

A STUDY ON THE MECHANICAL INTERACTION BETWEEN SOIL AND COLLOIDAL SILICA GEL FOR GROUND IMPROVEMENT

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ABSTRACT

In this paper, we explore the mechanical performance of colloidal silica grout to assess its potential for ground stabilisation and hydraulic barrier formation during decommissioning of major industrially contaminated sites. We consider two colloidal silica -soil systems: sand grouted with colloidal silica and kaolin clay mixed with colloidal silica. The aims of the paper are to evaluate the drained stress-strain behaviour (1-D compression and shear resistance) of colloidal silica-soil systems and to determine the particle interactions between soil and colloidal silica at a micron-scale so as to provide an understanding of the macroscopic mechanical behaviour. Two different colloidal silica-soil interaction mechanisms have been found: formation of a solid, cohesive matrix for the case of grouted sand, and increase of the clustering of clay particles for the case of clay mixtures. This paper illustrates for the first time that even under drained conditions colloidal silica can provide mechanical improvement. Colloidal silica-grouted sand showed an increased stiffness and enhanced peak friction angle, while still having a very low hydraulic conductivity ($\sim 10^{-10}$ m/s), typical of intact clay. Similarly, clay-colloidal silica mixtures showed reduced volumetric deformation, increased stiffness for low values of stress (~ 100 kPa), and increases in both the peak and the ultimate shear strength. Our results show that colloidal silica could be deployed in environments where not only hydraulic containment is critical, but where reduced deformation and enhanced resistance to shearing would be beneficial, for example in landfill capping or in the outer fill

layers of embankments designed to minimise internal seepage and infiltration.

1 **1. INTRODUCTION**

2 Over the last thirty years, Colloidal Silica (CS) has been investigated, and more recently
3 deployed, as a low viscosity grout for permeation grouting in soils and for grouting fractured
4 rock. CS has a number of properties that make it attractive. It has an initially low viscosity
5 (close to water) which means that very low injection pressures are required (Moridis et al.,
6 1995). The gel time of CS can be controlled from minutes to several days (Iler, 1979, Yates,
7 1990) and, once gelled, it has a hydraulic conductivity in the order of 10^{-9} m/s (Moridis et al.,
8 1996a). In addition, it is considered to be environmentally inert (Moridis et al., 1995) and
9 with particle sizes $<100\text{nm}$, it has high penetrability (Iler, 1979, Yates, 1990, Persoff et al.,
10 1995, Moridis et al., 1995).

11 The key material property that makes CS attractive for use in ground engineering is
12 undoubtedly its low hydraulic conductivity. As such it has been investigated for (i) controlling
13 fluid flow around wellbores within the petroleum industry (Jurinak and Summers, 1991), (ii)
14 as a permeation grout for barrier systems for contaminated sites (Persoff et al., 1995, Moridis
15 et al., 1995, Moridis et al., 1996a, Moridis et al., 1996b, Hakem et al., 1997, Moridis et al.,
16 1999, Persoff et al., 1999, Manchester et al., 2001), and (iii) for preventing water ingress in
17 the tunnelling and underground construction industry (Bahadur et al. (2007), Butrón et al.
18 (2010).

19 However, CS also provides some level of mechanical improvement. Indeed, a field test
20 by (Moridis et al., 1995) showed that “CS imparted sufficient structural strength to the matrix
21 to permit 10ft high vertical sections of the matrix (characterized by very loose, friable, and
22 heterogeneous materials) to stand without collapsing”. CS has also been investigated as a
23 means of increasing resistance to liquefaction in loose sands (Gallagher and Mitchell, 2002,

24 Gallagher and Finsterle, 2004, Gallagher et al., 2007, Gallagher and Lin, 2009, Huang and
25 Wang, 2016), and as stabilizer for collapsible clayey soils (Iranpour, 2016).

26 Despite its consideration for use in a range of different applications, limited data exist
27 which characterise the mechanical behaviour of grouted soils. The behaviour of pure CS silica
28 has been investigated (Axelsson, 2006, Funehag and Fransson, 2006, Funehag and Gustafson,
29 2008, Butrón et al., 2009) indicating the fragile nature of the gel. To date the mechanical
30 behaviour of grouted soils which has been reported has been largely limited to the undrained
31 behaviour of grouted sand. Unconfined compressive strength (UCS) tests of grouted soil
32 samples have been reported which demonstrate that grouted-sand specimens have UCS values
33 up to several hundreds of kPas and that increasing the concentration of silica in the colloidal
34 suspension increases the UCS and that UCS increases with curing time (Persoff et al., 1999,
35 Gallagher and Mitchell, 2002, Liao et al., 2003, Mollamahmutoglu and Yilmaz, 2010,
36 Changizi and Haddad, 2017). Undrained triaxial tests have also been conducted which
37 demonstrate the reduced deformation of grouted sand specimens (and hence reduced loss of
38 strength) when subjected to cyclic loading (to simulate earthquake loading) as a means of
39 assessing its potential to mitigate against liquefaction (Gallagher and Mitchell, 2002). A
40 reduction in compressibility and reduced strain at failure has also been observed for clayey
41 soil when mixed with a small amount of colloidal silica (less than 1% by weight) (Changizi
42 and Haddad, 2017).

43 The small increase in the mechanical resistance (an increase in the cohesion and a
44 decrease in the compressibility) coupled with the well-documented large reduction in
45 hydraulic conductivity (and hence increase in consolidation time) makes CS grouting or CS
46 soil mixtures a promising technique for a range of soil stabilization applications. In particular,
47 the undrained results reported to date in the literature indicate its potential for short-term

48 stability problems e.g. for temporary excavations, cuttings immediately after excavation,
49 tunnelling and construction in earthquake prone areas. In this paper, we explore the drained
50 behaviour of CS-soil systems to assess its potential for use in other ground improvement
51 applications. The drained behaviour of CS-soil systems has not been investigated until now.

52 In this research we consider two CS-soil systems: sand grouted with CS and kaolin clay
53 mixed with CS. The former is to simulate soil grouted via permeation grouting and the latter
54 to investigate a potential new material for ground engineering. The aims of the paper are (1)
55 to evaluate the drained stress-strain behaviour (1-D compression and shear resistance) of CS-
56 soil systems and (2) to determine the particle interactions between soil and colloidal silica at a
57 micron-scale so as to provide an understanding of the macroscopic mechanical behaviour.

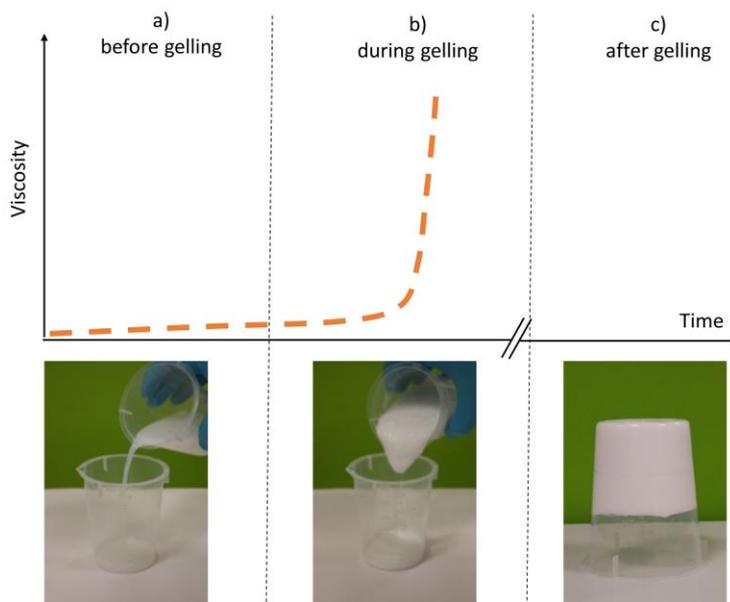
58 **2. MATERIALS AND SPECIMEN PREPARATION**

59 Five different materials were used during this experimental campaign: CS gel only,
60 Leighton Buzzard sand only, Leighton Buzzard sand grouted with CS, kaolin clay only and
61 kaolin clay mixed with CS. The preparation methods for these materials are each described in-
62 turn.

63 **2.1 CS gel**

64 Colloidal silica is an aqueous dispersion of silica particles (Figure 1), which are generally
65 uniform in size and can range from several, to hundreds, of nanometres. A colloidal silica
66 dispersion can be destabilized (Figure 1b) via the controlled application of an electrolyte.
67 Once destabilized, silica particles form siloxane bonds (Si-O-Si), resulting in an increase in
68 the viscosity (Figure 1a and Figure 1c) and eventually a connected matrix of nano-particles,
69 i.e. a gel (Figure 1b). The gelation rate and the gel time (Figure 1b) can be controlled by
70 varying several factors including: particle size, particle concentration, pH, electrolyte

71 concentration, valency and temperature (Iler, 1979, Pedrotti et al., 2017). Hence, colloidal
72 silica grouting requires the combination of two components: the colloidal silica suspension
73 itself and the addition of an electrolyte. In this study Meyco MP320 colloidal silica was used.
74 MP320 has a 40% silica weight concentration, a nominal particle size of 15 nm and a density
75 of 1300 kg/m³. The specific gravity of the silica particles is estimated to be 2.11.



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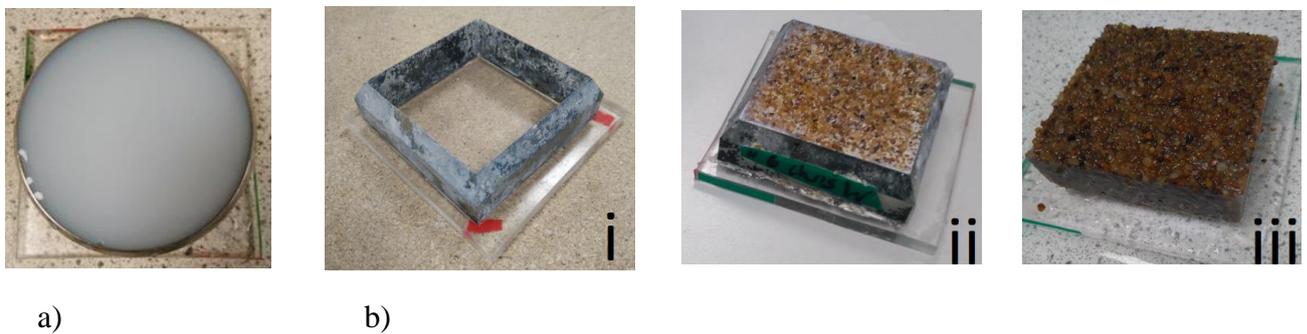
77 Figure 1. Gelling of CS: a) CS before gelling, b) CS close to the gel time, c) CS after gelling.

78 To prepare the CS gel samples, CS and the electrolyte solutions were hand mixed in a 5:1
79 ratio by volume respectively. A solution of NaCl with a concentration of 1.7 M (unless
80 otherwise specified), giving a final electrolyte concentration in the grout mix of 0.28 M, was
81 used in order to obtain a 1 hour gel time. The corresponding rapid increasing in viscosity
82 ended and a firm gel was obtained within a period of approximately less than two hours. The
83 required electrolyte concentrations were determined using the analytical model described in
84 Pedrotti et al. (2017).

85 In order to reduce water evaporation during sample preparation, once the CS and the

86 electrolyte solution were mixed, all specimens were placed in a chamber and kept at 20°C and
87 90% relative humidity (90% RH) until gelled. Once gelled, the specimens were cured. Unless
88 otherwise specified, all samples were cured for 1 week by storing under demineralised water
89 at 20°C.

90 For oedometer testing, specimens of colloidal silica were gelled and cured using the same
91 process, but within the oedometer ring moulds as required for later consolidation testing
92 (Figure 2a). The moulds were made up of a steel oedometer ring with a diameter of 75 mm
93 and thickness of 20 mm attached to a removable plastic base. Silicon grease was applied
94 around the contact between the ring and base to preventing leakage prior to gelling. After
95 curing and subsequent aging, the plastic bases were removed and the oedometer rings
96 containing the CS specimen were placed directly into the oedometer test cell.



97 Figure 2. Specimen preparation: (a) colloidal silica specimen during curing in oedometer
98 mould, (b) shearbox specimen *i.* mould, *ii.* sand grouted with CS in mould and *iii.* grouted
99 sand specimen after curing and removal from mould.

100 **2.2 Leighton Buzzard sand/ Leighton Buzzard sand grouted with CS**

101 Leighton Buzzard sand with a d_{50} of 1.2 mm, a specific gravity of 2.65 and a coefficient
102 of uniformity of 1.26 was used for all tests. Sand was washed prior to the experiment in order
103 to remove any fines.

104 For oedometer testing, the oedometer cutting ring was filled with sand, and a plastic

105 syringe was used to measure the required volume of CS. The grouting process was carried out
106 simply by pouring the CS on top of the sand (i.e. the syringe was not embedded). The
107 oedometer cutting ring was attached to a removable plastic base, the edges were sealed with
108 silicon grease to prevent grout leakage prior to the gel time. 148g of Leighton Buzzard sand
109 were grouted with 39 ml of CS mixture.

110 Specimens were subsequently gelled and cured, as described for the CS samples. For CS
111 grouted sand, each sample was prepared using a NaCl solution resulting in a gel time of
112 approximately 1 hour.

113 Sand and CS grouted sands were also tested in a shear box. For the shear box, each
114 specimen was prepared by placing 124 g of dry sand into a mould 60 mm x 60 mm x 20 mm
115 height (Figure 2b-i and Figure 2b-ii.). Each specimen was then saturated with 28 ml colloidal
116 silica grout prepared using NaCl. Each square mould had a plastic base, with silicon grease
117 applied at the contact between the mould and base. After curing and subsequent aging, the
118 plastic mould bases were simply detached and, using an extraction tool, the grouted soil
119 specimens (Figure 2b-iii) were transferred into the shear box without damage.

120 **2.3 Kaolin clay/ Kaolin clay mixed with CS**

121 Speswhite kaolin with a plastic limit (w_p) of 0.32 and a liquid limit (w_L) of 0.64 was used
122 for the tests presented in this paper. The grain size distribution shows it is composed of 20%
123 silt-sized particles and 80% clay-sized particles. Kaolin clay specimens were prepared
124 reconstituted from slurry with a water content equal to $1.5w_L$ ($w=0.96$).

125 Specimens of kaolin clay mixed with CS were prepared by hand mixing 100 g of kaolin
126 powder with 153 g of CS to produce a homogeneous slurry (no visible lumps or aggregates).
127 Hand mixing was selected so that results were directly comparable, since it is the standard
128 procedure for preparing clay reconstituted from slurry. This resulted in a specimen made by

129 100 g of kaolin, 96 g of water and 57g of silica particles. In this way, the ratio between the
130 mass of water (present in the CS) and the mass of solids of kaolin was the same as that for the
131 specimen of kaolin alone ($M_w/M_{s_kaolin}=0.96$). Using the same concentration of NaCl solution
132 resulted in a slightly shorter gel time in the clay specimens (compared to the sand specimens),
133 this may be a result of less available water in the grout mix (arising from water absorption by
134 clay particles) or due to cation exchange between the clay particles and the grout mix.

135 For oedometer testing, a pre-mixed specimen (slurry) of kaolin clay and CS was
136 transferred into the oedometer ring mould. The moulds containing the kaolin clay/CS mixture
137 was subsequently left to gel and cure using the process described for the CS specimens.

138 Speswhite kaolin and CS grouted sands were also tested in a shear box. For the shear box,
139 each specimen was prepared by placing the clay CS mixtures into a mould 60 mm x 60 mm x
140 20 mm height. As for the oedometer specimens, the moulds containing the kaolin clay/CS
141 mixture was subsequently left to gel and cure using the process described above.

142 **3. EXPERIMENTAL PROCEDURES**

143 **3.1 1-D compression tests**

144 1-D mechanical tests were performed in a front-loading oedometer cell (diameter 75 mm)
145 (Controls Testing Equipment Ltd) according to BS 1377-5. All samples were submerged
146 under water in the oedometer cell prior to loading. Samples were compressed in incremental
147 steps to the target vertical stress. Unloading was performed in one single step. For each
148 loading and unloading step, samples were allowed to consolidate for 24h, which was found to
149 be sufficiently long to allow for at least 90% of the consolidation for all samples. For each
150 step, consolidation time (t_{90}) and coefficient of consolidation was calculated according to the
151 conventional Taylor method and subsequently hydraulic conductivity determined. As the

152 initial height and mass of the samples were measured, this was used as a reference point for
153 calculation of the void ratio at each loading step.

154 **3.2 Direct shear tests**

155 Drained direct shearbox tests were conducted using a digital direct shear apparatus (ELE
156 International, Sheffield, UK) according to the BS1377-7 standard (BSI, 1990). For measuring
157 the horizontal shear force and both horizontal and vertical displacements the apparatus is
158 equipped with a 5 kN capacity load cell and two displacement transducers. The internal
159 dimensions of the shearbox body were 60 x 60 mm and 20 mm height. Due to the low
160 hydraulic conductivity of colloidal silica, excess pore water pressure may build up during
161 shearing. From consolidation data, it was determined that a very low shearing rate of 0.001
162 mm/min was required to prevent pore water pressure build-up and thus maintain drained
163 conditions during shearing. All specimens were sheared at this same rate, with each test
164 therefore taking place over a period of approximately 6 days. Vertical effective stresses of
165 100, 200, and 300 kPa were applied to reflect stresses in the near subsurface.

166 Shear tests data performed on kaolin clay reconstituted from slurry and consolidated to
167 50, 100, 150 and 300 kPa are reported here from Pedrotti (2018) (shear rate 0.02 mm/min)
168 and data for the sample consolidated to 300 kPa from Galvani (2003) (shear rate 0.005
169 mm/min).

170 **3.3 Suction measurement**

171 The WP4C dew-point potentiometer manufactured by Decagon Device Inc was used to
172 measure total suction for the sample cured at 90% R.H

173 **3.4 Scanning Electron Microscope Imaging**

174 Microscope images were performed by means of a Field Emission Scanning Electron
175 Microscope (Hitachi SU-6600). This apparatus is equipped with energy dispersive

176 spectroscopy, Oxford Inca 350 with 20mm X-Max detector and Wavelength dispersive
177 spectroscopy, Oxford Inca Wave 700 microanalysis system with Energy to allow elemental
178 analysis of metals and ceramic materials.

179 Microscope images were also obtained using a Tungsten Filament Scanning Electron
180 Microscope (Hitachi S-3700). This apparatus has Energy Dispersive Spectroscopy capability,
181 Oxford Inca 350 with 80mm X-Max detector, to allow elemental analyses of materials.

182 For SEM imaging specimens were oven dried at 105°C for at least 24hr.

183 **3.5 X-CT imaging**

184 CT images were performed by means of a Nikon XT H 320 XRay CT scanner. No
185 sample preparation is required for x-CT imaging, hence, samples remain entirely undisturbed.
186 In the present work, the voxel resolution was approximately 0.504 mm and the scanner
187 settings were energy 183 kV and current 204 μ A.

188 The reconstruction was carried out using CT Pro and CT Agent software (Nikon-
189 Metrology). The visualisation and analysis of the CT data were performed with AVIZO 9.0.

190

191 **4. INVESTIGATION ON THE MECHANICAL BEHAVIOUR**

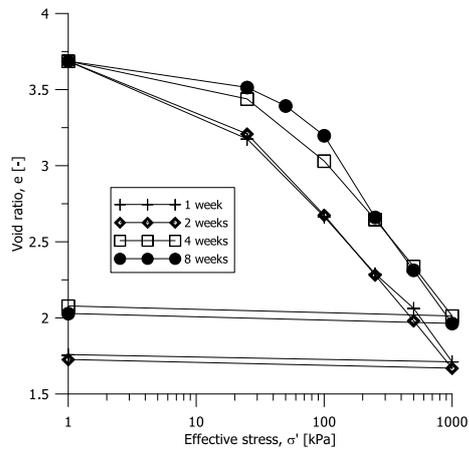
192 The mechanical behaviour of five different materials was investigated in order to
193 highlight the mechanical interaction between soil (i.e. sand and clay) and CS gel. CS gel only,
194 Leighton Buzzard sand only, Leighton Buzzard sand grouted with CS, kaolin clay only and
195 kaolin clay mixed with CS were tested.

196 **4.1 CS gel**

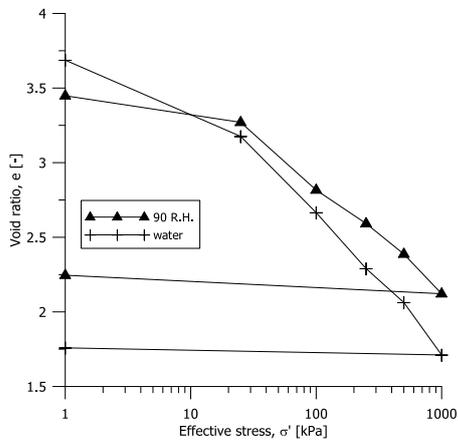
197 *1-D compression tests*

198 The mechanical behaviour upon 1-D compression of CS gel was investigated using the
199 oedometer (Figure 3). Figure 3a shows the void ratio change of four CS samples that were
200 cured under demineralised water for 1, 2, 4 and 8 weeks respectively. Since no deformation
201 occurred during curing, the initial void ratio of these samples is the same. The samples cured
202 for 1 and 2 weeks appear to follow a single compression curve. Similarly, the samples cured
203 for 4 and 8 weeks appear to follow a single (but different) compression curve; the 4 and 8
204 week samples appear to have a stiffer behaviour at low vertical stresses (up to 60 kPa), as if
205 the bonding between silica particles was stronger than the samples cured for less time. As the
206 vertical stress increases the compressibility becomes similar to that of the samples cured for 1
207 or 2 weeks, although the two pairs of curves never merge. Finally, upon unloading, all four
208 samples exhibit the same small elastic swelling, suggesting that the initial particle bonding
209 (and hence gel structure) was not recovered after yielding.

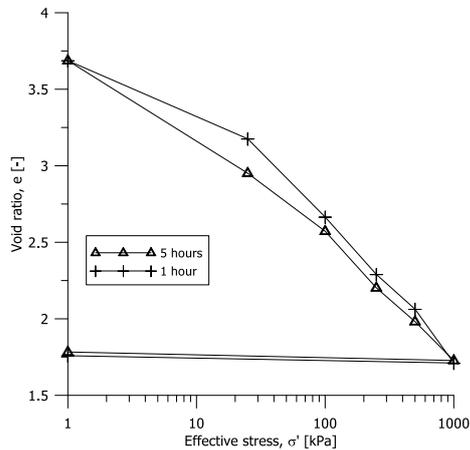
210



a)



b)



c)

211 Figure 3. 1-D compression curves for CS samples: a) tested after different curing
212 durations, b) exposed to different evaporation conditions during curing and c) prepared with
213 different gel times.

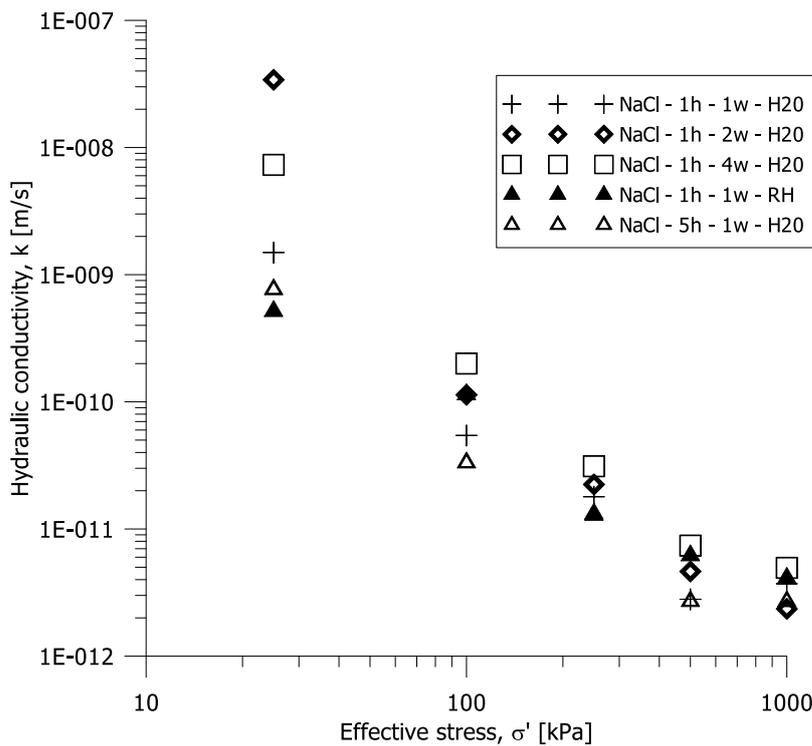
214 Figure 3b shows the void ratio change of two CS samples, prepared with a NaCl

215 electrolyte solution and cured for 1 week. One sample (water) was cured under demineralised
216 water (this same sample was reported in Figure 3a and called “1 week”) whilst the other was
217 cured at a 90% constant Relative Humidity (90 R.H.). After curing, the two samples were
218 tested in the oedometer cell under saturated conditions. Figure 3b demonstrates that the
219 sample cured at 90% RH has suffered some water loss and undergone shrinkage. Upon
220 saturation in the oedometer cell this reduction in volume was not fully recovered and
221 therefore the void ratio at the beginning of the test is smaller than that for the sample cured
222 under water. Upon 1-D compression, the two compression curves diverge and the behaviour
223 of the sample cured at 90% R.H. is stiffer than that of the sample cured under water. In order
224 to investigate the stress conditions at the beginning of consolidation, a similar sample was
225 cured at 90% RH and the total suction was measured. The average suction at the end of curing
226 was measured to be 1620 kPa. Upon drying the lateral earth pressure coefficient is generally
227 unknown, however with a value of suction this high, it seems reasonable to assume that the
228 “equivalent” vertical pre-consolidation stress is higher than 1000 kPa (the maximum vertical
229 stress applied during the oedometer test). Hence, it seems reasonable to ascribe the different
230 compression behaviour between the sample cured in saturated conditions and the sample
231 cured at 90% R.H. to a pre-consolidation stress due to the suction developed in the latter
232 sample. This high suction stress explains the stiffer behaviour of the sample cured at 90%
233 R.H., in terms of over-consolidation (Skempton and Jones, 1944, Sridharan and Nagaraj,
234 2000). Therefore, no information on whether the normal consolidation compressibility is
235 recovered can be determined, since the pre-consolidation stress was not overwhelmed.

236 In Figure 3c the effect of the gel time on 1-D compression was investigated. Two samples
237 were prepared by mixing CS with a NaCl electrolyte solution of different concentrations (1.7
238 M and 1.3 M, such that the samples had gel times of 1 hour and 5 hours respectively. Upon 1-

239 D compression (after 1 week curing in demineralised water), the difference in the
 240 compression curves was well within the repeatability of the test. This result suggests that,
 241 within the accuracy of the measurement, there is no difference in the mechanical behaviour
 242 due to different rates of electro-chemical bonding between particles in the CS.

243 The hydraulic conductivity calculated from the 1-D compression test for each sample at
 244 every loading step is reported in Figure 4. Values range between 10^{-9} and 10^{-12} m/s. Other
 245 than the reduction in hydraulic conductivity with increasing effective vertical stress, there is
 246 no clear pattern of behaviour between samples. The high variability of the points at the first
 247 steps is probably due to the difficulties to estimate the exact consolidation time because of the
 248 long duration of the tests.



249
 250 Figure 4 Hydraulic conductivity for different CS samples.

251 **4.2 Sand grouted with CS gel**

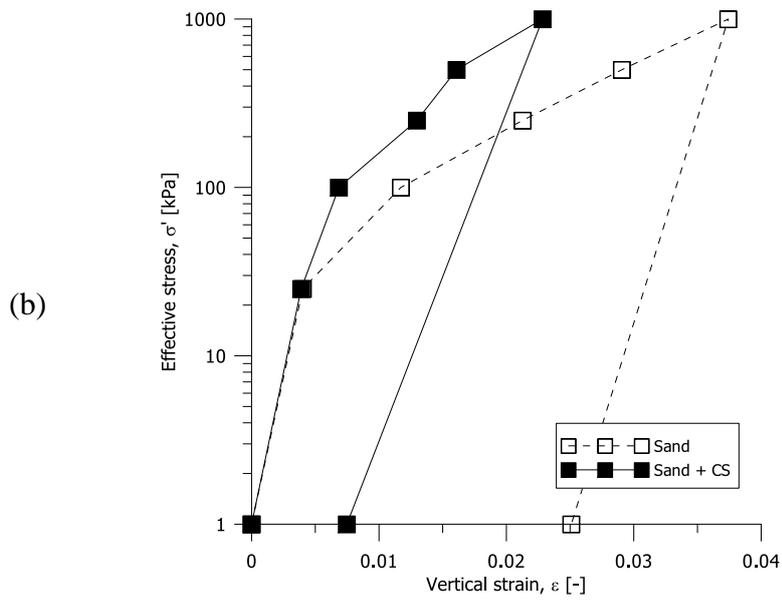
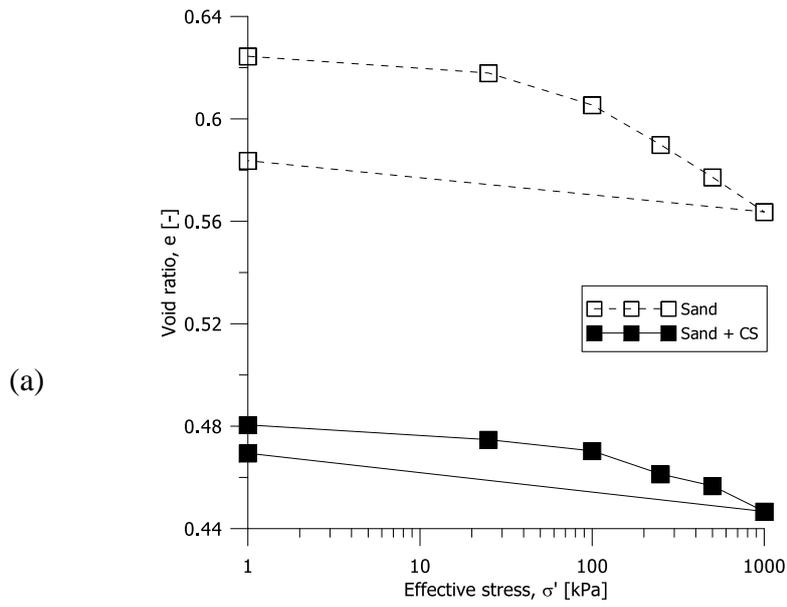
252 1-D compression tests and direct shear tests were carried out on Leighton Buzzard sand
253 only and Leighton Buzzard sand grouted with CS.

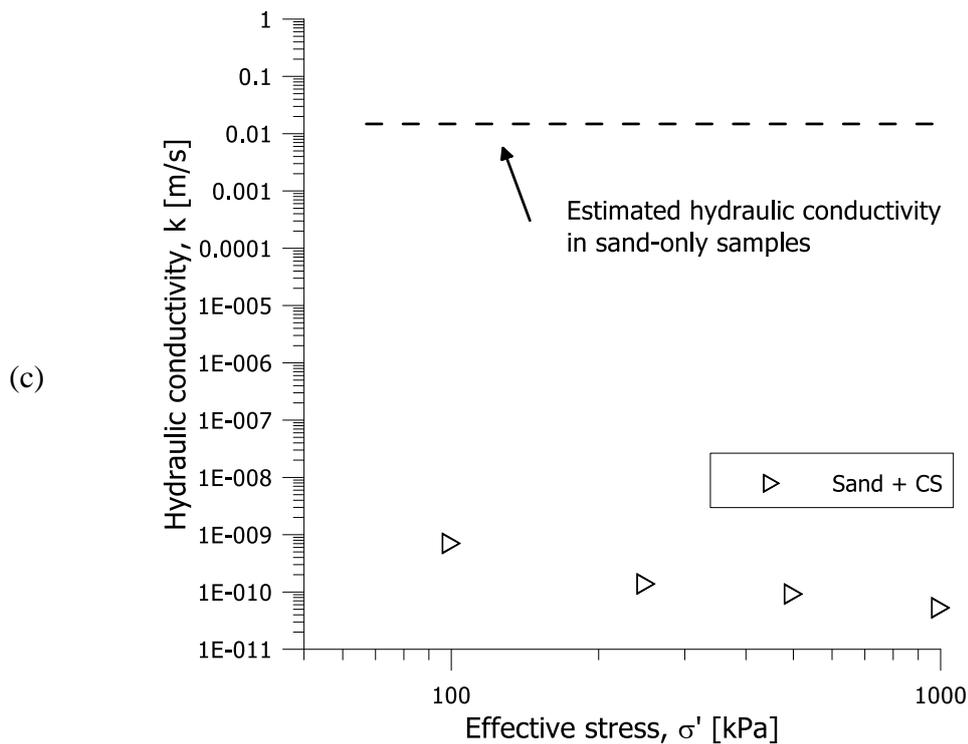
254 *1-D compression tests*

255 In Figure 5a, the change in void ratio upon 1-D compression of a sample of sand grouted
256 with CS is compared with the change in void ratio of sand only. The two samples were
257 prepared with the same initial density of sand, however the sample of sand grouted with CS
258 shows a void ratio lower than the sample with sand only, this is due to the fact that when
259 calculating the void ratio, the silica nano-particles has been considered as part of the solid
260 fraction.

261 To overcome this, Figure 5b shows the same test reported in Figure 5a but plots the
262 observed vertical strain against the effective stress. The sample of sand grouted with CS
263 shows a much stiffer response (i.e. reduced volume change) than the sand only sample. For
264 the grouted sand specimen, the compression behaviour remains stiffer than for sand only over
265 the full range of the investigated vertical stress.

266 It is worth noting that the hydraulic conductivity of sand after CS grouting reduced
267 dramatically. In Figure 5c, the hydraulic conductivity of grouted sand estimated from the
268 consolidation times during the oedometer tests is compared with the hydraulic conductivity of
269 sand only, estimated by using the Hazen's empirical formula (Hazen, 1893) from the grain
270 size analysis. As shown in Figure 5c, the hydraulic conductivity of the CS grouted sand is
271 similar to that expected for a clayey soil (about 10^{-10} m/s). Hence to summarise, the CS
272 grouted sand has a high stiffness similar to sandy soils, but a long consolidation time and low
273 hydraulic conductivity, generally characteristic of clayey soils.





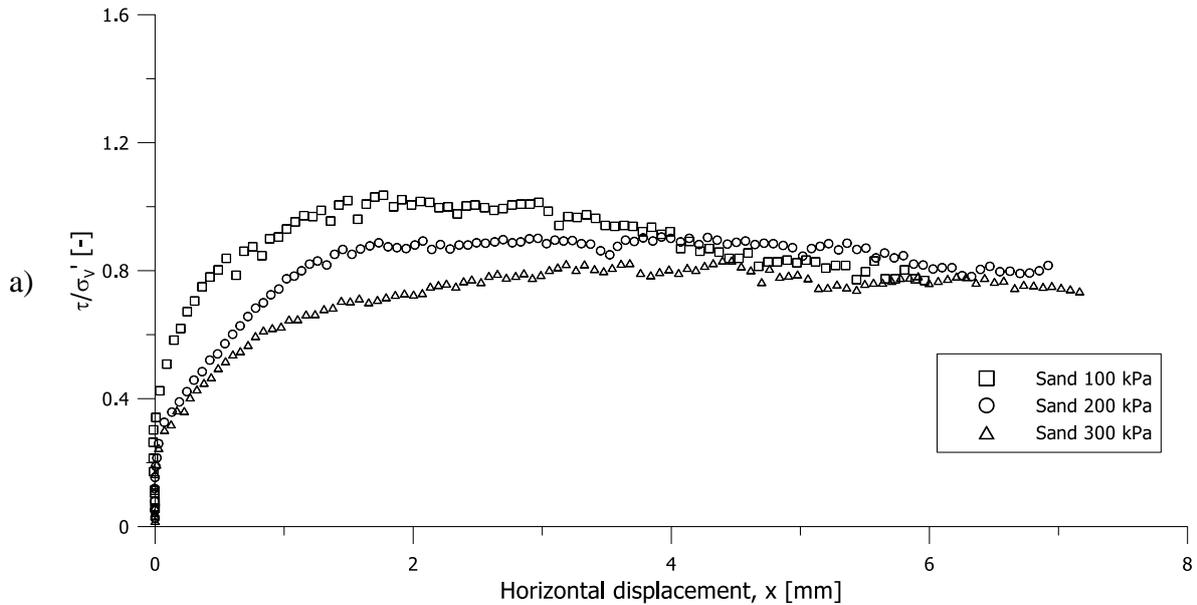
274 Figure 5. 1-D compression tests of sand and sand grouted with CS: (a) void ratio against
275 effective stress, (b) effective stress against vertical strain and (c) hydraulic conductivity
276 against effective stress

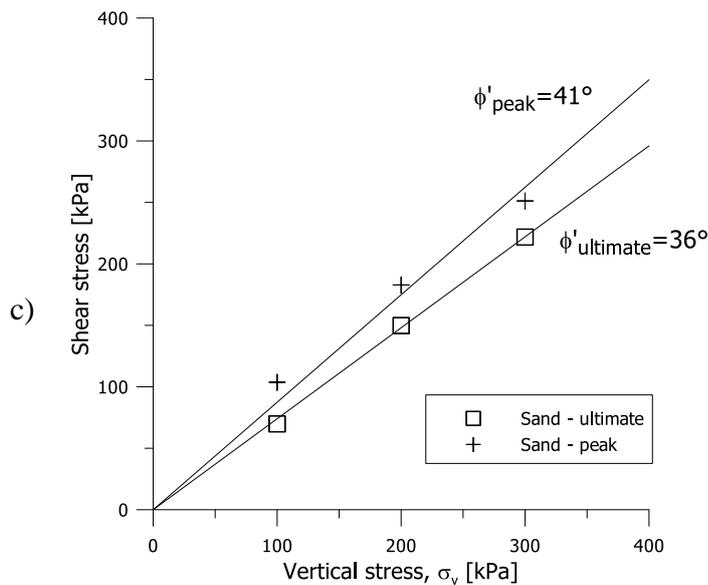
277 *Direct Shear tests*

278 Figure 6 shows the results of a shear test performed on three sand samples, consolidated to
279 100, 200 and 300 kPa under saturated conditions. In Figure 6a the horizontal displacement
280 versus the shear stress/effective vertical stress ratio (t/S'_v) is reported and in Figure 6b the
281 volumetric change in terms of horizontal versus vertical displacement is shown.

282 At the higher vertical stress (300 kPa) the sand exhibits a compressive behaviour, as the
283 vertical stress decreases (200 and 100 kPa) the volumetric behaviour becomes dilative. As
284 expected, all samples tend toward the same value of ultimate stress, and the sample sheared
285 with the lowest vertical stress has the highest peak stress. In order to take into account the
286 effect of the dilatancy, the ultimate shear stress is here defined according to Taylor (1948).

287 These are plotted in Figure 6c. For the ultimate conditions the friction angle, $\phi'_{ultimate}$, was
288 computed to be 36° and for the peak conditions, the friction angle $\phi'_{peak}=41^\circ$. The two
289 envelopes were forced to pass through the origin i.e. no cohesion was allowed.
290





291 Figure 6. Direct shear test on sand samples at different effective vertical stress. a) horizontal
292 displacement versus the shear stress/effective vertical stress ratio, b) volumetric change and c)
293 Direct shear envelopes for sand samples

294 Figure 7 (a-f) shows the shear tests performed on samples of sand grouted with CS for the
295 same values of vertical stress (100, 200 and 300 kPa). For each value of vertical stress two
296 samples were prepared, one cured under demineralised water for 1 week and one for 4 weeks.
297 All shear tests were conducted under saturated conditions.

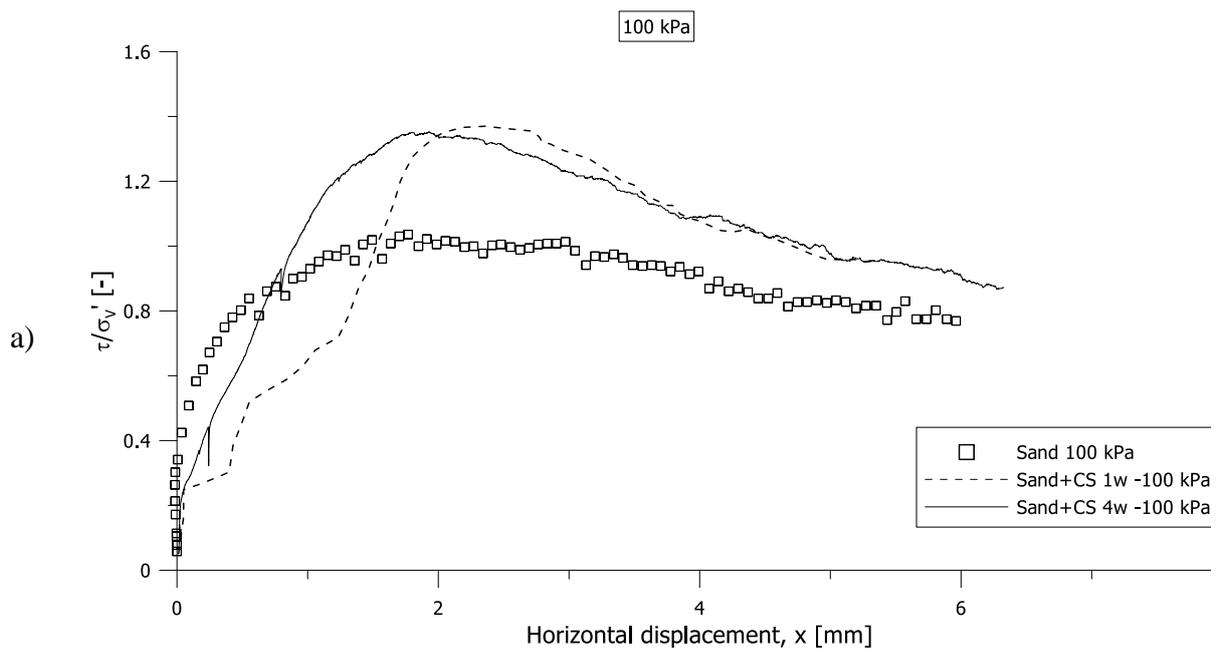
298 Figure 7a and b show the horizontal displacement versus the t/S'_v and versus the vertical
299 displacement, respectively, for an effective vertical stress of 100 kPa. Test results are plotted
300 for sand only, sand and CS cured for 1 week, sand and CS cured for 4 weeks. Figure 7c, d and
301 Figure 7e, f show the same results for samples sheared under effective vertical stresses of 200
302 and 300 kPa, respectively.

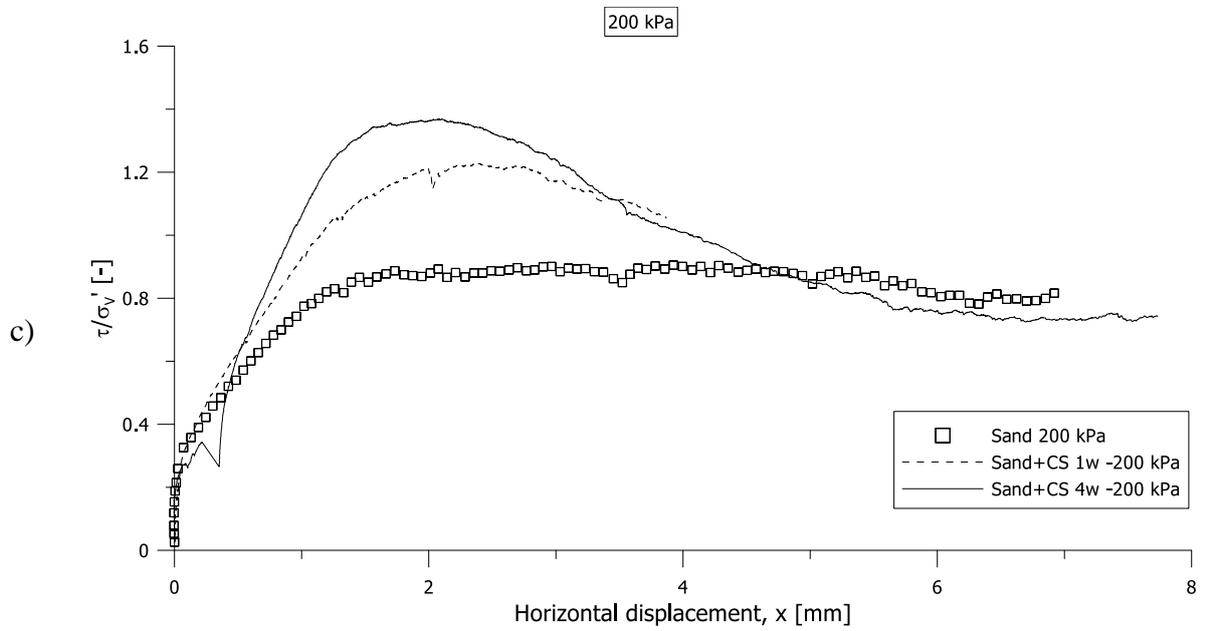
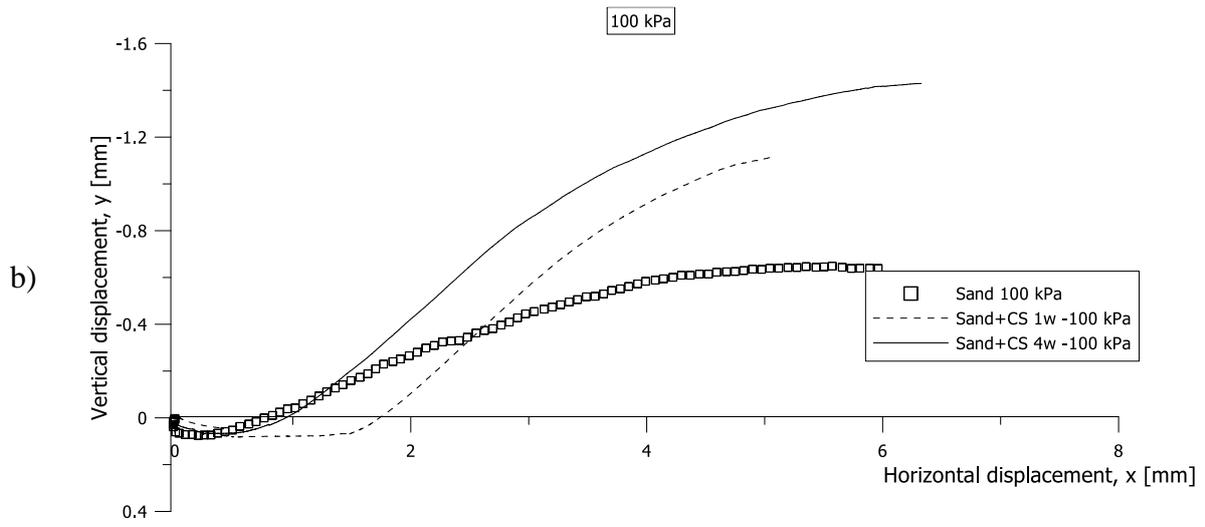
303 Looking at Figure 7a, the sample cured for 4 weeks shows an initial stiffer behaviour than
304 the sample cured for 1 week only. This is in agreement with the oedometer tests presented in
305 Figure 3a.

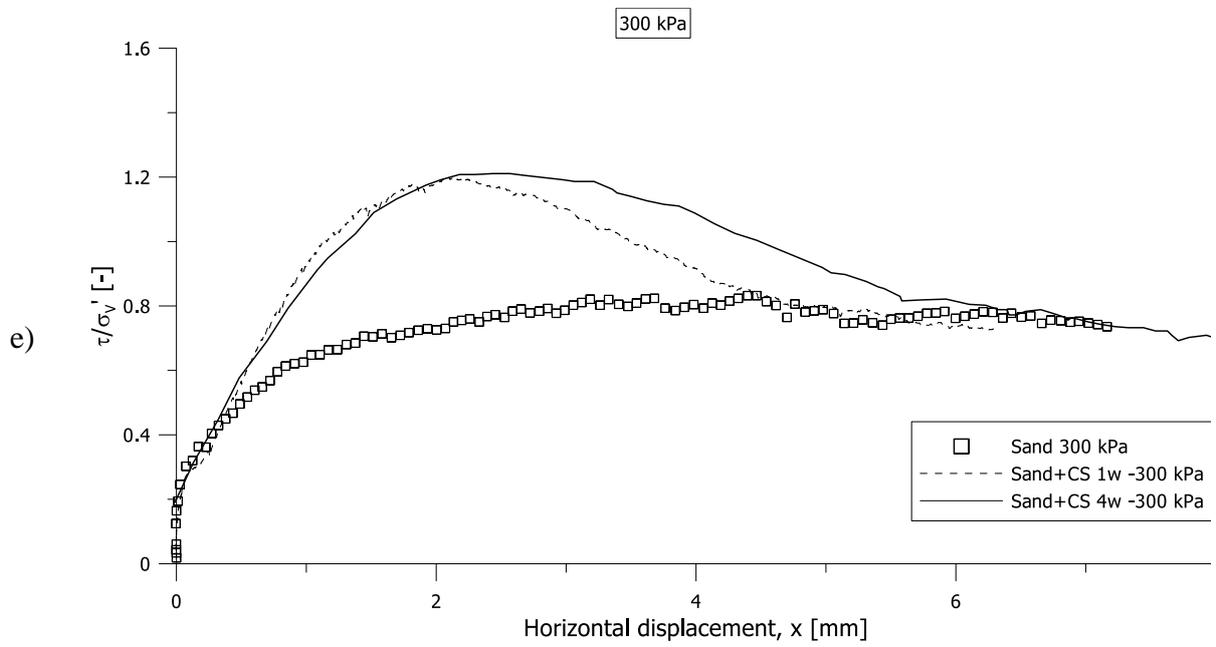
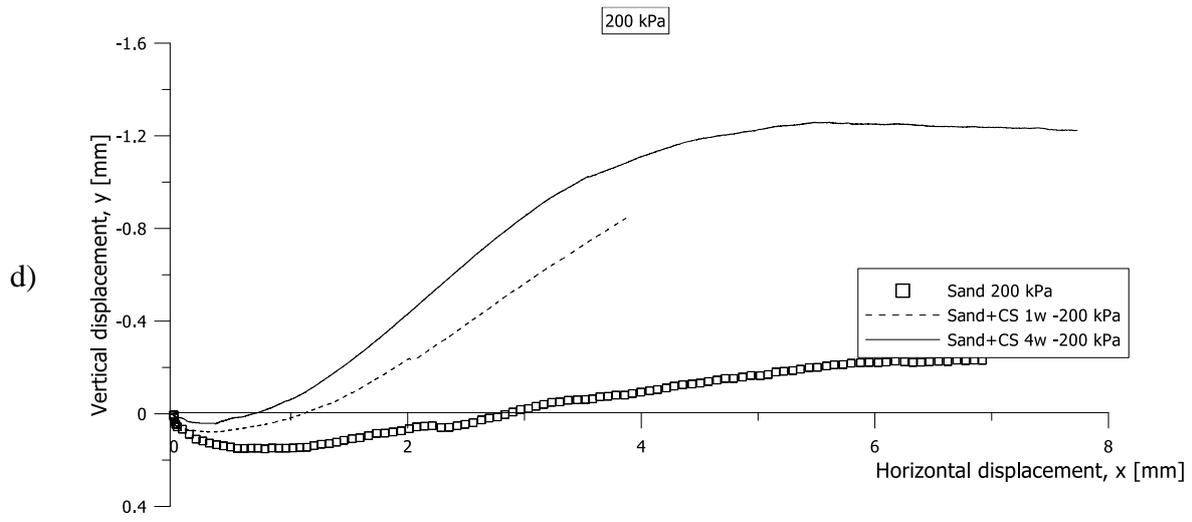
306 The sand only sample is the least compressible. It appears that the presence of the silica
307 has a lubricating effect (increasing the strain required to reach the peak shear stress) which is
308 counterbalanced by the hardening of the CS for longer curing times.

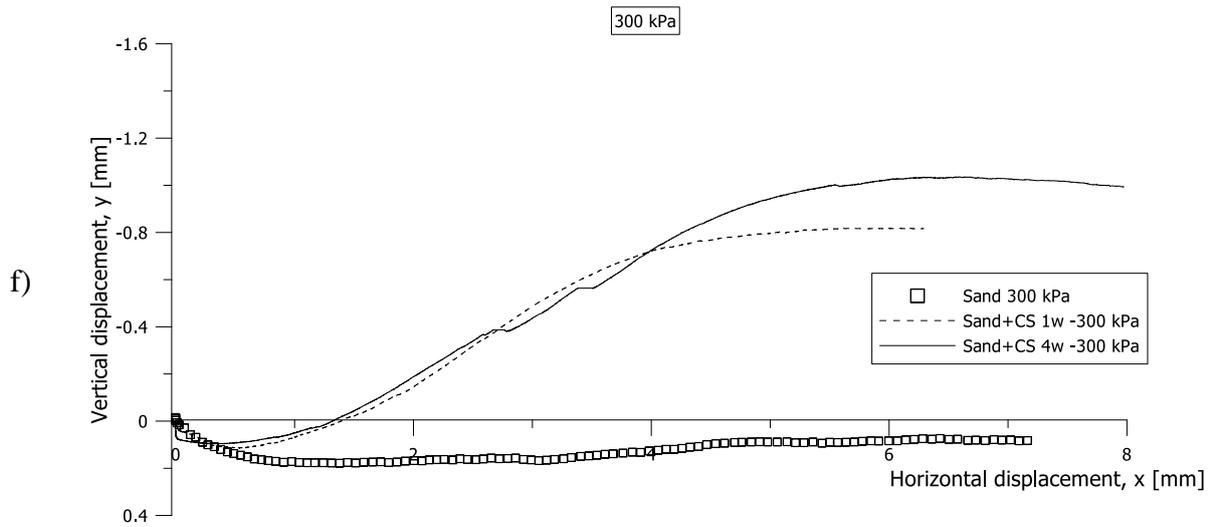
309 The two samples grouted with CS exhibit a peak at a similar shear stress/effective vertical
310 ratio, which is about 30% higher than the sample with sand only. After the peak, although the
311 ultimate shear stress of the grouted samples remains slightly higher than the sand-only
312 sample, the three curves appear to be converging. Figure 7b shows that the two grouted
313 samples have a larger dilatancy than the sand-only sample and that the dilatancy increases
314 with increasing curing time.

315







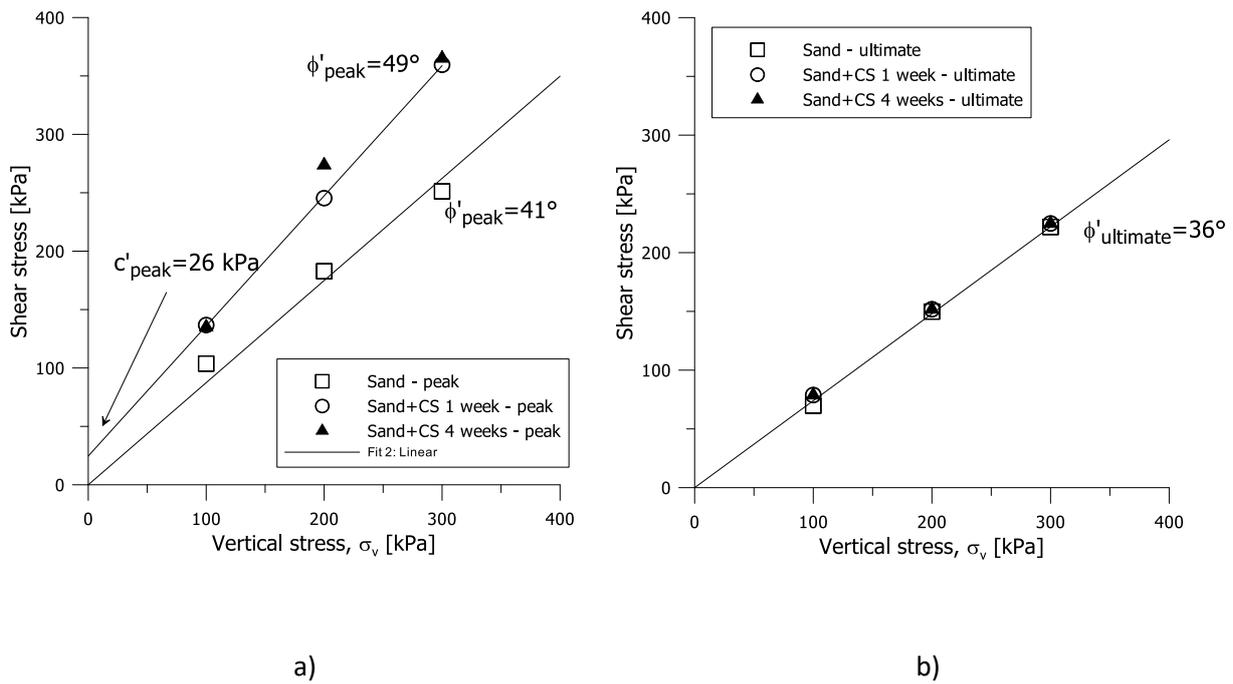


316 Figure 7. Direct shear test on sand sample grouted with CS. a) horizontal displacement versus
317 the shear stress/vertical stress ratio (effective vertical stress 100 kPa), b) volumetric change
318 (effective vertical stress 100 kPa), c) horizontal displacement versus the shear stress/vertical
319 stress ratio (effective vertical stress 200 kPa), d) volumetric change (effective vertical stress
320 200 kPa), e) horizontal displacement versus the shear stress/vertical stress ratio (effective
321 vertical stress 300 kPa), f) volumetric change (effective vertical stress 300 kPa).

322 Analysis of the results at higher vertical stresses in Figure 7c and Figure 7e shows that
323 the general behaviour is very similar to that at 100kPa i.e. all grouted samples show a higher
324 peak stress than with sand-only, and all grouted samples appear to converge to the same
325 ultimate stress as for sand-only. In addition, the volumetric change shown in Figure 7d and
326 Figure 7f is also similar to that in Figure 7b; the grouted samples are dilative and the longer
327 the curing time, the higher the dilatancy.

328 There are, however, a few differences in behaviour worth noting in the results for the
329 200kPa and 300kPa samples. In both sets of results, there is no initial difference in stiffness
330 between the grouted samples (regardless of curing time) and the sand only (Figure 7c and

331 Figure 7e respectively). Hence, the CS lubricating effect appears not to occur at higher
 332 vertical stresses and the additional particle bonding given by the CS becomes negligible.
 333 Also, for the 200kPa load, (Figure 7c) the grouted sample cured for 4 weeks exhibits a higher
 334 peak stress than the sample cured for 1 week, whereas for the 300 kPa load (Figure 7e) the
 335 peaks are the same for both curing times.



336 Figure 8. Shear envelopes: (a) peak shear stress envelope and (b) ultimate shear stress
 337 envelope for sand grouted with CS.

338 Figure 8a shows the peak shear stress envelope, sand-only specimens have a peak friction
 339 angle ϕ'_{peak} of 41° which compares with an average peak friction angle for the grouted
 340 samples of 49° . In addition, the grouted samples exhibit a drained cohesion $c' = 26$ kPa,
 341 which is attributed to bonding provided by the CS matrix before failure. Figure 8b presents
 342 the ultimate shear stress envelope for all of the above tests, confirming that they have a
 343 friction angle, $\phi'_{ultimate}$, of 36° . It is worth highlight that the presence of the particle bonding
 344 provided by the CS increases the peak shear strength and the drained cohesion at peak

345 conditions.

346 **4.3 Clay mixed with CS**

347 1-D compression tests and direct shear tests were carried out Speswhite kaolin clay mixed
348 with CS. The results were compared with tests on Speswhite kaolin clay only.

349 *1-D compression tests*

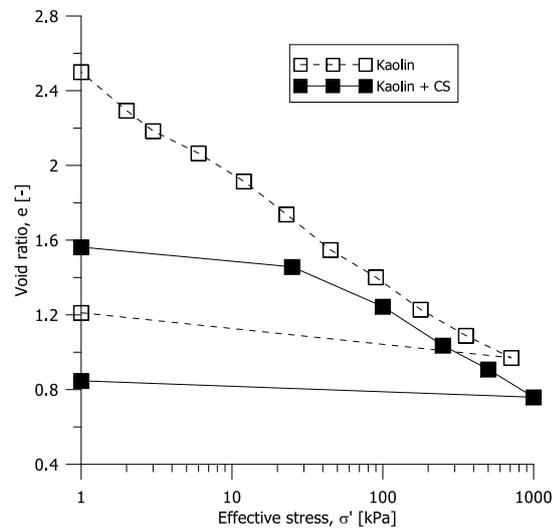
350 In Figure 9a, the change in void ratio upon 1-D compression of a sample of kaolin clay
351 mixed with CS is compared with the change in void ratio of a kaolin clay sample reconstituted
352 from slurry. The sample of kaolin clay mixed with CS at the beginning of the compression
353 test had a void ratio smaller than the sample reconstituted from slurry, and was much less
354 compressible for vertical stress lower than 30 kPa. As the vertical stress increases beyond
355 30kPa, the compressibility of the two samples becomes very similar, although the sample
356 mixed with CS remains denser than the sample reconstituted from the slurry. Despite the
357 similar normal compressibility, the swelling upon unloading was smaller for the sample
358 containing CS than for kaolin only. Hence, it appears that the presence of CS inhibits the
359 recovery of elastic deformation.

360 In the sample reconstituted from slurry, only kaolin and water are present, whereas in the
361 CS mixed sample, the solid fraction is made up of both kaolin and silica nano-particles. In
362 order to compare the mechanical behaviour, the two samples were prepared with the same
363 Mass of water/Mass of kaolin ratio. As a result the initial void ratio of the two samples is
364 different as the volume of silica particles contributes to the volume of solids present. To
365 overcome this, Figure 9b shows the same test as Figure 9a but plots the observed vertical
366 strain against the effective stress. This clearly shows that the sample prepared by mixing
367 kaolin clay and CS is far less compressible than the sample with kaolin only. The reduced
368 compressibility seems to be related to stiffer behaviour at the lowest load steps, caused by the

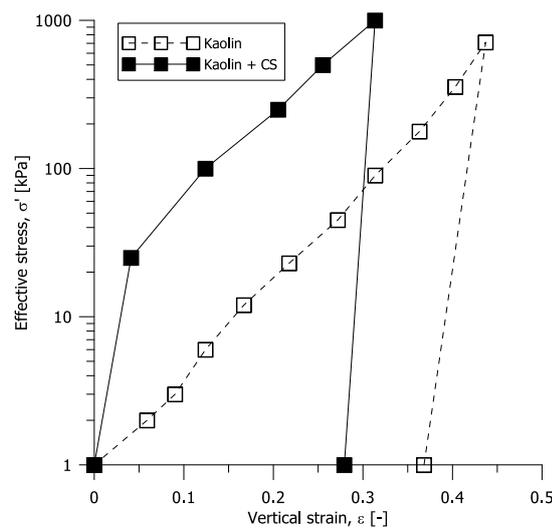
369 presence of the CS. Whereas, at higher vertical load, the two samples have the same
370 compressibility.

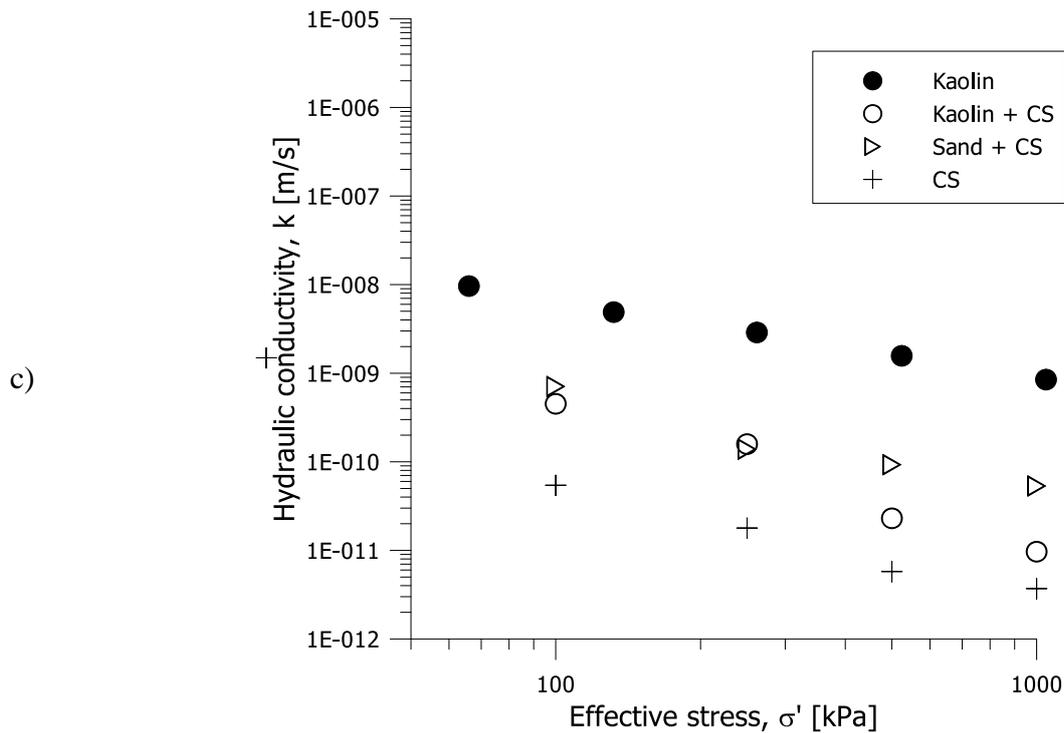
371 In Figure 9c the hydraulic conductivity determined during oedometric consolidation of
372 the kaolin and CS mixture is compared with the one of kaolin only. When silica is present the
373 hydraulic conductivity of the sample drops by two orders of magnitude. Indeed, when the
374 kaolin/CS sample is consolidated to 1000 kPa the hydraulic conductivity was determined to
375 be 9.7×10^{-12} m/s.

a)



b)





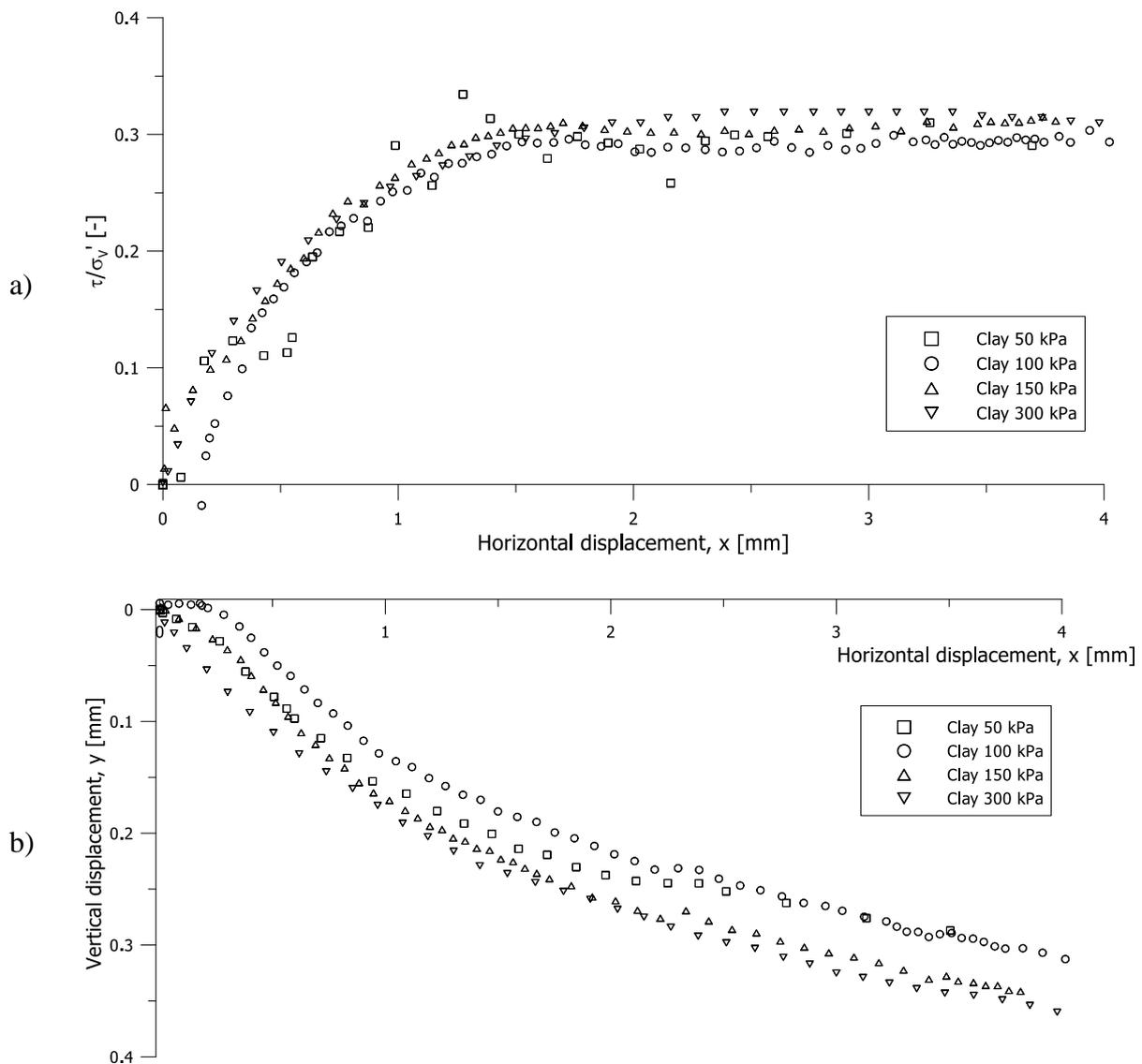
376 Figure 9. 1-D compression curves for kaolin reconstituted from slurry and kaolin mixed with
 377 CS. a) void ratio against effective stress, b) effective stress against vertical strain and (c)
 378 hydraulic conductivity upon oedometric compression.

379 For completeness, also the values of the hydraulic conductivity of the sample of sand
 380 grouted with CS (already presented in Figure 5c) is reported and the hydraulic conductivity of
 381 CS only (previously reported in Figure 4 as NaCl -1h -1w – H2O). It is interesting to note that
 382 also the sample of sand grouted with CS shows an hydraulic conductivity one order of
 383 magnitude lower than the sample of kaolin clay only and just one order of magnitude higher
 384 than CS only.

385 *Direct shear tests*

386 Figure 10 shows the results of a shear test performed on kaolin clay reconstituted from
 387 slurry and consolidated to 50, 100, 150 and 300 kPa (data from Pedrotti (2018) and Galvani
 388 (2003))

389 In Figure 10a the horizontal displacement versus the t/S_v' is reported and in Figure 10b
390 the volumetric change in terms of horizontal versus vertical displacement is shown. For the
391 four vertical stresses investigated the shear behaviour is similar. All the samples exhibit a
392 compressive behaviour and a very similar ultimate shear stress/effective vertical stress ratio.
393 For the ultimate conditions the friction angle, $\phi'_{ultimate}$, was computed to be 16° with a drained
394 cohesion equal to 2 kPa. No peak conditions were considered.



395 Figure 10. Direct shear tests on Speswhite kaolin samples at different effective vertical

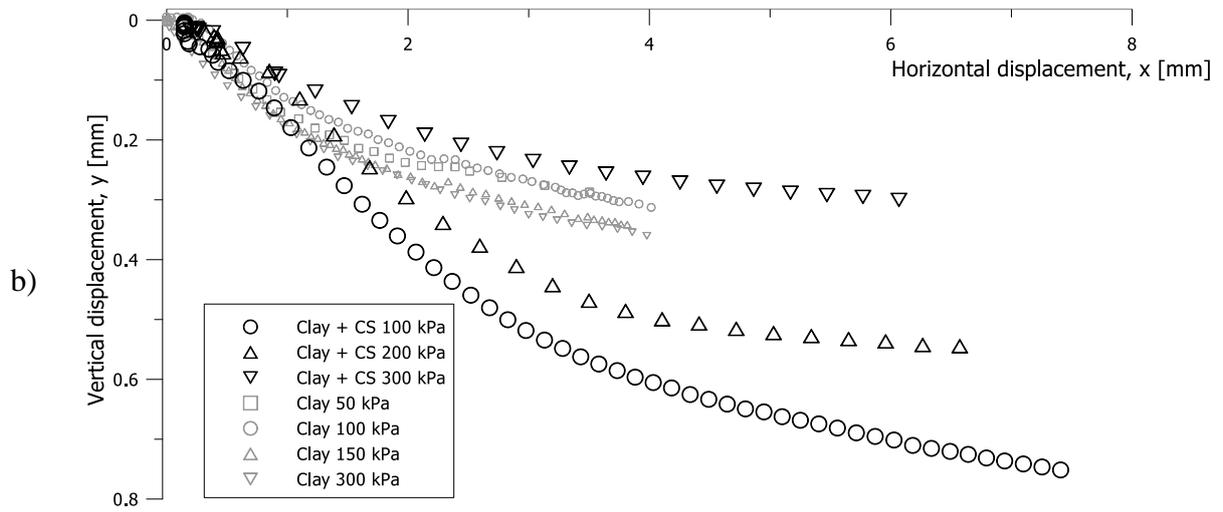
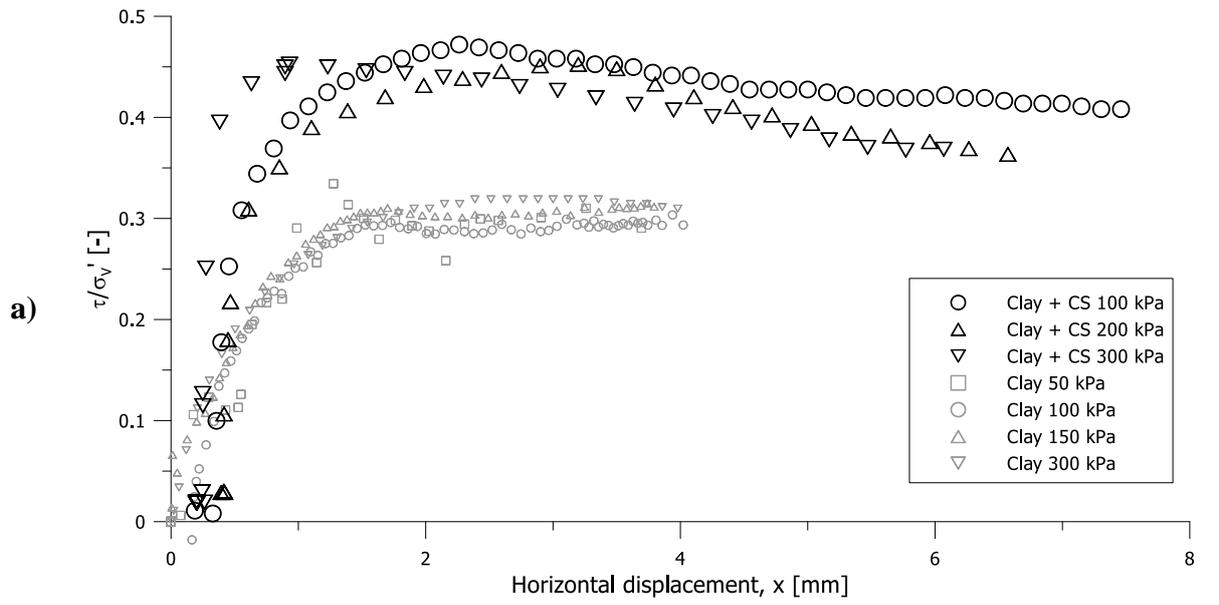
396 stresses. a) horizontal displacement versus the shear stress/effective vertical stress ratio, b)
397 volumetric change.

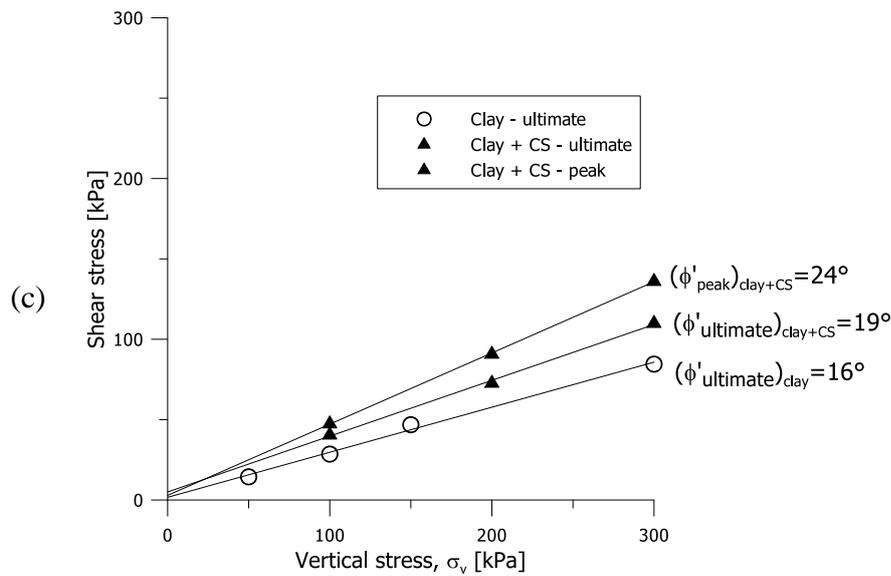
398 Figure 11 shows data from direct shear tests on samples of kaolin clay mixed with CS for
399 values of vertical stress equal to 100, 200 and 300 kPa. All shear tests were conducted under
400 saturated conditions. As reference, the data corresponding to the shear test on kaolin only
401 (already showed in Figure 10) are reported in grey.

402 Figure 11a shows the horizontal displacement versus t/S'_v . The three samples mixed
403 with CS exhibit a similar behaviour, showing a t/S'_v peak value of about 0.45 and an
404 ultimate value of about 0.37. Moreover, the sample consolidated to 100 kPa shows a slightly
405 higher ultimate t/S'_v than the samples consolidated to 200 and 300 kPa. The samples mixed
406 with CS show a t/S'_v at ultimate conditions about 30% higher than the shear stress/effective
407 vertical stress ratio of samples of kaolin clay only.

408 Figure 11b shows the horizontal displacement versus the vertical displacement. All the
409 three samples mixed with CS exhibit a compressive behaviour. Vertical compression
410 decreases as the consolidation stress increases. Upon shearing, the CS mixed samples showed
411 to be more compressible than samples prepared with kaolin clay only. Indeed, the vertical
412 deformation of clay-only and clay mixed with CS samples are comparable only for the case of
413 samples consolidated to 300 kPa.

414





415 Figure 11 Direct shear test on Speswhite kaolin and CS samples at different vertical stress. a)
 416 horizontal displacement versus the shear stress/vertical stress ratio, b) volumetric change and c)
 417 peak and ultimate shear envelopes .

418 In Figure 11 the shear envelope for the ultimate condition of samples of kaolin clay only,
 419 and the ultimate conditions and peak conditions for the clay mixed with CS are compared. For
 420 peak conditions the clay and CS mixed samples showed a friction angle $\phi'_{peak}=24^\circ$ and a
 421 drained cohesion of 3 kPa. For ultimate conditions, these samples showed a friction angle
 422 $\phi'_{ultimate}=19^\circ$ and a drained cohesion of 5 kPa.

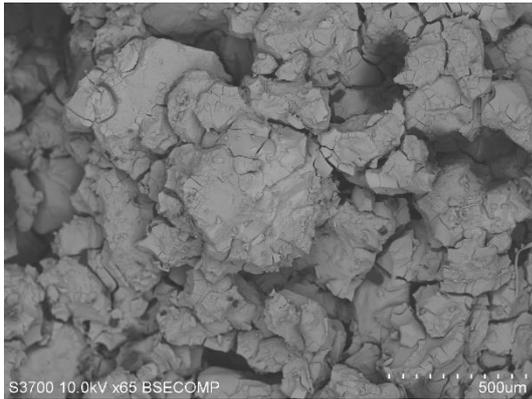
423 Mixing with CS increased the friction angle of kaolin clay in terms of both peak and
 424 ultimate shear strength. On the other hand, no increase in drained cohesion was recorded,
 425 suggesting that no relevant particle bonding due to the addition of CS was created in these
 426 samples.

427 5. MICROSTRUCTURAL INVESTIGATION

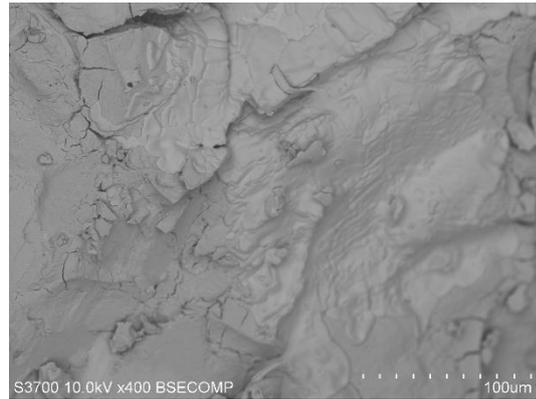
428 A microstructural investigation was carried out on both samples of Leighton Buzzard

429 sand grouted with CS and samples of Speswhite kaolin mixed with CS. Grouted sand was
430 imaged by means of SEM analysis and X-CT scan. SEM analysis was used for imaging and
431 for element analysis samples of clay mixed with CS.

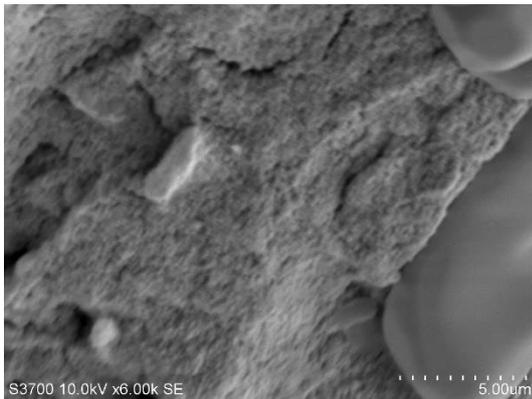
432 **5.1 Sand grouted with CS**



a) magnification factor of 65



b) magnification factor of 400



c) magnification factor of 6000

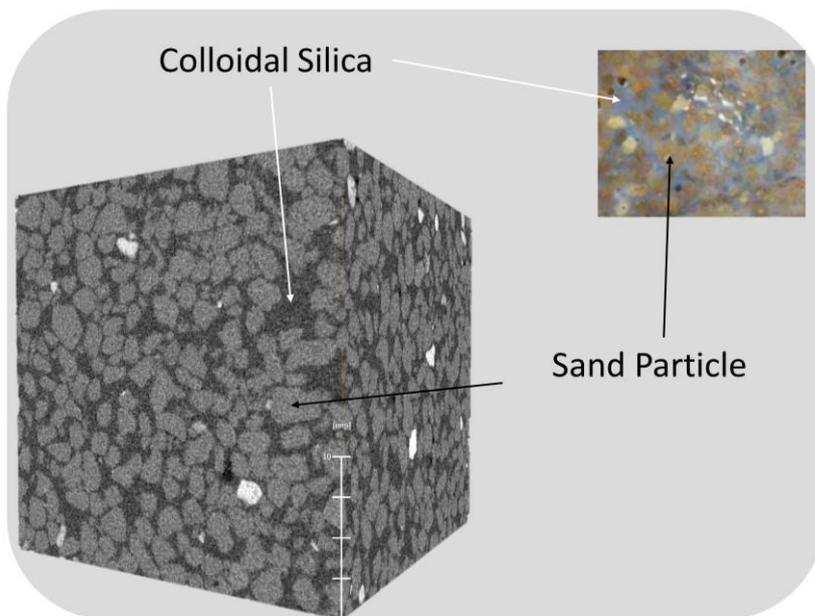
433 **Figure 12. SEM images of Leighton Buzzard sand mixed with CS**

434 Fig 12 shows the SEM image of a sample of Leighton Buzzard sand that was permeated by
435 CS for three different magnification factors at the same location. The sand particles are not
436 visible, they appear to be completely surrounded by a continuous matrix of CS (Figure 12a).
437 The desiccation cracks visible in the CS are due to the oven drying process, which is
438 necessary for imaging in the SEM. At the highest magnification (x6000, Figure 12c), the CS

439 clusters are clearly visible on the surface, and the sand particles are still not visible beneath
440 the coating of colloidal silica, which coats the sand particles in a continuous cover.

441 In Figure 13 a section of a 3D reconstruction of a sample of sand grouted via permeation
442 with CS is shown. This sample was prepared for shear testing. After curing, but before
443 shearing, the sample was scanned in the X-CT apparatus. No drying was required to be
444 carried out before scanning.

445 As already demonstrated by the SEM images (Figure 12), CS fills most of the voids
446 present between the sand particles (shown by the dark grey in Figure 13). Air voids would
447 appear black on the image. The whole porosity of the sample now depends only (excluding a
448 few remaining bubbles of air) on the porosity of the CS matrix. The CS matrix itself is not
449 visible as the pore size is at least 2-3 orders of magnitude smaller than the maximum
450 resolution of the scanner (~5 microns for beam settings used). It is evident that no pores
451 remain in the grouted sand sample that are due to the original sand structure.

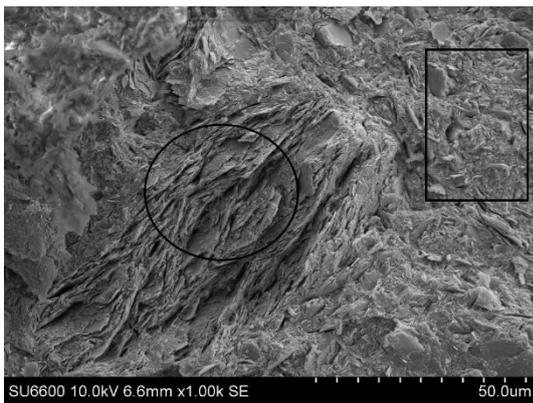


452

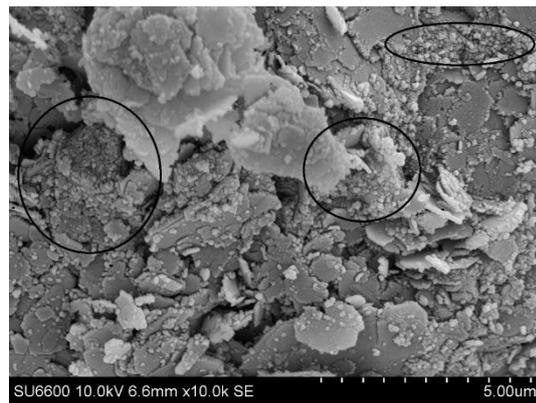
453 Figure 13. X-CT image of sand grouted with CS

454 **5.2 Clay mixed with CS**

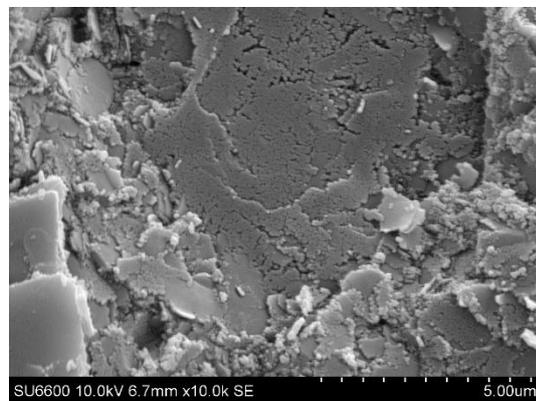
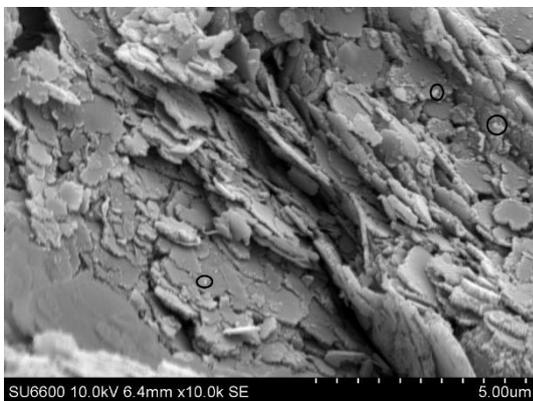
455 Figure 14a shows the SEM image of a sample of kaolin mixed with CS. This sample was
456 consolidated to 1000 kPa and then oven-dried (at 105°C) for at least 24h. The image has a
457 magnification factor of 1000 and the full-scale is approximately 0.1 mm (100 µm). Figure 14a
458 shows a highly heterogeneous pattern of particles of kaolin and a matrix of CS gel. Two
459 distinct areas of the image are highlighted: in the centre (the circle in Figure 14a) it appears
460 that only kaolin particles are present characterised by their hexagonal platy appearance
461 (Mitchell and Soga, 2005) whereas in the surrounding region (e.g. the rectangle in Figure 14a)
462 kaolin particles appear isolated and submerged in the colloidal silica matrix.
463



a) Magnification 1k – Energy 10kV.

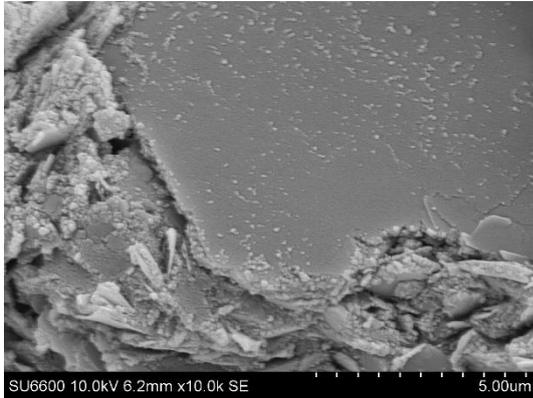


b) Magnification 10k – Energy 10kV.



c) Magnification 10k – Energy 10kV.

d) Magnification 10k – Energy 10kV.



e) Magnification 10k – Energy 10kV.

464 Figure 14. SEM image on sample of kaolin and CS consolidated to 1000 kPa.

465 Figure 14b, Figure 14c, Figure 14d and Figure 14e show SEM images from the same
466 sample but with a magnification factor of 10,000 and a full-scale of about 10 μm .

467 Figure 14b shows a SEM image focused on a region where the kaolin particles prevail. A
468 few clusters of CS particles (highlighted in the Figure) are still visible. Isolated clusters of CS
469 particles can also be identified on kaolin particles as small spheres in the image. It does not
470 appear that the clay particles and the CS matrix create any kind of interconnected
471 configuration.

472 In the region shown in Figure 14c only kaolin particles are present. Despite the fact that
473 the sample was prepared by mixing kaolin powder with CS, it is clear that the CS particles do
474 not fill the void space present within the structures formed by the kaolin particles, hence,
475 mixing between the CS matrix and the kaolin particles has not occurred at this scale. A few
476 small clusters of CS particles are present in Figure 14c (highlighted by the small circles)
477 however, they are sparse and appear to be negligible in terms of the microstructural
478 configuration.

479 By contrast, to the clay-rich area, the SEM image in Figure 14d shows a region where CS
480 is mainly present: only CS particles are apparent in the image centre, and no kaolin particles
481 are visibly submerged in the CS matrix. Throughout the whole sample, regions of kaolin
482 particles where CS was poorly present alternated with regions of CS, in which kaolin particles
483 seem to be isolated or not present at all.

484 Finally, Figure 14e is focused on a very large particle of kaolin, on which particle surface
485 element analysis was carried out in order to investigate whether CS particles coated the clay.
486 Elemental analysis was performed at 5 different points on the clay particle surface and then
487 compared with a similar analysis carried out on a particle of kaolin clay that was not exposed
488 to CS. The average values of the ratio Si/Al for the two different samples are reported in
489 Table 1. For the sample mixed with CS the amount of silica (Si) present on the surface is
490 higher than for the sample of kaolin only. This suggests that, despite not being visible in the
491 SEM images, some CS particles must be present as a coating on the kaolin particle. It is worth
492 noting that similar results were highlighted by Coe et al. (2016) in their study on the effect of
493 nano CuO on kaolin properties.

494 Table 1. Element analysis on sample of kaolin particles (values are weight [%] ratios).

	Si/Al
Kaolin	1.004
Kaolin + CS	1.725

495

496 **6. MICROSTRUCTURAL INTERPRETATION OF THE MECHANICAL**

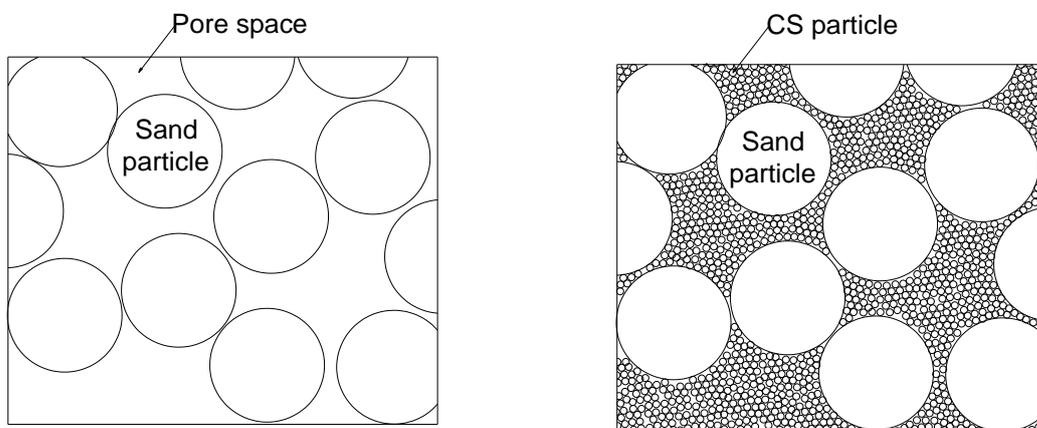
497 **INTERACTION BETWEEN SOIL AND COLLOIDAL SILICA**

498 **6.1 Sand grouted with CS**

499 To support the macroscopic tests with the microstructural information in Figures 12 and

500 13, a comparison of the conceptual model for particle configuration in sand-only and sand
501 grouted with CS is reported in Figure 15. In the oedometer tests, upon compression, the
502 presence of CS reduced the overall volumetric deformation exhibited by grouted sand samples
503 with increased stiffness over the range of stresses investigated. Considering compression at
504 the microstructural scale, upon vertical compression, particles in ungrouted samples are free
505 to achieve a denser configuration by rearranging into the pore space. By comparison, the
506 rearrangement of sand particles in the grouted samples is inhibited by the presence of the
507 colloidal silica, which occupies any accessible pore space around the sand particles. Hence,
508 the presence of CS in the pore space, not only generates a denser sample but also a stiffer one,
509 in agreement with the macroscopic tests.

510 Considering the microscopic scale, increased peak shear strength occurs because the
511 continuous matrix of CS that surrounds the sand particles provides a weak bonding between
512 particles, which macroscopically generates some cohesion until the CS matrix is broken along
513 the shear plane. After failure, the presence of the CS prevents compression upon shearing,
514 forcing a dilative behaviour (Figure 7), which in turn increases the peak resistance. However,
515 once the strength of the CS matrix is overwhelmed the sand particle-to-particle friction
516 controls the ultimate conditions.



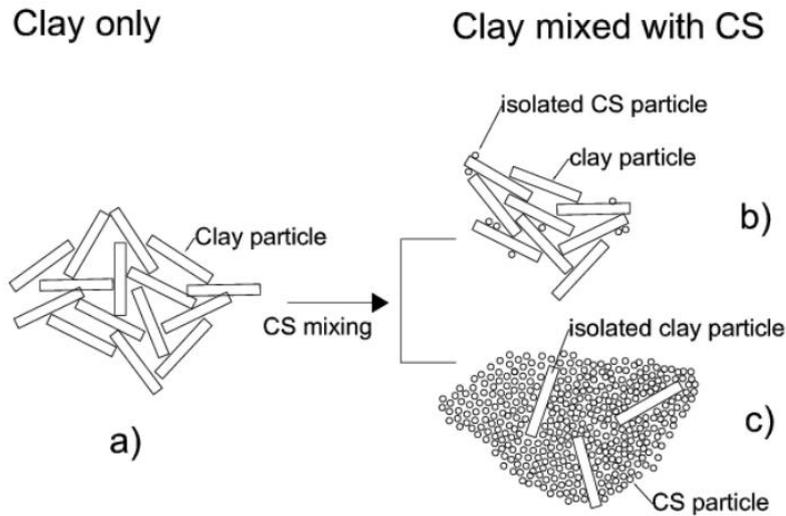
a)

b)

517 Figure 15. Conceptual model for particle configuration in sand grouted with CS. a) Not
518 grouted sand and b) grouted sand

519 **6.2 Clay mixed with CS**

520 To understand how the microstructural information can inform the results of the
521 macroscopic tests, a simplified sketch is shown of an ungrouted clay (Figure 16a) and of the
522 two different characteristic regions identifiable in the SEM image: sub-regions where kaolin
523 particles dominate (Figure 16b) and sub-regions where a matrix of CS particles dominates
524 (Figure 16c). In the macroscopic test, upon vertical compression, the clay samples mixed with
525 CS showed reduced volumetric deformation, with increased stiffness only at low stresses, and
526 above 100kPa the compressibility of the clay-CS samples became similar to that of the clay
527 only samples. In the sub-regions where kaolin particles dominate (Figure 16b) the clay
528 particle configuration is similar to the arrangement in clay-only samples, however, since the
529 pore water is shared with the sub-regions where CS dominates, the clay particle structure is
530 denser and therefore stiffer. Similarly, in the CS sub-regions (Figure 16c) the density is higher
531 than a sample with colloidal silica particles only, again because of the reduced amount of
532 water, as water is shared with the sub-regions of clay particles. Both sub-regions are therefore
533 expected to be at higher density and consequently exhibit a stiffer behaviour. Upon vertical
534 compression, as the vertical stress increases (exceeding 100 kPa) the difference in density
535 (and water content) between the clay-CS and the clay-only samples decreases, until the
536 compressibility of both become similar (Figure 9a). Such behaviour suggests that between the
537 two sub-regions, the regions dominated by the clay particles are controlling the macroscopic
538 compressive behaviour.



539

540 Figure 16. Particle configuration for kaolin mixed with CS samples. a) clay only , b) clay
541 mixed with CS where kaolin particles dominate and c) clay mixed with CS where CS particles
542 dominate

543 The micro-mechanisms controlling the shear strength of clays are not well understood,
544 and are therefore difficult to discuss here (Morgenstern and Tchalenko, 1967, Sridharan and
545 Venkatappa Rao, 1973, Burland, 1990, Tarantino and Tombolato, 2005). At a macroscopic
546 scale, the mixing of CS increased the peak and ultimate shear strength of the clay mixture but
547 did not have any effect on the drained cohesion. One may speculate that, in terms of shear
548 strength, the presence of sub-regions of CS at high density hampers the formation of a shear
549 surface, resulting in an increase in the energy required for failure (i.e. increasing the peak
550 shear stress). Furthermore, the silica to silica contacts would be expected to have higher

551 frictional resistance than the kaolin to kaolin contacts (Morrow et al., 2000) which explains
552 why the ultimate conditions of the clay-CS mixtures remain higher than the clay only samples
553 (in contrast to the grouted sands). Finally as suggested by the SEM pictures (Figure 14), CS
554 does not provide any bonding between clay particles and therefore no increase in cohesion
555 should be expected.

556 **9. CONCLUSIONS**

557 This paper has presented the drained stress-strain behaviour of CS gel, sands grouted with CS
558 and clay mixed with CS. Observations of the microstructural properties of the CS grouted
559 sand and clays have enabled the development of conceptual material models that can explain
560 the macroscopic observations.

561 For CS grouted sands:

- 562 • the presence of CS reduces the overall volumetric deformation during compression
563 and increases the stiffness, when compared with sand-only. This occurs because the
564 colloidal silica gel occupies all the accessible pore space, thus inhibiting the
565 rearrangement of particles upon compaction. This generates a sample that is both
566 denser and stiffer.
- 567 • the presence of CS reduces the overall volumetric deformation and enhances the peak
568 shear strength. This occurs because CS provides a weak bonding between sand
569 particles, generating cohesion. Once this matrix is broken, the presence of CS in the
570 pore space forces a dilative behaviour increasing the peak resistance. After failure of
571 the CS bonds, the sand particle-to-particle friction controls the ultimate conditions.

572 For CS clay mixtures:

573 • The presence of CS reduces the volumetric deformation and increases the stiffness for
574 low values of stress (~100kPa). This occurs because the CS grouted clay maintains
575 distinct sub-regions of kaolin and of CS, these sub-regions compete for pore water
576 resulting in a denser and stiffer material. This difference in water content decreases as
577 compression increases and water is expelled.

578 • The presence of CS increases both the peak and the ultimate shear strength but does
579 not effect the drained cohesion. This may occur because the sub-regions of CS impede
580 the formation of a shear surface, thus increasing the peak shear stress, and the silica to
581 silica contacts have a higher frictional resistance than the kaolin to kaolin contacts
582 increasing the ultimate shear-strength. Finally, since the CS is not incorporated into
583 the bonds between clay particles, no increase in cohesion is observed.

584 CS is well known for its low hydraulic conductivity and application for controlling fluid flow
585 in porous media. Its undrained behaviour has been previously reported suggesting its
586 application for short-term stability problems. This paper illustrates for the first time that even
587 under drained conditions CS can provide mechanical improvement; for grouted sands
588 increasing further the stiffness beyond that of sands and enhancing the peak friction angle.
589 Thus while still having a very low hydraulic conductivity ($\sim 10^{-10}$ m/s), typical of intact clay.
590 This paper also presents results on clays mixed with CS which have the potential to be novel
591 materials. Their application could be deployed in environments where not only hydraulic
592 containment is critical but where reduced deformation and enhanced resistance to shearing
593 would be beneficial, for example in landfill capping or in the outer fill layers of embankments
594 designed to minimise internal seepage and infiltration.

595 **ACKNOWLEDGEMENTS**

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598 Storage Solutions for Nuclear Waste Inventories (DISTINCTIVE).
599

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