

Scheduling Electric Vehicle Charging to Minimise Carbon Emissions and Wind Curtailment

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Abstract

This paper presents an investigation of the potential for coordinated charging of electric vehicles to i) reduce the CO₂ emissions associated with their charging by selectively charging when grid carbon intensity (gCO₂/kWh) is low and ii) absorb excess wind generation in times when it would otherwise be curtailed. A method of scheduling charge events that seeks the minimum carbon intensity of charging while respecting EV and network constraints is presented via a time-coupled linearised optimal power flow formulation, based on plugging-in periods derived from a large travel dataset. Schedules are derived using real half-hourly grid intensity data; if charging in a particular event can be done entirely through use of renewable energy that would otherwise have been curtailed, its carbon intensity is zero. It was found that if ‘dumb’ charged from the current UK mainland (GB) grid, average emissions related to electric vehicle (EV) charging are in the range 35-56 gCO₂/km; this can be reduced to 28-40 gCO₂/km by controlled charging – approximately 20-30% of the tailpipe emissions of an average new petrol or diesel car sold in Europe. There is potential for EVs to absorb excess wind generation; based on the modelled charging behaviour, 500,000 EVs (20% of Scotland’s current car fleet) could absorb around three quarters of curtailment at Scotland’s largest onshore wind farm.

Keywords: Electric vehicles, Renewable energy, Carbon intensity, Optimisation, Scheduling

1 Nomenclature

2 *Sets*

3 \mathcal{B} Buses, indexed by b

4	\mathcal{D}	Domestic loads, indexed by d
5	\mathcal{E}	Electric vehicle charging events, indexed by e
6	\mathcal{G}	Grid supply points, indexed by g
7	\mathcal{H}_b	Households connected to bus b
8	\mathcal{L}	Lines, indexed by l
9	\mathcal{T}	Time horizon comprised of ten-minutely timesteps, indexed by τ
10	\mathcal{V}_h	Set of electric vehicles at household h , indexed by v
11	<i>Parameters</i>	
12	B_l	Susceptance of line l
13	E_e^{\max}	Battery capacity in EV for charge event e
14	E_e^{start}	Energy storage content of EV at start of charge event e
15	E_e^{end}	Energy storage content of EV at end of charge event e
16	$P_{d,\tau}^{\text{D}}$	Active power demand from domestic load d in time period $[\tau, \tau+1]$
17	$P_{e,\tau}^{\text{E}}$	Active power demand from charge event e in time period $[\tau, \tau+1]$
18	P_e^{\max}	Max. charging power for EV in charge event e
19	S_l^{\max}	Active power capacity of a line l
20	V^{D}	Value of lost domestic load
21	V^{E}	Value of lost EV charging load
22	Γ	Cost of carbon emissions

23 *Variables*

24	$c_{g,\tau}^G$	Carbon intensity of grid supply point g at timestep τ
25	dE_e^{LHS}	Energy to be trimmed from beginning of charge event e
26	dE_e^{RHS}	Energy to be trimmed from end of charge event e
27	$E_{e,\tau}$	Energy storage content of EV in charge event e at timestep τ
28	$p_{d,\tau}^D$	Active power delivered to domestic demand d during time period
29		$[\tau, \tau + 1]$
30	$p_{e,\tau}^E$	Active power delivered to an EV e during time period $[\tau, \tau + 1]$
31	$p_{g,\tau}^G$	Active power from grid supply point g during time period $[\tau, \tau + 1]$
32	$p_{l,\tau}^L$	Active power flow on line l during time period $[\tau, \tau + 1]$
33	$SoC_{e,\tau}$	State of charge (per unit) of EV in charge event e at timestep τ
34	$t_e^s, t_e^{s'}$	Original start time of charge event e , adjusted start time of charge
35		event e
36	$t_e^d, t_e^{d'}$	Original departure time of charge event e , adjusted departure
37		time of charge event e
38	$t_e^{\gamma_e}, t_e^\infty, t_e^{\min}$	
39		Time at which the EV's SoC reaches γ_e in charge event e , time
40		at which the charging power reaches 1% of the maximum rated
41		power in charge event e , minimum of t_e^d and t_e^∞
42	$\delta_{b,\tau}$	Voltage angle at bus b during time period $[\tau, \tau + 1]$
43	γ_e	SoC at which the charging profile transitions from the constant
44		current to the constant voltage region in charge event e
45	λ_e	Decay constant of charging power applied during charge event e

46 *Abbreviations*

47	BM	Balancing mechanism
48	CC	Constant current
49	CV	Constant voltage
50	CP	Convex programming
51	ESO	Electricity system operator
52	EV	Electric vehicle
53	GB	Great Britain (referring to the largest island of the UK)
54	GIS	Geographical information systems
55	MILP	Mixed integer linear programming
56	NTS	National Travel Survey
57	OA	Output Area
58	RES	Renewable energy sources
59	SoC	State of charge (of an EV's battery)
60	V2G	Vehicle to grid

61 **1. Introduction**

62 *1.1. Motivation*

63 The transport sector made up a quarter – 8 Gigatonnes – of total world-
64 wide CO₂ emissions in 2016, over three quarters of which were from road
65 vehicles [1]. The World Health Organization estimates that 9 out of 10 peo-
66 ple worldwide are living under air that breaches safe limits [2]. While the
67 phasing out of fossil-fuelled vehicles in favour of plug-in battery electric ve-
68 hicles (EVs) is cited as a key part of the solution to both the decarbonisation
69 of the sector and the improvement of air quality by governments worldwide
70 from the UK [3] to China [4], Japan [5] and the USA [6], there has been
71 resistance to their adoption. Some of this has been due to the impression

72 that when charged from the power grid with its generation mix and associ-
73 ated carbon intensity, EVs do not offer any significant improvement in the
74 carbon emissions. This is perpetuated by studies such as [7] which claims
75 that, if charged from the German electricity system, electric vehicles (EVs)
76 are no ‘cleaner’ than diesel-powered vehicles. While the methods used in
77 [7] are under scrutiny and it has been shown in [8] that EVs have lower
78 associated carbon emissions than internal combustion engine vehicles when
79 charged from the electricity grids in any European Union member state, the
80 associated carbon emissions of EV charging should not be neglected. It is
81 suggested that the inherent flexibility of EV charging, given that the average
82 private car in the UK spends 96% of its time parked [9], has the potential
83 to interact positively with the grid in a way that optimises the use of re-
84 newable energy sources (RES). This paper presents an investigation of the
85 potential for EVs to i) reduce the CO₂ emissions associated with their charg-
86 ing by selectively charging when grid carbon intensity (gCO₂/kWh) is low
87 and ii) assist in further ‘greening’ the grid by using excess wind generation
88 in times when it would otherwise be curtailed due to lack of local demand
89 and transmission capacity to transport the power elsewhere.

90 *1.2. Relevant Literature*

91 The works reviewed in this section employ a wide range of techniques to
92 examine the potential integration of RES and EV charging via mathematical
93 optimisation. No matter the approach, they can be broadly divided into three
94 areas based on the objective function to be optimised: the maximisation of
95 RES output, the minimisation of RES curtailment (it is noted that while
96 framed differently, these two points are analogous) or the minimisation of
97 the associated carbon intensity of EV charging.

98 Works presented in [10], [11] and [12] all act to maximise RES output
99 within the setting of a microgrid or EV charging car park: effectively a single-
100 bus system with both RES generators and EV charging demand. In [10], the
101 authors present a mixed integer linear programming (MILP) approach to
102 minimise the total cost of supplying demand, given a time-varying generation
103 mix with intermittent RES output and a fixed assumption of the number of
104 EVs that make available a certain proportion of their batteries to be used
105 in a bidirectional energy exchange (also known as ‘Vehicle 2 Grid’ (V2G)).
106 Studies in [12] and [11] both present concepts of a charging station, where EVs
107 must queue to charge. While the methods used are different – the authors in

108 [12] formulate a Lyapunov optimisation, whereas a Markov decision process-
109 based approach is used in [11] – the objective functions in both papers are
110 formulated such that they are rewarded with increased use of RES (through
111 there being a lower cost of ‘dispatch’) and penalised with a longer queue
112 length. Whereas these microgrid/charging car park concepts certainly have
113 their applications, they are not suitable for the study of widespread EV
114 charging as the majority of which is expected to occur at private residencies
115 [13]. In [14], the authors use a MILP approach to simulate the operation
116 of an aggregator who is acting on the behalf of all EVs in a test network
117 to ensure they receive a pre-arranged quantity of energy during the time
118 during which the vehicle is available, subject to network constraints. The
119 aggregator’s objective is to minimise their own cost of buying energy for the
120 charging of EVs, which is at a minimum during times of maximum RES
121 output. While this approach is potentially an accurate reflection of how
122 large-scale demand response from EVs may arise, the study in [14] uses overly
123 simplistic assumptions as to when the EVs are plugged in and available, based
124 on a small survey in one town made by the authors. On the contrary, work
125 presented in this paper uses analysis from a large travel dataset to derive
126 individuals’ likely charging behaviour based on the energy requirements of
127 their travel habits.

128 In [15], the potential reduction in curtailment of wind energy generation
129 is calculated based on a future projection of the Danish energy system in
130 which 8 GW of wind power is installed and there are 500,000 EVs. All EVs
131 in the system are aggregated to form one charging profile, based on a sim-
132 ple assumption relating to typical commuting patterns. By controlling the
133 charging load via a heuristic method that seeks to maximise the utilisation
134 of wind power by charging, it is reported that curtailment can be reduced by
135 20%. Furthermore, [15] reports that the additional reduction in curtailment
136 from V2G approaches is insignificant, the total reduction from a controlled
137 V2G approach being 21%. In [16], the authors present analysis of the abil-
138 ity to reduce wind curtailment of six separate heuristic-based strategies for
139 controlled EV charging, reporting a reduction of wind curtailment from 13%
140 to 51% depending on the type of approach used. All strategies are tested
141 on the concept of a ‘nationwide battery’ active during the assumed charg-
142 ing period of 23:00-07:00, i.e. an aggregation of all the hypothetical EVs
143 served by the Dutch energy system – whose energy requirements are based
144 on average travel behaviour in the Dutch national travel survey – into one
145 flexible demand, similarly to the aggregation technique used in [15]. In [17],

146 the authors present optimisation of a MILP problem to minimise the cost of
147 generation given an availability of wind resource (with an associated dispatch
148 cost of zero) and a flexible EV charging demand. While the modelling of EV
149 charging demand in [17] is more sophisticated than in the aforementioned
150 works, based on five different hypothetical archetypes of EV charging relat-
151 ing to the speed at which the vehicles are to be charged, the model uses a
152 single aggregated load accounting for the total annual energy demand from
153 all of Germany’s projected 2030 EV fleet, an approach that fails to reflect
154 the diversity in drivers’ travel patterns and lacks detail compared with the
155 individual travel diary approach proposed in this paper.

156 Works that focus specifically on the carbon intensity of charging are rarer
157 than those that fit into the categories discussed in the preceding two sections.
158 In [18], the authors establish the likely carbon intensity of EV charging given
159 the average intensity (gCO_2/kWh) of the Danish electricity grid, though
160 there is no consideration of the flexibility of EV charging or scheduling of the
161 charging load. The study in [19] is similar but based on the GB electricity
162 system. Though the temporal variation in EV charging demand is considered,
163 it is assumed that an increase in demand as a result of EV charging will be
164 met by dispatchable generation and thus the resulting carbon intensity of EV
165 charging is equal to the carbon intensity of the dispatchable energy capacity
166 at a given time. Given the context of the GB system, this is composed of gas
167 and coal plants. In [20], the authors propose a convex programming (CP)
168 method to schedule EV charging to occur at the time of minimum grid carbon
169 intensity. In common with [14–17], it is suggested that the assumptions
170 regarding vehicles’ travel patterns are overly simplistic: it is assumed that
171 all vehicles are present between 17:00 and 08:00 the following morning, based
172 on the authors’ interpretation of a ‘typical’ working day. Furthermore, the
173 focus on plug-in hybrid EVs with battery capacities around 5 kWh limits the
174 effect that controlled charging can have, as the total flexibility is less than
175 if pure battery EVs with considerably larger battery capacities – such as in
176 this paper – are used. Although the primary goal in [17] is to maximise the
177 utilisation of wind power, it also presents the subsequent reduction in carbon
178 intensity of charging as a result of the optimisation; however, the results are
179 based on a constant grid intensity rather than a time series as presented in
180 this paper.

181 *1.3. Contribution*

182 A review of the relevant literature (section 1.2) has shown that while this
183 area of research is already well practised, there remain gaps in the collective
184 knowledge. This paper seeks to address these gaps as follows.

185 Firstly, whereas all of the works reviewed in section 1.2 use simplistic
186 assumptions regarding the temporal variation in EVs' availability based on
187 impressions of 'typical' driving patterns, this work uses a detailed simulation
188 of the possible plugging in habits of a representative fleet of EVs, using
189 two different models of charging behaviour to cover the possible spread in
190 charging event frequency and energy requirement.

191 Secondly, all but one of the works reviewed assume a constant grid carbon
192 intensity (the exception being [20], though they use a profile for only one
193 day, neglecting considerable day-to-day and seasonal variation resulting from
194 variations in demand and RES output). On the other hand, this work uses
195 half-hourly grid intensity data from the GB electricity system operator (ESO)
196 National Grid [21], and half-hourly curtailment data from Whitelee wind
197 farm [22], a large (539 MW) transmission-connected wind farm that is nearby
198 (< 15 km) to the simulated distribution network.

199 Thirdly, all the works reviewed consider fixed EV parameters, such as the
200 battery capacity and the charger power rating. However, it has been found
201 that this affects individuals' charging habits: for instance, in the *Electric*
202 *Nation*¹ EV trial that concluded in July 2019 [23] it was found that drivers
203 of EVs with larger battery capacities (> 35 kWh) are likely to charge less often
204 – on average, 2-3 times per week – compared to drivers of EVs with smaller
205 batteries (< 10 kWh) – on average, 5-6 times per week. These charging
206 behaviours determine the flexibility of EV charging and the times at which
207 the EVs are available to be charged. Consideration of these parameters is
208 therefore important; this work includes parametric study of how battery
209 capacity and charger power are likely to affect the ability of smart charging
210 to reduce the carbon intensity associated with EV driving.

211 The rest of this paper is organised as follows. Section 2 describes how
212 a model of a real distribution network is used to instantiate a fleet of EVs
213 with representative week-long travel diaries assigned to them from a large

¹The publicly-funded *Electric Nation* EV trial took place from January 2017 to December 2018 across various regions in the UK to provide data on EV charging habits for 673 vehicles comprising of 40 different models.

214 travel dataset. Section 3 describes how EV charge events ‘flexibility windows’
215 are derived from this fleet of EVs. Section 4 describes how grid carbon
216 intensity and wind curtailment are modelled. Section 5 describes how the
217 EVs’ charging is optimised to i) reduce the associated CO₂ emissions of their
218 charging and ii) reduce curtailment of Whitelee wind farm. Section 6 presents
219 the results for both studies. Conclusions and suggestions of further work from
220 this paper are made in section 7.

221 **2. Distribution Network and EV Fleet Modelling**

222 This section describes the method used to derive sets of EV charge events
223 based on the likely car-based transport energy requirements of residents
224 served by a given electricity network. To do this, geographical informa-
225 tion systems (GIS) data of a real distribution network is aligned with GIS
226 data from the 2011 UK Census to map the demographics of the area covered
227 by the network; in particular, the spatial distribution of vehicles within the
228 network and the indicative travel habits of the individuals who drive them.
229 Each vehicle is assigned a seven-day travel diary from the UK National Travel
230 Survey (NTS) based on the employment type and means of travel to work
231 of the driver. Using a heuristic method originally presented in [24], charging
232 schedules are derived using two models of charging behaviour designed to
233 cover the possible range of frequency and duration of charge events.

234 *2.1. Glasgow Southside Distribution Network*

235 The network model used to instantiate a fleet of EVs and to set con-
236 straints on their charging is derived from a real distribution network in the
237 residential-dominated Southside area of Glasgow, UK. The network consists
238 of a secondary (11/0.4 kV) substation and three 0.4 kV distribution feed-
239 ers. The network serves 157 households, spread amongst 47 endpoints (i.e.
240 there are some address points that are apartment blocks with multiple house-
241 holds). It is assumed that the different households are equally divided among
242 the three phases and that those phases are balanced. Figure 1 shows a plot
243 of the network topology with the location of the grid connection highlighted
244 (left) and a rendered 3D image of the area in question (right) – imagery from
245 Google Maps [25].



Figure 1: Glasgow Southside network used for instantiation of EV fleet (left) and rendered 3D image of area in question (right)

246 *2.2. Integration of Network Model with UK Census Data and National Travel*
 247 *Survey Travel Diaries*

248 In this study, a Monte Carlo-style approach is used to model uncertainties
 249 surrounding i) the demographics of the neighbourhood served by the network
 250 (Figure 1) – including the number of vehicles per household – and ii) the
 251 charging habits of the drivers of those vehicles.

252 *2.2.1. UK National Travel Survey Travel Diaries*

253 The UK NTS is conducted annually for around 15,000 residents in which
 254 they record all trips taken over a 7-day period [26]. The 7-day period recorded
 255 differs between the individuals recording the data, hence minimising any bias
 256 from seasonal effects and holidays. The resulting dataset for the years 2002-
 257 2016 as used in this study contains details of 2,042,058 car-based trips split
 258 between 126,186 week-long travel diaries, which have been aligned such that
 259 they all take place from 00:00 on Monday to 23:59 on Sunday. An example
 260 NTS travel diary is shown in Table 1.

Table 1: Example UK NTS travel diary (car-based trips)

Trip #	Origin	Destination	Trip Start	Trip End	Distance (miles)
1	Home	Food shop	Tu 09:30	Tu 09:50	3
2	Food shop	Home	Tu 10:40	Tu 11:00	3
3	Home	Other escort	Tu 18:15	Tu 18:20	0.25
4	Other escort	Home	Tu 18:20	Tu 18:25	0.25
5	Home	Other escort	Tu 19:40	Tu 19:45	0.25
6	Other escort	Home	Tu 19:50	Tu 19:55	0.25
7	Home	Food shop	W 09:30	W 09:50	3
8	Food shop	Home	W 10:30	W 10:45	3
9	Home	Work	Su 07:40	Su 08:00	7
10	Work	Home	Su 17:00	Su 17:20	7

261 Aside from filling in a travel diary, NTS respondents also answer some
 262 questions about themselves. In this study, the travel diaries are disaggregated
 263 on the basis of the individual’s employment type (employed, unemployed or
 264 self-employed) and their means of travel to work (car driver, car passenger,
 265 train, bus, bicycle, walk or N/A – i.e. unemployed/works from home). In
 266 accordance with UK Census data of the same fields, this is used to assign
 267 travel diaries to the fleet of EVs instantiated in the network that are likely
 268 to represent the travel habits of the individuals served by that network.

269 *2.2.2. 2011 UK Census Data*

270 The last completed Census in the UK was in 2011. The questions as
 271 used in this study are i) the number of vehicles at the household (0-4+),
 272 and ii) the employment type/means of travel to work (if applicable) – for ex-
 273 ample (employed, car driver), (self-employed, train) or (unemployed, N/A).
 274 Each busbar in the network is matched with its corresponding output area
 275 (OA), the smallest unit of Census data available covering approx. 50 house-
 276 holds, and hence distributions of responses to these two Census questions
 277 are returned. These distributions are used in a Monte Carlo-style approach
 278 (Algorithm 1) to instantiate a fleet of EVs and assign them with travel diaries
 279 – which, as already mentioned, have been disaggregated on the same basis –
 280 that are likely to represent the travel habits of the local population.

281 *2.2.3. Instantiation of EV Fleet in Network*

282 The network data and Census data are combined to create a fleet of EVs
 283 as described in Algorithm 1.

Algorithm 1 Instantiation of EV fleet based on study network Census data

```
1: for each  $b$  in  $\mathcal{B}$  do  
2:   Return set  $\mathcal{H}_b$  of households connected at  $b$   
3:   Return Census distributions of car/van availability and economic activity/means  
   of travel to work in corresponding OA  
4:   for each  $h$  in  $\mathcal{H}_b$  do  
5:     Assign domestic demand profile (section 2.3)  
6:     Sample distribution; return set  $\mathcal{V}_h$  of EVs at  $h$   
7:     for each  $v$  in  $\mathcal{V}_h$  do  
8:       Sample distribution; return economic activity/means of travel to work of  
       EV driver  
9:       Assign NTS travel diary of car-based trips
```

284 The approach in Algorithm 1 is repeated as a Monte Carlo-style simula-
285 tion for 100 trials. This is described further in section 4.1.

286 2.3. Domestic Demand Modelling

287 It is assumed in this study that domestic demand (i.e. that which exists
288 before the introduction of EVs) has zero flexibility. In this study, a higher-
289 order Markov chain based household energy demand model from [27] is used
290 to synthesise likely demand profiles for the domestic premises in the distri-
291 bution network. The model simulates household electricity demand based
292 on the active occupancy of households, derived from analysis of the results
293 of the UK Time Use Survey – a large-scale household survey of more than
294 20,000 individuals that aims to shed light on how people in the UK spend
295 their time [28]. The reader is directed to [27] for detailed information on
296 the domestic demand tool used in this study. Figure 2 shows the simulated
297 domestic demand for all households in this network for 100 trials, whereby
298 each trial represents the establishment of household characteristics as per Al-
299 gorithm 1. All trials were based on a winter weekday, as to reflect the peak
300 demand on the system and the ‘worst case’ as planned for by the distribution
301 network operator.

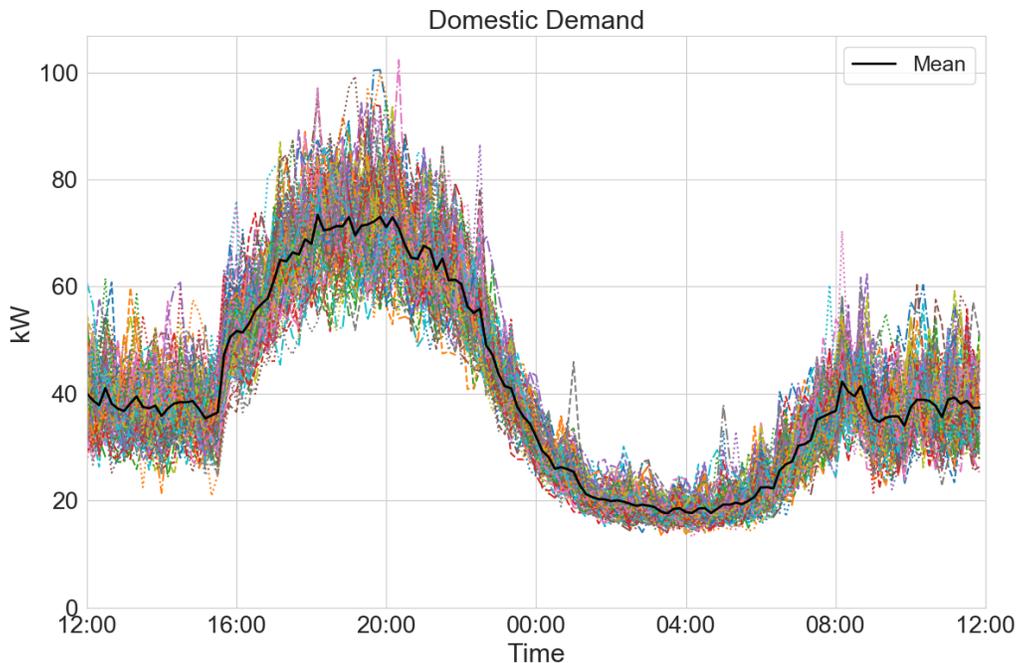


Figure 2: Domestic demand (kW) simulated for study network, 100 trials – mean demand across all trials shown as a black solid line

302 **3. Electric Vehicle Charge Event Modelling**

303 One of the most challenging aspects regarding modelling future electrified
 304 transport scenarios is the impact of human behaviour, including how individ-
 305 uals decide to schedule charge events. The frequency and duration of charge
 306 events, in addition to their energy requirement, determines the flexibility of
 307 EV charging and the extent to which their charging can be managed to seek
 308 the optimisation of some objective function.

309 Two methods are used to derive schedules of charge events from the NTS
 310 travel diaries (e.g. Table 1), designed to represent the spectrum of likely
 311 charging behaviours. These methods are described in sections 3.1-3.2.

312 *3.1. Minimal Charging Schedules*

313 The minimal charging schedules represent a scenario in which EV charg-
 314 ing is seen by users as an inconvenience, and therefore something that they
 315 would aim to minimise. They are derived using a heuristic originally pre-
 316 sented in the author’s earlier work [24]. In summary, the method returns

317 the minimum number of charge events required to satisfy the energy require-
 318 ments of an NTS travel diary (Table 1), choosing parked charging events first
 319 and resorting to en route charging events only when parked charging oppor-
 320 tunities are not sufficient to meet the travel diary’s energy requirements.
 321 This is done by ensuring that the vehicle’s state of charge (SoC) is always
 322 greater than or equal to a prescribed minimum; that which would give 25
 323 km of remaining range on a ‘combined’ energy consumption rate, based on
 324 how far a prudent driver would be willing to drive before charging. While
 325 the EV will minimise the time spent en route charging, gaining only enough
 326 energy it needs to arrive at the end of the trip with the minimum permitted
 327 SoC, it will seek to gain the maximum it can from any parked charging event
 328 – subject to the charger power and a standard Lithium-ion battery charging
 329 curve as further discussed in section 3.4.

330 The reader is referred to [24] for a detailed explanation of how this heuris-
 331 tic works. As an example, Table 2 shows a schedule of the minimum number
 332 of charge events necessary to meet the energy demand of the travel diary
 333 shown in Table 1. The SoC with which the vehicle starts the travel diary
 334 is randomised between the prescribed minimum and 100%. In this example
 335 case, it was randomised as 74%.

Table 2: Minimal charging schedule derived from NTS travel diary in Table 1 for an EV with a battery capacity of 24 kWh and a home charger rated at 3.7 kW AC, 88% efficiency

Trip #	Charge Type	Plug-in	Plug-out	E^{start} (kWh)	E^{end} (kWh)	P^{max} (kW)
8	home	W 10:45	Su 07:40	8.44	24	3.26

336 In Table 2, E^{start} and E^{end} are the energy storage contents of the EV at
 337 the start and end of the charge events respectively. P^{max} is the maximum
 338 rated DC power the EV can be charged at. Note that the AC charger rating
 339 (in this case, 3.7 kW) is multiplied by a one-way AC/DC converter efficiency
 340 of 88%, in common with empirical results presented in [29].

341 Table 2 shows that the EV was able to charge sufficiently to meet the
 342 energy requirements of its travel diary with one parked charging event taken
 343 at home at the end of trip 8. Note that although the EV could have charged
 344 after trips 2, 4 and 6, the driver chose not to as they could defer their
 345 charging until later in the week, thus finishing the week’s travel diary with
 346 the maximum possible SoC.

347 *3.2. Routine Charging Schedules*

348 The routine charging schedules represents a scenario in which EV charging
 349 at home is seen to carry negligible inconvenience (i.e. it has become routine)
 350 such that vehicles are always plugged in on arrival at home, irrespective of
 351 their SoC. Therefore, this section presents a modification to the heuristic
 352 described in [24], in that an EV will always charge at home, regardless of
 353 its SoC or the energy demand of future trips. The routine schedule could
 354 represent a scenario where individuals are incentivised to plug their vehicles
 355 in, for example if they are to be used as a flexible resource for the benefit of
 356 the grid.

357 Table 3 shows a schedule of charge events produced using the routine
 358 charging method for the NTS travel diary in Table 1.

Table 3: Routine charging schedule derived from NTS travel diary in Table 1 for an EV with a battery capacity of 24 kWh and a home charger rated at 3.7 kW AC, 88% efficiency

Trip #	Charge Type	Plug-in	Plug-out	E^{start} (kWh)	E^{end} (kWh)	P^{max} (kW)
2	home	Tu 11:00	Tu 18:15	10.36	24	3.26
4	home	Tu 18:25	Tu 19:40	23.86	24	3.26
6	home	Tu 19:55	W 09:30	23.86	24	3.26
8	home	W 10:45	Su 07:40	22.36	24	3.26

359 In Table 3, the EV charges at all the opportunities it gets: in this example,
 360 whereas it did not charge after trips 4, 6 and 8 under the minimal scenario,
 361 it did charge after these trips in the routine scenario. As a result, its energy
 362 requirements for these charge events tends to be less. Given that the total
 363 charging time is dictated by the duration of the parking event, charging under
 364 the routine method of charge event scheduling is typically more flexible than
 365 charging under the minimal method.

366 *3.3. Validation against Electric Nation Trial Data*

367 As already mentioned in section 1.3, it was found in the *Electric Nation*
 368 trial that drivers with larger batteries are likely to plug in on fewer occasions.
 369 The data collected in the trial in terms of average charging frequency per
 370 day, as taken from [23], is shown on a scatter plot in Figure 3 along with the
 371 average home charging frequency per day for all trials of all vehicles simulated
 372 with the minimal charging model in this study for both 24 kWh and 64 kWh
 373 battery capacities.

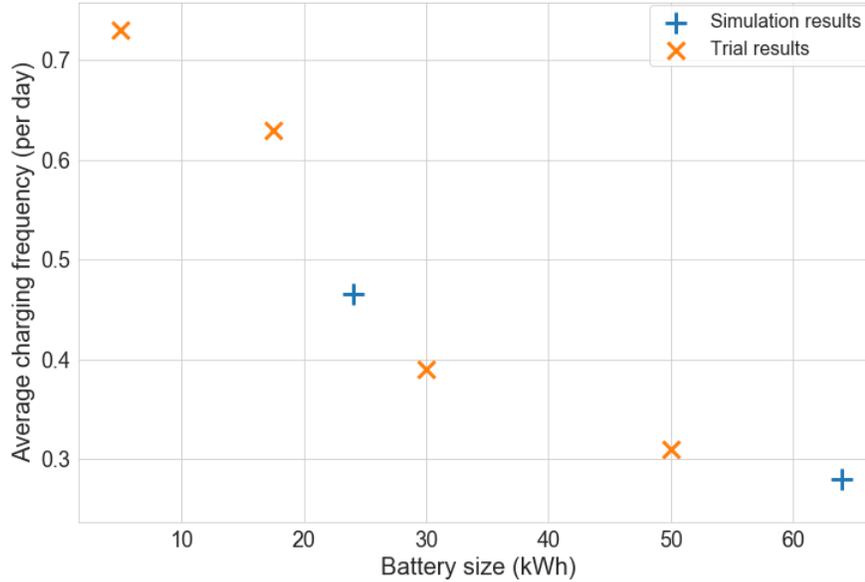


Figure 3: Scatter plot showing average charging frequency (events per day) against vehicle battery size for *Electric Nation* trial data and results from the simulation (minimal charging) in this study

374 Note that the battery sizes used for the *Electric Nation* data in Figure 3
 375 are the midpoints of the intervals reported, e.g. where the project reported
 376 that EVs with batteries of 10-25 kWh charged on average 0.63 times per day,
 377 the corresponding value used for the figure is 17.5 kWh.

378 Figure 3 shows that the pattern of a reduction in charging frequency for
 379 increasing battery size holds true for the simulation in this study when using
 380 the minimal charging scenario. Note that when using the routine charging
 381 method, the frequency of home plug-ins will not change as drivers will always
 382 plug-in at home; their charging frequency will be equal to the average number
 383 of times they arrive at home in a day.

384 3.4. Charging Flexibility Window

385 The optimisation performed in this study is carried out on the basis of one
 386 24 hour period in 10 minute timesteps, from midday to midday the next day.
 387 However, the charging schedules produced on the basis of a week-long travel

388 diary are 7 days long. Therefore, the week-long charge schedules are trimmed
 389 accordingly to establish a ‘flexibility window’ for each charging event that
 390 fits into the 24 hour window of the optimisation study. The process by which
 391 this is done is illustrated in Figure 4.

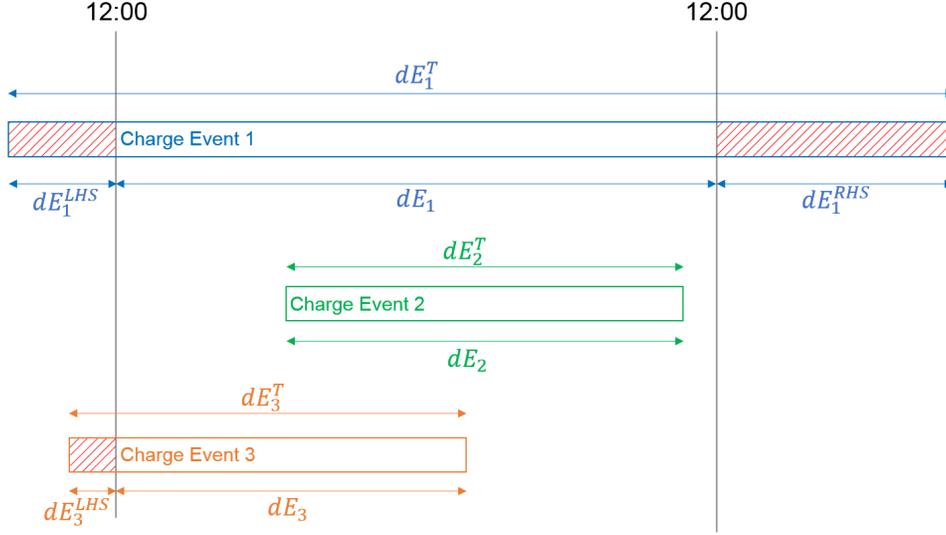


Figure 4: Illustrative example of charging flexibility window concept, showing how 7-day charging schedules are trimmed to 1-day charging flexibility windows for optimisation

392 Figure 4 illustrates how charge events are modified. Upon selection of the
 393 24 hour window within the 7-day long charging schedule, any charge events
 394 that are completely outside of the 24 hour window are discarded. Any that
 395 overlap the beginning and/or the end of the 24 hour window (e.g. Charge
 396 Events 1 and 3 in Figure 4) are trimmed accordingly as per (1), such that
 397 only the energy that would ordinarily have been delivered during the 24 hour
 398 window – under a ‘dumb’ charging schedule – is accounted for.

$$dE_e = dE_e^T - (dE_e^{LHS} + dE_e^{RHS}) \quad (1)$$

399 where dE_e^T is the total energy received by the vehicle during charging event
 400 e , dE_e is the trimmed energy, dE_e^{LHS} is the energy to be trimmed from the
 401 charge event e overlapping the start of the 24 hour window and dE_e^{RHS} is the
 402 energy to be trimmed from the charge event e overlapping the end of the 24
 403 hour window.

404 The energy that is to be trimmed from these charge events is calculated
 405 by consideration of a standard constant current-constant voltage (CC-CV)
 406 charging profile of a Lithium-ion battery, as used in [24, 29–34]. The resulting
 407 expressions for the calculation of dE_e^{LHS} and dE_e^{RHS} are given in (2). For the
 408 derivation of these expressions, the reader is referred to [24].

$$dE_e^{\text{LHS}} = \frac{\max\{0, (t_e^{\gamma_e} - t_e^s)\}}{(t_e^{\gamma_e} - t_e^s)} \int_{t_e^s}^{t_e^{\gamma_e}} P_e^{\text{max}} dt +$$

$$\frac{\max\{0, (t_e^{s'} - t_e^{\gamma_e})\}}{(t_e^{s'} - t_e^{\gamma_e})} \int_{t_e^{\gamma_e}}^{t_e^{s'}} P_e^{\text{max}} e^{-\lambda_e t} dt \quad (2a)$$

$$dE_e^{\text{RHS}} = \frac{\max\{0, (t_e^{\gamma_e} - t_e^d)\}}{(t_e^{\gamma_e} - t_e^d)} \int_{t_e^d}^{t_e^{\gamma_e}} P_e^{\text{max}} dt +$$

$$\frac{\max\{0, (t_e^{d'} - t_e^{\gamma_e})\}}{(t_e^{d'} - t_e^{\gamma_e})} \int_{t_e^{\gamma_e}}^{t_e^{\min}} P_e^{\text{max}} e^{-\lambda_e t} dt \quad (2b)$$

409 where t_e^s is the original start time of the charge event e , $t_e^{s'}$ is the adjusted
 410 start time of the charge event e (i.e. the start of the 24 hour window),
 411 t_e^d is the original departure time of charge event e and $t_e^{d'}$ is the adjusted
 412 departure time of the parking event following trip e (i.e. the end of the 24
 413 hour window). $t_e^{\gamma_e}$ is the time at which the EV's SoC reaches γ_e , the point
 414 at which the charging profile transitions from the CC to the CV region for
 415 charge event e – taken in this study to be 0.8, as shown in Figure 8. λ_e is the
 416 decay constant associated with the CV region. t_e^∞ is the time at which the
 417 charging power reaches a value close to zero (taken as 1% of the maximum
 418 rated power) and the charger switches off on account of the vehicle's battery
 419 being full. t_e^{\min} is the minimum of t_e^d and t_e^∞ (3).

$$t_e^{\min} = \min\{t_e^d, t_e^\infty\} \quad (3)$$

420 4. Grid Carbon Intensity and Wind Curtailment Modelling

421 4.1. Grid Carbon Intensity

422 Half-hourly carbon intensity data for the GB grid was obtained from
 423 National Grid [21]. Table 4 shows the assumed carbon intensity of each
 424 generation type, which is used by National Grid to calculate the carbon
 425 intensity based on the generation mix per half-hour settlement period.

Table 4: Carbon Intensity and generation by fuel type from 1 June 2018 to 31 May 2019; data: [21, 22]

Fuel Type	Carbon Intensity (gCO₂/kWh)	Generation (TWh)	Generation (%)
Gas – Combined Cycle	394	115.3	41.0
Gas – Open Cycle	651	0.01	0.0
Wind	0	41.08	14.6
Hydro	0	5.3	1.9
Coal	937	9.7	3.4
Nuclear	0	57.1	20.3
Dutch Imports	474	6.7	2.4
French Imports	53	12.8	4.6
Irish Imports	458	1.8	0.7
Solar	0	11.5	4.1
Biomass	120	17.1	6.1
Other	300	2.8	1.0
Total	-	281	-

426 Based on the data in Table 4, the average GB grid carbon intensity for
 427 1 June 2018 to 31 May 2019 is estimated at 221 gCO₂/kWh. This figure
 428 continues the significant reduction in carbon intensity from 469 g/kWh (com-
 429 bustion only) for the UK in 2013 [8], to under 350 g/kWh in 2015 [35]. To
 430 meet UK government targets for decarbonisation, these trends must continue
 431 to be in line with the Committee on Climate Change (CCC) target of below
 432 200g/kWh for 2020 to below 100 g/kWh in 2030 [36].

433 In this study, a Monte Carlo-based method is used to conduct the analysis
 434 for 100 trials, i.e. 100 simulated fleets of EVs, each based on a run of the
 435 method shown in Algorithm 1, with 100 sets of resulting charging schedules.
 436 Each trial, in which a 24 hour period of the EVs’ charging schedules are
 437 optimised for minimal carbon intensity, is conducted over a matching 24
 438 hour period of carbon intensity data. The grid carbon intensity of the 100 24
 439 hour periods as used in this study were selected randomly from the period 1
 440 June 2018 to 31 May 2019 (Figure 5).

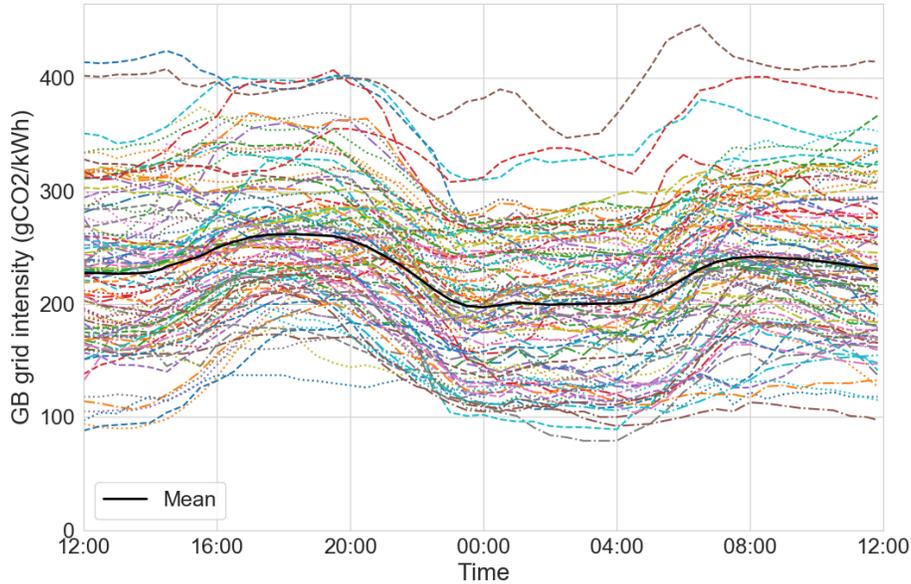


Figure 5: Half-hourly GB grid carbon intensity (gCO_2/kWh) for 100 randomly selected weekdays in the period 1 June 2018 to 31 May 2019

441 Figure 5 shows significant variation in the grid carbon intensity, ranging
 442 from $79 \text{ gCO}_2/\text{kWh}$ at 04:00 on 23 August 2018 to $447 \text{ gCO}_2/\text{kWh}$ at 07:00
 443 on 23 January 2019. The mean carbon intensity value at each settlement
 444 period is shown to be lower in the night-time (22:00-05:00) than in the day.
 445 This is an important result, as EV charging is generally more likely to be
 446 done overnight as people are parked at home [37].

447 4.2. Wind Curtailment

448 Whitelee wind farm is a 215-turbine, 539 MW onshore wind farm near
 449 Eaglesham, approximately 15 km to the south of Glasgow. Wind generation
 450 in Scotland is curtailed if exports from Scotland exceed the capacity of the B6
 451 boundary – the transmission corridor between Scotland (which usually runs a
 452 generation surplus) and England (which usually runs a deficit). During these
 453 times, the wind farm’s output is curtailed at an average cost of $\text{£}70/\text{MWh}$
 454 (based on the average bid price from [22]). Whitelee represented 11.5% of
 455 total Scottish wind farm curtailment from 1 June 2018 to 31 May 2019.

456 The wind farm and test network are in close proximity; electrically, they are
 457 connected by 275 and 132 kV transmission lines. It is assumed that these
 458 have sufficient capacity headroom to allow increased demand from Glasgow
 459 (as a result of EV charging) to be balanced by curtailed wind energy from
 460 Whitelee (Figure 6, adapted from [38]). Therefore, for any period in the
 461 100 days represented in Figure 5 in which there was also curtailment at
 462 Whitelee, the grid carbon intensity for that period was set to 0 gCO₂/kWh
 463 – in accordance with the methodology used in [21].

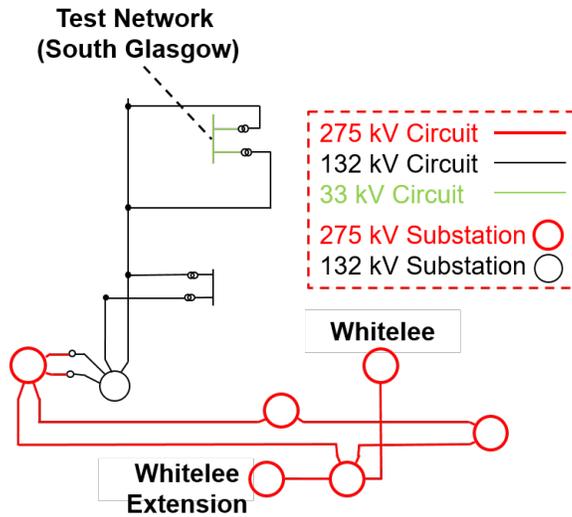


Figure 6: Network diagram from Whitelee wind farm to the test network in the south side of Glasgow, adapted from [38]. Note: Sections of the electrical line diagram have been removed to focus on the connection between Whitelee and the test network location.

464 Half-hourly curtailment data for the Whitelee wind farm was obtained
 465 from the Elexon Balancing Mechanism Reports [22]. Out of 365 days from 1
 466 June 2018 to 31 May 2019, 112 (31%) saw some curtailment. Figure 7 shows
 467 the total curtailment by half-hour settlement period (left) and a histogram of
 468 daily curtailment volumes (right) for Whitelee wind farm during that period.

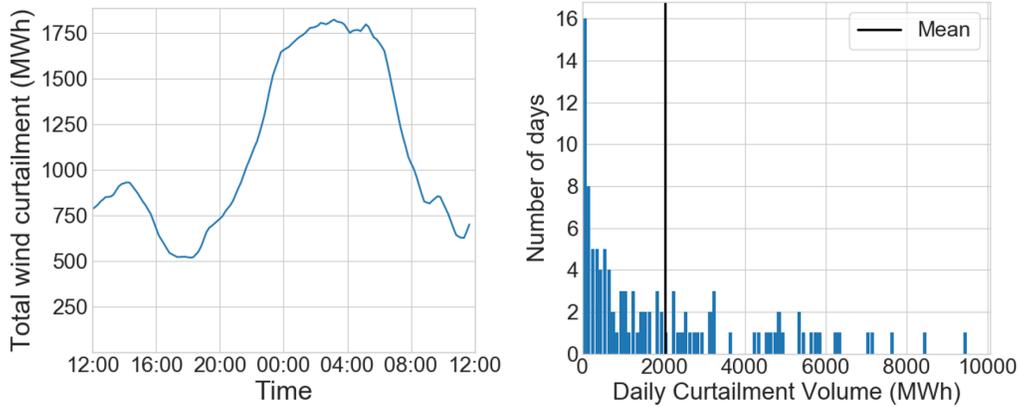


Figure 7: Total wind curtailment volumes by half-hour settlement period (left) and histogram of daily wind curtailment volumes (right) of Whitelee wind farm for 112 days where generation was curtailed, 1 June 2018 to 31 May 2019 (bin width = 100 MWh)

469 Figure 7 shows that more generation was curtailed at night than in the
 470 afternoon and evening, likely due to the sum of domestic and industrial
 471 demand being higher in the afternoon/evening than at night. As was the case
 472 for carbon intensity, this is an important result as EV charging is generally
 473 more likely to be done overnight. Figure 7 also shows that the mean daily
 474 curtailment on the 112 days in the year that saw some curtailment was 2030
 475 MWh. The total curtailment of Whitelee wind farm through the year was
 476 227,841 MWh which, at Whitelee’s average bid price of £70/MWh, gives a
 477 potential value of absorbing this curtailment through EV charging of up to
 478 £15.9m².

479 5. Optimal EV Charging

480 In this section, an optimisation model is presented that aims at providing
 481 an optimal schedule for EV charging – i.e. that which maximises charging
 482 at times of minimum CO₂ intensity – whilst respecting network constraints
 483 and meeting required energy demand of EVs within their flexibility windows
 484 (section 3.4).

²The total cost of the B6 constraint would be the sum of the cost of accepted bids to reduce output and offers to replace it on the other side of the boundary. Therefore, this value is likely to be an under-estimate of the true value of absorbing this curtailment as it does not include the cost of accepted offers.

485 *5.1. Power Flow*

486 The power balance equation is given as (4), $\forall b \in \mathcal{B}, \tau \in \mathcal{T}$:

$$\sum_{g \in \mathcal{G}} p_{g,\tau}^{\text{G}} = \sum_{e \in \mathcal{E}} p_{e,\tau}^{\text{E}} + \sum_{d \in \mathcal{D}} p_{d,\tau}^{\text{D}} + \sum_{l \in \mathcal{L}} p_{l,\tau}^{\text{L}} \quad (4)$$

487 where \mathcal{B} is the set of busbars in the network, \mathcal{T} is the time horizon (the set
 488 of 10 minute timesteps indexed by τ), \mathcal{E} is the set of charge events across all
 489 EVs in the fleet, \mathcal{D} is the set of domestic demands (i.e. one per household)
 490 and \mathcal{L} is the set of lines in the network. $p_{g,\tau}^{\text{G}}$ is the active power contribution
 491 from the grid supply point g in the time period $[\tau, \tau + 1]$, $p_{e,\tau}^{\text{E}}$ is the active
 492 power drawn by an EV in charge event e to charge its battery in the time
 493 period $[\tau, \tau + 1]$, $p_{d,\tau}^{\text{D}}$ is the active power drawn by domestic demand d in the
 494 time period $[\tau, \tau + 1]$ and $p_{l,\tau}^{\text{L}}$ is the active power flow on line l in the time
 495 period $[\tau, \tau + 1]$.

496 The power flow equations are given as (5a-5b), $\forall l \in \mathcal{L}, \tau \in \mathcal{T}$:

$$p_{l,\tau}^{\text{L}} = -\text{B}_l (\delta_{b,\tau} - \delta_{b',\tau}) \quad (5a)$$

$$-\text{S}_l^{\text{max}} \leq p_{l,\tau}^{\text{L}} \leq \text{S}_l^{\text{max}} \quad (5b)$$

497 where B_l and S_l^{max} are the susceptance and rating respectively of line l , and
 498 $\delta_{b,\tau}$ and $\delta_{b',\tau}$ are the voltage angles at b and b' , denoting the busbars at either
 499 end of line l , in the time period $[\tau, \tau + 1]$.

500 *5.2. EV Charging Model*

501 The energy storage content of an EV $E_{e,\tau}$ during charge event e at
 502 timestep τ is related to that in the previous timestep and the energy gained
 503 in the time period $\Delta\tau = [\tau, \tau + 1]$ (10 minutes) by (6).

$$E_{e,\tau} = p_{e,\tau}^{\text{E}} \Delta\tau + E_{e,\tau-1} \quad (6)$$

504 The power drawn by an EV is constrained by a CC-CV charging profile
 505 (Figure 8) typical of lithium ion batteries [24, 29–34], in which the maximum
 506 charging power is equal to the rated power P_e^{max} for a battery SoC up to γ_e ,
 507 after which it linearly decreases to zero at an SoC of 1. In this work, γ_e is set
 508 to 0.8 in accordance with a real lithium ion battery charging profile from an
 509 ABB charger as presented in [31]. The charging power constraint is stated
 510 formally in (7), $\forall \tau \in \mathcal{T}$

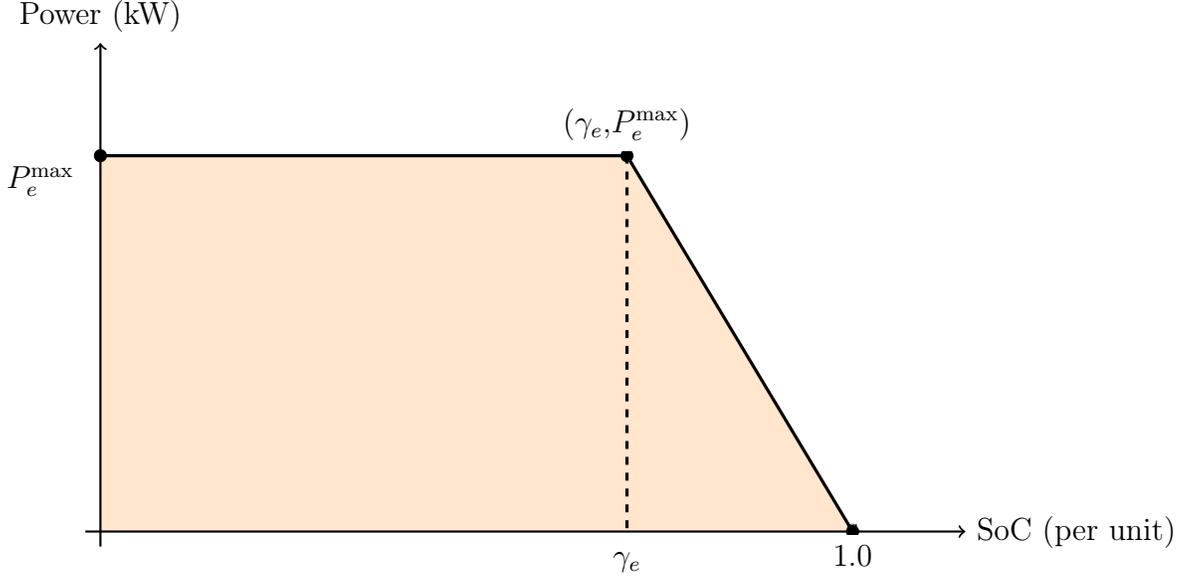


Figure 8: EV charging power constraint as a function of battery SoC

$$p_{e,\tau}^E \leq \begin{cases} P_e^{\max}, & SoC_{e,\tau} \leq \gamma_e \\ \left(\frac{1 - SoC_{e,\tau}}{1 - \gamma_e} \right) P_e^{\max}, & SoC_{e,\tau} > \gamma_e \end{cases} \quad (7)$$

511 where $SoC_{e,\tau}$ is the state of charge of an EV e at timestep τ , calculated as
 512 in (8).

$$SoC_{e,\tau} = \frac{E_{e,\tau}}{E_e^{\max}} \quad (8)$$

513 where E_e^{\max} is the EV's battery capacity in charge event e .

514 5.3. Objective Function

515 The goal of the optimisation is to minimise the objective function (9):
 516 the sum of the cost of CO₂ emissions plus the sum of the cost of not meeting
 517 any demand, both domestic and from EV charging. Although the values of
 518 lost domestic load and lost transport energy are likely to be different, in this

519 work the values of lost load V^D and V^E are both taken as £17,000/MWh³ in
520 accordance with the value published by London Economics for the Depart-
521 ment of Energy & Climate Change and Ofgem [39]. The cost of emissions
522 is given by the total emissions in kg multiplied by a cost per kg Γ – in this
523 work, the UK carbon floor price (2018-2021) of £18/tonne (£0.018/kg) [40]
524 is used.

$$\min \sum_{\tau \in \mathcal{T}} \left(\underbrace{\sum_{g \in \mathcal{G}} \Gamma c_{g,\tau}^G p_{g,\tau}^G}_{\text{Cost of } CO_2 \text{ emissions}} + \underbrace{\sum_{d \in \mathcal{D}} V_d^D (P_{d,\tau}^D - p_{d,\tau}^D)}_{\text{Cost of shedding domestic load}} + \underbrace{\sum_{e \in \mathcal{I}} V_e^E (P_{e,\tau}^E - p_{e,\tau}^E)}_{\text{Cost of shedding EV demand}} \right) \Delta\tau \quad (9)$$

525 where $c_{g,\tau}^G$ is the grid carbon intensity of grid supply point g during the time
526 period $[\tau, \tau + 1]$. $P_{d,\tau}^D$ is the active power demand from domestic demand d
527 during the time period $[\tau, \tau + 1]$; $P_{e,\tau}^E$ is the active power demand from EV
528 charging event e during the time period $[\tau, \tau + 1]$.

529 The objective function in (9) is minimised subject to the constraints in
530 (4-8). The problem is solved using the CPLEX solver using OATS [41] opti-
531 misation software.

532 5.4. Justification of Linearised Optimal Power Flow Formulation

533 It is generally acknowledged that a full AC power flow formulation is re-
534 quired to reliably report results for distribution networks given the significant

³In reality, it would be reasonable to expect that these values would be quite different, due to the variation in consumers' willingness to pay for domestic electricity (which would vary depending on which appliance was being used, when it was being used and, of course, by whom) and transport, which would also be expected to vary significantly in time depending on when any period of lost load would occur relative to tasks that would be deemed important to the consumer. However, as in this study the network was able to serve all load within thermal limits under the DC power flow assumptions, any relative difference in these values would have zero effect on the results presented.

535 line impedances and consequential variation in voltage magnitudes and an-
 536 gles [42]. To reduce the computational burden of the Monte Carlo approach
 537 used in this study, the linearised approach detailed in sections 5.1-5.3 was
 538 applied. To check the suitability of the approach, the resulting controlled
 539 EV charging profiles were input as loads to an AC load flow. The minimum
 540 endpoint voltage for all endpoint busbars in the network recorded over the
 541 24 hour period modelled for each combination of EV parameters, for both
 542 minimal and routine charging schedules, is shown in Figure 9. Across 100
 543 trials, the mean of the minimum voltages for each endpoint is shown by the
 544 marker and the 95% confidence interval is shown by the error bars on each
 545 side.

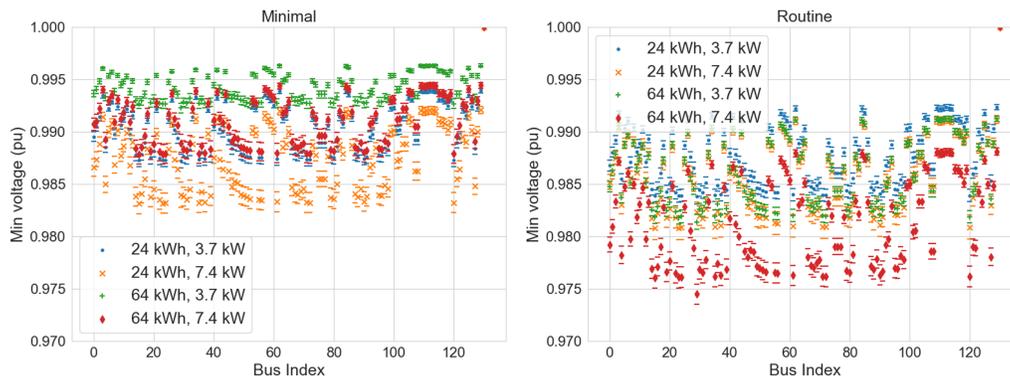


Figure 9: Minimum endpoint voltage resulting from controlled EV charging schedules and domestic loading, all combinations of EV parameters – minimal (left) and routine (right) charging behaviour

546 Figure 9 shows the variation in voltage stress placed on the network by
 547 different EV parameter combinations and charging scheduling models; these
 548 patterns are further discussed in section 6.1. It should be noted that no
 549 matter the variation, all voltages are within statutory GB limits of +10/-
 550 6%.

551 5.5. Carbon Intensity Minimisation

552 The optimisation described in sections 5.1-5.3 is performed for the 100 24-
 553 hour periods as shown in Figure 5. For each 24-hour period, a different set of
 554 generated household demand profiles (Figure 2) and EV charge events (based
 555 on the instantiation of EVs and travel diaries in the network as per Algorithm

556 1) is used. The resulting seven day charging schedules were trimmed to
557 ‘charging flexibility windows’ as per the method described in section 3.4. By
558 performing the optimisation, the EVs’ charging demand is shifted to times of
559 minimal carbon intensity where their flexibility windows and the constraints
560 in (4-7) allow. The same analysis is carried out for four different combinations
561 of EV battery capacity (24 kWh, 64 kWh) and charger power (3.7 kW, 7.4
562 kW).

563 Results are presented both with and without the inclusion of curtailment
564 from Whitelee wind farm. For the former, this was represented by the substi-
565 tution of the grid carbon intensity with 0 gCO₂/kWh for any timestep where
566 curtailment of Whitelee occurred. The volume of wind curtailment was ne-
567 glected in this analysis because any curtailed volume in the period analysed
568 was three orders of magnitude greater than the peak EV charging demand
569 from the test network.

570 *5.6. Wind Generation Curtailment Reduction*

571 A single bus model was used (Figure 10), with a generator to represent the
572 volume of curtailed wind energy from Whitelee (taken from [22]). The volume
573 of curtailed wind is compared for an increasing number of EVs from 10,000
574 to 1,000,000, for both the minimal and routine charging schedule models. LV
575 network constraints are not considered in this part of the work due to the
576 computational burden involved – it is recognised that this could limit the
577 flexibility available from EVs and further work into this area is highlighted
578 in section 7. Managing distribution network constraints, and coordinating
579 access to flexible assets between distribution and transmission level markets
580 is a subject of ongoing research [43–45], and is out of the scope of this work.

581 There are currently over 2.4 million private cars in Scotland [46] and,
582 based on the Scottish Government’s target for all sales of new cars and vans
583 to be zero emission by 2032 [47], it is reasonable to expect that there could
584 be at least a million battery EVs within the Scottish ‘Central Belt’, where
585 approximately 65% of the population live (i.e. behind the B6 boundary
586 constraints which result in curtailment at Whitelee).

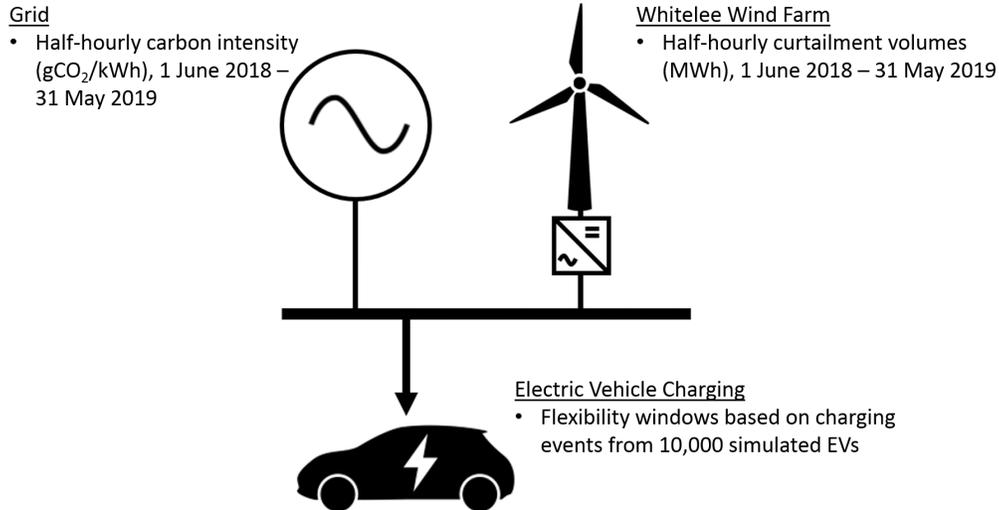


Figure 10: Schematic showing single bus model used to study potential of EV charging to utilise excess wind generation

587 Simulating up to 1,000,000 individual EVs was not possible as this would
 588 exceed the amount of travel data on record. 10,000 simulated EVs were scaled
 589 up to 50,000, 100,000, 250,000, 500,000, 750,000 and 1,000,000 EVs by multi-
 590 plying the battery capacity E_e^{\max} , charger power P_e^{\max} , initial energy storage
 591 content E_e^{start} and final energy storage content E_e^{end} of each EV accordingly.
 592 This approach of aggregating EVs to form large flexible demands has been
 593 demonstrated before – as previously discussed in section 1.2 – in [15] and
 594 [16].

595 A spread of EV battery capacities is analysed, with each vehicle being
 596 assigned a battery capacity randomly out of a set of capacities found on the
 597 EV market: 24, 30, 40, 60 and 75 kWh. All EVs were assumed to have
 598 7.4 kW charging capability, to reflect the trend towards higher power home
 599 chargers⁴.

600 The linearised problem formulation in (4-8) was used to minimise carbon

⁴in the UK, there is generally no difference in price between ‘slow’ and ‘fast’ home chargers – e.g. the WallPod EV charger retails at £320 in the UK for either 3.7 or 7.4 kW configuration [48] – thus it is likely that 7.4 kW chargers will soon become the norm.

601 intensity as in the carbon intensity minimisation study. As shown in Figure
602 10, a generator was used to represent the curtailment at Whitelee wind farm
603 whose power output was constrained as per (10).

$$p_{w,\tau}^G \leq P_{w,\tau}^{\text{UB}} \quad (10)$$

604 where $P_{w,\tau}^{\text{UB}}$ represents the maximum power output from the wind generator
605 w in time period τ , equal to the average curtailed wind power per timestep
606 at Whitelee: therefore, in periods with no wind curtailment, $P_{w,\tau}^{\text{UB}}$ is zero.

607 The wind generator was modelled as having 0 g/kWh carbon intensity and
608 the grid was modelled as having the national carbon intensity. The 112 days
609 on which curtailment occurred at Whitelee were modelled with increasing
610 EV numbers to establish how effectively the flexibility from EVs could be
611 used to reduce wind curtailment based on real curtailment data.

612 **6. Results**

613 Results are presented for the minimisation of the CO₂ emissions associ-
614 ated with EV charging (section 6.1) and for the minimisation of curtailment
615 at Whitelee wind farm (section 6.2).

616 *6.1. Controlling Electric Vehicle Charging to Minimise Carbon Intensity*

617 *6.1.1. Charging demand profiles*

618 Figures 11 and 12 show the uncontrolled charging profiles for the 100 days
619 simulated for the minimal and routine charging schedules respectively, with
620 a solid black line showing the mean charging demand in all cases.

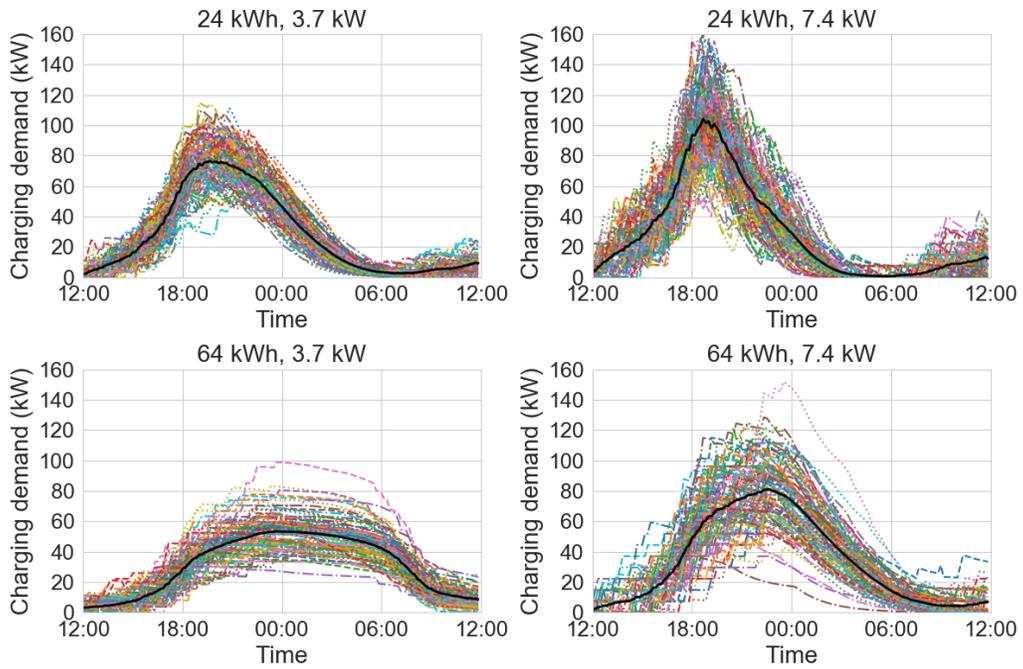


Figure 11: Uncontrolled charging demand profiles for all battery size/charger power combinations – minimal charging behaviour

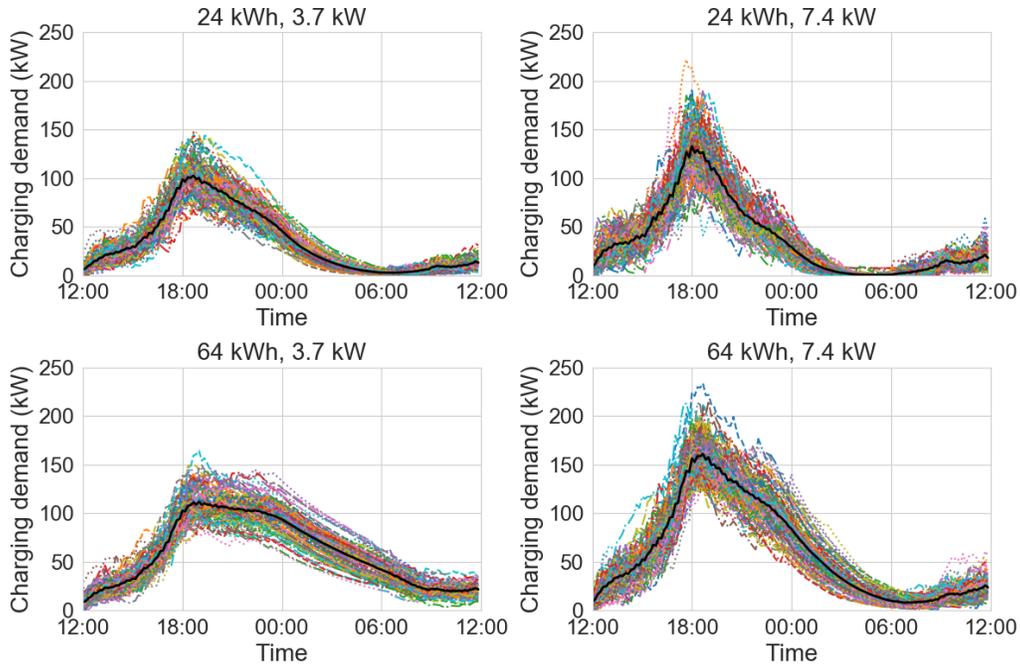


Figure 12: Uncontrolled charging demand profiles for all battery size/charger power combinations – routine charging behaviour

621 The effect of EV parameters on uncontrolled EV charging demand is
 622 shown in Figures 11 and 12. When drivers are trying to minimise their
 623 charging frequency (as in Figure 11), an increase in battery size leads to a
 624 reduction in the peak demand, and a shift of the peak to a later point in the
 625 evening. Increasing the charger power leads to a sooner, sharper peak with
 626 a greater magnitude. If drivers routinely plug their EVs in irrespective of
 627 their SoC (as in Figure 12), several interesting effects can be observed. The
 628 variation in charging profiles day to day becomes smaller, and the effect of
 629 battery size is reduced. The longer ‘tail’ of the charging profile in the larger
 630 battery sizes compared to the smaller ones is due to a larger energy storage,
 631 enabling the possibility of a longer charging duration. Increasing charging
 632 power is still shown to bring the peak charging demand forward and increase
 633 its magnitude.

634 Figures 13 and 14 show the controlled charging profiles for the 100 days,
 635 after having been scheduled as per the method presented in section 5, for the
 636 minimal and routine charging schedule models respectively.

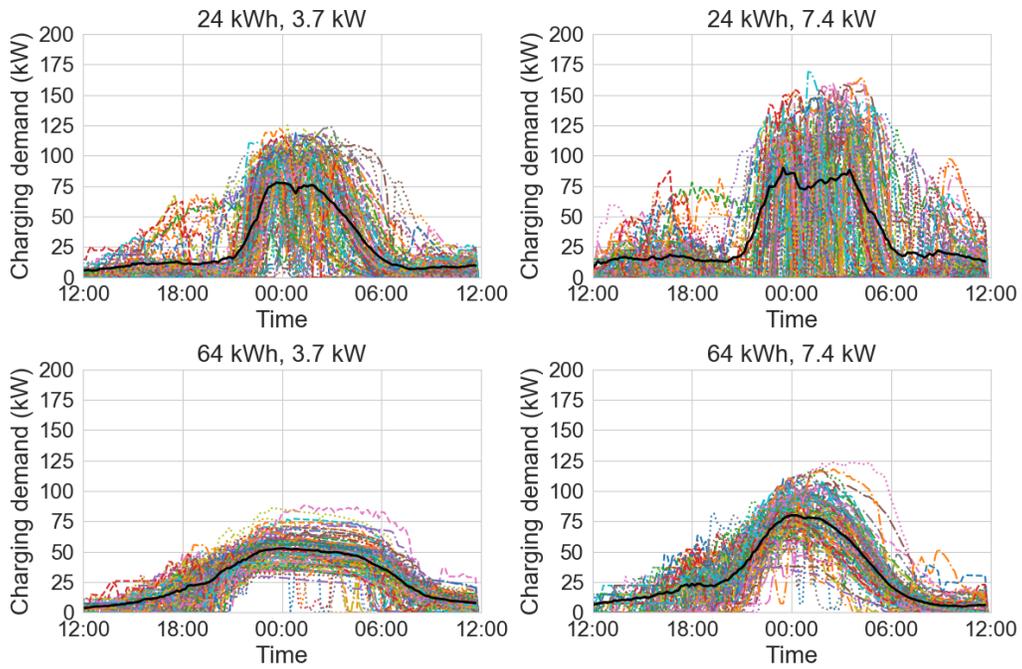


Figure 13: Controlled charging demand profiles (minimisation of carbon intensity) for all battery size/charger power combinations – minimal charging behaviour

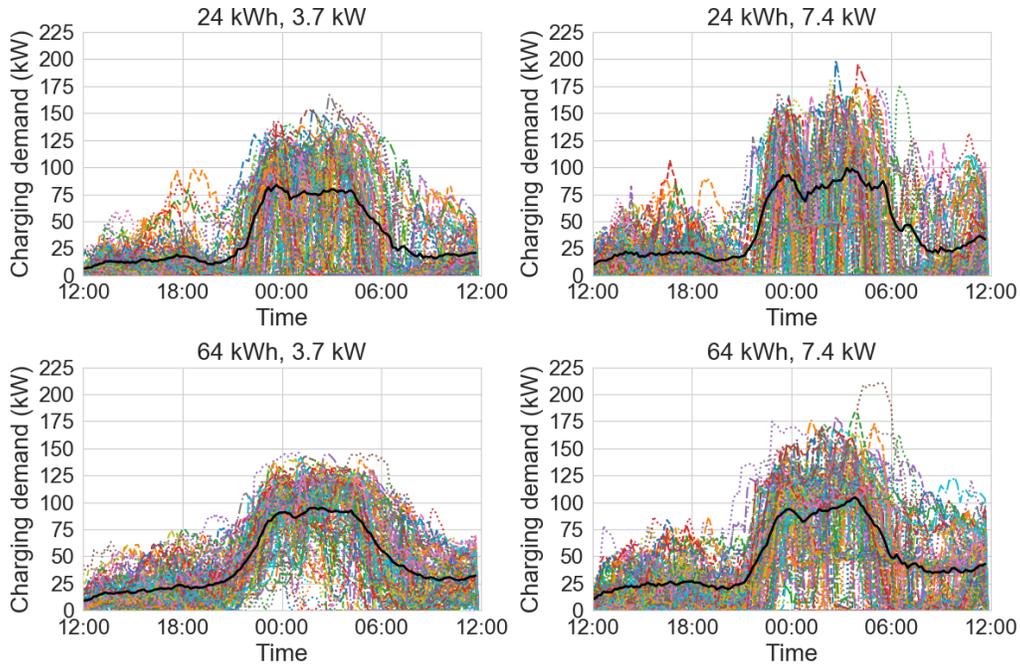


Figure 14: Controlled charging demand profiles (minimisation of carbon intensity) for all battery size/charger power combinations – routine charging behaviour

637 A great variation in controlled charging demand is shown in Figures 13
 638 and 14, which is a direct result of the significant variation in carbon intensity
 639 (Figure 5). It is shown in the black solid lines representing the mean charging
 640 profile that the bulk of charging demand was usually delayed to the middle of
 641 the night where carbon intensity is lowest. In the minimal charging schedule
 642 case, there is shown to be significantly less variation in the controlled charging
 643 load for the larger battery size, especially with the slow charging rate. This
 644 is suggested to be due to a lower flexibility with these charge events; as
 645 these drivers tend to plug in on fewer occasions, their energy demand from
 646 any given charge event is greater; furthermore, if the charging power is lower,
 647 there is less that can be done to shift this charging demand in time. If drivers
 648 plug in routinely, the mean controlled charging profiles are more similar to
 649 one another. This is suggested to be due to an increased flexibility of the
 650 charging events for EVs with bigger batteries, due to an increase in their
 651 charging frequency and therefore a reduction in the required energy from a
 652 given charge event.

653 *6.1.2. Reduction in Carbon Intensity of EV Charging*

654 Figures 15 and 16 show boxplots of the carbon intensity associated with
655 all charge events on all 100 days in the simulation for uncontrolled charging
656 then controlled charging, with and without consideration of curtailment of
657 Whitelee wind farm, for the minimal and routine charging schedule cases
658 respectively.

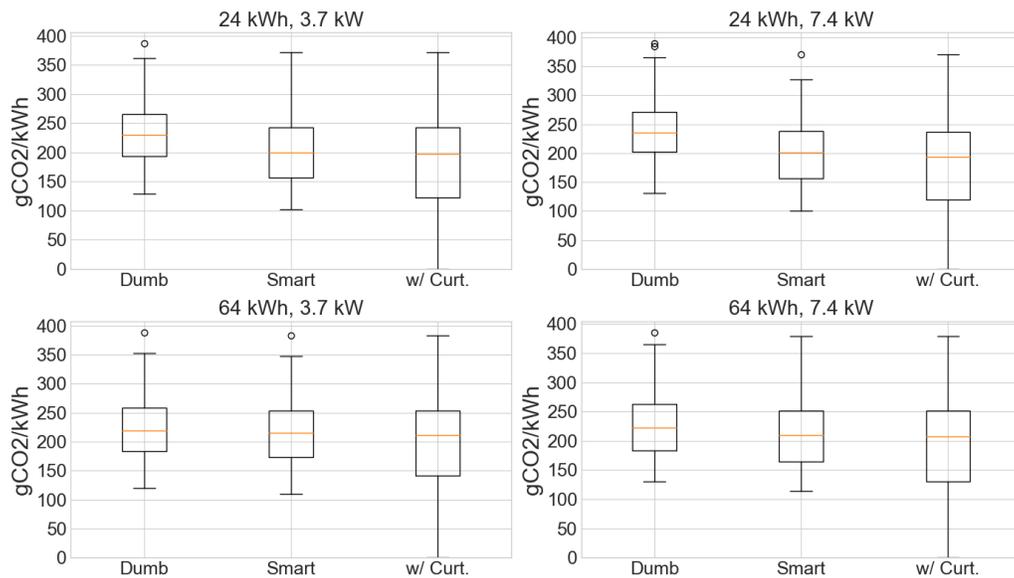


Figure 15: Reduction in carbon intensity from controlled charging, with and without the inclusion of curtailment from Whitelee wind farm, for all battery size/charger power combinations – minimal charging behaviour

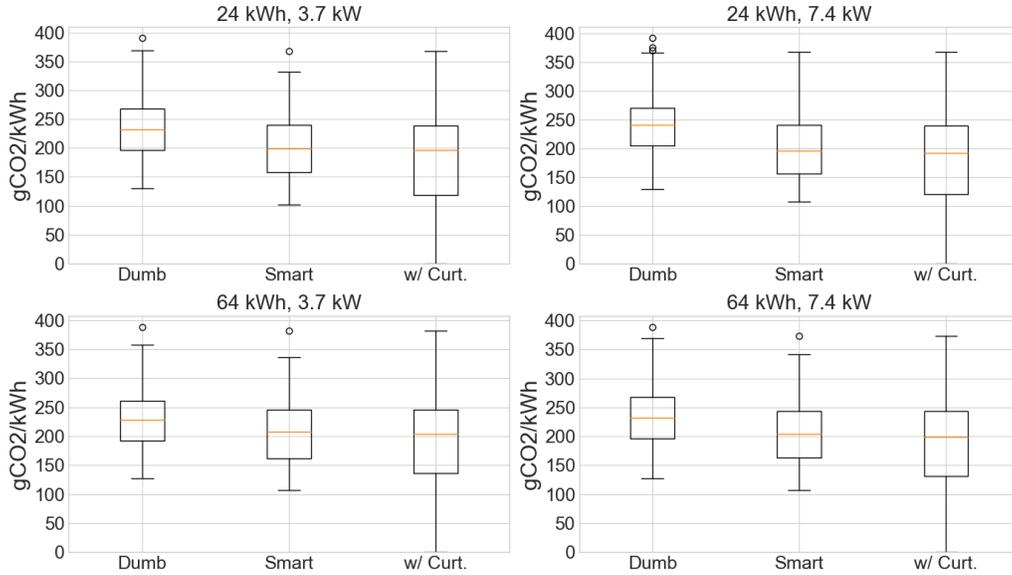


Figure 16: Reduction in carbon intensity from controlled charging, with and without the inclusion of curtailment from Whitelee wind farm, for all battery size/charger power combinations – routine charging behaviour

659 Figures 15 and 16 show a steady reduction in the carbon emissions asso-
 660 ciated with EV charging. As previously discussed, the charging load of EVs
 661 with larger batteries under the minimal charging model is less flexible than
 662 those under the routine charging model; as a result, it is shown that if EV
 663 drivers with large batteries only plug in when they need to, it is more difficult
 664 for controlled charging to reduce the carbon intensity associated with their
 665 vehicles' charging.

666 The reduction in the mean carbon intensity associated with EV charging
 667 for all parameter combinations and both charging scheduling models is shown
 668 in Tables 5 and 6.

Table 5: Summary results: reduction in mean carbon intensity of driving (gCO₂/kWh) from smart charging with and without consideration of curtailment of Whitelee wind farm – minimal charging schedules

Mean Carbon Intensity (gCO₂/kWh) – Minimal Charging			
Parameters	Dumb Charge	Smart Charge	With Curtailment
24 kWh, 3.7 kW	234.0	201.7 (-13.8%)	176.2 (-24.7%)
24 kWh, 7.4 kW	241.5	199.7 (-17.3%)	171.4 (-29.0%)
64 kWh, 3.7 kW	221.8	215.0 (-3.1%)	193.5 (-12.8%)
64 kWh, 7.4 kW	226.4	210.5 (-7.0%)	187.1 (-17.4%)

Table 6: Summary results: reduction in mean carbon intensity of driving (gCO₂/kWh) from smart charging with and without consideration of curtailment of Whitelee wind farm – routine charging schedules

Mean Carbon Intensity (gCO₂/kWh) – Routine Charging			
Parameters	Dumb Charge	Smart Charge	With Curtailment
24 kWh, 3.7 kW	237.4	200.8 (-15.4%)	172.8 (-27.2%)
24 kWh, 7.4 kW	243.7	201.6 (-17.3%)	172.3 (-29.3%)
64 kWh, 3.7 kW	228.5	208.0 (-9.0%)	182.9 (-20.0%)
64 kWh, 7.4 kW	235.9	205.6 (-12.8%)	179.5 (-23.9%)

669 If EVs are dumb charged (i.e. there is no control of their charging), the
670 CO₂ emissions associated with their charging is, on average, in the region
671 221-243 gCO₂/kWh. For context in vehicle emissions, the average tailpipe
672 emissions of new petrol and diesel cars purchased in Europe in 2019 were
673 121.5 gCO₂/km and 123.4 gCO₂/km respectively [49]. Given that typi-
674 cal electricity consumption values of EVs on the market from the United
675 States Environmental Protection Agency (EPA)⁵ are in the range from 0.16
676 kWh/km (based on the city consumption of a 2019 Hyundai Kona Electric
677 64) to 0.23 kWh/km (based on the highway consumption of a 2018 Tesla
678 Model S 100) [51], this means that associate EV emissions, if charged from

⁵The EPA’s Federal Test Procedure is designed to allow direct comparison of emissions and fuel economy between different vehicles for real-world driving conditions based on city and highway driving cycles. These figures tend to be more conservative than European data, which unlike in the US, result from tests carried out by manufacturers themselves. This is likely to have been a key contributing factor in the ‘Dieselgate’ scandal 2015-present [50].

679 the 2019 GB generation mix, are in the range 35.4-55.9 gCO₂/km. If EVs
680 are dumb charged, their carbon intensity is reduced with larger batteries and
681 lower charger power ratings, because this shifts the charging load later into
682 the night (as in Figures 11 and 12) when carbon intensity is typically lower
683 (Figure 5).

684 Controlling EV charging, such that all EV charge requirements are met
685 and the network is always operated within its thermal limits, can reduce the
686 CO₂ emissions associated with charging by up to 17%. Higher charging power
687 enables the greatest reduction, as this enables more of the energy demand to
688 be met in the times of lowest carbon intensity. Increases in battery size are
689 shown to make it more difficult to reduce the carbon intensity of charging,
690 whereas increases in charger power are shown to make it easier. This is
691 because of the effect of these parameters on the flexibility of charge events,
692 as previously discussed. If drivers plug in routinely, the effect of increasing
693 battery size is reduced.

694 If there is local RES generation to absorb that would otherwise be cur-
695 tailed, then in this analysis the carbon intensity was set at 0 gCO₂/kWh
696 for these time periods as per the method used in the National Grid carbon
697 intensity calculator [21]. In this case, controlling EV charging to take place
698 in these periods can further reduce the associated emissions of charging, by
699 up to 29% with respect to the original. Carbon emissions at this level would
700 result in associated emissions of EV driving in the range (using the same
701 energy consumption values as before) 27.6-39.6 gCO₂/km, around a quarter
702 of the corresponding average for petrol and diesel cars.

703 The carbon intensity of the grid has been modelled as independent of
704 demand. Although the scale of modelling means that the load presented
705 by the EVs' charging is negligible in comparison to GB demand, if such a
706 scheme were implemented on a large (e.g. nationwide) fleet of EVs then
707 their charging would effect grid intensity – if their charging were to come
708 online such that dispatchable thermal plants had to be brought online, then
709 the carbon intensity associated with their charging would be equivalent to
710 the carbon intensity of the dispatchable plant. At present, there are several
711 electricity tariffs on offer in the UK aimed at EV drivers with access to
712 private residential charging, which offer varying electricity prices based on
713 forecasts of RES output and wholesale electricity prices [52–54]. As the
714 penetration of RES continues to increase in line with government targets, an
715 increased variance in grid intensity is likely. By following the regions of lowest
716 grid intensity, the presence of EVs would effectively be incentivising further

717 RES generators to come online by providing a greater level of certainty that
 718 the energy they generate would be consumed, even if produced outside of a
 719 traditional domestic demand peak (such as that shown in Figure 2).

720 Aside from potentially reducing their own associated carbon emissions,
 721 EV charging can potentially use RES generation that would otherwise be
 722 curtailed. Results for this part of the study are presented in section 6.2.

723 *6.2. Controlling Electric Vehicle Charging to Absorb Excess Wind Genera-*
 724 *tion*

725 Figure 17 shows boxplots of the percentage reduction in curtailment on
 726 each of the 112 days with curtailment in the period 1 June 2018 – 31 May
 727 2019 for fleets of EVs of various sizes. Figure 18 shows the total percentage
 728 reduction in curtailment over the whole period for the same fleet sizes.

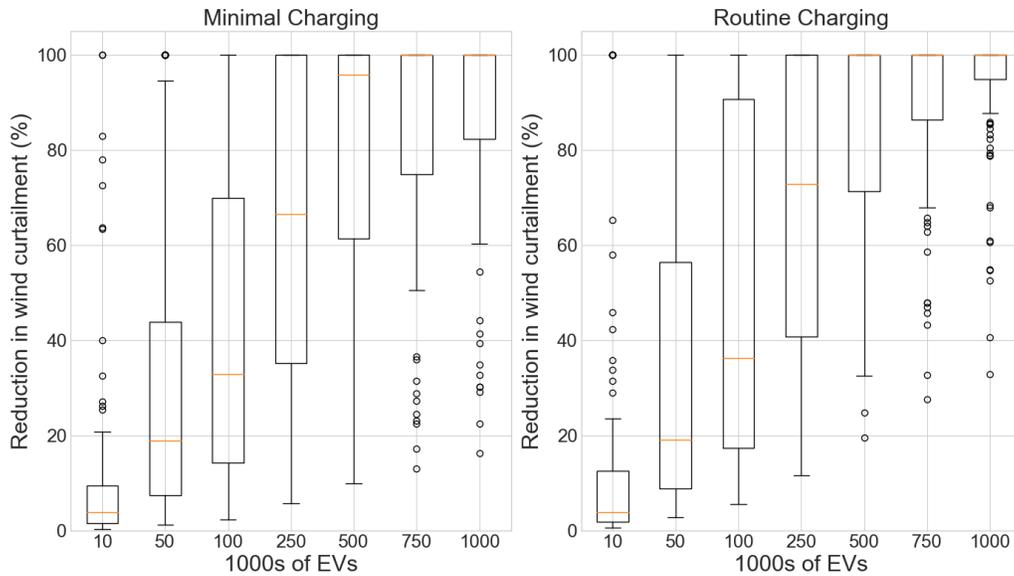


Figure 17: Box plots showing percentage reduction in wind curtailment at Whitelee wind farm on 112 days with curtailment from the optimisation of charging from fleets of EVs of various sizes (1000s)

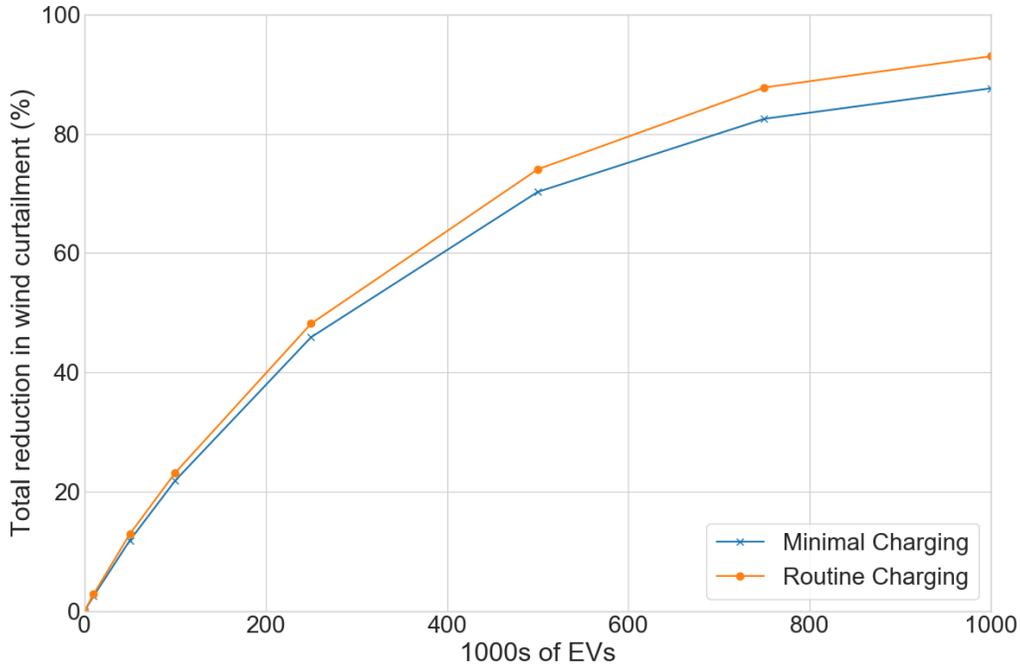


Figure 18: Total reduction in curtailment of generation at Whitelee wind farm over period 1 June 2018 to 31 May 2019 from the optimisation of charging from fleets of EVs of various sizes (1000s)

729 Figure 17 shows the rate of increase in curtailment reduction as the fleet
 730 of EVs increases in size. While the variance is high (due to the variance in
 731 the volume of curtailment on each day and the time of day at which this
 732 occurs), it is shown that the reduction in curtailment continues to increase
 733 with an increasing size of EV fleet. Figure 18 shows that this rate of increase
 734 is diminishing; this is due to a subset of days for which the curtailment
 735 cannot be reduced to zero even by the charging of 1,000,000 EVs. These are
 736 days in which a large volume of curtailment occurs in the middle of the day
 737 (when there are fewer EVs plugged in); however, as shown in Figure 7, wind
 738 curtailment in the daytime is rarer than in the nighttime.

739 It is shown in Figure 18 that if drivers charge routinely, then there is
 740 more potential for EV charging to be able to reduce curtailment. This effect
 741 is most pronounced for large fleets: with a fleet of 1,000,000 EVs, whereas
 742 93.0% of Whitelee wind farm’s total curtailment can be used to charge these
 743 EVs if they are charged routinely, 87.6% of total curtailment can be used

744 for the minimal charging case. The reason for these numbers not being
745 vastly different is that the energy for these EVs to carry out their transport
746 requirements remains the same for both cases – though the extra flexibility
747 resulting from routine charging can be better utilised to reduce curtailment
748 at the wind farm. Given that the absorption of this curtailment potentially
749 has significant value, it could be expected that drivers could be incentivised
750 to plug in routinely when arriving home so as to maximise any revenue that
751 may be made from the absorption of curtailment.

752 *6.3. Discussion – EV Flexibility in the Balancing Mechanism*

753 A potential market mechanism to reward EV flexibility for reducing wind
754 curtailment is the GB balancing mechanism (BM). Aggregated EV flexibility
755 could be accessed by National Grid ESO in the BM to manage transmission
756 system constraints, offering an alternative to wind curtailment (i.e. rather
757 than paying wind generators to turn down their output, the ESO could pay
758 EV charging aggregators to turn up their demand). However, access to the
759 BM is currently limited for smaller participants such as EVs – this is due
760 to the economics of scale favouring a smaller number of larger units, the
761 requirement for any participant to be a fully licensed supplier (unless granted
762 a derogation by the regulator) and the ESO favouring larger units in the BM
763 at short timescales [55].

764 However, the introduction of the ‘virtual lead party’ under the GB imple-
765 mentation of project TERRE will allow smaller aggregators (with a minimum
766 aggregated BM unit size of 1 MW) to participate in the BM without the need
767 to be fully licensed suppliers [55, 56]. Furthermore, the ESO has introduced
768 a distributed resource desk, which has resulted in increased participation of
769 industrial and commercial aggregators in the BM [57]. Coupled with the
770 projected growth in EV penetration, this reduction in the barriers to access
771 the BM is likely to contribute positively to the business case of aggregation
772 of EV charging for the provision of grid services.

773 **7. Conclusion and Further Work**

774 This paper has presented an investigation into the potential of controlling
775 EV charging to i) reduce the carbon emissions associated with their charging
776 and ii) to provide demand when there is excess renewable electricity genera-
777 tion in the system (that ordinarily has to be curtailed).

778 The numerical results presented in this paper represent important quan-
779 titative research to network owners, system operators, grid service providers,
780 would-be EV consumers and vehicle manufacturers as it highlights the per-
781 ceived 'value' of the flexibility of EV charging.

782 If EV charging were able to follow the times of low carbon intensity and
783 take advantage of RES curtailment, then the emissions associated with their
784 charging was shown to be in the region 27-40 gCO₂/km; a 30% reduction on
785 the 'dumb charging' carbon intensity of 35-56 gCO₂/km. Although this offers
786 an improvement of up to a factor 5 relative to average new petrol and diesel
787 cars, it remains considerably higher than the carbon emissions associated
788 with electrified public transport or other low carbon transport options (e.g.
789 carpooling and cycling/use of e-bikes) [58].

790 It is shown that there is significant potential to absorb excess RES gen-
791 eration from the flexibility of EV charging: the results shown in section 6.2
792 imply that a fleet of 500,000 EVs, which would equate to an EV penetration
793 of approximately 20% based on Scotland's total car fleet of 2.4 million, could
794 absorb approximately three quarters of curtailment at GB's largest onshore
795 wind farm. It was discussed that market mechanisms need to evolve to allow
796 this. On the basis of the work presented in this paper, the authors suggest
797 the following to be valuable pieces of further work:

- 798 1. In a practical controlled charging set-up the charging controller would
799 likely not have access to such detailed information as the leave time
800 and the required energy transfer of each vehicle. Furthermore, while
801 the analysis presented in this paper is based on historic carbon intensity
802 and curtailment data, in practice, any scheduling of charge events would
803 be done on the strength of forecasting. On this basis, it is recommended
804 that further work be undertaken to investigate how such a controlled
805 charging regime could be operated with an imperfect set of information
806 (e.g. based on forecasts of driving behaviour, carbon intensity and
807 curtailment), and what the result would be compared to the 'perfect
808 information' example as presented in this paper.
- 809 2. Aside from the growth in EVs, there are other opportunities presented
810 from distributed energy resources such as distributed heating, storage
811 and demand side response: the potential of these technologies to con-
812 tribute towards a flexible energy system that can interact positively
813 with the grid to further enable decarbonisation could be evaluated, in
814 comparison with what was studied in this paper.

815 3. Distribution constraints (thermal and voltage) could limit the flexi-
816 bility available to the transmission system operator from EVs located
817 at the distribution level. A tractable method of modelling distribution
818 network constraints, such as a full AC optimal power flow or an approx-
819 imation to it as previously discussed in section 5.3, could be developed
820 to schedule large fleets of EVs over networks of millions of nodes. This
821 could be done using a web of cells or a hierarchical structure of passing
822 flow limits from one level (distribution) to the next (transmission) as
823 proposed in [44].

824 **Acknowledgement**

825 This work has been done through the Engineering and Physical Sciences
826 Research Council (EPSRC) Centre for Doctoral Training on Future Power
827 Networks and Smart Grids at the University of Strathclyde, funded by grant
828 EP/L015471/1. This work has been further supported by the EPSRC AG-
829 ILE project (EP/S003088/1) and the Realising Energy Storage Technolo-
830 gies in Low-carbon Energy Systems (RESTLESS) project (EP/N001893/1).
831 Grateful thanks are expressed to SP Energy Networks and Ciaran Higgins
832 for provision of the Glasgow Southside distribution network data, and to
833 Graeme Flett of the Energy Systems Research Unit (ESRU) at the Univer-
834 sity of Strathclyde for the assistance in integrating the domestic demand
835 model used in this paper.

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