

1 Integrated Design of Monitoring, Analysis and Maintenance for
2 Filamentous Sludge Bulking in Wastewater Treatment

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12
13 **Abstract:** Stable operation of activated sludge process is often compromised by the
14 occurrence of filamentous sludge bulking in wastewater treatment. Standard
15 maintenance is implemented as a single task, which is inefficiently manipulated based
16 on purely chemical dosage by experiences. This paper proposes a novel and efficient
17 maintenance framework, including a set of activities: incipient fault detection,
18 causality analysis, remaining useful life (RUL) prediction and maintenance schedule,
19 to develop a collective strategy for sludge bulking management. In this framework,
20 Canonical Correlation Analysis (CCA) work together with Kurtosis (KU) and an
21 autoregressive moving average (ARMA) to identify incipient sludge bulking and to
22 capture the evolution of sludge bulking over a long horizon. The proposed framework
23 was tested by the collected the field data. The results showed that the proposed
24 framework is capable of detecting (Type I error, 2.1%; Type II error, 0%), locating
25 (root cause: temperature), calculating RUL (32-days) and maintaining sludge bulking.

29 Keywords: Fault diagnosis; Maintenance; Wastewater; Filamentous sludge bulking;
30 Virtual measurement

31 **1 Introduction**

32 Activated sludge process (ASP) is the most commonly used technique to remove the
33 organic material and nutrients from wastewater (Hartley, 2008; Ng, Ong, & Hossain,
34 2000). Successful operation of ASP highly depends on efficient biological
35 conversions in bioreactors and normal sludge separation in secondary clarifiers.
36 Excessive growth of filamentous bacteria in secondary clarifiers often results in
37 sludge settleability deterioration, poor operational performance and high treatment
38 cost (Martins, Pagilla, Heijnen, & van Loosdrecht, 2004; Olsson, 2012). This is
39 termed as filamentous sludge bulking, which is considered as the most serious
40 problem over 50% ASP-based Wastewater Treatment Plants (WWTPs) worldwide
41 (Fan, et al., 2018; Guo, et al., 2013; Martins, et al., 2004; Rossetti, Tomei, Nielsen, &
42 Tandoi, 2005). Condition-based maintenance (CBM) is a commonly used
43 decision-making strategy to enable real-time diagnosis of incipient failure and
44 prognosis of future system health (Allison, Dickson, Fisher, & Thrush, 2018;
45 Kenway, et al., 2015; Bin Liu, Liang, Parlikad, Xie, & Kuo, 2017; Bin Liu, Wu, Xie,
46 & Kuo, 2017). By resorting to condition-based maintenance, , it is desirable to
47 transform data into knowledge to support sludge bulking management in a wastewater
48 plant efficiently and costly (Montserrat, Bosch, Kiser, Poch, & Corominas, 2015).

49 Occurrence of filamentous sludge bulking mainly arises from the imbalance of
50 bacteria in secondary clarifiers and exhibits drifting degradation pattern. Multiple
51 sensors are usually allocated around the entire plant to gain the global insight of
52 working status for filamentous sludge bulking, thus leading to inevitable increase of
53 the sensory data dimensions. This high-dimension data may present redundancy and
54 irrelevance. Statistical process monitoring, including Principal Component Analysis
55 (PCA) (Jiang, Yan, & Huang, 2016; Merello, García-Diego, & Zarzo, 2014),
56 Independent Component Analysis (ICA) (J.-M. Lee, Qin, & Lee, 2006) and Canonical
57 Correlation Analysis (CCA) (Asendorf & Nadakuditi, 2017), were typically used to

58 refine and recognize faulty features from multisensory measurements. These methods
59 tended to explore the data by building an empirical model. The derived model was
60 then taken as a reference to justify the desired process behavior for the incoming data
61 by Hotelling's T^2 or squared predicted errors (SPE). To deal with nonlinear and
62 dynamic issues of aforementioned methods, Bayesian Networks and enhanced PCA
63 were proposed (Baoping Cai, Liu, & Xie, 2016; B. Cai, Zhao, Liu, & Xie, 2017; Ge,
64 2018). If the nonlinearity with respect to a process is even complex, distributed
65 paralleled PCA can be used by dividing such global complexity into local simplicity
66 (Zhu, Ge, & Song, 2017). However, in the early stage of sludge bulking, the process
67 is stationary fairly and the collected data are very limited. Linear models can provide
68 more straightforward and more efficient ways for fault detection. Among the linear
69 methods, CCA is able to maximize the correlation between variable groups, and
70 identify a fault with correlated within-set covariance (Z. Chen, Ding, Zhang, Li, &
71 Hu, 2016; Z. Chen, Zhang, Ding, Shardt, & Hu, 2016; Ding, 2014; Y. Liu, Liu, Zhao,
72 & Xie, 2018, 2019). However, since the CCA-based process monitoring is based on
73 correlation rather than causality among data, CCA fails to precisely locate root cause.
74 In case of filamentous sludge bulking, it is difficult for an operator to make decisions
75 without any information on the root cause. One of the alternatives is to resort to
76 contribution plots (Vitale, de Noord, & Ferrer, 2015). Despite the advantages of
77 contribution plots, it always suffers from fault smearing, i.e., the negative influence of
78 faulty variables usually propagates to non-faulty variables. Also, contribution plots
79 cannot suggest fault propagation graphically. In this light, integration of CCA with
80 other methods provides potentials to deal with this issue. Root diagnosis issue has
81 been addressed in the plant-wide oscillation identification. By performing plant-wide
82 oscillation identification, undesired oscillations can be recognized either in the control
83 loops or in manipulated variables (J. Lee, Kang, & Kang, 2011; Zhu, et al., 2017).
84 Root causality diagnosis of plant-wide oscillations is mainly divided into spectral
85 envelop, adjacency matrix, causality analysis, transfer entropy and Bayesian network
86 (Wang, Yang, Chen, & Shah, 2016). Among these methods, Granger causality based

87 and transfer entropy based causality analysis are direct methods which are able to
88 reveal variable causality using temporal data (Sarrigiannis, 2013; Vicente, Wibral,
89 Lindner, & Pipa, 2011). However, all of the root cause analysis methods are sensitive
90 to the noises, which is likely to cast the actual fault.

91 Despite the availability of fault identification methods and root cause analysis for
92 fault detection in the early stage, rapid recovery of sludge bulking is difficult and time
93 consuming. Accurate prediction of remaining useful life (RUL) for sludge bulking is
94 indispensable, i.e., how much time is reserved to correct sludge bulking? The concept
95 of RUL has been widely used in many important applications, such as product
96 manufacturing, material science, biostatistics and econometrics. However, the critical
97 and hidden features about RUL calculation are usually not directly observable, due to
98 measurement delay or expensive measurement costs. Thus, increasing demand has
99 accelerated the integration of virtual sensors (virtual measurements) to derive such
100 hard-to-measured variables. Virtual sensors are usually used to estimate
101 hard-to-measured (unobservable) variables by other easy-to-measured (observable)
102 variables. To deal with the complex process behaviors, nonlinear models, such as
103 Artificial Neural Networks (ANN), Support Vector Machine (SVM), are usually used
104 to approach the evolutions of a quality-related but hard-to-measured variables
105 (Zeynoddin, Bonakdari, Azari, et al., 2018). However, it is difficult to define the
106 evolution of a variable as a purely linear or nonlinear process, but a hybrid behavior
107 instead (Bonakdari, Moeeni, et al., 2019). Moeeni .et. al. proposed a mixture of an
108 ARMA and an ANN model to capture such hybrid behaviors (Moeeni & Bonakdari,
109 2017, 2018). Another alternative is to use a purely linear model with enhanced
110 preprocessing techniques (Bonakdari, Zaji, Binns, & Gharabaghi, 2019; Isa Ebtehaj,
111 Bonakdari, & Gharabaghi, 2019; I. Ebtehaj, Bonakdari, Zeynoddin, Gharabaghi, &
112 Azari, 2019). Despite their well perdition performance, the issue is that these methods
113 are mostly limited for single-step prediction, which is not able to provide sufficient
114 and necessary information for RUL calculation. The other important issue is that, at
115 the onset of the evolution of sludge bulking, the collected data are always very limited

116 and insufficient to build nonlinear models, such as Neural Networks or Gaussian
117 Processes Regression (H. Liu, Yang, Huang, Wang, & Yoo, 2018; Y. Liu, et al.,
118 2019). Therefore, an ARMA (Autoregressive moving average model) model with
119 preprocessing techniques is a better choice fairly. The ARMA-based prediction is
120 effective with limited number of time series data being available. Also, an ARMA is
121 able to provide models with acceptable precision and minimum parameters
122 (Zeynoddin, Bonakdari, Ebtehaj, et al., 2018). Even though fault detection,
123 propagation identification, causality analysis and RUL prediction have been
124 investigated individually and intensively, few papers are devoted to jointly coordinate
125 them for sludge bulking management. Also, none of the methodologies are qualified
126 for the desirable features and exhibit some limitations. To address these limitations,
127 integrating all the methods is an alternative to individual methods. Such an
128 incorporative approach can make full use of the available information and overcome
129 the limitations of individual methods, therefore leading to better decision making. In
130 this work, a novel and hybrid framework for fault detection, causality analysis, fault
131 propagation, RUL prediction and decision-making for maintenance is introduced from
132 a systematic point of view.

133 Overall, condition-based maintenance cannot be seen as a single task instead, the
134 whole aspects of maintenance must be viewed as a set of activities: fault detection,
135 propagation identification, causality analysis, remaining useful life (RUL) prediction
136 and maintenance strategies. Firstly, a CCA model together with Kurtosis (KU) is
137 constructed to derive a new Squared predicted errors (SPE), SPE_{KU} , for feature
138 extraction and fault detection. In general, CCA is able to discriminate quality-relevant
139 and quality-irrelevant variables, and then to explore their correlation to formulate a
140 fault detection index, i.e., SPE, for fault recognition. However, SPE index of CCA is
141 not sensitive sufficiently for an incipient fault. In this paper, KU is utilized to refine
142 fault-related feature with respect to SPE, in such a way that abnormal SPE signal can
143 be amplified and captured properly. Practically, sludge volume index (SVI) is utilized
144 to describe the sludge bulking. To justify if sludge bulking occurs, SVI values at 150

145 mg/L, 180 mg/L, 200 mg/L or even 280 mg/L are always documented as the control
146 limit (Rensink, 1974). Nonetheless, even though SVI is usually used to pre-alarm
147 sludge bulking occurrence, it is difficult to measure on-line. Moreover, due to lack of
148 other relevant information, such as DO (Dissolved Oxygen), nutrient and so on,
149 recognition of the root cause with respect to filamentous sludge bulking is difficult
150 once a fault is declared by SPE_{KU} . In this light, multivariate Granger Causality
151 (MVGC) is, secondly, proposed in this paper to assimilate more information into fault
152 identification. By performing MVGC, the framework is able to capture the spatial and
153 temporal dependency as well as causality among variables on one hand. On the other
154 hand, MVGC can provide a visual cause and effect description among the variables
155 that are most suspected to be the root cause of the sludge bulking fault in a graphical
156 way. However, the root cause analysis will deviate significantly if improper features
157 are forwarded into the MVGC. Thus, KU is implemented to process each raw variable
158 before running MVGC, aiming to amplify signal variation to facilitate sequential
159 MVGC treatment. Thirdly, an ARMA (Autoregressive moving average)-based
160 multiple-step-ahead model serves as a virtual instrument to measure SVI over a long
161 term. This will facilitate the relevant Remaining Useful Life (RUL) estimation and be
162 able to achieve sufficient time for maintenance before a failure occurs. Given the
163 resulted RUL, maintenance strategies are divided into preventive maintenance and
164 corrective maintenance. During the preventive maintenance period, the fault evolution
165 is not that severe. The derived root causes can be used to trigger decision-making for
166 filamentous sludge bulking maintenance. Even though many maintenance schemes
167 are recommended based on the output of real industries and lab research during
168 different scenarios, few experts devote to summarization of filamentous sludge
169 bulking maintained strategies for management. In this work, a proper preventive
170 maintenance for many root causes is summarized. On the contrary, due to the severity
171 of filamentous sludge bulking during the corrective maintenance period, proper
172 chemical dosage is necessary. Because of knowledge limitation and severity of
173 filamentous sludge bulking, the majority of operators prefer to dose chemicals directly,

174 which implies improper cost saving and insufficient time saving for maintenance.
175 Overall, to ensure that filamentous sludge bulking can be managed in a timely and
176 cost-effective way, this paper classifies the entire maintenance period into preventive
177 and corrective maintenance. As a first attempt, preventive maintenance is mainly used
178 to deal with incipient sludge bulking, such as adjustment of operational parameters.
179 Once the preventive maintenance strategy does not work well, corrective maintenance
180 has to be triggered, which is to dose chemicals up to the seriousness.

181 Section 2 presents the novel framework for the condition-based maintenance of
182 sludge bulking. The proposed methodologies are validated and discussed using
183 simulation with operational data being collected from a full-scale wastewater
184 treatment plant (WWTP) in Section 3. Conclusions are drawn in Section 4.

185

186 **2 The Proposed Framework**

187 The proposed framework is shown in Fig. 1 and defined as following:

188 (1) Fault detection: selected variables and samples are fed to train and test a CCA
189 model. The SPE derived from the CCA model is then treated by the KU. Once an
190 incipient fault is recognized by SPE_{KU} , the procedure will step into fault location at
191 the stage (2) and RUL prediction at the stage (3). That is to say, root cause analysis
192 and RUL calculation will be triggered once an incipient sludge bulking is recognized.
193 Otherwise, it will go back to fault detection if a new sample arrives. (2) Fault
194 location: once an incipient fault is declared, KU is used to refine more sensitive
195 features from selected variables to justify if significant change is happening. The
196 extracted features are re-organized with the variation sequence against the time. That
197 is to say, the variable with the earliest jump could be most potential rooting cause and
198 will be picked up to be the highest priority in the feature matrix. The derived feature
199 matrix will be then fed to MVGC for root cause analysis. (3) RUL prediction: once
200 the predicted SVI crosses over the SPE_{KU} control limit, the RUL will be calculated
201 based on the multi-step prediction of an ARMA model. The ARMA model will make
202 multi-step prediction of SVI until the predicted SVI values reach the control limit,

203 200mg/L. (4) Maintenance: based on the derived RUL and the profile of a fault
 204 propagation given by the MVGC, maintenance decisions can be suggested relying on
 205 the summarized expert knowledge. Preventive maintenance, such as adjustment of
 206 operational parameters, is used to deal with incipient sludge bulking. Once the SVI
 207 attains corrective control limit (CCL_{limit}), corrective maintenance has to be triggered,
 208 which is to dose chemicals up to the seriousness.

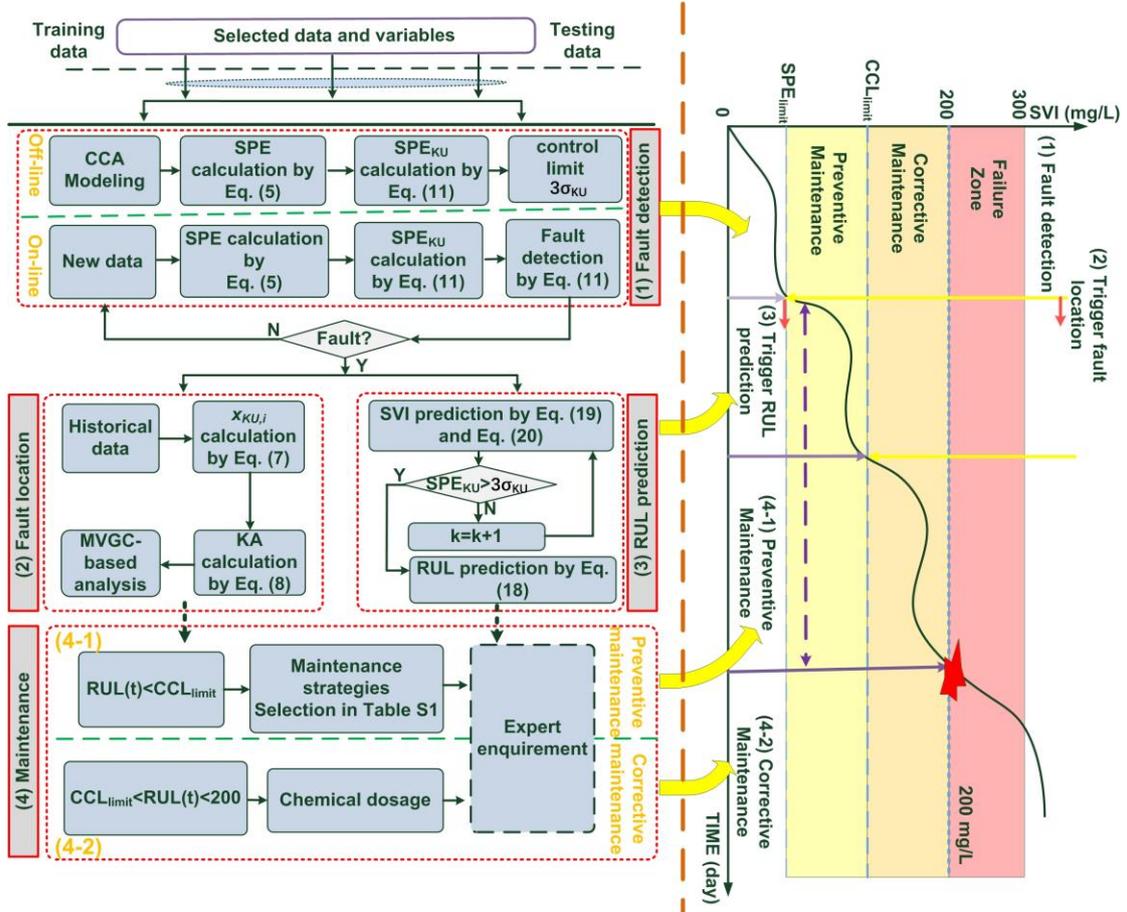


Fig. 1 Schematic diagram of algorithm implementation

2.1 CCA-based fault identification

CCA is a method to correlate two vectors by maximizing correlations among them. Suppose that N samples of the process data are collected, and X_1 and X_2 represent input variables and response variables, respectively, where $X_1 \in \mathbb{R}^{d_1 \times N}$ and $X_2 \in \mathbb{R}^{d_2 \times N}$, $d = d_1 + d_2$. d_1 and d_2 represent the number of variables for X_1 and X_2 , respectively. Let X_1 and X_2 be centered by mean, then

$$\begin{bmatrix} \Sigma_{X_1 X_1} & \Sigma_{X_1 X_2} \\ \Sigma_{X_2 X_1} & \Sigma_{X_2 X_2} \end{bmatrix} \approx \frac{1}{N} \begin{bmatrix} X_1 X_1^T & X_1 X_2^T \\ X_2 X_1^T & X_2 X_2^T \end{bmatrix} \quad (1)$$

218 Let the matrix Σ_T

$$219 \quad \Sigma_T = \Sigma_{X_1 X_1}^{-1/2} \Sigma_{X_1 X_2} \Sigma_{X_2 X_2}^{-1/2} \quad (2)$$

220 By performing the singular value decomposition (SVD) on the matrix,

$$221 \quad \Sigma_T = U \Lambda V^T \quad (3)$$

222 Two canonical correlation vectors with respect to X_1 and X_2 can be defined as $J =$

223 $\Sigma_{X_1 X_1}^{-1/2} U(:, 1:l)$ and $L = \Sigma_{X_2 X_2}^{-1/2} V(:, 1:l)$, where l is the number of selected

224 components and $l \leq \min(d_1, d_2)$. The residual vectors are defined for as follows,

$$225 \quad e = L^T X_2 - \Lambda_l J^T X_1 \quad (4)$$

226 Squared predicted errors (SPE) can be formulated as follows:

$$227 \quad SPE = e^T e \quad (5)$$

228 The derived SPE is then taken as a reference to justify the desired process behavior

229 for the incoming data. In order to recognize the dissimilar behaviors properly, the

230 control limit is defined necessarily as follow:

$$231 \quad SPE_{lim} = \varsigma \chi_{1-\alpha}^2(\tau) \quad (6)$$

232 where $\varsigma = \Sigma_{SPE} / 2\mu_{SPE}$, $\tau = 2\mu_{SPE}^2 / \Sigma_{SPE}$, Σ_{SPE} and μ_{SPE} are estimated mean and

233 variance of R , α is the significance level and can be defined as 99%, 95% and 90%,

234 generally. Typically, CCA is able to act as process monitoring model. However, since

235 CCA is not sensitive to incipient fault, fault feature is usually missed.

236 2.2 Kurtosis-based Feature extraction

237 Kurtosis is one of the typical and efficient ways being able to capture signal variations.

238 The reason why Kurtosis indicator works well for feature extraction is that it is able to

239 measure the heaviness of the tails in the distribution of signal, thus leading to high

240 values of the kurtosis parameter. Therefore, the kurtosis could be used to identify

241 changes in signals. Kurtosis value is on where $x_i(t)$, $i = 1, 2, \dots, d$ and $t =$

242 $1, 2, \dots, N_t, \dots, N$, is the time series signal taken from X_1 or X_2 . d is the number of

243 variables and N is the number of sampling points. As shown in Eq. (7), σ_i^4 in

244 denominator is able to amplify the unstable variations and further extract the faulty

245 features (de la Rosa, Agüera Pérez, Palomares Salas, & Sierra Fernández, 2015;

246 Joanes & Gill, 1998).

$$247 \quad KU_i = \frac{\sum_{t=1}^{N_t} (x_i(t) - \bar{x}_i)^4}{(N_t - 1)\sigma_i^4} \quad (7)$$

248 KU_i represents the KU value with respect to the i th variable, whereas $KU_i(t)$
 249 represents the KU value with respect to the i th variable at the sample time, t . To
 250 identify the variation, we also define the amplitude as follows:

$$251 \quad KA_i = \frac{KU_i(t) - KU_i(t-m)}{KU_i(t)} \quad (8)$$

252 where m is the number of delay steps and can be determined by auto-correlation
 253 analysis and partial-correlation analysis. The purpose of Eq. (8) is to ensure that
 254 change points of KU_i can be identified timely. \bar{x}_i is the mean value of the signal x_i
 255 in the interval of $[1, N_t]$ is defined as

$$256 \quad \bar{x}_i = \frac{1}{N_t} \sum_{t=1}^{N_t} x_i(t) \quad (9)$$

257 σ is the standard deviation of the signal and is given as

$$258 \quad \sigma_i = \sqrt{\frac{1}{N_t - 1} \sum_{t=1}^{N_t} (x_i(t) - \bar{x}_i)^2} \quad (10)$$

259 Due to the normalization, KU values are assumed to follow Gaussian distributions.
 260 Also, let $x_i(t) = SPE_i(t)$ and substitute $x_i(t)$ into Eq. (7), the SPE_{KU} can be
 261 derived as Eq. (11) and justified by 3-sigma limits (three times standard deviations)
 262 can serve for fault detection.

$$263 \quad SPE_{KU,i}(t) = \left| \frac{KU_i(t) - \overline{KU}_i}{\sigma_{KU}} \right| \leq 3\sigma_{KU} \quad (11)$$

264 where \overline{KU}_i and σ_{KU} represent the mean values and standard variance of KU_i . Once
 265 $SPE_{KU}(t)$ value at the sample time t , i.e., $SPE_{KU}(t)$, crosses over the control limit
 266 $3\sigma_{KU}$, a fault state will be declared. Otherwise, it will not.

267 In this paper, KU is used for two folds. One is for feature extraction of SPE to
 268 enhance fault detection as aforementioned in the stage (1): Fault detection. Generally,
 269 CCA-based fault detection is insensitive to incipient faults. Kurtosis is able to make
 270 SPE more sensitive to incipient faults as shown in Eq. (11). The other function of
 271 Kurtosis is to refine the features from original variables and then feed to MVGC,
 272 aiming to provide preliminary sequence information for MVGC. Depending on the
 273 assumption that the variable with the earliest and significant variations could have

274 more potential to be the rooting cause, movement of the variable with the earliest and
 275 significant variations to lower dimension of the input matrix is able to facilitate
 276 MVGC analysis. This is mainly due to the fact that MVGC is based on the time series
 277 analysis and is heavily temporal correlation. Thus, the feature feeding to MVGC can
 278 be defined similarly as Eq. (7).

279 2.3 MVGC-based root cause analysis

280 Since CCA-based process monitoring is based on correlation rather than causality
 281 among data, CCA technology cannot locate exact rooting cause. In case an
 282 abnormality occurs in an industrial process, it is difficult for an operator to take
 283 accurate actions to diagnose the root cause of a fault. Also, due to the closed-loop
 284 structure of an OD process, the sludge bulking fault is not limited in a local unit, but
 285 rather propagates as global variations. This phenomenon is featured by causality
 286 which can approach the cause-effect relationship among different variables.
 287 Reorganization of the causality is to find the root cause and present the fault
 288 propagation paths before maintenance. Granger causality test is one of the approaches
 289 to deal with this issue. The main motive behind the Granger causality test is to
 290 identify causality by determining if one time series is useful in forecasting another.
 291 Also, Granger causality test is a graphical model and can provide an intuitive way to
 292 present causality.

293 Assuming that x_1 and x_2 are two time-series variables selecting from X_1 or X_2 .
 294 A time series x_1 is said to Granger-cause x_2 if x_1 values provide statistically
 295 significant information about future values of x_2 through a series of t -tests and
 296 F -tests. Suppose that the temporal dynamics of two time series $x_1(t)$ and $x_2(t)$
 297 with time lag being length p

$$298 \quad I(t) = \begin{pmatrix} x_1(t) \\ x_2(t) \end{pmatrix} \quad (12)$$

299 To qualify the G-causality from $x_2(t)$ to $x_1(t)$, $F_{2 \rightarrow 1}$ is used to stands for the
 300 “degree to which the past of $x_2(t)$ helps predict $x_1(t)$, over and above the degree to
 301 which $x_1(t)$ is already predicted by its own past”. To approach causality, a VAR
 302 (Vector Auto-regressive) model is always used. In the VAR model, the VAR(p)

303 decomposes as

$$304 \begin{pmatrix} x_1(t) \\ x_2(t) \end{pmatrix} = \sum_{j=1}^p \begin{pmatrix} A_{11,j} & A_{12,j} \\ A_{21,j} & A_{22,j} \end{pmatrix} \begin{pmatrix} x_1(t-j) \\ x_2(t-j) \end{pmatrix} + \begin{pmatrix} \varepsilon_1(t) \\ \varepsilon_2(t) \end{pmatrix} \quad (13)$$

305 where p is the maximum number of lagged observations or the model order, A
 306 represents the coefficients of the model, and $\varepsilon_1, \varepsilon_2$ are the residuals (prediction
 307 errors) for each time series. The residuals covariance is given as

$$308 \Sigma = cov \begin{pmatrix} \varepsilon_1(t) \\ \varepsilon_2(t) \end{pmatrix} = \begin{pmatrix} \Sigma_{11} & \Sigma_{12} \\ \Sigma_{21} & \Sigma_{22} \end{pmatrix} \quad (14)$$

309 The regression with respect to $x_1(t)$ is defined as follows:

$$310 x_1(t) = \sum_{j=1}^p A_{11,j} x_1(t-j) + \sum_{j=1}^p A_{12,j} x_2(t-j) + \varepsilon_1(t) \quad (15)$$

311 By exclusion of effect induced by $x_2(t)$

$$312 x_1(t) = \sum_{j=1}^p A_{11,j} x_1(t-j) + \varepsilon_1'(t) \quad (16)$$

313 Defining $cov(\varepsilon_1) = \Sigma_{11}$ and $cov(\varepsilon_1') = \Sigma_{11}'$. Thus the G-causality from $x_2(t)$ to
 314 $x_1(t)$ is defined to be the log-likelihood ratio

$$315 F_{2 \rightarrow 1} = \ln \frac{|\Sigma_{11}'|}{|\Sigma_{11}|} \quad (17)$$

316 G-causality in Eq. (17) can quantify the reduction in prediction error when the past of
 317 the process $x_2(t)$ is included in the explanatory variables of a VAR model for
 318 $x_1(t)$. If the variance of ε_1 is reduced by the inclusion of x_2 in the Eq. (16), then it is
 319 said that x_2 G-causes x_1 . Also, G-causality is easy to generalize to the multivariate
 320 (conditional) case in which the G-causality of $x_2(t)$ on $x_1(t)$ is tested in the
 321 context of multiple additional variables $x_3(t), \dots, x_d(t)$. More details can be found in
 322 the MVGC toolbox (Seth, 2010).

323 2.4 RUL prediction

324 The purpose of prognosis is to predict the time to failure of a degrading
 325 component or subsystem, also called remaining useful life (RUL), by assessing the
 326 current degradation state of a component or subsystem, its past degradation trend or
 327 profile given by the continuous monitoring module with the known future operating
 328 conditions of the component or subsystem. RUL is the time left before a component
 329 or subsystem, which is assigned for a particular job or a function, reaches its end of
 330 life. In the ASP process, SVI is always chosen to indicate the evolution of the sludge

331 bulking, thus SVI is selected as an evaluation variable to calculate RUL. RUL of
 332 sludge bulking can be expressed as

$$333 \quad RUL = \inf\{t: x_{SVI}(t) \geq C | x_{SVI}(0) < C\} = t_f - t_0 | t_f > t_0 \quad (18)$$

334 where t_f signifies the random failure time, t_0 signifies the current age. C is the
 335 threshold level and x_{SVI} is the SVI variable. To predict RUL , the evolution variable,
 336 SVI, is obtained necessarily. Degrade However, SVI cannot be observed directly.
 337 ARMA model serve as a virtual instrument to predict SVI over a long period in this
 338 paper. During the long-term prediction, historical and currently measured values are
 339 collected and served as the starting point for the first step prediction. Then, the
 340 multi-step ahead prediction based on an ARMA model is performed in a subsequent
 341 iterative way. Based on the ARMA model obtained through the above steps, iterative
 342 multi-step prediction is provided in as follows, where k is the steps of prediction:

343 When $1 < k \leq n_c$,

$$344 \quad \hat{x}_{SVI}(t_0 + k | t_0) = \sum_{i=1}^{n_a} a_i \hat{x}_{SVI}(t_0 + k - i | t_0) + \sum_{i=k}^{n_c} c_i \hat{v}(t_0 + k - i) \quad (19)$$

345 where \hat{x}_{SVI} are the predicted values of SVI and $\hat{v}(t), \hat{v}(t-1), \dots, \hat{v}(t+k-n_c)$
 346 can be estimated by the Recursive Extended Least Square (RELS) method. More
 347 details can see the reference (J. Chen, Ganigue, Liu, & Yuan, 2014). n_a, n_c are the
 348 orders of a and c , respectively.

349 When $k > n_c$,

$$350 \quad \hat{x}_{SVI}(t_0 + k | t_0) = \sum_{i=1}^{n_a} a_i \hat{x}_{SVI}(t_0 + k - i | t_0) \quad (20)$$

351 when $t_0 + k - i \leq t_0$, $\hat{x}_{SVI}(t_0 + k - i | t_0) = x(t_0 + k - i)$. Therefore, assuming
 352 the prediction horizon $L > n_c$, multi-step optimal prediction $\hat{x}_{SVI}(t_0 + k | t_0)$, $k =$
 353 $1, 2, \dots, h_1$ can be recursively obtained by applying the estimated values $\hat{a}_i, \hat{c}_i,$
 354 $\hat{v}(t_0), \dots, \hat{v}(t_0 + k - n_c)$ to replace $a_i, c_i, v(t), \dots, v(t_0 + k - n_c)$ in Eq.(19) and
 355 Eq.(20). h_1 is the terminal point during the prediction horizon.

356 2.5 Maintenance

357 The challenge afterward mainly lies in decision-making after identifying the root
 358 cause of sludge bulking. Even though many schemes have been proposed to deal with
 359 this problem, few experts devote to summarize this field knowledge.

Table 1 Causal matrix for filamentous sludge bulking

Monitored variables and their abbreviation	T	BOD ₅	TP	COD	SNO	SRT	MLSS	TN	SVI
(1) Temperature (T)	NaN	0.0075	0.0003	0.0076	0.0005	0.0126	0.0089	0.0013	0.0265
(2) Biological Oxygen Demand concentration in effluent for five days (BOD ₅)	0.0135	NaN	0.0447	0.0032	0.0001	0.0001	0	0	0.0010
(3) Total phosphorus (TP)	0.0008	0.0172	NaN	0.0001	0.0001	0.0001	0.0085	0.0023	0.0111
(4) Chemical Oxygen Demand (COD)	0.1099	0.0199	0.0091	NaN	0.0138	0.0159	0.0080	0.0178	0.0074
(5) NO ₂ -N (SNO)	0.0357	0.0094	0.0347	0.0046	NaN	0.0007	0.0076	0.0129	0.0007
(6) Sludge Retention Time (SRT)	0.0024	0.0028	0.0002	0.0038	0	NaN	0.0112	0.0408	0.0380
(7) Mixed liquid suspended solids (MLSS)	0.0236	0.0291	0.0444	0	0.0071	0.0331	NaN	0.0190	0.0131
(8) Total nitrogen concentration in effluent (TN)	0.0091	0.0068	0.0589	0.0315	0.0167	0.0010	0.0293	NaN	0.0089
(9) Sludge Volume Index (SVI)	0.2748	0.0092	0.0002	0.0001	0.0351	0.0009	0.1181	0.008	NaN

(1), ..., (9) REPRESENT THE ORDER OF VARIABLES IN THE MVGC ANALYSIS; (X1) MEANS THIS VARIABLE IS IN THE VECTOR X1;
 (X2) MEANS THIS VARIABLE IS IN THE VECTOR X2;

360 As profiled in Fig.1, deterioration of sludge bulking typically becomes more severe
 361 as the time evolution. For different stage, we have to take different actions. Firstly, we
 362 summarized the basic preventive maintenance strategies from many WWTPs as Table
 363 S1. Preventive maintenance is performed as Table S1 (Supplementary Information),
 364 once Eq. (10) is met (SPE_{KU} control limit). Also, RUL can be derived by calculating
 365 Eq. (18) in this stage. By investigating Table S1 deeply, nine typical Sludge bulking
 366 scenarios are summarized with respect to different root cause.

367 For some cases, preventive maintenance is not able to approach sludge bulking
 368 completely. To ensure sufficient time to perform the corrective maintenance if
 369 crossing over the corrective control limit, we define the corrective control limit
 370 (CCL_{limit}) as follows:

$$371 \quad \hat{x}_{SVI} > 50\%(200 - SPE_{KU}) = CCL_{limit} \quad (21)$$

372 50% was derived by trading off the volume of dosed chemicals, the type of dosed
373 chemicals as well the severity degree of sludge bulking by the field experts. During
374 the corrective maintenance, we have to further added coagulants or FeSO₄ to kill
375 filamentous bacteria. However, once SVI cross over 200 mg/L, we have to shut down
376 the wastewater plant to avoid polluted wastewater discharge into river.

377 **3 Results and discussions**

378 The proposed predictive CBM framework is assessed by a full-scale Oxidation Ditch
379 (OD) WWTP in Beijing. This section describes the detail of the corresponding
380 WWTP with filamentous sludge bulking.

381 3.1 A full-scale WWTP with an OD treatment

382 In this case study, a full-scale WWTP (Beijing, China) with a modified activated
383 sludge process is presented for assessment (Fig. 2). This modified treatment process is
384 able to improve biodegradable organics removal by resorting to utilize long solids
385 retention times (SRTs). The main parameters of this WWTP are shown as follows: the
386 average influent flow is about 170, 000 m³/d; an average OD hydraulic retention time
387 (HRT) is 16.5 h; SRT is equal to 15-22 d. The main reason why OD is applied in
388 many WWTPs is that removal performance can be achieved with lower weir overflow
389 rate, less sludge production and more energy savings. However, due to the larger land
390 area requirement than typical activated sludge treatment processes, suspended solids
391 concentrations in the discharge of a WWTP occurs frequently. Filamentous sludge
392 bulking occurred due to the significant temperature decrease in this case. All data are
393 sampled at one-day interval. The selected monitored variables for model construction
394 are shown as Table S2 (Supplementary Information). 213 data points are sampled
395 from the field at day interval. From the 70th day of the collected data, filamentous
396 sludge bulking has occurred slightly due to the low temperature of influent and lasts
397 over about half a year. During this period, part of polluted wastewater has been
398 flowed into the river without any declaration.

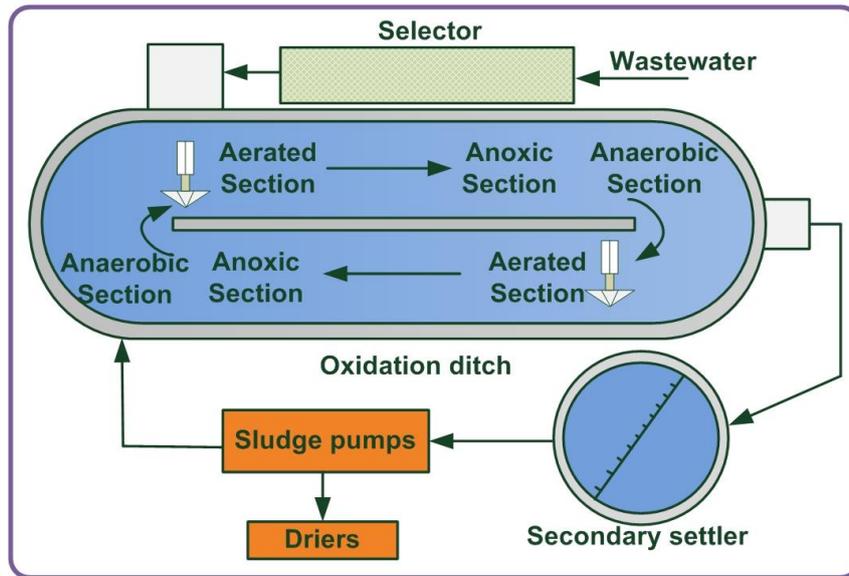


Fig. 2 Schematic diagram of a full-scale oxidation ditch process

399

400

401 The reason why filamentous sludge bulking is difficult to control mainly lies on the
 402 fact that, based on evidence provided by microbiological observations by Ovez and
 403 Orhan (Ovez S, 2007), chemical dosage for most cases provides only temporary and
 404 superficial way for the treatment of filamentous sludge bulking. The existence of
 405 uncertainties, such as weather, operation, and so on, adds further complexity for
 406 filamentous sludge bulking. Therefore, it is imperative to propose a framework to
 407 support filamentous sludge bulking, which can also be assisted with the expert
 408 knowledge.

409 3.2 Performance evaluation criteria

410 To evaluate the performance of CCA-based fault detection, both of Type-I error
 411 (faulty detection rate) and Type II error (false alarm rate) are used in this paper
 412 (Narayana Moorthy, Martins, Sousa, Ramos, & Fernandes, 2014). Type-I error is to
 413 describe how many faulty samples are mis-identified as normal samples. Thus,

414 Type I error = $\frac{\text{number of mis-identified faulty samples}}{\text{total number of faulty samples}}$. On the contrary, Type-II error is to

415 describe how many normal samples are mis-identified as faulty samples. Thus,

416 Type II error = $\frac{\text{number of mis-identified normal samples}}{\text{total number of normal samples}}$.

417 The Root Mean Square Error (RMSE) and correlation coefficient (r_c) were used to
 418 assess the prediction performance of ARMA model. The RMSE is defined as follows
 419 for quality comparisons of different models:

$$420 \quad RMSE = \sqrt{\frac{1}{N} \sum_{i=1}^N (y_i - \hat{y}_i)^2} \quad (23)$$

421 where y_i and \hat{y}_i are the measured and prediction values, respectively. The
 422 correlation coefficient (r_c) is quantified as follows:

$$423 \quad r_c = \frac{\sum_{i=1}^N (y_i - y'_i)(\hat{y}_i - \hat{y}'_i)}{\sqrt{\frac{1}{N} \sum_{i=1}^N (y_i - y'_i)^2} \sqrt{\frac{1}{N} \sum_{i=1}^N (\hat{y}_i - \hat{y}'_i)^2}} \quad (24)$$

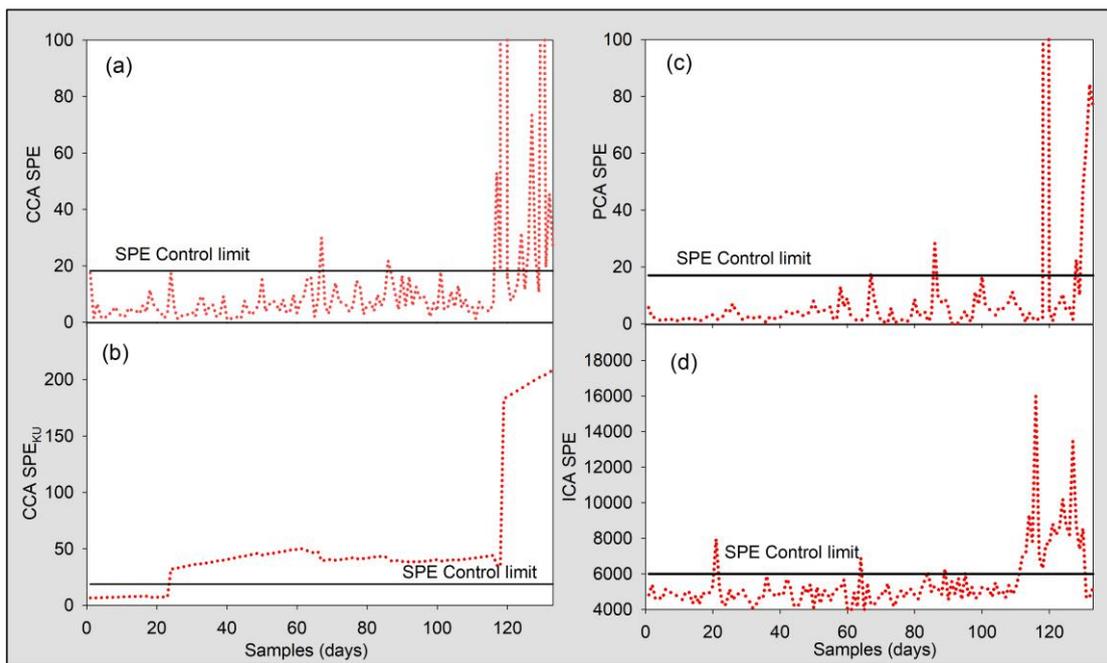
424 y'_i and \hat{y}'_i are the mean of y_i and \hat{y}_i , respectively. N is the number of datasets.

425

426 3.3 Fault detection

427 The purpose of this section is to detect an incipient fault as early as possible, which
 428 will facilitate the fault pre-caution and guarantee sufficient time for sequential
 429 maintenance. In our methods, CCA is used for incipient fault detection firstly. The
 430 number of latent variables for CCA, l , is selected as 5. $X_1 =$
 431 $[SRT, T, MLSS, SNO, COD]$ and $X_2 = [TP, BOD_5, TN, SVI]$. X_1 is a vector
 432 consisting of easy-to-measured variables, whereas X_2 is composed of the
 433 hard-to-measured variables in the discharge of the wastewater plant. For the 213 data
 434 points, 50 samples are used for fault detection model training, whereas the remaining
 435 is used for testing. By performing Eq. (4)-(6), it is obvious in Fig. 3 (a) that the SPE is
 436 able to detect the fault until the 120th day of the testing set approximately. To achieve
 437 better performance of fault detection in our methodology, KU is further used to
 438 enhance the SPE signals of CCA to refine the fault features. On the basis of Eq. (11),
 439 SPE_{KU} and its control limit are derived. Due to the incorporation of KU, the SPE_{KU} is
 440 able to recognize the incipient fault at the 23rd day of testing set, which is 97 days
 441 earlier compared with the pure SPE index of CCA (Fig. 3 (b)). This mainly lies in the
 442 fact that KU is capable of amplifying the residual errors and making fault detection
 443 more sensitive. As shown in Fig.3 (b), the control limit of SPE_{KU} is learned from the
 444 training data, whose significant level is 0.05. For SPE, Type II error is equal to

445 4/20=20% and Type I error is equal to 95/143=66.4%. However, for SPE_{KU} , Type II
 446 error is equal to 0/20=0% and Type I error is equal to 3/143=2.1%. Therefore, it is
 447 obvious that SPE_{KU} achieved better performance than SPE in terms of Type II and
 448 Type I errors. To fully compare with other typical fault detection methods,
 449 PCA-based and ICA-based methods are also implemented. PCA-based and ICA-based
 450 SPE achieved similar performance with CCA counterpart, but still performed worse
 451 than CCA-based SPE_{KU} (Fig. 3 (c) and Fig. 3 (d)) in terms of Type II and Type I
 452 errors.

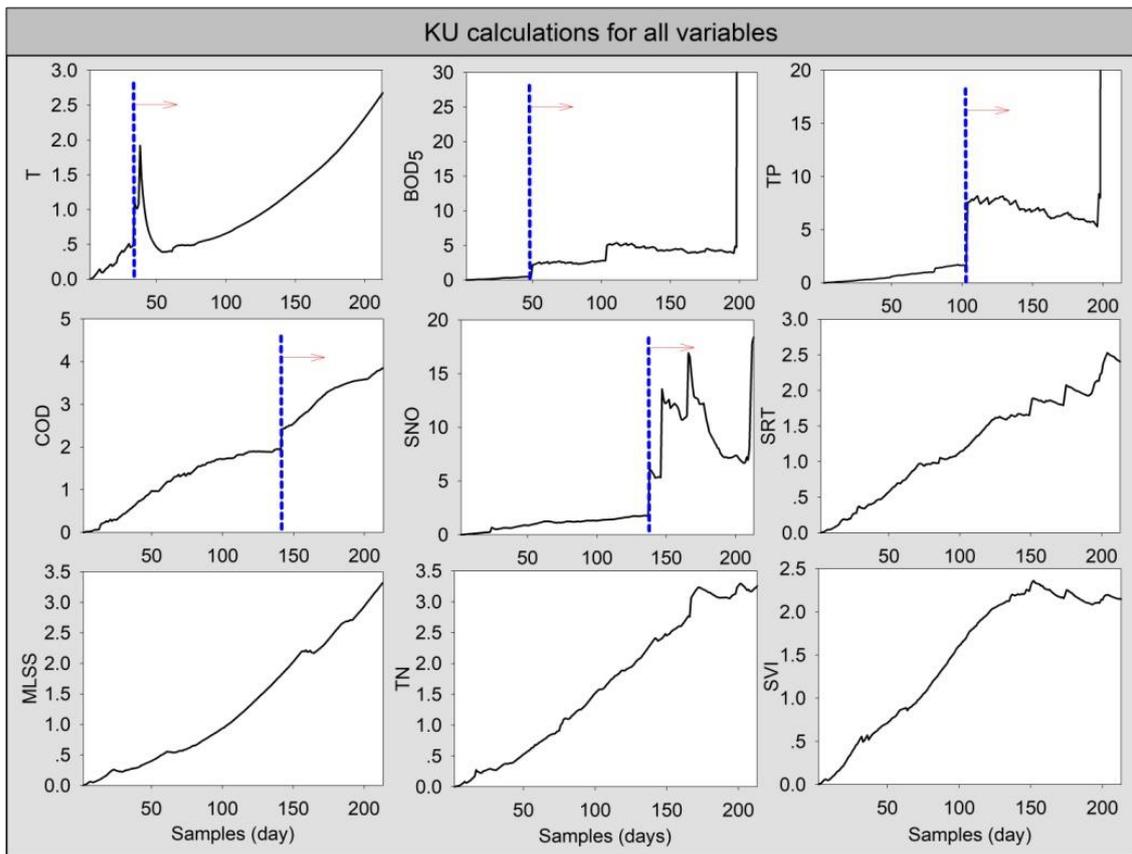


453
 454 Fig. 3 SPE-based Fault detection with PCA, ICA and CCA

455 3.4 Fault identification

456 Traditionally, contribution plot based fault identification methods usually result in
 457 smearing effect and then leading to false identification. To deal with this problem, KU
 458 is firstly used to extract features for each variable as shown in Fig.4. To further
 459 capture the variation features, the variation rate, KA_i , is designed to assess the true
 460 occurrence time. Based on Eq. (8), the degree of variations for each variable can be
 461 derived. As profiled in Fig. 4, the variables, $[T, BOD_5, TP, COD, SNO]$, exhibit
 462 significant variations during different time domain, but others are not. It is import to
 463 notice that the sludge bulking occurs at the 70th day (20th day in the testing dataset)

464 and it is identified at the 73th day (23th day in the testing dataset). During this period,
 465 the obvious variations can be only seen from T and BOD_5 . Due to the time delay
 466 among variables, it is reasonable to assume that the occurrence of abnormal events for
 467 the first time could be the source of a fault. Therefore, the sequences of variables in
 468 the original data set are reorganized as the first column of Table I. Since the
 469 filamentous sludge bulking is typically indicated by SVI, SVI serves as the target
 470 variable and tabulates as Table 1 (Row 10, Column 10). The reason why the proposed
 471 framework re-organizes variable sequence herein is that the core of MVGC is time
 472 series analysis favoring temporal features and re-organization of variables is able to
 473 facilitate the graphical representation.



474

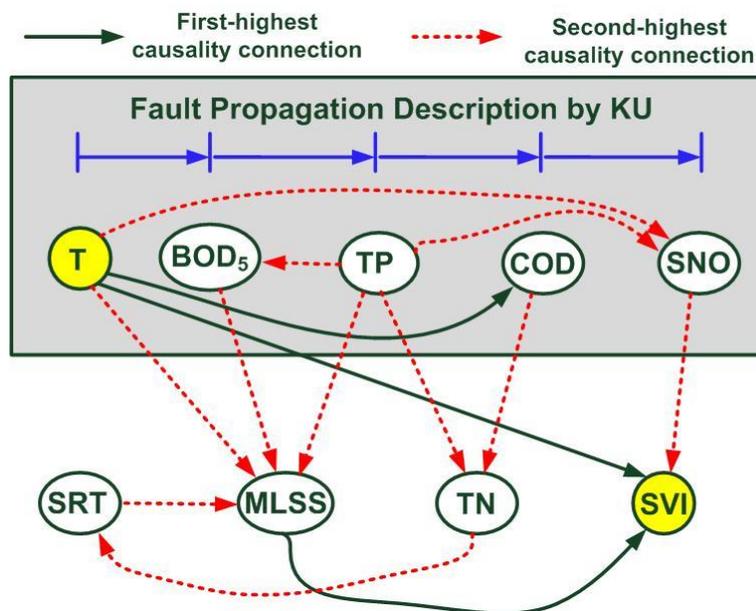
475

Fig. 4 Feature extraction for each raw variable by KU

476

477 The refined features by KU are then fed to MVGC for causality analysis. The causal
 478 results as tabulated in Table 1 show that the highlighted red cells suggest the
 479 maximum causal effect of column variables among variables. Fig. 5 further shows the

480 first-highest causal relationship among variables, i.e., COD, SVI and MLSS.
 481 Moreover, the causality network is built as Fig. 5 based on the cause-effect correlation
 482 of Table 1. During the network construction, since $F_{SRT \rightarrow MLSS} > F_{MLSS \rightarrow SRT}$ (Table
 483 1), direction $F_{SRT \rightarrow MLSS}$ is selected. This can be explained by the fact that longer
 484 SRT is indeed able to result in higher MLSS. In the mean time, $F_{T \rightarrow SVI} > F_{SVI \rightarrow T}$
 485 (Table 1), direction $F_{T \rightarrow SVI}$ is selected. The temperature variation mainly comes
 486 from influence of external environment, rather than the treatment processes itself.
 487 Thus, it is reasonable to explain that the varied temperature T will lead to the variation
 488 of SVI by affecting the bacteria behaviors. The results in Fig. 5 suggest that, due to
 489 acting as the most sources for other variables, T has the highest probability to be the
 490 cause of the occurrence of a fault and SVI is the final target variable. It deserved to
 491 notice from Fig.5 that both solid lines that generated from T are able to converge into
 492 SVI. One is $T \rightarrow SVI$. The other is $T \rightarrow COD \rightarrow TN \rightarrow SRT \rightarrow MLSS \rightarrow SVI$. Both represent
 493 the relative highest probability of the fault propagation. Therefore, the developed
 494 algorithm for fault amplification can be efficiently used to indicate the fault
 495 propagation path in a graphical way.

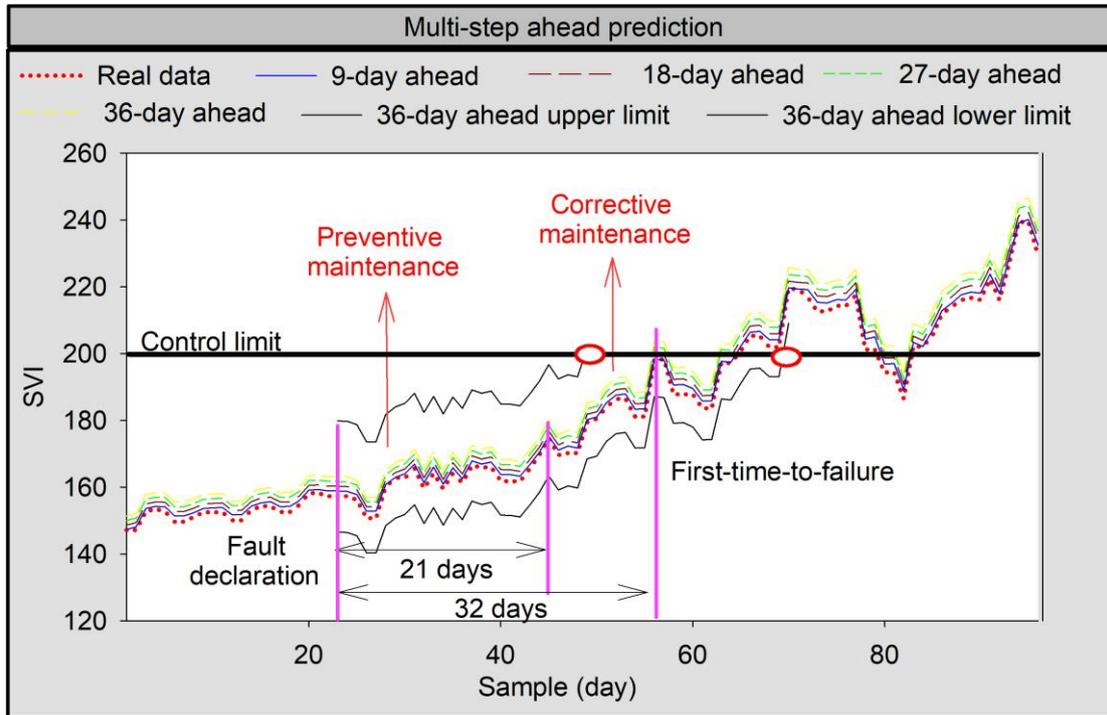


496
 497 Fig. 5 Fault propagation route

498 3.5 Fault prognosis and RUL prediction

499 To implement the RUL prediction, ARMA is used for multi-step-ahead prediction

500 of SVI firstly over a long term once the incipient fault is declared by the SPE_{KU} at the
501 23rd day (during the testing dataset). The data are treated by the first-order
502 differencing. Then, the orders for AR term and MA term are selected for 3 and 1,
503 respectively by analyzing the ACF (Auto-correlation Function) and PCF (Partial
504 correlation Function) (More details can see the Supplementary Information). 36 steps
505 ahead predictions are derived in this case study. Among them, 9-step,18-step,27-step
506 and 36-step ahead predictions are shown in Fig. 6, suggesting that all the prediction
507 results are acceptable, even though the prediction performance is accompanied by
508 somehow deterioration as more steps ahead prediction is performed (Table 2). The
509 deterioration is mainly due to lack of necessary information to compensate the
510 prediction deviation as prediction horizon moves ahead. It is important to notice that
511 the deterioration is not that obvious between the 23rd day and 43rd day. On the
512 contrary, the deterioration of multi-step-ahead prediction become more obvious after
513 the 55th day. This can be partly explained that an ARMA model is linear model and
514 more suitable for a fairly stationary process (0-43rd day), whereas performs worse in
515 the non-stationary process (after the 43rd day). After the incipient fault declaration, the
516 fault costs 32 days to reach the control limit, 200 mg/L, for the first time. That is,
517 RUL is equal to 32 in this case study. It is important to notice in Fig. 6 that the
518 uncertainty level of 36-day-ahead prediction using an ARMA model can be profiled
519 as an envelope. Even though uncertainties from the former algorithm chain
520 (CCA-SPE-KU-MVGC-ARMA) cannot be described by each step, all of them can be
521 ultimately reflected upon the uncertainty level of the ARMA-based predictions. If
522 conserved decision-making is necessary, 36-day-ahead upper limit will be preferred to
523 decide the RUL. RUL is equal to 26, which is 6-day-ahead over the scenario
524 depending on the mean values based decision-making.



525

526

Fig. 6 Multi-step prediction on the basis of an ARMA model

527

Table 2 RMSE and r_c of multi-step prediction using a ARMA model

Index	9-day-ahead	18-day-ahead	27-day-ahead	36-day-ahead
<i>RMSE</i>	1.63	3.19	4.83	6.5
r_c	0.983	0.975	0.967	0.959

528

529 3.6 Maintenance strategy

530 By aforementioned analysis, the sludge bulking stems from abnormal temperature
 531 variations. In wastewater treatment system, seasonal variations always induce
 532 temperature oscillations, therefore imposing negative influence on the metabolic
 533 activities for the microbial population and the gas-transfer rates as well as the settling
 534 characteristics of activated sludge. Typically, 25-35 °C is considered as the optimum
 535 temperatures for common bacteria. Particularly, when the temperature dropped to
 536 around 5 °C, the autotrophic nitrifying bacteria will de-function. Once the control
 537 limit of SPE_{KU} is reached, preventive maintenance is triggered. To deal with this
 538 problem, preventive maintenance actions are implemented with the aid of Table S1
 539 (Supplementary Information). The day that the SPE_{KU} is reached is 23rd and SVI is

540 equal to 157.3 mg/L. CCL_{limit} can be derived as 178.3 mg/L by Eq. (21). Therefore,
541 21 days are kept for preventive maintenance, the remaining 11 days are left for
542 corrective maintenance. To minimize the negative effect of temperatures during
543 preventive maintenance stage, adjustment of operational parameters is necessary,
544 including SRT, C/N ratio, pH, TN and SNO. By analyzing Fig. 5, SRT, BOD_5 and TP
545 can have direct effect on SVI through MLSS. In a wastewater plant, SRT is the most
546 convenient factor among them to adjust. Once the preventive maintenance strategy
547 does not work well and the CCL_{limit} is attained, corrective maintenance has to be
548 triggered. During this stage, we have to further add coagulants or $FeSO_4$ to kill
549 filamentous bacteria. However, in case that SVI crosses over 200 mg/L, we have to
550 shut down the wastewater plant to avoid polluted wastewater discharge into river.
551 Additionally, it is worthwhile to notice that, by defining preventive and corrective
552 maintenance for sludge bulking control, a guideline can be formed and the operators
553 could achieve better control performance with lower operational cost, rather than
554 operating in an ad-hoc way.

555 3.7 Discussion: implications, implementation and future research

556 The present work proposes a condition-based maintenance framework. In this novel
557 hybrid framework, fault detection, location, propagation identification, remaining
558 useful life (RUL) prediction and maintenance are performed for sludge bulking
559 control. This is the first attempt to propose a framework for sludge bulking
560 management systematically, providing water utilities with a tool for sludge bulking
561 control. The results showed that this framework can be successfully applied to
562 filamentous sludge bulking management. To facilitate discussions, a flowchart that
563 briefly the calculation process is shown as Fig. 7.

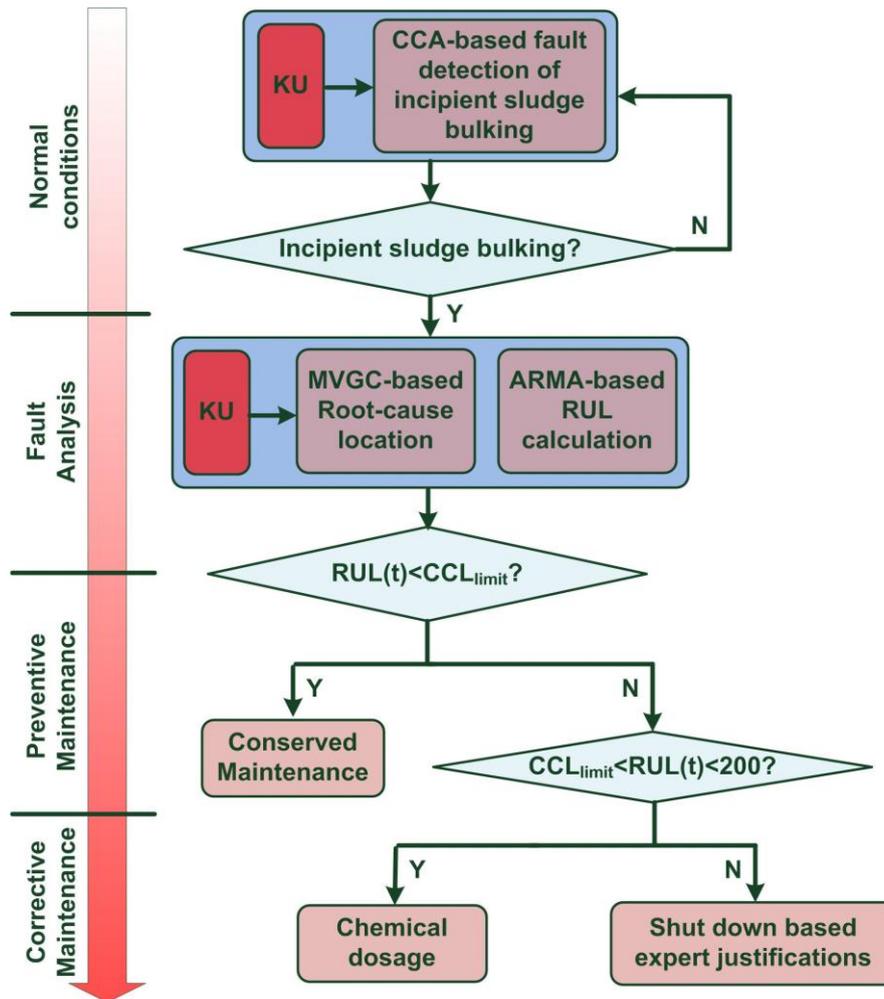


Fig. 7 The flowchart of proposed framework

564

565

566 In this work, even though PCA, ICA and PLS could perform better than CCA or
 567 maybe not, it is still the first attempt to use statistical method to serve as a pre-alarm
 568 system rather than just act as a fault detection component. Also, MVGC, ARMA and
 569 KU can be substituted by their similar algorithms if necessary. In fact, the motive
 570 behind this paper is to overcome the limitations of individual methods and strengthen
 571 global system collaboration by coordinating CCA, MVGC, ARMA, KU and Expert
 572 knowledge from a systematic point of view. Another issue in this work is the
 573 uncertainty analysis of hyper-parameters, such as the order of ARMA model, the
 574 number of latent variables for CCA, the percentage to separate RUL for preventive
 575 and corrective maintenance, and so on. One of potentials is resorting to build a
 576 meta-analysis model upon the system, which is able to use heuristic methods, such as
 577 Artificial Bee Colony, Cuckkoo search, Firefly algorithm and so on (Cheng, Chou, &

578 Cao, 2017), to optimize these hyper-parameters automatically, rather than depend on
579 empirical setting. In addition, since the algorithms, i.e., CCA-SPE-KU-MVGC-
580 ARMA-Expert knowledge table, is serially connected with each other in the proposed
581 framework, a slight fault in the former component could lead to the latter system
582 failure. Even if these issues cannot be fully solved, the maintenance and operations
583 are indeed alleviated significantly by involvement of operators in the fault detection,
584 location and prognosis components. Moreover, to assess these uncertainties,
585 sensitivity analysis is one of alternatives able to gain essential insights on algorithm
586 behavior, on its structure and on its response to changes in the algorithm inputs (Feng,
587 et al., 2019). Local sensitivity analysis methods (such as generalized tornado diagrams,
588 Spiderplots, Differentiation-based methods, and so on) and global sensitivity analysis
589 methods (such as Monte-Carlo-simulation, Gaussian processes model, Bayesian
590 Networks, and so on) have been developed, giving rise to the chain behaviors
591 exploration (Borgonovo & Plischke, 2016; Pianosi, et al., 2016). Another solution is
592 to take the algorithm chain as a serial system for reliability analysis (Feng, et al., 2019;
593 B. Liu, Yeh, Xie, & Kuo, 2017). It is also important to notice that the condition-based
594 maintenance is a partially automatic rather than a fully automatic system. This
595 represents that human maintenance behavior is also necessary and formulates a
596 Human-Cyber-Physical Systems (HCPS) for optimization (He, Chan, Qiao, &
597 Guizani, 2018).

598 In this article, KU is able to improve CCA and MVGC to make them more sensitive
599 to detect and locate the root of the fault. KU is sensitive to impulsive faults, especially
600 incipient faults, but are less effective for performance degradation assessment because
601 filter-based kurtosis value decreases gradually as fault severity grows. However, other
602 indicators, such as the root mean square (RMS), have less sensitivity to impulse faults,
603 but can reflect the growth of fault severity. Coordination of KU and other indicators to
604 improve the effectiveness can be studied in future. In our case studies, *RMSE* and
605 correlation coefficient (r_c) are used to assess the prediction performance of an ARMA
606 model. To clarify and enhance comparison of a model prediction performance, mean

607 absolute error (MAE), mean absolute relative error (MARE), Bias statistical
608 parameters, Akaike Information Criterion (AIC), mean squared error (MSE), Bayesian
609 Information Criterion (BIC) or Schwarz Bayesian Criterion (SBC) can be also served
610 as performance indicators (Bonakdari, Zaji, Shamshirband, Hashim, & Petkovic, 2015;
611 Can, Tosunoglu, Lu, & Kahya, 2012; Isa Ebtehaj, Bonakdari, Moradi, Gharabaghi, &
612 Khozani, 2018; Shaghaghi, Bonakdari, Gholami, & Ebtehaj, 2017; Yurekli, Kurunc, &
613 Ozturk, 2005). The prediction model used in MVGC is an ARMA model, which is
614 limited in capturing linear relationship among variables. The next step will extend
615 MVGC to nonlinear MVGC or enhance transfer entropy based causality analysis. In
616 terms of field implementation, this methodology has been designed as simple as
617 possible, thus should be implementable in most of the commercially available PLC
618 systems.

619

620 **4 Conclusions**

621 A novel condition-based maintenance framework, consisting of fault detection,
622 location, identification, RUL prediction and maintenance, was proposed and applied
623 to an oxidation process for filamentous sludge bulking management. In this
624 framework, CCA with Kurtosis indicator was indeed able to capture the sludge
625 bulking features as earlier as possible with Type I error and Type II error being 2.1%
626 and 0%, respectively. Sequentially, MVGC was feasible to diagnose the root cause of
627 the fault and showed the propagation pathways of the fault in the system graphically.
628 32-steps-ahead predictions were derived by a virtual measurement (an ARMA model)
629 and assessed in terms of $RMSE$ (6.5) and r_c (0.959). Given the prediction outcome of
630 the virtual sensor, an associated maintenance strategy was suggested to intervene the
631 filamentous sludge bulking. Compared with the existing methods, the proposed
632 framework exhibits a distinct advantage to treat the maintenance a systematic point of
633 and provide a guideline for filamentous sludge bulking management. Last but not
634 least, we envision reasonably that correctly locating the root-cause of sludge bulking
635 and timely recognizing the fault evolutions are able to avoid under-intervention or

636 over-intervention bulking management, thus saving more work force and chemical
637 dosage costs. Without loss of generality, the proposed framework is applicable to
638 manage other degradation processes, such as material corrosion, sensor drifting errors,
639 and so on. However, the coordination of preventive and corrective maintenance is not
640 globally optimized. In the future research, we will investigate on integrating
641 maintenance with evolutionary algorithms to optimally assign preventive and
642 corrective tasks.

643

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648

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