

1 **Influence of the Site-Specific Component of Kappa on the Magnitude-Dependency of**
2 **Within-Event Aleatory Variabilities in Ground-Motion Models**

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13 **Abstract**

14 The aleatory-variability component (standard deviation) of a ground-motion motion has a large
15 influence on results of a probabilistic seismic hazard assessment. kappa, a measure of high-
16 frequency attenuation, has site- and record-specific effects that have been suggested as reasons for
17 observing heteroscedastic aleatory variability within earthquake ground motions. Specifically,
18 kappa has been proposed as a reason why ground motions from small earthquakes are more
19 variable than those from large earthquakes, which is modelled by magnitude-dependent within-
20 event standard deviations in ground motion prediction equations (GMPEs). In this study, we use

21 ground motions simulated using the stochastic method to examine the influence of the site-specific
22 component of kappa on aleatory variability of earthquake ground motions and examine the
23 hypothesis that this could be a cause of the observed heteroscedasticity in this variability. We
24 consider simulations with both fixed and continuous stress drop distributions and the site-specific
25 component of kappa to demonstrate that variation in the stress drop parameter contributes
26 minimally to magnitude-dependency, unlike the site-specific component of kappa, which causes
27 significant magnitude-dependency. Variation in the site-specific component of kappa is, therefore,
28 proposed to be at least partially responsible for the magnitude-dependency captured in the aleatory-
29 variability components of some recent GMPEs. It is found, however, that the expected impact of
30 the site-specific component of kappa on aleatory variability is much greater than modelled in these
31 GMPEs, which suggests that there could be a mitigating effect that is not captured within the
32 simulations (e.g. correlated inputs to the simulations).

33 **Introduction**

34 The uncertainty in ground-motion predictions is usually separated into epistemic uncertainty (due
35 to a lack of knowledge), which in theory can be reduced, and aleatory variability (due to the
36 randomness of the natural process), which is theoretically irreducible. A ground motion prediction
37 equation (GMPE), more generally called a ground-motion model, is a simple representation of the
38 physical processes associated with the generation and propagation of ground-motions (Douglas
39 and Edwards, 2016). Observed earthquake ground motions often show considerable deviations
40 from the predictions from these models, which is shown by wide residual distributions. Hence, the
41 aleatory variability component of GMPEs, often modelled as a lognormal distribution of a standard
42 deviation, σ , and zero mean, is a central part of GMPEs (Strasser et al., 2009). The value of σ
43 greatly influences the predicted ground-motion, even more so at low annual frequencies of

44 exceedance (AFE) that are of particular interest to earthquake engineering (Bommer and
45 Abrahamson, 2006; Toro, 2006).

46 Conventionally, σ is split into between-event and within-event components. The between-event
47 component (τ) captures the variability associated with event-specific factors (e.g. randomness in
48 the earthquake source) that have not been accounted for in the GMPE. The within-event
49 component (ϕ) models the variability associated with record-specific factors (e.g. randomness in
50 the local site amplification for a given site class).

51 A commonly-used site parameter is the high-frequency attenuation operator, kappa (κ) (Anderson
52 and Hough, 1984). This parameter describes the observed fall-off above the corner frequency (f_c)
53 of the Fourier amplitude spectrum of the accelerogram recorded at a site. Anderson and Hough
54 (1984) determined the decay of the Fourier amplitude spectrum to occur above $f > \sim 2$ Hz, but
55 subsequent studies (e.g. Anderson and Humphreys, 1991) suggested this decay occurs when $f > f_c$.
56 Anderson and Hough (1984), observing that κ increases with source-to-site distance, proposed that
57 κ is related to both the near-surface site conditions and the regional geological structure (i.e. κ is
58 both site- and record-specific).

59 The site- and record-specific nature of κ results in this parameter contributing to ϕ within GMPEs.
60 The influence of κ is not well understood and since it is a purely empirical parameter, a physical
61 explanation is likely to be inherently problematic. Douglas and Jousset (2011) postulate that
62 variations in κ_0 may be a reason for the magnitude-dependency of ϕ that is sometimes captured in
63 GMPEs, particularly those covering a wide magnitude range (Ambraseys et al., 2005; Boore et al.,
64 2014). However, Douglas and Jousset (2011) did not investigate this idea in detail. Therefore, this
65 study examines the influence of the site-specific component of kappa (κ_0) upon ϕ (the path-
66 dependent attenuation is modelled by the considered attenuation model – see Table 1), with an

67 emphasis on its potential to explain the magnitude-dependency (heteroscedasticity) of this
68 variability within some recent GMPEs. This study begins with a brief review of recent studies
69 examining the magnitude-dependency of ground-motion variability, followed by an analysis
70 examining: (1) the influence of κ_0 upon ϕ within simulation and (2) how well these simulated
71 results match the ϕ models in some recent GMPEs.

72

73 **Studies on the Magnitude-Dependency of Ground-Motion Variability**

74 The magnitude-dependency of σ for peak ground acceleration (PGA) was first examined in-depth
75 by Youngs et al. (1995), with the magnitude-dependency of τ being found to be stronger than the
76 magnitude-dependency of ϕ . Youngs et al. (1995) confirmed that non-linear site effects contribute
77 to the magnitude-dependency of σ , as proposed first by Chin and Aki (1991). Youngs et al. (1995)
78 proposed that the magnitude-dependency of σ could also be due to: (1) the magnitude-dependent
79 variability of the stress drop parameter ($\Delta\sigma$), (2) metadata errors for small magnitude earthquakes
80 and (3) the duration of ground-motion being shorter for small events than for larger earthquakes.

81 Ambraseys et al. (2005) found a statistically-significant magnitude-dependency in σ for short-
82 period ($<1s$) spectral acceleration (SA) but that this statistical significance did not hold for long-
83 period ($>1s$) SAs. They noted that the lack of statistical significance could be attributed to the
84 cut-offs used to filter the strong-motion records, which resulted in fewer long-period than short-
85 period SAs, rather than a true effect. Ambraseys et al. (2005), in contrast to Youngs et al. (1995),
86 assumed that the magnitude-dependency of σ was partitioned equally between τ and ϕ (rather than
87 being predominantly associated with τ) because of the complex mapping of the magnitude-
88 dependency upon both components. The magnitude-dependency could be due to site or

89 propagation path variability (thus manifesting in ϕ), due to the regression method used to derive
90 the GMPE (thus manifesting in τ) or due to metadata issues associated with estimation of source-
91 to-site distances and magnitudes (thus manifesting in ϕ and potentially τ depending on the spatial
92 distribution of sites relative to the earthquake source).

93 Bommer et al. (2007) demonstrated that reduction of the lower magnitude limit of the strong-
94 motion data used to derive a GMPE (from moment magnitude 5 to 3) significantly increases τ but
95 minimally increases ϕ (see their Figure 12). This lends support to Youngs et al. (1995)'s
96 observation that the magnitude-dependency of τ is stronger than the magnitude-dependency of ϕ .

97 Bommer et al. (2007) demonstrated that the expanded magnitude range increases ϕ slightly more
98 for short-period ground motions than ϕ for long-period ground-motions. Expansion of the
99 magnitude range likely increases ϕ for a given magnitude because of the inclusion of more sites
100 and additional records from each site. The increased site variability affects the shorter periods
101 more, so the responsible mechanism must cause greater variability at these periods than at longer
102 periods. This is suggestive of variation in κ_0 among sites potentially being a responsible
103 mechanism for the observed heteroscedasticity.

104 Bommer et al. (2007) also noted that the increased variability resulting from an increased
105 magnitude range could be due to the incorporation of data from different regions because: (1)
106 different instrument types are often used in different regions and (2) ground motions generated by
107 smaller earthquakes are more sensitive to differences in regional attenuation (due to differing
108 crustal structures and Q). Sensitivity analyses reported by Bommer et al. (2007) indicated,
109 however, that the median predictions and associated variabilities were not significantly influenced
110 by the inclusion/exclusion of different regional datasets. In contrast, Chiou et al. (2010)

111 demonstrated that, by accounting for regional differences in Californian ground motions, the
112 magnitude-dependency of τ is decreased.

113 Douglas and Jousset (2011) demonstrated using stochastic simulations that variations in κ_0 affect
114 PGA more for small magnitude earthquakes than for large magnitude earthquakes, and proposed
115 that this may explain the magnitude-dependency of σ within some GMPEs. This observation was
116 the trigger for the current study, which examines this potential explanation in more detail.

117 Through consideration of a standard Brune (1970; 1971) source spectrum model, Kotha et al.
118 (2017) expanded upon the physical explanation for the influence of $\Delta\sigma$ on the magnitude-
119 dependency of τ provided by Youngs et al. (1995). For a given moment magnitude (M_w), an
120 increase in $\Delta\sigma$ lowers the corner frequency (f_c), and increases ground-motion amplitudes for $f >$
121 f_c whilst ground-motion amplitudes for $f < f_c$ remain unmodified. If one considers a primary
122 frequency f_1 and a secondary frequency f_2 , when $(f_1, f_2) < f_c$ neither f_1 or f_2 is affected by
123 variability in $\Delta\sigma$, so their correlations are strong. When $(f_1, f_2) > f_c$, ground-motion amplitudes
124 increase monotonically with variation in $\Delta\sigma$, so their correlations are also strong. Therefore, Kotha
125 et al. (2017) state that for large magnitude earthquakes with a low f_c , stronger correlations would
126 be expected over a wide range of $(f_1, f_2) > f_c$ than would be observed for small magnitude
127 earthquakes. This is observed in the correlation coefficients computed by Kotha et al. (2017) over
128 the range of considered values for f_2 (with a fixed f_1) for large and small earthquakes (see their
129 Fig. 3), supporting this expanded physical explanation for the influence of $\Delta\sigma$ on the magnitude-
130 dependency of τ .

131 It should be noted that heteroscedasticity has been observed in the ground-motion residuals of
132 several GMPEs but the final aleatory-variability models recommended for these GMPEs are

133 homoscedastic. For example, Kotha et al. (2020) observed heteroscedasticity of τ with respect to
134 magnitude, but due to the limited number of large earthquakes compared to many small to
135 moderate earthquakes within their dataset, they decided that this observation was not convincing
136 enough to be incorporated into their final model. However, GMPEs have been developed which
137 successfully account for some of the effects contributing to the heteroscedasticity of σ . Kotha et
138 al. (2019) accounted for the influence of earthquake size on ϕ due to azimuthal variation of ground-
139 motions (small earthquakes have simpler radiation patterns than large earthquakes, resulting in
140 larger ϕ for smaller earthquakes), reducing ϕ within their proposed model. Such an example is
141 highlighted within this study because failing to capture the influence of earthquake size due to
142 azimuthal variation of ground-motions on ϕ in GMPEs results in greater uncertainty in estimations
143 of κ_0 .

144

145 **Investigating Ground-Motion Variability Using Stochastic Simulations**

146 To investigate how ground motions vary with changes in κ_0 , simulations were undertaken using
147 the stochastic method as implemented in the SMSIM software (Boore, 2005). Stochastic
148 simulations were undertaken using Bora et al. (2017)'s stochastic model for Europe with a Brune
149 (1970; 1971) source spectrum model and κ_0 distributions sampled from various published κ_0
150 models (Table 1). Appropriate κ_0 distributions were sampled from the considered models for an
151 average shear-wave velocity of the top 30 m (V_{s30}) of 620 m/s (roughly equivalent to “soft rock”).
152 Bora et al. (2017) state a reference V_{s30} of 620 m/s was used for the computation of their provided
153 κ_0 distribution, and so a V_{s30} of 620 m/s was used for the computation of the other κ_0 distributions
154 too. Considering a different V_{s30} value is unlikely to affect the results significantly.

155 For each magnitude, ϕ was computed from the simulations for a hypocentral distance (R_{hypo}) of
156 40 km for PGA and SA for periods of 0.2 s and 1 s (Figure 1) and moment magnitudes in the range
157 1 to 6.5. The ϕ values were computed for $R_{hypo} = 40$ km to eliminate the influence of regional
158 attenuation and because this is close to the center of strong-motion databases used to derive
159 empirical GMPEs for active shallow crustal regions. The absolute rate of change of ϕ with respect
160 to magnitude is used to characterize its magnitude-dependency (Figure 2). A larger rate of change
161 indicates a greater magnitude-dependency of ϕ .

162 The computed ϕ are compared to values provided by empirical GMPEs developed for similar
163 magnitude ranges (Figure 1; Figure 2). Empirical GMPEs developed for small magnitude
164 ($M_w < 3$) earthquakes are scarce (even more so those with heteroscedastic σ) compared to the
165 number of empirical GMPEs developed for moderate to large magnitude earthquakes. Due to this
166 scarcity of suitable models, and because ϕ generally contributes more to the total aleatory
167 variability than τ , for the GMPE for which ϕ is not provided (Bindi et al., 2007), the value of σ is
168 plotted instead.

169 For each sampled κ_0 distribution (see Table 1 for details on these κ_0 distributions and all other
170 inputted parameters), stochastic simulations were undertaken using: (1) a fixed $\Delta\sigma$ of 5.65 MPa
171 and (2) a $\Delta\sigma$ distribution sampled from the Bora et al. (2017) stochastic model (Figure 1; Figure
172 2). Variation in $\Delta\sigma$ was considered because the trade-off between the $\Delta\sigma$ and κ_0 parameters means
173 $\Delta\sigma$ must be varied to determine if it contributes to the magnitude-dependency of ϕ (Rodriguez-
174 Marek et al., 2013). This trade-off between $\Delta\sigma$ and κ_0 is especially significant for small earthquakes
175 due to their high corner frequencies from short rupture durations, which in turn results in the
176 generated ground-motions being more affected by scattering and attenuation (Sumy et al., 2017).

177 Simulations were also undertaken with a fixed κ_0 of 0.0308 s to examine the effect of varying only
178 stress drop (Figure 1; Figure 2).

179

180 **Results and Discussion**

181 For a fixed κ_0 and a $\Delta\sigma$ distribution sampled from Bora et al. (2017), the computed ϕ for PGA,
182 SA(0.2 s) and SA(1 s) are all small and show minimal magnitude-dependency, with ϕ increasing
183 slightly with magnitude (Figure 1; Figure 2). This weak magnitude-dependency observed when
184 only κ_0 is fixed suggests that $\Delta\sigma$ contributes minimally to the magnitude-dependency of ϕ for PGA,
185 SA(0.2 s) and SA(1 s). The ϕ computed for PGA for a sampled κ_0 distribution and a $\Delta\sigma$ distribution
186 sampled from Bora et al. (2017) show minimal difference to the corresponding ϕ computed with
187 the same κ_0 distributions and a fixed $\Delta\sigma$. This further supports the view that $\Delta\sigma$ has a minimal
188 influence on the magnitude-dependency of ϕ for PGA. The magnitude-dependency of ϕ with
189 varying κ_0 is considerably stronger for PGA than for SA(0.2 s) or SA(1 s) (Figure 2). Variations
190 in κ_0 potentially lead to stronger magnitude-dependency of ϕ for PGA than for SA(0.2 s) or SA(1
191 s) because κ_0 describes the decay of specifically high-frequency ground-motions, and therefore
192 PGA is more sensitive to said variations in κ_0 than SA(0.2 s) or SA(1 s), resulting in stronger
193 magnitude-dependency being observed for PGA. The seemingly limited influence of $\Delta\sigma$ on the
194 magnitude-dependency of ϕ observed within this study is supportive of Kotha et al. (2017)'s
195 findings that $\Delta\sigma$ has a noticeable influence on the magnitude-dependency of τ , therefore lending
196 support to their expanded physical explanation of how $\Delta\sigma$ influences τ too. However, due to the
197 complex mapping of magnitude-dependency onto both ϕ and τ , an expanded investigation into the
198 influence of $\Delta\sigma$ on the magnitude-dependency of both components of σ should be undertaken in
199 the future.

200 The computed ϕ for PGA, SA(0.2 s) and SA(1 s) are all larger for smaller magnitudes because as
201 discussed above, ground-motions generated from smaller earthquakes are more affected by
202 scattering and attenuation (Sumy et al., 2017). The magnitude-dependency of ϕ is inherently
203 stronger when a κ_0 distribution with greater variability is considered (Figure 2). For example, the
204 maximum magnitude-dependency of ϕ for PGA with the Bora et al. (2017) κ_0 distribution (highest
205 variability) is approximately 30% stronger than the maximum magnitude-dependency of ϕ with
206 the Edwards et al. (2011) κ_0 distributions (lowest variability). The observation of stronger
207 magnitude-dependency of ϕ for PGA than for SA(0.2 s) or SA(1 s) due to solely variation in κ_0
208 (Figure 2) suggests, as first proposed by Douglas and Jousset (2011), that κ_0 is at least partly
209 responsible for observed heteroscedastic ϕ in GMPEs for short-period SAs.

210 For PGA, ϕ computed from the simulated ground-motions are larger at lower magnitudes than the
211 values provided by the considered GMPEs, whereas for SA(0.2 s) and SA(1 s) ϕ computed from
212 the simulated ground-motions are more similar to those in the considered GMPEs (Figure 1), with
213 this being more so for SA(1 s) than for SA(0.2 s). ϕ for PGA computed from the simulated ground-
214 motions with the Chandler et al. (2006) and Edwards et al. (2011) κ_0 distributions are larger than
215 the values provided by the considered GMPEs below approximately M_w 2.5. As discussed above,
216 the larger ϕ computed using the Bora et al. (2017) κ_0 distribution is inherently due to its wider
217 distribution. Of the considered GMPEs, the models which provide values most similar to ϕ
218 computed from the simulated ground-motions are: Ameri et al. (2017), Chiou et al. (2010), Boore
219 et al. (2014) and Ambraseys et al. (2005). Of these, only the Ameri et al. (2017) GMPE was
220 developed for earthquakes of $M_w < 2.5$, and therefore was the only one of these GMPEs that does
221 not need extrapolation (Figure 1). Extrapolation of GMPEs below their designated magnitude
222 ranges cannot be the sole factor responsible for the difference between ϕ for PGA from the

223 simulated ground-motions and the GMPEs for $M_w < 2.5$. The observation that the simulated ϕ
224 values for SA(0.2 s) and SA(1 s) are more similar to the ϕ provided by the considered GMPEs can
225 be partly attributed to κ_0 having a more significant impact on PGA than SA(0.2 s) or SA(1 s), and
226 hence by default, variations in κ_0 are better modeled in GMPEs for SA(0.2 s) and SA(1 s) than for
227 PGA. The better modelling for SA(0.2 s) and SA(1 s) is likely due to κ_0 being a parameter
228 describing the decay of high frequency ground-motions, rather than low frequency ground-
229 motions.

230 The magnitude-dependency of ϕ for PGA computed from the simulated ground-motions is overall
231 far stronger than the magnitude-dependency observed in the considered empirical GMPEs with
232 heteroscedastic ϕ (Figure 2). For example, the maximum magnitude-dependency of ϕ for PGA
233 computed from the simulations with the Edwards et al. (2011) κ_0 distribution is 200% stronger and
234 130% stronger than the magnitude-dependency of ϕ in the Bommer et al. (2007) and Ambraseys
235 et al. (2005) GMPEs, respectively. The only exception to this observation is over the moment
236 magnitude interval M_w 4.5 - M_w 5.5, within which the magnitude-dependency of ϕ for PGA is far
237 greater for the Boore et al. (2014) GMPE than the simulated ground-motions with any of the
238 considered κ_0 distributions (Figure 2). The simulated magnitude-dependencies of ϕ for PGA are
239 likely stronger overall than from the considered empirical GMPEs because the functional forms of
240 the considered GMPEs lack terms modeling variations in κ_0 .

241 More varied results are observed for the magnitude-dependency of ϕ for SA(0.2 s) and SA(1 s)
242 computed from the ground-motion simulations when compared to the considered heteroscedastic
243 GMPEs than for PGA. For SA(0.2 s), the magnitude-dependency of ϕ computed from the
244 simulated ground-motions is lower than for the Ambraseys et al. (2005) or Bommer et al. (2007)
245 GMPEs, but lower than the Boore et al. (2014) GMPE, except over the magnitude interval M_w 4.5

246 - M_w 5.5, within which as for PGA and SA(1 s) it is far greater than ϕ computed from the simulated
247 ground-motions. For SA(1 s), the magnitude-dependencies of ϕ computed from the ground-motion
248 simulations can only be compared to the Boore et al. (2014) GMPE due to the other considered
249 GMPEs lacking heteroscedastic ϕ for SA(1 s). Therefore, for SA(1 s), limited comparisons can be
250 made with respect to the magnitude-dependency of ϕ computed from the ground-motion
251 simulations and the considered GMPEs. As for PGA and SA(0.2 s), the magnitude-dependency
252 of ϕ is far smaller for the Boore et al. (2014) GMPE than the magnitude-dependency of ϕ computed
253 from the simulated ground-motions with any of the considered κ_0 distributions, except over the
254 magnitude interval M_w 4.5 - M_w 5.5 when magnitude-dependency of ϕ is far greater for the Boore
255 et al. (2014) GMPE. The magnitude-dependency of ϕ computed from the ground-motion
256 simulations is overall more similar to the Boore et al. (2014) GMPE for SA(1 s) than for PGA or
257 SA(0.2 s). This greater similarity for SA(1 s) can potentially be explained by κ_0 describing the
258 decay of specifically high frequency ground-motions; if variations in κ_0 have a limited influence
259 on longer period ground-motions, then such variations will likely not have as pronounced an effect
260 for SA(1 s) as they do for PGA. This supports the reasoning above that the absence of terms which
261 model variations in κ_0 within the considered GMPEs will result in more pronounced differences
262 between the magnitude-dependencies of ϕ for PGA and SA(0.2 s) compared to SA(1 s).

263 Variations in κ_0 result in the magnitude-dependency of ϕ being marginally smaller for SA(0.2 s)
264 than for SA(1 s). The magnitude-dependency of ϕ would be expected to be greater for SA(0.2 s)
265 than for SA(1 s) because κ_0 describes the decay of high-frequency ground-motions. This could be
266 explained by a trade-off between the influence of κ_0 and $\Delta\sigma$ on ϕ at moderate spectral periods, in
267 which κ_0 has a stronger influence on ϕ at smaller spectral periods and $\Delta\sigma$ has a stronger influence
268 on ϕ at larger spectral periods. The presence of such a trade-off is potentially supported by the

269 observations that (1) as the spectral period increases, the magnitude at which peak magnitude-
270 dependency ϕ for a fixed κ_0 and a $\Delta\sigma$ distribution sampled from Bora et al. (2017) increases and
271 (2) for SA(0.2 s), the peak magnitude-dependency of ϕ computed with a non-fixed κ_0 occurs at a
272 greater magnitude than for either PGA or SA(1 s) whilst also being smaller than for either PGA or
273 SA(1 s).

274 The magnitude-dependency of ϕ for PGA due solely to variation in κ_0 being far stronger than the
275 magnitude-dependency observed within the considered GMPEs (regardless of whether they have
276 heteroscedastic or homoscedastic ϕ) suggests: (1) future empirical GMPEs should include terms
277 to model variation in κ_0 [there are some recent models in this direction (Laurendeau et al., 2013;
278 Hassani and Atkinson, 2018)] and (2) that empirical GMPEs with homoscedastic ϕ are inadequate
279 for regions with high variability in κ_0 because high variability in κ_0 results in strong magnitude-
280 dependency of ϕ particularly at short periods (Figure 2).

281 It should be acknowledged that there is potential for a circular argument associated with the
282 sampled distributions for both κ_0 and $\Delta\sigma$ used within the ground-motion simulations. The sampled
283 distributions have been developed based on models fit to data. These models are then used to
284 examine the influence of κ_0 and $\Delta\sigma$ on the magnitude-dependency of ϕ . If these distributions have
285 been well modeled (i.e. $\Delta\sigma$), then a minimal impact on the magnitude-dependency is observed,
286 whereas if the distribution has been less well modelled (i.e. κ_0) a considerably greater influence on
287 magnitude-dependency could be observed. However, the observations resulting from variation in
288 κ_0 are reasonably well explained. This suggests that κ_0 is sufficiently modelled for examining its
289 influence upon the magnitude-dependency of ϕ despite the larger uncertainty generally associated
290 with the modelling of κ_0 compared to $\Delta\sigma$.

291

292 **Conclusions**

293 In this short article, the hypothesis that variations in κ_0 , modeling high-frequency attenuation,
294 amongst sites could be a least partly responsible for the magnitude-dependency in within-event
295 variabilities in some ground-motion models is examined. To examine this hypothesis a series of
296 ground-motion simulations using the stochastic method were conducted using various distributions
297 of the key input parameters. Despite the variabilities computed from the simulated ground-motions
298 being higher than those in the considered ground-motion models and the magnitude-dependency
299 being stronger, this study lends support to the hypothesis that κ_0 is a contributing factor to the
300 magnitude-dependent variability of earthquake ground motions, particularly for short-period
301 response spectral accelerations. The mismatch between the variabilities from the simulations and
302 the empirical ground-motion models suggests that there are unmodelled correlations between the
303 key input parameters that lead to reduced variabilities in observed ground motions. This study
304 highlights once again the importance of accounting for variations in κ_0 within ground-motion
305 predictions, including when using empirical ground-motion models.

306 **Data and Resources**

307 All data generated in the simulations undertaken in this paper used information from published
308 sources listed in the references.

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417 **Table 1** Parameters of the Bora et al. (2017) stochastic model for Europe and the considered k_0
 418 distributions.

Parameter	Estimate of Parameter
Source Spectrum Model	Brune Point Source
Stress Drop ($\Delta\sigma$)	Mean = 5.65 MPa, Standard Deviation = $\log(0.33)$
Geometric Spreading	$R^{-1.14}$ for $R \leq 70$ km $R^{-0.50}$ for $R > 70$ km
Anelastic Attenuation (Q_0)	610 for $R \leq 40$ km 1152 for $R > 40$ km
Near-Source Shear Wave Velocity (β)	3500 m/s
Near-Source Density (ρ)	2800 kg/m ³
Sampled κ_0 Distributions*	B17: 0.0341 s, standard deviation 0.024 s (Bora et al., 2017 - k_0 model for Europe) C06: 0.0636 s, standard deviation 0.022 s (Chandler et al., 2006 - k_0 model for global application) E11: 0.0218 s, standard deviation 0.020 s (Edwards et al., 2011 - k_0 for foreland Switzerland)
Site V_{s30}	620 m/s

419 *The provided means and standard deviations are those for the sampled k_0 values used within the
420 ground-motion simulations, rather than the published means and standard deviations of the
421 considered k_0 distributions.

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423 **List of Figure Captions**

424 **Figure 1** (a) ϕ for PGA from the simulated ground-motions, (b) ϕ for PGA from the considered
425 GMPEs, (c) ϕ for SA(0.2 s) from the simulated ground-motions, (d) ϕ for SA(0.2 s) from the
426 considered GMPEs, (e) ϕ for SA(1 s) from the simulated ground-motions and (f) ϕ for SA(1 s) from
427 the considered GMPEs. B17 = Bora et al. (2017), C06 = Chandler et al. (2006) and E11 = Edwards
428 et al. (2011). Dashed lines indicate extrapolation of GMPE standard deviation beyond the model's
429 magnitude range.

430

431 **Figure 2** (a) Rate of change of ϕ with respect to magnitude for PGA, (b) rate of change of ϕ with
432 respect to magnitude for SA(0.2 s) and (c) rate of change of ϕ with respect to magnitude for SA(1
433 s). B17 = Bora et al. (2017), C06 = Chandler et al. (2006) and E11 = Edwards et al. (2011). Dashed
434 lines indicate extrapolation of GMPE standard deviation beyond the model's magnitude range of
435 applicability. The considered GMPEs with homoscedastic ϕ were not plotted. The Ameri et al.
436 (2017) GMPE was not plotted due to only τ being heteroscedastic with respect to magnitude.

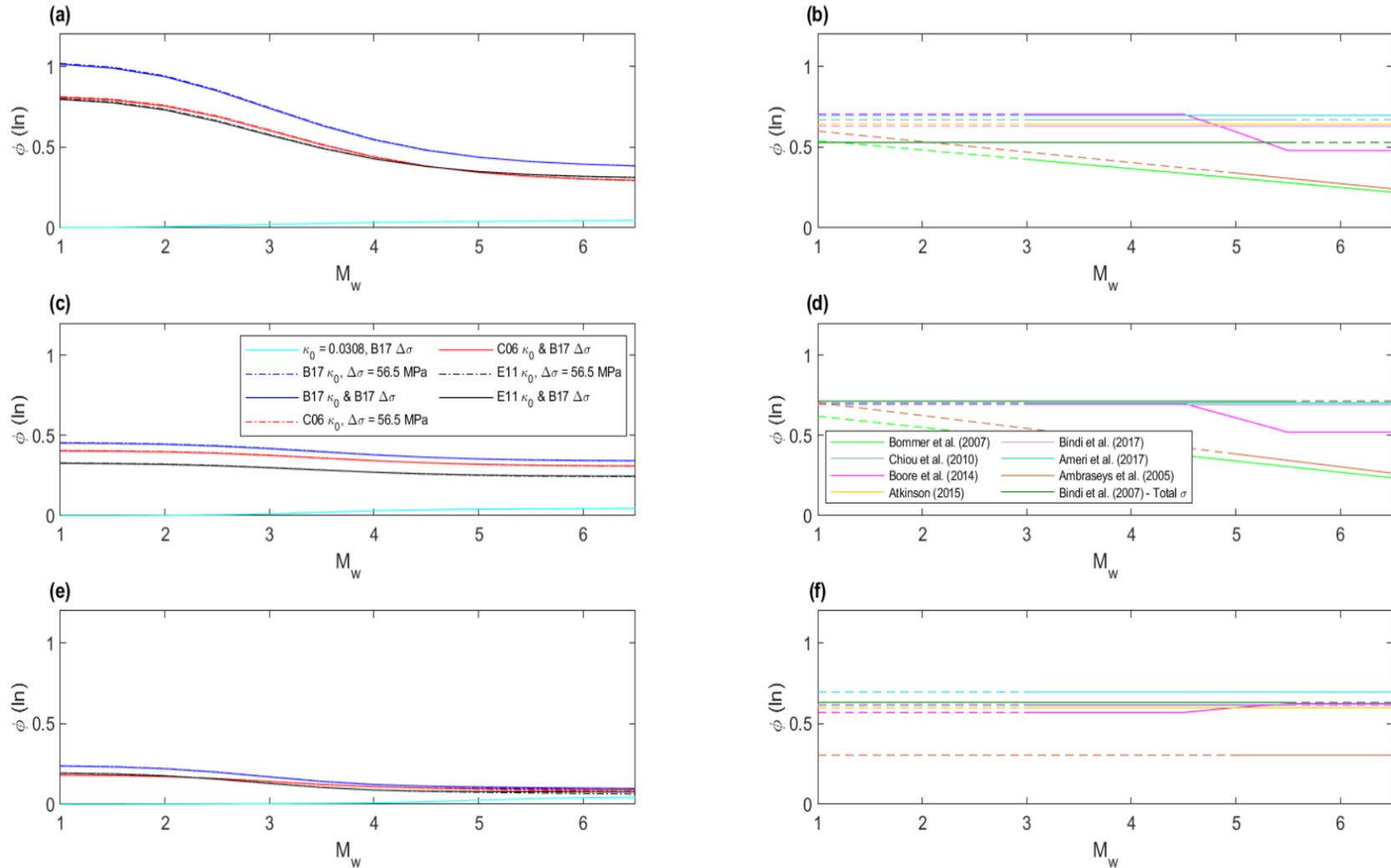


Figure 1 (a) ϕ for PGA from the simulated ground-motions, (b) ϕ for PGA from the considered GMPEs, (c) ϕ for SA(0.2 s) from the simulated ground-motions, (d) ϕ for SA(0.2 s) from the considered GMPEs, (e) ϕ for SA(1 s) from the simulated ground-motions and (f) ϕ for SA(1 s) from the considered GMPEs. B17 = Bora et al. (2017), C06 = Chandler et al. (2006) and E11 = Edwards et al. (2011). Dashed lines indicate extrapolation of GMPE standard deviation beyond the model's magnitude range.

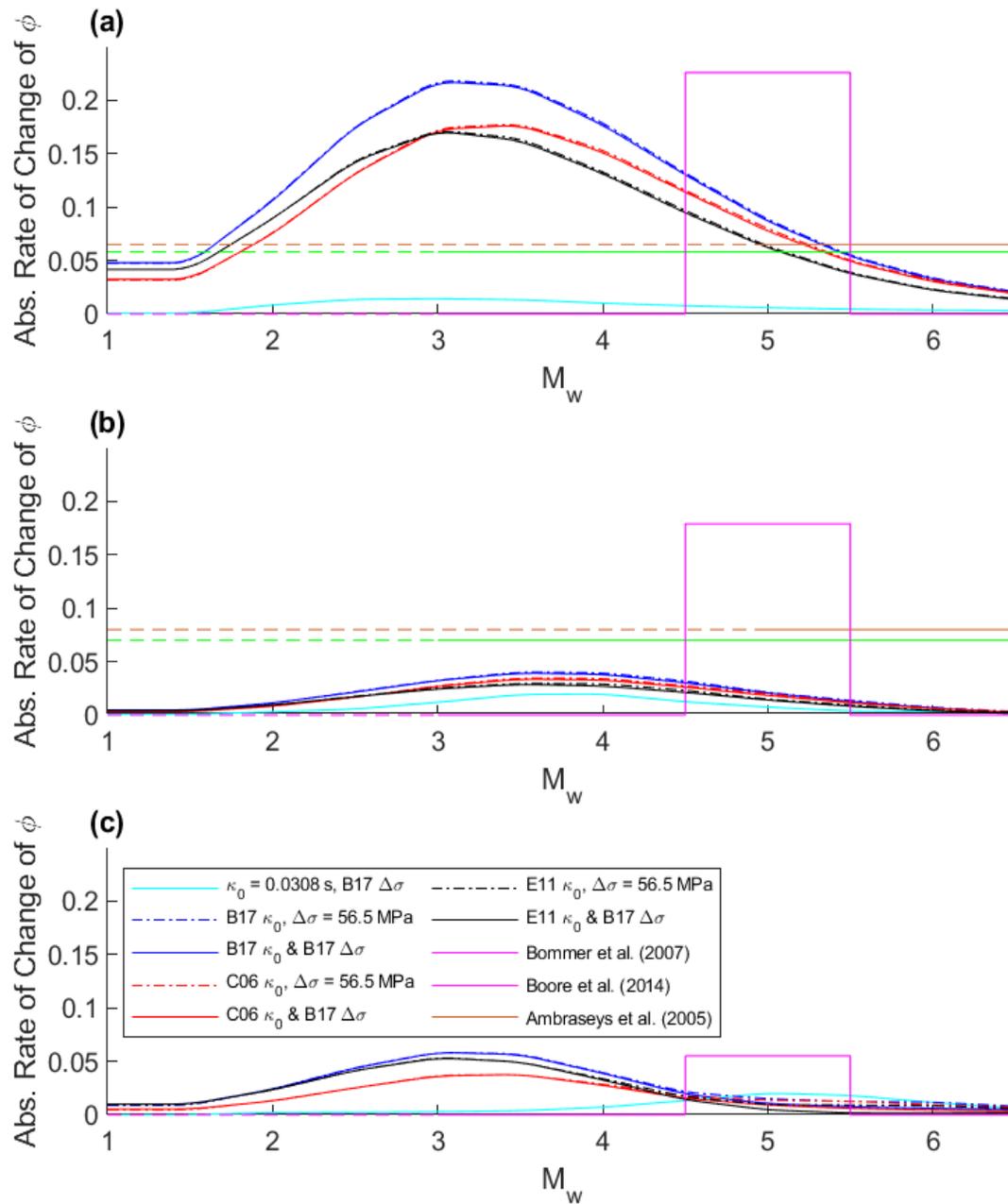


Figure 2 (a) Rate of change of ϕ with respect to magnitude for PGA, (b) rate of change of ϕ with respect to magnitude for $SA(0.2\text{ s})$ and (c) rate of change of ϕ with respect to magnitude for $SA(1\text{ s})$. B17 = Bora et al. (2017), C06 = Chandler et al. (2006) and E11 = Edwards et al. (2011). Dashed lines indicate extrapolation of GMPE standard deviation beyond the model's magnitude range of applicability. The considered GMPEs with homoscedastic ϕ were not plotted. The Ameri et al. (2017) GMPE was not plotted due to only τ being heteroscedastic with respect to magnitude.