# Analysis of Wide-Band Oscillation of Hybrid MMC Interfacing Weak AC Power System

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Abstract—The wide-band oscillation of the hybrid MMC induced by excessive power infeed under weak AC power system integration is analyzed in this paper. A closed-loop state-space-based time-domain small-signal model is firstly established to investigate the instability problem. Different from the findings in two-level VSCs or half-bridge MMCs, the root locus analysis and participation factor analysis in this paper reveals that the oscillation frequency and involved control loops are highly related to the operation status. When hybrid MMC operates as a rectifier, a low-frequency oscillation is observed with the d-channel control loop mainly participated. In contrast, a high-frequency oscillation occurs with a q-channel control loop mainly involved when the hybrid MMC operates as an inverter. This wide-band oscillation phenomenon is explored with the aid of two simplified loop-gain-based s-domain models, which are derived referring to the selective modal analysis approach. To suppress the oscillation, sensitivity analysis regarding the impact of parameters on the phase margin is conducted to recognize effective parameter adjustment methods. The analysis results are validated by detailed electromagnetic simulations.

Index Terms-Power system modeling, small-signal model, modular multilevel converter, weak AC system, HVDC transmission

#### Nomenclature

#### Subscripts

- · · · · · · · · · · · · · · · · · · ·	
<i>x</i> , <i>y</i>	axis of the rotating frame synchronized with
	AC system voltage
d, q	axis of the rotating frame synchronized with
	the measured PCC voltage by PLL

per unit ри

fil filtered signals before entering the controller

ref reference values for the controller

0 steady-state values

# **Variables**

$u_s$	AC system voltage
P	AC-side active power injected into MMCs
Q	reactive power absorbed by MMCs
$u_{dc}$	DC terminal voltage of MMCs
$i_{dc}$	DC output current of MMCs

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i	AC-side current of MMCs
$i_x$ , $i_y$ / $i_d$ , $i_q$	axis components of <i>i</i> under $xy / dq$ frame
$u_p$	PCC voltage
$u_{px}, u_{py}$	axis components of $u_p$ under $xy / dq$ frame
$u_{pd}$ , $u_{pq}$	
$i_p, i_n$	upper and lower arm current
$u_{c,avg}$	average capacitor voltage
$M_x$ , $M_y$ /	fundamental-frequency modulation signal in xy
$M_d$ , $M_q$	/ dq frame
$M_{x2}, M_{y2}/$	second harmonic modulation signal in xy / dq
$M_{d2}, M_{q2}$	frame
$M_{dc}$	DC modulation signal
$u_{px2}^{\Sigma}, u_{py2}^{\Sigma}$	second harmonic of the total capacitor voltage
px2, $py2$	in one phase arm under xy frame
$u_{px}^{\Sigma}, u_{py}^{\Sigma}$	fundamental-frequency component of total
px, $py$	capacitor voltage in one arm under xy frame
$u_{p0}^{\Sigma}$	DC component of the total capacitor voltage
$i_{\it diff}$	circulating current
$i_{diff0}$	DC component of $i_{diff}$
$i_{diffx2},i_{diffy2}$	second harmonic of $i_{diff}$ in $xy$ frame
$e_{v}$	AC-side internal output voltage of MMCs
$e_{dc}$	DC-side internal output voltage of MMCs
$x_P, x_Q, x_{Id}, x_{Iq}$	state variables in ACC outer and inner loop
$\chi_{Pdc}, \chi_{Idc}$	state variables in DCC outer and inner loop
$\theta$	PCC voltage phase angle

#### Parameters

1 arameters	
$R_s/L_s$	equivalent AC system resistance/inductance
$K_T$	turn-ratio of the AC transformer
$R_T/L_T$	AC transformer resistance/inductance
$C_{sub}$	capacitance of sub-modules in MMC
$L_{arm}/R_{arm}$	inductance and equivalent resistance per arm
$N_{sub}$	total number of sub-modules in one MMC arm
$K_{PO}/K_{PI}$	proportional gain for ACC outer/inner loop
$K_{IO}/K_{II}$	integral gain for ACC outer/inner loop
$L_{pu}$	feedforward gain for AC current in ACC
$K_{POdc}/K_{PIdc}$	proportional gain for DCC outer/inner loop
$K_{IOdc}/K_{IIdc}$	integral gain for DCC outer/inner loop
$K_{Ppll}/K_{Ipll}$	proportional and integral gain of PLL
$f_p, f_{uac}, f_{iac},$	the cutting-off frequencies of the 2 <sup>nd</sup> order
$f_{uc}, f_{udc}, f_{idc}$	low-pass filters for power, AC voltage, AC
	current, average capacitor voltage, DC voltage
	and DC current.

# I. INTRODUCTION

With the increasing impetus for bulk inland renewable power transmission, the overhead line (OHL) based modular multilevel converter high-voltage-direct-current (MMC-HVDC) scheme is preferred, which puts forward high requirements for the DC fault current isolation. Till now, most of the MMC-HVDC projects adopt the half-bridge

sub-modules (HBSMs) based topology, which cannot actively interrupt the DC fault current and needs the cooperation of high-power DC circuit breakers (DCCBs) [1][2]. The hybrid MMC consisting of HBSMs and full-bridge sub-modules (FBSMs) is promising in OHL-HVDC with its inherent ability to interrupt the DC fault current [3]. In the cable-based HVDC systems, the operation of the hybrid MMC can be the same as the half-bridge MMC during normal operation. When a DC fault is detected, the hybrid MMC will be blocked to interrupt the fault current. But for OHL application, due to the frequent occurrence of temporary DC faults, the operation of the hybrid MMC needs to be improved to facilitate DC-fault-ride-through without blocking the converters. Improved control strategies need to be proposed to realize the DC-fault-ride-through of the hybrid MMC. In a ±800kV three-terminal OHL-HVDC project under construction in China [3], named as Kun-Liu-Long (KLL) project, two terminals (Liubei and Longmen) adopt the hybrid MMC topology, and the decoupled AC and DC current control will be used [4]-[5].

Apart from the DC fault handling issue, the small-signal stability of the converters should also be investigated to avoid underlying oscillation problems, especially under weak AC system integration [6]-[7]. As reported, due to the interaction between the converter and the AC system, unexpected oscillations in the converters' current, voltage or power emerging from sub-synchronous frequency to high-frequency range are observed [7].

The stability problem for a half-bridge MMC project integrated with the weak AC system has occurred in China. The minimum short-circuit-ratio (SCR) of a ±420kV/ 1250MW back-to-back MMC-HVDC project in China can be as low as 1.9 [6], which imposes a limit to the transferable active power. A 1270Hz resonance occurs in the AC voltages for a ±350kV/ 1000MW back-to-back MMC-HVDC project after AC transmission lines are out of service and SCR drops to 3.3 [8]. During the test of KLL project, according to actual operation data, the SCR of the AC system connected to the Liubei terminal may drop below 2 due to the topology change caused either by AC fault clearance or scheduled transmission line maintenance. In this case, the Liubei terminal becomes connected to a weak AC system, which may impose stability risk for the KLL project. Therefore, both constructed and under-construction MMC projects are confronting the stability problem under a weak AC system connection. It is necessary to investigate the small-signal stability between MMCs and the weak AC system to guarantee a safe operation.

The stability between voltage-source-converters (VSCs) and the weak AC system has been an ever-lasting topic and attracted great interest both in industry and academia. The mainly researched topology till now includes two-level VSCs and half-bridge MMCs. In [9], the joint impact of SCR and phase-lock-loop (PLL) gain on the small-signal stability of the VSC under the active power and AC voltage control mode is investigated. While in [10] and [11], the mutual coupling between the power and AC voltage control loop is revealed under high active power penetration [10] or low SCR [11]. Besides the time-domain analysis, *Wen et al* proposed a *dq* impedance model based on the measured frame for grid-tied

VSCs [12][13]. The negative resistance feature of  $Z_{qq}$  is supposed to be the cause of the instability. Similarly in [14],  $Z_{qq}$  is found to display negative resistance behavior within the PLL bandwidth. For the VSCs in wind farm applications, Huang and Wang et al proposed the small-signal model under the DC and AC bus voltage control mode[15][16]. While for half-bridge MMCs, the AC impedance model is derived in [8] and [17]. A low-pass filter is added for the feedforward point of common coupling (PCC) voltage, and the high-frequency resonance of the AC bus voltage is effectively eliminated [8]. The time-domain small-signal models for half-bridge MMCs are studied in [18]-[21]. Given that the control strategy of the hybrid MMC for OHL application is different from the traditional two-level VSCs or half-bridge MMCs, the small-signal model suitable for the hybrid MMCs remains to be investigated, and its stability characteristic under weak AC system integration remains to be explored.

Besides the absence of a suitable small-signal model for the hybrid MMC, some questions remain in the existing analytical models for VSCs. For example, the outer loop of the controller is neglected in [8], [12]-[14]. While the inner control loop is neglected in [15]-[16]. There is no agreement on which control dynamics should be ignored. Generally, the simplification is based on the different response speeds of the control loops corresponding to the special time scale, and the ignorance of a certain time scale consequently results in the exposure of oscillation in a limited frequency range. While for the wide-band oscillation problem, as addressed in this paper, various time scales should be considered, so the theoretical foundation needs to be established for the simplification of control dynamics, for example, based on the weighted contribution to the instability, rather than time-scales. The DC voltage dynamics should also be considered rather than regarded as constants such as in [9], [12]-[14], so the impact of the DC network or other terminals can be reflected. As revealed in [11] and [22], the impact of operation status on small-signal stability is remarkable, while most existing researches only focus on the inverter status. Both active power directions should be researched, especially for the master converter, the transmitted active power or power direction of which can be varied during operation.

The contributions of this paper are as follows:

- 1) The closed-loop state-space-based small-signal model for the hybrid MMC with fault-ride-through control strategy is derived for the first time.
- 2) A wide-band oscillation between the master hybrid MMC and the weak AC system is revealed by modal analysis and validated by simulation for the rectifier and inverter status.
- 3) The simplified s-domain models for oscillation analysis are derived referring to the selective modal analysis (SMA) approach [23], which produces satisfying results on judging the stability and oscillation frequency more efficiently compared with the complicated state-space small-signal model.

The paper is organized as follows. The time-domain small-signal model of the hybrid MMC is proposed and validated in Section II. Then, the wide-band oscillation under weak AC system integration for the inverter and rectifier

 $Q_{fil}$ 

Reactive power controller Inner-loop

current

controller

operation is disclosed in simulation and analyzed by the small-signal model in Section III. Sensitivity studies for different parameters and the participation factor analysis for the wide-band oscillation are carried out in Section III. Due to the complexity of the time-domain model, the simplified s-domain models based on the SMA approach are studied in Section IV to analyze the stability more efficiently. Both time-domain and s-domain analysis have proposed proper parameter adjustment methods to enhance the stability, which is validated in Section V. Finally, the conclusion is drawn in Section VII.

#### II. TIME-DOMAIN SMALL-SIGNAL MODEL

#### A. A brief introduction to the hybrid MMC

Fig. 1 depicts the equivalent circuit of a hybrid MMC connected to the AC system through the AC transformer. Each arm of the hybrid MMC consists of HBSMs and FBSMs in series connection. All the variables are sampled and filtered before entering the control system. For OHL-based transmission, to avoid long-time power interruption, the hybrid MMC is required to ride through the DC faults without blocking in *KLL* project.

The traditional direct current vector control for the half-bridge MMC is depicted in Fig. 2 (a). To facilitate DC fault-ride-through, an improved direct current vector control for hybrid MMC is designed in Fig. 2 (b) [4]-[5], which is also named as the AC/DC decoupled control strategy. The detailed control structure of the AC/DC decoupled control is depicted in Fig. 3, which will be implemented in the KLL project. The controller consists of the AC current control (ACC) loop, the DC current control (DCC) loop and the circulating current suppression control (CCSC) loop, which separately produces the fundamental modulation signal  $M_d\cos(\omega t)+M_q\sin(\omega t)$ , the DC modulation signal  $M_{dc}$ , and the second harmonic modulation signal  $M_{d2}\cos(2\omega t)+M_{q2}\sin(2\omega t)$ . The structures of ACC and CCSC are similar to those of the vector-based current controller for half-bridge MMCs. While the outer-loop control targets of the d-channel and q-channel for ACC are separately set to be  $u_{c,avg}$  and Q. The outer-loop control target for DCC is  $u_{dc}$  or P. The inner-loop of DCC regulates DC current.

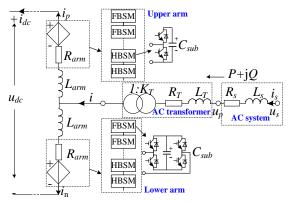
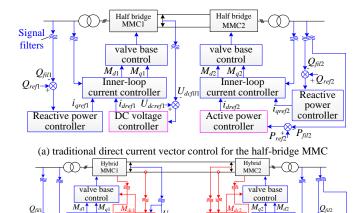


Fig. 1. Equivalent circuit of the hybrid MMC system for a single phase.



Inner-loop

current

controller

(b) improved direct current vector control for the hybrid MMC Fig. 2. Direct current vector control for a point-to-point MMC system.

controller

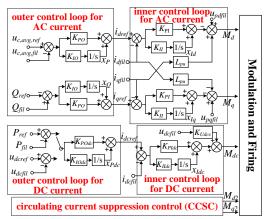


Fig. 3. AC/DC decoupled control strategy of the hybrid MMC.

#### B. Small-signal model of the hybrid MMC

The open-loop state-space model of the hybrid MMC is proposed in the authors' earlier work [26]. The state-space model is built under rotating frames using the dynamic phasor method for a single phase. The oscillating variables in the static ABC frame are transformed into the xy rotating frame. The small-signal model can be written as:

$$\Delta \dot{\boldsymbol{X}}_{8th} = \boldsymbol{A}_{8th} \Delta \boldsymbol{X}_{8th} + \boldsymbol{B}_{8thdc} \Delta \boldsymbol{u}_{dc} + \boldsymbol{B}_{8thac} \Delta \boldsymbol{I}_{ac} + \boldsymbol{B}_{8thctrl} \Delta \boldsymbol{M}$$
(1) where  $\boldsymbol{X}_{8th} = [\boldsymbol{u}_{px2}^{\Sigma}, \boldsymbol{u}_{py2}^{\Sigma}, \boldsymbol{u}_{px}^{\Sigma}, \boldsymbol{u}_{py}^{\Sigma}, \boldsymbol{u}_{p0}^{\Sigma}, i_{diffx2}, i_{diffy2}, i_{diffy2}]^{T}.$ 

The state variables are described by the internal electric dynamics of the hybrid MMC. The input quantities include the AC current  $I_{ac}=[i_x, i_y]^T$ , the DC terminal voltage  $u_{dc}$  and the modulation signals  $M=[M_x, M_y, M_{x2}, M_{y2}, M_{dc}]^T$ . The expressions for the matrices in (1) can be conveniently obtained from reference [26].

The electric system of the hybrid MMC outputs the AC internal voltage  $e_{vxy} = [e_{vx}, e_{vy}]^T$  to the AC system, and outputs the DC internal voltage  $e_{dc}$  and the DC current  $i_{dc}$ =3 $i_{diff0}$  to the DC network. The equivalent circuit of the AC and DC port is depicted in Fig. 4.

The expressions for  $e_v$  and  $e_{dc}$  are:

$$\begin{bmatrix} e_{vx} \\ e_{vy} \end{bmatrix} = \begin{bmatrix} \frac{M_x}{4} & \frac{M_y}{4} & \frac{M_{x2} - 2M_{dc}}{4} & \frac{M_{y2}}{4} & \frac{M_x}{2} \\ \frac{-M_y}{4} & \frac{M_x}{4} & \frac{M_{y2}}{4} & -\frac{M_{x2} + 2M_{dc}}{4} & \frac{M_y}{2} \end{bmatrix} \cdot (2)$$

$$\begin{bmatrix} u_{vx2}^{\Sigma} & u_{vy2}^{\Sigma} & u_{vx}^{\Sigma} & u_{vy}^{\Sigma} & u_{v0}^{\Sigma} \end{bmatrix}^{T}$$

$$e_{dc} = M_{dc} u_{p0}^{\Sigma} - \frac{1}{2} \left( M_{x} u_{px}^{\Sigma} + M_{y} u_{py}^{\Sigma} + M_{x2} u_{px2}^{\Sigma} + M_{y2} u_{py2}^{\Sigma} \right)$$
 (3)

In this paper, the control dynamics are added to form a closed-loop state-space-based small-signal model. Different from the electric dynamics, the control dynamics are modeled under the rotating frame synchronized with the measured PCC voltage by PLL, namely, *dq* frame. The state-space model of

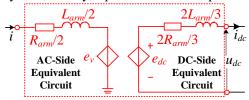


Fig. 4. Equivalent circuit of the hybrid MMC AC/DC ports.

the ACC, DCC, CCSC and PLL can be easily obtained by exploring the control block diagrams. The small-signal models of ACC and DCC are written as:

$$\dot{\mathbf{X}}_{C} = \mathbf{A}_{C} \Delta \mathbf{X}_{C} + \mathbf{B}_{Cfil} \Delta \mathbf{y}_{Cfil} + \mathbf{B}_{Cref} \Delta \mathbf{u}_{Cref} 
\Delta \mathbf{M}_{da} = \mathbf{C}_{C} \Delta \mathbf{X}_{C} + \mathbf{D}_{Cfil} \Delta \mathbf{y}_{Cfil} + \mathbf{D}_{Cref} \Delta \mathbf{u}_{Cref}$$
(4)

$$\Delta \dot{X}_{Cdc} = A_{Cdc} \dot{X}_{Cdc} + B_{Cdcfil} \dot{y}_{Cdcfil} + B_{Cdcref} \dot{u}_{Cdcref}$$

$$M_{dc} = C_{Cdc} \dot{X}_{Cdc} + D_{Cdcfil} \dot{y}_{Cdcfil} + D_{Cdcref} \dot{u}_{Cdcref}$$
(5)

where  $X_C = [x_P, x_Q, x_{Id}, x_{Iq}]^T$ ,  $u_{Cref} = [u_{c,avg,ref}, Q_{ref}]^T$ ,  $y_{Cfil} = [u_{c,avg,fil}, Q_{fil}, i_{qfil}, i_{qfil}, u_{pqfil}]^T$ ,  $M_{dq} = [M_d, M_q]^T$ ,  $X_{Cdc} = [x_{Pdc}, x_{Idc}]^T$ ,  $u_{Cdcref} = [P_{ref}, u_{dcref}, i_{dcref}]^T$ ,  $y_{Cdcfil} = [P_{fil}, u_{dcfil}, i_{dcfil}]^T$ . The matrices in (4) and (5) can be directly derived from Fig. 3.

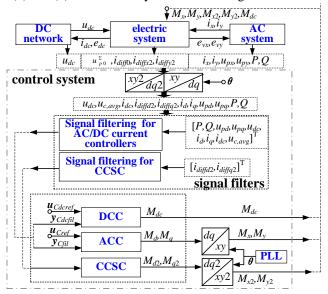


Fig. 5. Modeling frame for the closed-loop state-space model of hybrid MMC. In this paper, the signal filters for controllers are modeled as the second-order low-pass filter. The small-signal model for CCSC, PLL and the signal filters can be referred to [21], which are the same as the models for half-bridge MMCs. The overall

modeling frame for the closed-loop state-space model is depicted in Fig. 5. The overall small-signal model can be easily obtained by linearizing each of the subsystems in a modular way.

#### C. Validation of the small-signal model

In the following simulation, a two-terminal hybrid MMC system is built, as shown in Fig. 6. The DC line is equivalent to one  $\pi$ -section, which is also adopted in [27]-[29] for small-signal stability analysis.

The detailed parameters of the hybrid MMC and the AC system are displayed in the Appendix. The strength of the AC system connected to the hybrid MMC can be decided by SCR as calculated by:

$$SCR = \frac{P_{ac}}{P_{dcN}} \tag{6}$$

where  $P_{ac}$  is the short-circuit capacity of the AC system, and  $P_{dcN}$  is the rated capacity of the hybrid MMC. Since the AC system is equaled as a *Thevenin* circuit,  $P_{ac}$  can be adjusted by varying the internal impedance  $R_s$ +j $\omega L_s$ . In this configuration, the SCRs of the AC system 1 and 2 are respectively 2 and 20, which indicates a weak and strong AC system.

The master hybrid MMC1 is connected to the weak AC system, which regulates the DC voltage and reactive power. While the other terminal hybrid MMC2 is connected to a strong AC grid, which regulates the active and reactive power. The electromagnetic model of the two-terminal system is built in PSCAD/EMTDC.

In order to distinguish the flexible control of the DC voltage, the reference for the DC voltage is intentionally set to be 70% of the rated value. The reactive power and active power are set to be 0.2 and 0.5 (in per unit). To validate the correctness of the proposed small-signal model, the DC voltage reference is decreased from 0.7 to 0.65 at 1s. The step responses of the electromagnetic model and the small-signal model are compared in Fig. 7, which shows good consistency.

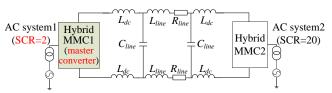
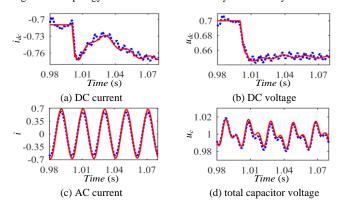


Fig. 6. The topology of the tested two-terminal hybrid MMC system.



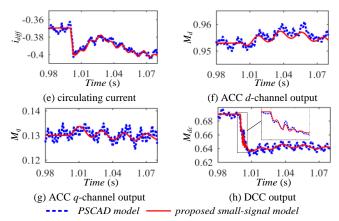


Fig. 7. Validation of the small-signal model (all in per unit).

# III. SMALL-SIGNAL STABILITY ANALYSIS UNDER WEAK AC SYSTEM INTEGRATION

Conventionally, the master hybrid MMC is connected to a strong AC system to support the DC voltage of the whole HVDC system and balance the active power. While under some scenarios, such as scheduled transmission line maintenance or incidental AC fault trip, the topology of the AC system varies, which may result in a sudden change of AC system parameters. Consequently, the hybrid MMC will face sudden SCR dip during operation while maintaining high-level active power transmission. This may lead to a wide-band oscillation problem, as will be disclosed in the simulation and explained by the small-signal stability analysis in this section.

#### A. Simulation of the wide-band oscillation

Suppose that the active power flowing from AC side to DC side is the default positive direction. In practice, the active power direction of the master converter may be bidirectional. In this paper, by adjusting the active power reference of hybrid MMC2, the operation status of hybrid MMC1 can be changed accordingly. When hybrid MMC1 is the receiving end, as shown in Fig. 8 (a), with the rise of the inverted active power, the active and reactive power start oscillating, while the average capacitor voltage remains stable. The dominant oscillation frequency at  $P_{pu}$ = -0.56 is 185.6Hz. When hybrid MMC1 is the sending end, as shown in Fig. 8 (b), with the rise of the rectified active power, the average capacitor voltage and the active power start oscillating, while the reactive power contains slight oscillation. The dominant oscillation frequency at  $P_{pu}$ =0.60 is 7.33Hz.

Based on the simulation results, it is clear that for the tested hybrid MMC1 integration to a weak AC system with SCR below 2, instability occurs when over 60% active power is transmitted. The frequency of the triggered oscillation in the active power, reactive power or the average capacitor voltage varies from several Hz to several hundred Hz, showing wide-band oscillation characteristics. The active power transmission direction imposes a notable impact on the oscillation frequency or the electric variables with evident oscillation.

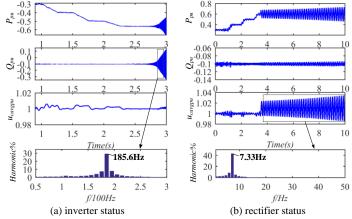


Fig. 8. Instability caused by the high-level active power under weak AC system integration. Active power  $(P_{pu})$ , reactive power  $(Q_{pu})$ , average capacitor voltage  $(u_{cavgpu})$ , harmonic component analysis.

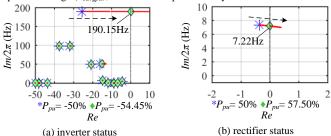


Fig. 9. Root locus analysis with active power increasing.

#### B. Root locus analysis

Based on the small-signal model, the impact of the active power on small-signal stability is studied through root locus analysis. As shown in Fig. 9 (a), when the inverted active power exceeds 54.45% of the rated capacity, eigenvalues move from the left-half-plane (LHP) to the right-half-plane (RHP), which indicates an unstable system. Similarly, as shown in Fig. 9 (b), when the rectified active power exceeds 57.5% of the rated capacity, the system also becomes unstable.

Let the inverted active power be 56%, and the RHP eigenvalues are calculated as  $9.180\pm j189.96*2\pi$ , which indicates that the oscillation frequency of the unstable mode is 189.96Hz. As can be seen, the calculated oscillation frequency is closed to the simulated oscillation frequency 185.6Hz in Fig. 8 (a). Similarly, let the rectified active power be 60%, and the RHP eigenvalues are calculated as  $0.127\pm j7.16*2\pi$ , which indicates 7.16Hz oscillation frequency. The calculated oscillation frequency is also consistent with the simulated result 7.33Hz.

# C. Sensitivity analysis

The sensitivity of the eigenvalue  $\lambda_i$  towards a certain parameter  $\alpha$  can be calculated as  $\Delta \lambda_i / \Delta \alpha$ . The parameters to be analyzed include Q, PLL parameters ( $K_{Ppll}$ ,  $K_{Ipll}$ ), ACC parameters ( $K_{PO}$ ,  $K_{IO}$ ,  $K_{PI}$ ,  $K_{II}$ ), DCC parameters ( $K_{POdc}$ ,  $K_{IOdc}$ ,  $K_{PIdc}$ ,  $K_{IIdc}$ ) and cutting-off frequencies of various signal filters ( $f_P$ ,  $f_{uac}$ ,  $f_{iac}$ ,  $f_{uc}$ ,  $f_{udc}$ ,  $f_{idc}$ ).

The sensitivity calculation results for the real part of the critically unstable eigenvalue in Fig. 9 (a) and (b) are depicted in Fig. 10 (a) and (b) respectively. Under inverter status, the remarkable sensitivities are positive, which indicates that

decreasing  $K_{PO}$ ,  $K_{PI}$  or the absorbed Q can effectively pull the unstable mode to the LHP. While under rectifier status, the remarkable sensitivities are negative, which indicates that increasing  $K_{PO}$  or the absorbed Q can effectively pull the unstable mode to the LHP. Moreover, the remarkable sensitivities under inverter status are much larger than those under rectifier status, which indicates that the parameter adjustment is more effective under the inverter status with respect to enhancing the stability.

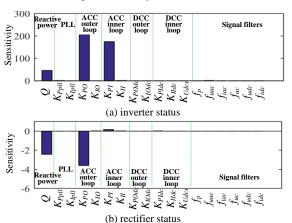


Fig. 10. Sensitivity analysis of the critically unstable eigenvalue to parameters.

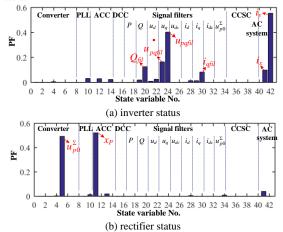


Fig. 11. Participation factor analysis with critical active powers.

#### D.Participation factor analysis

Participation factor (PF) analysis is conducted to reveal the unstable modes under critical active power levels, as shown in Fig. 11. It is obvious that the distributions of PFs under two unstable modes are different to each other, which accords with the observation of the instability through different signals in Fig. 8.

As shown in Fig. 11 (a), the state variables with the two highest PFs are the measured reactive component of PCC voltage  $u_{pqfil}$  and the reactive component of the AC current  $i_y$ . Since the unstable mode is concerned with the reactive-power-related state variables, it can be inferred that the small-signal stability of the inverted hybrid MMC is mainly affected by the control stability of ACC q-channel.

As shown in Fig. 11 (b), the unstable mode is mainly related to the average capacitor voltage and the outer loop state variable of ACC d-channel. Since the average capacitor

voltage is the input signal of ACC *d*-channel, it can be inferred that the small-signal stability of the rectified hybrid MMC is mainly affected by the control stability of ACC *d*-channel.

#### IV. SIMPLIFIED S-DOMAIN MODELS

The former participation factor analysis and simulation results reveal that the concerned wide-band oscillation is decoupled regarding the involved control loops, i.e., the ACC *q*-channel control mainly participates in the high-frequency oscillation under inverter status and the ACC *d*-channel control is related to the low-frequency oscillation under rectifier status. In this section, we refer to the selective modal analysis approach and simplify the analysis model based on loop-gain, in order to obtain a more intuitive understanding of the instability.

## A. SMA approach

SMA is firstly presented in [23]. Originally, this analysis approach is used to propose a reduced-order model that accurately contains the eigen-structure of the selected modes of interest [24][25]. The first step of SMA is to classify the system state variables into relevant state variables (RSVs) and less relevant state variables (LRSVs) by participation factor analysis to the selected modes. Then, the dynamic models for LRSV are converted to static models by replacing the 's' Laplace operators with eigenvalues of the selected modes. In this way, the system is reduced into a condensed form for analyzing the selected modes without changing the eigen-structure. For more information about SMA, please refer to [23].

In SMA approach, the dynamics of LRSVs are neglected in the state-space-based reduced order model. In this paper, we refer to this idea and neglect the small-signal expressions of the distinguished LRSVs, in order to effectively derive a simplified loop-gain-based model.

B. Simplified s-domain model of ACC q-channel under inverter status

Based on Fig. 11 (a), the RSVs to the unstable mode come from the AC current, PLL, ACC q-channel and signal filters for Q,  $u_{pq}$  and  $i_q$ .

The complete small-signal model for  $i_y$  of the hybrid MMC can be condensed by neglecting the LRSVs, as shown below. Notice that the control inputs  $\Delta M_x$  and  $\Delta M_y$  should be retained.

$$s\Delta i_{y} = \frac{1}{4L_{tot}} \left[ M_{y0} \frac{\Delta u_{px2}^{\Sigma}}{\Delta u_{px2}} + \left( M_{x20} + 2M_{dc0} \right) \frac{\Delta u_{py}^{\Sigma}}{\Delta u_{py}^{\Sigma}} - 2M_{y0} \frac{\Delta u_{p0}^{\Sigma}}{\Delta u_{p0}^{\Sigma}} - M_{x0} \frac{\Delta u_{py2}^{\Sigma}}{\Delta u_{py2}^{\Sigma}} - \left( u_{px20}^{\Sigma} - 2u_{p00}^{\Sigma} \right) \Delta M_{y} - M_{y20} \frac{\Delta u_{px}^{\Sigma}}{\Delta u_{px}^{\Sigma}} + u_{py20}^{\Sigma} \Delta M_{x} + u_{py0}^{\Sigma} \frac{\Delta M_{x2}}{\Delta u_{py2}^{\Sigma}} - u_{px0}^{\Sigma} \frac{\Delta M_{y2}}{\Delta u_{py2}^{\Sigma}} + 2u_{py0}^{\Sigma} \frac{\Delta M_{dc}}{\Delta u_{cc}^{\Sigma}} - 4\omega L_{tot} \frac{\Delta i_{x}}{\Delta u_{cc}^{\Sigma}} - 4R_{tot} \Delta i_{y} \right]$$

$$(7)$$

where  $L_{tot} = L_{arm}/2 + (L_T + L_s)/K_T^2$ ,  $R_{tot} = R_{arm}/2 + (R_T + R_s)/K_T^2$ .

Based on (7), we can express  $\Delta i_v$  with  $\Delta M_x$  and  $\Delta M_v$  as:

$$\Delta i_{y} \approx -\frac{u_{py20}^{\Sigma}}{4(sL_{tot} + R_{tot})} \Delta M_{x} + \frac{u_{px20}^{\Sigma} - 2u_{p00}^{\Sigma}}{4(sL_{tot} + R_{tot})} \Delta M_{y}$$
 (8)

Though the participation factor of  $\Delta i_x$  in Fig. 11 (a) is not zero, we assume that  $i_x$  is not closely related to ACC q-channel control. Thus, we neglect  $\Delta i_x$  in order to simplify the derivation for the open-loop gain. In this way, the small-signal models of PCC voltage can be approximated by ignoring  $\Delta i_x$ :

$$\Delta u_{px} = \frac{\omega L_s}{K_T} \Delta i_y - \left(\frac{R_s}{K_T} + \frac{sL_s}{K_T}\right) \Delta i_x$$
 (9)

$$\Delta u_{py} = -\frac{\omega L_s}{K_T} \frac{\Delta i_x}{\Delta i_x} - \left(\frac{R_s}{K_T} + \frac{sL_s}{K_T}\right) \Delta i_y$$
 (10)

The small-signal model of the PLL can be expressed as:

$$\Delta \theta = \left[ \frac{K_{Ppll} s + K_{Ipll}}{s^2 + K_{Ppll} s + K_{Ipll}} \right]_{G_{prl}} \frac{u_{px0} \Delta u_{py} - u_{py0} \Delta u_{px}}{u_{px0}^2 + u_{py0}^2}$$
(11)

Substitute (9) and (10) into (11), and we can obtain the relation between  $\Delta\theta$  and  $\Delta i_v$ :

$$\Delta\theta \approx \left[ G_{PLL} \frac{-sL_s u_{px0} - R_s u_{px0} - \omega L_s u_{py0}}{K_T \left( u_{px0}^2 + u_{py0}^2 \right)} \right]_{G_{\theta \ iv}} \Delta i_y \tag{12}$$

The relation of xy frame and dq frame can be expressed as:

$$\begin{bmatrix} \Delta \beta_{d} \\ \Delta \beta_{q} \end{bmatrix} = \begin{bmatrix} \cos \theta_{0} & \sin \theta_{0} \\ -\sin \theta_{0} & \cos \theta_{0} \end{bmatrix} \begin{bmatrix} \Delta \beta_{x} \\ \Delta \beta_{y} \end{bmatrix} + \begin{bmatrix} -\sin \theta_{0} & \cos \theta_{0} \\ -\cos \theta_{0} & -\sin \theta_{0} \end{bmatrix} \begin{bmatrix} \beta_{x0} \\ \beta_{y0} \end{bmatrix} \Delta \theta$$
(13)

The ACC *d*-channel output  $\Delta M_d$  is omitted for ACC *q*-channel analysis, then  $\Delta M_x$  and  $\Delta M_y$  can be approximated:

$$\Delta M_{x} = \cos \theta_{0} \frac{\Delta M_{d}}{\Delta M_{d}} - \sin \theta_{0} \Delta M_{q} + \left[ -\left(M_{d0} \sin \theta_{0} + M_{q0} \cos \theta_{0}\right)\right]_{Gy} \Delta \theta$$
(14)

$$\Delta M_{y} = \sin \theta_{0} \, \Delta M_{d} + \cos \theta_{0} \Delta M_{q} + \left( M_{d0} \cos \theta_{0} - M_{q0} \sin \theta_{0} \right)_{G_{M_{e},q}} \Delta \theta$$
(15)

Substituting (14) and (15) into (8), we can obtain:

$$\Delta i_{y} \approx \left[ \frac{\sin \theta_{0} u_{py20}^{\Sigma} + \cos \theta_{0} \left( u_{px20}^{\Sigma} - 2 u_{p00}^{\Sigma} \right)}{4 \left( s L_{tot} + R_{tot} \right)} \right]_{G_{iy\_Mq}} \Delta M_{q} + \left[ \frac{-G_{Mx\_\theta} u_{py20}^{\Sigma} + G_{My\_\theta} \left( u_{px20}^{\Sigma} - 2 u_{p00}^{\Sigma} \right)}{4 \left( s L_{tot} + R_{tot} \right)} \right]_{G_{\Sigma=0}} \Delta \theta$$
(16)

Substitute (12) into (16), and  $\Delta i_y$  can be expressed by  $\Delta M_q$ . In the following derivation, we shall express  $\Delta M_q$  with  $\Delta i_y$  by considering ACC q-channel dynamics.

By neglecting the LRSV  $\Delta i_{dfil}$ , the small-signal model of the output of ACC q-channel is approximated as:

$$\Delta M_{q} = \Delta u_{pqfil} + G_{in} \Delta i_{qfil} + G_{in} G_{out} \left( \Delta Q_{ref} - \Delta Q_{fil} \right) - L_{pu} \frac{\Delta i_{dfil}}{\Delta i_{dfil}}$$
(17)

where  $G_{in}$  and  $G_{out}$  are respectively the transfer functions of the inner and outer loop of ACC.

$$G_{in}(s) = K_{PI} + \frac{K_{II}}{s}, G_{out}(s) = K_{PO} + \frac{K_{IO}}{s}$$
 (18)

The complete calculation for  $\Delta Q$  is:

$$\Delta Q = \frac{3}{2K_T} \left( u_{py0} \Delta i_x - u_{px0} \Delta i_y + i_{x0} \Delta u_{py} + i_{y0} \Delta u_{px} \right)$$
 (19)

By substituting (9)-(10) into (19) and neglecting  $\Delta i_x$ , we can approximate the relation between  $\Delta Q$  and  $\Delta i_y$ :

$$\Delta Q \approx \left[ -s \frac{3L_s i_{x0}}{2K_T^2} - \frac{3}{2K_T} \left( u_{px0} + \frac{R_s i_{x0}}{K_T} + \frac{\omega L_s i_{y0}}{K_T} \right) \right]_{G_0} \Delta i_y \quad (20)$$

 $\Delta i_q$  can be approximated by neglecting  $\Delta i_x$ :

$$\Delta i_{q} = \cos \theta_{0} \Delta i_{y} - \sin \theta_{0} \frac{\Delta i_{x}}{\Delta i_{x}} + \left( -i_{x0} \cos \theta_{0} - i_{y0} \sin \theta_{0} \right)_{G} \Delta \theta$$
(21)

Substitute (12) into (21), and we can express  $\Delta i_q$  with  $\Delta i_y$ :

$$\Delta i_q \approx \left(\cos\theta_0 + G_{iq_-\theta}G_{\theta_-iy}\right)_{G_-} \Delta i_y \tag{22}$$

 $\Delta u_{pq}$  is approximated by substituting (9) and (10) into (23):

$$\Delta u_{pq} = \cos \theta_0 \Delta u_{py} - \sin \theta_0 \Delta u_{px} + \left( -\cos \theta_0 u_{px0} - \sin \theta_0 u_{py0} \right)_G \quad \Delta \theta$$
 (23)

$$\Delta u_{pq} \approx \left( G_{uq_{-\theta}} G_{\theta_{-}iy} - \frac{\cos \theta_{0} L_{s} s + \cos \theta_{0} R_{s} + \sin \theta_{0} \omega L_{s}}{K_{T}} \right)_{G_{-}i_{-}i_{-}} \Delta i_{y} (24)$$

Suppose that transfer functions of signal filters for the AC current, AC voltage and the reactive power are respectively  $G_{fiac}$ ,  $G_{fuac}$  and  $G_{fp}$ , then, the variables on the right side of (17) can all be expressed by  $\Delta i_y$ .  $\Delta M_q$  can be expressed as:

$$\Delta M_{q} \approx \left(G_{uq_{-}iy}G_{fuac} + G_{in}G_{iq_{-}iy}G_{fiac}\right)_{G_{Mq_{-}iy}} \Delta i_{y} + G_{in}G_{out}\left(\Delta Q_{ref} - \Delta Q_{fil}\right)$$
(25)

Based on the derivation above, the block diagram for ACC *q*-channel control model is shown in Fig. 12. The open-loop transfer function can be obtained as:

$$G_{ACCq}(s) = \frac{G_{in}G_{out}G_{iy\_Mq}G_{Q\_iy}G_{fp}}{1 - G_{iy\_\theta}G_{\theta_{0}}G_{y} - G_{iy\_Ma}G_{Ma_{0}}G_{y}}$$
(26)

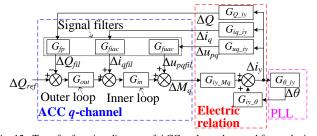


Fig. 12. Transfer function diagram of ACC q-channel control for analyzing the instability.

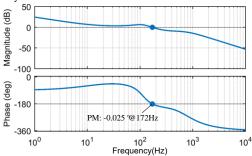
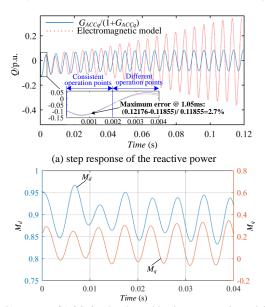


Fig. 13. Bode diagram of  $G_{ACCq}$  under 54.45% inverted active power.



(b) outputs of ACC d and q channel in electromagnetic model Fig. 14. Step response comparison of the reactive power between the simplified model and electromagnetic model.

# C. Accuracy verification and analysis of $G_{ACCq}(s)$

Let the inverted active power of the hybrid MMC be the critical value 0.5445 p.u., and the corresponding bode diagrams of  $G_{ACCq}$  are presented in Fig. 13.

As shown in Fig. 13, the phase margin (PM) of  $G_{ACCq}$  is narrowly negative (-0.0025 ), which indicates a critically unstable state. The crossover frequency is 172.2Hz, which is a little deviated from the mode calculation result 190Hz or the electromagnetic simulation results 185.6Hz.

To explain this error, the closed-loop step response of  $G_{ACCq}/(1+G_{ACCq})$  is compared with the electromagnetic model. As shown in Fig. 14 (a), the reactive power is stepped from -0.1 p.u. to zero. The first swings of the two oscillation waveforms match relatively well. Considering that the operation points of the two models can be regarded consistent within 2ms, the maximum error of the two waveforms within 2ms is calculated, which is only 2.7%. However, the error becomes larger with the increase of time, showing different oscillation frequencies. This is caused by the variation of the operation points. The simplified model  $G_{ACCq}$  is derived based on certain operation point, and neglects the impacts of other current control loops. However, as shown in Fig. 14 (b), the oscillation in the output of ACC d-channel  $M_d$  gradually increases, which consequently affects the operation point. Within 2ms, the variation of  $M_d$  is below 5%, and its impact on the operation point can be neglected, thus it is reasonable to only calculate the maximum error within 2ms in the step response.

Nevertheless,  $G_{ACCq}$  can also be employed to analyze the impact of various parameters on stability by comparing PMs under different configurations. We assume that the variation of certain parameter will not change the classification of RSVs and LRSVs regarding the concerned mode. This is actually guaranteed through detailed calculation of PFs under different configurations. As shown in Fig. 15 (a) and (b), even though  $f_p$  and  $f_{uac}$  are varied at a wide range, the classification of RSVs

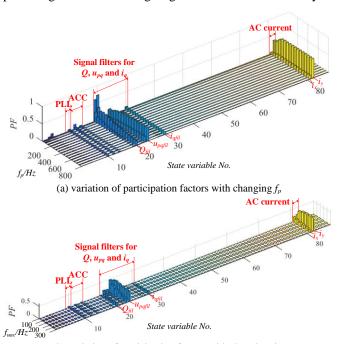
and LRSVs almost keeps unchanged.

TABLE I displays the PM variations against different parameters. The increments of PM are different. PM can be obviously increased by reducing the proportion gains for ACC, or by reducing cutting-off frequencies for power and AC voltage signal filters. In contrast, increasing the output reactive power or reducing PLL gain cannot significantly increase PM.

To highlight the effective parameter adjustment methods, Fig. 16 depicts the corresponding bode plots. As shown in Fig. 16 (a), PM rises up to 38.9 °after  $K_{PO}$  decreases from 1.0 to 0.5. Similarly, PM rises up to 13.8 °after  $K_{PI}$  decreases from 1.0 to 0.5 in Fig. 16 (b). The impact of control parameters on the stability accords with the sensitivity analysis results in Fig. 10 (a). It should be noticed that the reduction of  $K_{PO}$  or  $K_{PI}$  indicates the reduction of control bandwidth of the ACC q-channel outer or inner control loop, leading to the deterioration of reactive power and reactive current control.

While in Fig. 16 (c), with the reduction of  $f_p$  for the reactive power, the PM decreases at first and then increases with a further reduction of  $f_p$ . In this case, the PM equals to 37.8° when  $f_p$ =40Hz. In Fig. 16 (d), the PM keeps increasing with the reduction of  $f_{uac}$ . Notice that the sensitivities for the cutting-off frequencies of the signal filters in Fig. 10 are not notable. This is due to the difference in the considered variation range of the cutting-off frequencies for the calculation. For the sensitivity study in Fig. 10, the variation step is set to be only 0.1Hz away from the default values.

Based on the analysis above, it is recommended to slow down the ACC *q*-channel control or to deliberately decrease the cutting-off frequency of the signal filters for the reactive power signal or PCC voltage signal to enhance the stability.



(b) variation of participation factors with changing  $f_{uac}$  Fig. 15. Variation of participation factors with changing cutting-off frequencies of the signal filters at a wide range.

TABLE I
PHASE MARGIN VARIATION AGAINST DIFFERENT PARAMETERS UNDER

INVERTER OPERATION			
Parameters		Value variation	Phase margin variation
	$K_{PO}$	1→0.5	-0.025°→38.9°
ACC	$K_{IO}$	50→10	-0.025°→3.89°
ACC	$K_{PI}$	$1 \rightarrow 0.5$	-0.025°→13.8°
	$K_{II}$	100→20	-0.025°→4.37°
	$f_p$	800Hz→40Hz	-0.025°→37.8°
Signal filters	$f_{uac}$	$300Hz\rightarrow50Hz$	-0.025°→72.2°
	$f_{iac}$	800Hz→2000Hz	-0.025°→8.52°
PLL	$K_{Ppll}$	80→1	-0.025°→5.74 °
Reactive power	Q	-10% →-40% (p.u.)	-0.025°→0.567°

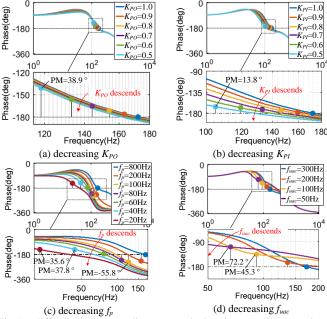


Fig. 16. Effective parameter adjustment methods to increase phase margins.

D.Simplified s-domain model for ACC d-channel under rectifier status

Based on Fig. 11 (b), the RSVs to the unstable mode are related to  $u_{p0}^{\Sigma}$ , ACC *d*-channel, AC current ( $\Delta i_x$ ) and PLL.

The complete expression for  $\Delta u_{p0}^{\Sigma}$  can be condensed by neglecting LRSVs and retaining  $\Delta M_x$  and  $\Delta M_y$ :

$$s\Delta u_{p0}^{\Sigma} = \frac{1}{8C_{arm}} \left[ -4M_{dc0} \frac{\Delta i_{diff0}}{\Delta i_{diff0}} + 2M_{x20} \frac{\Delta i_{diffx2}}{\Delta i_{diffx2}} + 2M_{y20} \frac{\Delta i_{diffy2}}{\Delta i_{diffy2}} + M_{x0} \Delta i_x + M_{y0} \frac{\Delta i_y}{\Delta i_y} - 4i_{diff00} \frac{\Delta M_{dc}}{\Delta d_{cc}} + i_{x0} \Delta M_x + i_{y0} \Delta M_y + 2i_{diffx20} \frac{\Delta M_{x2}}{\Delta M_{x2}} + 2i_{diffy20} \frac{\Delta M_{y2}}{\Delta M_{y2}} \right]$$
(27)

Then,  $\Delta u_{n0}^{\Sigma}$  can be approximated as:

$$\Delta u_{p0}^{\Sigma} \approx \frac{M_{x0}}{8C_{arm}s} \Delta i_x + \frac{i_{x0}}{8C_{arm}s} \Delta M_x + \frac{i_{y0}}{8C_{arm}s} \Delta M_y$$
 (28)

The complete expression for  $\Delta i_x$  can be condensed as:

$$s\Delta i_{x} = \frac{1}{4L_{tot}} \left[ -M_{x0} \frac{\Delta u_{px2}^{\Sigma}}{\Delta u_{px2}^{\Sigma}} - M_{y0} \frac{\Delta u_{py2}^{\Sigma}}{\Delta u_{py2}^{\Sigma}} - M_{y20} \frac{\Delta u_{py}^{\Sigma}}{\Delta u_{py}^{\Sigma}} + \right.$$

$$\left. \left( 2M_{dc0} - M_{x20} \right) \frac{\Delta u_{px}^{\Sigma}}{\Delta u_{px}^{\Sigma}} - 2M_{x0} \Delta u_{p0}^{\Sigma} - 4R_{tot} \Delta i_{x} + \right.$$

$$\left. 4\omega L_{tot} \frac{\Delta i_{y}}{\Delta u_{y}^{\Sigma}} - \left( u_{px20}^{\Sigma} + 2u_{p00}^{\Sigma} \right) \Delta M_{x} - u_{py20}^{\Sigma} \Delta M_{y} - \right.$$

$$\left. u_{px0}^{\Sigma} \frac{\Delta M_{x2}}{\Delta u_{yy2}^{\Sigma}} - u_{py0}^{\Sigma} \frac{\Delta M_{y2}}{\Delta u_{yy2}^{\Sigma}} - u_{px0}^{\Sigma} \frac{\Delta M_{dc}}{\Delta u_{px2}^{\Sigma}} \right]$$

$$\left. (29)$$

Then,  $\Delta i_x$  can be approximated as:

$$\Delta i_{x} \approx \frac{-M_{x0} \Delta u_{p0}^{\Sigma}}{2(sL_{tot} + R_{tot})} - \frac{\left(u_{px20}^{\Sigma} + 2u_{p00}^{\Sigma}\right) \Delta M_{x} + u_{py20}^{\Sigma} \Delta M_{y}}{4(sL_{tot} + R_{tot})}$$
(30)

Different from (9) and (10), the small-signal models of PCC voltage can be approximated by ignoring  $\Delta i_y$ :

$$\Delta u_{px} = \frac{\omega L_s}{K_T} \cdot \Delta i_y - \left(\frac{R_s}{K_T} + \frac{sL_s}{K_T}\right) \Delta i_x \tag{31}$$

$$\Delta u_{py} = -\frac{\omega L_s}{K_T} \Delta i_x - \left(\frac{R_s}{K_T} + \frac{sL_s}{K_T}\right) \frac{\Delta i_y}{\Delta i_y}$$
(32)

Substitute (31) and (32) into (11), and PLL dynamics can be accordingly obtained as:

$$\Delta\theta \approx \left[ G_{PLL} \frac{sL_s u_{py0} + R_s u_{py0} - \omega L_s u_{px0}}{K_T \left( u_{px0}^2 + u_{px0}^2 \right)} \right]_{G_{\theta, ir}} \Delta i_x$$
 (33)

The ACC q-channel output  $\Delta M_q$  is ignored for ACC d-channel analysis. Then,  $\Delta M_x$  and  $\Delta M_y$  can be approximated:

$$\Delta M_x = \cos \theta_0 \Delta M_d - \sin \theta_0 \frac{\Delta M_a}{\sigma} + G_{Mx \theta} \Delta \theta \tag{34}$$

$$\Delta M_{y} = \sin \theta_{0} \Delta M_{d} + \cos \theta_{0} \Delta M_{a} + G_{My} \theta \Delta \theta$$
 (35)

Substituting (34) and (35) into (28), we can get:

$$\Delta u_{p0}^{\Sigma} = \left(\frac{M_{x0}}{8C_{arm}s}\right)_{G_{uc0\_ix}} \Delta i_{x} + \left(\frac{i_{x0}G_{Mx\_\theta} + i_{y0}G_{My\_\theta}}{8C_{arm}s}\right)_{G_{uc0\_\theta}} \Delta \theta + \left(\frac{i_{x0}\cos\theta_{0} + i_{y0}\sin\theta_{0}}{8C_{arm}s}\right)_{G_{uc0\_Md}} \Delta M_{d}$$
(36)

Substituting (34) and (35) into (30), we can get:

$$\Delta i_{x} = \left[ \frac{-\left(u_{px20}^{\Sigma} + 2u_{p00}^{\Sigma}\right)\cos\theta_{0} - u_{py20}^{\Sigma}\sin\theta_{0}}{4\left(sL_{tot} + R_{tot}\right)} \right]_{G_{ix\_Md}} \Delta M_{d} + \left[ \frac{-\left(u_{px20}^{\Sigma} + 2u_{p00}^{\Sigma}\right)G_{Mx\_\theta} - u_{py20}^{\Sigma}G_{My\_\theta}}{4\left(sL_{tot} + R_{tot}\right)} \right]_{G_{ix\_\theta}} \Delta\theta + (37)$$

$$\left[ \frac{-M_{x0}}{2\left(sL_{tot} + R_{tot}\right)} \right]_{G_{ix\_\theta}} \Delta u_{p0}^{\Sigma}$$

For the three equations (33), (36) and (37), consider  $\Delta\theta$ ,  $\Delta i_x$  and  $\Delta u_{p0}^{\Sigma}$  as the three unknown variables and  $\Delta M_d$  as the input, then we can express  $\Delta u_{p0}^{\Sigma}$  and  $\Delta i_x$  with  $\Delta M_d$  as:

$$\Delta u_{p0}^{\Sigma} = \begin{cases} \frac{1}{G_{f}} \left[ \left( G_{uc0_{-}ix} + G_{uc0_{-}\theta} G_{\theta_{-}ix} \right) G_{ix_{-}Md} + \right] \\ G_{uc0_{-}Md} \left( 1 - G_{ix_{-}\theta} G_{\theta_{-}ix} \right) \right] \end{cases} \Delta M_{d} \quad (38)$$

$$\Delta i_{x} = \left(\frac{G_{ix\_Md} + G_{ix\_uc0}G_{uc0\_Md}}{G_{f}}\right)_{G_{uc},u,u} \Delta M_{d}$$
(39)

where 
$$G_f = 1 - G_{ix\_\theta} G_{\theta\_ix} - (G_{uc0\_ix} + G_{uc0\_\theta} G_{\theta\_ix}) G_{ix\_uc0}$$
.

In the following, we should express  $\Delta M_d$  with  $\Delta u_{n0}^{\Sigma}$  and  $\Delta i_x$ by considering ACC d-channel dynamics.

The complete expression for  $\Delta M_d$  is:

$$\Delta M_d = G_{in} G_{fiac} \Delta i_d + L_{pu} G_{fiac} \Delta i_q + G_{fuac} \Delta u_{pd} - G_{in} G_{out} \left( \Delta u_{coveref} - G_{fuc} \Delta u_{p0}^{\Sigma} \right)$$

$$(40)$$

Though the participation factors of the signal filters for the AC current or AC voltage are little, we retain  $\Delta i_d$ ,  $\Delta i_a$  and  $\Delta u_{pd}$ in (40) since they can be easily expressed with  $\Delta i_x$ .  $\Delta i_d$  and  $\Delta i_q$ can be approximated by ignoring  $\Delta i_{\nu}$  as:

$$\Delta i_{d} = \cos \theta_{0} \Delta i_{x} + \sin \theta_{0} \frac{\Delta i_{y}}{\Delta i_{y}} + \left( -i_{x0} \sin \theta_{0} + i_{y0} \cos \theta_{0} \right)_{G_{d}, \theta} \Delta \theta$$
(41)

$$\Delta i_{a} = \cos \theta_{0} \frac{\Delta i_{y}}{\Delta i_{y}} - \sin \theta_{0} \Delta i_{x} + G_{ia} \theta \Delta \theta \tag{42}$$

Substituting (33) into (41) and (42), and we can get:

$$\Delta i_d \approx \left(\cos\theta_0 + G_{id_{-\theta}}G_{\theta_{-ix}}\right)_{G_{id_{-ix}}} \Delta i_x \tag{43}$$

$$\Delta i_q \approx \left(-\sin\theta_0 + G_{iq_-\theta}G_{\theta_-ix}\right)_{G_{i_-i_-}} \Delta i_x \tag{44}$$

 $\Delta u_{pd}$  is originally expressed as:

$$\Delta u_{pd} = \cos \theta_0 \Delta u_{px} + \sin \theta_0 \Delta u_{py} + \left( -u_{px0} \sin \theta_0 + u_{py0} \cos \theta_0 \right)_{G_{ud}, \theta} \Delta \theta$$
(45)

Substituting (31) and (32) into (45),  $\Delta u_{pd}$  is represented as:

$$\Delta u_{pd} = \left[ G_{ud_{-}\theta} G_{\theta_{-}ix} - \frac{L_{s} \cos \theta_{0} s + R_{s} \cos \theta_{0} + \omega L_{s} \sin \theta_{0}}{K_{T}} \right]_{G_{ud_{-}ix}} \Delta i_{x}$$
(46)

Then  $\Delta M_d$  can be expressed as:

$$\Delta M_{d} = -G_{in}G_{out} \left( \Delta u_{cavgref} - \Delta u_{cavgfil} \right) + \left( G_{in}G_{fiac}G_{id\_ix} + L_{pu}G_{fiac}G_{iq\_ix} + G_{fuac}G_{ud\_ix} \right)_{G_{ud\_ix}} \Delta i_{x}$$

$$(47)$$

The block diagram for ACC d-channel control model can be obtained, as shown in Fig. 17. The open-loop transfer function can be obtained as:

$$G_{ACCd} = \frac{G_{in}G_{out}G_{uc0\_Mdf}G_{fuc}}{G_{Md-ix}G_{ix-Mdf} - 1}$$
(48)

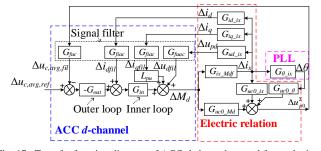


Fig. 17. Transfer function diagram of ACC d-channel control for analyzing the instability.

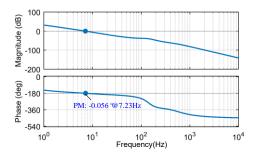


Fig. 18. Bode diagram of  $G_{ACCd}$  under 57.50% rectified active power.

### E. Accuracy verification and analysis of $G_{ACCd}(s)$

Let the rectified active power of the hybrid MMC be the critical value 0.5750 p.u., and the corresponding bode diagram of  $G_{ACCd}$  is presented in Fig. 18. It can be seen that the PM of  $G_{ACCd}$  is narrowly negative, which indicates a critically unstable state. The crossover frequency is 7.23Hz, which accords with the mode calculation result 7.22Hz. Hence,  $G_{ACCd}$ is proved to be effective in judging stability and the oscillation frequency for the rectified hybrid MMC connected with the weak AC system. The maximum rectified active power can also be efficiently determined by  $G_{ACCd}$ .

Similarly,  $G_{ACCd}$  can be employed to analyze the impact of control parameters on stability by comparing PMs under different configurations. TABLE II displays the PM variations against different parameters. PM can be obviously increased by raising  $K_{PO}$  or reducing  $K_{IO}$  for ACC outer loop. In contrast, the increments of PM are not notable for other parameters, such as increasing absorbed reactive power or PLL gain.

To highlight the effective parameter adjustment methods, Fig. 19 depicts the corresponding bode plots. As shown in Fig. 19 (a), when  $K_{PO}$  rises from default 0.4 to 1.4, PM rises to 8.37°. The impact of increasing  $K_{PO}$  accords with the sensitivity analysis results in Fig. 10 (b). In Fig. 19 (b), when  $K_{IO}$  drops from default 300 to 50, PM rises to 19.7 °. It should be noticed that the increase of  $K_{PO}$  or the reduction of  $K_{IO}$ results in the rise of control bandwidth of the outer loop for ACC d-channel, leading to the acceleration of control effect for the average capacitor voltage.

Based on the analysis above, it is recommended to speed up the ACC d-channel control to enhance stability.

TABLE II PHASE MARGIN VARIATION AGAINST DIFFERENT PARAMETERS UNDER RECTIFIER OPERATION

Parameters		Value variation	Phase margin variation
•	$K_{PO}$	$0.4 \rightarrow 1.4$	-0.056°→8.37°
ACC	$K_{IO}$	300→50	-0.056°→19.7°
ACC	$K_{PI}$	$1\rightarrow 2$	-0.056°→0.92°
	$K_{II}$	50→500	-0.056°→0.68°
	$f_{uac}$	300Hz→50Hz	-0.056°→0.82°
Signal filters	$f_{iac}$	$800Hz\rightarrow300Hz$	-0.056°→1.17°
	$f_{uc}$	250Hz→1000Hz	-0.056°→0.53°
PLL	$K_{Ppll}$	80→120	-0.056°→1.83 °
Reactive power	Q	-10%→20% (p.u.)	-0.056°→0.863°

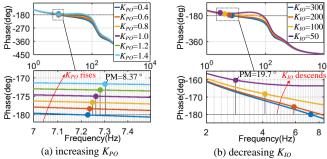


Fig. 19. Effective parameter adjustment methods to increase phase margins.

#### V.OSCILLATION MITIGATION VERIFICATION

In this section, the effectiveness of the parameter adjustment on damping the oscillation caused is validated electromagnetic simulation. The enhancement of transferable active power is also verified. A detailed calculation of the parameter adjustment versus the maximum stability-limited active power can be referred to [30]. It should be noticed that when the system configuration is varied, for example, the AC system SCR or MMC arm reactance are changed, we can similarly re-calculate the relationship and obtain suitable adjustment ranges for the control parameters by the small-signal models in this paper.

As shown in Fig. 20 (a), the inverted active power of the master hybrid MMC reaches 0.6 p.u. at 1.75s, and the reactive power starts to oscillate. At 1.8s,  $K_{PI}$  is reduced from 1 to 0.5, and the oscillation is suppressed effectively, then the inverted active power continues rising up to 0.9 p.u. with no oscillation. Similarly, in Fig. 20 (b), the high-frequency oscillation is successfully suppressed after  $f_{uac}$  is reduced from 300Hz to 100Hz, and the inverted active power continues rising up to 1 p.u..

As shown in Fig. 20 (c), the rectified active power of the master hybrid MMC reaches 0.65 p.u. at 3.75s, and the average capacitor voltage starts to oscillate. At 5.5s,  $K_{PO}$  is increased from 0.4 to 1.4, and the oscillation is suppressed, then the active power continues to rise up to 0.9 p.u.. Similarly in Fig. 20 (d), the low-frequency oscillation is effectively suppressed after  $K_{IO}$  is reduced from 300 to 10, and the rectified active power continues to rise up to 0.9 p.u. with retaining stability, but the oscillation is poorly damped.

According to Fig. 16 (c), decreasing  $f_p$  is supposed to be effective in improving stability. While the step response of ACC q-channel inner-loop is shown in Fig. 21 (a), indicating that this method may increase the overshoot of  $i_{qfil}$ . Moreover, PLL gain is recommended to be reduced under weak AC system integration by many researchers such as in [9],[11],[13] for two-level VSCs, which is also proved to be effective in damping the oscillation in this paper, however, it introduces serious deterioration towards the dynamic performance of ACC q-channel outer-loop control, as shown in Fig. 21 (b). This is also proved in bode analysis for  $G_{ACCq}$ , as shown in Fig. 22 (a). When  $K_{Ppll}$  is much reduced, though the stability margin of  $G_{ACCq}$  in the high-frequency range is slightly improved, the stability margin in the low-frequency range is worsened, indicating underdamped low frequency oscillation,

as reflected in Fig. 21 (b). While for the rectifier operation, as shown in Fig. 22 (b), the increase of  $K_{Ppll}$  leads to slight stability improvement in the low-frequency oscillation range.

The final suggested parameter adjustment methods are given in TABLE III. It should be noted that when multiple parameters are adjusted, TABLE III can be used to direct the adjustment.

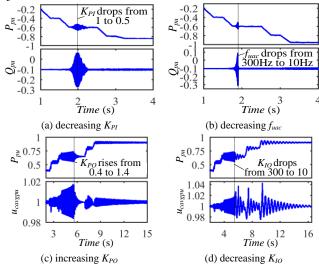


Fig. 20. Effectiveness of different parameters adjustment on suppressing oscillation and enhancing transferable active power.

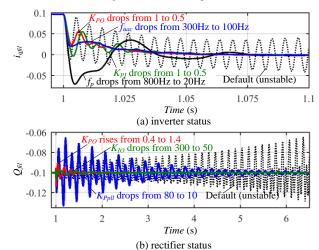
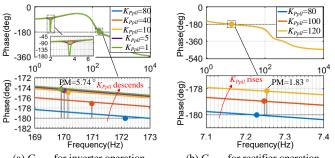


Fig. 21. Dynamic performance of parameter adjustment methods.



(a)  $G_{ACCq}$  for inverter operation (b)  $G_{ACCd}$  for rectifier operation Fig. 22. Varying PLL gain  $K_{Ppll}$  to increase phase margins under different operation states. TABLE III

RECOMMENDED PARAMETER ADJUSTMENT METHOD **Operation** Suggested parameter Physical explanation adjustment status Decrease  $K_{PO}$  or  $K_{PI}$ Decelerate the outer or inner loop of inverter

		ACC q-channel control
	Decrease $f_{uac}$	Decrease bandwidth of the low-pass
		signal filter for PCC voltage
rectifier	Increase $K_{PO}$ ,	Accelerate the outer loop of ACC
recurrer	decrease $K_{IO}$	d-channel control

#### VI. CONCLUSIONS

This paper investigates a wide-band oscillation of the master hybrid MMC connected to the weak AC grid triggered by excessive penetration of the active power. high-frequency (several hundred Hz) and low-frequency (several Hz) oscillations can be activated under the inverter and rectifier status separately.

The full-order time-domain small-signal model is developed. Key parameters and dominant state variables regarding the unstable modes are identified through sensitivity and participation factor analysis. The oscillation is considered to be triggered by the mismatch of control speed towards the weak AC grid condition. The high-frequency oscillation is related to over-quick ACC q-channel control, while the low-frequency oscillation is related to over-slow ACC d-channel control.

Simplified s-domain models to calculate the closed-loop control gain for ACC d/q-channel are developed referring to SMA approach. Sensitivity analysis towards phase margins reveals effective parameter adjustment methods that can enhance the stability. Generally, when the hybrid MMC is connected to a weak AC grid or facing a sudden SCR dip of the AC system, the proportion gain of the ACC outer and inner loop, or the cutting-off frequency for PCC voltage filter are recommended to be relatively small under inverter status; while under rectifier status, the proportion /integral gain of the ACC outer loop is suggested to be increased/decreased.

**APPENDIX** TABLE A I PARAMETERS OF THE TESTED HYBRID MMC AND AC SYSTEM

	Values	
	Rated DC voltage	640kV
	Rated capacity	1000MVA
Hybrid	Arm inductance	112mH
MMC	Arm equivalent resistance	$0.01\Omega$
	Number of FBSM/HBSM	100/100
	Submodule capacitance	10 mF
AC	Rated voltage grid/converter-side	400kV/352kV
transformer	Leak inductance	15%
	Rated voltage	400 kV
AC system	Internal impedance (AC system 1)	80∠85.62°Ω
	Internal impedance (AC system 2)	8∠82.83° Ω
	$L_{dc}$	100mH
DC line	$C_{line}$	2μF
DC lille	$L_{line}$	1mH
	$R_{line}$	1.2Ω

TABLE A II CONTROL PARAMETERS OF THE HYBRID MMC1

Control parameters		Values
PLL	$K_{Ppll}$	80
ILL	$K_{Ipll}$	500
	$f_p$	800Hz
Signal	$f_{uac}$	300Hz
filters	$f_{iac}$	800Hz
	$f_{udc}$	300Hz

	$f_{idc}$	800Hz
	$f_{uc}$	500Hz
ACC	$K_{PO}$	1(Inverter) 0.4 (Rectifier)
	$K_{IO}$	100(Inverter) 300 (Rectifier)
	$K_{PI}$	1
	$K_{II}$	50
DCC	$K_{POdc}$	1.2
	$K_{IOdc}$	800
	$K_{PIdc}$	2
	$K_{IIdc}$	100
	$K_{Udcs}$	1

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