USING ARTIFICIAL NEURAL NETWORK TO PREDICT THE FRACTURE PROPERTIES OF THE INTERFACIAL TRANSITION ZONE OF CONCRETE AT THE MESOSCALE

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Abstract

Concrete is a multi-phase heterogeneous material in which the interfacial transition zone (ITZ) between aggregates and mortar significantly affects the cracking behaviour of concrete, especially under tensile load. In this paper, the artificial neural network (ANN) method is applied in predicting the fracture properties of ITZ in concrete. To form the data pool for the training of the ANN, a large number of two-dimensional (2D) meso-scale fracture simulation of concrete under direct tensile load is conducted. Cohesive crack elements are used in simulating arbitrary cracking in the ITZ and mortar. After the verification of the trained ANN model, the tensile strength and fracture energy of the concrete ITZ are predicted by using the RILEM direct tensile test results, i.e., stress–displacement curve, as the input for the ANN. It has been found that, the trained ANN performs well in predicting the ITZ properties and the computed stress–displacement curve together with the optimized ITZ fracture parameters has a good agreement with that from the RILEM test results. The randomness of aggregates has little effect on the predicted ITZ tensile strength while it becomes slightly bigger on the predicted ITZ fracture energy. The tensile strength ratio of ITZ to mortar are calculated 0.38-0.47 and the fracture energy ratio of ITZ to mortar are 0.18-0.58. These inversely predicted fracture properties of concrete ITZ can be useful complementation to the existing dataset and 2D fracture simulation of concrete structures.

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1. Introduction

As the most widely used construction material worldwide, concrete has attracted considerable research interest in the past few decades particularly for improved sustainability, enhanced strength and prolonged service life. To better understand the concrete properties and develop new concretes [1-4] to satisfy the pressing demands from the changing environment, the meso-scale structure of concrete and their relationship with the exhibited engineering properties becomes a key. At the meso-scale, concrete is made of multi-phase material components and the interfacial transition zone (ITZ) between the aggregates and the (mortar) matrix is normally the weakest part in such a composite [5-7]. Therefore, the mechanical behaviour, especially the fracture properties, of the ITZ in concrete in important in predicting the concrete performance.

The size of fracture process zone (FPZ) during concrete cracking is not small enough for negligible so concrete is normally considered as a quasi-brittle material. Hillerborg et al. [8] proposed the cohesive crack model to characterize the behaviour of a finite-size FPZ, which has developed to become one of the most robust fracture models for concrete. There are two independent parameters in the cohesive law: the tensile strength and fracture energy. So far, lots of researches have been carried out to measure the strength and fracture energy of concrete by experiments [9, 10]. In particular, several methods including three-point bending test [11], compact tension test [12], wedge splitting test [13] and uniaxial tensile test [14], have been proposed to determine the strength and fracture energy for concrete. Amongst the proposed methods, the uniaxial tensile test is the direct and most accurate method for obtaining the stress–displacement (of notch) relation which represents the true uniaxial mechanical behaviour compared to others [9]. However, it should also be mentioned that, most experimental and theoretical work were focused on Mode I fracture while studies on Mode II fracture properties have not been very clearly understood yet. It is even questionable that Mode

55   II fracture energy obtained from the test is the real material property [15]. The argument is

56   related to the fact that creating a pure Mode II fracture for quasi-brittle materials in experiment

57   is extremely challenging [10].

58

59   Compared with other the aggregates and cement mortar, the fracture properties of ITZ are much

60   more difficult to be tested. Rao and Prasad [16] designed notched rock-mortar specimens by

61   casting fresh mortar on the rock surface and found that the tensile strength of interface between

62   the rock and mortar was $1/16 - 1/3.5$ times of that of mortar. Gu et al. [17, 18] tested the

63   bonding strength of the ITZ and found the bonding strength was about 50% of the tensile

64   strength of the mortar. Dong et al. [19] carried out the three-point bending test for a concrete-

65   rock beam with the interface located at the geometric centre; they obtained the tensile strength

66   and fracture energy of ITZ which were 1.37 MPa and 19.3 N/m, respectively. Meanwhile, the

67   ITZ properties are closely related to the processing and manufacturing of concrete including

68   mixing, transportation, compaction, etc. Moreover, by nano-indentation test, Xiao et al. [5]

69   obtained the elastic modulus and hardness of ITZ in concrete and found that the hardness value

70   for ITZ were about 80% - 85% of that for mortar. However, it should also be noted that the

71   nano-indentation results on ITZ properties are at different length scale to above mentioned

72   meso-scale ITZ tests and they may not be directly comparable.

73

74   In the past decade, some researchers proposed to model concrete arbitrary cracking by inserting

75   zero-thickness cohesive elements into the mesh of multi-phase concrete [6, 7, 20-26]. The

76   meso-scale modelling based on cohesive elements provides an effective approach to investigate

77   the toughening fracture mechanism of concrete cracking, such as aggregate bridging, void

78   formation, or microcrack shielding. Yang et al. [6, 21, 22] modelled concrete fracture under

79   the uniaxial tensile test in 2D as a heterogeneous material by inserting cohesive elements and

80   the heterogeneity was achieved by random aggregates distribution [6, 22] or random elements

81   properties [21]. Further, Ren et al. [7] obtained more realistic concrete meso-structures through

82   X-ray computed tomography scanning and carried out 2D uniaxial tensile simulations by the

83   imaged based mesh with cohesive elements. They found that the micro cracks were always

84   initiated at the ITZ before connected to form the macro cracks and the overall stress-

85   displacement relationship of concrete was mainly determined by ITZ fracture properties.

86   Recently, Ren et al. [27] and Trawiński et al. [26] established 3D numerical model using

87   cohesive elements based on X-CT scanning results of concrete specimen and modelled the

88   concrete cracking under direct uniaxial loading. Their researches revealed that 3D modelling

89   would be a very powerful tool to unveil the damage and failure mechanisms in a more realistic

90   way. However, 3D simulations for concrete fracture at meso-scale level, due to the highly

91   nonlinear equation system and the softening-induced instabilities, are very time-consuming

92   [26]. The limitation on computing efficiency brings great challenges in the widespread

93   application of 3D meso-scale fracture models especially when a large number of simulations

94   are necessary.

95

96   Trial and error is usually used to estimate the ITZ properties for application in the meso-scale

97   simulation of concrete cracking. However, this method cannot always yield accurate and

98   reliable results. Instead, inverse analysis method has been widely employed to determine the

99   mechanical parameters of materials and structures, such as rock creep parameter [28], residual

100   stress by wilding [29] and overall fracture properties of composites [28, 30, 31]. Recently the

101   application of artificial intelligence in civil engineering has proved powerful and has potential

102   to solve new problems. In light of the fracture properties of the concrete ITZ, given the

103   difficulties in the experimentation, an inverse method based on artificial neural network would

104   be a promising solution.

4

105

106   This paper aims to use the artificial neural network (ANN) in the prediction of the fracture

107   properties of ITZ in concrete. Concrete is considered as a heterogeneous material at the meso-

108   scale, consisting of polygonal aggregates, mortar and ITZ. A multi-phase fracture model

109   involving cohesive elements is established and the uniaxial direct tensile test from RILEM is

110   employed and reproduced in the finite element simulation. A large number of simulations are

111   conducted with prior known values of ITZ tensile strength and fracture energy to form the data

112   pool to train the ANN. After the training and validation of the ANN, the real ITZ tensile

113   strength and fracture energy are inversely attained, against the RILEM test results. A

114   parametric study focusing on some underlying factors that may influence the accuracy of the

115   ANN prediction on the fracture properties of ITZ in concrete is carried out.

116

117   **2.   Meso-scale fracture model for concrete**

118   A meso-scale structure for concrete is firstly developed by randomly generating and packing

119   aggregates. Although realistically aggregates should have rough edges, it is almost impossible

120   to mesh the aggregates with extremely irregular edges in finite element modelling [7, 17]. We

121   simplified the aggregate shape as the polygon with a random size and 4 to 13 sides. An

122   aggregate in a regular polygon (Figure 1a) is generated with random sides in 4 - 13 and a

123   random size in a specified grading range. To change the regular polygon to irregular one, the

124   vertex of the regular polygon will be randomly moved to/away from the centre and then rotated

125   between the adjacent vertices (Figure 1b and 1c).

126

127   Once the meso-structure of concrete is generated and meshed, cohesive elements are embedded

128   into the boundaries of the mesh. The ITZ and mortar matrix have cohesive elements inserted

129   to approximately simulate arbitrary cracking but the material properties of the cohesive

130   elements are defined separately for these two phases. The mechanical properties of aggregates

131   are considerably stronger than mortar and the ITZ excluding the ultra-high performance

132   concrete (UHPC). In this study, the fracture of aggregates is not simulated and the ITZ is

133   assumed as zero thickness interface. More details on the insertion process of cohesive elements

134   has been introduced in the authors' previous study [32]. Figure 2 shows the concrete model

135   consisting of solid elements for the aggregates and mortar, and cohesive elements in the mortar

136   and the interfaces. The mesh size is 1 mm for the worked example and we will discuss the mesh

137   dependency later.

138

139   Normally, a traction–separation law is used as the constitutive model for the zero-thickness

140   cohesive elements [7]. The calculation thickness for the cohesive elements is 1 so the element

141   strain is replaced by the relatively displacement of the crack face. The traction stress of

142   cohesive elements is a function of the corresponding relative displacements of the crack surface.

143   In general, the traction–separation laws for the cracks can be expressed as follows:

144
$$\sigma_n = f(\delta_n) \tag{1}$$

145
$$\sigma_s = f(\delta_s) \tag{2}$$

146   where σ_n and σ_s are the normal and shear traction stress, respectively. δ_n and δ_s are the

147   corresponding opening displacement and slipping displacement, respectively; f is the function

148   describing the traction and separation relationship.

149

150   For a cohesive crack, the traction stresses will linearly increase to the peak strength by a penalty

151   stiffness and then gradually decrease to zero. The traction–separation relationship for the

152   opening and shearing in the linearly elasticity stage can be expressed as follows:

153
$$\sigma_n = K_n < \delta_n > \tag{3}$$

154
$$\sigma_s = K_s \delta_s \tag{4}$$

155   where $<\ >$ is the Macaulay bracket which equals zero if the value of normal displacement is

156   smaller than zero (i.e., compression). The K_n and K_s are the penalty stiffness at the normal and

157   shear directions, respectively. Penalty stiffness is a numerical parameter to control the

158   deformation of the zero-thickness cohesive element.

159

160   Figure 3 illustrates the constitutive relationship for the cohesive crack with an exponential post-

161   peak softening behaviour. The area under the traction-separation curve is the corresponding

162   fracture energy. It should be mentioned that, the softening behaviour can be in a linear, bilinear

163   even any pre-defined shape. The damage initiation will occur when the critical displacement

164   satisfies the following equation:

165   $$\left(\frac{\sigma_n}{\sigma_n^0}\right)^2 + \left(\frac{\sigma_s}{\sigma_s^0}\right)^2 = 1 \tag{5}$$

166

167   where σ_n^0 and σ_s^0 are the tensile strength and shear strength of the cohesive crack, respectively.

168   It should be mentioned that the experimental data on the shear fracture properties are very

169   limited [7]. Although some researches considered the shear strength was larger than tensile

170   strength and proposed to use the ratio of shear strength to tensile strength to model concrete

171   cracking, the ratio was randomly assumed and not verified by experiments [20, 34]. Moreover,

172   there is even a doubt whether shear fracture energy is a material property [15, 20]. For uniaxial

173   direct tensile test, tensile fracture is the main failure type. As such, Mode I fracture properties

174   are considered as most significant parameters in the simulations and the parameters for Mode

175   II fracture are assumed to be the same as those for Mode I fracture according to existing studies

176   on tensile fracture modelling of meso-scale concrete [21, 24, 26, 35].

177

178   An effective displacement coupling normal and shear separation is proposed to calculate the

179   damage evolution:

$$\delta = \sqrt{<\delta_n>^2 + (\delta_s)^2} \tag{6}$$

181 where δ is the effective displacement.

182

183 Further, the damage value under the exponential damage curve can be calculated as follows

184 [24]:

$$D = 1 - (\frac{\delta_0}{\delta_m})\left\{1 - \frac{1 - \exp{(-\alpha(\frac{\delta_m - \delta_0}{\delta_f - \delta_0}))}}{1 - \exp{(-\alpha)}}\right\} \tag{7}$$

186 where δ_0 is the critical displacement when the stress reaches the peak strength (i.e., D=0); Due

187 to the same value of tensile and shear strength, the critical displacements for the pure tensile,

188 pure shear and mixed-mode cracking become the same (the inner circle in Figure 3). δ_m is the

189 maximum effective displacement during the loading history; δ_f is the completely failure

190 displacement which is the same for the pure tensile, pure shear and mixed-mode cracking (i.e.,

191 the outer circle in Figure 3). α is a softening parameter representing the damage evolution rate.

192

193 Thus, the post-peak traction stresses can be expressed as follows:

$$\sigma_n = (1 - D)K_n < \delta_n > \tag{8}$$

$$\sigma_s = (1 - D)K_s\delta_s \tag{9}$$

196 It should be mentioned that, D is the stiffness damage value while not the strength damage

197 value. Once the cohesive strength σ_0, failure displacement δ_f and the softening parameter α

198 are determined, the fracture energy (i.e., the area under the softening curve) can be obtained as

199 follows:

$$G_f = \int_0^{\delta_f} f(\delta)\,\delta \tag{10}$$

201 For quasi-static simulations by implicit analysis programs, a small value of viscosity can be

202 introduced to help convergence, making the stiffness matrix positive definite. The viscosity

203   regularizes the constitutive relationship of the cohesive element by modifying the damage

204   value D to D_v as follows:

205 $$\dot{D}_v = (D - D_v)/\mu \tag{11}$$

206   where D_v is the viscous damage variable for regularization of the constitutive equations. $\dot{D}_v$ is

207   the derivative of viscous stiffness degradation variable with respect to time; μ is the viscosity

208   parameter which should be sufficiently small to improve the rate of convergence without

209   compromising results. When viscosity is introduced to the model, D is not applicable any more

210   while D_v becomes effective. The material stiffness matrix is then modified.

211

212 **3.   Direct tensile test on fracture properties of concrete**

213   RILEM [11, 14] recommended a closed-loop uniaxial tensile test method to obtain the stress–

214   displacement relationship which describes the overall fracture behaviour for concrete. The

215   experimental data on RILEM round-robin tests [11, 14] is used to validate the developed

216   numerical method and the starting point for the inverse analysis. In the round-robin tests, the

217   mix proportion by weight for concrete was 1:2:2.5:0.56 in terms of cement, fine aggregate,

218   coarse aggregate and water respectively. In addition, 10 mm single-sized coarse aggregates

219   were used. The coarse aggregates were defined as aggregates with size larger than 2.36 mm

220   according to British Standard 882 [36]. To reduce the complexity of the mesh, only coarse

221   aggregates larger than 2.36 mm are modelled in this study, while fine aggregates and cement

222   are treated as mortar phase [22]. The total area fraction of coarse aggregates can be calculated

223   by the weight mix proportion and materials densities as follows:

224 $$P_a = \frac{P_w/\rho_{agg}}{\rho_{con}} \tag{12}$$

225   where P_a is the area/mass percentage of the coarse aggregates in the total. P_w is the percentage

226   by weight of the coarse aggregates in the total, which is about 0.41 according to the mix

227 proportion by weight in their experiments [11, 14]. ρ_{agg} and ρ_{con} are the density of the coarse

228 aggregate (limestone) and the normal concrete, respectively. The values of density for

229 limestone and normal concrete are about 2400 kg/m^3 and 2700 kg/m^3, respectively [37]. The

230 calculated area fraction of the coarse aggregates is about 36.7% by Equation (12). More details

231 on the experiments can be found in the references [11, 14].

232

233 A 2D concrete model with the same size of the experimental sample is developed. The model

234 dimensions are 100 mm×150 mm and two notches are created with width 2 mm and depth 10

235 mm in the middle of the model. Figure 2 shows the typical mesh with element size 1 mm. Table

236 2 lists the values for the geometric and mechanical parameters and their sources. Yang et al.

237 [7] have found that the interfacial cohesive strength and fracture energy are the dominant

238 factors governing the fracture process of concrete. Rao et al. [38] investigated the relationship

239 between the mortar splitting tensile strength and the water/cement ratio and generalized the

240 Abrams' law for predicting the tensile strength of mortar. In Rao's experiments, the mortar

241 tensile strength changes from 1.76 to 2.66 MPa when the water/cement ratio decreases from

242 0.65 to 0.3. According to Abrams' generalization law, the mortar strength for the water/cement

243 ratio 0.56 was estimated as 2.2 MPa [38]. Further, the fracture energy of the mortar was

244 predicted as 72N/m according to Rao's experimental data on mortar fracture energy [16].

245 Moreover, a parametric study of a realistic range of tensile strength and fracture energy of

246 mortar on the fracture behaviour of the concrete sample in this research will be carried out. The

247 damage evolution rate parameter α is obtained by fitting the Equations (7) and (8) with RILEM

248 data [11, 14]. The tensile strength and fracture energy of ITZ are regarded as targets which will

249 be inversely determined. The effects of mortar strength and fracture energy on the inverse

250 analysis will be investigated by parametric studies later.

251

252   The top and bottom surfaces of the specimen for experiments were tied to the loading plates

253   by stiff glue [11]. For the direct uniaxial tension modelling, the frictional and rotational effects

254   were considered minor and the tensile displacements (y direction) were directly applied to top

255   and bottom nodes. The average stress of the model is obtained by dividing the reaction forces

256   by the net cross section area. The crack width w is obtained from the average value of the

257   separating displacements of the two notches.

258

259   **4.   Establishing the artificial neural network and the inverse analysis**

260   The artificial neural network (ANN) has been widely employed for learning, predictions and

261   making decisions based on data. There are three basic datasets for the ANN model: training,

262   testing and validation datasets. First, training dataset is used to fit the model. Then testing

263   dataset is used to provide an unbiased evaluation of a final model fit on the training dataset.

264   The validation is to evaluate a given model by a dataset [39]. The inverse analysis method

265   based on ANN for determining the ITZ fracture properties of concrete is as follows: First, a

266   known solution for the overall fracture behaviour (i.e., the whole stress-crack width

267   relationship) should be obtained with a high reliability and accuracy. Then, a meso-scale

268   concrete model consisting of aggregates, mortar and ITZ should be developed. This model is

269   able to obtain the overall structural performance and the whole stress-crack width curve of the

270   concrete by assigning different material properties to different phrases. We select the tensile

271   strength and fracture energy of ITZ as the target variables and the other material parameters

272   are treated as constants. Numerical simulations with a number of initial values for the tensile

273   strength and fracture properties of ITZ are conducted. Accordingly, the stress-crack width

274   curves from the simulations can be obtained. For establish the ANN, the initial values for the

275   tensile strength and fracture energy of ITZ are used as input data and the stress-crack width

276   curves from the corresponding simulations are output data. These input and output data are

11

277   randomly divided into training, testing and validation dataset. Then an objective function for

278   calculating the error between the computed outputs and experimental stress-crack width curve

279   is created in the ANN. For a given output value (i.e., the overall stress-crack width curve), an

280   optimization algorithm is used to find optimized ITZ values which make the objective function

281   minimum. Further, the computed stress-crack width curve with optimized values will be

282   compared with experimental results. Then, the error between the numerical and experimental

283   results are calculated. If the error falls below a threshold value, i.e., negligibly small, the ITZ

284   values are determined and the inverse analysis processes are accomplished. If the error is over

285   the threshold value, the current numerical results will be added to re-train the network and

286   inverse the targeted ITZ fracture properties. However, it is likely that the errors cannot be

287   reduced even after lots of iterations. In this case, the retraining and inverse analysis will be

288   forced to quit and the ITZ properties will be determined by the final inverse analysis with the

289   corresponding error. The maximum iterations for retraining is set as 10 in this study.

290

291   RILEM uniaxial direct tensile test [14] obtained the whole stress-crack width curve of concrete

292   which is chosen as the known solution. The developed meso-scale fracture model for concrete

293   is used to generate the input and output data for establishing the ANN. The uniform design

294   which uniformly scatters the design points in the domain range is employed for choosing the

295   initial values for the ITZ tensile strength and failure displacement. Figure 4 illustrates the 20

296   sets of input values for ITZ fracture properties according to the previous studies on ITZ

297   properties [5, 16-19]. The initial ITZ values and their corresponding stress-crack width curves

298   from simulations are then used as the ANN training, testing and validation input and output

299   data, respectively. The ANN is established in Matlab and the output for the stress-crack width

300   curve is read by a Matlab open-source application [40]. It should be mentioned that, the stress-

301   crack width curves from simulations and experiments are represented by 40 discrete points

302   which are linearly spaced to train the ANN. Figure 5 shows the computed stress-crack width

303   curves. An objective function considering both the errors of peak point and all the 40 points at

304   the stress-crack width curve is designed as follows:

305    $$\text{Fit} = \min \sum_{i=1}^{40} \left\{ \frac{[\max(y_i) - \max(x_i)]^2}{[\max(x_i)]^2} + \frac{(y_i - x_i)^2}{[\text{sum}(x_i)]^2} \right\} \qquad (13)$$

306   where y_i and x_i are the stresses for the ith point from the network and the experiment,

307   respectively; The $\max(y_i)$ and $\max(x_i)$ are the maximum stresses (i.e., tensile strength) from the

308   network and the experiment, respectively.

309

310   Back-propagation (BP) algorithm is used to train the network. In this method, the error

311   calculated at the output of the network is propagated back through the layers of neurons to

312   update the weights [39]. The network contains 8 hidden layers and the account for training,

313   validation and testing dataset 80%, 10% and 10%, respectively. Figure 6(a)-(d) show the linear

314   regression of network outputs with respect to targets for training, validation, testing and all sets.

315   The targets are the values of simulated stress at the 40 points from simulations while the outputs

316   are the values of stress at the 40 points predicted from the network. The R values for all the

317   datasets are larger than 0.99, which means the fit is very good and the output tracks the targets

318   very well for all datasets. Figure 7 shows the variations of Mean Squared Error of the outputs

319   for the learning and testing sets plotted against different number of epochs. The error quickly

320   decreases to smaller than 0.001 with epochs increasing and the errors of testing and validation

321   sets have similar characteristics. Moreover, overfitting does not occur because neither testing

322   nor validation error increased before epoch 32. Therefore, the established ANN can well predict

323   the target variables.

324

325   The optimized tensile strength and fracture energy for concrete ITZ are 1.02 MPa and 28.9

326   N/m, respectively. Figure 8 shows the stress-crack width curves from both the numerical model

327 with the optimized ITZ fracture properties and the RILEM experiment [14]. The computed

328 stress-crack width curve has a good agreement with that from RILEM experiment. The error

329 between the two curves by Equation (13) is 1.8%. Therefore, the ITZ tensile strength and

330 fracture energy can be well predicted by the ANN. The ratio of ITZ tensile strength to mortar

331 tensile strength is about 0.46 time and the fracture energy of ITZ is about 0.4 time of the fracture

332 energy of the mortar.

333

334 **5. Parametric study and discussion**

335 The aggregates in the heterogeneous concrete model are randomly generated and packed.

336 Therefore, the heterogeneity of concrete will affect the concrete cracking. Figure 9 illustrates

337 the effect of concrete heterogeneity on the stress-displacement curves by 10 random

338 heterogeneous models which use the same materials mechanical parameters including the

339 optimized ITZ fracture properties. It can be seen that, the stress-displacement curves are very

340 close at the linear increase stage before the peak-stress and have slight differences at the

341 softening stage. Although the stress-displacement curve has a reasonable repeatability, the

342 variabilities may affect the values of optimized ITZ fracture properties. Further, based on the

343 same 20 sets of initial values for simulations and the inverse method, the ITZ fracture properties

344 for each heterogeneous model are determined. Table 2 shows the values of the optimized ITZ

345 tensile strength, fracture energy, iteration number and error. It can be found that, the tensile

346 strength varies from 0.96-1.03 MPa and the fracture energy varies from 13.1-28.9 N/m for

347 different heterogeneous models. Figure 10 illustrates the stress-displacement curves from

348 RILEM experiment and the numerical simulations with optimized ITZ fracture properties. The

349 error between the stress-displacement curves from the experiment and numerical simulation

350 varies from 0.6% to 3.1%, which proves the numerical model and inverse analysis method are

351 reliable. The mean value and coefficient of variation for the ITZ tensile strength are 1.00 MPa

14

352 and 2.8%, respectively. Therefore, the determined ITZ tensile strength is about 0.46 time of

353 the mortar strength. The mean value and coefficient of variation for the fracture energy of ITZ

354 are 20.9 N/m and 27%, respectively. The ratio of the ITZ fracture energy to mortar fracture

355 energy is about 0.18-0.40 with a relatively high degree of variability. The values obtained for

356 ITZ will be useful in the meso-scale modelling of concrete fracture; however, it may be noted

357 that more cases should be included in the inverse analysis by considering a variety of material

358 composition and geometric configuration. It will then give a range of values for ITZ properties

359 and the possible correlation to some underlying parameters. Figure 11 shows the typical crack

360 patterns for three heterogeneous models. It can be found that, the macro cracks are formed at

361 the middle of the specimen and the interfaces dominate the crack path. It is interesting to find

362 that, two macro cracks occur for model 9 where the cracks propagate from two notches. Due

363 to the distributions of aggregates and driving effects of ITZ, the left crack propagates to the top

364 of the right notch. Although the post-peak stress has decreased to about zero, the two macro

365 cracks have not completely connected.

366

367 As introduced in Equation (11), the viscosity is a numerical parameter to overcome the

368 convergence problem. Parametric studies are carried out to investigate the effect of viscosity

369 on the stress-displacement curve and crack pattern. Figure 12 illustrates the stress-displacement

370 curves for the heterogeneous model 1 with the viscosity values 1.0×10^{-5}, 5.0×10^{-5} and 1.0×10^{-4}

371 ^{4}. It can be seen that, the smaller the viscosity is, the smaller the peak strength of concrete is.

372 A very small value of viscosity has little effect on the stress-displacement curve. However, the

373 increment steps for the simulations with the viscosity values 1.0×10^{-5}, 5.0×10^{-5} and 1.0×10^{-4}

374 are 1640, 624 and 432, respectively. The convergence can be significantly improved by a

375 relatively larger viscosity. Figure 13 shows the crack patterns of the heterogeneous model 1 for

376 different values of viscosity. It can be seen that, there is no difference in the crack patterns of

377 heterogeneous model 1 with the viscosity 1.0×10^{-5}, 5.0×10^{-5} and 1.0×10^{-4}. Therefore, the

378 viscosity in this study is determined as 5.0×10^{-5} for improving the convergence without

379 compromising results.

380

381 Although the mesh dependency has been reduced through replacing the strain by separation

382 displacement in the constitutive model of cohesive element, the crack patterns and overall

383 stress-displacement may also be mesh-dependent if the size ratio of fracture process zone to

384 cohesive element is not large enough. Figure 14 illustrates the stress-displacement curves for

385 the heterogeneous model 1 with element size 0.5 mm, 1 mm and 2 mm. It can be found that,

386 the stress-displacement curves are almost the same for the meshes with the three chosen

387 element sizes. The increment steps for the simulations with element size 0.5 mm, 1 mm and 2

388 mm are 3079, 624 and 764, respectively. Figure 15 shows the crack patterns for the

389 heterogeneous model 1 with the three element sizes. It can be seen that, the element size has

390 little effects on the crack patterns while the crack paths are slightly different for the three

391 element sizes. In consideration of calculation efficiency, the smaller the element size is, the

392 larger the degree of freedom of the mesh is and more CPUs time will be required for each

393 increment step. Therefore, the element size is set as 1 mm in this study.

394

395 It has been found that the ITZ fracture properties dominate the overall fracture of concrete for

396 uniaxial tensile tests [23, 27, 42]. However, it should be mentioned that the tensile strength and

397 fracture energy of the mortar in this study are estimated according to previous experiments [16,

398 38]. Therefore, the effects of mortar tensile strength and fracture energy on the inversed results

399 are investigated. The optimized values of tensile strength and fracture energy from the inverse

400 analysis of heterogeneous model 8 are listed in Table 3. It can be seen that, for the mortar

401 tensile strength varying from 1.9 to 2.5 MPa, the optimized ITZ tensile strength and fracture

16

402   energy change from 1.10-0.94 MPa and 31.9-22.5 N/m, respectively. The larger the mortar

403   strength is, the smaller the optimized ITZ tensile strength and fracture energy are. The mean

404   values of the optimized ITZ tensile strength and fracture energy are 1.05 MPa and 29.6 N/m,

405   respectively. In addition, the values for coefficient of variation of the optimized ITZ tensile

406   strength and fracture energy are 7.1% and 15.8%, respectively. Figure 16 shows the stress-

407   displacement curves from the inversed results with different mortar strengths and fracture

408   energies. It can be found that, the stress-displacement curves from the simulations have a good

409   agreement with that from experimental results. Figure 17 illustrates the crack pattern for the

410   heterogeneous model 8 with different mortar strengths and fracture energies. It can be seen that,

411   the crack patterns from the inversed results are almost the same.

412

413   **6.   Conclusions**

414   This paper proposed a method to inversely determine the ITZ fracture properties of concrete

415   based on meso-scale concrete fracture model and artificial neural network. A three-phase

416   concrete model containing aggregate, mortar and ITZ was developed and zero-thickness

417   cohesive elements were used to simulate the cracking in the mortar and ITZ. RILEM direct

418   uniaxial tensile test was employed as the worked example to demonstrate the inverse method

419   and the benchmark to inversely determine the ITZ properties. A number of simulations with

420   initial ITZ fracture properties were carried out to obtain the stress-displacement curves which

421   was used for training the artificial neutral network. Various factors have been considered in the

422   parametric study in confirming the robustness of the developed method. Specific conclusions

423   can be obtained as follows:

424   (1)   The developed fracture model can reproduce the cracking phenomena (i.e.,

425   micro cracks initiation, crack deflection, bridging etc.) of concrete at meso-scale. The

426   established artificial neural network showed a good performance in optimizing the fracture

427   properties of ITZ by minimizing the objective function. The computed stress-crack width curve

428   with the optimized tensile strength and fracture energy of ITZ has a good agreement with that

429   from the RILEM experiment. The proposed method is robust and reliable on determining the

430   tensile strength and fracture energy of ITZ once the mortar and aggregate properties are

431   obtained.

432   (2)   For 10 different heterogeneous models, the mean values and coefficients of

433   variance for ITZ tensile strength and fracture energy are 1.0 MPa and 2.8%, 20.9 N/m and 27%,

434   respectively. The randomness of aggregates has little effect on the optimized ITZ tensile

435   strength but slightly bigger effect on the optimized ITZ fracture energy.

436   (3)   The larger the tensile strength of mortar is, the smaller the optimized ITZ

437   strength and fracture energy are. However, in the ranges of mortar strength (1.9-2.5 MPa) and

438   fracture energy (60-92 N/m), the values for coefficient of variation of the optimized ITZ tensile

439   strength and fracture energy are 7.1% and 15.8%, respectively. The optimized ITZ results

440   would be reliable according to the estimations of mortar fracture properties.

441   (4)   The tensile strength ratio of ITZ to mortar are 0.38-0.47 and the fracture energy

442   ratio of ITZ to mortar are 0.18-0.58 according to the parametric study on aggregate randomness

443   and variety of mortar fracture properties. These ratios can well be used for meso-scale fracture

444   modelling of concrete. It should be noted, however, that these values were derived without the

445   consideration of more complex 3D mechanisms including aggregate distribution and the

446   heterogeneity out of the plane. Therefore, the accuracy of directly using these data in 3D meso-

447   scale fracture simulation of concrete is not verified.

448

449

456 **References**

457 [1] D. Fukuda, Y. Nara, Y. Kobayashi, M. Maruyama, M. Koketsu, D. Hayashi, H. Ogawa, K.
458 Kaneko, Investigation of self-sealing in high-strength and ultra-low-permeability concrete in
459 water using micro-focus X-ray CT, Cem. Concr. Res. 42(11) (2012) 1494-1500.
460 [2] D. Fan, S. Yang, Mechanical properties of C-S-H globules and interfaces by molecular
461 dynamics simulation, Constr. Build. Mater. 176 (2018) 573-582.
462 [3] M.B. Leite, P.J.M. Monteiro, Microstructural analysis of recycled concrete using X-ray
463 microtomography, Cem. Concr. Res. 81 (2016) 38-48.
464 [4] H. Zhang, Y.J. Huang, Z.J. Yang, S.L. Xu, X.W. Chen, A discrete-continuum coupled finite
465 element modelling approach for fibre reinforced concrete, Cem. Concr. Res. 106 (2018) 130-
466 143.
467 [5] J. Xiao, W. Li, D.J. Corr, S.P. Shah, Effects of interfacial transition zones on the stress–
468 strain behavior of modeled recycled aggregate concrete, Cem. Concr. Res. 52 (2013) 82-99.
469 [6] X. Wang, M. Zhang, A.P. Jivkov, Computational technology for analysis of 3D meso-
470 structure effects on damage and failure of concrete, Int. J. Solids. Struct. 80 (2016) 310-333.
471 [7] W. Ren, Z. Yang, R. Sharma, C. Zhang, P.J. Withers, Two-dimensional X-ray CT image
472 based meso-scale fracture modelling of concrete, Eng. Fract. Mech. 133 (2015) 24-39.
473 [8] A. Hillerborg, M. Modeer, P.E. Petersson, Analysis of crack formation and crack growth in
474 concrete by means of fracture mechanics and finite elements, Cem. Concr. Res. 6(6) (1976)
475 773-781.
476 [9] S. Khalilpour, E. BaniAsad, M. Dehestani, A review on concrete fracture energy and
477 effective parameters, Cem. Concr. Res. 120 (2019) 294-321.
478 [10] Q. Lin, S. Wang, P.Z. Pan, W.W. Ji, Y. Lu, Fracture initiation under pure shear revisited:
479 Remarks on the mode II fracture in quasi-brittle materials, Theor. Appl. Fract. Mech. 109
480 (2020).
481 [11] B.I.G. Barr, M.K. Lee, E.J. de Place Hansen, D. Dupont, E. Erdem, S. Schaerlaekens, B.
482 Schnütgen, H. Stang, L. Vandewalle, Round-robin analysis of the RILEM TC 162-TDF beam-
483 bending test: Part 1—Test method evaluation, Mater. Struct. 36(9) (2003) 609-620.
484 [12] A.N. Amirkhanian, D.W. Spring, J.R. Roesler, G.H. Paulino, Forward and Inverse
485 Analysis of Concrete Fracture Using the Disk-Shaped Compact Tension Test, J. Test. Eval.
486 44(1) (2016).
487 [13] E. Brühwiler, F.H. Wittmann, The wedge splitting test, a new method of performing stable
488 fracture mechanics tests, Eng. Fract. Mech. 35(1) (1990) 117-125.
489 [14] B.I.G. Barr, M.K. Lee, B. Barragán, D. Dupont, R. Gettu, J.F. Olesen, H. Stang, L.
490 Vandewalle, Round-robin analysis of the RILEM TC 162-TDF uni-axial tensile test: Part 1,
491 Mater. Struct. 36(4) (2003) 265-274.

492 [15] A. Carpinteri, S. Valente, G. Ferrara, G. Melchiorrl, Is mode II fracture energy a real
493 material property?, Comput. Struct. 48(3) (1993) 397-413.
494 [16] G.A. Rao, B.K. Raghu Prasad, Influence of type of aggregate and surface roughness on
495 the interface fracture properties, Mater. Struct. 37(5) (2004) 328-334.
496 [17] L. Hong, X. Gu, F. Lin, Influence of aggregate surface roughness on mechanical properties
497 of interface and concrete, Constr. Build. Mater. 65 (2014) 338-349.
498 [18] X. Gu, L. Hong, Z. Wang, F. Lin, Experimental study and application of mechanical
499 properties for the interface between cobblestone aggregate and mortar in concrete, Constr.
500 Build. Mater. 46 (2013) 156-166.
501 [19] W. Dong, Z. Wu, X. Zhou, N. Wang, G. Kastiukas, An experimental study on crack
502 propagation at rock-concrete interface using digital image correlation technique, Eng. Fract.
503 Mech. 171 (2017) 50-63.
504 [20] Z. Yang, X. Frank Xu, A heterogeneous cohesive model for quasi-brittle materials
505 considering spatially varying random fracture properties, Comput. Method. Appl. M. 197(45-
506 48) (2008) 4027-4039.
507 [21] Z.J. Yang, X.T. Su, J.F. Chen, G.H. Liu, Monte Carlo simulation of complex cohesive
508 fracture in random heterogeneous quasi-brittle materials, Int. J. Solids. Struct. 46(17) (2009)
509 3222-3234.
510 [22] X. Wang, Z. Yang, A.P. Jivkov, Monte Carlo simulations of mesoscale fracture of concrete
511 with random aggregates and pores: a size effect study, Constr. Build. Mater. 80 (2015) 262-
512 272.
513 [23] X.F. Wang, Z.J. Yang, J.R. Yates, A.P. Jivkov, C. Zhang, Monte Carlo simulations of
514 mesoscale fracture modelling of concrete with random aggregates and pores, Constr. Build.
515 Mater. 75 (2015) 35-45.
516 [24] W. Trawiński, J. Bobiński, J. Tejchman, Two-dimensional simulations of concrete
517 fracture at aggregate level with cohesive elements based on X-ray μCT images, Eng. Fract.
518 Mech. 168 (2016) 204-226.
519 [25] A. Tabiei, W. Zhang, Cohesive element approach for dynamic crack propagation:
520 Artificial compliance and mesh dependency, Eng. Fract. Mech. 180 (2017) 23-42.
521 [26] W. Trawiński, J. Tejchman, J. Bobiński, A three-dimensional meso-scale modelling of
522 concrete fracture, based on cohesive elements and X-ray μCT images, Eng. Fract. Mech. 189
523 (2018) 27-50.
524 [27] W. Ren, Z. Yang, R. Sharma, S.A. McDonald, P.M. Mummery, Three-Dimensional In
525 Situ XCT Characterisation and FE Modelling of Cracking in Concrete, Complexity 2018 (2018)
526 1-11.
527 [28] L. Yang, Z.D. Li, Inverse Analysis of Rock Creep Model Parameters Based on Improved
528 Simulated Annealing Differential Evolution Algorithm, Geotech. Geol. Eng. 37(2) (2019) 639-
529 649.
530 [29] Y.P. Cao, N. Hu, Z.H. Yao, H. Fukunaga, An Inverse Approach for Constructing the
531 Residual Stress Caused by Welding, in: M. Tanaka, G.S. Dulikravich (Eds.), Inverse Problems
532 in Engineering Mechanics III, Elsevier Science Ltd, Oxford, 2002, pp. 201-208.
533 [30] B. Shen, G.H. Paulino, Identification of cohesive zone model and elastic parameters of
534 fiber-reinforced cementitious composites using digital image correlation and a hybrid inverse
535 technique, Cem. Concr. Compos. 33(5) (2011) 572-585.
536 [31] B.C. Hill, O. Giraldo-Londoño, G.H. Paulino, W.G. Buttlar, Inverse Estimation of
537 Cohesive Fracture Properties of Asphalt Mixtures Using an Optimization Approach, Exp.
538 Mech. 57(4) (2017) 637-648.
539 [32] S. Yang, X. Xi, K. Li, C.Q. Li, Numerical Modeling of Nonuniform Corrosion-Induced
540 Concrete Crack Width, J. Struct. Eng. 144(8) (2018) 04018120.

541 [33] S.T. Yang, K.F. Li, C.Q. Li, Numerical determination of concrete crack width for
542 corrosion-affected concrete structures, Comput. Struct. 207 (2018) 75-82.
543 [34] X. Xi, S. Yang, C.Q. Li, M. Cai, X. Hu, Z.K. Shipton, Meso-scale mixed-mode fracture
544 modelling of reinforced concrete structures subjected to non-uniform corrosion, Eng. Fract.
545 Mech. 199 (2018) 114-130.
546 [35] P. Grassl, M. Jirásek, Meso-scale approach to modelling the fracture process zone of
547 concrete subjected to uniaxial tension, Int. J. Solids. Struct. 47(7-8) (2010) 957-968.
548 [36] B.S. Institution, Specification for Aggregates from Natural Sources for Concrete, London,
549 1992.
550 [37] A. 211.1-91, Standard Practice for Selecting Proportions for Normal, Heavyweight, and
551 Mass Concrete, 2009.
552 [38] G.A. Rao, Generalization of Abrams' law for cement mortars, Cem. Concr. Res. 31(3)
553 (2001) 495-502.
554 [39] R. S., N. P., Artificial Intelligence: A Modern Approach (3rd Edition), Prentice Hall2009.
555 [40] G. Papazafeiropoulos, M. Muñiz-Calvente, E. Martínez-Pañeda, Abaqus2Matlab: A
556 suitable tool for finite element post-processing, Adv. Eng. Software 105 (2017) 9-16.
557 [41] W. Dong, D. Yang, X. Zhou, G. Kastiukas, B. Zhang, Experimental and numerical
558 investigations on fracture process zone of rock-concrete interface, Fatig. Fract. Eng. Mater.
559 Struct. 40(5) (2017) 820-835.
560 [42] P. Zhang, X. Hu, S. Yang, W. Yao, Modelling progressive failure in multi-phase materials
561 using a phase field method, Eng. Fract. Mech. 209 (2019) 105-124.
562 [43] H. Gercek, Poisson's ratio values for rocks, Int. J. Rock Mech. Min. Sci. 44(1) (2007) 1-
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564

565 **LIST OF TABLES**

569

570   Table 1 Mechanical parameters for different material phases of concrete

Description	Symbol	Values
Young's modulus of aggregate	E_{Agg}	80 GPa [24]
Young's modulus of mortar	E_{Mor}	23 GPa [24]
Poisson's ratio of aggregate	v_{Agg}	0.16 [43]
Poisson's ratio of mortar	v_{Mor}	0.22 [24]
Tensile strength of mortar	σ_{Mor}	2.2 MPa [16, 38]
Fracture energy of mortar	G_{Mor}	72 N/m [16, 38]
Failure displacement of mortar	$\delta_{\text{f,Mor}}$	0.23 mm
Evolution rate parameter	α	7 [11]
Tensile strength of ITZ	σ_{ITZ}	0.55 MPa
Fracture energy of ITZ	G_{ITZ}	11 N/m
Failure displacement of ITZ	$\delta_{\text{f,ITZ}}$	0.14 mm

571

572

573   Table 2 Optimized ITZ fracture properties for different heterogeneous models

Random heterogeneous model	Tensile strength (MPa)	Fracture energy (N/m)	Strength ratio of ITZ to mortar	Fracture energy ratio of ITZ to mortar	Error
1	1.02	28.9	0.46	0.40	1.8%
2	0.98	18.7	0.45	0.26	0.8%
3	0.96	17.1	0.44	0.24	2.9%
4	1.01	21.2	0.46	0.29	1.8%
5	1.01	15.9	0.46	0.22	3.1%
6	1.03	24.1	0.47	0.33	2.6%
7	1.01	26.3	0.46	0.37	1.2%
8	1.03	28.1	0.47	0.39	0.6%
9	0.96	13.1	0.44	0.18	0.7%
10	0.97	15.7	0.44	0.22	1.9%
Mean	1.00	20.9			
CoV	2.8%	27%			

574

575

576   Table 3 Optimized ITZ fracture properties for different values of mortar strength and fracture

577   energy

Mortar Strength	Mortar fracture energy	ITZ Tensile strength	ITZ fracture energy	Strength ratio of ITZ to mortar	Fracture energy ratio of ITZ to mortar	Error
1.9 MPa	72 N/m	1.11 MPa	31.9 N/m	0.58	0.44	1.3%
2.2 MPa	72 N/m	1.03 MPa	28.1 N/m	0.47	0.39	0.6%
2.5 MPa	72 N/m	0.94 MPa	22.5 N/m	0.38	0.31	0.6%
2.2 MPa	60 N/m	1.06 MPa	35.0 N/m	0.48	0.58	3.6%
2.2 MPa	94 N/m	1.13 MPa	30.3 N/m	0.51	0.32	0.6%

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580

LIST OF FIGURES

603

| (a) | (b) | (c) |

Figure 1 Generation of the irregular polygon: (a) regular polygon; (b) moving vertex; (c) rotating vertex

Cohesive elements in the mortar

Cohesive elements in the ITZs
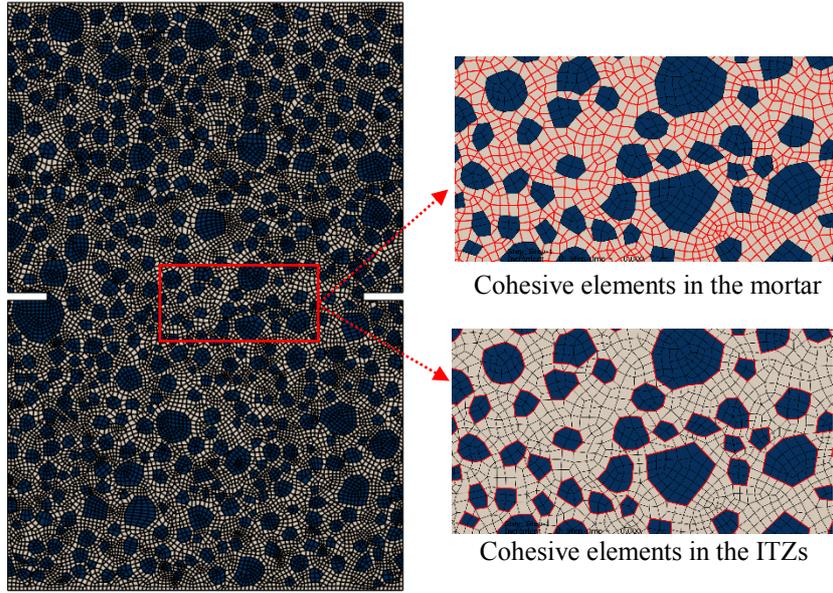
610

611   Figure 2 Meso-scale concrete model with cohesive elements

612

$$(\sigma_n)^2 + (\sigma_s)^2 = (\sigma^0)^2$$

K_p

δ_0 δ_0

δ_0

$\delta_{n,f}$

$\delta_{m,f}$

G_C

$\delta_{s,f}$

δ_s

δ_n
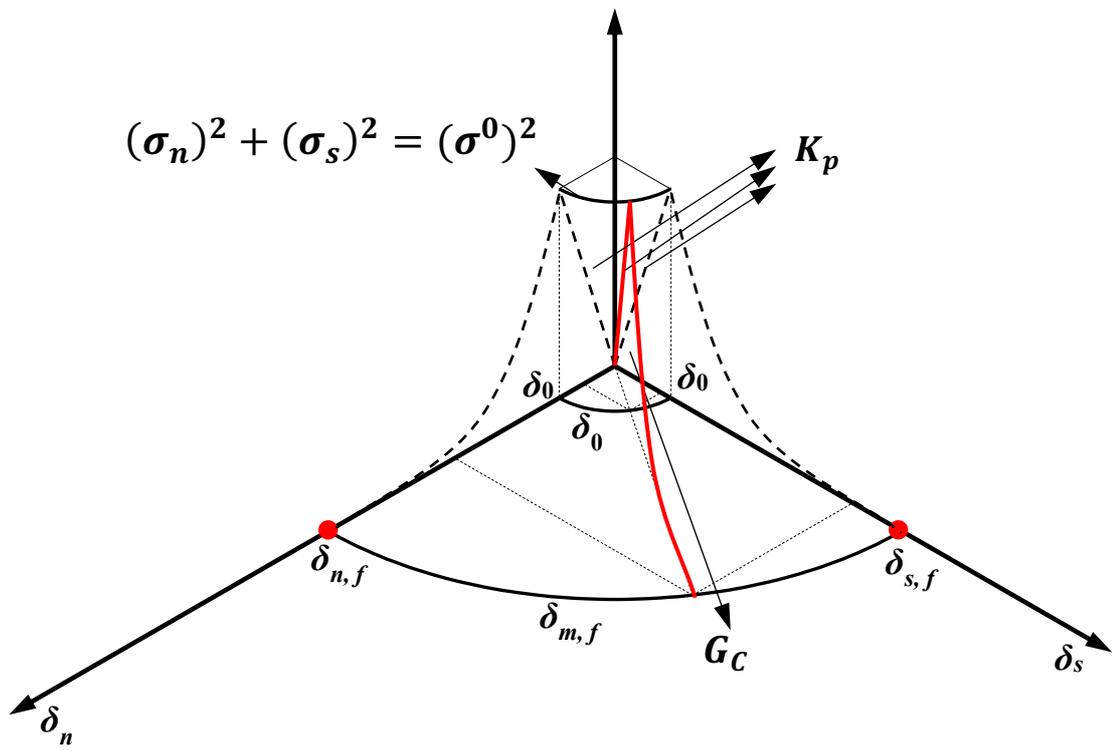
613

614   Figure 3 Stress-displacement relationship for the cohesive element

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616
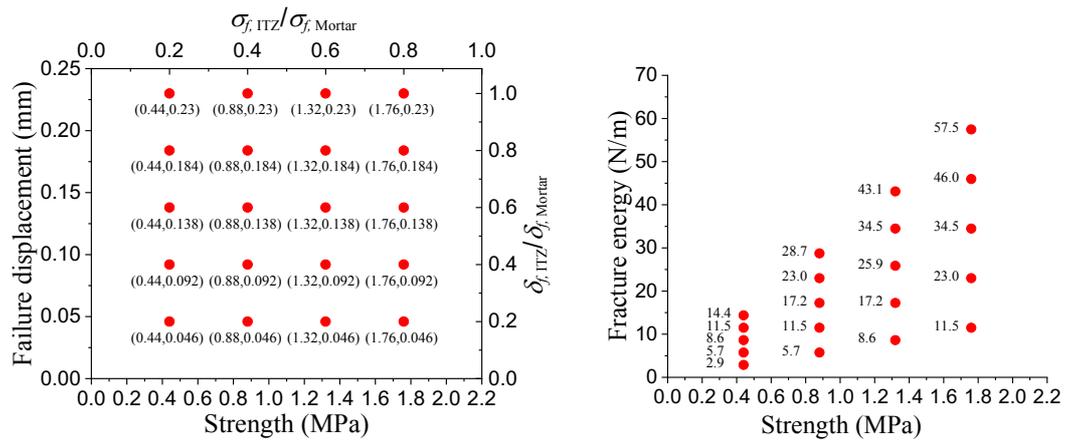
617

618   Figure 4 The initial values for ITZ fracture properties in the simulations for training (a) the
619   strength and failure displacement; (b) the corresponding values of fracture energy

620
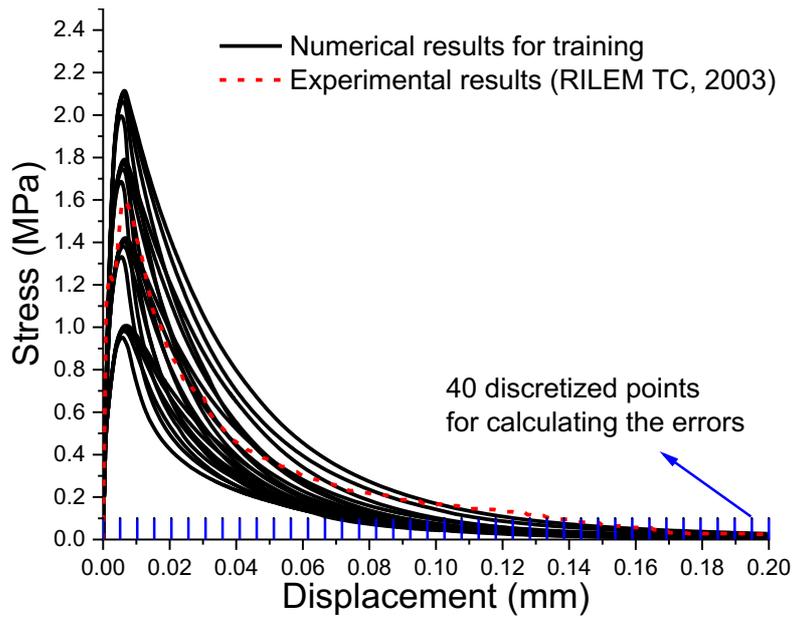
Figure 5 Stress-displacement curves for training neutral network
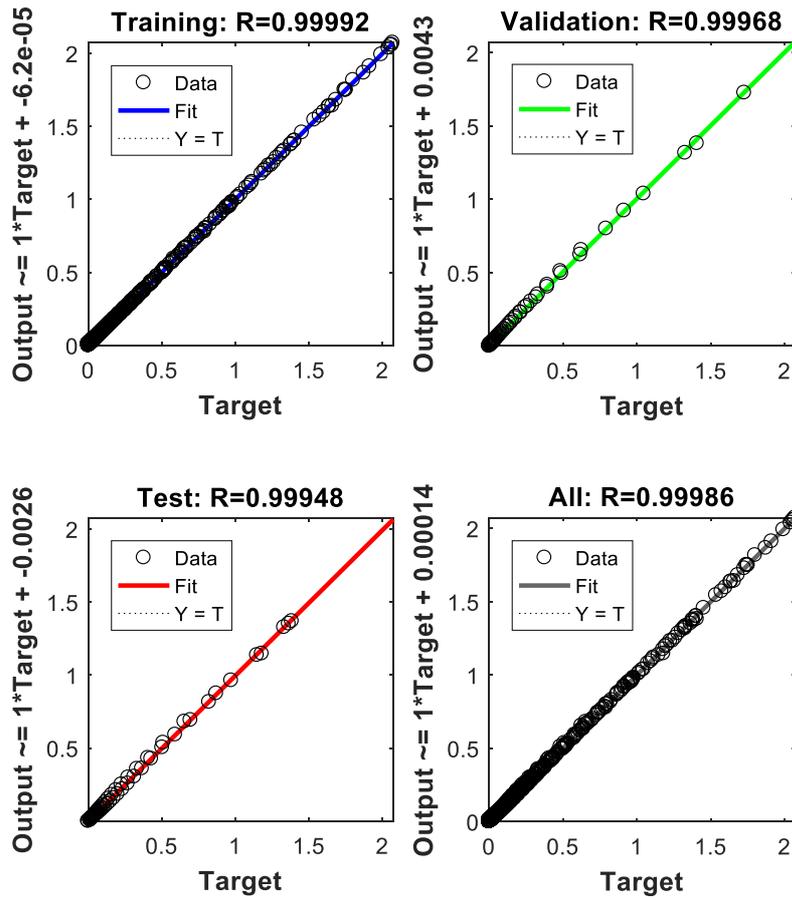
624

625   Figure 6 The regressions of network outputs with respect to targets for (a) training set; (b)
626   validation set; (c) test set; (d) all data

627

Best Validation Performance is 8.7309e-05 at epoch 32
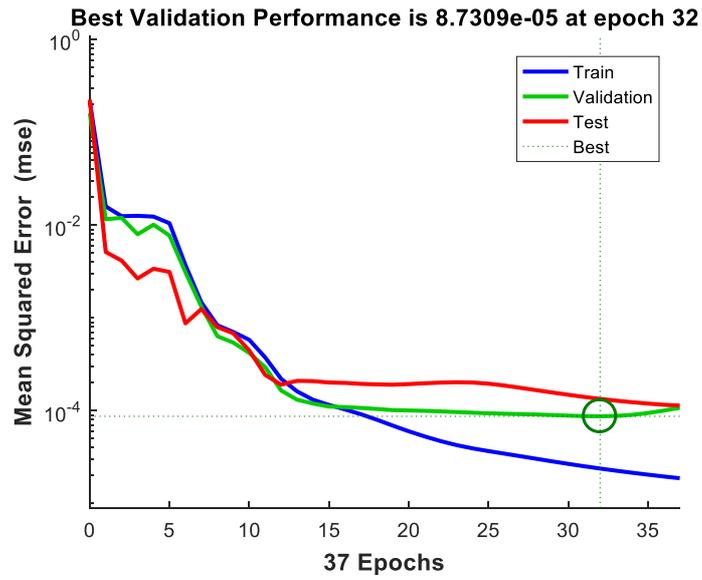
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629 Figure 7 Mean squared errors of the network data with the epoch increasing

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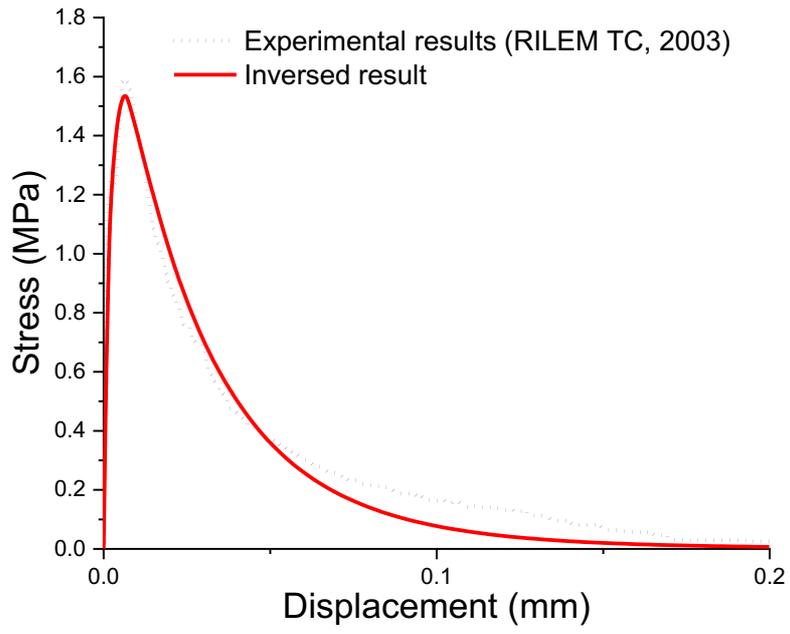
633

634   Figure 8 Stress-displacement curves from the experiment and numerical result with inversed
635   ITZ fracture properties

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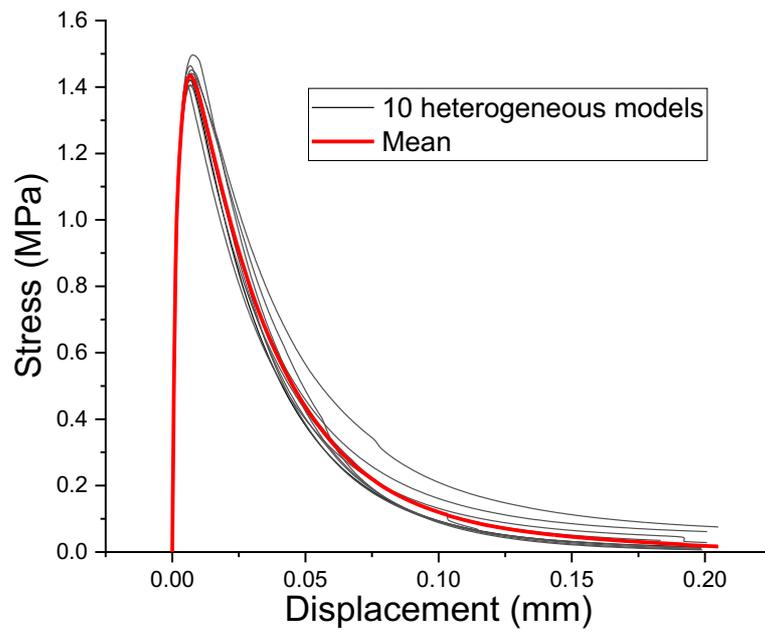
Figure 9 Effect of aggregate randomness on the stress-displacement curve

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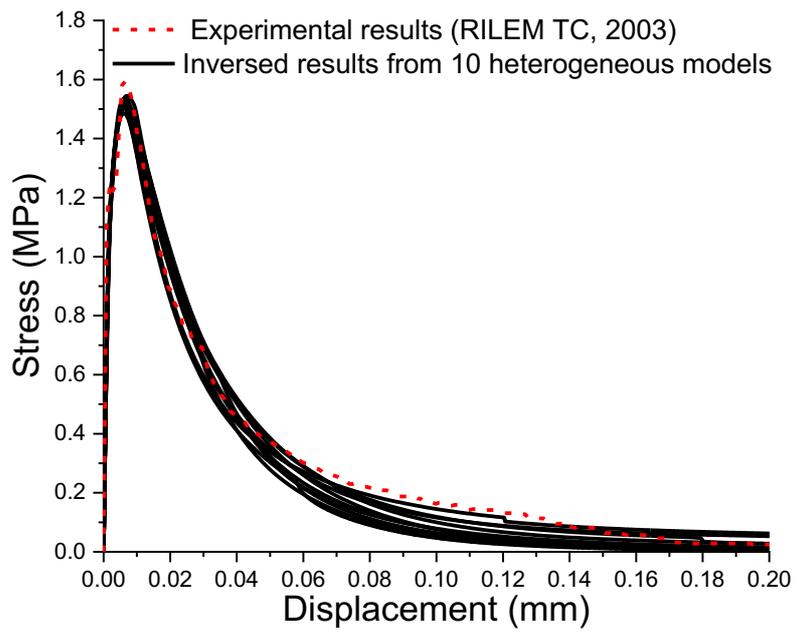
646   Figure 10 Stress-displacement curves from the experiment and inversed results for 10
647   heterogeneous models

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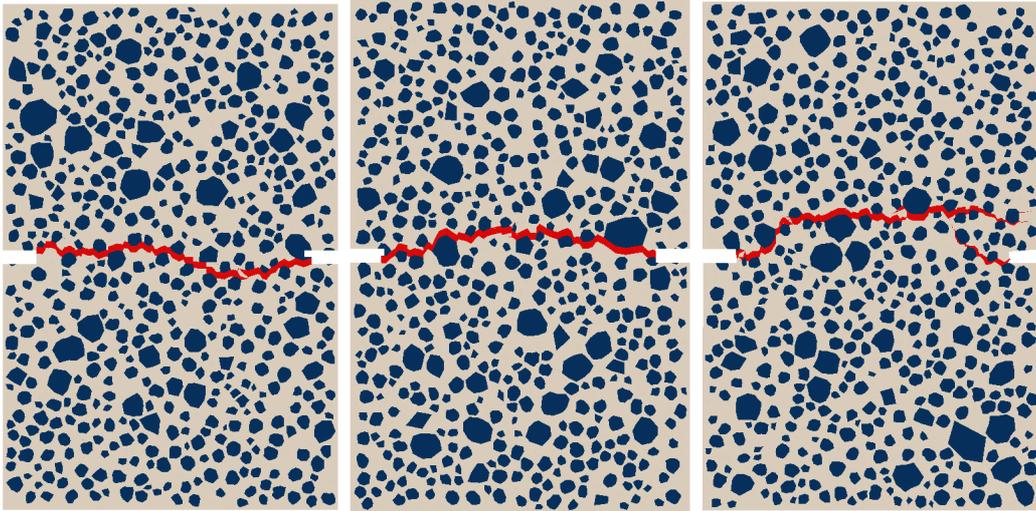
650 Figure 11 Typical crack patterns from the inversed results

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652
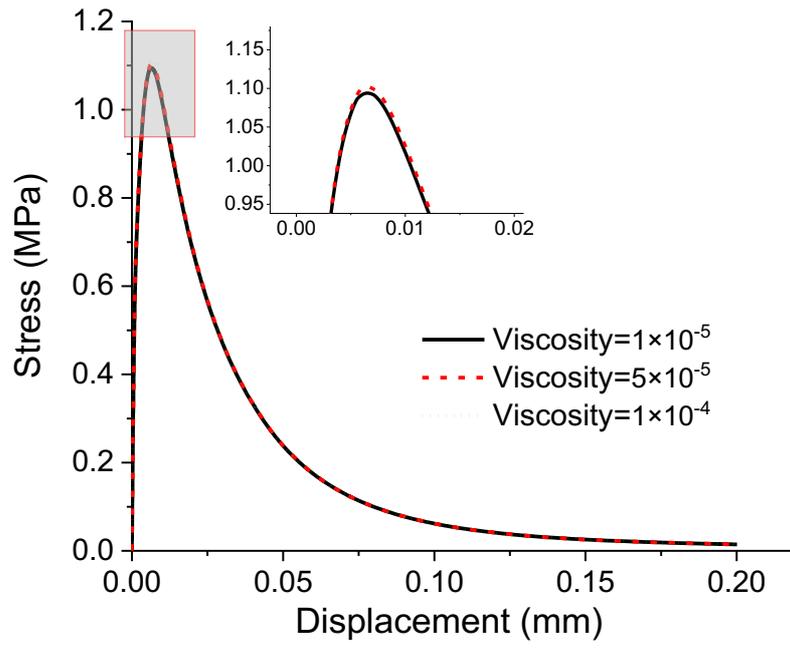
Figure 12 Effect of the viscosity on the stress-displacement curve of concrete

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654
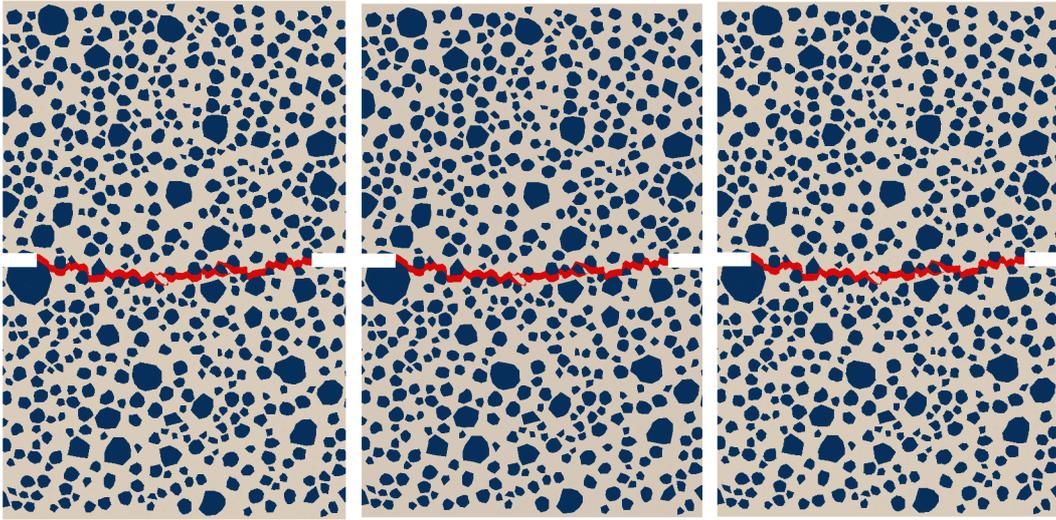
(a) viscosity=1.0×10^{-5} (b) viscosity=5.0×10^{-5} (c) viscosity=1.0×10^{-4}

Figure 13 Effect of the viscosity on the crack patterns of concrete
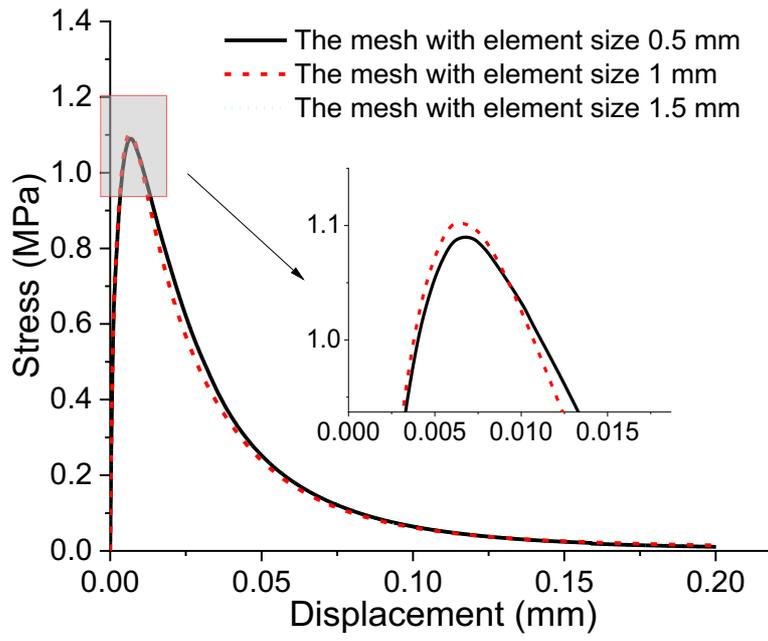
Figure 14 Effect of element size on the stress-displacement curve of concrete

(a) element size 0.5 mm   (b) element size 1 mm   (c) element size 1.5 mm
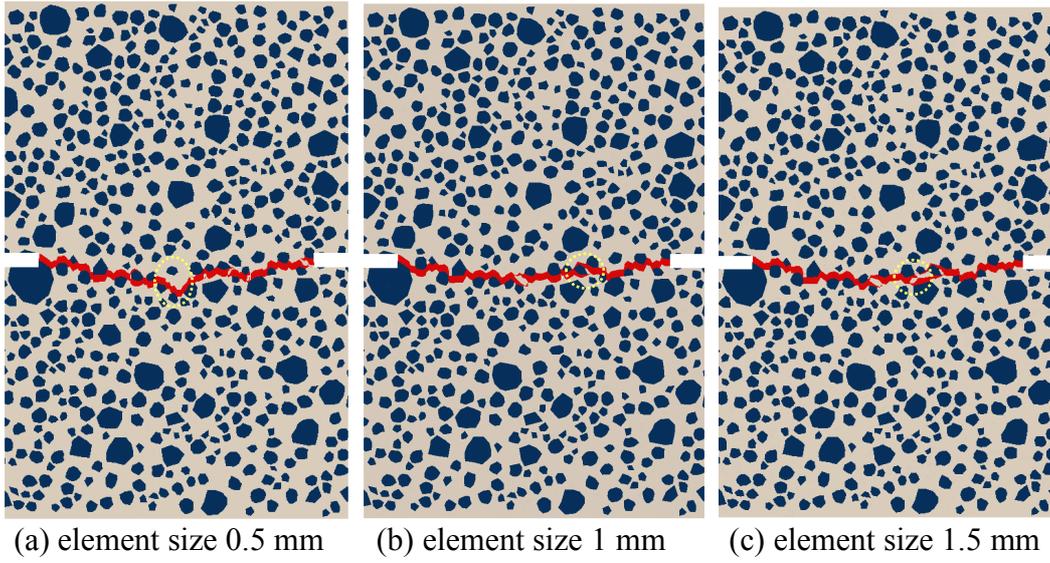
Figure 15 Effect of element size on the crack patterns of concrete

(a) Effect of mortar strength

(b) Effect of mortar fracture energy
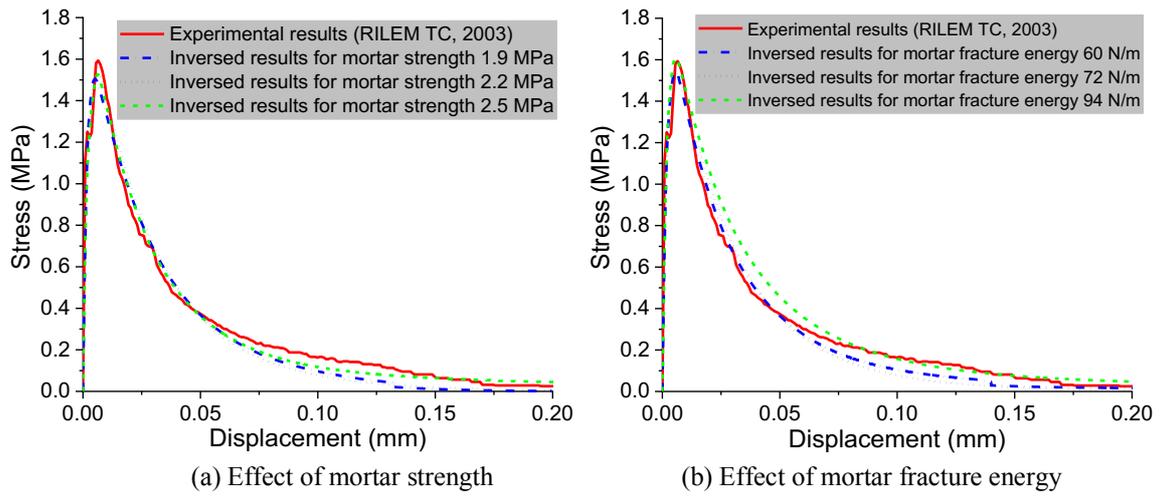
Figure 16 Stress-displacement curves from inversed results for different values of mortar fracture properties
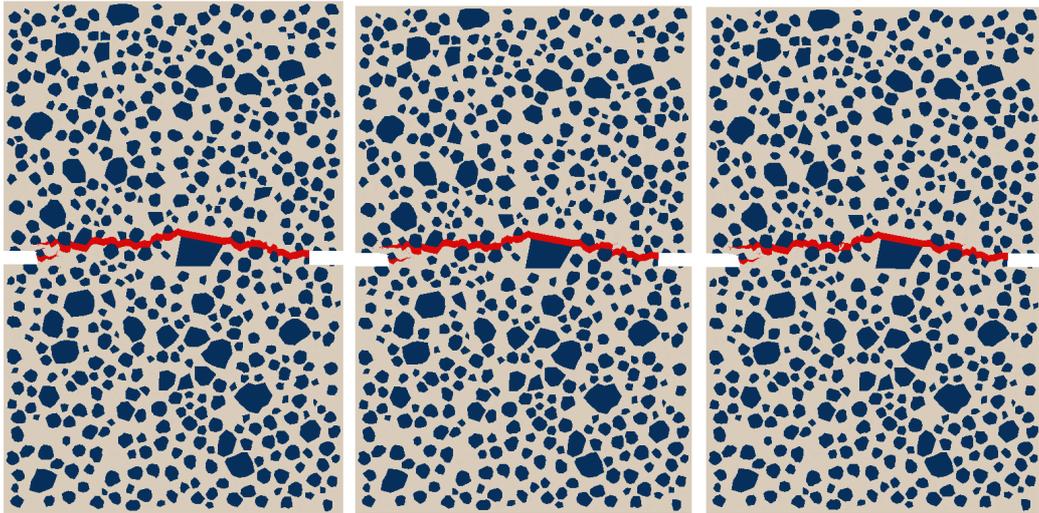
676
677   (a) σ_{Mor}=1.9 MPa, G_{Mor}=72 N/m (b) σ_{Mor} =2.2 MPa, G_{Mor}=72 N/m (c) σ_{Mor} =2.5 MPa, G_{Mor} =72 N/m
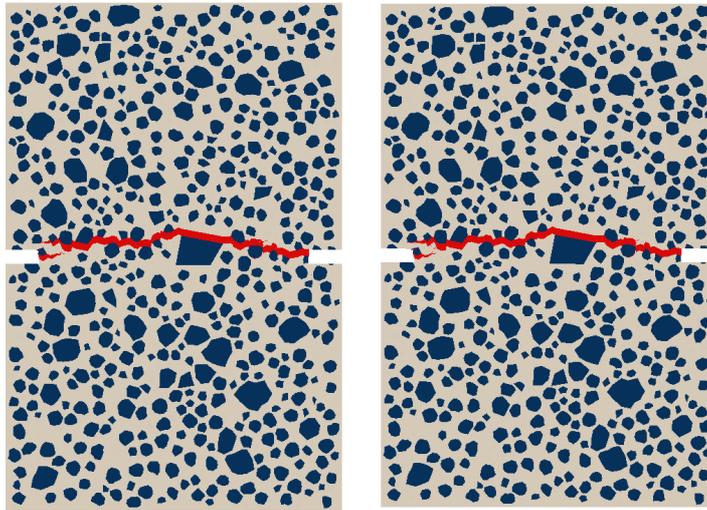
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679   (d) σ_{Mor}=2.2 MPa, G_{Mor}=60 N/m   (e) σ_{Mor}=2.2 MPa, G_{Mor}=94 N/m

680   Figure 17 Crack patterns of the inversed results for different values of mortar fracture
681   properties

682