

30 FFC was $R^2 = 0.93$, reflecting an acceptable predictive power of this model. Since the
31 flowability of the blends can be predicted from single component size and shape
32 descriptors, the integrated network can assist formulators in selecting excipients and
33 their concentrations to improve flowability with minimal experimental effort and
34 material. The presented modelling approach can thus be employed instead of actual
35 measurements throughout the process development stage resulting in the (i) minimization
36 of the time required, (ii) exploration and examination of the design space, and (iii)
37 minimization of material waste.

38 **Keywords:** Integrated network; Pharmaceutical powder; Powder flow; Radial basis function.

39 **Abbreviations:** RBF, radial basis function; IN, integrated network; FFC, flow function
40 coefficient; PLS, partial least square; MCC, microcrystalline cellulose; DEM; discrete element
41 method; PE, Polyethylene; PVC; Polyvinylchloride; PF; Phenylformaldehyde resin; SEM,
42 scanning electron microscope; MISO; multi-input single output; RMSE, root mean square error

43

44 1. Introduction

45 Powder flow along with powder compression properties play a crucial role in the
46 manufacturing of pharmaceutical tablets. Powder flow, in particular, is a critical issue of
47 practical importance in those industries that primarily deal with granular materials such as the
48 pharmaceutical industry, this being due to the fact that the flow behaviour can significantly
49 affect the manufacturing efficiency and final product quality (e.g. dose uniformity) [1]. Poorly
50 flowing powders can, for instance, lead to segregation during die filling before compaction [1].
51 Powders with good flowability characteristics (easy and free flowing powders) are therefore
52 vital to prevent tableting issues and ensure a consistent quality of the final drug product [2]. In
53 general, two main forces usually affect powder flow: (i) driving forces that consist of

54 gravitation, powder mass and the angle of inclination of the powder in relation to any bed; and
55 (ii) dragging forces that usually include cohesion forces between similar surfaces, adhesion
56 between unlike surfaces, water bridges and mechanical interlocking, and electrostatic forces
57 [3-7]. Powders are, accordingly, classed to be free flowing when the driving forces are much
58 more than the dragging ones, whereas poor powder flow occurs when the dragging forces are
59 the primary forces in the powder bed [8]

60 A considerable body of research has been devoted to the understanding of particle and
61 granular flow properties and the factors that affect these properties using various
62 pharmaceutical powders [2-3, 8]. For instance, it has been found that particle flow properties
63 are significantly affected by particle size and shape for both brittle and elastic pharmaceutical
64 powders [9]. Garg *et al.* (2018) studied two commonly used brittle pharmaceutical powders,
65 namely, Calcium Phosphate and Dicalcium Phosphate. It was shown that the Calcium
66 Phosphate with a relatively larger particle size displayed good flow properties and less
67 cohesiveness when compared to the Dicalcium Phosphate with a relatively large particle size
68 [9]. Fu *et al.* (2012) investigated three grades of Lactose powders. The obtained results
69 indicated that the powder flow properties of the three grades were significantly affected by
70 both the particle size and shape [10]. The flow of elastic powders such as Microcrystalline
71 Cellulose (MCC) was also sensitive to the changes in the particle size and shape [11]. Hou and
72 Sun (2008) examined the flow of eleven grades of MCC. The results demonstrated a decrease
73 in the powder flow rate with a decrease in the particle size even though the chemical nature
74 and particle morphology were similar. In addition, it was found that a change in the particle
75 morphology towards a more spherical morphology led to better flow and less cohesiveness.
76 Furthermore, surface modifications (e.g. using silicified MCC) also led to better flow properties
77 [11].

78 Modelling and predicting the powder flow properties of a material are essential in many
79 pharmaceutical, chemical and agricultural applications. In general, modelling paradigms can
80 be classified as either mechanistic (or semi mechanistic) or data-driven models. For example,
81 a data-driven model, partial least square (PLS) regression, was developed to linearly relate the
82 particle size and shape distributions represented by multiple descriptors to the bulk powder
83 flowability of various pharmaceutical materials [12]. Kachrimanis *et al.* (2003) implemented
84 an artificial neural network, as a data-driven model, to map eight inputs to the powder flow rate
85 in a circular orifice using three different pharmaceutical excipients [13]. In addition, the
86 discrete element method (DEM), as a numerical method that is usually utilized to
87 model/simulate the motion of a relatively large number of small particles, was utilized to
88 simulate the flow behaviour of various powders [14-15]. Such a method allows one to model
89 and consider the effect of equipment dynamics. Furthermore, a kinematic flow model, as a
90 semi-mechanistic paradigm, was also established to characterize the particles flow in two-
91 dimensional moving bed using three materials, namely, Polyethylene (PE), Polyvinylchloride
92 (PVC) and Phenylformaldehyde (PF) resin [16]. The presented modelling paradigms (i.e.
93 mechanistic- and data-driven models) have, in general, their limitations and strengths. On the
94 one hand, mechanistic (or semi-mechanistic) based models can be implicitly built on some
95 assumptions (e.g. monodisperse particle size distribution) that are not usually valid and may
96 lead, as a result, to inaccurate results [17]. In addition, some of these models (e.g. DEM) are
97 considered to be computationally taxing, particularly when more than billions of particles need
98 to be considered, which is the actual case in powder flow [17]. Data-driven models, as the name
99 indicates, rely significantly on the available data and its quality, which may include not only
100 the number of the data points but also their distribution in the space under investigation [18].
101 As such, sparse and limited amount of data can decrease the performance of a data-driven
102 models [18]. Modelling and predicting the powder flow behaviour is indeed a challenging task,

103 this being due to (i) large number of parameters (e.g. several particle size and shape factors)
104 that affect the powder flow; (ii) **a huge variety of excipients and APIs as well as mixtures**
105 **of various excipients and API's that may possess different flow characteristics to their**
106 **parent materials. Huge efforts are being towards the understanding of powders and as**
107 **such their predictions. Authors such as Wang *et al.* (2016) have successfully established**
108 **mathematical correlations between cohesion and the flow function coefficient. Their**
109 **analysis of 41 powders using a ring shear tester enabled the proposed method that**
110 **augmented shear cell data analysis and significantly reduced the complexity of the shear**
111 **cell data also [19]. Leung *et al.* 2017 further studied 1130 powders to test this correlation.**
112 **The authors identified a near-perfect inverse correlation between the flow function**
113 **coefficient and cohesion. It was concluded that improving the flowability of**
114 **pharmaceutical powder requires an alteration in the interparticulate properties rather**
115 **than altering the friction properties of pharmaceutical powders [20]. A big data**
116 **approached was also used by Megarry *et al.* 2019 where the authors examined 3909**
117 **historical experimental data from a shear cell. Their characterisation aided in**
118 **establishing an operating space that can be used as a process flow map to guide**
119 **formulators in future development [21].**

120 In this research work, the ultimate aim is to develop a fast, cost effective and more
121 accurate predictive model to represent the powder flow properties of various pharmaceutical
122 **powders and blends from single component data. This model can guide formulators to**
123 **select excipients and their concentration that optimises the powder flowability.** Firstly, a
124 single radial basis function (RBF) network, as a relatively simple model, is implemented to
125 map the particle size, shape **and different blend ratios** to the flow properties. **The RBF**
126 **network was, however, not able to describe the complex nature of powder flowability**
127 **resulting in a poor prediction performance. This was addressed by developing an**

128 integrated network **based on a combination of RBF models. Since the integrated network**
129 **can mathematically be represented as a combination of superposition and composition**
130 **functions that are usually dense in a convex data space, it can circumvent** the challenges
131 posed by the single RBF network.

132 **2. Materials and Methods**

133 2.1. Materials

134 Three pharmaceutically-relevant powder materials having different grades were
135 investigated in this research paper. These powder materials are MCC, Dicalcium Phosphate
136 Dehydrate and Lactose. Eight grades of MCC having different particle size and shape were
137 supplied by JRS Pharma (UK). These grades are VivaPur® MCC PH101, VivaPur® MCC
138 PH102, VivaPur® MCC PH105, VivaPur® MCC PH100, VivaPur® MCC PH200, VivaPur®
139 MCC PH302, MCC Prosolv 50 and MCC Prosolv 90. Five Dicalcium Phosphate Dihydrate
140 grades, namely, DI-CAFOS A12, DI-CAFOS A60, DI-CAFOS A150, DI- DI-CAFOS D14
141 and DI-CAFOS D16, were supplied by Chemische Fabrik Budenheim KG (Germany). Seven
142 Lactose Monohydrate grades were supplied by MEGGLE Group (Wasserburg, Germany).
143 These are Flowlac 90, Flowlac 100, Granulac 70, Granulac 200, Inhalac 250, Inhalac 400 and
144 Tablettose 80. In addition to being commonly used in the pharmaceutical industry, these
145 powder materials were selected for this research work because of their different flow
146 properties. The range of powder properties was further extended by mixing a combination of
147 the different excipients at various ratios (3:1, 1:1, 1:3) as denoted in Table ???. Furthermore,
148 such a range of **pharmaceutical excipients and blends with different properties as utilized**
149 **aids in the building of a robust flow model.**

150 2.2. Particle Size and Morphology Analysis

151 Electron micrographs of all the excipient grades were obtained using a scanning
152 electron microscope (SEM) (Quanta FEG 250), which was operated at 20kV. The samples were
153 mounted on a metal stub with double-sided adhesive tape and coated under vacuum with carbon
154 in a nitrogen atmosphere. Several magnifications (i.e. $\times 100$ –500 and 1000) were used to
155 observe the shape and surface topography of the particles.

156 A QICPIC instrument (Sympatec, UK) was utilized to characterise the particles in terms
157 of size and shape. In order to ensure that the dispersing line was clean and free from
158 contaminants, two spoonful of sand (40-100 mesh) were passed through it prior to analysis.
159 The primary sample container containing each excipient grade was thoroughly mixed by rolling
160 and inverted by hand as well as mixed using a spatula. Before starting the measurement, the
161 sample, approximately 2 g, was gently inverted and agitated to evenly disperse it and, thus,
162 reduce loss of material in the vials. The M7 lens was selected for this study, where each
163 measurement was repeated three times. The WINDOX software was utilized to perform the
164 statistical analysis of the obtained measurements. **The following particle size and shape**
165 **properties were determined and used as input parameters for the models:**

- 166 • **Particle size:** D_{10} , D_{50} , D_{90} , $D_{4,3}$
- 167 • **Aspect ratio:** S_{10} and S_{50}

168 **The particle size and shape properties of the binary blends were determined from**
169 **the single component size and shape properties using a volume-based mixing rule. The**
170 **physical property ($x_{\text{mix},i}$) is calculated from the single component properties $x_{i,j}$ of**
171 **material j and property i (more details about $x_{i,j}$ are provided in section 2.4.1):**

$$172 \quad x_{\text{mix},i} = \sum_{j=1}^N f_{\rho,j} x_{i,j} \quad (1)$$

173
174 **with $N = 2$ as the number of components/materials. $f_{\rho,i}$ is the volume based fraction**
175 **considering particle true density, ρ_i , and calculated by**

176
$$f_{q,i} = \frac{q_i}{\sum_{j=1}^N q_j} f_i. \quad (2)$$

177 with f_i as the weight based fraction of material i .

178 2.2.1. True Density Measurements

179 The true density of all the excipients, as detailed in section 2.1, was determined using a
180 Micromeritics Accupyc II pycnometer 100 (Micromeritics, USA). The test was carried
181 out using a multi-run system (10 runs) with a standard deviation of 0.005% for all the
182 excipients.

183

184 2.3. Flow Properties Measurements

185 A Ring shear tester (RST-XS, Dietmar Schulze, Wolfenbuttel, Germany) was utilized
186 to characterise the flow of the powders. **The investigated powders also included a list of 66**
187 **powder blends in the ratio of 3:1, 1:1 and 1:3 of MCC, DCP and Lactose grades as**
188 **detailed in section 2.1. In making the blends for FFC determinations, the appropriate**
189 **powders were weighted out in their desired ratios as %w/w and blended in a Turbula**
190 **mixer for 10 minutes to ensure homogeneity. These powders were then immediately**
191 **analysed.** The cell was over-filled with the sample **powder of interest** and then a spatula was
192 used to gently smoothen the surface. The weight of the shear cell and the sample was
193 determined and recorded using the software provided. A pre-shear stress of 4,000 Pa was
194 applied to erase the powder history. Normal loads applied were **25%, 38%, 51%, 65% and 25%**
195 of 4,000 Pa. In order to assess the powder flowability, the flow function coefficient (FFC) can
196 be used. Such a coefficient can be expressed as follows [12]:

197
$$FFC = \frac{\sigma_c}{\sigma_u} \quad (1)$$

198 where σ_c is the consolidation stress that compacts the beds and σ_u represents the unconfined
199 yield stress that makes the powder bed to flow. The powder flowability can be classified into:
200 (i) not flowable ($FCC < 1$); (ii) very cohesive powder ($1 \leq FCC < 2$); (iii) cohesive powder
201 ($2 \leq FCC < 4$); (iv) easy flowing powder when the FCC value is in the range of ($4 \leq FCC <$
202 10); and (v) free flowing powder when the ($FCC > 10$) [12, 22].

203 **The bulk density of the materials (RHOB in kg/m³) was automatically determined by the**
204 **ring shear tester (RST-XS, Dietmar Schulze, Wolfenbuttel, Germany). This parameter**
205 **gives an indication of how these materials may pack and was thus used as one of the**
206 **predicted output parameters for the model development.**

207

208 2.4. Radial Basis Function Network

209 2.4.1. Model Development

210 This section briefly introduces an RBF network that is used in this research to model
211 the powder flow properties. Readers are referred to various books and research papers for more
212 in-depth reading, in particular references [23-24]. The RBF network usually maps an ($N + 3$)-
213 dimensional input space (\mathbf{x}) to a one-dimensional output space (y_T). **The full input space is**
214 **defined as**

$$\begin{aligned} 215 \quad \mathbf{x}_{\text{full}} &= [x_1 \quad x_2 \quad x_3 \quad x_4 \quad x_5 \quad x_6] \\ 216 \quad &= [D_{10} \quad D_{50} \quad D_{90} \quad D_{4,3} \quad S_{10} \quad S_{50}] \end{aligned} \quad (3)$$

217 The output parameter is either $y_T = FCC$ or $y_T = RHOB$.

218 Such a network typically consists of an input layer, basis functions acting as a hidden
219 layer and an output layer [17, 23]. Basis functions ($\phi_i(\mathbf{X})$) are functions of the radial

220 Euclidian distance from a defined centre. A Gaussian function is a common selection for the
221 basis function, which can be written as follows [23]:

$$222 \quad \phi_i(\mathbf{x}) = \exp\left(-\frac{(\mathbf{x} - \boldsymbol{\mu}_i)^2}{2\boldsymbol{\sigma}_i^2}\right) \quad (4)$$

223 where $\boldsymbol{\mu}_i$ and $\boldsymbol{\sigma}_i$ are the centre and the standard deviation of the i th function, respectively.

224 The output of the mapping can then be expressed as a linear combination of these basis
225 functions [23]:

$$226 \quad y(\mathbf{x}) = \sum_{i=1}^I w_i \phi_i(\mathbf{x}) + w_0 \quad (5)$$

227 where w_0 and w_i are the bias and the coefficient connecting the i th basis function to the output
228 layer, respectively. The general structure of the RBF network is presented in Figure 1. The
229 numbers of neurons in the input and output layers are determined by the process under
230 investigation (i.e. the numbers of the inputs and outputs). In order to minimize the error of
231 predicting each output, multi-input single output (MISO) model is commonly utilized. The
232 optimal number of the basis functions is the one that achieves a trade-off between good training
233 and good generalization capabilities. Thus, it corresponds to the minimum error usually
234 measured via the root mean square error (RMSE).

235 The RBF parameters (e.g. connecting coefficients and bias) are usually optimized via
236 the use of the back-propagation network. In general, back-propagation is a supervised learning
237 algorithm that aims to minimize the mean squared error between the target output and the
238 predicted output [17, 23, 25]. Such an algorithm typically involves two phases, namely,
239 forward and backward phases. The forward phase calculates the network predicted output

240 according to the inputs, whereas the backward phase adapts the network parameters (e.g. the
241 connecting coefficients) based on the error performance via the use of an elicited optimization
242 algorithm. Various optimization algorithms including, but not limited to, gradient descent,
243 quasi-Newton optimisation, conjugate gradient, Levenberg-Marquardt and nature inspired
244 optimization algorithms (e.g. Genetic algorithm), have been presented in the related literature
245 [20, 25]. In this research paper, the scaled conjugate gradient (SCG) algorithm is utilized to
246 optimize the RBF network parameters.

247 2.5. Integrated Network

248 2.5.1. Model Development

249 The integrated network, as a data based model, relies on predicting the output via two
250 phases. The structure of such a network for MISO is depicted in Figure 2. In the first phase,
251 the N -dimensional input space (\mathbf{x}) and the one-dimensional target space (y_T) are utilized to
252 develop and train M models having different structures (e.g. number of basis functions). Then,
253 the predicted outputs (**i.e. the predicted flow properties from each model**) from these models
254 ($y_{P1}, y_{P2} \dots y_{PM}$) and the target output are used, in the second phase, to develop and train a single
255 model leading to the final predicted output (\hat{y}_p) [26]. The idea of this integrated network is
256 that the different model structures in the first phase can play a complementary role in
257 representing the **underlying patterns between the input parameters investigated and the**
258 **flowability parameters (i.e. FCC and RHOB)**. Furthermore, training the **model** in two phases
259 helps in extracting the associated knowledge from the available limited data [26].

260 The predicted output of the integrated network can analytically be expressed as a
261 combination of composition and superposition of the basis functions as follows [26]:

$$\hat{y}_P = \sum_{m=1}^M w_m^{(2)} \phi_m \left(\sum_{k=1}^K w_k \phi_k(x) + w_0 \right) + w_0^{(2)} \quad (6)$$

263

264 **where K is the number of the basis functions in each model in the first phase and M**
 265 **represents the number of the RBF models defined in the first phase.** The rest of the
 266 parameters are as defined in Section 2.4, where the superscript number in Eq. 6 is utilized to
 267 distinguish the parameters used in Phase II from the ones used in Phase I. It has been proved
 268 that the superposition and composition functions are dense in a convex data space [27-28].
 269 Thus, the function presented in Eq. 6 can minimize the difference between the predicted and
 270 the target outputs and can significantly improve the predictive performance [26]. The SCG
 271 algorithm is utilized with the backpropagation network to optimize the network parameters for
 272 the two phases.

273 3. Results and Discussions

274 3.1 Micrometric and flow properties

275 The micrometric properties of the three powder materials used in this research study
 276 are summarized in Table 1. **The powders in this table are also the powders used in making**
 277 **the blends for FFC and RHOB determination.** The electron micrographs obtained by SEM
 278 for the different grades of MCC, DCP and Lactose are depicted in Figures 3, 4 and 5,
 279 respectively. As shown in Figure 3, the MCC microsphere 100 has, as expected, spherical
 280 particles with diameter values are in the range of approximately 150 μm to 300 μm . It is worth
 281 mentioning that a similar morphology can also be observed for the MCC microsphere 200,
 282 however, the particle diameter values are in the range of approximately 200 - 300 μm . These
 283 results were further confirmed by the QICPIC analysis. It was also observed that the MCC
 284 PH101 and MCC PH102 have elongated plate-like particles, with size in the range (40 –

285 350 μm). It is worth emphasising at this stage that the former has a smaller particle size when
286 compared to the latter. A similar particle shape can also be observed for the MCC PH105 and
287 MCC PH302. However, differences in the particle size are shown in Figure 3. For instance,
288 particle size of the MCC PH105 is smaller than that of the MCC PH102 and larger than that of
289 the MCC PH101, whereas the size of the MCC PH302 is larger than these grades. The silicified
290 grades of MCC have also elongated plate-like particles. A look at Figure 1 and Table 1 suggests
291 that the sphericity descriptors decrease in order: MCC PH200 > MCC PH100 > MCC PH302 >
292 MCC prosolv 90 > MCC PH105 > MCC PH101 > MCC prosolv 50 > MCC PH102.

293 Different particle morphologies can also be noticed for the DCP grades, as presented in
294 Figure 4. For example, the D160 and A150 grades show an aggregated plate-like morphology
295 with relatively large particle size (i.e. $D_{4,3}$ is approximately 160.3 μm). A similar morphology
296 is noticeable for the D14 and A12 but the particle size is less than 100 μm . In contrast to these
297 grades, the A60 grade has the most spherical particle shape with uniform size distribution ($D_{4,3}$
298 is approximately 76.12 μm). The sphericity descriptors for these grades are listed in Table 1.
299 In Figure 5, it can be seen that Lactose shows versatile morphologies ranging from cubical to
300 complete spherical particles. For instance, Flowlac 90 and Flowlac 100 have completely
301 spherical particles with quite similar particle size distributions, as presented in Table 1.
302 Granulac 70 and Granulac 200 show cubical morphology with different particle size (i.e.
303 Granulac 70 has a larger particle size ($D_{4,3}=173.27 \mu\text{m}$) when compared to Granulac 200
304 ($D_{4,3}=58.90 \mu\text{m}$).

305 The FFC values of the various grades (**MCC, DCP and Lactose**) of the powder
306 materials investigated are shown in Figure 6a-c. It is apparent that D160 has the best
307 flowability, with an FFC value of approximately 65. Among the MCC and Lactose grades,
308 MCC PH200 and Flowlac 100 have the best flowability with FFC values equal to

309 approximately 33 and 20, respectively. Statistical correlation analysis across the powders
310 investigated was carried out between the size and shape descriptors of the powders investigated
311 and the flowability represented by the FFC and RHOB. Reasonable linear correlation
312 coefficient values among most of them are listed Table 2. Different correlation values can also
313 be observed in Table 2. For instance the relationship between the D_{50} and the FFC is stronger
314 than the relationship between D_{50} and the RHOB. In addition, the relationship between the D_{90}
315 and the FFC is a strong direct relationship (i.e. the correlation coefficient is positive), whereas
316 the relationship between the D_{90} and the RHOB is a weak inverse one (i.e. the correlation
317 coefficient is negative). **The analysis of variance showed that the various materials have**
318 **significant effects on the flow properties, where the p-values were less than 0.05.**

319 **It was also interesting to note that of the true densities determined, the DCP**
320 **samples had the highest values ranging from 2.38 – 2.92 kg/m³ whereas the MCC and**
321 **Lactose grades had values ranging from 1.40 – 1.97 kg/m³ and 1.54 – 1.68 kg/m³**
322 **respectively (Table 1).**

323 **The blends for the MCC, DCP and Lactose grades displayed a range of FFC values**
324 **which were correlated to their particle size descriptors (i.e. $D_{4,3}$ values) (Figure 7a-e). It**
325 **was noticeable that an increase or a decrease in one of the ratios of the blends (3:1, 1:1 or**
326 **1:3) had a significant influence on the FFC values. This was correlated directly to the**
327 **calculated particle size descriptors of the blend under investigation. This indicated that**
328 **the development of the linear volume-based mixing rule (Eq. 1) for the blend in**
329 **determining their particle size descriptors is possible and can be used to determine the**
330 **particle size descriptor of any potential ratios which can be fed into a model and the FFC**
331 **thus predicted.**

332 3.2. Radial Basis Function Network

333 An RBF model was employed to model and predict the flowability of the various
334 pharmaceutical powders investigated. The experimental data were randomly classified into two
335 sets: training set (**60**), which allows the RBF model to learn the input/output relationships, and
336 testing set (**26**), by which the generalization capabilities of the developed RBF model are tested.
337 In addition to the various powders **and the different powder blends** used, particle size
338 represented by its descriptors (i.e. D_{10} , D_{50} , D_{90} and $D_{4.3}$) and particle shape represented by its
339 sphericity descriptors (i.e. S_{10} and S_{50}) were considered as input variables, whereas the powder
340 flow represented by the FFC and RHOB was considered as an output. The number of basis
341 functions selected was the one that corresponded to the minimum RMSE values **for both**
342 **training and testing sets**. For the FFC, Figure 8 shows the RBF performance for both the
343 training and the testing data sets using 6 basis functions, with a RMSE (training, testing) =
344 **[2.90, 5.16]**. **The testing RMSE value is approximately twice the training RMSE value,**
345 **which, at first glance, could be attributed to an over-training problem. However, it was**
346 **noted that one of the FFC values in the testing set was larger than 60, whereas, in the**
347 **training set, most of the values are less than 30, thus, an error residual of 5 is actually less**
348 **than 10% of the target value.** The coefficient of determination (R_2) values for the training
349 and testing sets are **0.80** and **0.79**, respectively. **The close R_2 values are an evidence that the**
350 **over-training problem was not the case in this work.** In a similar manner, an RBF model
351 was developed for the RHOB. The performance measures presented by the R_2 (training, testing)
352 and RMSE (training, testing) values are **[0.78, 0.77]** and **[112, 151]**, respectively, as
353 summarized in **Table 3**. The results obtained indicate that the RBF network cannot represent
354 and accurately predict the flow properties. This can be attributed to **the limited number of**
355 **data points (i.e. powder samples) and to** the so-called “curse of dimensionality”, which refers
356 to the phenomenon that occurs when one deals with spaces of high dimensionality comprising
357 of many input variables.

358 The predictive performance of the RBF model can, thus, be improved by reducing the
359 dimensionality of the process (i.e. reducing the number of input variables). Therefore, an RBF
360 model was developed using **the materials and their mixtures**, D_{50} , $D_{4,3}$ and S_{50} . The model
361 performance values for the FFC and the RHOB are R_2 (training, testing) = **[0.84, 0.85]** and R_2
362 (training, testing) = **[0.82, 0.83]**, respectively. **The RMSE values for the FFC and the RHOB**
363 **are [2.12, 4.72] and [109, 142], respectively, as listed in Table 3.** These performance
364 measures indicate that the RBF model developed using less inputs is superior to that of the
365 RBF network developed using **all the** inputs, with an overall improvement of 7%. Although,
366 such a model satisfactorily modelled the flow of the investigated powders, reducing the number
367 of inputs may affect the generalization capabilities of the model. All the size descriptors should
368 be included in the model, in order to take into account a multimodal or wide size distribution.
369 Therefore, an integrated network is presented to capture the relationships between all the size
370 and shape descriptors and the flow properties.

371 3.3. Integrated Network

372 In order to implement the integrated network, ten RBF networks, with different number
373 of basis functions and different connecting coefficient values, and a single RBF one in the first
374 and second phases, respectively, were developed (**Table 3**). For each model in the first phase,
375 the data was randomly classified into two sets: training set (**60**) and testing set (**26**). **For each**
376 **flow property, the network parameters are listed in Table 3.** It is worth emphasising at this
377 stage that the number of data points (**i.e. powder samples**) in training and testing data sets
378 were the same for all RBF networks but their distributions in the space under investigation
379 were different. For this reason, these models can play a complementary role in representing the
380 possible patterns by considering the different areas in the space under investigation.

381 The integrated network performance **measures** for the FFC **were** R_2 (training, testing)
382 = **[0.92, 0.93]** and **RMSE (training, testing) = [1.41, 1.92]**, as shown in Figure 9, while the

383 performance **measures** for the RHOB were R_2 (training, testing) = [0.91, 0.90] and **RMSE**
384 **(training, testing) = [75, 93]**, as shown in Figure 10. The output predictions in Figures 8 and
385 9 elucidate a satisfactory performance, where it was noticeable that most of the predicted values
386 fitted properly within the 90% confidence interval. In addition, the prediction performance of
387 the integrated network was superior to that of the single RBF network presented, with overall
388 improvements of approximately **16%** and **19%** in R_2 for the FFC and RHOB, respectively.
389 These results prove the ability of the integrated network in handling the difficulties of
390 modelling the powders flowability **and in dealing with the limited number of data points,**
391 **this being due to the dense function represented by the superposition and composition**
392 **functions presented in Eq. 6.**

393 **4. Conclusions**

394 Modelling and predicting the flow properties of powder materials are essential in many
395 industries, in particular the pharmaceutical industry, this being due to the fact that powder flow
396 behaviour can affect the manufacturing efficiency and determine the final product quality. In
397 this research work, data-driven **models** were **developed** to predict the flow properties of
398 various commonly used pharmaceutical powders **and blends**. Firstly, a radial basis function
399 (RBF) network was utilized to map the size (i.e. D_{10} , D_{50} , D_{90} and $D_{4,3}$) and shape (i.e. S_{10} and
400 S_{50}) descriptors to the flow properties represented by the flow function coefficient (FFC) and
401 the bulk density (RHOB). **The simple RBF network, however, was not able to capture the**
402 **highly nonlinear input/output relationships and the high dimensionality of the flowability.** An
403 integrated network was thus implemented to model the flow properties. In such a structure, the
404 output was predicted by training and modelling the acquired data in two consecutive stages.
405 The integrated network was successfully able to (i) capture the relationships between the
406 **particle** size and shape and the flow properties, (ii) deal with the high dimensionality of the

407 space under investigation, and (iii) predict the flow properties accurately. Furthermore, the
408 integrated network thus outperformed the single RBF network in terms of the predictive
409 performance and the generalization capabilities. **Such a model has the ability to guide**
410 **formulators in selecting excipients and their concentrations that can improve the**
411 **flowability of a powder blend. Employing such a model can therefore reduce time and**
412 **material waste.** There is however a need to improve the interpretability of the input/output
413 relationships, **which can be achieved by** incorporating fuzzy logic systems in the modelling
414 structure.

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