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1 Introduction

Sketches, with their flexibility and suggestiveness, are in many ways ideal for expressing emerging design concepts. This can be seen from the fact that the process of representing early designs by free-hand drawings was used as far back as in the early 15th century [1]. On the other hand, CAD systems have become widely accepted as an essential design tool in recent years, not least because they provide a base on which design analysis can be carried out. Efficient transfer of sketches into a CAD representation, therefore, is a powerful addition to the designers’ armoury.

It has been pointed out by many that a pen-on-paper system is the best tool for sketching. One of the crucial requirements of a computer aided sketching system is its ability to recognise and interpret the elements of sketches. ‘Sketch recognition’, as it has come to be known, has been widely studied by people working in such fields: as artificial intelligence to human-computer interaction and robotic vision. There are three main issues in adopting sketch recognition for supporting conceptual design activities:

- Sketch capture: Conversion of a bitmap sketch to a computational model through a sketch recognition technique is an important task, currently most relevant to the detailed design stage, and is still a major research issue. During this process all the vagueness contained in the original sketch is removed.

- Interpretation of the sketch structure/content: It is not always easy to interpret the meaning of a sketch correctly, even for example such a basic attribution of 2D or 3D. The confusion between 2D and 3D often occurs from misunderstanding the structure of the sketch.

- Capturing the intended meaning: One sketch stroke can have different intended meanings such as a geometric shape or abstract idea. In the case of a geometric shape, a sketch can only be meaningful in the sense of 2D or 3D geometry. However, in the case of an abstract idea, it could be a symbol, character, functional relationship between entities, concept or idea, i.e., in this case a sketch may have a meaning beyond the simple geometry represented by the sketch strokes.

Despite the continuing efforts to solve the problem of appropriate conceptual design modelling, it is difficult to achieve completely accurate recognition of sketches because usually sketches implicate vague information, and the idiosyncratic expression and understanding differ from each designer.
2 Existing Approaches to Conceptual Design Support

Considerable work has been done to solve various problems encountered in trying to give computational support of design sketching activities (see Table 1). These efforts can be classified into three main areas: geometric modelling, spatial arrangement and design environment support as follows.

Table 1. Summary of various approaches [2] – see references for comments

<table>
<thead>
<tr>
<th>Area</th>
<th>Sub-Area</th>
<th>Functionality</th>
<th>Technology</th>
<th>Works</th>
</tr>
</thead>
<tbody>
<tr>
<td>Geometric Modelling</td>
<td>2-Dimensional Sketehing</td>
<td>• Automatic line tidy</td>
<td>• Pre-processing / processing</td>
<td>Easel, FFDS, Electronic Cocktail Napkin.</td>
</tr>
<tr>
<td></td>
<td></td>
<td>• Symbol recognition</td>
<td>• Fuzzification/fuzzy filter</td>
<td></td>
</tr>
<tr>
<td></td>
<td>3-Dimensional Sketehing</td>
<td>• Automatic surface creation</td>
<td>• Image processing</td>
<td>Akeo, Lipson, HoloSketch, SKETCH,</td>
</tr>
<tr>
<td></td>
<td></td>
<td>• 3D sketching environment</td>
<td>• Sketch interpreter</td>
<td>Viking, ISO-Sketcher.</td>
</tr>
<tr>
<td></td>
<td></td>
<td>• Geometric model structure analysis</td>
<td>• Direct-manipulation interaction</td>
<td></td>
</tr>
<tr>
<td></td>
<td>Sketch recognition</td>
<td>• Symbol/diagram recognition</td>
<td>• Sketch interpretation</td>
<td>LOOS, SPIDA, ABLOOS, THESYS, WRIGHT.</td>
</tr>
<tr>
<td></td>
<td></td>
<td>• Hidden line (re)construction</td>
<td>• Low level recogniser</td>
<td></td>
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<tr>
<td></td>
<td></td>
<td>• Image retrieval by diagram</td>
<td>• Soft constraint</td>
<td></td>
</tr>
<tr>
<td></td>
<td></td>
<td></td>
<td>• Perceptual analysis</td>
<td></td>
</tr>
<tr>
<td></td>
<td>Spatial (Re) arrangement and analysis</td>
<td>• Spatial layout analysis</td>
<td>• Goal object(GOB)</td>
<td></td>
</tr>
<tr>
<td></td>
<td>Vague spatial relationship modelling</td>
<td>• Location constraints</td>
<td>• Constrained heuristic search</td>
<td></td>
</tr>
<tr>
<td></td>
<td></td>
<td>• Uncertain region</td>
<td>• Similarity of spatial pattern</td>
<td></td>
</tr>
<tr>
<td></td>
<td></td>
<td></td>
<td>• Vague spatial relationship modelling</td>
<td>GEMCON.</td>
</tr>
<tr>
<td>Design Environment</td>
<td>GUI builder by sketching</td>
<td>• Interface programming without coding</td>
<td>• Storyboard mechanism</td>
<td>SILK.</td>
</tr>
<tr>
<td>Support</td>
<td>Past design retrieval by sketching</td>
<td>• Retrieval by partial design elements</td>
<td>• Case based reasoning</td>
<td>Archie-II, A.S.A.</td>
</tr>
<tr>
<td></td>
<td>Front-end system</td>
<td>• Retrieval by image</td>
<td>• Object-oriented programming</td>
<td></td>
</tr>
<tr>
<td></td>
<td></td>
<td>• Universal modelling interface</td>
<td>• Vague geometric modeller</td>
<td>ARCHPLAN, ISO-Sketcher.</td>
</tr>
</tbody>
</table>

2.1 Geometric Modelling

The work belonging to this category focuses on representing the shape of a design that has been determined during conceptual design. Many researchers in this area have concentrated on shape (re)construction of a rough 2D/3D sketch (be it on a 2D plane), involving a variety of sketch recognition techniques. Although some remarkable techniques have been developed, there are still limitations in applying them to conceptual design work. The basic problem is the requirement of any computational geometric model to be deterministic and precise. It leaves no room for being vague either intentionally or accidentally. When an early idea is ‘refined’, the original one is simply replaced by the precise geometric model. This can lead to premature loss of vague information and misrepresentation of a designer’s intent.
2.2 Spatial Arrangement

Spatial arrangement is concerned with the modelling and analysis of the spatial relationships of geometric models. Guan [3] points out that this approach usually deals with the problem of physical arrangement of objects and spaces to fulfill the needs of various human activities, based on a variety of explicitly or implicitly defined requirements and criteria that usually conflict with one another. This problem is common in many areas, including architectural and mechanical design. The essential issues addressed in this area of work are analysis and modelling based on spatial relationships between geometric models. Most systems attempt to model 2D spatial layout within their specific requirements using techniques such as numerical constraints. Despite the stated aim of supporting the conceptual design activities, most work in the area of spatial arrangement does not serve the purpose particularly well. Most systems feature automatic decision-making techniques in interpreting the geometric information and this alone is insufficient. They tend to concentrate on representing the spatial relationships between 2D rectangular shapes, apart from Kameyama et al. [4] that supports 3D spatial layout. On the other hand, a few systems support vague spatial relationships that can occur in rough geometric sketches. WRIGHT and GEMCON adopted some inequality types (including =, <, ≤, ≥, ≈, [, ]) and linguistic values (including above, below, front, behind, left, right). Thus it is possible to consider relations between design units that do not have fixed locations or fixed dimensions. However, both systems suffer from their inability to be more specific; for example, if A > B, by how much.

2.3 Design Environment Support

A number of systems have been developed to support the environment of geometric modelling serving diverse purposes. SILK allows designers to sketch quickly a user interface using an electronic stylus. It recognises 2D sketched shapes and turns these into an active user interface without re-implementation or programming. It also provides a “storyboard” mechanism to test subjects to evaluate the interface in its early, sketchy state. Some serve as a case browser, emphasising presentation of information to users over adaptation or application of past solutions. Yet others were developed to implement a front-end system. For example, ARCHPLAN explores the usefulness of object-oriented programming techniques to support the abstractions of the design process and the resulting design solution. ISO-Sketcher supports an autonomous pseudo-3D sketching environment, linked at run-time to an underlying geometric modeller, GEMCON. ISO-Sketcher is said to offer the early-stage geometry designer an environment supporting a minimum commitment approach, in which the designer is not compelled to make any commitments as to size, location or spatial relationships until desired. However, the system can only deal with the spatial arrangement of vague objects within a limited space and does not provide any effective means to model and manage vague geometric information.

3 Vague Geometric Modelling

The works examined above have made significant contributions in the integration of sketches, either computer-aided or otherwise, in the prevailing CAD environment. One major element, which has received but scant attention so far, is concerned with representing and managing the vague ideas and information contained in sketches. Some researchers have pointed out the importance of dealing with vagueness during conceptual design. For example, Martin [5] argues that a method is required to represent incompletely specified shapes, or indeed, classes
of shapes that agree with such an incomplete specification to a greater or lesser extent. Lipson et al. [6] points out the necessity of incorporating analysis tools in conceptual design. Lim et al. [7] proposed “the necessity and methods of the representation and maintenance of vague geometric ideas to support characteristics of conceptual design stage”.

In this paper, the word *vagueness* is defined as “the uncertainty about meaning” [8] which “can be represented by a probability distribution over possible meanings”. The uncertainty should be modelled in a form which allows the (re)utilisation of the information [8]. To allow a (re)utilisation of the uncertainty, a vague geometric model should include the entire possible range of vague types or values. Based on the definitions of vagueness, a Vague Geometric Model (VGM) can be defined as ‘a geometric model which implicates ill-defined abstractions, numerical values and/or spatial information’. Furthermore, Vague Geometric Modelling (VGMing) can be defined as ‘a modelling method that can represent and maintain the vague information contained in a VGM’.

Deliberate preservation and handling of vague information is a non-trivial task and represents a departure from current approaches used in sketch recognition. Preserving the vagueness will undoubtedly call for new techniques to represent and model the vague information, which, in our case, is mostly geometrical. It is also in accordance with the principle of minimum commitment, that is, in keeping as many options open for as long as possible. Consequently, a new approach is required for an effective VGMing technique that can represent vague information. To represent vague information of a shape, we suggest that the following functions should be satisfied.

- **Alternatives by multiple probabilities of each element**: A sketch stroke can represent multiple alternatives, such as a straight line, curve, or even geometric shape. Hence, the shape type of an object can be changed by a choice of alternatives within each child-element (in this paper, the term ‘child-element’ is used to explain the hierarchical subclass of a shape element which could be a rough sketch stroke). This means that the probability of a vague shape can be different depending upon which alternative child-element is chosen. Keeping all the possibilities like this is helpful for discovering hidden features in a representation without being fixated to a single perspective (see [9]). These unexpected discoveries could be more easily found in the original rough sketch when the original ideas are maintained without any refinement (see also [2, 5]).

- **Combination of probabilities of child-elements in a hierarchical structure**: Biederman [10] argued that a set of ‘geons’ (geometrical ions) can represent a wide range of shape variations. According to his proposal, single geons correspond to elementary shapes (e.g. cylinders, curved cylinders, and bricks) and all shapes can be represented by a combination of geons. As Kavakli [11] argues a significant proportion of drawn parts, whether from memory, imagination or by over-tracing, are produced part by part, which implies that most sketching activities are done by drawing parts of an object. Since an object is drawn by the combination of the parts, a hierarchical structure of these parts could be one way of representation that can be used for VGMing. This allows a clearer understanding of the nature of the vague element, and makes it easier to show a combination of vagueness that could be represented as probabilities (see Figure 1). With this structure, therefore, possible alternative interpretations of the element, object and the sketch as a whole can be made more visible [2].

- **Clustering of a vague shape by customised viewpoints**: Classification and clustering is necessary to represent a possible region of vague information. Everitt [12] pointed out that
the idea of sorting similar things into categories is clearly a primitive one since classification, in the widest sense, is needed for the development of language. Language consists of some words which help us recognise and communicate the different types of events, objects and people. In order to perform clustering, appropriate criteria are needed. Vague shapes may also be clustered differently depending on different viewpoints [13]. As some researchers [9, 13-15] argued, this kind of vagueness happens frequently when the designer and the user are different. In addition, the criteria could be more abstractly specified if the type of the object (i.e. design concept) is predefined.

<table>
<thead>
<tr>
<th>Element(n) : A sketch stroke</th>
</tr>
</thead>
<tbody>
<tr>
<td>Object : An Object which involves multiple elements</td>
</tr>
<tr>
<td>Object hierarchy</td>
</tr>
<tr>
<td>Classification hierarchy</td>
</tr>
</tbody>
</table>

- **Has-part** relations are employed to link concepts of the type from more general levels to more detailed levels with respect to the whole design.
- **Has-kind** relations are employed to link concepts of the type from higher abstraction levels to lower abstraction levels.

![Figure 1. Hierarchical structure of vague information [2]](image)

### 4 Prototype System

A prototype system, I-MAGI, is currently under development using Macintosh Common Lisp (MCL) 4.0 running under MacOS 8.6. The details of the prototype system process are as follows. Detailed methods are described in [2], thus, only a brief overview is presented here.

- **Input:** Sketching (draw new stroke) behaviour is similar to a natural sketching behaviour such as pencil-and-paper. Each stroke contains a series of original (x, y) points sampled along a path drawn by the designer. When drawing a stroke, the sample data points of the stroke are stored. If the drawing tool (e.g. mouse button or digital pencil) is released, the combination of line segments is considered as one stroke. During sketching, a designer can group strokes together to form compound strokes, which are then treated as a single element of the object.
• Pre-processor: Each new stroke entered is first sent to the pre-processor, which initially identifies the potential vertices and self-intersection points. These points are given probabilities of being vertices of a polygon according to their spatial relationships with the neighbouring points of the stroke. First, each connected four line segments, which are created by the five original points, are sequentially analysed (we use the term line-unit to denote these bunch of line segments, Figure 2). A line-unit is used to identify the probability of the third point of each line-unit. Basically, the pre-processor identifies all the potential vertices and intersection points apart from unintentional vertices because of a designer’s hand vibration (i.e. hand shaking). The pre-processor checks the type of one line-unit, and if the shape type of line-unit is ‘\(\backslash /\)’ or ‘\(\_\backslash /\)’, then it is not considered as potential vertices. Second, the pre-processor checks each pair of line segments in a stroke respectively to find the intersection points (see Figure 3). Figure 4 shows an example of possible vertices and self-intersection points with associated probabilities. The initial numbers of vertex (ver-num) and self-intersection (sel-num), \((x, y)\) coordinates, and probabilities are identified.

• Processor: The above vertex probability information is then sent stroke by stroke to the processor, which analyses the probabilities of each stroke representing the primitive elements which are pre-defined by the system (see the primitive elements of third hierarchical level in Figure 1).

• Post-processor: When the designer has defined one object containing a number of strokes, these processed strokes and the probabilities are sent to the post-processor which carries out the three tasks sequentially. Firstly, the size of the input object is now expanded as 3D co-ordinates if applicable. Second, the vague relative spatial relationship is analysed by the combination of distance and direction when there are more than two objects. Third, the \(VGM\), which is created through the process, is clustered by customised viewpoints.

• Output: Finally, the designer gets a \(VGM\) and various alternatives associated with vague information.

![Figure 2.](image-url)  
(a) Sequential capturing of the line-unit, and the third point of the line-unit. (b) The exception to identify the potential vertices
\( \nu \): Total number of points in the stroke (i.e., \( \nu = 6 \)).

\( L_{ij} \): Line segment between \( i \) and \( j \).

\begin{verbatim}
for i = 1 to \( \nu 
for j = (i + 1) \) to \( \nu 
    \text{Find-intersection} (L_{i(i+1)}, L_{j(j+1)})
end
end
\end{verbatim}

\( n \): Total number of points in the stroke (i.e., \( n = 6 \)).

\( L_{ij} \): Line segment between \( i \) and \( j \).

**Figure 3.** General algorithm to find intersection point

**Figure 4.** The probabilities of the vertices and intersection points from the sample stroke

## 5 Conclusion

Visualisation of conceptual models, in the form of sketches, is important for a more flexible and dynamic design. Sketches often play an important role in concept generation in design. Consequently, to capture, model and more fully utilise these concepts we need to integrate the sketching activities into the CAD environment. Much work to date on sketch recognition and computer-aided sketching systems support the need to provide computational based sketching. However, current approaches do not offer any method of representing and managing vague information often found in conceptual ideas as reflected in sketches.

In this paper, the existing approaches and representative works with sketching to conceptual design have been reviewed. A possible approach to vague geometric modelling based on a hierarchical structure and probabilistic method, and their associated issues have been discussed with the prototype system I-MAGI. The new approach will support minimum commitment by: a) modelling of vague shape itself; and b) maintaining the vagueness relating to the interpretation of shape rather than fixing upon a particular shape.

Currently, the prototype system is under development.
References


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