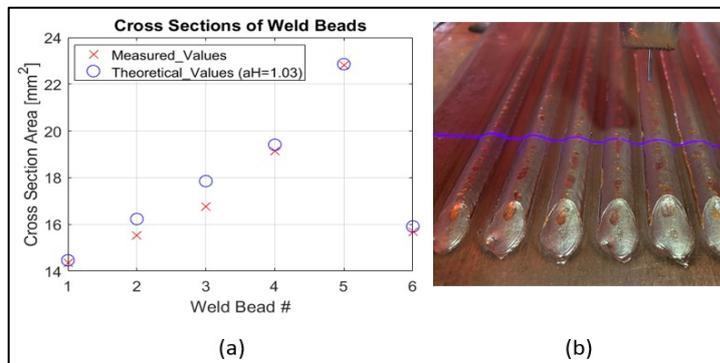
463 **Table 4. Chemical composition of solid wire (%) - (Based on manufacturer certificate)**

C	Si	Mn	P	S	Ni	Cr	Mo	Cu	V	Al	N	Ti+Zr
0.081	0.86	1.46	0.011	0.007	0.02	0.04	0.01	0.02	<0.01	<0.01	0.007	0.008

464

#### 465 **4.2. Welding Parameters Configuration**

466 To determine the deposition coefficient  $a_H$ , which is described in Section 3.1, beads with  
 467 different welding parameters were deposited and the cross-section area of each one was  
 468 measured using the laser scanner with settings indicated in Table 5. Comparing each cross-  
 469 section area with the theoretically expected value from Eq:3:2 is shown in Figure 14.



**Figure 14. Highlighted cross section of welding beads with different welding parameters: (a) Measured values with laser scanner relative to theoretical values of Eq:3:2, (b) Deposited welding beads (front side-end of weld beads)**

**Table 5. Laser Scanner 2910-100/BL Inspection setting**

Settings Parameter	Value
Exposure Time (ms)	1.5
Number of Profiles (Hz)	105
Saturation (%)	78
Filter Median (taps)	5
Inspection Distance (mm)	140

470 Obtaining the correct value of  $a_H$  is driven from initial trials of welding V-grooves where the  
471 proposed schematic solution of the welding joint did not match the volume of the actual  
472 welding result. Changing this parameter alters the schematic solution and the proposed number  
473 of passes as well. As a result, the constant  $a_H$  found to be  $a_H = 1.03$ . Following this  
474 investigation, each of the welding configurations  $w_c = [v, u]$  selected for these experiments  
475 and used as input to the welding framework are stated in Table 6, sorted in descending order  
476 of their cross-section area. The selection of these welding configurations aligns with the  
477 industrial partner's WPS for the welding joints provided in Table 7, as well with the purpose  
478 to have beads that form a window of varying cross-section area, where in that case covers 14.46  
479  $\text{mm}^2$ -17.85  $\text{mm}^2$  . As it is shown in Section 4.3, selecting welding configurations that form a  
480 fine window of cross-section areas can lead to different sequences of welding parameters linked  
481 to the minimum solution of the cost function for varying V-groove geometries, as well for the  
482 same welding geometry and for different cost functions (Table 12).

483 **Table 6. Welding Parameters ( $n=4$ ) along with theoretical, measured cross-section areas and recorded**  
484 **electrical parameters**

Welding Configuration	Robot Speed (mm/s)	Wire Feed Speed (mm/s)	Theoretical Cross Section ( $\text{mm}^2$ ) *	Measured Cross Section ( $\text{mm}^2$ )	Current (A)	Voltage (Volts)
$w_{c1}$	5	76.63	17.85	16.77	144	21.9
$w_{c2}$	5	68.3	15.91	15.69	131	21.3
$w_{c3}$	5.5	76.63	16.23	15.52	144	21.9
$w_{c4}$	5.5	68.3	14.46	14.35	131	21.3

485 \* Eq:3:2 calculates the theoretical cross-section area in the welding framework

486 Moreover, if the number of welding current values increase by two then the wire feed speeds  
487 change as well and selecting two additional robot speeds brings the total number of welding  
488 configurations to  $n + 2 = 6$ . Hence, Eq:3:6 storing the number of total permutations, gets the  
489 value  $(n + 2)^k$  where the size of array P in Figure 9 increases to  $(n + 2)^k \times k$  and as a result  
490 additional time is required to investigate and build all the different welding instances.

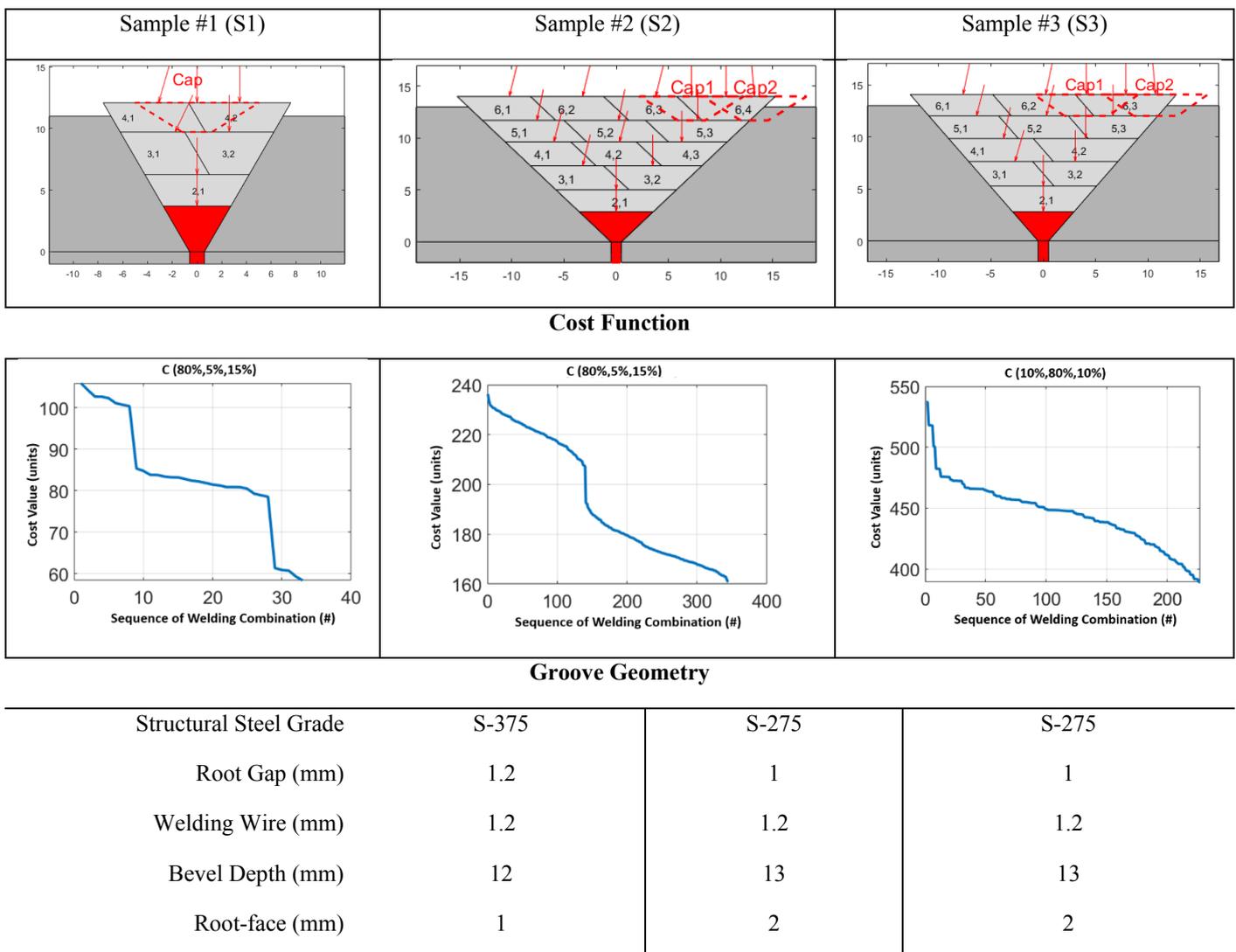
491 The weaving restriction enforced by parameter delta ( $\delta$ ), was found experimentally to be  $\delta =$   
492 2. A condition in weaving reported in [24], was used in the algorithm described in Section 3.2  
493 which compensates the weaving width of the welding torch since the molten weld puddle can  
494 fuse with the edges of the groove without the tip of the wire flush with them.

### 495 **4.3. Experimental Validation and Results**

496 For the experimental verification trials, three different groove geometries and material  
 497 combinations were selected based on commonly used marine and manufacturing  
 498 configurations to highlight both the applicability and flexibility of the proposed concept. The  
 499 geometric characteristics of the welded bevelled joints are shown in, Table 7, along with the  
 500 minimum value of the used cost function for each sample. The red arrows represent the pose  
 501 of the welding torch for every weld pass, based on the path layout model presented in [24].

502 Figure 15 illustrates the 14 deposited weld passes for sample S3 which validates the proposed  
 503 welding solution in terms of adequately filling the whole groove with the generated welding  
 504 passes resulting in a cap height above the top surface of average value 0.9 mm. The generated  
 505 welding parameters produced from the welding framework are stored in Table 8 to Table 10  
 506 for S1, S2 and S3 samples, respectively.

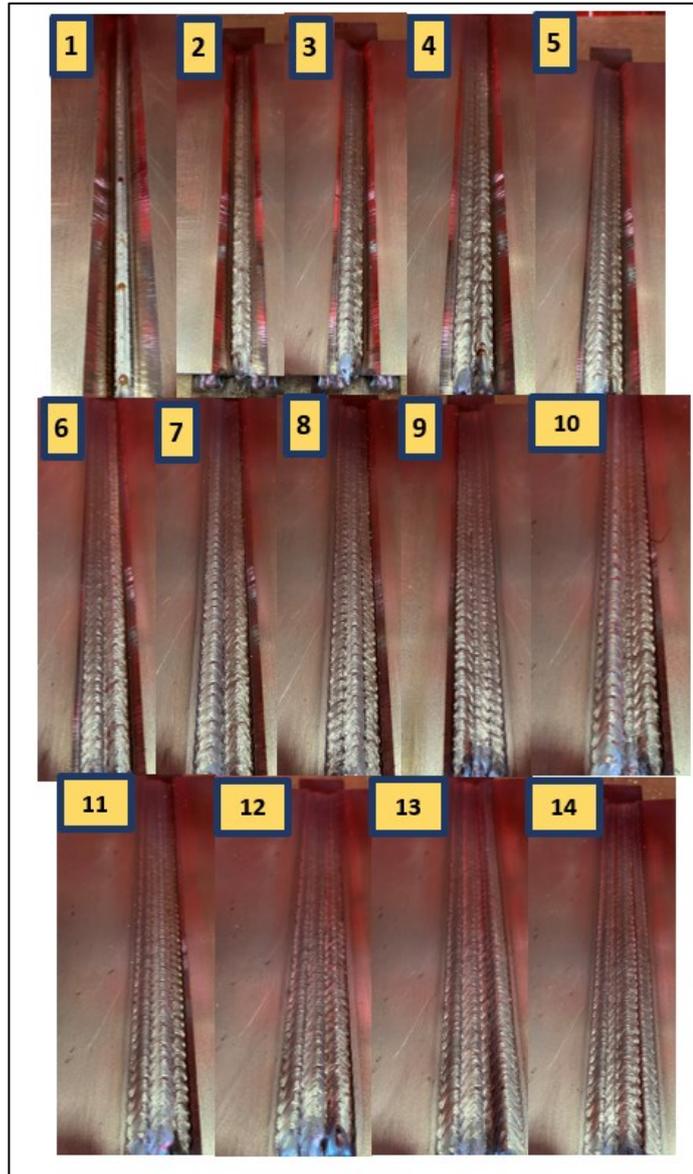
507 **Table 7. Highlighted is the proposed solution of the welding framework for each V-groove sample along**  
 508 **with the cost function used and geometric properties of the weld joints**



Groove Angle (°)	60	93	82
Root Height Offset (mm)	3.7	2.9	2.8
Length of joint (mm)	300	300	300

509

510



511

512

Figure 15. The generated welding sequence for the minimum value of cost function C(10%, 80%, 10%) resulted in 14 weld passes for sample S3

513

514

Table 8. S1 Generated welding parameters

Layer Number (#)	Pass Number (#)	Wire Feed	Robot Speed (mm/s)	Offset-middle of the	Height from root-	Angle of	Weaving Width (mm)	Consumable Material (g)	Arc Welding Time (s)
------------------	-----------------	-----------	--------------------	----------------------	-------------------	----------	--------------------	-------------------------	----------------------

		Speed (mm/s)		seam (mm)	face (mm)	torch (°)			
1	1	60	4.50	0	3.70	0	0.73	32.93	66.66
2	1	83.30	5.50	0	6.26	0	2.21	37.40	54.54
3	1	76.63	5	-1.77	9.72	25.61	1.99	37.85	60
3	2	76.63	5	2.60	9.72	0	1.60	37.85	60
4	1	76.63	5.50	-3.10	12.09	16.02	2.30	34.41	54.54
4	2	76.63	5.50	3.44	12.09	0	2.13	34.41	54.54
4	3	68.96	5.50	0	12.09	0	3	30.97	54.54

515

516

**Table 9. S2 generated welding parameters**

Layer Number (#)	Pass Number (#)	Wire Feed Speed (mm/s)	Robot Speed (mm/s)	Offset- middle of the seam (mm)	Height from root- face (mm)	Angle of torch (°)	Weaving Width (mm)	Consumable Material (g)	Arc Welding Time (s)
1	1	55	5	0	2.90	0	1.55	27.17	60
2	1	93.30	5.50	0	5.01	0	3.78	41.90	54.54
3	1	76.60	5.50	-3.21	7.33	13.77	2.86	34.41	54.54
3	2	76.6	5.50	3.50	7.33	0	2.72	34.31	54.54
4	1	68.30	5.50	-5.98	9.63	14.77	2.50	30.67	54.54
4	2	68.30	5.50	0.30	9.63	14.77	2.50	30.67	54.54
4	3	68.30	5.50	6.29	9.63	0	2.357	30.67	54.54
5	1	76.63	5.50	-7.61	11.70	11.69	3.11	34.41	54.54
5	2	76.63	5.50	0.21	11.70	11.69	3.11	34.41	54.54
5	3	76.63	5.50	7.82	11.70	0	3.00	34.41	54.54
6	1	76.63	5.50	-10.25	14.01	13.72	2.86	34.41	54.54
6	2	76.63	5.50	-3.23	14.01	13.72	2.86	34.41	54.54
6	3	76.63	5.50	3.79	14.01	13.72	2.86	34.41	54.54
6	4	76.63	5.50	10.53	14.01	0	2.73	34.41	54.54
6	5	68.96	5.50	7.236	14.01	0	3	30.97	54.54
6	6	68.96	5.50	13.26	14.01	-5	3	30.97	54.54

517

**Table 10. S3 Generated welding parameters**

Layer Number (#)	Pass Number (#)	Wire Feed Speed (mm/s)	Robot Speed (mm/s)	Offset-middle of the seam (mm)	Height from root-face (mm)	Angle of torch (°)	Weaving Width (mm)	Consumable Material (g)	Arc Welding Time (s)
1	1	55	5	0	2.8	0	0.93	27.17	60
2	1	93.30	5.50	0	4.26	0	3.07	41.9	54.54
3	1	68.30	5.50	-2.71	7.63	16.17	2.25	30.67	54.54
3	2	68.30	5.50	3.05	7.63	0	2.08	30.67	54.54
4	1	76.63	5	-3.80	9.84	12.42	3.12	37.85	60
4	2	76.63	5	4.04	9.84	0	3.00	37.85	60
5	1	68.30	5.50	-6.38	12.01	14.24	2.41	30.67	54.54
5	2	68.30	5.50	0.27	12.01	14.24	2.41	30.67	54.54
5	3	68.30	5.50	6.66	12.01	0	2.27	30.67	54.54
6	1	76.63	5.50	-7.67	14.06	11.99	2.94	34.41	54.54
6	2	76.63	5.50	0.21	14.06	11.99	2.94	34.41	54.54
6	3	76.63	5.50	7.88	14.06	0	2.83	34.41	54.54
6	4	68.96	5.50	4.10	14.06	0	3	30.97	54.54
6	5	68.96	5.50	10.72	14.06	-5	3	30.97	54.54

519

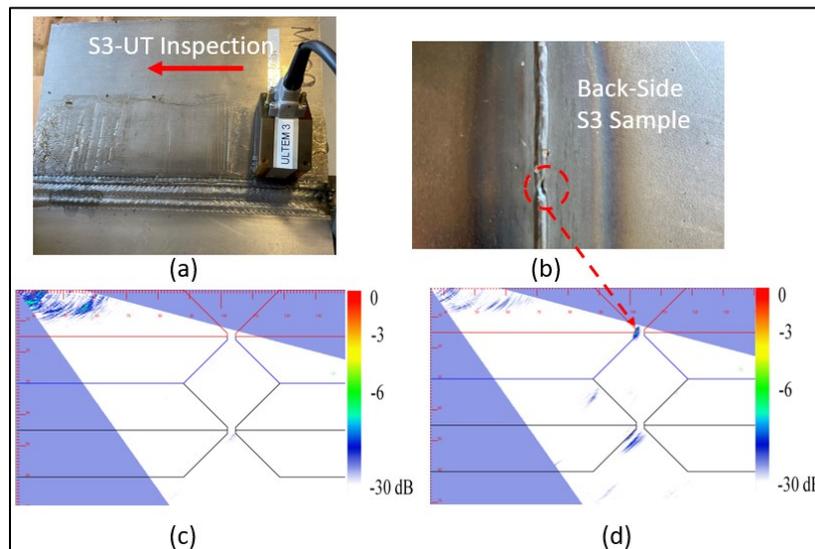
#### 520 4.3.1. Ultrasound Inspection for Defects

521 There exists established acceptance standards specific to welds and their final application  
 522 defining limits related to the presence and size of flaws. These undesirable internal defects can  
 523 reduce the life span and structural integrity of the weldments [16]. Thus, the integrity of the  
 524 above welding results are commonly verified through Non-Destructive Testing (NDT) utilizing  
 525 ultrasound inspection.

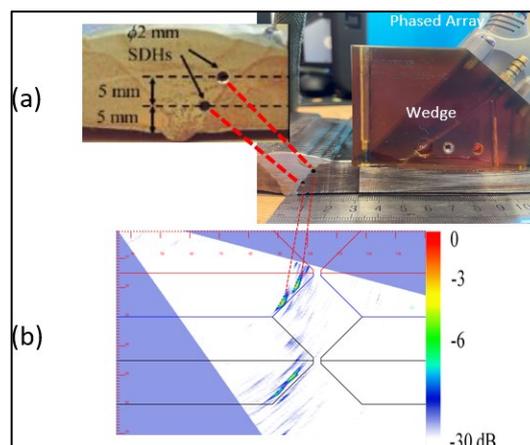
526 For that purpose, Phased Array Ultrasonic Testing (PAUT), as the preferred method for  
 527 inspection of welded samples, is employed to inspect the produced weldments [36]. An  
 528 ultrasonic probe of 5 MHz with a linear array of 64 elements of 0.5 mm pitch was used to  
 529 perform sectorial scans. An Ultem wedge of 37.6° was attached to the array and the focal laws  
 530 were generated to form an S-scan covering a range of 35°-75°. Gain calibration, according to  
 531 BS EN ISO 17640 was performed, and the reflections from defects compared with the reference

532 response signal. The calibration is depicted in Figure 17 where two side-drilled holes of  $\varnothing$  2  
 533 mm diameter in a 15 mm thick welded section are inspected with the phased array probe. The  
 534 gain was set to 50 dB, where the signal amplitude indicates 100% of the scale bar.

535 Following the gain calibration, each produced welded joint was inspected at room temperature  
 536 along the length of the welding axis. In some positions, lack of root penetration was identified  
 537 and is reported in Figure 16. No indication for lack of fusion on sidewalls or inter-pass lack of



**Figure 16. Phased array inspection and indication of lack of root penetration: (a) Sample S3 showing the direction of inspection, (b) Back-side of sample S3 where lack of root penetration exist, indicated by the red circle, (c) Sector scan 35°-75°: where no defects are found, (d) Sector scan 35°-75°: reflection caused from lack of root penetration**



**Figure 17. Gain calibration using two side-drilled holes of  $\varnothing$  2 mm for PAUT inspection**

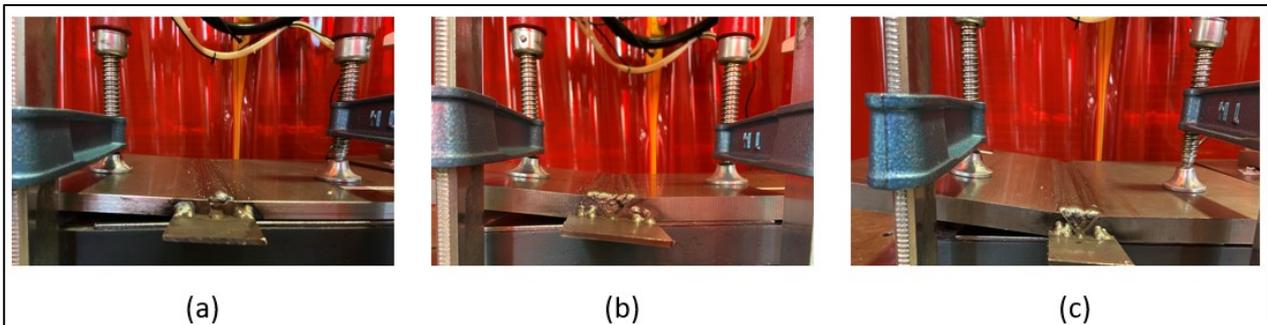
538 fusion was detected across all samples, which can frequently occur in welded joints during  
 539 manufacturing [37].

540 Lack of root penetration may have been caused by misalignment fitting of the parent metal  
541 plates during joint setup and uneven height of root face caused by bevelling of the weld  
542 grooves. As mentioned previously, the welding parameters for root and hot pass are instructed  
543 from the operator and are not included in the automation of the proposed welding framework,  
544 which is discussed in this paper.

#### 545 **4.3.2. Distortion on the Weldments**

546 Distortion was observed along the vertical direction of welding as shown in Figure 18. The  
547 inter-pass temperature was held at 70°C, and clamping was consistent across all samples.  
548 Distortion was more severe in samples S2 and S3, where their structural steel grade is lower  
549 than S1 and the thickness of the plates is 3 mm higher. Also, on all samples, metal straps were  
550 tack welded on both sides to prevent excessive distortion.

551 Distortion is attributed in the order which the generated welding passes are deposited. The  
552 deposition is side to side, always starting from the left of the groove (seen from the front-side  
553 of Figure 18) generating increased heat on the left parent plate introducing distortion.



**Figure 18. Distortion observed on welded samples: (a) Sample 1-Material S-375 with seven welding passes, (b) Sample 2-Material S-275 with 16 welding passes, (c) Sample 3-Material S-275 with 14 welding passes**

554 Moreover, weaving is required on every welding pass, except the root pass, which increases  
555 the heat input as the welding torch spends more time inside the groove.

## 556 **5. Discussion**

### 557 **5.1. Generated Welding Results and Cost Functions**

558 Three manufactured samples were produced by the proposed welding framework with the cost  
559 function concept described in Section 3.4, and presented in this work with welding parameters  
560 recorded in Table 8 to Table 10. The samples were welded using the generated welding  
561 parameters and visual inspection showed no undercuts or lack of fusion between adjacent  
562 passes. This was also validated from the PAUT inspection presented in Section 4.3.1.

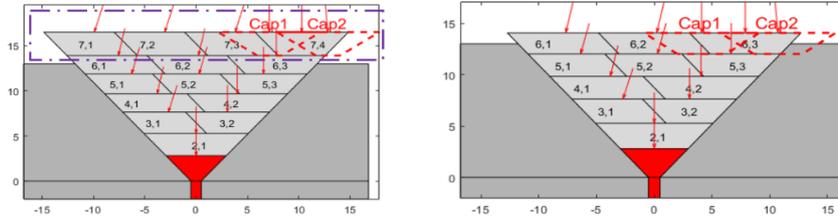
563 The welding parameters utilized to weld each sample, were extracted from the optimum  
 564 generated instance of the V-groove linked to the minimum value of the assigned cost function.  
 565 Regarding sample S2, where cost function  $C(80\%, 5\%, 15\%)$  was assigned, comparing  
 566 between its maximum and minimum values, the welding time was decreased by 32.9% and the  
 567 amount of filler wire by 26.18%. Similar savings are noticed regarding the cost function of  
 568 sample S3,  $C(10\%, 80\%, 10\%)$ , where the reduction in welding time and in the amount of filler  
 569 wire was 28.3% and 27.38% respectively. These reductions are reported in Table 11 for both  
 570 samples, between maximum and minimum values of each cost function. In addition, from the  
 571 schematic comparison, the additional amount of filler wire for both samples (purple dotted  
 572 box), linked to the maximum solution is assigned to the cap pass area, which can be defined as  
 573 the less efficient solution for the cost function.

574 **Table 11. Comparison between maximum and minimum values of cost function  $C(80\%,5\%,15\%)$  and**  
 575  **$C(10\%,80\%,10\%)$  respectively for samples S2 and S3 regarding the amount of filler wire and arc time**

Sample S2	MAX	MIN	Decrease in %
Amount of filler material (g)	628.18	463.68	26.18
Arc time (s)	1259.1	843.63	32.9
Schematic Solution			

Sample S3	MAX	MIN	Decrease in %
Amount of filler material (g)	542.97	394.26	27.38
Arc time (s)	1011.8	725.45	28.30

Schematic  
Solution



576

577 Samples S1 and S2, utilise the same form of the cost function to reflect the difference on the  
 578 amount of possible unique sequences of welding parameters and the increase in the values that  
 579 the function receives as the weld groove geometry changes in depth, groove angle and gap  
 580 offset. As it was expected, sample S2 required two more welding layers and nine welding  
 581 passes than sample S1. The selection of weighting coefficients for the cost function depends  
 582 solely on the operator's choice, and different cost functions can be compared only in the degree  
 583 that the result is driven by the operator's choice of the parameter to minimise at most.

584 This can be understood better in sample S3 with cost function  $C(10\%, 80\%, 10\%)$ , which  
 585 highlights the aim to reduce at most the filler consumable material relative to the other two  
 586 parameters. Comparing the utilized cost function relative to  $C(80\%, 5\%, 15\%)$  for the same  
 587 sample, the amount of filler wire is reduced by 4.34 grams, but the additional arc welding time  
 588 is increased by 9.91 seconds since the  $w_3$  is reduced by 5%. The expected outcome which is  
 589 shown in Table 12, is validated from the reflection of the weighting coefficients in the  
 590 generated sequence of welding parameters in layers 4 and 5 if the cost function  
 591  $C(80\%, 5\%, 15\%)$  was deployed instead of  $C(10\%, 80\%, 10\%)$ .

**Table 12. Different generated welding parameters in layers 4 and 5 for sample S3 using cost function  $C(80\%, 5\%, 15\%)$  instead of  $C(10\%, 80\%, 10\%)$**

Layer Number (#)	Pass Number (#)	Wire Feed Speed (mm/s)	Robot Speed (mm/s)	Consumable Material (g)	Arc Welding Time (s)
4	1	76.63	5/5.50	37.85/34.41	60/54.54
4	2	76.63	5/5.50	37.85/34.41	60/54.54
5	1	68.3/76.63	5.50	30.67/34.41	54.54
5	2	68.3/76.63	5.50	30.67/34.41	54.54
5	3	68.3/76.63	5.50	30.67/34.41	54.54

597

598 Moreover, large variations in the results of different cost functions, for the same geometry, can  
 599 be achieved when the selected welding parameters  $w_c$  stored in vector  $\tilde{W}$  varies a lot in terms  
 600 of the cross-section area. However, selecting beads with excessive large cross-section area  
 601 decrease the total welding arc time, whereas the total heat input is increased.

602 The algorithm described in Section 3.2, which is called in every new layer, to determine the  
 603 number of welding passes has the advantage to adjust the initial welding parameters and adapt  
 604 in that way to varying V-groove geometries. The manufactured samples did not require this  
 605 utility, since geometries with groove angles above  $95^\circ$ , tend to require this logic as more passes  
 606 stack together to reduce the weaving width but conversely the height of the layer increases  
 607 above the restriction of 5 mm. To better clarify the adaption ability of the framework an  
 608 example is provided. Considering the V-groove geometry with characteristics as shown in  
 609 Table 13, using the welding parameters reported in Table 6 and cost function  $C(80\%,5\%,15\%)$   
 610 it was found that the initial number of layers that can fit according to Section 3.4.1 equals to  
 611 six. According to Section 3.4.2 investigation for permutations within iterations is performed  
 612 for seven layers and the total number of permutations based on Eq:3:6 equals to 16,384. It was  
 613 found that violations on the height and weaving width took place for layers 3,4,5 and 6 and the  
 614 logic described in Section 3.3 to adapt the given welding parameters was utilized 22,464 times  
 615 resulting in total additional time of 0.1135 sec. Moreover, the average time spent in this logic  
 616 when a violation occurred was  $5.0537e - 06$  sec and the welding configuration  $w_c = [5,76.63]$   
 617 had to change to  $[5.1,73.29]$  and in other instances to  $[5.15,71.62]$ , thus two or three iterations  
 618 of this logic for 22,464 times added the additional time. The reported execution times are  
 619 extracted from a workstation with an Intel Core i7 @ 2.60 GHz, 16.0 Gb of RAM, Windows  
 620 10x64 bit architecture.

621 **Table 13. V-groove geometry where violation on height and weaving width occurred in layers 3,4,5 and 6**

Geometric Parameter	Value
Root Gap (mm)	3
Welding Wire (mm)	1.2
Bevel Depth (mm)	15
Root-face (mm)	1
Groove Angle ( $^\circ$ )	120
Root Offset (mm)	2.5

622

## 623 **5.2. Performance assessment over the state-of-the-art**

624 Based on the available information that exists in the relevant works reported in Table 1, an  
 625 experimental simulation comparison of the performance of the proposed framework is  
 626 performed.

627 Regarding [24] and [25] the same groove geometry is used, where in the lateral the wire feed  
 628 speed used for every welding bead is not reported. This does not allow the calculation of the  
 629 amount of filler material used. To compare with [24], the same restrictions on the size of the  
 630 weld bead, weaving width and welding parameters were utilized relative to this method and  
 631 the cost function  $C(10\%,10\%,80\%)$  was assigned to reduce at most the arc welding time. To  
 632 have a common base of comparison the length of the joint was normalized to 300 mm and the  
 633 same root pass was used. The results are depicted in Table 14. Following the restrictions on the  
 634 height and weaving width for every welding layer that exist in [24], one more additional layer  
 635 and cap pass are added. As explained in Figure 6, this occurs from the investigation for the  
 636 numbers of layers and passes per layer and the need to find the optimum sequence of welding  
 637 configurations, by utilizing the same welding parameters as in [24]. As a result, by  
 638 redistributing the welding parameters and forming the required layers, delivers savings,  
 639 compared to prompting the user to decide for the number of layers and what are the welding  
 640 parameters that every layer can get assigned.

641 **Table 14. Quantitative comparison of the proposed welding framework relative to the work reported in**  
 642 **[24]**

	Layers	Number of Passes	Material (g)	Arc Time (s)
H. Zhang [24]	5	8	1400.49	1815.06
This body of work	6	9	1047.32	1551.33
Difference	+1	+1	-25.22 %	-14.53%

643

644 Since in the work reported in [25], the wire feed speed for every pass is omitted and the same  
 645 groove geometry is used as in [24], the results from the above table are used to compare with  
 646 the arc time required to weld the whole geometry. It can be seen in Table 15, that the amount  
 647 of welding passes deposited was 51, thus this method was not efficient to achieve a better arc  
 648 time than [24] and the proposed work herein.

649

650  
651

**Table 15. Quantitative comparison of the proposed welding framework relative to the work reported in [25]**

	Layers	Number of Passes	Material (g)	Arc Time (s)
S.J. Yan et al [25]	10	51	N/A	3657.45
This body of work	6	9	1047.32	1551.33
Difference	-4	-42	N/A	-57.58%

652

653 The proposed framework is also compared to [23] where a much smaller groove geometry with  
654 an angle of 25 ° is utilized than the previous works. The welding parameters for the root-pass  
655 from [23] were used. For the filling passes the welding parameters stated in Table 6 were  
656 assigned to the vector  $\tilde{W}$ , since in [23] the same welding pass is used for all the passes in the  
657 different layers. The cost function  $C(10\%,10\%,80\%)$  was utilized and the generated results of  
658 the welding framework are compared in Table 16.

659  
660

**Table 16. Quantitative comparison of the proposed welding framework relative to the work reported in [23]**

	Layers	Number of Passes	Material (g)	Arc Time (s)
T.-Y.Huang et al. [23]	5	7	237.19	432.17
This body of work	6	9	229.69	274.19
Difference	+1	+2	-3.16%	-13.42%

661

662 Regarding [7] and [22], which use the same experimental verification, there are not enough  
663 information to validate the characteristics of the utilized V-groove geometry.

## 664 **6. Future Work**

665 Future work should focus on the full automation of the welding procedure, investigating a  
666 suitable methodology for root and hot pass welding parameter allocation based on the gap and  
667 root face of the joints. Additionally, the order in which the welding beads are deposited, which  
668 revealed distortion, should be investigated, and incorporated to avoid adverse effects on the  
669 structural integrity of the weldments. Moreover, effort should be placed on the acceptance  
670 flexibility of the framework from irregularities that occur during bevelling and fitting of the  
671 parent plates prior to welding. Nonetheless, the procedure described in Section 3.4.3, to find  
672 the minimum value of the cost function for all the different weld instances can be optimized

673 by incorporating other methods, such as random search instead of grid search. This requires  
674 the modelling of the probability distribution of the parameters that affect the optimum result  
675 and concentrating around this area of search. As a result, this advancement will benefit welding  
676 geometries that require numerous welding layers to fill the groove area.

677 The basis of comparison for the presented welding framework is the current state of the art as  
678 depicted in Table 1. In addition, multiple welding trials and characterizations for varying  
679 groove geometries will be a key objective of future work.

680 It must be noted that in this body of work, we do not compare the result with that of a manual  
681 welder and what they could achieve, but foresee this as a significant body of future work fully  
682 characterizing and quantifying the overall decrease of welding costs through expansion of the  
683 cost function minimization approach.

684 Furthermore, this approach is not limited only in single-sided V-grooves and can be extended  
685 to different types of joints such as tee, lap corner and edge where multi-pass welding is  
686 required. Therefore, this work can be conceived as the foundation of projecting the multi-pass  
687 welding procedure as a real problem in manufacturing through the automation of welding and  
688 the benefits it can offer.

## 689 **7. Conclusion**

690 In this paper, an algorithmic framework for automated off-line robotic multi-pass V-groove  
691 weld path planning and sequencing is developed and validated. It can generate robotic welding  
692 paths and welding parameters for varying single-sided V-groove geometries, based on the  
693 operator's choice to minimize a cost function based on the number of welding passes, welding  
694 time and filler wire consumption.

695 The population of welding passes per layer is driven from the algorithm presented in Sections  
696 3.2 and 3.3, which generates the number of welding beads through the imposed restrictions on  
697 maximum weaving and height of every welding pass. The developed work builds on the  
698 algorithm in previous work [24] where the user prompts to enter the total number of layers,  
699 number of passes and welding parameters. The adaptability of the welding parameters  
700 accomplishes the generation of welding passes irrespective of the geometric characteristics of  
701 the V-groove geometry. As a result, the robotic weld path planning process is accelerated  
702 without the need to re-program and teach the path points in space for the welding torch to  
703 follow.

704 The integrated cost function concept introduces the flexibility in the automation of different  
705 welding parameters per layer as happens in manual welding. All the alternative ways that a V-  
706 groove geometry can be welded, based on the stored welding configurations on vector  $\tilde{W}$  are  
707 investigated, resulting in comparisons and savings between different approaches, always based  
708 on the operator's business plan. In this way, planning of resources can be perceived, predicting  
709 the overall welding procedure, and instantly deploying robotic welding between different V-  
710 groove joints. In practice, the developed system can potentially reduce welding direct costs by  
711 minimizing the combination of the number of passes, arc time and filler consumable material  
712 through the assigned cost function. For example, in the trial of sample S2, the arc welding time  
713 and amount of filler wire were found to be 32.9% and 26.18% lower, respectively, than the  
714 worst-case available welding parameter combination. Since an operator does not decide for  
715 welding parameters, the cost function always satisfies the optimum result. As a result, a  
716 decrease of costs from the worst feasible way to weld the joint is achieved. Nonetheless,  
717 indirect costs by utilizing welders in other tasks at the same time and reduced overwork from  
718 induced defects can further decrease the manufacturing costs.

719 Experimental results validate the welding framework utilizing different V-groove geometries  
720 of two types of steel grade. The proposed solution for each joint is examined under the actual  
721 welding result. Based on the proposed sequence of welding parameters which minimized the  
722 allocated cost function along with the respective robotic welding path, fusion of the beads with  
723 parent metal is achieved, proving the feasibility of each solution. The need for additional cap  
724 passes is reported and formalized to conclude the automated multi-pass robotic welding  
725 framework. Moreover, the feasibility of the proposed work is enhanced when the structural  
726 integrity of the weldments is assessed using PAUT inspection. Lack of root penetration was  
727 reported, which may have been caused by uneven root face of the metal plates from the bevelling  
728 of the groove sides and misalignment during fitting. Other defects were not identified,  
729 demonstrating an excellent overall fusion of the parent metals under the deposited weld passes.

730 In summary, this paper introduces and presents a new automated weld parameter and pass  
731 deposition sequencing framework, which builds on the current state of the art, that enables  
732 automatic planning of multi-pass welding for single-sided V-groove geometries, through  
733 minimisation of a user defined novel cost-function for clear commercial and technical benefits.

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