

1 **Application of NARX neural network for predicting marine engine**
2 **performance parameters**

3 Y. Raptodimos* and I. Lazakis

4 *Department of Naval Architecture, Ocean and Marine Engineering, University of*
5 *Strathclyde, Glasgow, United Kingdom*

6

7 * Corresponding author details:

8 Yiannis Raptodimos

9 Department of Naval Architecture, Ocean and Marine Engineering, University of
10 Strathclyde

11 Henry Dyer Building, 100 Montrose Street, Glasgow G4 0LZ, Scotland UK

12 yiannis.raptodimos@strath.ac.uk

13

14 Other author details:

15 Iraklis Lazakis

16 Department of Naval Architecture, Ocean and Marine Engineering, University of
17 Strathclyde

18 Henry Dyer Building, 100 Montrose Street, Glasgow G4 0LZ, Scotland UK

19 iraklis.lazakis@strath.ac.uk

20

21 **Application of NARX neural network for predicting marine engine**
22 **performance parameters**

23

24 **Y. Raptodimos & I. Lazakis**

25 *Department of Naval Architecture, Ocean and Marine Engineering, University of*
26 *Strathclyde, Glasgow G4 0LZ, United Kingdom*

27

28 **Abstract**

29

30 Though the maritime industry is still predominantly reliant on a time-based,
31 prescriptive approach to maintenance, the increasing complexity of shipboard systems,
32 heightened expectation and competitive requirements as to ship availability and
33 efficiency and the influence of the data revolution on vessel operations, favour a
34 properly structured Condition Based Maintenance (CBM) regime. In this respect
35 Artificial Neural Networks (ANNs) can be applied for predictive maintenance
36 strategies that can assist decision makers in selecting appropriate maintenance actions
37 for critical ship machinery. This paper focuses on developing a Nonlinear
38 Autoregressive with Exogenous Input (NARX) ANN model for forecasting future
39 values of performance parameters of a marine main engine. Moreover, a detailed
40 sensitivity analysis is conducted to examine the performance and robustness of the
41 developed NARX model, based on the dataset applied for its training. Through the
42 NARX model, a predictive monitoring approach can be achieved for ship machinery
43 monitoring as high forecasting accuracy was achieved for the case study of a main
44 engine cylinder exhaust gas outlet temperature. The sensitivity analysis overall
45 demonstrated the good performance and generalisation of the NARX model as it
46 successfully considers different values of the time series data for conducting the one-
47 step-ahead output.

48

49 **Keywords:** ANN; NARX; time series analysis; ship condition monitoring; marine
50 engine;

51

52 **Nomenclature**

53

AI	Artificial Intelligence
ANN	Artificial Neural Network
APE	Absolute Percentage Error
BS	British Standards
CBM	Condition Based Maintenance
DWT	Deadweight Tonnage
INCASS	Inspection Capabilities for Enhanced Ship Safety
ISEMMS	Integrated Ship Energy & Maintenance Management System
MAPE	Mean Absolute Percentage Error
MCR	Maximum Continuous Rating
MINOAS	Marine Inspection Robotic Assistant System

MSE	Mean Square Error
MUNIN	Maritime Unmanned Navigation through Intelligence in Networks
NAR	Nonlinear Autoregressive
NARX	Nonlinear Autoregressive with Exogenous Input
RNN	Recurrent Neural Network
SOM	Self-Organising Map

54

55 **1. Introduction**

56

57 *1.1 Maintenance and CBM*

58

59 The marine industry is responsible for the transportation of the vast majority of the
60 merchandise worldwide, as over 80% of global trade by volume is carried on board
61 ships, emphasising the importance of maritime transport for trade and development
62 (UNCTAD 2017). In this context and considering the emerging trends currently
63 shaping the outlook for seaborne cargo flows in combination with technological
64 advancements, the safe, efficient and environmentally friendly operation of ships is
65 extremely important. In this respect, maintenance is an important contributor to reach
66 the intended life-time of technical capital assets and is defined as a combination of all
67 the technical and associated administrative activities required to keep equipment,
68 installations and other physical assets in the desired operating condition or to restore
69 them to this condition (BS, 1993). Furthermore, routine and periodic maintenance
70 accounts for approximately 20% of a ship's operational expenses (Stopford 2009).

71

72 The importance of maintenance is also demonstrated by the fact that it is the only
73 shipboard activity to have one whole element assigned to it in the ISM code (IMO
74 1993). Moreover, technological advances, overburdened crew and high cost of
75 ownership, have resulted in considerable interest in advanced maintenance techniques
76 (INCASS 2015a). Though the industry is still predominantly reliant on a time-based,
77 prescriptive approach to maintenance, the increasing complexity of shipboard systems,
78 heightened expectation and competitive requirements as to ship availability and
79 efficiency and the influence of the data revolution on vessel operations, favour a
80 properly structured Condition Based Maintenance (CBM) regime (Tinsley 2016).

81

82 Unlike breakdown and preventive maintenance, CBM focuses on not only fault
83 detection and diagnostics of components but also degradation monitoring and failure
84 prediction (Prajapati et al. 2012). The heart of CBM is condition monitoring which
85 aims in collecting data regarding equipment conditions and is applied through various
86 tools by recording and evaluating different measurable parameters. Data can include
87 vibration, acoustic, temperature, oil and lubricant and current signal measurements.
88 Sullivan et al. (2010) and Pascual (2015) describe such condition monitoring
89 technologies and techniques in depth.

90

91 It is only recently that new approaches investigating the enhancement of ship's
92 reliability, availability and profitability have been considered according to Lazakis and
93 Olcer (2015). The outcome of this study indicated that preventive maintenance is still
94 the preferred approach by ship operators, closely followed by predictive maintenance;
95 hence, avoiding the ship corrective maintenance framework and increasing overall
96 ship reliability and availability. Moreover, shifting from scheduled, rule-based
97 maintenance to a data-driven approach can lead to more accurate and timely
98 maintenance, resulting in lower costs, greater availability of ship systems and
99 increased safety. Consequently, the maritime industry is seeking for increased
100 reliability, maximum uptime and optimal operational efficiency, as well as ensuring
101 safe and sustainable environmental performance in harsh environments.

102

103 *1.2 Artificial Neural Networks*

104

105 Artificial Neural Networks (ANNs) can readily address modelling problems that are
106 analytically difficult and for which conventional approaches are not practical,
107 including complex physical processes having nonlinear, high-order and time-varying
108 dynamics. Therefore, they can be applied for predictive maintenance strategies that
109 can assist decision makers in selecting appropriate maintenance actions for critical ship
110 machinery. Moreover, Raza and Liyanage (2009) also stated that there has been an
111 increasing demand for testing and implementing intelligent techniques as a subsidiary
112 to existing condition monitoring programs and that artificial neural networks have
113 emerged as one of the most promising techniques in this regard.

114

115 According to Nasr et al. (2012) ANNs provide an effective analysing and diagnosing
116 tool to understand and simulate the nonlinear behaviour of complex systems. As more
117 data describing the system condition and its influencing parameters become available,
118 data-based methods are being increasingly applied in the field of fault detection (Tan
119 et al. 2012), fault diagnostics (Tamilselvan and Wang 2013) and for predicting the
120 residual useful life (Tian et al. 2010).

121

122 Opposed to the traditional model-based methods, ANNs are data-driven and self-
123 adaptive methods, meaning that there are few a priori assumptions about the models
124 under study. They learn from past examples and capture subtle functional relationships
125 among the data even if the underlying relationships are hard to describe or unknown.
126 Secondly, ANNs have good generalisation capabilities. After being trained on the data
127 presented to them, ANNs have the ability to correctly simulate data they have not seen
128 before. Thirdly, ANNs are universal functional approximators and have more general
129 and flexible functional forms than the traditional analytical and statistical methods.

130

131 Adjallah et al. (2007) applied ANN for classifying bearing faults based on condition
132 monitoring of bearing acceleration signals in order to ease the burden of decision
133 making on system and equipment integrity. In addition, Zhu (2009) utilised ANN to
134 diagnose faults of a marine diesel engine related to variations in valve clearance and

135 engine cylinder loads. Their research indicated that ANN has a high degree of accuracy
136 when predicting ship main engine faults and can improve the reliability of the engine
137 overall. Furthermore, Zhou and Xu (2010) applied neural networks for the fault
138 diagnosis of a marine engine cooling system by using failure modes as input to the
139 network and failure causes as output based on simulated data.

140

141 Basurko and Uriondo (2015) applied ANNs for CBM of medium speed diesel engines
142 in operation for the case study of a fishing vessel. The developed ANN analyses actual
143 monitored data to determine engine faulty conditions. Moreover, Noor et al. (2016)
144 applied ANN modelling on a marine diesel engine in order to predict its performance
145 in terms of output torque, brake power, brake specific fuel consumption and exhaust
146 gas temperature using as input data various engine speeds and loads. Results showed
147 that the prediction error of the ANN model was lower than the mathematical model.
148 Raptodimos and Lazakis (2018) presented the application of the Self-Organising Map
149 (SOM) neural network for data clustering applications and monitoring of a marine
150 diesel engine, utilising the unsupervised nature of the SOM algorithm. Moreover,
151 Cipollini et al. (2018) investigated data-driven models for performing CBM on a ship
152 propulsion system. The results confirmed the possibility to implement regression
153 techniques for CBM and that amongst the machine learning models tested, ANN
154 models generally showed the best performance.

155

156 Although ANNs have recently gained importance in time series applications
157 (Aizenberg et al. 2016, Laboissiere et al. 2015, Liu et al. 2015, Szoplik 2015), there is
158 a gap in the literature regarding such ANN applications in the marine industry which
159 could assist in reporting future health status of systems and components and provide
160 users with the earliest warning of potential faults. Aizenberg et al. (2016) performed
161 time series analysis using multilayer neural network for forecasting oil production in
162 the Gulf of Mexico. They concluded that the choice of embedding dimensions from
163 time series data is a challenging and ongoing task requiring additional research effort.

164

165 Bearing the above in mind, this paper focuses on developing a Nonlinear
166 Autoregressive with Exogenous Input (NARX) ANN model for forecasting future
167 performance parameter values of a marine main engine that can be utilised for
168 predictive maintenance strategies. Moreover, a detailed sensitivity analysis is
169 conducted to examine the performance and robustness of the developed NARX model,
170 based on specific marine main engine components. A NAR model is also presented
171 for comparison purposes. Through the NARX model, a predictive monitoring
172 approach can be achieved for ship machinery monitoring, that assists in preventing
173 failures and issues advanced warnings of potential faults leading to appropriate
174 maintenance actions and suggestions.

175

176 The present research paper is organised as follows: Section 2 presents the suggested
177 methodology while Section 3 presents the case study application through which the

178 methodology is applied and associated results. Finally, the discussion and conclusion
 179 of this research study is presented in Section 4 and 5 respectively.

180

181 2 Materials and methods

182

183 2.1 NARX methodology

184

185 A time series is a sequential set of data points, measured typically over successive
 186 points in time spaced at uniform time intervals. It is mathematically defined as a set of
 187 vectors $y(t)$, $t = 0, 1, 2, \dots, d$ where t represents the time elapsed with a set of discrete
 188 values y_1, y_2, y_3, \dots , etc. The variable $y(t)$ is treated as a random variable and the
 189 measurements taken during an event in a time series are arranged in a proper
 190 chronological order. In the NARX model, future values of a time series $y(t)$ are
 191 predicted from past values of $y(t)$ and another external series $x(t)$. Therefore, compared
 192 to the Nonlinear Autoregressive (NAR) model, NARX can consider external
 193 (exogenous) input for predicting the time series $y(t)$ and detecting changes in model
 194 parameters due to external conditions as seen in equation 1.

195

$$y(t) = f(x(t-1), \dots, x(t-d), y(t-1), \dots, y(t-d)) \quad (1)$$

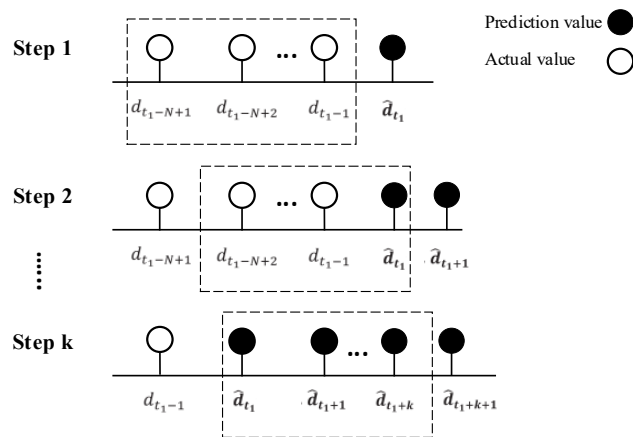
196

197 where $x(t)$ is the observation of the exogenous input at time t

198

199 Although the NARX network is applied for short-term forecasting, multi-step-ahead
 200 predictions can be acquired if knowledge of the future exogenous inputs is known.
 201 This is done by using the output of a one-step ahead prediction as the input for the
 202 subsequent prediction in an iterative process as described below and presented in
 203 Figure 1.

204



205

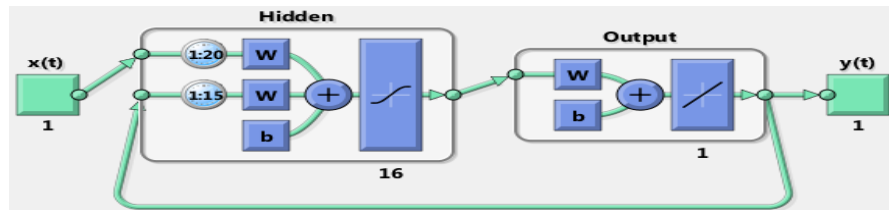
206 Figure 1: Procedure for multi-step-ahead NARX predictions

207

208 Data are normalised for direct use in network training by transforming them to the
 209 network's operating range, shaped to meet the requirements of the network input layer
 210 and are adapted to the nonlinearities of the neurons, so that their outputs should not

211 cross the saturation limits (Maier and Dandy 2000). The data is pre-processed in the
 212 ANN models by mapping data to a matrix row with minimum and maximum values
 213 from -1 to 1 for conducting proper analysis and improving efficiency of the network
 214 training. Additionally, the time series data is prepared by shifting time by the minimum
 215 amount to fill input states and layer states for network open loop and closed loop
 216 feedback modes. This allows the original time series data to remain unchanged, easily
 217 customising it for networks with different numbers of delays. Tapped delay lines are
 218 used to store previous values of the $x(t)$ and $y(t)$ sequences. Figure 2 presents the
 219 NARX model utilised in this paper.

220



221

222

Figure 2: Representation of NARX model

223

224 The NARX model is initially designed as feedforward backpropagation networks.
 225 During training, the network weights and biases are updated after all the inputs and
 226 target values have been presented to the network. The networks are autoregressive as
 227 the only inputs are lagged target values and lagged external input values in the case of
 228 the NARX model. The Bayesian regularisation backpropagation algorithm is primary
 229 used for training the NARX network. This algorithm updates the weight and bias
 230 values according to Levenberg-Marquardt optimisation. It minimises a combination of
 231 squared errors and weights and then determines the correct combination to produce a
 232 network which generalises well and avoids overtraining.

233

234 The performance of the network is evaluated using the *Mean Square Error (MSE)*
 235 average sum of square errors and *Correlation Coefficient (R)*. The ANN is then trained
 236 based on the above parameters in open loop, as a feedforward network. The trained
 237 ANN can then be converted to closed loop mode and the data is reformatted to simulate
 238 the network's closed loop response in order to carry out multi-step-ahead predictions.
 239 The output $y(t)$ is fed back to the input of the network. The trained ANN is converted
 240 to closed loop by replacing the feedback input and creating a feedback connection from
 241 the network output to the network input, thus making the network a Recurrent Neural
 242 Network (RNN) as presented in Figure 2.

243

244 The network architecture and training parameters are selected to minimise prediction
 245 errors. Furthermore, the forecasting results obtained are evaluated through defined
 246 performance measures (Aladag 2017); the Absolute Percentage Error (APE) and Mean
 247 Absolute Percentage Error (MAPE). The accuracy of each forecast is expressed as the
 248 APE which is calculated as:

249

$$APE = \left| \frac{y(t) - \hat{y}(t)}{y(t)} \right| \times 100\% \quad (2)$$

250

251 MAPE represents the percentage of average absolute error of forecasted values from
 252 original ones, showing the magnitude of overall error occurring due to forecasting and
 253 it is calculated as follows:

254

$$MAPE = \frac{1}{N} \sum_{i=1}^N APE \quad (3)$$

255

256 where $y(t)$ is the actual observation, $\hat{y}(t)$ is the forecasted observation for the same
 257 time interval t and N in the number of data points.

258

259 2.2 Measurement uncertainty-calculation of prediction intervals

260

261 Sensor measurements are often distorted by noise and bias, thereby masking the true
 262 condition of the system which can lead to incorrect estimation results (Bocaniala et al.
 263 2006). The prediction intervals are defined as:

264

$$\text{Prediction Intervals} = \widehat{y}_{pred} \pm t_{1-\frac{a}{2}, n-2} \times SE_{\widehat{y}_{pred}} \quad (4)$$

265

266 where \widehat{y}_{pred} is the predicted point, t is the value of the two tailed “ t ” distribution for
 267 a probability equal to a , n is the number of samples in the data and $SE_{\widehat{y}_{pred}}$ is the
 268 standard error of the prediction (standard deviation of the sampled population). Given
 269 a dataset x , the standard error of the prediction is calculated through equation 5:

270

$$SE_{\widehat{y}_{pred}} = s \sqrt{1 + \frac{1}{n} + \frac{(x - \bar{x})^2}{S_x^2(n-1)}} \quad (5)$$

271

272 where s is the standard error, S_x is the standard deviation of x and \bar{x} is the sample
 273 average of x .

274

275 Therefore, a prediction interval forecast consists of an upper and lower limit between
 276 which a future value is expected to lie with a prescribed probability. Furthermore, it is
 277 important to mention that no generally accepted method of calculating prediction
 278 intervals exist (Chatfield 2000).

279

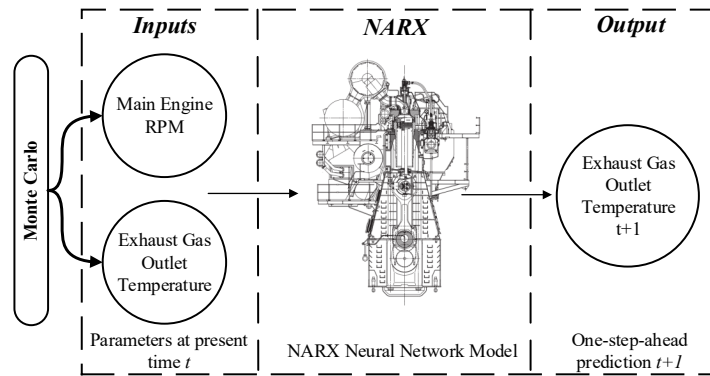
280 2.3 Sensitivity analysis methodology

281

282 Saltelli et al. (2008) defines sensitivity analysis as the field examining how uncertainty
 283 in model outputs can be apportioned, qualitatively or quantitatively, to different

284 sources of uncertainty in the model input. The Monte Carlo method is used as a
 285 comprehensive approach for accomplishing the sensitivity analysis (Wei et al. 2013).
 286 In the context of Monte Carlo simulation, this is described as the process of
 287 approximating the model output through repetitive random application of the model's
 288 algorithm. Monte Carlo sensitivity analysis is performed with Latin hypercube
 289 sampling which is a sampling scheme designed to ensure that the upper and lower ends
 290 of the data used in the sensitivity analysis are well included in the analysis (Firestone
 291 et al. 1997). Furthermore, this sampling method is generally recommended over simple
 292 random sampling and is one of the most widely used random sampling methods for
 293 Monte Carlo based analysis (Shields and Zhang 2016). Figure 3 provides a graphical
 294 outline of the sensitivity analysis regarding the inputs and output for the one-step-
 295 ahead prediction of the NARX model.

296



297

298 Figure 3: Graphical outline of NARX model inputs and output for sensitivity analysis

299

300 The sensitivity analysis is conducted by varying the inputs of the NARX model, the
 301 main engine rpm and/or cylinder exhaust gas outlet temperature at timestep t
 302 representing the present time, used for producing the subsequent one-step-ahead
 303 prediction $t+1$ output. Based on the above, both the main engine rpm and exhaust gas
 304 outlet temperature parameters are varied to examine the output of the NARX model.

305

306 3 Case study

307

308 3.1 Case study description

309

310 The methodology is applied on a two-stroke, eight-cylinder marine diesel engine of a
 311 Panamax container ship. The main particulars of the Panamax ship case study are
 312 demonstrated in Table 1 below.

313

314 Table 1: Case study main characteristics

Principal characteristics	
Year built	2009
Ship type	Cellular container
DWT (summer)	50829 tons

Length overall	260.00 <i>m</i>
Beam	32.00 <i>m</i>
Depth moulded	19.30 <i>m</i>
Draft (summer)	12.60 <i>m</i>
Engine particulars	
Main engine	HSD MAN B&W 8K90MC-C
Maximum Continuous Rating (MCR)	49680 <i>BHP @ 104 RPM</i>
Number of cylinders	8
Bore	900 <i>mm</i>
Stroke	2300 <i>mm</i>
Exhaust gas temperature sensor characteristics	
Sensor type	Type K (NiCr-Ni) Thermocouple
Measuring range	0-800 °C
Specified accuracy	± 1%
Measurement frequency	Hourly

315

316 The NARX model developed forecasts the upcoming 20 hourly values of the exhaust
317 gas outlet temperature of cylinder 5 of the main engine. A dataset consisting of 920
318 hourly measurements is utilised. Data was collected by utilising existing sensors
319 installed in the various systems and components of the main engine. The
320 measurements for the main engine performance parameter was recorded hourly (one
321 measurement per hour) as stated in Table 1 and saved on the vessel's onboard data
322 acquisition system. The specified sensor accuracy of ± 1% is assumed over the entire
323 sensor measurement range.

324

325 The data acquisition system is connected to the main engine sensors and other
326 machinery sensors in the engine room. Measurements from the various sensors are set
327 to be recorded on an hourly basis from the data acquisition system and are stored on a
328 platform developed by the shipping company. Overall, the data stored in the platform
329 is pre-processed by the data acquisition system in order to remove and rectify potential
330 faulty sensor readings. As such, the data used for the cylinder exhaust gas outlet
331 temperature has been pre-processed and further data pre-processing is considered out
332 of scope for this research. The stored data is accessible from the shipping company's
333 platform to crew and onshore personnel and data logs can be extracted in a Microsoft
334 Excel spreadsheet format for the various monitored machinery equipment with the
335 respective hourly timestamps.

336

337 The first 900 hourly measurements are used for training the NARX model while the
338 last 20 measurements are used to validate the model accuracy through the APE and
339 MAPE criteria. The exhaust gas outlet temperature parameter was selected for the case
340 study as the results of the NARX model developed for the cylinder exhaust gas outlet
341 temperature parameter varies significantly for different main engine rpm speeds

342 compared to the other main engine modelled parameters. Moreover, the exhaust gas
343 temperature is directly emitted from the engine cylinders and therefore will indicate
344 the operation and condition of the engine and its combustion process and is a valuable
345 source of diagnostic information regarding the technical condition of elements such as
346 the cylinder and piston, scavenging air, fuel supply system amongst other (Taylor
347 1996). The main engine rpm is utilised as the exogenous input in the NARX model.
348 For the main engine, the performance parameters largely depend on the main engine
349 rpm. Thus, the integration of knowledge or data related to the engine rpm speed is
350 applied as exogenous input in the NARX models. Table 2 presents the training
351 parameters applied for training the NARX model.

352
353
354
355
356
357
358
359

360 Table 2: NARX training parameters

Training conditions	Value	Description
net.trainParam.epochs	1000	Maximum number of epochs
net.trainParam.goal	0	Performance goal
net.trainParam.lr	0.01	Learning rate
net.trainParam.max_fail	6	Maximum validation failures
net.trainParam.min_grad	1E-05	Minimum performance gradient
net.trainParam.time	inf	Maximum time to train (seconds)
net.trainFcn	trainbr	Training algorithm
net.performFcn	mse	Performance function
net.divideFcn	divideblock	Dataset division
net.divideParam	70%-0%-30%	Training, validation, test set ratio

361
362
363
364
365
366
367
368
369
370
371
372

Training stops when any of the following conditions are met; The maximum number of epochs (iterations) for training is reached, performance is minimised to the goal, the maximum amount of time is exceeded, the validation performance has increased more than the maximum number of validation failures since the last time it decreased. In terms of the training algorithm, the Bayesian regularisation backpropagation algorithm was selected for network training that uses Jacobian derivatives as it updates the weight and bias values according to Levenberg-Marquardt optimisation. This algorithm minimises a combination of squared errors and weights in the network and then determines the correct combination to produce a network which generalises well (Okut 2016). Moreover, this training algorithm includes the validation data in the training set, hence the dataset is split 70% for training and 30% for testing in a time

373 sequence manner. This is done compared to splitting the dataset randomly in order to
374 preserve the correlation relationships of the time series data.

375

376 The number of delays is set experimentally. Experimental runs with different number
377 of network feedback delays were performed to obtain an accurate prediction model
378 that performs well. The developed NARX model consists of 16 neurons in the hidden
379 layer and uses a hyperbolic tangent function in the hidden layer and a linear transfer
380 function in the output layer. Moreover, 15 feedback delays of the target time series $y(t)$
381 and 20 input delays of the external input $x(t)$ which is the main engine rpm are applied
382 as presented in Figure 2. Once training is complete, the network is converted into
383 closed loop form and its own predictions $y(t)$ in the output layer become the feedback
384 inputs for carrying out one-step-ahead or multi-step-ahead predictions alongside the
385 external input $x(t)$ time series.

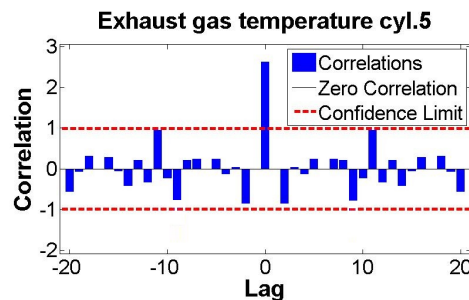
386

387 3.2 NARX results

388

389 The error autocorrelation function is used to validate the NARX network performance.
390 This function describes how the prediction errors are related in time. For a faultless
391 prediction network model, there should be only one non-zero value of the
392 autocorrelation function occurring at zero lag implying that the forecast errors are
393 entirely uncorrelated with each other. Figure 4 presents the error autocorrelation
394 function results for exhaust gas outlet temperature of main engine cylinder 5.

395



396

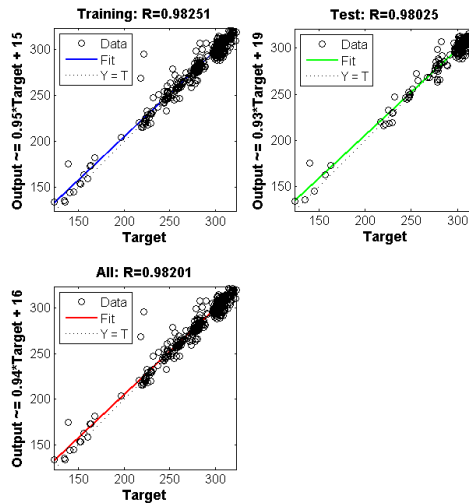
397

Figure 4: Error autocorrelation function

398

399 Satisfactory network training has been achieved as the forecast errors are completely
400 uncorrelated with each other and fall within the 95% confidence limits around zero
401 which are calculated based on the sample size of the time series data generated from
402 the MATLAB autocorrelation function. This implies that the prediction errors are
403 completely uncorrelated with each other. Figure 5 presents the correlation coefficient
404 R results for the training and test datasets.

405



406

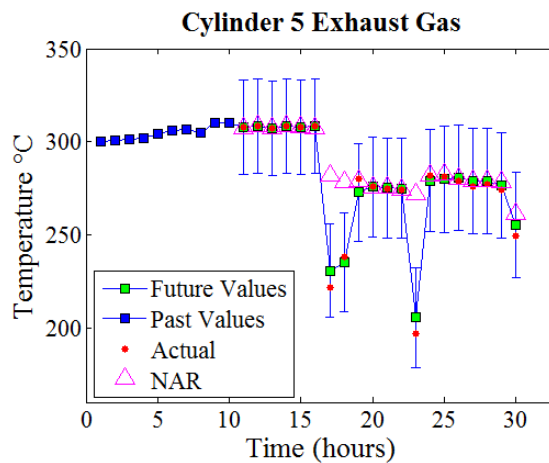
407

Figure 5: NARX training and test sets R results

408

409 Figure 6 presents the resulted forecasted results with their 95% prediction intervals
 410 for the exhaust gas outlet temperature.

411



412

413 Figure 6: NARX forecast results for exhaust gas outlet temperature of cylinder 5 and
 414 comparison with NAR results

415

416 The forecasted NARX results are plotted in green for timesteps 11-30 hours (20
 417 forecasted values) while the actual values are plotted as red dots on the graph.
 418 Moreover, the magenta triangles represent the associated results for the corresponding
 419 NAR model. Compared to the NARX model, the NAR model performs a univariate
 420 time series forecast by only considering the time series data of the exhaust gas
 421 parameter. This is presented in order to demonstrate the superiority of the NARX
 422 model against the NAR model. As observed by examining the graph, compared to the
 423 NAR model, the trained NARX model is capable of identifying the fluctuations in the
 424 modelled parameter through the addition of the main engine rpm as the exogenous
 425 input to the time series model and analysis. Specifically, in the 17th, 18th and 23rd hour

426 mark the exhaust gas temperature forecasted values fall close to the actual monitored
 427 values compared to the NAR results.

428

429 As observed, although the NAR model for the cylinder exhaust gas forecasts most
 430 values successfully, the results obtained have significant errors in timesteps 17, 18 and
 431 23 specifically, owing mostly in the alteration of the main engine's rpm. Specifically,
 432 from timestep 1-15 the engine speed is equal to 61-63 rpm while at timestep 16 it is
 433 reduced to 40 rpm and is then increased to 51 rpm, thus explaining the shift in the
 434 parameters and the reasonable hiatus of the NAR model to capture this change.
 435 Specifically, in the 17th hour interval, for the NAR model the APE value between the
 436 forecasted and actual exhaust gas outlet temperature value is equal to 27.26%, while
 437 the results for the NARX model indicate a major reduction in the APE of 23.12%
 438 magnitude, resulting in an APE value for the NARX model of 4.14%. Furthermore, in
 439 the 18th hourly mark the APE is reduced from 16.97% to 1.20% and at 23 hours it is
 440 reduced from 38.10% obtained in the NAR model to 4.52% by applying the NARX
 441 model. Moreover, the overall model MAPE value is reduced from 4.64% down to
 442 1.02%. The APE and MAPE results for the NAR and NARX models are presented in
 443 the Appendix.

444

445 3.3 Sensitivity analysis results

446

447 Both the main engine rpm and the exhaust gas temperature input values are altered
 448 progressively from their original value at present time t in order to examine the output
 449 of the NARX model regarding the one-step-ahead forecast result at time $t+1$. Table 3
 450 presents the different tests conducted for the various input values.

451

452 Table 3 Input parameter ranges from their baseline (rpm=61.9, exhaust gas=310.3
 453 °C)

Reference	% difference from baseline	Engine rpm values (rpm)	Exhaust gas values (°C)
<i>Test -1</i>	[0% -2%]	61.9-60.6	310.3-304.1
<i>Test -2</i>	[-2% -4%]	60.6-59.4	304.1-297.9
<i>Test -3</i>	[-4% -6%]	59.4-58.2	297.9-291.7
<i>Test -4</i>	[-6% -8%]	58.2-56.9	291.7-285.5
<i>Test -5</i>	[-8% -10%]	56.9-55.7	285.5-279.3
<i>Test -6</i>	[-10% -20%]	55.7-49.5	279.3-248.2
<i>Test -7</i>	[-20% -30%]	49.5-43.3	248.2-217.2
<i>Test +1</i>	[0% +2%]	61.9-63.1	310.3-316.5
<i>Test +2</i>	[+2% +4%]	63.1-64.4	316.5-322.7
<i>Test +3</i>	[+4% +6%]	64.4-65.6	322.7-328.9
<i>Test +4</i>	[+6% +8%]	65.6-66.8	328.9-335.1
<i>Test +5</i>	[+8% +10%]	66.8-68.0	335.1-341.3
<i>Test +6</i>	[+10% +20%]	68.0-74.3	341.3-372.4

Test +7 [+20% +30%] 74.3-80.5 372.4-403.4

454

455 Figure 7 presents the results for the described 14 test cases regarding the NARX t+1
456 Monte Carlo results. The results of the Monte Carlo analysis for each test case is
457 presented and the forecasting result for the exhaust gas temperature one-step-ahead
458 prediction (308°C) from Figure 6 is presented as the baseline reference for comparing
459 the sensitivity analysis outputs.

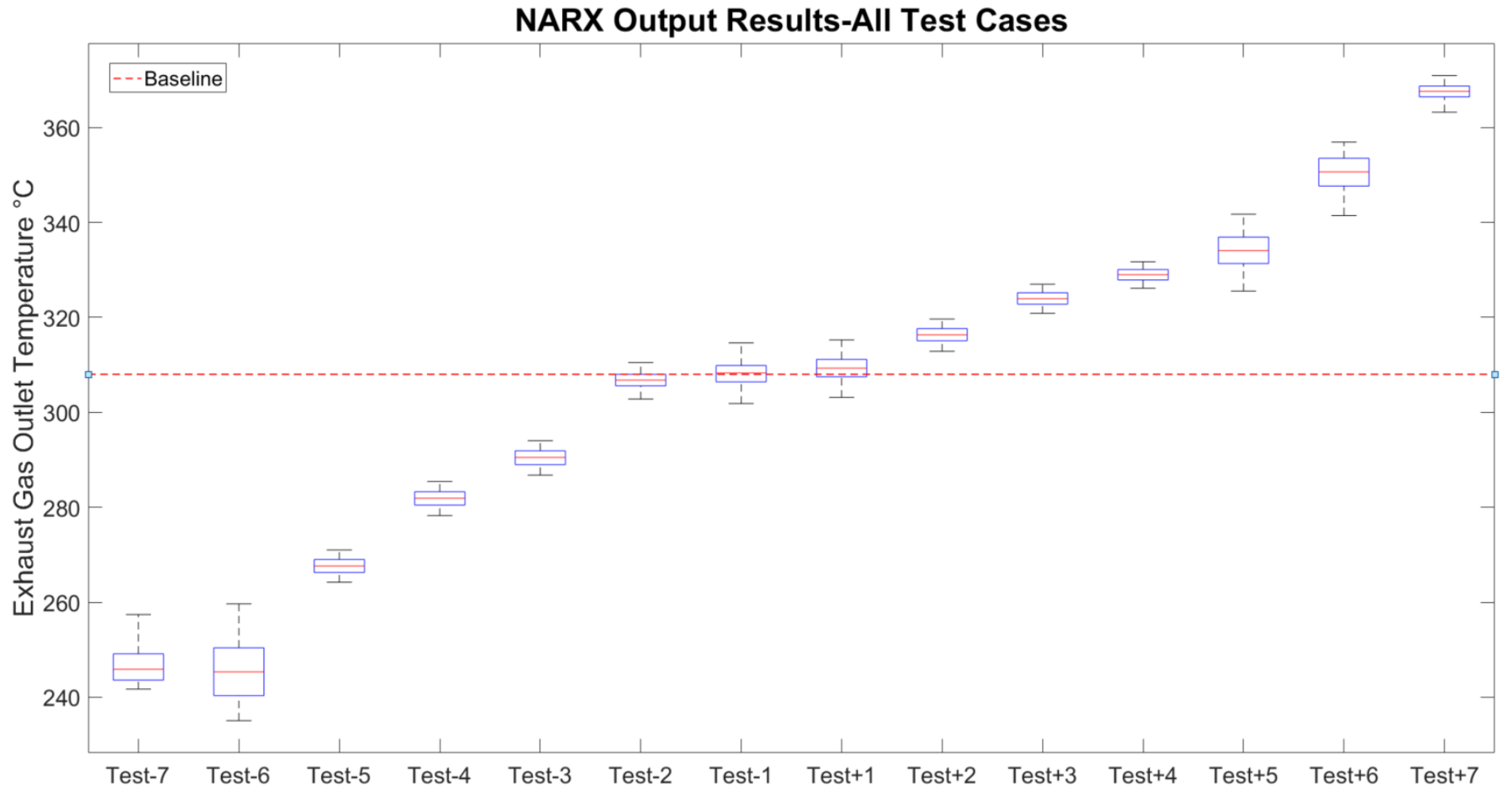


Figure 7: NARX sensitivity analysis results

439 As observed in Figure 7, for Test-2 to Test+2 the results indicate satisfactory network
 440 output for rational reductions and increments of the input parameters around the
 441 baseline value. Moreover, in the remaining test cases the error is increased from the
 442 baseline as both the exogenous NARX input and exhaust gas input time series data are
 443 reduced and increased respectively to protracted ranges. Concurrently, the response of
 444 the NARX model to these input parameters also demonstrates its generalisation
 445 capabilities and that overfitting manifestations have been evaded. Figure 8 presents the
 446 error results obtained from the baseline for the average forecasted results $t+1$ of Monte
 447 Carlo analysis for each test case.
 448

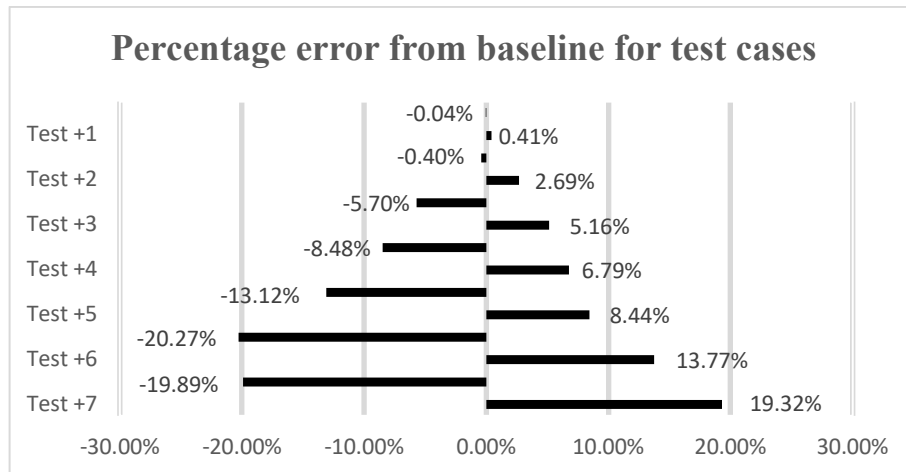


Figure 8: Error results from baseline for each test case

449
 450
 451

452 It can be observed that the errors are insignificant for the test cases Test-1, Test+1,
 453 Test-2 and Test+2 where reasonable changes in the input parameters were executed.
 454 Hence the model is considered robust and the differences in values in these test cases
 455 do not cause any significant effects in the outcome. On the other hand, for the
 456 remaining test cases the output of the variable and error from baseline increases as the
 457 input parameters take on acute values.

458
 459
 460

4 Discussion

461 The NARX model provided highly accurate forecast results by evaluating network
 462 training and performance, calculated prediction intervals and the APE and MAPE
 463 criteria against the actual recorded values. The results obtained for the error
 464 autocorrelation function demonstrate the uncorrelation of errors with each other, thus
 465 ensuring satisfactory network performance and confidence in the forecasting analysis.
 466 Overall, high network fits to the input data were achieved, specifically 98.25% for the
 467 training set and 98.02% for the test set. According to Shine et al. (2018), R values
 468 greater than 0.90 suggest the strength of agreement between actual and predicted values
 469 is excellent, values between 0.80 and 0.90 is considered substantial, while values
 470 between 0.65 and 0.80 are considered moderate and poor if lower than 0.65. The
 471 forecasted results are demonstrated in two segments of time including the actual data

472 and the forecasted future data. The NAR model was capable of forecasting with small
473 APE values most of the multi-step ahead predictions. Furthermore, it was unable to
474 detect the shift in parameter measurements due to the alteration in the main engine
475 rpm. In order to resolve this issue, the NARX model was developed by introducing the
476 main engine's rpm as exogenous input to the time series model and indicated that the
477 it can identify the fluctuations in the modelled parameters and thus reduced
478 significantly the APE and MAPE values compared to the results obtained from the
479 respective NAR models.

480

481 The Bayesian regularisation backpropagation algorithm was used for training the
482 NARX network. This algorithm can provide better solutions for smaller datasets
483 compared to the Levenberg-Marquardt training algorithm, which can also be applied
484 depending on the amount of data available for training (Kayri 2016). When the dataset
485 is small, Bayesian regularisation provides better generalisation performance than early
486 stopping. This is because it does not require that a validation dataset be separate from
487 the training dataset. However, the Bayesian regularisation method takes longer to
488 converge than early stopping (Demuth and Beale 2002).

489

490 Although the raw input data undergoes data cleansing and clustering process, it is
491 assumed that adequate data quality exists. It is assumed that no faults or alarms
492 occurred during the onboard measurement campaigns regarding the data collected for
493 analysis. This was confirmed after discussions with the shipping company which
494 provided the data. Moreover, data collection intervals are acquired in uniform time
495 step intervals (hourly), ensuring consistency in the predictions of the developed NARX
496 model.

497

498 The NARX model has been introduced for dynamic time series analysis and
499 forecasting, utilising performance parameter data for predicting the future system
500 state, thus enhancing the monitoring framework with predictive capabilities. Research
501 contribution has also been achieved by implementing and integrating sophisticated
502 methods and algorithms for the developed novel framework. This approach can also
503 be applied to other systems in the shipping industry and beyond, thus offering the
504 foundation and opportunity for academics to adapt this approach for applications in
505 other sectors and further validate and enhance the research. The AI tools can provide
506 ship operators with early warnings of upcoming faults to mitigate potential issues in
507 advance, which helps reduce unplanned downtime and increased availability by
508 enabling the crew onboard the ship and the onshore personnel to prepare accordingly
509 and proactively.

510

511 The sensitivity analysis was performed by utilising Monte Carlo analysis with the
512 Latin hypercube sampling method ensuring and demonstrating correct network
513 training and generalisation capabilities. The sensitivity analysis was carried out for
514 investigating the change in the NARX model output by shifting systematically both
515 the exhaust gas temperature outlet and main engine rpm parameter. Overall, the

516 sensitivity analysis demonstrated reliable performance of the NARX model output and
517 that it is tolerable to reasonable changes in the input parameters. Therefore, the output
518 is robust to reasonable changes in parameter values within the model. For the extreme
519 test case scenarios, the error from the baseline is increased as expected for the exhaust
520 gas outlet temperature.

521

522 The main aim of time series modelling is to carefully collect and rigorously study the
523 past observations of a time series to develop an appropriate model which describes the
524 inherent structure of the series. This model is then used to generate future values for
525 the series. The procedure of fitting a time series to a proper model is termed as time
526 series analysis, while time series forecasting can be termed as the act of predicting the
527 future by understanding the past (Hipel and McLeod 1994). An important task when
528 forecasting a value of y from one or more predictor variables is to obtain an estimate
529 of the likely amount of error inherent in the forecast (Chatfield 1995). A prediction
530 interval is an assessment of this forecast error and is a range that is probable to contain
531 the response value of a single new observation and allows assessment of future
532 uncertainty (Chatfield 1993). The NARX network provided highly accurate forecasted
533 results contained in their calculated prediction intervals. This outcome provides a high
534 level of confidence in the model predictions by addressing uncertainty in the
535 predictions.

536

537 The forecast accuracy of the NARX model depends on a variety of factors. These
538 include factors such as the amount of data available for training the NARX model as
539 the data will determine the NARX architecture and thus the forecasting and
540 generalisation capabilities. Moreover, the trendline of the historical data influence the
541 NARX forecasting output as it *“learns from the past to predict the future”*.

542

543 Paucity of literature in the topic of ANN time series forecasting for marine condition
544 monitoring presents difficulties in comparing the work in this paper with other
545 research. Moreover, various papers utilising data-driven methods use different datasets
546 as input, thus making any head-to-head comparisons subjective in nature as the size
547 and nature of the data will depict the architecture of the data-driven tool. For this
548 reason, this paper also included the NAR model in the case study results in order to
549 achieve a suitable comparison of the NAR and NARX model by using the same exact
550 dataset for training and simulation.

551

552 The most recent research projects between academia and industry MINOAS (Caccia
553 et al. 2010), INCASS (INCASS 2015b), MUNIN (Burmeister et al. 2014) and
554 ISEMMS (Gkerekos et al. 2017) indicate the current research trend and exploration of
555 advanced maintenance techniques. These techniques focus on machinery condition
556 monitoring applications onboard, through the utilisation of artificial intelligence,
557 reliability and data-driven methods to provide CBM functionalities and decision
558 support. Moreover, Zaman et al (2017) presented the challenges and opportunities of

559 big data analytics in the shipping sector and potential functionalities with regards to
560 ship safety, energy management and performance monitoring amongst other.

561

562 **5 Conclusions**

563

564 In the present paper, the application of a NARX neural network model for the cylinder
565 exhaust gas outlet temperature parameter of a marine main engine was presented. In
566 its wider context, the NARX model can predict various main engine performance
567 parameters. The capabilities and advantages of utilising the NARX neural network
568 have been demonstrated and the methodology is applicable for any performance
569 parameter of the main engine; provided data exists for these performance parameters.
570 The main concluding remarks are:

571

- 572 • The proposed methodology can be applied to other machinery systems such as
573 diesel generators, boilers, turbochargers etc. and can also be extended beyond
574 machinery systems, as it has the flexibility and capability factors to adapt
575 accordingly due to its data-driven nature.
- 576 • The AI model can provide a prediction model for CBM in shipping by
577 providing early warnings of upcoming faults to mitigate potential issues in
578 advance.
- 579 • High forecasting accuracy was achieved by employing the NAR and NARX
580 models. The case study demonstrated that up to 35% increased forecasting
581 accuracy can be achieved by introducing the main engine rpm as the exogenous
582 input in the NARX models compared to the accuracy of the NAR models. In
583 the NAR model, the APE value between the 23rd hour forecasted and actual
584 exhaust gas outlet temperature value is equal to 38.10%, while the results for
585 the NARX model indicate a major reduction in the APE of 33.58% magnitude,
586 resulting in an APE value for the NARX model of just 4.52%.
- 587 • The overall model MAPE value is reduced from 4.64% down to 1.02%.
- 588 • The sensitivity analysis overall addressed uncertainty in the predictions and
589 demonstrated the good performance and generalisation of the NARX model as
590 it successfully considers the different values of the exogenous input data for
591 conducting the one-step-ahead output for lower and higher main engine rpm
592 values and exhaust gas temperature values from the baseline.

593

594 Future research areas are identified that can extent the research scope. As more data
595 becomes available, the NAR and NARX models should be trained again to fully take
596 advantage of the new information so that the models can capture the developing trend
597 of the monitored system more accurately. When and how to implement such an update
598 should be further examined. Future research also includes investigating NARX
599 capabilities for forecasting various other main engine parameters. Moreover, a set of
600 parallel NARX models can be utilised to forecast multiple performance parameters,

601 and then fuse them in an ANN diagnostic classifier for the whole main engine system
602 in order to develop an overall CBM tool.

603

604 **Acknowledgments**

605

606 The work in this paper is partially funded by INCASS project. INCASS has received
607 research funding from the European Union's Seventh Framework Programme under
608 grant agreement No. 605200. This publication reflects only the authors' views and
609 European Union is not liable for any use that may be made of the information contained
610 herein.

611

612 **References**

613

- 614 Adjallah KH, Yang H, Mathew J, Ma L. 2007. Basis pursuit-based intelligent
615 diagnosis of bearing faults. *Journal of Quality in Maintenance Engineering*.13:152-
616 162.
- 617 Aizenberg I, Sheremetov L, Villa-Vargas L, Martinez-Muñoz J. 2016. Multilayer
618 Neural Network with Multi-Valued Neurons in time series forecasting of oil
619 production. *Neurocomputing*. 175:980-989.
- 620 Aladag CH. 2017. *Advances in Time Series Forecasting: Volume 2* Sharjah, United
621 Arab Emirates: Bentham Science Publishers.
- 622 Basurko OC, Uriondo Z. 2015. Condition-Based Maintenance for medium speed
623 diesel engines used in vessels in operation. *Applied Thermal Engineering*. 80:404-
624 412.
- 625 Bocaniala CD, Jain LC, Palade V. 2006. *Computational intelligence in fault*
626 *diagnosis* London, UK: Springer.
- 627 Burmeister H-C, Bruhn W, Rødseth ØJ, Porathe T. 2014. Autonomous Unmanned
628 Merchant Vessel and its Contribution towards the e-Navigation Implementation: The
629 MUNIN Perspective. *International Journal of e-Navigation and Maritime Economy*.
630 1:1-13.
- 631 Caccia M, Robino R, Bateman W, Eich M, Ortiz A, Drikos L, Todorova A, Gaviotis
632 I, Spadoni F, Apostolopoulou V. 2010. MINOAS a Marine INSpection rObotic
633 Assistant: system requirements and design. *IFAC Proceedings Volumes*. 43:479-484.
- 634 Chatfield C. 1993. Calculating Interval Forecasts. *Journal of Business & Economic*
635 *Statistics*.11:121-135.
- 636 Chatfield C. 1995. Model uncertainty, data mining and statistical inference. *Journal*
637 *of the Royal Statistical Society Series A (Statistics in Society)*.419-466.
- 638 Chatfield C. 2000. *Time-series forecasting* Florida, USA: Chapman & Hall/CRC
639 Press.
- 640 Cipollini F, Oneto L, Coraddu A, Murphy AJ, Anguita D. 2018. Condition-Based
641 Maintenance of Naval Propulsion Systems with supervised Data Analysis. *Ocean*
642 *Engineering*. 149:268-278.
- 643 Demuth H, Beale M. 2002. *Neural Network Toolbox-For use with MATLAB User's*
644 *Guide version 4* United States: The MathWorks Inc.
- 645 Firestone M, Fenner-Crisp P, Barry T, Bennett D, Chang S, Callahan M, Burke A,
646 Michaud J, Olsen M, Cirone P. 1997. *Guiding principles for Monte Carlo analysis*.
647 Washington, DC: US Environmental Protection Agency.

648 Gkerekos C, Lazakis I, Theotokatos G. 2017. Implementation of a self-learning
649 algorithm for main engine condition monitoring. *Maritime Transportation and*
650 *Harvesting of Sea Resources: Proceedings of the 17th International Maritime*
651 *Association of the Mediterranean (IMAM).*
652 Hipel KW, McLeod AI. 1994. *Time series modelling of water resources and*
653 *environmental systems* Amsterdam, The Netherlands: Elsevier.
654 IMO. 1993. *International Safety Management (ISM) Code, Resolution A741(18).*
655 London, UK.
656 INCASS. 2015a. Deliverable D5.4 'Data exchange'. UK.
657 INCASS. 2015b. Deliverable D8.1 Exploitation Plan. UK.
658 Kayri M. 2016. Predictive Abilities of Bayesian Regularization and Levenberg–
659 Marquardt Algorithms in Artificial Neural Networks: A Comparative Empirical
660 Study on Social Data. *Mathematical and Computational Applications.*21:20.
661 Laboissiere LA, Fernandes RAS, Lage GG. 2015. Maximum and minimum stock
662 price forecasting of Brazilian power distribution companies based on artificial neural
663 networks. *Applied Soft Computing.* 35:66-74.
664 Lazakis I, Ölçer A. 2015. Selection of the best maintenance approach in the maritime
665 industry under fuzzy multiple attributive group decision-making environment.
666 *Proceedings of the Institution of Mechanical Engineers, Part M: Journal of*
667 *Engineering for the Maritime Environment.*230:297-309.
668 Liu H, Tian H-q, Liang X-f, Li Y-f. 2015. Wind speed forecasting approach using
669 secondary decomposition algorithm and Elman neural networks. *Applied Energy.*
670 157:183-194.
671 Maier HR, Dandy GC. 2000. Neural networks for the prediction and forecasting of
672 water resources variables: a review of modelling issues and applications.
673 *Environmental Modelling & Software.* 15:101-124.
674 Nasr MS, Moustafa MAE, Seif HAE, El Kobrosy G. 2012. Application of Artificial
675 Neural Network (ANN) for the prediction of EL-AGAMY wastewater treatment
676 plant performance-EGYPT. *Alexandria Engineering Journal.* 51:37-43.
677 Noor M, MH MY, MM N. 2016. Prediction of Marine Diesel Engine Performance by
678 Using Artificial Neural Network Model. *Journal of Mechanical Engineering and*
679 *Sciences (JMES).*10:1917-1930.
680 Okut H. 2016. Bayesian Regularized Neural Networks for Small n Big p Data. In:
681 *Artificial Neural Networks-Models and Applications.* London, UK: InTech.
682 Pascual DG. 2015. *Artificial Intelligence Tools: Decision Support Systems in*
683 *Condition Monitoring and Diagnosis* USA: Crc Press.
684 Prajapati A, Bechtel J, Ganesan S. 2012. Condition based maintenance: a survey.
685 *Journal of Quality in Maintenance Engineering.*18:384-400.
686 Raptodimos Y, Lazakis I. 2018. Using artificial neural network-self-organising map
687 for data clustering of marine engine condition monitoring applications. *Ships and*
688 *Offshore Structures.* 13:649-656.
689 Raza J, Liyanage JP. 2009. Application of intelligent technique to identify hidden
690 abnormalities in a system: A case study from oil export pumps from an offshore oil
691 production facility. *Journal of Quality in Maintenance Engineering.*15:221-235.
692 Saltelli A, Ratto M, Andres T, Campolongo F, Cariboni J, Gatelli D, Saisana M,
693 Tarantola S. 2008. *Global sensitivity analysis: the primer* New Jersey, USA: John
694 Wiley & Sons.
695 Shields MD, Zhang J. 2016. The generalization of Latin hypercube sampling.
696 *Reliability Engineering & System Safety.* 148:96-108.

697 Shine P, Murphy MD, Upton J, Scully T. 2018. Machine-learning algorithms for
698 predicting on-farm direct water and electricity consumption on pasture based dairy
699 farms. *Computers and Electronics in Agriculture*. 150:74-87.
700 Stopford M. 2009. *Maritime economics 3e* New York, USA: Routledge.
701 Sullivan GP, Pugh R, Melendez AP, Hunt WD. 2010. *Operations & Maintenance*
702 *Best Practices-A guide to achieving operational efficiency*. UDo Energy, translator.
703 Third ed. Washington D.C, USA.
704 Szoplik J. 2015. Forecasting of natural gas consumption with artificial neural
705 networks. *Energy*. 85:208-220.
706 Tamilselvan P, Wang P. 2013. Failure diagnosis using deep belief learning based
707 health state classification. *Reliability Engineering & System Safety*. 115:124-135.
708 Tan WL, Nor NM, Abu Bakar MZ, Ahmad Z, Sata SA. 2012. Optimum parameters
709 for fault detection and diagnosis system of batch reaction using multiple neural
710 networks. *Journal of Loss Prevention in the Process Industries*. 25:138-141.
711 Taylor DA. 1996. *Introduction to marine engineering* USA: Elsevier Ltd.
712 Tian Z, Wong L, Safaei N. 2010. A neural network approach for remaining useful
713 life prediction utilizing both failure and suspension histories. *Mechanical Systems*
714 *and Signal Processing*. 24:1542-1555.
715 Tinsley D. 2016. Dawning of new era in asset maintenance. *Marine Power &*
716 *Propulsion Supplement 2016*.
717 UNCTAD. 2017. *Review of Maritime Transport 2017*. Geneva, Switzerland: U
718 Nations.
719 Wei P, Lu Z, Yuan X. 2013. Monte Carlo simulation for moment-independent
720 sensitivity analysis. *Reliability Engineering & System Safety*. 110:60-67.
721 Zaman I, Pazouki K, Norman R, Younessi S, Coleman S. 2017. Challenges and
722 Opportunities of Big Data Analytics for Upcoming Regulations and Future
723 Transformation of the Shipping Industry. *Procedia Engineering*. 194:537-544.
724 Zhou J, Xu L. The fault diagnosis of marine engine cooling system based on artificial
725 neural network (ANN). *Proceedings of the The 2nd International Conference on*
726 *Computer and Automation Engineering (ICCAE); 2010*.
727 Zhu J. Marine diesel engine condition monitoring by use of BP Neural Network.
728 *Proceedings of the Proceedings of the International MultiConference of Engineers*
729 *and Computer Scientists 2009*.

Appendix

NAR APE and MAPE results

Parameter	Results	t+1	t+2	t+3	t+4	t+5	t+6	t+7	t+8	t+9	t+10
Cylinder Exhaust Gas Temperature no.5	Actual	308.10	308.30	307.50	308.40	307.80	308.30	221.60	238.10	279.80	276.20
	ANN Prediction	308.00	308.30	307.13	308.35	307.86	308.42	230.78	235.25	272.75	275.84
	APE	0.03%	0.00%	0.12%	0.02%	0.02%	0.04%	4.14%	1.20%	2.52%	0.13%

Parameter	Results	t+11	t+12	t+13	t+14	t+15	t+16	t+17	t+18	t+19	t+20
Cylinder Exhaust Gas Temperature no.5	Actual	275.00	274.10	196.70	282.10	281.00	278.70	276.00	277.20	274.20	249.20
	ANN Prediction	275.20	274.90	205.60	279.05	280.02	280.67	279.06	279.04	276.65	255.32
	APE	0.07%	0.29%	4.52%	1.08%	0.35%	0.71%	1.11%	0.66%	0.89%	2.46%

MAPE=1.02%

NAR APE and MAPE results

Parameter	Results	t+1	t+2	t+3	t+4	t+5	t+6	t+7	t+8	t+9	t+10
Cylinder Exhaust Gas Temperature no.5	Actual	308.10	308.30	307.50	308.40	307.80	308.30	221.60	238.10	279.80	276.20
	ANN Prediction	307.50	308.30	307.50	308.40	307.80	307.30	282.00	278.50	279.00	275.10
	APE	0.19%	0.00%	0.00%	0.00%	0.00%	0.32%	27.26%	16.97%	0.29%	0.40%

Parameter	Results	t+11	t+12	t+13	t+14	t+15	t+16	t+17	t+18	t+19	t+20
Cylinder Exhaust Gas Temperature no.5	Actual	275.00	274.10	196.70	282.10	281.00	278.70	276.00	277.20	274.20	249.20
	ANN Prediction	275.20	273.90	271.65	282.00	282.30	280.13	279.13	279.04	278.41	261.32
	APE	0.07%	0.07%	38.10%	0.04%	0.46%	0.51%	1.13%	0.66%	1.54%	4.86%

MAPE=4.64%