

1 **Development of an extended mean value engine model for predicting** 2 **the marine two-stroke engine operation at varying settings**

3 Gerasimos Theotokatos^{a,1}, Cong Guan^{b,1,*}, Hui Chen^b, Iraklis Lazakis^a

4 a Department of Naval Architecture, Ocean & Marine Engineering, University of Strathclyde, 100
5 Montrose Street, Glasgow G4 0LZ, UK

6 b Key Laboratory of High Performance Ship Technology of Ministry of Education, School of Energy
7 and Power Engineering, Wuhan University of Technology, 1178 Heping Road, Wuhan 430063, China

8 * Corresponding author.

9 1 These authors contributed equally to this work.

10 **Abstract** This study focuses on the development of an extended MVEM capable of predicting the
11 engine performance parameters (thermodynamic, flow and mechanical) of two-stroke marine engines
12 at varying settings of injection timing and turbine area. The extension employed mapping of a number
13 of the engine parameters carried out based on a zero-dimensional model. Both the zero-dimensional
14 and the mean value engine models were developed in MATLAB/Simulink environment following the
15 same modular approach and their accuracy was validated against experimental data from shop trials.
16 Subsequently, the zero-dimensional model was used for engine parametric simulation by changing the
17 start of fuel injection and the turbocharger turbine area. By analyzing the derived results, the
18 relationships between the investigated engine parameters were established and the appropriate
19 corrections were applied in the MVEM. The extended MVEM was benchmarked against the
20 zero-dimensional model and MVEM at steady and transient conditions and the derived results were
21 analysed and discussed revealing the advantages and limitations of the investigated modelling
22 approaches. Based on the obtained results, the proposed extension methodology improves the MVEM
23 prediction capability without considerably increasing the complexity and the execution time and
24 therefore, it can be employed for the engine performance prediction in control system design

- 1 investigations overcoming limitations of the MVEM.
- 2 **Key words** Extended mean value engine model; Zero-dimensional model; Marine two-stroke diesel
- 3 engine simulation; Varying engine settings; Models benchmarking.

1 **1. Introduction**

2 The large two-stroke marine diesel engine is widely used for propulsion of the vast majority of
3 vessels in the last few decades due to its high efficiency and reliability. In order to attain improved fuel
4 efficiency and achieve environmentally cleaner operation, engine manufacturers have developed
5 electronically controlled versions of marine diesel engines [1,2]. In these, the computer-controlled
6 high-pressure hydraulic systems with advanced sensors, actuators and control valves have been used to
7 replace the camshaft that exists in traditional engine versions for adjusting the fuel injection timing and
8 exhaust valve opening/closing. Additionally, turbochargers with variable geometry turbines and exhaust
9 gas waste gate valves have been applied for increasing the engine efficiency throughout the whole
10 engine operating envelope especially at low load conditions. Furthermore, recently turbocharging
11 systems with two-stages have been investigated for implementation in marine engines in order to
12 simultaneously increase efficiency and reduce NO_x emissions [3,4]. For reducing SO_x emissions, two
13 alternative measures have been proposed and used [5]; these include either the engine operation by
14 using a low sulphur fuel or the installation of a scrubber in the engine exhaust pipe. Low sulphur heavy
15 fuel oil (LSHFO), marine gas oil (MGO) and natural gas stored in liquefied form (LNG) are the
16 alternative proposed for immediate implementation by the maritime industry stakeholders, whilst other
17 alternative fuels including methanol, ethanol and hydrogen are proposed for future usage.

18 As the development of a large two-stroke marine diesel engine is time consuming and costly
19 procedure, various engine modelling techniques have been used for investigating the engine
20 steady-state performance and transient response as well as for testing the alternative design of the
21 engine systems. In the current literature, different model types have been reported to predict engine
22 performance under various conditions. They are categorized as transfer function models [6], cycle
23 mean value models [7-15], zero- or one-dimensional models [16-25] and computational fluid dynamic

1 models [26,27]. As the modeling complexity increases, i.e. from transfer function models to
2 computational fluid dynamic models, the representation of the engine working process is improved, but
3 at the same time a greater execution time and amount of input data are required, so that the model
4 becomes more laborious. As the MVEMs are a compromise between the simpler transfer function
5 models and the more detailed zero- or one-dimensional models, these are widely used in investigations
6 that include the development and design of the engine control systems, where a fast execution time and
7 model simplicity are needed [6,28,29]. The MVEMs employ a limited amount of input data and
8 reasonable execution time whilst predicting the engine behaviour with adequate accuracy, whereas their
9 drawbacks include their inability to predict the in-cycle variation (e.g. per degree of crank angle) [6]
10 and as a result the engine brake specific fuel consumption (BSFC) and efficiency under different
11 settings (e.g. varying start of injection timing, turbine area and exhaust gas bypass, etc.). In the cases
12 where in-cylinder parameters are required, the zero- or one-dimensional models can be used. For the
13 case where the estimation of engine performance at varying settings is of interest [30], the
14 zero-dimensional models seem to be the appropriate option. Furthermore, for adequately predicting
15 emissions, two-zone or multi-zone combustion models are required along with the appropriate
16 emissions kinetics mechanisms, which further increase the model complexity and the running time
17 [31,32], thus rendering the zero-dimensional models application quite challenging for cases that require
18 simulation of engine transients for long periods, varying engine settings and control system design [6],
19 for example, ship maneuvering predictions [33] or system components control [34].

20 Theotokatos [12] reported the MVEM categories and the development of a modular MVEM in
21 MATLAB/Simulink environment. The advantages and drawbacks of two different approaches were
22 also discussed based on previously published data. Dimopoulos et al. [35] included the diesel engine
23 models of different levels of accuracy and complexity in the component model library of an integrated

1 marine energy system simulation platform called COMplex Ship Systems MOdelling and Simulation
2 (COSSMOS), providing the users with the flexibility to select the desired ones according to the
3 intended application. Nikzadfar et al. [36] introduced an extended MVEM for control-oriented
4 modeling of diesel engines transient performance and emissions by utilizing Artificial Neural Networks
5 (ANN) to mimic the engine cycle thermodynamic model. The applied neural network technology
6 requires a large number of data sets to capture the in-cylinder process with desired level of accuracy,
7 and besides that the amount of data increases significantly if emissions are to be modelled. Nielsen et al.
8 [34] simplified the original mean value engine model by removing the non-dominant dynamics and
9 developed a control-oriented model of the oxygen fraction in the scavenge air manifold. This model
10 can be used effectively for the engine control system design but cannot provide the engine performance
11 predictions at varying engine settings as it still has to confront the mean value engine model limitations.
12 Fadila and Charbel [37] developed an extension of MVEM and in-cylinder single zone model for high
13 speed four-stroke diesel engine dedicated for Hardware in the Loop (HIL) applications. The model only
14 includes the air system, combustion system, exhaust system and fuel system without considering the
15 turbocharger and propeller, which means it cannot be regarded as a full engine model. In addition, a
16 quad core Real Time Processor Computer (RTPC) is needed in order for the in-cylinder extended
17 model to be run in real time. Extending the modular MVEM reported in Theotokatos [12], Baldi et al.
18 [38] proposed a combined MV-0D approach applied for a large marine four-stroke diesel engine, where
19 the zero-dimensional model was used for representing the closed cycle of one engine cylinder and the
20 mean value engine model employed for simulating the open part of the cycle as well as for the other
21 engine components. Nevertheless, the zero-dimensional model needs to be called at each time step
22 resulting in long execution time particularly when the engine transient simulation for a long time period
23 is considered. Based on a similar modelling approach, Tang et al. [39] improved further the hybrid

1 engine model calculation speed by estimating the cylinder exhausting and scavenging processes as
2 linear functions and abandoning engine cylinder cycles at certain intervals. This hybrid model can be as
3 fast as the MVEM for the steady state conditions in that the boundaries of every cylinder cycles remain
4 the same, however the calculation speed is improved at the expense of the engine performance
5 prediction precision during the dynamic process.

6 Although hybrid modelling approaches offer an acceptable execution time, the engine control
7 systems design applications require simpler models as even limited zero-dimensional modelling
8 introduces complexity [6,34]. In order to capture the engine performance at varying settings with
9 reasonable execution time, an effective approach is to use a MVEM coupled with lookup tables or
10 response surfaces representing the engine cylinders parameters variation, which can be derived from
11 the zero-dimensional model parametric runs. In this respect, the advantages of the MVEMs, i.e. the
12 modularity and low execution time, along with the more accurate prediction of engine performance
13 parameters at varying settings that zero-dimensional models provide can be exploited. A similar
14 modelling approach was used in Livanos et al. [40,41] for designing and testing control schemes for an
15 ice-class tanker propulsion plant system. The used engine model included lookup tables derived by
16 using a calibrated zero-dimensional model parametric runs, and the in-cylinder engine performance
17 parameters were estimated by using linear interpolation. However, as this is a case-dependent approach
18 of modelling marine engines, an extended MVEM based on analytical expressions can provide an
19 additional advantage and more flexibility as it could capture both the flow and mechanical parameters
20 variation. This is a novel element of the present study as there is not reported a general approach for
21 extending the MVEM by applying the corrective formulae to the respective parameters. As the
22 electronically controlled versions of marine engines become more popular and new components that
23 require control such as waste gate exhaust valves, variable geometry turbine, exhaust gas recirculation

1 (EGR) and turbocharger cut-out valves are used nowadays, this extended mean value engine model is
2 an alternative for providing both adequate accuracy and fast running times with reduced modelling
3 complexity. Besides that, the extended MVEM can be used to predict with fidelity the engine operation
4 under different conditions without requiring re-calibrations of the model parameters for representing
5 engine with varying settings.

6 The proposed extended modelling approach was employed herein to investigate a large two-stroke
7 engine performance prediction with varying start of injection (SOI), turbine area and exhaust gas
8 bypass settings. The model was benchmarked against the zero-dimensional model and MVEM, and the
9 simulation results were used to discuss its advantages and drawbacks against the other two modelling
10 approaches.

11 **2. Models description**

12 The zero-dimensional and mean value engine models used in this work were previously developed
13 by the authors in MATLAB/Simulink environment following a modular concept. The zero-dimensional
14 model has been described in detail in Guan et al. [30] where it was used for the prediction of a two-stroke
15 large engine performance at slow steaming conditions. The MVEM was described in detail in
16 Theotokatos [12]. The models structure is shown in Fig. 1. Each part of the engine is represented by a
17 block that exchanges variables with the adjacent blocks through the appropriate connections. The models
18 use a number of elements including flow elements, receivers, mechanical elements (shaft and load) and
19 control element (PI governor). For both models, the scavenging and exhaust receivers are considered to
20 be flow receiver elements (control volumes), whilst the turbocharger components (compressor and
21 turbine) are represented as flow elements. Fixed fluid elements of constant pressure and temperature are
22 used for modelling the engine boundaries. Shaft elements are used for calculating the engine crankshaft

1 and turbocharger shaft rotational speeds. The engine governor element, which is used to adjust the engine
2 fuel rack position, is considered to be of the proportional-integral (PI) type and incorporates the
3 appropriate fuel rack limiters, whereas the propeller element is used for calculating the propeller torque.
4 The thermodynamic properties of the working medium either air or gas are considered to be functions of
5 temperature, pressure and fuel-air equivalence ratio [42].

6 The flow elements use as input variables the pressure, temperature and the properties of the
7 working medium contained in the adjacent elements (flow receiver(s) or fixed fluid), whereas their
8 output variables include the mass and energy flow rates entering and exiting the flow element as well
9 as the absorbed (for the case of compressor) or produced torques. The mass and energy flows are
10 provided as input in the adjacent flow receiver elements, whereas the torques are required as input in
11 the shaft elements. The output of turbocharger shaft element, i.e. the turbocharger speed, is provided to
12 the compressor and turbine elements. The output of the crankshaft element includes the engine and
13 propeller rotational speeds; the former is supplied as input to the engine cylinders and engine governor
14 elements, whereas the latter is advanced in the propeller element.

15 The difference between the zero-dimensional model and MVEM lies in the cylinder block. The
16 zero-dimensional model cylinder block is more comprehensive as it simulates the closed cycle process
17 (compression, combustion and expansion) by using a one-zone approach, and the scavenging process by
18 employing a two-zone approach [30]. The zero-dimensional model cylinder block uses as input the
19 scavenging ports and exhaust valves profiles as well as the fuel variable injection timing. On the
20 contrary, the MVEM cylinder block is simpler and the flow is calculated by using an equivalent orifice
21 approach whereas the cylinder performance parameters are calculated by using algebraic equations.

22 **2.1 Zero-dimensional model**

1 The cylinders are modelled as flow receiver elements using either the open or closed
2 thermodynamic systems consideration depending on their operating phase (open cycle or closed cycle,
3 respectively). For calculating the cylinder working fluid thermodynamic parameters, the mass and
4 energy conservation laws as well as the ideal gas state equation in each considered control volume zone
5 are used [43-45]. Assuming that the system can be characterized by using the temperature, mass,
6 pressure and equivalence ratio, the one zone model employs three first-order differential equations for
7 calculating the temperature, the mass and the burnt fuel fraction along with the ideal gas equation for
8 calculating the pressure and algebraic equations for estimating the working fluid properties. The two
9 zone scavenging model (the first zone includes air whereas the second zone includes exhaust gas)
10 employs six first-order differential equations for calculating the temperature and the mass for each zone,
11 the burnt fuel fraction of the second zone and the cylinder pressure in conjunction with the algebraic
12 equations for calculating the working medium properties.

13 The Woschni-Anisits combustion model [45] is used for describing the combustion process. This
14 model employs a simple Wiebe function, the shape factor and the combustion duration of which are
15 calculated by using a reference point respective values along with the combustion air/fuel equivalence
16 ratio and engine speed. In this respect, the model constants need to be calibrated for one operating point
17 as the model adjusts the model parameters in other operating points. The Woschni model [46] is
18 employed for calculating the cylinder gas to wall heat transfer coefficient with the default value being
19 as proposed for large two-stroke engine. For the estimation of the engine friction losses, an equation
20 providing the engine friction mean effective pressure as a function of the cylinder maximum pressure
21 and the average piston speed is used [47]. When all the engine cylinders are considered to be identical,
22 the only input parameter that varies is the phase angle of each cylinder. The individual cylinders
23 interact via the intake and exhaust manifolds. The torque and inertia of each cylinder are summed up

1 and provided as input for the calculation of engine crankshaft rotational speed. The combustion model
2 constants in the zero-dimensional model are given in Table 1.

3

4 **2.2 Mean value engine model**

5 The engine cylinders block is regarded as a flow element in the MVEM. The air mass flow rate
6 entering the cylinder is calculated considering the equivalent of two consecutive orifices, each one
7 representing the cylinders scavenging ports and exhaust valve. The mass flow rate of the exhaust gas,
8 exiting the engine cylinders, is estimated by using the continuity equation adding the mass flow rates of
9 the air entering the engine cylinders and the injected fuel. The latter is calculated using the number of the
10 engine cylinders, the engine rotational speed and the injected fuel mass per cylinder and per cycle, which
11 is regarded as a function of engine fuel rack position. A critical parameter for the MVEM set up and
12 calibration is the fuel chemical energy proportion in the exhaust gas (ζ), which represents the working
13 medium energy flow change across the cylinder (increase of the energy flow of the air entering the
14 cylinders) as fraction of the fuel energy released within the combustion chamber [6,45]. Thus, the
15 parameter ζ can be used to calculate the energy flow rate exiting the engine cylinders element according
16 to the following equation:

$$17 \quad \dot{m}_e h_{e_cyl_d} = \dot{m}_a h_{a_cyl_u} + \zeta \eta_{comb} \dot{m}_f H_L \quad (1)$$

18 Previous studies [6,45] showed that the parameter ζ can be approximated as a linear function of
19 the engine brake mean effective pressure (BMEP) [48]:

$$20 \quad \zeta = k_1 + k_2 BMEP \quad (2)$$

21 Typically, ζ is calculated and calibrated for each load using available engine performance data
22 measured during the engine trials or provided by the engine manufacturer [49]. As the parameter ζ is
23 calibrated for the specific engine settings, its re-calibrations are required for varying SOI settings. To

1 overcome this limitation, the extension of the MVEM is proposed herein.

2 The indicated mean effective pressure is calculated as the product of the rack position, the
3 engine maximum indicated mean effective pressure and the combustion efficiency, which, in turn,
4 is regarded as a function of engine air to fuel ratio [44]. The friction mean effective pressure that
5 includes all the engine mechanical losses is considered a function of the indicated mean effective
6 pressure and the engine crankshaft speed according to [6,12]. The engine brake mean effective
7 pressure is calculated by subtracting the friction mean effective pressure from the indicated mean
8 effective pressure, whereas the engine torque is calculated using the brake mean effective pressure
9 and engine cylinders displacement volume [43].

10 **3. Models validation**

11 The two-stroke marine diesel engine MAN Diesel & Turbo 7K98MC steady state operation was
12 simulated by using both the zero-dimensional model and the MVEM developed in MATLAB/Simulink
13 environment. The engine is of the cross-head type and turbocharged by using the constant pressure
14 turbocharging system concept equipped with three turbocharger units. One air cooler unit is installed
15 downstream each compressor in order to cool the hot compressed air. In addition, three electric driven
16 blowers are used for providing adequate air flow when the engine operates at loads below 40%. Each
17 blower receives the air exiting the respective engine air cooler unit and discharges that to the engine
18 scavenging air receiver. The blowers are activated when the engine air scavenging receiver pressure
19 becomes lower than 1.55 bar, whereas they are switched off for pressure values greater than 1.7 bar.
20 The main engine characteristics as well as the required input data were taken from the engine
21 manufacturer project guide [50]. The engine steady state performance data were obtained from the
22 engine shop trial measurements. The main engine parameters are given in Table 2.

1 Both models were set up by providing all the required input data, which included the engine
2 geometric data, the turbocharger compressor and turbine performance maps, the engine ambient
3 conditions, the constants of engine model equations and the propeller loading. The exhaust valves and
4 scavenging ports profiles as well as the fuel injection timing are needed for the zero-dimensional model.
5 The above required data was collected by using the engine project guide [50], whereas the compressor
6 and turbine maps were available from authors previous work [11]. Initial conditions are also required
7 for the variables that are calculated by integrating differential equations, i.e. the engine/propeller shaft
8 and turbocharger shaft rotational speeds as well as the pressure and temperature of air and gas
9 contained in the engine receivers. The engine three turbocharger units as well as the installed air
10 coolers and blowers were considered to have identical performance.

11 To validate both models simulation runs under steady state operating conditions at 25%, 50%, 75%
12 and 100% of the engine MCR load were performed, as these loads were investigated in the official
13 engine shop tests. The percentage error between the predicted engine performance parameters and the
14 respective shop trial data of both models are given in Table 3. It can be inferred that both models
15 predictions exhibit sufficient accuracy for the high engine load region and the engine operation at low
16 loads (down to 25% load). Therefore, both the engine zero-dimensional model and MVEM are
17 considered to provide satisfactory accuracy and can be used with fidelity for investigating the engine
18 operation.

19 Apart from the simulation of the official shop tests engine operating points, additional simulation
20 runs were conducted at 10%, 15%, 20%, 30%, 35%, 40% and 85% load, respectively. A set of the
21 predicted engine performance parameters including the receivers pressures and temperatures, the
22 temperature of the exhaust gas exiting the engine, the turbocharger speed, the brake specific fuel
23 consumptions corrected at ISO conditions, the total air to fuel ratio, the cylinder maximum pressure

1 and compression pressure (for zero-dimensional model) is presented in Fig. 2. The respective
2 parameter values obtained from the engine experimental data from shop trials for the engine loads 25%,
3 50%, 75% and 100% are also shown in Fig. 2. Despite the fact that the MVEM cannot predict the
4 in-cylinder parameters, the two models seem to provide satisfactory predictions covering the whole
5 engine operating region. The cylinder pressure diagrams derived by using the zero-dimensional model
6 at 25%, 50%, 75% and 100% engine loads are presented in Fig. 3.

7 The minimum value of the brake specific fuel consumption is observed at 85% load, at which the
8 fuel injection timing is the most advanced leading to the most advanced combustion start as it can be
9 deduced from the pressure diagrams shown in Fig. 3, resulting in almost the same cylinder maximum
10 pressure value as the one in 100% load. Due to the activation of the engine blowers, discontinuities in
11 the engine performance parameters variations are observed between 35% and 40% load. The blower
12 activation results in a greater air flow entering the engine cylinders and thus increases the air to fuel
13 ratio. Therefore, the temperature of the exhaust gas contained in the engine receiver and the
14 temperature of the gas exiting turbine reduce approximately 42 K compared to their respective values
15 at 40% load (where the blowers are not activated). In addition, at engine loads 35% and lower, the
16 scavenging air receiver temperature increases around 5 K compared to the respective value of
17 approximately 302 K at 40% load. This is attributed to the blower compression process, which results
18 in air temperature rise. At 25% engine load, the exhaust gas temperature slightly increases due to the
19 fact the engine air to fuel ratio reduces since the compressor operates at lower speed. At 20% engine
20 load and lower, there is a decrease in the exhaust gas temperature, which is attributed to the fact that the
21 fuel amount injected to engine cylinders is reduced more drastically in comparison with the respective
22 air flow rate, and as a result, the air to fuel ratio increases.

1 **4. Extension of MVEM based on zero-dimensional model results**

2 In this section, the extension of the MVEM is described. This involves the following steps:

- 3 a) Mapping of the engine performance parameters based on the zero-dimensional model;
- 4 b) Derivation of the analytical equations for the identified model parameters corrections;
- 5 c) Incorporation of the derived equations to the MVEM;
- 6 d) Validation of the extended MVEM based on various case studies.

7 **4.1 Mapping and analysis of engine performance parameters based on zero-dimensional model**

8 As inferred by Guan et al. [30], the MVEM cannot predict the engine performance at varying
9 settings including changes of the fuel injection timing and the turbine area. Thus, the zero-dimensional
10 model was used to map the engine performance parameters representing the engine operation at varying
11 settings.

12 **4.1.1 SOI change**

13 First, changes of SOI in the range from -2 to $+3^{\circ}\text{CA}$ were considered for various engine loads from
14 10% up to 100% of MCR. The resulting relative changes of the engine performance parameters at each
15 load were calculated using as basis the parameters reference values shown in Fig. 2, which were
16 calculated considering the respective reference fuel injection timing values. The calculated engine
17 performance parameters variations as function of the SOI change and engine load are presented in Fig. 4.
18 Discontinuities can be observed at the region of 40% load owing to the blowers activation. It can be
19 clearly inferred from Fig. 4 that the SOI variation affects in a lesser or a greater extent the engine
20 performance parameters depending on the engine load. The engine parameters that are influenced most
21 significantly at around 40% load region are the scavenging receiver pressure, the cylinder pressure drop
22 (defined as the difference in scavenging and exhaust receivers pressures), the turbocharger speed as well

1 as the cylinder compression pressure. The cylinder temperature at exhaust valve open (EVO) is affected
2 in a lesser extent at this load point, whereas the SOI variation effect on the cylinder maximum pressure
3 remains comparable at all loads. The cylinder pressure drop exhibits a maximum relative change of 15%,
4 whilst the other engine parameters are influenced much less with the observed maximum relative change
5 being at around 6%.

6 In order to show more noticeably the influence of SOI on the in-cylinder pressure, the variation of
7 calculated engine cylinder pressure and heat release rate diagrams as a result of SOI change at 75% load
8 is presented in Fig. 5. From Fig. 5(a), it can be observed that as expected the SOI retard results in a
9 significant reduction of the cylinder maximum pressure accompanied with an increase of the exhaust gas
10 temperature during the expansion phase including EVO point (not shown in Fig. 5). As it is well reported
11 in the literature, this is due to the fact that the SOI retard shifts the combustion process towards the
12 expansion phase (as can be also inferred from Fig. 5(b)), thus a proportion of the fuel energy is added
13 later into the cylinder working fluid. A slight increase of the cylinder compression pressure at 75% load
14 is observed with the SOI retard as shown in Fig. 5(a), which is attributed to the increase of the scavenging
15 receiver pressure (as can be inferred from Fig. 4). This is due to the fact that the SOI retard leads to a
16 higher exhaust gas temperature so that the greater available exhaust gas energy increases the
17 turbocharger speed and eventually the scavenging receiver pressure. The SOI retard also leads to a higher
18 specific fuel consumption as shown in Fig. 7, which will be presented later on in this section, as the lower
19 cylinder maximum pressure and the higher cylinder compression pressure result in a lower engine brake
20 power and therefore, a greater fuel amount is needed for obtain the same brake power. From the
21 preceding discussion it is inferred that the well-known behaviour of the engine parameters caused by
22 varying SOI is confirmed, which indicates that the developed zero-dimensional model can predict the
23 expected parameters trade-offs.

1 The parameter ζ is used in the mean value engine model to represent the fuel chemical energy
2 proportion in the exhaust gas entering the turbine as it was introduced in Equation (1). This parameter is
3 very critical for the model calibration and the prediction of the exhaust receiver temperature and as a
4 result, the other engine performance parameters. The parameter ζ was calculated according to Equation
5 (1) by using the derived zero-dimensional model results, in specific, the energy flow of exhaust gas
6 exiting the cylinder, the energy flow of air entering the cylinder, the combustion efficiency, the fuel mass
7 flow rate and the lower heating value. The relative variation of ζ as function of the SOI change and
8 engine load is presented in Fig. 6. The relative change of the parameter ζ (from the baseline value used
9 for the calculation as presented in Fig. 2) takes values in the range from -0.02 to 0.035 with the SOI
10 change spanning from -2 to +3°CA. It can be inferred that the fuel chemical energy proportion in the
11 exhaust gas at the turbine inlet increases with the SOI retard as well as the overall ζ relative change
12 follows a monotonic trend.

13 By applying surface fitting using the MATLAB curve fitting tool, it was found that the following
14 equation can be used to represent the ζ relative change as function of the SOI change (in degrees CA) and
15 the engine load fraction:

$$16 \quad \Delta \zeta_{SOI} = (k_1 + k_2 \cdot L + k_3 \cdot \Delta SOI) \cdot \Delta SOI \quad (3)$$

17 The obtained R-square value was above 0.99, which indicates that the derived equation successfully
18 captured the involved parameters correlation.

19 The engine brake specific fuel consumption at these settings was also predicted using the
20 zero-dimensional model; its relative change was plotted as function of the SOI change and the engine
21 load as shown in Fig. 7. As explained above, the SOI retard results in the reduction of the maximum
22 cylinder pressure, which consequently, increases the engine brake specific fuel consumption. The BSFC
23 relative change values (from the baseline values predicted by the zero-dimensional model and presented

1 in Fig. 2) are in the range between -0.015 to 0.034 with the SOI change being from -2 to +3°C.A.
2 Similarly to the SOI influence in the relative change of ζ , the BSFC relative change follows a monotonic
3 trend with the fuel injection timing change and the engine loads. In addition, the BSFC is more sensitive
4 to the SOI influence as the engine load increases.

5 The following equation was derived to represent the BSFC relative change as function of the SOI
6 change and the engine load. By comparing Equations (3) and (4), it can be deduced that both ζ and BSFC
7 relative changes follow similar functions with load and SOI change. The calculated R-square value was
8 also above 0.99.

9
$$\Delta BSFC_{SOI} = (k_1 + k_2 \cdot L + k_3 \cdot \Delta SOI) \cdot \Delta SOI \quad (4)$$

10 **4.1.2 Turbine area change**

11 Subsequently, the turbine area change influence on the engine performance parameters was
12 investigated. Simulation runs were performed by applying changes of the turbine area between -20% and
13 +20% at engine loads from 25% to 100% using the zero-dimensional model. The engine performance
14 parameters relative changes at each load were calculated considering the baseline values (shown in Fig.
15 2) derived by using the reference turbine area. The calculated engine performance parameters variations
16 as function of the turbine area change and the engine load are presented in Fig. 8. The performance
17 parameters reference values at each load are calculated from the zero-dimensional model steady state
18 results without blower activation in order to decouple the blower influence.

19 It can be inferred from Fig. 8 that the engine parameters including the scavenging receiver pressure,
20 the cylinder pressure drop and the turbocharger speed are most significantly affected by the turbine area
21 change with an observed maximum relative change at 30% (much higher than the ones of the other
22 parameters). The derived relative change of BSFC is found to be in the range of $\pm 3\%$. At engine loads
23 lower than 75%, the turbine area reduction results in decreasing BSFC due to the considerable increase of

1 the maximum cylinder pressure. However, the reduction of BSFC becomes less distinctive at the
2 ultra-low load region since the turbocharger speed is too low to ensure sufficient air flow. At loads above
3 75%, the reduction of turbine area causes the engine cylinders air flow restriction (as it is deduced by the
4 considerable reduction of the cylinder pressure drop), which has as a result the decrease of the engine
5 efficiency, thus increasing the BSFC.

6 A very detailed description of the engine operation with turbocharger cut-out (equivalent to the
7 reduction of turbine area) can be found in the authors' previous works [11,30], where it was concluded
8 that when turbine area changes are employed, the MVEM has the capability of predicting the engine
9 performance parameters variation apart from the brake specific fuel consumption. This is because of the
10 MVEM limitation on representing the in-cylinder process, on the contrary to the zero-dimensional
11 model. As it can be inferred from Fig. 8, the scavenging receiver pressure is greatly influenced by the
12 change of turbine area. The scavenging air receiver increase results in the BSFC reduction as well as in
13 lowering the engine thermal loading as more air is trapped into the engine cylinders. Based on the
14 zero-dimensional model results, the relative variation of the BSFC as function of the scavenging receiver
15 pressure relative change and the engine load was derived and shown in Fig. 9. The one turbocharger unit
16 cut-out operation was also included as it follows the same trend as the case with reduction of turbine area
17 and thus, it can be considered as the extreme condition of the turbine area variation. The relative change
18 of the BSFC was found to be between -0.06 and 0.07, whilst the relative change of the scavenging
19 receiver pressure lies in the range -0.2-+0.43.

20 By applying curve fitting, it was found that the following Equation (5) can be used to represent the
21 BSFC relative change as function of the scavenging receiver pressure relative change and the engine load
22 in the case of variable turbine area:

$$\Delta BSFC_{VGT} = (k_1 + k_2 \cdot L + k_3 \cdot \Delta p_{sca,VGT}) \cdot \Delta p_{sca,VGT} \quad (5)$$

1 The scavenging receiver pressure relative change in the case of variable turbine area used in
 2 Equation (5) is calculated based on the scavenging receiver pressure values ($p_{sca,ref}$) shown in Fig. 2, as
 3 follows:

$$4 \quad \Delta p_{sca,VGT} = (p_{sca,VGT} - p_{sca,ref}) / p_{sca,ref} \quad (6)$$

5 where $p_{sca,VGT}$ is the calculated scavenging receiver pressure for the case of turbine area change.

6 The R-square for this correlation was calculated approximately 0.97, which indicates an adequate
 7 prediction of the used non-linear curve fit.

8 The derived coefficients values for the investigated slow speed two-stroke diesel engine are
 9 provided in Table 4. In this respect, the proposed extension methodology could be generalised and
 10 applied during the MVEM set-up process. However, this requires further validation, which is out of the
 11 scope of the present work.

12 **4.2 Incorporation of the derived corrective equations in the MVEM**

13 Since the fuel chemical energy proportion in the exhaust gas entering the turbine as well as the
 14 engine brake specific fuel consumption with varying SOI settings cannot be predicted by the MVEM,
 15 appropriate corrections need to be employed.

16 Firstly, the ζ correction to capture the dependency on the SOI change is applied in the MVEM by
 17 using the following equation:

$$18 \quad \zeta = \zeta_{ref} (1 + \Delta \zeta_{SOI}) = (k_{z1} \bar{P}_b + k_{z0}) (1 + \Delta \zeta_{SOI}) \quad (7)$$

19 where ζ_{ref} denotes the ζ parameter for the reference engine operation (without including varying settings
 20 of SOI and turbine area).

21 Secondly, the BSFC correction to capture the dependency on the SOI change is subsequently
 22 introduced in the indicated mean effective pressure calculation assuming that the change of the friction

1 mean effective pressure is insignificant, as follows:

$$2 \quad \bar{P}_i = \bar{P}_{i,ref} / (1 + \Delta BSFC_{SOI}) = F_R \bar{P}_{i,max} \eta_{comb} / (1 + \Delta BSFC_{SOI}) \quad (8)$$

3 where $\bar{P}_{i,ref}$ denotes the indicated engine mean effective pressure for the reference engine operation.

4 Equations (7) and (8) in conjunction with Equations (3) and (4) conclude the correction procedure
5 for the case of the SOI change. In addition, the steps described below are applied for the case where
6 simultaneous turbine area and SOI changes are used.

7 As the engine brake specific fuel consumption with varying turbine area cannot be predicted by the
8 MVEM, the correction of the indicated mean effective pressure needs to be employed similarly to
9 Equation (8), by estimating the BSFC relative change according to Equation (5). Since the fuel injection
10 timing also influences the scavenging receiver pressure (variation up to 6% as can be inferred from Fig.
11 4), the scavenging receiver pressure reference values ($p_{sca,ref}$) used in Equation (6) should be modified.
12 The new reference pressure ($p_{sca,SOI,ref}$) is estimated by using the initial reference values ($p_{sca,ref}$ from Fig.
13 2) and their relative change values ($\Delta p_{sca,SOI}$ shown in Fig. 4), according to the following equation:

$$14 \quad p_{sca,SOI,ref} = p_{sca,ref} (1 + \Delta p_{sca,SOI}) \quad (9)$$

15 The scavenging receiver pressure relative change variation in the case of SOI change ($\Delta p_{sca,SOI}$) as
16 function of the SOI change and the engine load (presented in Fig. 4) was analysed by using the MATLAB
17 curve fitting tool. Due to the fact that the blowers were activated below the 40% engine load point, a
18 piecewise function was applied to capture this parameter variations. It was found that the similar
19 formulae (as provided in Equations (3)-(5)) can be used to correlate these three variables at both above
20 and below the 40% engine load with the calculated R-square values being 0.9937 and 0.9837,
21 respectively. In addition, an interpolation function was used to smooth the transition in the range between
22 30% and 40% loads.

23 Based on the above analysis, the relative change of the scavenging receiver pressure in the case of

1 varying SOI can be derived using the following piecewise function:

$$2 \quad \Delta p_{sca,SOI} = \begin{cases} f_1(SOI, L) & L > 0.4 \\ (L-0.3)/0.1 \cdot f_1(SOI, L) + (0.4-L)/0.1 \cdot f_2(SOI, L) & 0.3 < L < 0.4 \\ f_2(SOI, L) & L < 0.3 \end{cases} \quad (10)$$

3 where:

$$4 \quad f_1(SOI, L) = (k_1 + k_2 \cdot L + k_3 \cdot \Delta SOI) \cdot \Delta SOI$$

$$5 \quad f_2(SOI, L) = (k_4 + k_5 \cdot L + k_6 \cdot \Delta SOI) \cdot \Delta SOI$$

6 The values of the constants in Equation (10) are provided in Table 5.

7 For the case that only turbine area change is employed, $\Delta p_{sca,SOI}$ equals to zero and therefore, the
8 scavenging receiver pressure baseline values used for the turbine area change correction (p_{sca,SOI_ref} in
9 Equation (9)) are the same as the respective initial reference values ($p_{sca,ref}$ shown in Fig. 2).

10 Finally, the indicated mean effective pressure is corrected by using the following equation:

$$11 \quad \bar{P}_i = F_R \bar{P}_{i,max} \eta_{comb} / (1 + \Delta BSFC_{SOI} + \Delta BSFC_{VGT}) \quad (11)$$

12 It can be inferred from Equation (11) that the applied BSFC corrections affect the calculated
13 indicated mean effective pressure, and as a result the brake mean effective pressure. Therefore, the rack
14 position calculated by the engine governor model will be different in the predictions of the original
15 MVEM and the extended MVEM. Thus, for the same engine operating point, different amount of fuel
16 and as a result a different value of BSFC will be calculated. In summary, the extension of MVEM can be
17 readily applied following the proposed correction procedure, the flowchart of which is illustrated in Fig.
18 10.

19 5. Case studies

20 In order to examine the extended MVEM capability of accurately predicting the engine
21 performance parameters in the case of VIT and VGT, various sets of SOI and turbine areas were tested
22 under engine steady state conditions. First, the case with both the SOI retarded by 3°CA and the turbine

1 area reduced by 20% at 25%, 50%, 75% and 100% engine loads was investigated. The predicted engine
2 performance parameters from the zero-dimensional model, the original MVEM as well as the extended
3 MVEM are shown in Fig. 11. The validated zero-dimensional model is considered to provide the
4 baseline predictions.

5 Retarding the SOI results in the increase of the exhaust temperature and the fuel consumption as
6 explained above, whereas reducing the turbine area decreases the exhaust temperature and the fuel
7 consumption at low load region as can be seen from Fig. 8. Therefore, their combinatory effect on the
8 engine performance parameters depends on the specific conditions. In comparison to the normal engine
9 operation (shown in Fig. 2), the considered settings substantially increase the receiver pressures and
10 turbocharger speed at all loads resulting in lower predicted exhaust temperature at loads below 50% and
11 higher at loads above 50%. Additionally, the fuel injection timing influence on the receiver pressures, the
12 turbocharger speed as well as the exhaust temperatures becomes more significant as the engine load
13 increases.

14 As it can be observed in Fig. 11, the original MVEM lacks the capability of predicting the BSFC
15 with changing either the SOI or the turbine area. The calculated BSFC values from the original MVEM
16 are very close to the ones derived from the reference engine operation as shown in Fig. 2, exhibiting
17 considerable errors in comparison with the respective results of the other two models. As load increases,
18 the SOI retard influence on the BSFC becomes more considerable. The engine cylinder cycle becomes
19 less efficient as explained above and therefore, the predicted BSFC values are considerably greater than
20 the ones in the normal operation.

21 The ζ correction renders the extended MVEM adequate for accurately predicting the exhaust gas
22 temperature in the engine receiver and the turbine outlet, whereas the BSFC correction (eventually
23 affecting the rack position) enables the extended MVEM sufficient prediction for the fuel mass flow rate.

1 The relative errors between the extended MVEM and zero-dimensional model are in the range of 0.5 to
2 1.0% for the BSFC and 0.05 to 1.03% for the other parameters, which reveals the fact that all the main
3 engine parameters derived from the extended MVEM and the zero-dimensional model match well. Thus,
4 the proposed MVEM extension approach with corrections for fuel injection timing and turbine area is
5 considered to be effective. The predicted fuel mass flow rate deviations between the original MVEM and
6 the other two models are not so noticeable due to their relatively small values, but they actually follow a
7 consistent variation trend similar to the BSFC one, which is expected since the BSFC is calculated
8 considering the fuel mass flow rate and the engine brake power. The original MVEM predictions exhibit
9 errors in the range 0.4-5.1% for the BSFC and 0.2-3.9% for the other parameters, and therefore, it needs
10 to be used with caution for the investigation of the engine performance in cases of engine varying
11 settings.

12 Moreover, to test other engine settings, different combinations of SOI and turbine area changes as
13 shown in Table 6 were considered. It should be noted that the extended MVEM applied all the
14 corrections and values presented in Table 4. The validated zero-dimensional model was used to provide
15 the required reference values. The predicted results were compared with the corresponding ones obtained
16 by using the zero-dimensional model and the derived relative errors are presented in Fig. 12. The engine
17 settings included the SOI advanced and retarded by 2°CA along with the turbine area changes of -20%,
18 -10%, +10% and +20% at 4 different loads (25%, 50%, 75% and 100%). So totally 32 combination
19 cases were investigated as presented in Table 6. It can be observed from Fig. 12 that the deviations of the
20 main engine parameters in the most cases are less than 1% and the highest deviation is 2.1%, which
21 demonstrates that the extended MVEM predictions are accurate enough and the model can be used for
22 investigating the engine performance in VIT and VGT studies.

23 Having validated the extended MVEM capability at steady state conditions, the next step was to

1 examine the extended MVEM prediction accuracy with varying engine settings at transient operation.
2 The following three engine settings change schedules were defined at 75% engine load in order to test the
3 models response: (a) the start of fuel injection ramp changes shown in Fig. 13 (a); (b) the turbine area
4 change percentage ramp variation (between -20% and +20% the normal turbine area) shown in Fig. 13
5 (b); (c) the exhaust gas bypassed by the waste gate ramp changes (compared to the normal exhaust gas
6 amount) presented in Fig. 13 (c). A set of the derived simulation results including the scavenging air
7 receiver pressure, the exhaust gas receiver temperature, the turbocharger speed, the air to fuel ratio, the
8 air mass flow rate and the BSFC, is presented in Fig. 14-16 using the zero-dimensional model, the
9 original MVEM as well as the extended MVEM.

10 As the original MVEM does not handle the varying fuel injection timing, its predicted values for all
11 the engine parameters almost remained constant as can be observed from Fig. 14. The extended MVEM
12 results sufficiently match the ones of the zero-dimensional model, although slight steady deviations are
13 observed with the maximum error being at 0.81%. Based on the derived results, it can be concluded that
14 the extended MVEM can capture the engine performance variation with the SOI changes at transient
15 operation.

16 As already explained above, the original MVEM can be used to simulate the engine behaviour but
17 cannot adequately predict the BSFC variation with the turbine area changes. This can be also easily
18 inferred from Fig. 15 where it is observed that the original MVEM derived results are very similar with
19 the results of the other two models except for the BSFC. The extended MVEM can capture the engine
20 performance variation with the turbine area changes including the BSFC changes at transient operation
21 as its predictions match the ones of the zero-dimensional model with the maximum error being found to
22 be 0.92%.

23 As the exhaust gas bypass considerably influences the scavenging receiver pressure, its effect is

1 comparable to the effect of VGT. This can be also observed from the results presented in Fig. 16. It can
2 be inferred that the extended MVEM adequately predicts all the engine performance parameters with
3 the exhaust gas bypass changes (the maximum error is 0.75%), thus improving the MVEM predictive
4 capability. Therefore, it can be concluded that the extended MVEM can be used with fidelity to
5 investigate the engine operation with exhaust gas bypass.

6 From the above analysis, it was proved that the extended MVEM has the capability of predicting
7 the engine performance parameters (power, speed, BSFC, efficiency), the working medium states
8 (pressure and temperature, air to fuel ratio), the flow parameters (flow rates), and turbocharger
9 parameters (speed, pressure ratio, efficiency) in both steady state and transient conditions.

10 The three models running time on a standard personal computer with Intel Core i7-2600 processor
11 for the preceding three investigated cases was examined and the results are shown in Table 7. It can be
12 inferred from that the extended MVEM requires around double execution time in comparison with the
13 original MVEM due to the incorporation of the corrective equations, whereas it is still approximately 7
14 times faster than real time and 570 times faster than the zero-dimensional model. It should be noted
15 that the zero-dimensional model included blocks for all the engine cylinders; much less execution time
16 is expected in case where one cylinder is only modelled and the other cylinders parameters are
17 calculated by considering each cylinder phase angle. Although the MATLAB/Simulink environment
18 offers the platform for an effective development and set-up, implementation of the zero-dimensional
19 model in MATLAB or another programming language considerably reduces the models execution
20 time.

21 **6. Conclusions**

22 The extension of a MVEM was developed based on analytical corrective equations which were

1 derived by using the curve fitting of a detailed zero-dimensional model parametric runs results. The
2 engine performance parameters variations were thoroughly analysed at varying SOI and turbine area
3 settings using the zero-dimensional model. The extended MVEM was benchmarked against the
4 zero-dimensional model and the original MVEM. The main conclusions derived from this work are
5 summarized as follows.

6 The engine parameters in specific, the scavenging receiver pressure, the cylinder pressure drop, the
7 turbocharger speed and the cylinder compression pressure, are influenced most significantly by the SOI
8 variation at around 40% load region; however, the cylinder temperature at EVO is affected in a less
9 extent at this load point whereas the SOI variation effect on the cylinder maximum pressure remains
10 comparable at all loads. The cylinder pressure drop exhibits a maximum relative change of 15%, whilst
11 the other engine parameters are influenced much less, with the observed maximum relative change being
12 at around 6%. The SOI retard shifts the combustion process towards the expansion phase resulting in a
13 significant reduction of cylinder maximum pressure accompanied with an increase of the exhaust gas
14 temperature at EVO, which eventually leads to higher BSFC. As the SOI changes are from -2 to +3°C_A,
15 the parameter ζ relative change was found to vary in the range of -0.02 to 0.035, whereas the BSFC
16 relative change was calculated between -0.015 and 0.034. Furthermore, both the overall ζ and BSFC
17 relative changes follow a monotonic trend with various fuel injection timings and engine loads.

18 The effects of turbine area change on the engine parameters including the scavenging receiver
19 pressure, the cylinder pressure drop and the turbocharger speed are the most significant with an observed
20 maximum relative change at 30%. At engine loads lower than 75%, the turbine area reduction results in
21 an increase of the scavenging receiver pressure and as a result the maximum cylinder pressure, thus
22 decreasing BSFC; however as load decreases further the reduction of BSFC becomes less distinctive
23 since the turbocharger speed is too low to ensure sufficient air flow. At loads above 75%, the reduction of

1 turbine area causes the engine cylinders air flow restriction, which has as a result the decrease of the
2 engine efficiency thus increasing the BSFC.

3 The MVEM cannot make reliable predictions at varying fuel injection timing settings as it does not
4 represent the in-cylinder process; however, it has the capability of predicting the engine performance
5 parameters variation apart from the brake specific fuel consumption at varying turbine area settings. The
6 extension of MVEM can be implemented by incorporating the corrective equations in the corresponding
7 parameters following the provided correction procedure. The extended MVEM can predict with an
8 adequate accuracy the engine performance parameters variations, thus overcoming the limitations of the
9 original MVEM. The execution time of the extended MVEM is longer than the original MVEM but
10 reasonable and substantially less than the zero-dimensional model. As the extended MVEM runs seven
11 times faster than the real time, it can be widely used in applications of engine and its components control
12 system design, such as waste gate exhaust valves, variable geometry turbine, EGR and turbocharger
13 cut-out valves.

14 In conclusion, the extended MVEM is a tool that improves the prediction capability of the mean
15 value modelling approach without considerably increasing the complexity and the execution time of the
16 model setting up procedure and therefore, it is expected to be employed in a variety of applications as the
17 new electronically controlled versions of marine diesel engines have been becoming quite popular in the
18 shipping industry the recent years and additional engine controlled components are employed for
19 increasing the efficiency and reducing emissions.

20

21 **Acknowledgements** Part of this work was conducted in the framework of MOVE project funded by
22 Innovate UK. This publication reflects only the authors' views; Innovate UK is not liable for any use that
23 may be made of the information contained herein. The research work performed by Dr. Guan and Prof.

1 Chen was supported by the Fundamental Research Funds for the Central Universities of China (WUT:
2 2017IVA023) and the National Natural Science Foundation of China (No. 51579200).

3

4

5

6

References

- [1] Wärtsilä. Marine solutions (2nd ed.). Publication no: SPEN-DBAC136254; 2012.
- [2] MAN Diesel & Turbo. Marine engine IMO Tier II programme 2013. Publication no. 4510-0012-00ppr; 2013.
- [3] Raikio T, Hallbäck B, Hjort A. Design and first application of a 2-stage turbocharging system for a medium-speed diesel engine. In: Proceedings of the 26th CIMAC world congress on combustion engine technology, Bergen, paper no. 82; 2010.
- [4] Thomas B, Markus K, Armin R, Melanie H. Second generation of two-stage turbocharging Power2 systems for medium speed gas and diesel engines. In: Proceedings of the 27th CIMAC world congress on combustion engine technology, Shanghai, paper no. 134; 2013.
- [5] Lindstad HE, Rehn CF, Eskeland GS. Sulphur abatement globally in maritime shipping. 2017. Transportation Research. Part D. 57. 303–313.
- [6] Xiros N. Robust control of diesel ship propulsion. Berlin: Springer; 2002.
- [7] Kyrtatos NP, Koumbarelis I. Performance prediction of next-generation slow speed diesel engines during ship manoeuvres. Trans IMarE 1994; 106(Part I): 1-26.
- [8] Kyrtatos NP, Theodossopoulos P, Theotokatos G, Xiros N. Simulation of the overall ship propulsion plant for performance prediction and control. In Proceedings of the conference on advanced marine machinery systems with low pollution and high efficiency; 1999.
- [9] Campora U, Figari M. Numerical simulation of ship propulsion transients and full scale validation. Pro IMechE, Part M: J Engineering for the Maritime Environment 2003; 217: 41-52.
- [10] Livanos G, Theotokatos G, Kyrtatos NP. Simulation of large marine two-stroke diesel engine operation during fire in the scavenging air receiver. J Marine Eng Technol 2003; 3: 9-16.

- [11] Guan C, Theotokatos G, Zhou P, Chen H. Computational investigation of a large containership propulsion engine operation at slow steaming conditions. *Applied Energy* 2014; 130: 370-383.
- [12] Theotokatos G. On the cycle mean value modelling of a large two-stroke marine diesel engine. *Proc IMechE, Part M: J Engineering for the Maritime Environment* 2010; 224: 193-205.
- [13] Theotokatos G, Tzelepis V. A computational study on the performance and emission parameters mapping of a ship propulsion system. *Proc IMechE, Part M: J Engineering for the Maritime Environment* 2013; DOI: 10. 1177/1475090213498715.
- [14] Sapra H, Godjevac M, Visser K, Stapersma D, Dijkstra C. Experimental and simulation-based investigations of marine diesel engine performance against static back pressure. *Applied Energy* 2017; 204: 78-92.
- [15] Sui C, Song E, Stapersma D, Ding D. Mean value modelling of diesel engine combustion based on parameterized finite stage cylinder process. *Ocean Engineering* 2017; 136: 218-232.
- [16] Hountalas DT. Prediction of marine diesel engine performance under fault conditions. *Appl Therm Eng* 2000; 20: 1753-1783.
- [17] Scappin F, Stefansson SH, Haglind F. Validation of a zero-dimensional model for prediction of NO_x and engine performance for electronically controlled marine two-stroke diesel engines. *Appl Therm Eng* 2012; 37: 344-352.
- [18] Woodward JB, Latorre RG. Modeling of diesel engine transient behavior in marine propulsion analysis. *Tran Soc Nav Archit Mar Eng* 1984; 92: 33-49.
- [19] Hendrics E. Mean value modelling of large turbocharged two-stroke diesel engines. SAE technical paper no 890564; 1989.
- [20] Chesse P, Chalet D, Tauzia X. Real-time performance simulation of marine diesel engines for the training of navy crews. *Mar Technol* 2004; 41(3): 95-101.
- [21] Payri F, Olmeda P, Martin J, Garcia A. A complete 0D thermodynamic predictive model for direct injection diesel engines. *Applied Energy* 2011; 88: 4632-4641.
- [22] Raptotasios SI, Sakellariadis NF, Papagiannakis RG, Hountalas DT. Application of a multi-zone combustion model to investigate the NO_x reduction potential of two-stroke marine diesel engines using EGR. *Applied Energy* 2015; 157: 814-823.
- [23] Rakopoulos CD, Dimaratos AM, Giakoumis EG, Rakopoulos DC. Evaluation of the effect of engine, load and turbocharger parameters on transient emissions of diesel engine. *Energy Conversion*

and Management 2009; 50(9): 2381-2393.

[24] Cordtz R, Schramm J, Andreasen A, Eskildsen SS, Mayer S, Stefan E. Modeling the distribution of sulfur compounds in a large two stroke diesel engine. *Energy & Fuels* 2013; 27 (3): 1652-1660.

[25] Cordtz R, Mayer S, Eskildsen SS, Svend S, Schramm J. Modeling the condensation of sulfuric acid and water on the cylinder liner of a large two-stroke marine diesel engine. *Journal of Marine Science and Technology* 2017; <https://doi.org/10.1007/s00773-017-0455-9>

[26] Pang KM, Karvounis N, Walther JH, Schramm J. Numerical investigation of soot formation and oxidation processes under large two-stroke marine diesel engine-like conditions using integrated CFD-chemical kinetics. *Applied Energy* 2016; 169: 874-887.

[27] Gugulothu SK, Reddy KHC. CFD simulation of in-cylinder flow on different piston bowl geometries in a DI diesel engine. *J Appl Fluid Mech* 2016; 9: 1147-55.

[28] Dong TP, Zhang FJ, Liu BL, An XH. Model-based state feedback controller design for a turbocharged diesel engine with an EGR system. *Energies* 2015; 8: 5018-39.

[29] Dong TP, Liu BL, Zhang FJ, Wang YM, Wang BL, Liu P. Control oriented modeling and analysis of gas exchange and combustion processes for LTC diesel engine. *Appl Therm Eng* 2017; 110: 1305-14.

[30] Guan C, Theotokatos G, Chen H. Analysis of two stroke marine diesel engine operation including turbocharger cut-out by using a zero-dimensional model. *Energies* 2015; 8: 5738-5764.

[31] Zheng JN, Caton JA. Second law analysis of a low temperature combustion diesel engine: Effect of injection timing and exhaust gas recirculation. *Energy* 2012; 38: 78-84.

[32] Poran A, Tartakovsky L. Performance and emissions of a direct injection internal combustion engine devised for joint operation with a high-pressure thermochemical recuperation system. *Energy* 2017; 124: 214-226.

[33] Mizythras P, Boulougouris E, Theotokatos G. Numerical study of propulsion system performance during ship acceleration. *Ocean Engineering* 2017; Accepted for publication.

[34] Nielsen KV, Blanke M, Eriksson L, Laursen MV. Control-oriented model of molar scavenge oxygen fraction for exhaust recirculation in large diesel engines. *Journal of Dynamic Systems, Measurement, and Control* 2017; DOI: 10.1115/1.4034750.

[35] Dimopoulos G, Georgopoulou C, Stefanatos I, Zymaris A, Kakalis N. A general-purpose process modelling framework for marine energy systems. *Energy Convers. Manag.* 2014; 10 (86): 325-339.

- [36] Nikzadfar K, Shamekhi AH. An extended mean value model (EMVM) for control-oriented modeling of diesel engines transient performance and emissions. *Fuel* 2015; 154: 275-292.
- [37] Fadila M, Charbel S. Combined mean value engine model and crank angle resolved in-cylinder modeling with NO_x emissions model for real-time diesel engine simulation at high engine speed. *Energy* 2015; 88: 515-527.
- [38] Baldi F, Theotokatos G, Andersson K. Development of a combined mean value-zero dimensional model and application for a large marine four-stroke diesel engine simulation. *Applied Energy* 2015; 154: 402-415.
- [39] Tang YY, Zhang JD, Gan HB, Jia BZ, Xia Y. Development of a real-time two-stroke marine diesel engine model with in-cylinder pressure prediction capability. *Applied Energy* 2017; 194: 55-70.
- [40] Livanos G, Simotas G, Kyrtatos NP. Tanker propulsion plant transient behavior during ice breaking conditions. In: *Proceedings of the 16th International offshore and polar engineering conference*, San Francisco; 2006.
- [41] Livanos G, Papalambrou G, Kyrtatos NP. Electronic engine control for ice operation of tankers. In: *Proceedings of the 25th CIMAC world congress on combustion engine technology*, Viena, Austria, paper no. 44; 2007.
- [42] Klein M. Single-zone cylinder pressure modeling and estimation for heat release analysis of SI engines. Ph.D. Dissertation, Linköping University, Linköping, Sweden, 2007.
- [43] Heywood JB. *Internal Combustion Engines Fundamentals*. Mc-Graw-Hill, 1998.
- [44] Watson N, Janota MS. *Turbocharging the Internal Combustion Engine*. Macmillan Press, 1982.
- [45] Merker GP, Schwarz C, Stiesch G, Otto F. *Simulating Combustion*. Springer-Verlag, Berlin, Germany, 2006.
- [46] Woschni G. A universally applicable equation for the instantaneous heat transfer coefficient in the internal combustion engine. SAE Paper 1967. no 670931.
- [47] McAulay K, Wu T, Chen S, Borman G, Myers P, Uyehara O. Development and evaluation of the simulation of the compression-ignition engine. SAE Paper 1965. no 650451.
- [48] Meier E. A simple method of calculation and matching turbochargers. Publication CH-T 120 163E. Brown Boveri & Company Ltd. Baden. Switzerland; 1981.
- [49] MAN Diesel & Turbo. Computerized engine application system-engine room dimensioning. <<http://marine.man.eu/two-stroke/ceas>> [accessed 13.01.2017].

Nomenclature

a	combustion model constant (-)
A	air
BMEP	brake mean effective pressure (bar)
BSFC	brake specific fuel consumption (g/kW h)
F_R	fuel rack position (-)
h	specific enthalpy (J/kg)
H_L	fuel lower heating value (J/kg)
k	coefficients
L	engine load (-)
m	mass (kg)/combustion model constant (-)
\dot{m}	mass flow rate (kg/s)
N	rotational speed (r/min)
p	pressure (Pa)
\bar{p}	mean effective pressure (Pa)
\dot{Q}	heat transfer rate (W)
R	gas constant (J/kg K)
t	time (s)
T	temperature (K)
u	specific internal energy (J/kg)
V	volume (m ³)

Subscripts

a	air
b	brake
com	compression/compressor
$comb$	combustion
cyl	cylinder
d	downstream
e	exhaust gas
exh	exhaust receiver
f	fuel
i	indicated
max	maximum
nor	normal
out	outlet
ref	reference
sca	scavenging receiver
tc	turbocharger
tur	turbine
u	upstream

Greek symbols

Δ	difference
ζ	proportion of the chemical energy of the fuel contained in the exhaust gas

Abbreviations

BDC	bottom dead center
CA	crank angle

η	efficiency	EGR	exhaust gas recirculation
φ	fuel/air equivalence ratio	EVC	exhaust valve close
		EVO	exhaust valve open
		ISO	International Organization for Standardization
		MCR	maximum continuous rating
		MVEM	mean value engine model
		SOI	start of injection
		SPC	scavenging port close
		SPO	scavenging port open
		VGT	variable geometry turbine
		VIT	variable injection timing

List of figure captions

Fig. 1. Engine model implemented in MATLAB/Simulink environment.

Fig. 2. Steady state simulation results and comparison with shop trial data.

Fig. 3. Zero-dimensional model predicted cylinder pressure diagrams and comparison with shop trial data.

Fig. 4. Effect of SOI change on engine parameters predicted by the zero-dimensional model.

Fig. 5. Effect of SOI change on cylinder pressure and heat release rate at 75% engine load predicted by the zero-dimensional model.

Fig. 6. Zero-dimensional model calculated points and fitted surface of ζ relative change as function of SOI change and engine load.

Fig. 7. Zero-dimensional model calculated points and fitted surface of BSFC relative change as function of SOI change and engine load.

Fig. 8. Effect of turbine area change on engine parameters predicted by the zero-dimensional model.

Fig. 9. Zero-dimensional model calculated points and fitted surface of BSFC relative change as function of scavenging receiver pressure relative change and engine load.

Fig. 10. The flow chart of the extended MVEM approach correction procedure.

Fig. 11. Engine performance parameters predictions from extended MVEM and comparison with the

zero-dimensional model and MVEM predictions.

Fig. 12. Errors between extended MVEM predictions and zero-dimensional model.

Fig. 13. The engine settings change schedule.

Fig. 14. Simulation results for the engine transient operation with SOI changes.

Fig. 15. Simulation results for the engine transient operation with turbine area changes.

Fig. 16. Simulation results for the engine transient operation with exhaust gas bypass changes.

List of table captions

Table 1 The combustion model constants in zero-dimensional model.

Table 2 MAN Diesel & Turbo 7K98MC engine parameters [50].

Table 3 Percentage errors of the predicted parameters against experimental data from shop trials.

Table 4 Coefficients values for Equations (3), (4) and (5).

Table 5 Constants of Equation (10).

Table 6 The examined combinations of SOI and turbine area changes at different loads.

Table 7 Models execution time comparison.

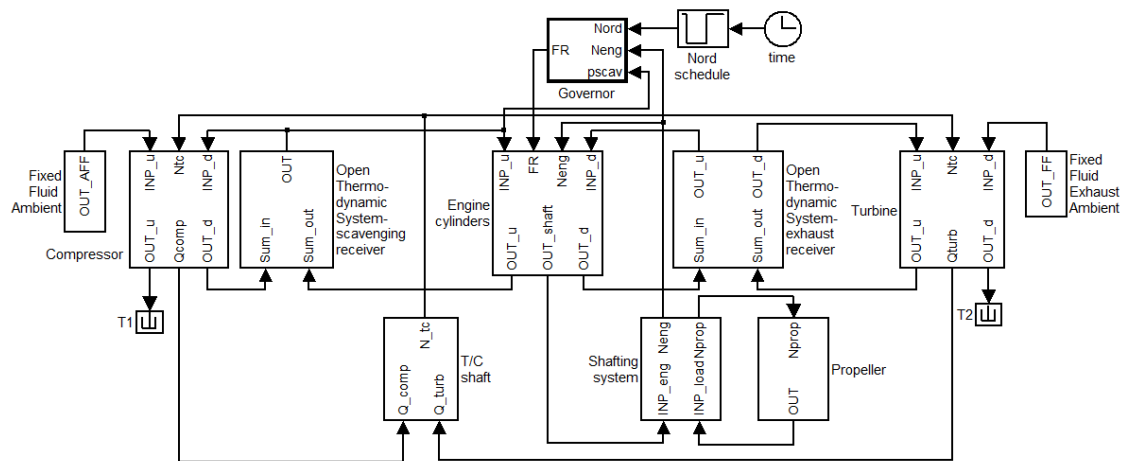


Fig. 1. Engine model implemented in MATLAB/Simulink environment.

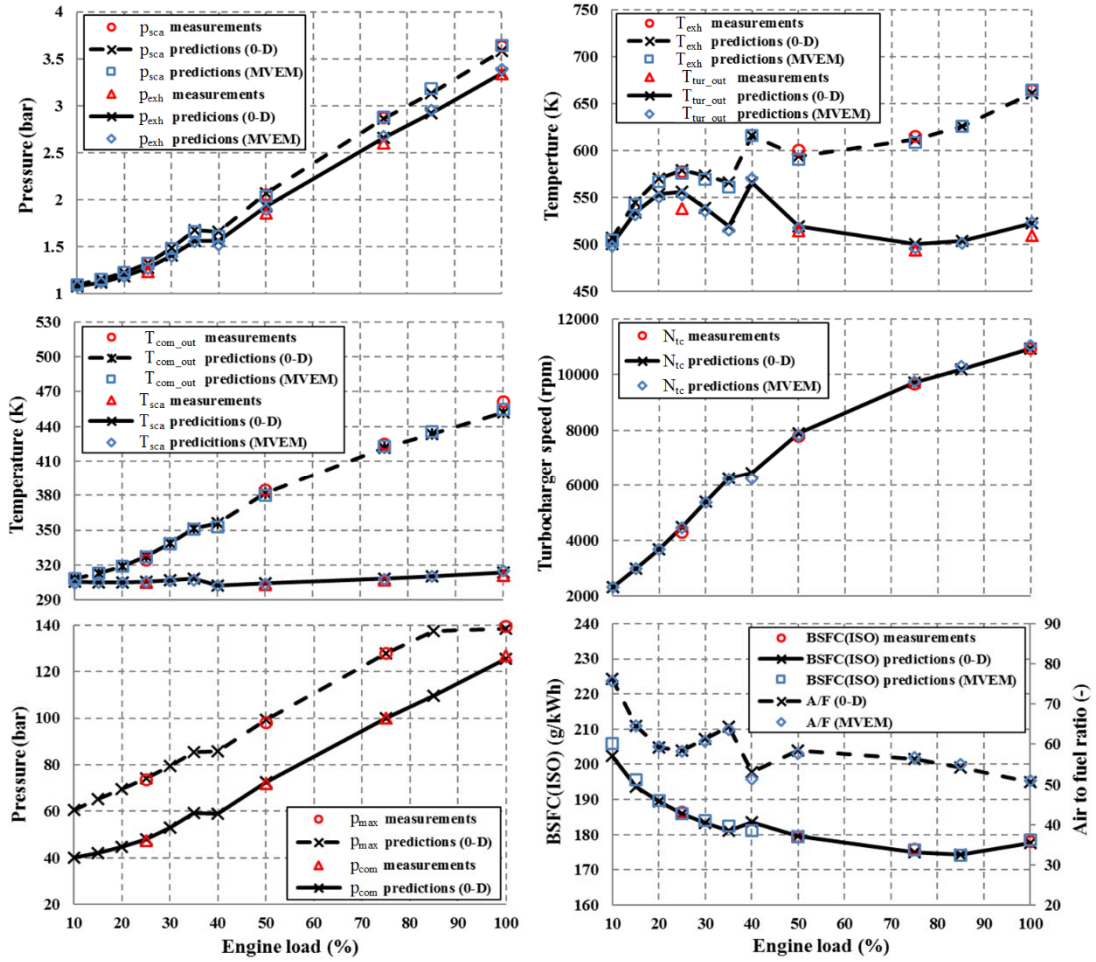


Fig. 2. Steady state simulation results and comparison with shop trial data.

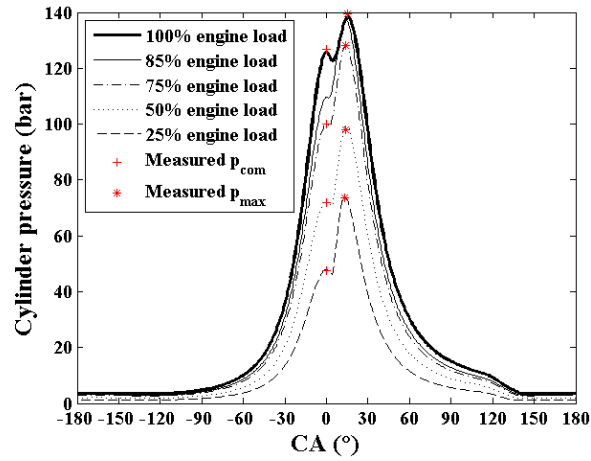


Fig. 3. Zero-dimensional model predicted cylinder pressure diagrams and comparison with shop trial data.

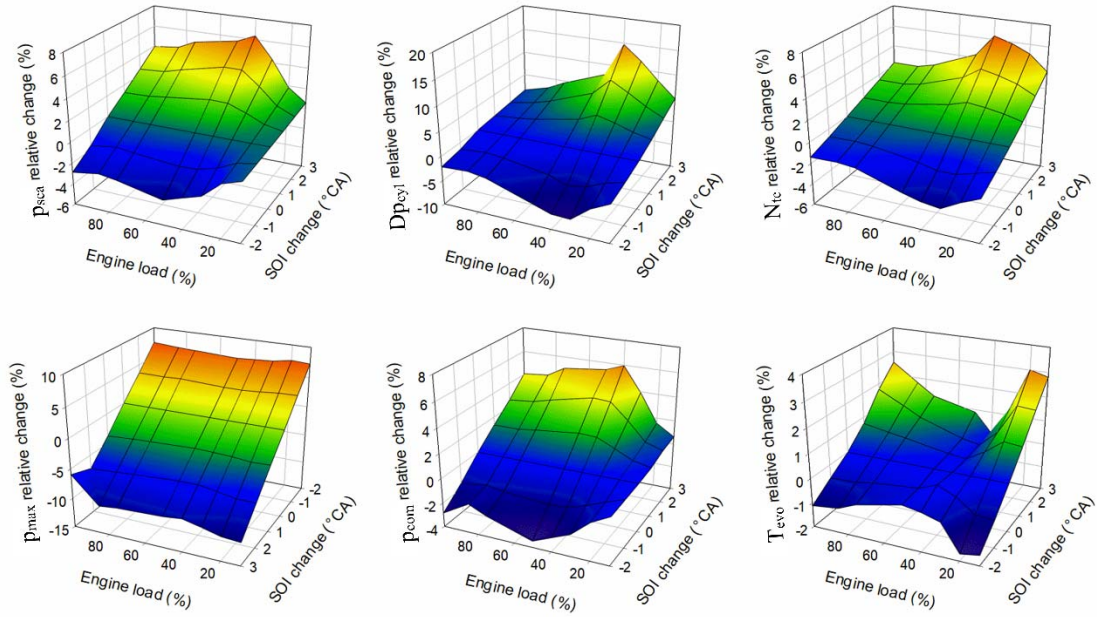


Fig. 4. Effect of SOI change on engine parameters predicted by the zero-dimensional model.

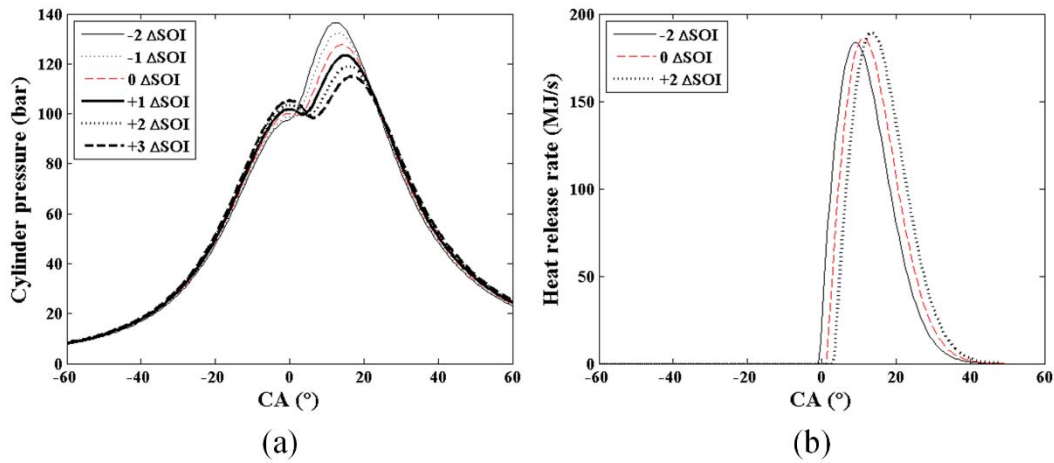


Fig. 5. Effect of SOI change on cylinder pressure and heat release rate at 75% engine load predicted by the zero-dimensional model.

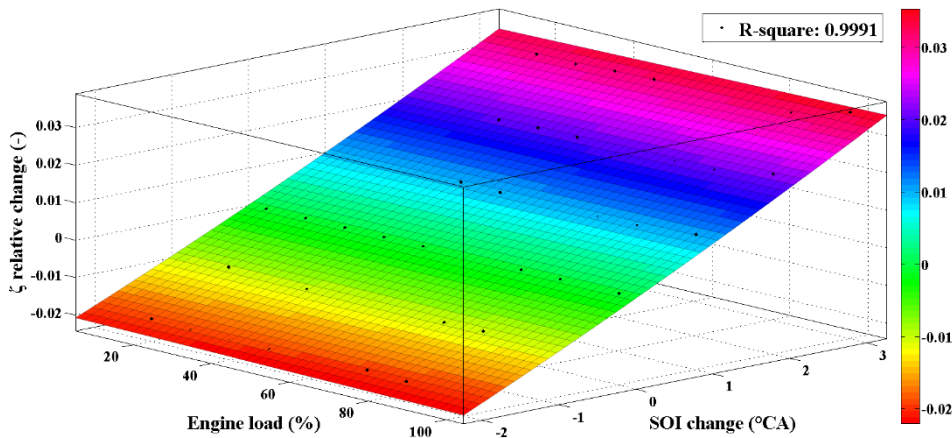


Fig. 6. Zero-dimensional model calculated points and fitted surface of ζ relative change as function of SOI change and engine load.

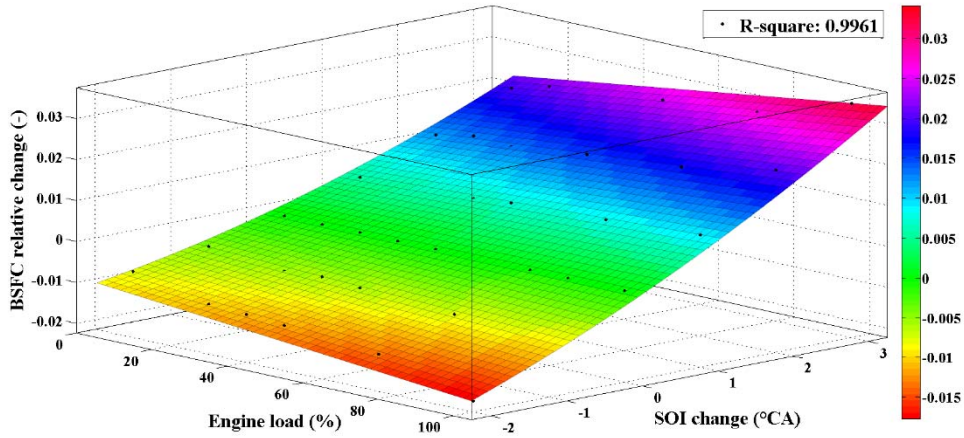


Fig. 7. Zero-dimensional model calculated points and fitted surface of BSFC relative change as function of SOI change and engine load.

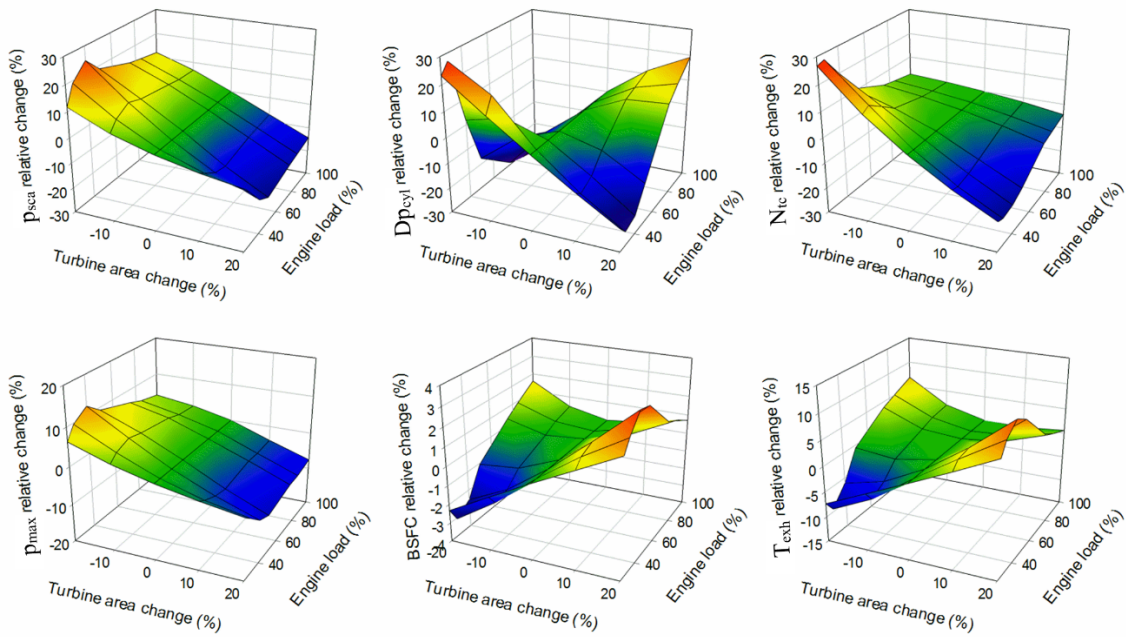


Fig. 8. Effect of turbine area change on engine parameters predicted by the zero-dimensional model.

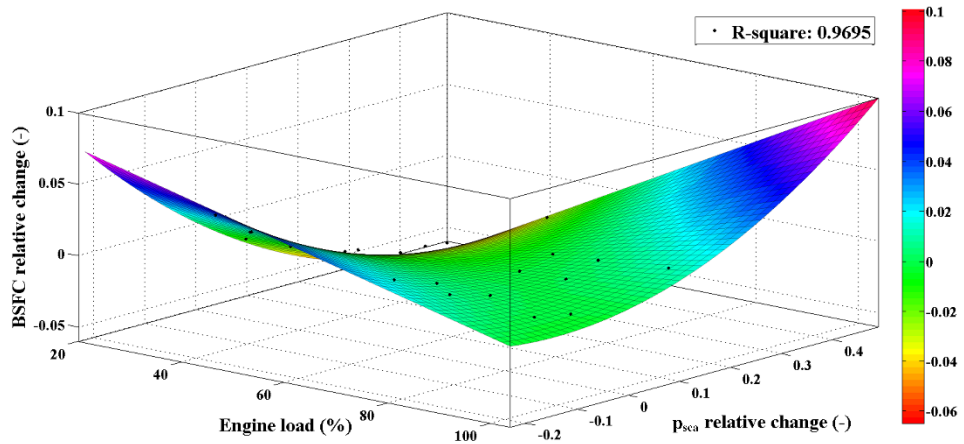


Fig. 9. Zero-dimensional model calculated points and fitted surface of BSFC relative change as function of scavenging receiver pressure relative change and engine load.

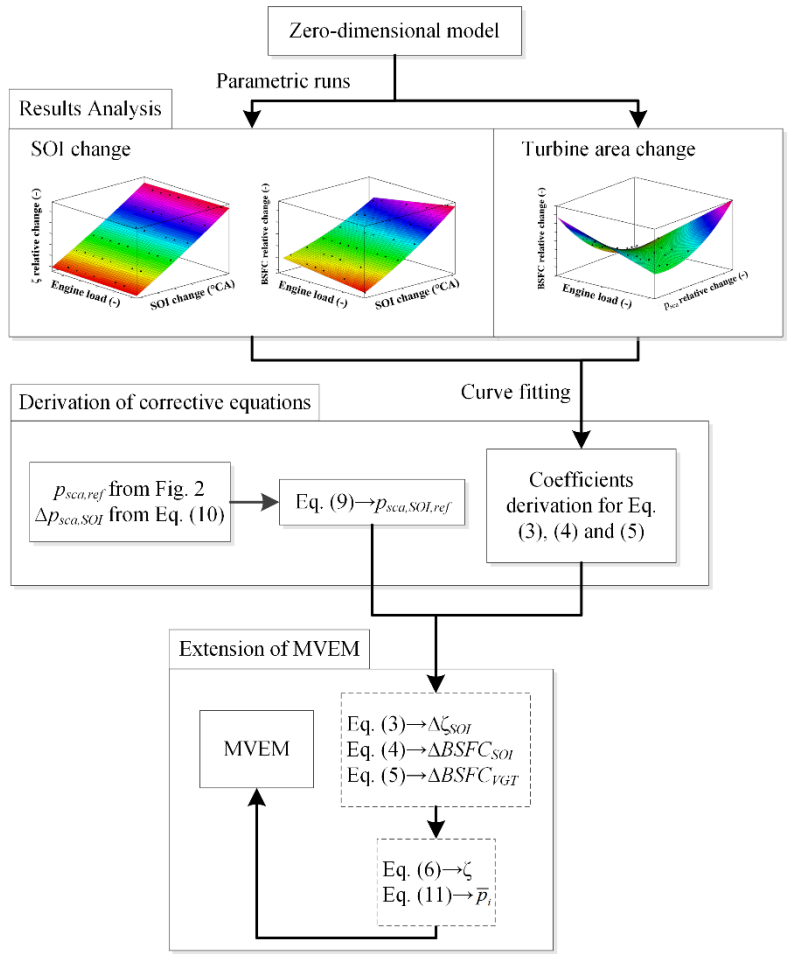


Fig. 10. The flow chart of the extended MVEM approach correction procedure.

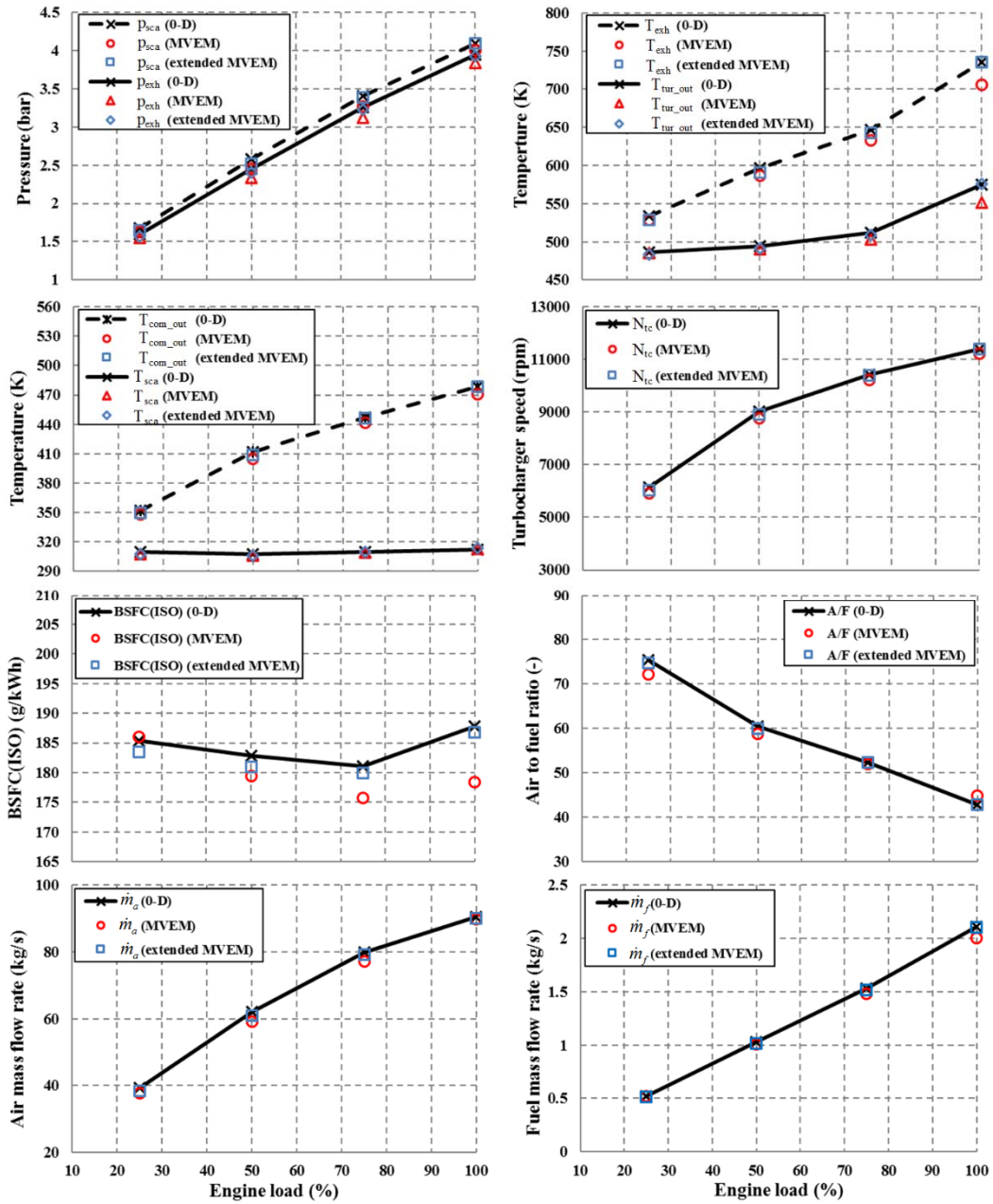


Fig. 11. Engine performance parameters predictions from extended MVEM and comparison with the zero-dimensional model and MVEM predictions.

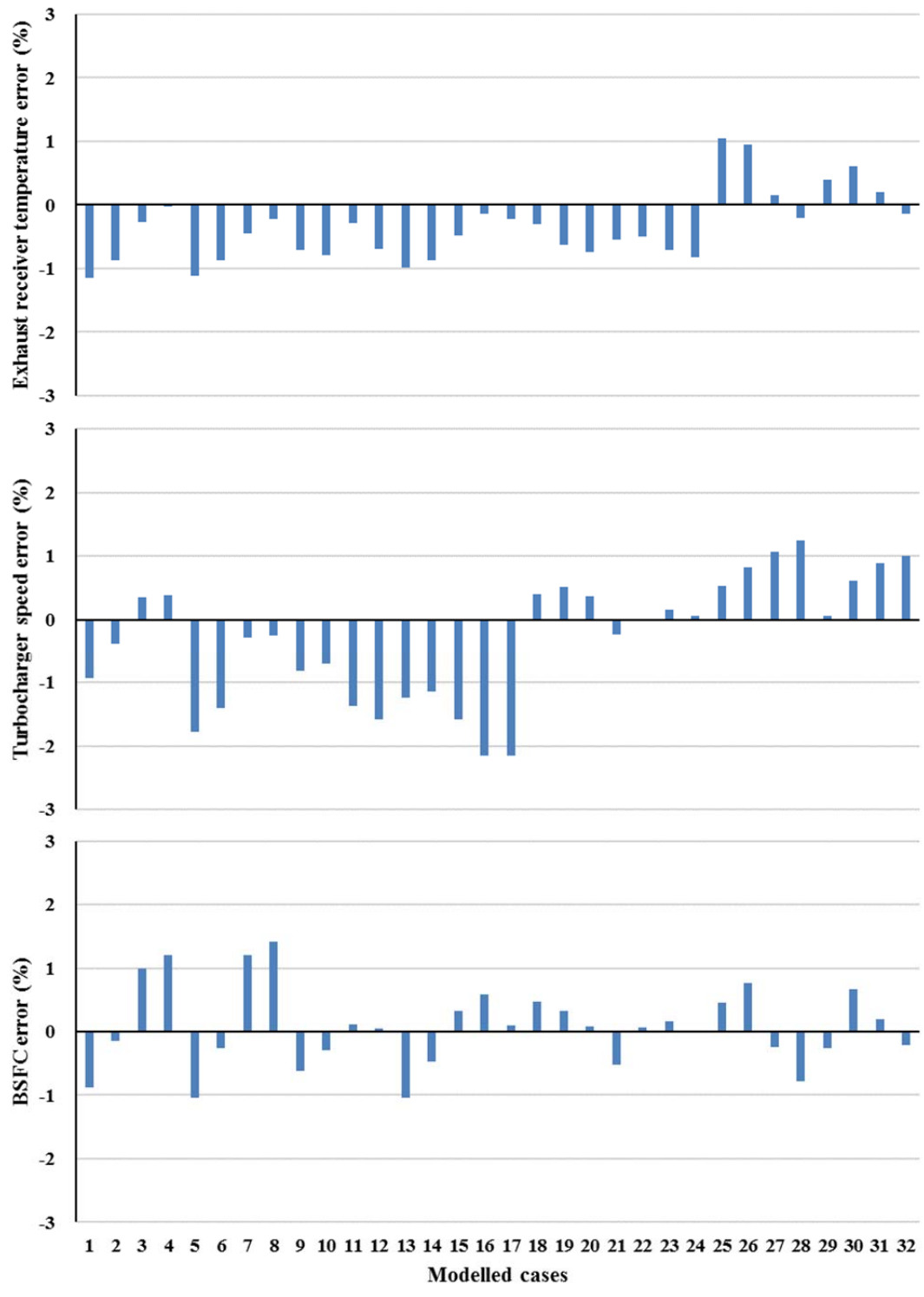


Fig. 12. Errors between extended MVEM predictions and zero-dimensional model.

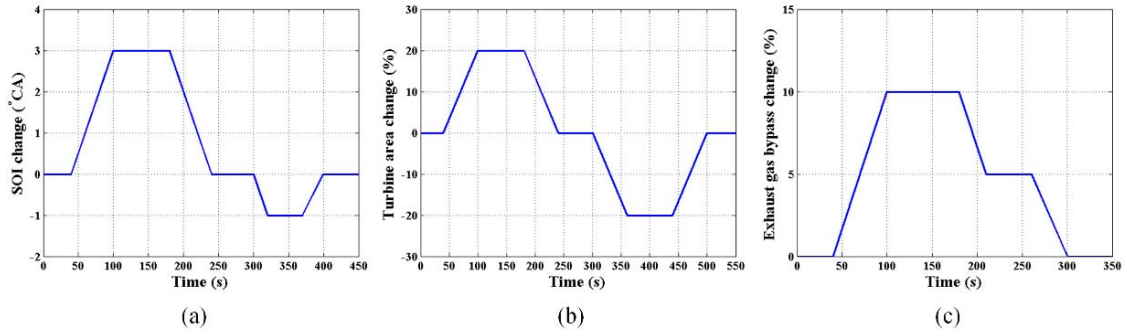


Fig. 13. The engine settings change schedule.

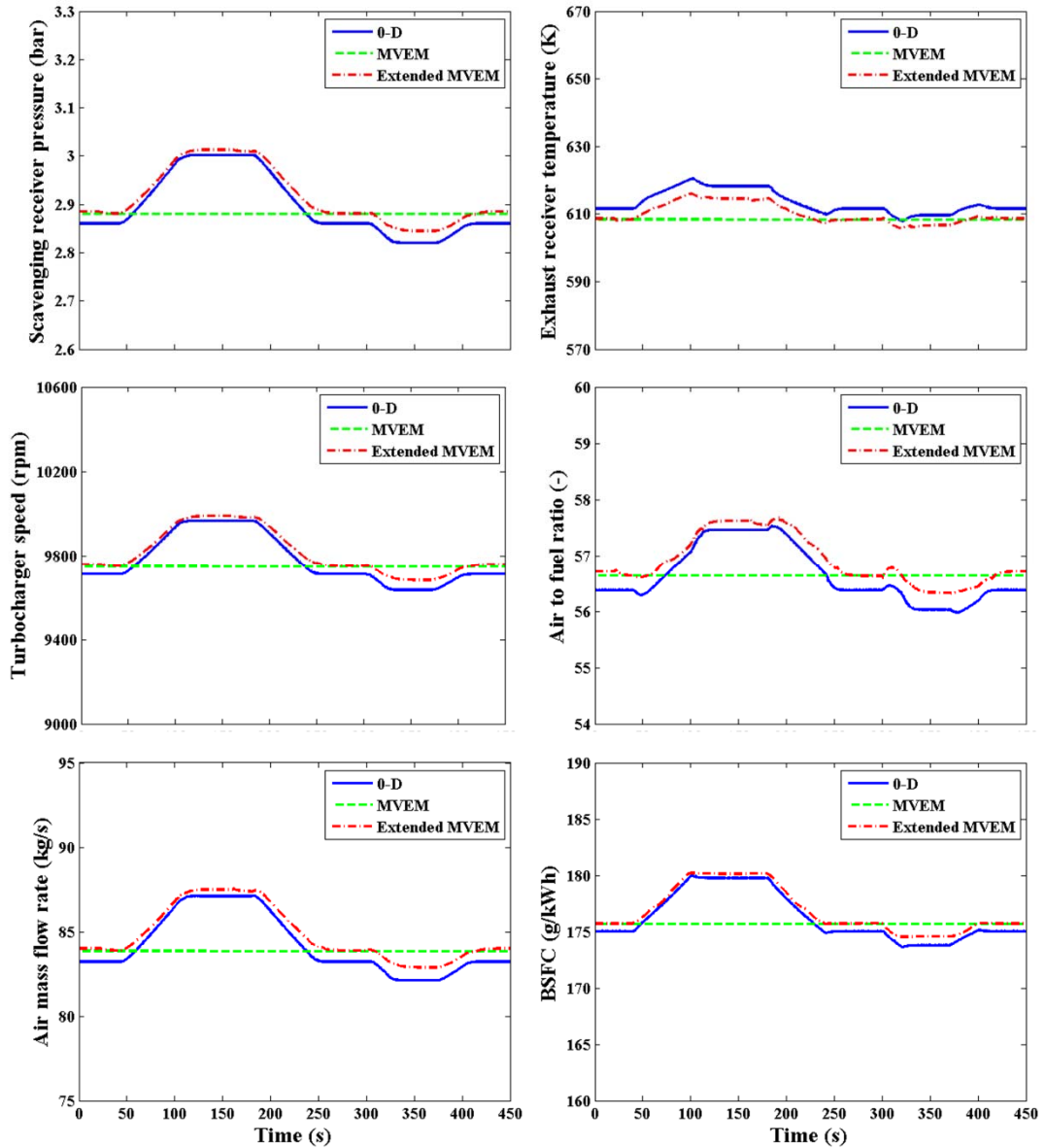


Fig. 14. Simulation results for the engine transient operation with SOI changes.

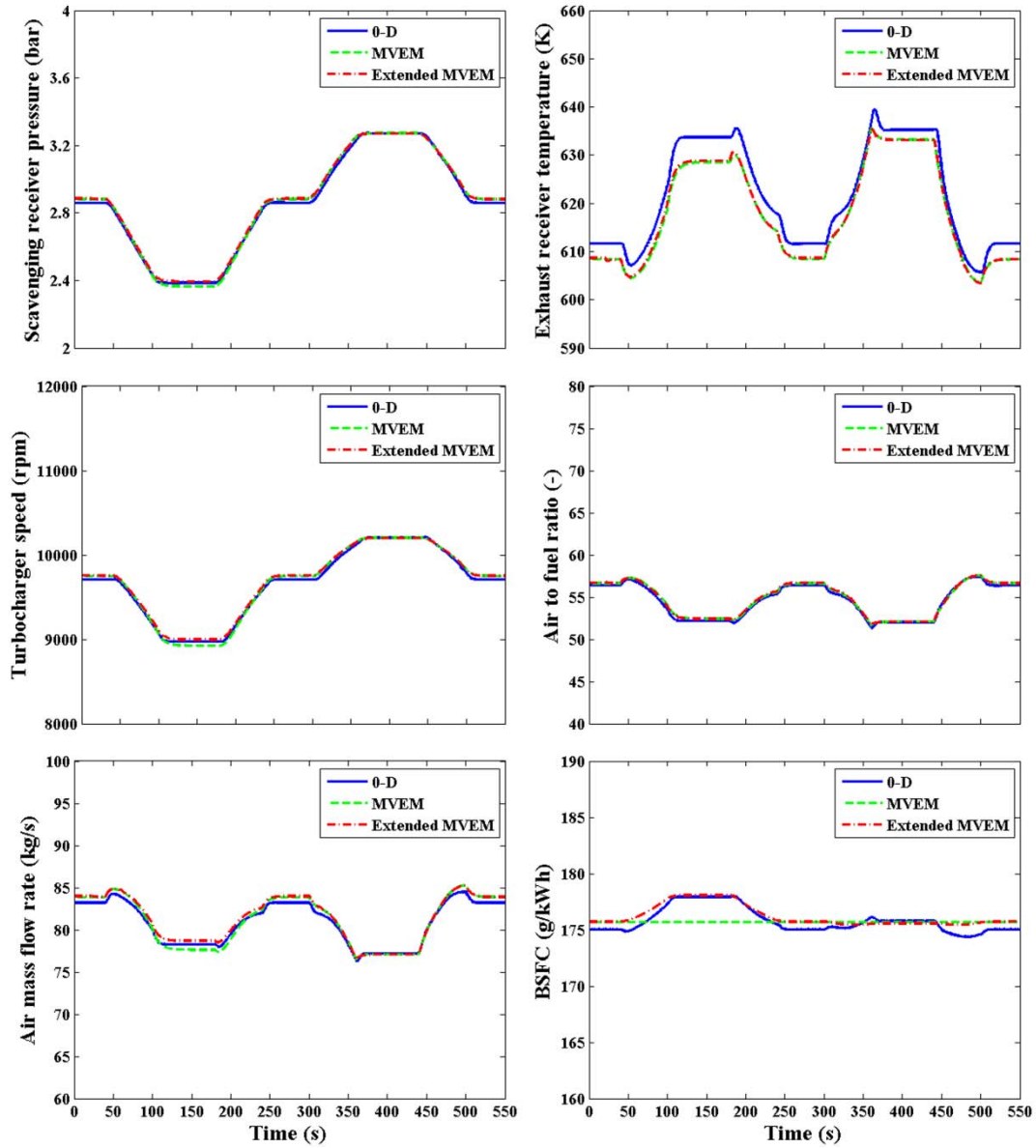


Fig. 15. Simulation results for the engine transient operation with turbine area changes.

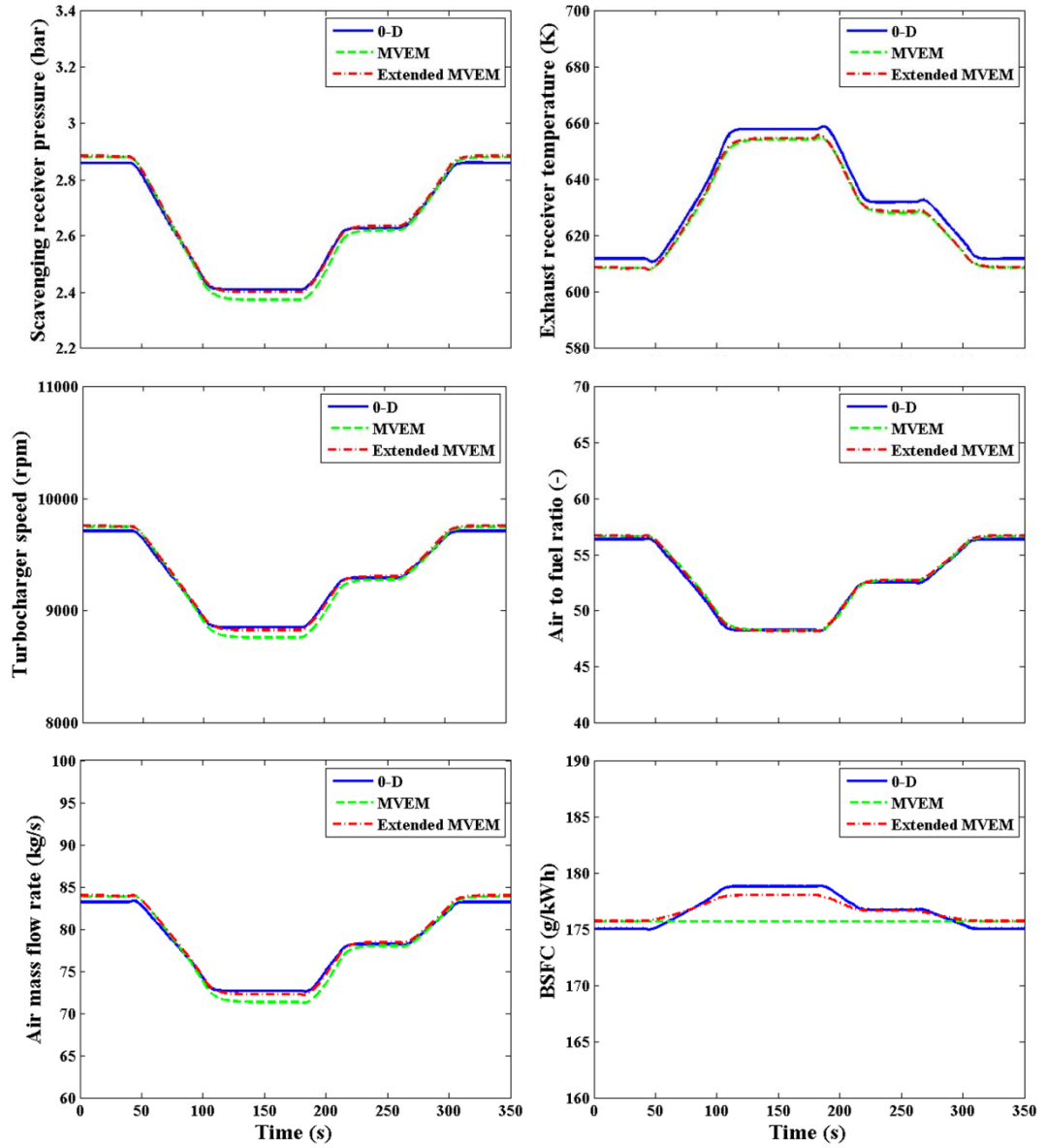


Fig. 16. Simulation results for the engine transient operation with exhaust gas bypass changes.

Table 1 The combustion model constants in zero-dimensional model.

a	10
m	0.93
Combustion duration (°CA)	47
Combustion air to fuel equivalence ratio	2.13
Reference engine speed (r/min)	85.4

Table 2 MAN Diesel & Turbo 7K98MC engine parameters [50].

Bore	980 mm
Stroke	2660 mm
Number of cylinders	7
Brake power at MCR	40055 kW
Engine speed at MCR	94 r/min
BMEP at MCR	18.2 bar
Compression ratio	17.5
Connecting rod length	3220 mm
EVO	74°CA before BDC
EVC	87°CA after BDC
SPO	42°CA before BDC
SPC	42°CA after BDC
Turbocharger units	3

Table 3 Percentage errors of the predicted parameters against experimental data from shop trials.

Model	Zero-dimensional model				MVEM			
	100	75	50	25	100	75	50	25
Engine load (% MCR)	Error (%)							
Brake power	1.02	1.01	0.99	0.92	1.03	1.01	0.99	0.94
BSFC	-0.16	-0.55	0.08	-0.18	0.25	-0.19	-0.03	-0.17
Turbocharger speed	-0.03	0.41	1.47	4.52	0.85	0.82	0.25	3.72
Scavenging air receiver pressure	-1.39	-0.40	0.89	0.54	0.18	0.29	-0.68	0.24
Exhaust gas receiver pressure	0.20	2.23	4.11	3.13	1.38	2.66	2.41	2.72
Scavenging air receiver temperature	0.72	0.39	0.45	0.24	1.10	0.24	0.22	0.21
Exhaust gas receiver temperature	-0.46	-0.48	-1.08	0.37	-0.02	-1.01	-1.65	-0.26
Exhaust gas temperature after turbocharger	2.52	1.18	0.99	3.25	2.64	0.35	0.67	2.66
Maximum cylinder pressure	-0.71	-0.07	1.46	0.59	-	-	-	-
Cylinder compression pressure	-0.81	0.23	0.86	1.16	-	-	-	-

Table 4 Coefficients values for Equations (3), (4) and (5).

	k_1	k_2	k_3
$\Delta\zeta_{SOI}$	$9.649 \cdot 10^{-3}$	$5.358 \cdot 10^{-4}$	$1.908 \cdot 10^{-4}$
$\Delta BSFC_{SOI}$	$4.831 \cdot 10^{-3}$	$3.920 \cdot 10^{-3}$	$4.759 \cdot 10^{-4}$

$$\Delta BSFC_{VGT} \quad -3.484 \cdot 10^{-1} \quad 4.079 \cdot 10^{-1} \quad 2.640 \cdot 10^{-1}$$

Table 5 Constants of Equation (10).

k_1	k_2	k_3	k_4	k_5	k_6
2.359	-1.142	$4.044 \cdot 10^{-2}$	$-5.176 \cdot 10^{-1}$	5.899	$2.748 \cdot 10^{-2}$

Table 6 The examined combinations of SOI and turbine area changes at different loads.

Case number	1	2	3	4	5	6	7	8
Engine load (%)	25							
SOI change (°CA)	-2				+2			
Turbine area change (%)	-20	-10	+10	+20	-20	-10	+10	+20
Case number	9	10	11	12	13	14	15	16
Engine load (%)	50							
SOI change (°CA)	-2				+2			
Turbine area change (%)	-20	-10	+10	+20	-20	-10	+10	+20
Case number	17	18	19	20	21	22	23	24
Engine load (%)	75							
SOI change (°CA)	-2				+2			
Turbine area change (%)	-20	-10	+10	+20	-20	-10	+10	+20
Case number	25	26	27	28	29	30	31	32
Engine load (%)	100							
SOI change (°CA)	-2				+2			
Turbine area change (%)	-20	-10	+10	+20	-20	-10	+10	+20

Table 7 Models execution time comparison.

	0-D	MVEM	Extended MVEM
Transient run	Execution time (s)		
Case (a)	26827	19	44
Case (b)	31496	26	52
Case (c)	22217	21	39