PERFORMANCE OF A GASKETED JOINT UNDER BOLT UP AND COMBINED PRESSURE, AXIAL AND THERMAL LOADING – FEA STUDY

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Abstract

In this paper the strength and sealing performance of a gasketed bolted flanged pipe joint is studied under bolt up and combined operating conditions using 3D nonlinear finite element analysis. The key combinations of internal pressure, axial and thermal loading are considered. The strength of the joint is seen to be affected by the axial and thermal loading combination whereas the joint sealing is seen to be dependent on the bolt up strategy during assembly and is slightly affected under pressure but only partially affected under axial loading in certain locations. Thermal loading was also considered and was found to have a significant effect on the sealing performance up to 100°C, but beyond that no sealing was observed, resulting in the possibility of leakage and hence increasing the risk of overall joint failure. Finally, the joint load capacities are determined under various combined loadings showing its safe and unsafe operational limits.

Keywords: Gasketed, combined, loading, bolt up, axial, thermal, sealing, strength, performance, finite element analysis

Notations

AL	Axial loading (kN)
AGSS	Average gasket stress (MPa)
DP	Design pressure (MPa)
IP	Internal pressure (MPa)
PT	Proof test pressure (MPa)
SI	Principal stress (MPa)
SINT	Stress intensity (MPa)
SY	Axial (longitudinal) stress (MPa)
UY	Axial displacement (mm)
Тетр	Temperature (°C)
HT	Hub top location
HB	Hub bottom location
HF	Hub flange fillet

1. INTRODUCTION

Conventional gasketed bolted flange joints are widely used for connecting pressure vessels and pipes in process and oil and gas industries. The performance of a gasketed flanged pipe joint is characterized by two key measures – joint strength and joint sealing. It is therefore important to evaluate its integrity and sealing performance in the actual operating condition when multiple loads are acting on the system. It is noted that the available designs rules for flange joints in international design codes are mainly concerned with their strength but do not sufficiently consider their sealing [1,2]. Abid *et al.* [3] has experimentally studied the performance of gasketed joints under bolt up and different operating conditions from a mechanical perspective i.e. combined internal pressure plus axial loading; combined internal pressure plus bending loading. However, application of thermal loading has not been considered to date, due to its complexity of application during experimental studies. In addition, Abid *et al.* and *Fukuoka et al.* [4-11] in their numerical studies have concluded that gasketed joints show better sealing performance if bolts in a joint are tightened as per ASME bolt tightening strategy [12] as compared to the various accepted industrial practices [13].

Researchers [14-20] have concluded that under additional axial loading in addition to the internal pressure, the performance of the joint is significantly affected. Abid *et al* [21-24] under combined internal pressure and variable temperature (static and transient) loading concluded that thermal loading becomes dominant for the failure of gasketed joint performance. In real world applications, bolted pipe joints are increasingly subjected to different structural and thermal loads in combination; even to the extent that they are subjected to thermal and pressure shocks for high end applications. In the available literature to date, no experimental or numerical studies have been observed under combined internal pressure, axial and thermal loading. From an experimental view, it is almost impossible to apply such boundary conditions to observe their behaviour in a large scale parametric study with different size ranges and classes. Therefore, keeping in mind the importance of combined axial and thermal loading, the bolted joint performance is studied under combined internal pressure (design and proof test), axial and thermal loading using detailed non-linear finite element methods. It is concluded that the methodology developed can provide a base for all sizes and classes under different combined operating conditions.

2. GEOMETRIC MODEL, FINITE ELEMENT MODELING AND MESHING

Figure 1 shows the key dimensions of the flange, bolts, and spiral wound gasket respectively taken from [21]. The size of gasket is taken according to the gasket suppliers as per flange size and class [28]. A complete 3D, 360 degree model of the flange joint has been developed and, due to the symmetry of the geometry and loading conditions, half the gasket thickness with flange and pipe of length 300mm for one side of joint is modelled [Figure 2a]. The commercial finite element programme, Ansys, is employed and SOLID45 structural elements and SOLID70 thermal elements are used to model flange, bolt, gasket and pipe [25]. Threedimensional (3D) 'surface-to-surface' CONTA174 contact elements, in combination with TARGE170 target elements are used between the flange face and gasket, the bolt shank and flange hole, the top of the flange and the bottom of the bolt, to simulate contact distribution for both the structural and thermal effects. 3D interface elements, INTER195, are used as a special gasket element for meshing of the gasket, which is compatible with SOLID45 structural elements and SOLID70 thermal elements. The gasket meshing requires two faces i.e. source and target faces and therefore the source face, which is the top area of the gasket, is meshed with SHELL 63 elements. A total of 32639 elements are used in the complete flange joint model comprising of flange, pipe, bolts and gasket.

3. MATERIAL PROPERTIES AND BOUNDARY CONDITIONS

The material properties for the flange, bolt and pipe are taken from [26] and are given in Table 1. Based on the complexity in a gasketed bolted flanged pipe joint, the geometrical (contact conditions), material and loading non linearity are considered. The performance of a gasketed pipe flange joint is largely influenced by the gasket stiffness in the thickness direction, therefore, a simplified material modelling method is used due to its relative accuracy and computational cost [27]. As such, the gasket nonlinearity is considered with the

elastic moduli during loading and unloading in each pass, directly calculated for input [Table 2]. As a benchmark problem, a flange joint size of 4 inch, 900# Class is selected in this study with dimensions as shown below.



Figure 1: Joint Dimensions: (a) Pipe Flange & Bolts (b) Spiral Wound Gasket (All Dimensions in mm)

Table	1:	Material	Propert	ies
			1	

Material	Temp	Thermal	Thermal	Specific	Poisson's	Young's	Yield
	(^{o}C)	Conductivity	Expansion	Heat	Ratio	Modulus	Strength
		<i>k</i> (W/m-k)	α (m/m-k)	Capacity	υ	Y (MPa)	σ_Y
				c (J/kg.k)			(MPa)
	20	47	12.5E-6	448	0.3	1.75E05	248
ASTM 350 L F2	100	47	13.5E-6	478	0.3	1.68E05	248
(Flange	200	46	14E-6	508	0.3	1.62E05	241
& Pipe)	300	45	14.4E-6	548	0.3	1.56E05	238
	400	43	14.8E-6	598	0.3	1.49E05	235
	20	37	14.1E-6	460	0.3	1.69E05	723
SA193	100	37	15.1E-6	490	0.3	1.64E05	723
B7	200	36	15.6E-6	520	0.3	1.57E05	717
(Bolts)	300	34	16E-6	560	0.3	1.50E05	713
	400	32	16.4E-6	610	0.3	1.42E05	710

	20	20	3E-6	461	0.3	1.64E05	206
ASTM	100	20	4E-6	491	0.3	1.59405	206
A182	200	19	4.5E-6	520	0.3	1.52E05	200
(Gasket)	300	17	5E-6	561	0.3	1.45E05	194
	400	15	5.5E-6	612	0.3	1.37E05	191

Applied	Bolt	Average	Elastic mod	lulus (MPa)
Torque (Nm)	preload (kN)	Gasket stress (MPa)	loading	unloading
210	37	30	319	3186
310	55	45	390	4407
400	70	60	450	5537
505	89	75	500	6598

Table 2: Elastic modulus calculated for each pass during loading and unloading

4. BOUNDARY AND CONTACT CONDITIONS

In order to 'make' a virtual joint assembly, the bolts are constrained in radial and tangential direction and are free to elongate in the axial direction. During bolt tightening, a displacement constraint (UY) is applied at the bottom of the bolts to achieve the target pre-stress. Contact is therefore initiated between the flange face and the bottom of the bolt. Additionally, contact is established between the flange raised face bottom and the gasket top surface by applying a sufficiently small displacement at the bottom of bolts (UY= -0.01mm) in such a way that it does not produce stress in the joint components. The required target stress in the bolts is achieved by applying a second value of displacement in sequence at the bottom of the bolts. After applying pre-stress in all the bolts according to the current ASME guidelines i.e. as per sequence 1 (1,3,5,7,2,4,6,8) in the first three passes and in last pass as per sequence 2 – chase pass (1,2,3,4,5,6,7,8,). For the operating conditions, an internal pressure equal to the design pressure (15.3MPa) and proof test pressure (23MPa) was applied. The end-cap loading (21.48MPa due to internal pressure) is applied to the end of the pipe as nodal forces across the walls of the pipe and at a suitable distance away from the joint. Axial load ranging from 100~400kN and thermal loading ranging from 100~400°C was applied in addition to the design and proof test pressure and the analysis was performed to investigate the overall joint behavior. All applied loading magnitudes are given in Table 3 and the applied boundary conditions are shown in Figure 2b.



Figure 2: (a) Modeling and meshing of flange, bolt and gasket; (b) Boundary conditions

Table 3: Loading Condition

Type of Loading	Load
Bolt up as per ASME strategy	Torque = 700 Nm
Combined Loading: Internal Pressure + Axial + Thermal	Design Pressure (DP) = 15.3 MPa Proof Test Pressure (PT) = 23 MPa Axial Loading (AL) = 100-400 kN Temperature (Temp) = 100-400 °C

5. FINITE ELEMENT MODEL VERIFICATION

The FE models developed were verified under thermal and structural loading. For thermal loading, at internal and external sections of the pipe; 100° C surface load with convective coefficient (150 W/m²K) and 20°C surface load with convective coefficient (20 W/m²K) respectively were applied. For structural load completion, an internal pressure (DP= 15.3 MPa) at inner pipe section and end cap loading (21.48 MPa) at pipe end was applied. Based on wall thickness/diameter ratio >1/20, Lame's theorem was used for analytical solution. Numerical results for temperature distribution and structural stresses are measured along inside and outside wall of the pipe and are observed to be in good agreement with the analytical results [Table 4].

Table 4:	Comparison	between	numerical	and	analytical	results
					2	

Т	hermal V	verification		Structural Verification			
Inside sur temperatur	face e (°C)	Outside surface temperature (°C)		Inside pipe wall (MPa)		Outside pipe wall (MPa)	
(Analytical)	(FEA)	(Analytical)	(FEA)	(Analytical)	(FEA)	(Analytical)	(FEA)
88.12	87.98	87.54	87.54	57.12	56.54	87.54	87.54

6. RESULTS AND DISCUSSION

The performance of the gasketed flanged pipe joint under combined loading is discussed and summarized under various different combined loadings and sequences in the following sections.

6.1. Design pressure plus combined loading

In order to study the effect of loading sequence, firstly an internal pressure was applied up to design pressure (15.3MPa) and then an axial load was increased to 400kN. Finally keeping axial load constant at 400kN, the temperature was gradually increased from 100-400 °C and joint behavior was analyzed.

6.1.1. Axial bolt stress variation

Figure 3a shows different bolt bending behavior in each bolt during preloading when using tightening sequence 1 and 2. During the joint assembly, the axial stresses are seen to increase in bolts 1,5,3,7; whereas in bolts 2,4,6,and 8 these show relaxation in pass 4. Under the application of the internal (design) pressure, the axial stresses all increased in all bolts with the maximum value found in bolt 5 (377MPa). Figure 3b shows the gradual increasein average bolt stress with the additional axial load of 100-400kN. Bolt 5 shows the overall maximum stress increase of 280MPa at the design pressure to 302MPa when subjected to the axial load of 400KN. Under the additional thermal loading (100-400°C), the average bolt stresses are observed to relax with the maximum relaxation at 400°C in almost all the bolts



[Figure 3c]. Overall, maximum stress in all the bolts is noted to be lower than the allowable stress of 700MPa.

Figure 3: (a) Individual bolt bending behaviour under Bolt Up and Design Pressure; (b) Average bolt stress variations under; Bolt up + Design pressure + Axial loading (c) Average bolt stress variations under; Bolt up + Design pressure + Axial loading + Temperature

6.1.2. Stress variation at hub flange fillet

The principal stress, axial stress and stress intensity are found to exceed the the yield stress of flange material (248MPa) even under initial bolt up; which is then further increased under the application of the internal pressure. The maximum principal stress, stress intensity and axial stress at the design pressure all increase from 355MPa to 368MPa; 285MPa to 298MPa and 236MPa to 240MPa respectively under the application of the additional axial load of 400kN [Figure 4(a)]. Under the superposed thermal loading (100-400°C), all measured

stresses were observed to increase to the maximum at temperature of 100°C; whereas under 200-400°C, the stresses gradually decreased and the maximum stresse relaxation was observed at 400°C [Figure 4(b)].



Figure 4: Flange stress variation (S1, SINT, SY) under; (a) Bolt UP + Design Pressure + Axial Loading (b) Bolt Up + Design Pressure + Axial Loading + Temperature

6.1.3. Gasket stress variation

The outer and inner nodes on the gasket sealing ring corresponding to the relevant bolt locations were selected in order to study the contact stress variation and hence the effect of bolt scatter on the joint sealing performance during each bolt tightening sequence on the joint. The nomenclature of the representative nodes on the gasket close to each bolt is shown in Figure 5.



Figure 5: Nomenclatures of selected nodes on Gasket

As per gasket manufacturer specification, 68MPa (compressive) is the recommended seating stress of the gasket which ensures that the leakage does not take place [28]. During bolt up, the gasket stresses were found to be higher than the required seating stress (-129MPa to - 139MPa); which are slightly reduced but are more than the minimum required seating stress

of -68MPa (-127MPa on outer ring and -90MPa on inner ring). The conclusion therefore is that there should not be any leakage at any location. With the additional axial load of 100-400kN, the gasket seating stress decreases to a minimum of -114MPa at G6 at outer ring with the axial load applied at 400kN. This shows sealing occurs along the outer seal ring and is due, in part, to the flange rotation. At the inner ring location, the gasket seating stress reduces to -57MPa at G6 and -61MPa at G7 at the applied axial load of 400kN, resulting in the possible leakage Figure 6(a,b). It is concluded that, provided there has been no relaxation during joint assembly at these locations, there should be no sealing failure as a value of -86MPa seating stress is achieved at all the other locations with the next 'at risk' locations being G6 and G7.

Under the additional thermal loading of 100-400°C, the temperature effect are found to be dominant resulting in gasket seating stress relaxation lower than is at 400°C along G1 to G4 and G6 and at 300°C along G2 at outer ring. Along the inner ring, at a temperature of 200-400°C, the minimum gasket seating stress was found to be -50MPa, concluding that sealing failure and possible leakage is imminent [Figure 6(c,d)].



Figure 6: Gasket stress variation at Outer Sealing Ring (left column), Inner Sealing Ring (right column) under: (a,b) Bolt UP + Design Pressure + Axial Loading (c,d) Bolt Up + Design Pressure + Axial Loading + Temperature

6.2. Proof test pressure plus Combined loading

In order to study the effect of loading sequence, the internal pressure was first applied at the proof test pressure of 294MPa and the temperature was increased to 400°C. f]Finally, the temperature was fixed at 400°C, and the axial load was gradually increased from 100-400kN and the joint behaviour was assessed.

6.2.1. Axial bolts stress variation

The maximum axial stress was observed in Bolt 5 at the proof test pressure (294MPa) and at the temperature of 400°C (315MPa) respectively, which further increased to 339MPa with the additional axial load of 400kN. Similarly, the minimum axial stress was observed in Bolt 4 at 167 MPa and 125MPa at the proof test pressure (167MPa) and at temperature of 400°C (152MPa), which further increased to 152MPa with the additional axial load of 400kN. Overall, the relaxation in all bolts stress was observed at 400°C shows dominant effect of temperature, whereas the stress increased gradually under additional axial loading.

6.2.2. Stress at hub flange fillet

Figure 7 shows yielding at hub flange fillet under bolt up and at the proof test pressure. Under additional axial load of 400kN, the maximum principal stress at 200°C (388MPa) decreased to 369MPa; the maximum stress intensity at 200°C (264MPa) increased to 287MPa; and the maximum axial stress at 200°C (288MPa) increased to 295MPa. Under the additional axial load of 400kN, the maximum principal stress at 400°C (383MPa) decreased to 343MPa; the maximum stress intensity at 400°C (291MPa) remained constant; and the maximum axial stress at 400°C (280MPa) increased to 296MPa.



Figure 7: Flange stress variation (S1, SINT, SY) at Bolt Up + Proof test Pressure + Temperature (400°C) + Axial Loading

6.2.3. Gasket stress variation

Under the bolt up and proof test pressure and additional axial load of 300kN and 400kN, the minimum compressive gasket stress on outer seal ring of -112MPa at 200°C was observed to decrease to -94MPa; whereas along the inner seal ring, the minimum gasket stress of -89MPa was found to decrease to -54MPa at bolt location G2, G3, G4 and G6. Under the bolt up and proof test pressure, and at the additional axial load of 400kN, the minimum compressive gasket stress on outer seal ring of -92MPa in the gasket at 400°C decreased to -55MPa at G2, G3, G4; whereas along the inner seal ring, the minimum stress of -56MPa decreased to -49MPa along all bolt locations at inner side ring [Figure 8]. This concludes this is a possible leakage path under both the axial and thermal loading conditions with higher temperature more dominant in sealing failure risk.



Figure 8: Gasket stress variation at; (a) Outer Sealing Ring; (b) Inner Sealing Ring under Bolt Up + Proof test pressure + Temperature (400°C) + Axial Loading Overall joint strength and sealing performance is summarized in Table 5 under different applied loading conditions.

Loading	Joint Strength failure		Sealing failure
Loading	Bolts	Hub Flange Fillet	Gasket
BU	Safe	Unsafe at certain locations	Safe
DP+AL	Safe	Unsafe at certain locations	Unsafe at G6, G7 at 400kN
DP+AL (400kN) +TEMP(100- 400°C)	Safe	Unsafe at certain locations	Unsafe at G2, G3, G4, G6 at 200°C Unsafe at all location at 300°C and 400°C
PT+TEMP(400°C) +AL (100-400kN)	Safe	Unsafe at certain locations	Unsafe at G2, G3, G4, G6 at 200°C Unsafe at all location at 200°C and above

 Table 5: Performance (joint strength and sealing failure) under different loading

7. CONCLUSIONS

Gasketed bolted flanged pipe joint behavior (strength and sealing) has been studied under bolt up and combined internal pressure, axial and thermal loading. For the specific case study considered, the maximum stresses at the bolts, pipe, hub pipes and hub center were found to be within the allowable stress under bolt up and combined loading. However at the hub flange fillet, the stresses were seen to exceed the yield stress even at the bolt up state and also under additional different combined loading therefore showing local failure. The stresses increased gradually under the design and proof test pressure and axial loading. Any additional applied thermal loading resulted in bolt stress relaxation and the possibility of flange rotation due to yielding at hub flange fillet, therefore showing its dominant role in joint integrity.

The sealing capability of the gasket bolted flanged pipe joint was found to be highly dependent on the bolt tightening strategy employed during joint assembly; which in the present study was implemented in accordance with ASME guidelines. The recommended gasket seating stress was achieved during bolt up and this slightly relaxed under the design and proof test pressure and was reasonably affected under axial load with sealing failure at certain locations. The thermal loading was shown to be a dominant effect with sealing performance

acceptable up to 100°C, whereas beyond that no sealing was observed leading to possible leakage and hence a joint failure scenario.

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