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Abstract—The increasing share of volatile and inverter-based energy sources render electric power grids increasingly susceptible to disturbances. Established Load Frequency Controls (LFCs) schemes are rigid and require careful tuning, making them unsuitable for dynamically changing environments. In this paper, we present a fast and tuningless frequency control approach that tackles these shortcomings by means of modern grid monitoring and communications infrastructures in a two-fold concurrent process. First, direct observation of supply and demand enables fast power balancing decoupled from the total system dynamics. Second, primary resources are actively involved in frequency restoration by systematic adjustment of their frequency reference setpoints. In contrast to the commonly used Automatic Generation Control (AGC), the proposed Direct Load Frequency Control (DLFC) does not require an integrator for frequency control in the closed loop even under partial grid observability. The approach is Lyapunov-stable for a wide range of system parameters, including ramping limits of controlled resources. A performance study against AGC has been conducted on a three-area power system in simulations as well as in a real laboratory grid with an installed generation capacity of 110 kW.

Index Terms—Automatic Generation Control, Distributed Systems, Load Frequency Control, Low Inertia Systems, Power Quality, Renewable Energy Sources, Web-of-Cells

I. INTRODUCTION

The increasing number of inverter-based Distributed Energy Resources (DERs) and High Voltage Direct Current (HVDC) tielines reduces the inertia of the power system and thereby its ability to withstand disturbances [1], [2]. Established Load Frequency Control (LFC) schemes, notably Automatic Generation Control (AGC), have difficulties coping with the entailed changing dynamics and the volatility of renewable energy sources because of their rigid tuning requirements [3], [4]. A direct consequence is the rising number of frequency violations as reported by the European Network of Transmission System Operators for Electricity (ENTSO-E) [5]. However, the blurring line between Transmission System Operators (TSOs) and Distribution System Operators (DSOs), the expanding monitoring infrastructure, and the availability of new flexibility resources opens new possibilities for LFC [6], [7], [8].

The work presented in this paper was supported by the European Commission under the FP7 project ELECTRA (grant no: 609687).

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The shift towards horizontally integrated grids entails an active management role for DSOs [9]. Their biggest asset is awareness of the available flexibility through monitoring the infrastructure close to the customers and DERs [10]. The ongoing roll-out of Smart Meters (SMs) and Remote Terminal Units (RTUs) [11] steadily increases the monitoring coverage of distribution grids, whose economical and technical benefits for real-time control are highlighted by the European Commission [12], [13]. Information and Communication Technology (ICT) is the key enabling factor, for which reason the development of data management policies, standardized data exchange, and TSO-DSO data interfaces, is being actively pursued [14]. Currently, these efforts are focused on the energy retail market, but regulatory authorities and System Operators (SOs) emphasize the benefits of harnessing flexibility at the distribution level. Regulatory issues concerning data ownership and privacy, as well as questions about the hierarchies between TSOs, DSOs, and third parties, such as aggregators, remain open so far. Nevertheless, it is reasonable to assume that a near-complete observability of the electric grid will be achieved in the foreseeable future.

This paper presents a fast and tuningless LFC approach called Direct Load Frequency Control (DLFC), suitable for dynamically changing power grids, which harnesses modern means of monitoring and communication under the assumption of reasonably high grid observability. The DLFC is simple, consisting only of two algebraic equations and first-order low-pass filters describing two concurrent processes. First, area imbalances are obtained through direct observation of production and consumption, which enables the fast activation of secondary resources. Second, primary resources are actively involved in frequency restoration by systematically adjusting their frequency references. The frequency is effectively treated as a local quantity in our method, as we infer it over the primary resources’ output state with regard to their nominal setpoints. The resulting control loop is largely decoupled from the non-linearities of the actuators; secondary power is only activated in response to local events; and no integrators are required to mitigate steady-state errors if the primary droop capabilities are well-known. Active state data exchange between neighboring areas enables load sharing, and the only free parameter is the control interval.

While we assume a high degree of monitoring coverage, the DLFC is able to perform frequency control also under partial observability. In this case, tieline restoration requires additional observers that are incorporated into the control law.
via an auxiliary term. The auxiliary hook can furthermore be used for other corrective terms like tertiary control, or time synchronization. Analytical and experimental examinations prove the DLFC’s ability to regulate the frequency for a wide range of disturbances, parameters, and uncertainties, as well as under conditions of partial observability and controllability. Its performance stands up to optimally tuned AGCs without the associated parametrization effort.

This paper is structured as follows. Section II-A features a literature review of related works, a detailed description of AGC, and an overview of the proposed DLFC approach. Section III contains the grid model and derivation of the DLFC along with a stability proof using Lyapunov’s direct method. Section IV covers the experimental setup, corresponding parameters, and implementation considerations for verifying the DLFC’s applicability. Section V contains performance comparisons of AGC and DLFC under changing physical parameters using simulations, as well as the experimental verification in the laboratory grid along with a discussion of the results. Finally, Section VI concludes the findings and addresses open issues and potential future research.

II. COMPARATIVE STUDY

This section presents an overview of the literature related to the proposed approach. With AGC being commonly used in present-day secondary control, it is introduced in detail and used as the reference implementation. Its description also sets the scene for the grid modeling in Section III.

A. Literature Review

Studies on LFC for interconnected power systems predominantly focus on two categories: adaptive approaches and Multi-objective Optimization Problems (MOPs).

The PI controllers used by AGC require tuning to achieve the desired performance while ensuring stable operation. Adaptive tuning aims to automatize this process with minimal model knowledge. The adaptive controller used in [15] observes the Area Control Error (ACE) of all involved control areas to calculate a global gain correction factor. Mathematical optimization is performed in [4] using an event-triggered, adaptive dynamic programming approach, whereas [16] relies on sequential quadratic programming taking into consideration the governor limits. The approach in [17] uses a special observer for the chaotic behavior of interconnected controllers as an input to the optimization problem. Machine learning is another take on adaptive control, which operates by observing solely performance metrics without models. Examples are the fuzzy control approach in [18] and the Adaptive Neuro-Fuzzy Inference System (ANFIS) approach in [19].

MOPs aim to find optimal setpoints bearing on the observed states and underlying physical models. Model Predictive Control (MPC) incorporates the current and future constraints on a system to solve the MOP. A centralized approach suitable for smaller synchronous areas, like the Nordic grid, is investigated in [20]. The distributed MPC (DMPC) presented in [21] decomposes large problems into smaller ones, which are then solved independently and reassembled using active data exchange. Parameter uncertainties are explicitly accounted for by the robust DMPC approach in [22].

In-depth reviews of the mentioned control strategies and many more are presented in [23], [24]. Compared to the proposed DLFC, however, most approaches have drawbacks regarding their practical realization. The stability of adaptive controllers in interconnected systems is difficult to prove, particularly in the presence of the time delays inherent in ICT-based systems [25]. On the other hand, approaches requiring accurate state-space representations are strongly dependent on the accuracy of the model. The complexity of large-scale grids in the presence of the rising number of DERs, faster system dynamics, as well as the necessity of deploying distributed versions of the algorithms across utilities, render the implementation of approaches like MOP very challenging.

B. Automatic Generation Control

AGC is widely used in secondary control for its simplicity and well-understood behavior. Its input signal is the ACE $P_{\text{ACE}}^i = \Delta P_{\text{tie}}^i + B_i \Delta f_i$, with the tie line error $\Delta P_{\text{tie}}^i = P_{\text{tie}}^i - P_{\text{tie}}^0$ and the bias factor $B_i$ [26]. The net power interchange $P_{\text{tie}}^i$ between neighboring areas is scheduled at $P_{\text{tie}}^0$. The bias factor $B_i$ is an estimation of the area’s droop gain (frequency-response characteristic) $k_i = \frac{1}{R_i} + D_i$, including the primary devices’ speed droop $R_i$ and the damping factor $D_i$ of frequency dependent loads. AGCs are typically realized as PI-controllers

$$P_{\text{sec}}^i = V_i^P \delta_i^P + \frac{1}{T_i} \int_{t_0}^{t} P_{\text{ACE}}^i (\tau) \, d\tau \quad (1)$$

using the proportional gain $V_i^P$ and the integral time constant $T_i$. The determination of these parameters is done by observing the area response to major grid events (such as a tripping prime mover), with further adjustments during normal operation. The resulting secondary power setpoint $P_{\text{sec}}^i$ gets subsequently dispatched to the units participating in secondary control. Fig. 1 shows the corresponding signal flows.

C. Overview of the Proposed Approach

The DLFC is based on a set of assumptions regarding ICT and monitoring as described in Section I, which transcends the capabilities of traditional control areas. Therefore, we refer to them as Cells to provide a clear distinction. More information on the Web-of-Cells concept can be found in [27] and [28].

In a nutshell, Cells have the following capabilities: (i) A high degree of observability using direct measurements, State Estimation (SE), and/or lumped information from aggregators, which are combined in an Electrical Data Observer (EDO); (ii) The primary resources used for secondary control allow changing their reference frequency setpoints remotely; (iii) The droop gains of the primary resources under control are well known; (iv) Neighboring Cells exchange state information. Quality-of-Service of the communications is not investigated in this paper; however, the corresponding demands of the DLFC are low, as this is only needed for load sharing but not frequency control. A study of the influence of networking uncertainties on LFC was conducted in [29].
The signal flows of the DLFC and the AGC are shown side-by-side in Fig. 1. On the DLFC side, the EDO acquires state information from the Cell, and the auxiliary block allows for incorporating additional corrective powers. The primary devices perform Frequency Containment Control (FCC) and actively participate in secondary control as part of the method. The FCCs report their droop gains and output powers to the EDO, which forwards the aggregate values to the DLFC, and takes the reference frequency signal in return. Neighboring Cells appear as atomic devices with droop capabilities, and as such they exchange state information, similarly to the FCCs. Both LFCs feed their power regulation signal into a dispatcher that evaluates the participation factors for all plants bidding into secondary control. Economic dispatch strategies for liberalized grids can be found in [30]. The mathematical description of the DLFC is presented in the following section.

III. METHODOLOGY

The DLFC formulation uses the definitions of variables in Section II-B and Fig. 1, a generation-oriented frame of reference (power flows into Cells are positive), and the constants are positive where applicable.

A. Cell Modeling

The change of frequency (rotational speed of synchronous generators) is a function of generation and load imbalances $P_{imb}$ described by the swing equation

$$J \omega \dot{\omega} = P_{imb}$$

(2)

with the inertia $J$ and the (angular) frequency $\omega = 2\pi f$

[26]. Within a synchronous area $\mathcal{A}$, we define a neighborhood $\mathcal{N}_i = \{i, \mathcal{AC}_i\} \subseteq \mathcal{A}$ to describe its dynamic behavior using (2). The Cell under consideration is denoted by $i$, and $j \in \mathcal{AC}_i$ are the adjacent Cells coupled over tie-lines with the breaker state $\delta_{ij}(n)$. The neighborhood is described by

$$J = J^{pri,c} + J^{unc} = J_i + \sum_{j \in \mathcal{AC}_i} \delta_{ij} J_j,$$

(3)

$$P_{imb} = P^{pri,c}_i + P^{pri,ac}_i + P^c + P^{unc}_i + P^{tie}_i + P^{uno},$$

$$= f^{sec}_i + \sum_{j \in \mathcal{AC}_i} \delta_{ij} P^{imb}_{ij}.$$  

(4)

$J^{pri,c}$ is the combined inertia of the controllable synchronous machines, whereas $J^{unc}$ includes uncontrollable generators and other resources like synchronous condensers. $P^{pri,c}$ and $P^{pri,ac}$ are the active power contributions of the controllable and uncontrollable primary resources (including synchronous machines, inverter-based devices and frequency-dependent loads), $P^c$ is that of the directly controllable devices and aggregated flexibility resources, $P^{uno}$ is that of the uncontrollable resources, and $P^{tie}$ is the net interchange over tie-lines. $P^{uno}$ represents the unobserved generation and consumption that lacks direct feedback into the control loop. The power output of the primary resources is

$$P^{pri}_i = P^{pri}_0 - k \Delta f,$$

with the resources’ power being $P^{pri}_0$ at $f_0$, their total droop gain $k$, and the frequency deviation $\Delta f = f - f_r$. The reference frequency $f_r$ can be remotely adjusted on the controllable primary resources and is $f_0$ for all others.

B. Proposed Secondary Control

The DLFC consists of two concurrently operating control stages that enable frequency control without the need for an integrator. Direct observations of electric power production and consumption are used to determine the secondary power setpoint, and remaining mismatches (e.g., due to partial observability or measurement errors) are systematically captured by primary resources. The tasks of primary (droop control) and secondary (balancing) resources of established control schemes are preserved but their activation is conducted differently, which is described in the following.

Secondary control executes at intervals of $T^{sec}$; the integer $n$ indexes the discrete-time sequence $t = n T^{sec}$.

1) Direct Power Balancing: The ACE infers the area imbalance over the measured frequency and the tie-lines’ active power flows. Both quantities are dynamically coupled to the primary response of the whole synchronous area, against which the AGC PI-parameters need to be tuned. The DLFC circumvents this issue by using the aggregate power balances from within the area instead of the area boundaries. Determination of secondary power setpoints is therefore decoupled from the external grid.

The total observable power of one Cell is

$$P^{obs}_i(n) = P^{pri}_i(n) + P^{sec}_i(n) + P^{pri,ac}_i(n) + P^{tie}_i(n),$$

(6)

with the sum of all closed tie-line schedules,

$$P^{tie}_{0,i,j}(n) = \sum_{j \in \mathcal{AC}_i} \delta_{ij} P^{tie}_{0,i,j}(n),$$

(7)

features all powers of (3) directly captured by the metering system. One notable difference is the use of setpoint values instead of actual measured states for some quantities. State information about primary resources’ deviations from their intended setpoints are needed for frequency control in Section III-B2, whereas the avoidance of the actual state of tie-lines decouples the power balancing response from the other Cells. The optimal secondary power setpoint therefore becomes

$$P^{sec}_i(n + 1) = -P^{obs}_i(n) + P^{max}_i(n),$$

(8)
with the auxiliary power term $P_{\text{aux}}$ used for hooking in additional corrective terms (e.g., tieline observers to detect remaining load or generation unobserved by the power matching stage, or time corrections). Mismatches of observed and actual imbalances are handled in the next step.

2) **Primary Frequency Control:** Primary resources adjust their power output based on the locally measured frequency, as described in (5). The frequency can therefore be found indirectly, by means of the deviation of the resources’ output from their operating points at $f_0$, according to $\Delta P_{\text{pri},c} = P_{\text{pri},c} - P_0 = -k_c \Delta f$. This effectively expresses the frequency as a local instead of a global quantity, which the DLFC then uses for systematically adjusting the primary reference frequency $f_r$ within the Cell. Hence, a Cell’s secondary control reacts as quickly as allowed by its primary and secondary resources together, irrespectively of the dynamics of the rest of the synchronous system.

The steady-state balance neighborhood $\mathcal{N}_{\mathcal{H}_i}$ is

$$0 = \Delta P_{\text{pri},c} + \Delta P_{\text{pri},uc} + \Delta P_{\text{tie}}^r + P_{\text{aux}},$$

(9)

with the primary resources covering $\Delta P_{\text{pri},c}$, which is not compensated by the power balancing stage in Section III-B1. Applying $\Delta P_{\text{pri},c} = -k_c (f - f_r)$ to (9) and rearranging for $f_r$ results in $f_r = f - \frac{1}{k_c} (\Delta P_{\text{pri},uc} + \Delta P_{\text{tie}}^r + P_{\text{aux}})$, which is equivalent to $f_r = f + \frac{\Delta P_{\text{pri},c}}{k_c}$. Setting $f = f_0$ yields the optimal reference frequency

$$f_{r,i}^*(n+1) = f_0 + \frac{\Delta P_{\text{pri},c,i}(n) + \sum_{j \in \mathcal{A}_C} \delta_j(n) \Delta P_{\text{pri},c,j}(n)}{k_c^i(n)} \sum_{j \in \mathcal{A}_C} \delta_j(n) k_c^j(n)$$

(10)

for any given steady-state deviation $\Delta P_{\text{pri},c}$ in $\mathcal{N}_{\mathcal{H}_i}$. As (9) also includes the tieline states, the collectivity of Cells are able to cover for saturated Cells that are unable to provide balancing capability.

Assuming that the effective droop gain $k_c$ is not precisely known, the adjusted value $\hat{k}_c = \bar{k}_c (1 + \epsilon)$ is used in (10) to prove stability in Section III-C. Here, the best estimate of $k_c$ is $\bar{k}_c$, which gets slightly increased by the relaxation $\epsilon$. Choosing $\epsilon = 2 \sigma$, $\sigma$ being the variance of $\bar{k}_c$, yields a 95% probability that $\hat{k}_c \geq k_c$.

3) **Low-pass Filtering:** Low-pass filtering of the optimal balancing power $P_{\text{sec},i}(n+1)$ and reference frequency $f_{r,i}^*(n+1)$ serves several purposes in the DLFC: it suppresses measurement noise as well as aliasing effects from the discrete-time sampling. It smooths the secondary response, and it increases the stability margin. The filtered signals

$$P_{\text{sec},i}^*(n+1) = P_{\text{sec},i}(n) + \frac{T_{\omega_L}}{2\pi} (P_{\text{sec},i}^*(n+1) - P_{\text{sec},i}(n)),$$

(11)

$$f_{r,i}(n+1) = f_{r,i}(n) + \frac{T_{\omega_L}}{2\pi} (f_{r,i}^*(n+1) - f_{r,i}(n)),$$

(12)

are acquired using the filter cutoff $\omega_L$ and are sent to the secondary dispatcher and the primary devices, respectively. The filter cutoff is the only free parameter in the controller and must respect the control interval’s Nyquist frequency

$$\omega_L < \frac{\pi}{T_c}.$$

(13)

It can otherwise be chosen as fast as the quality of the input signals allows, which renders the DLFC tuningless.

C. **Proof of Stability**

The stability of the closed control loop is assessed on the continuous system using Lyapunov’s second method [26]. A Lyapunov candidate $V(x) : \mathbb{R}^m \rightarrow \mathbb{R}$ is any function that fulfills the property $V(0) = 0$ for the equilibrium $x_{SS} = 0$. The system is stable if $\forall x : V(x) \geq 0$ and $\forall x \notin \{0\} : V(x) \leq 0$, and $V(x)$ is then called the Lyapunov function.

1) **Continuous System Representation:** We transform the discrete-time controllers using the forward Euler method $y(n+1) = y(n) + T_e c f(y(n))$ and rearrange $f(y(n))$ to the left side to obtain a continuous representation of the system$^1$. Using Eqs. (2)–(8) and (10)–(12) we obtain

$$\dot{z} = f_z(z) = \begin{pmatrix}
-\hat{k}_c (f - f_r) - k_c^r (f - f_0) + P^p + P_{\text{aux}}^p \\
-\omega_L P_{\text{sec},\text{obs}} \sqrt{f_0 - f_r - \gamma^* (f - f_s)} \\
\omega_L P_{\text{sec}} (f_r - f_r^*)
\end{pmatrix},
$$

(14)

with the state vector $z = [f, P_{\text{sec}}, f^{*}_r, f^*_r]^T$, the exogenous input $P^p$, the ratio $\gamma_{\text{obs}} = |P_{\text{sec}}^p|$ representing how much of $P^p$ is observed, and the droop gain distortion $\gamma^* = \frac{k_c}{\hat{k}_c}$.

The proof requires $f(0) = 0$, hence a coordinate transformation of (14) is necessary. Solving $f_z(z_{SS}) = 0$ for the steady-state solution $z_{SS}$ and introducing $x = z - z_{SS} = [x_1, x_2, x_3, x_4]^T$ yields

$$\dot{x} = f_z(x) = f_z(x + z_{SS}).$$

(15)

2) **Lyapunov Function:** The chosen Lyapunov candidate is

$$V(x) = J x_1^2 (\gamma^* \gamma - \gamma^*)^2 \left(\frac{x_1 + f_0}{k_c} \right)^2 + (x_{\text{sec}} - \gamma_{\text{obs}})^2 (1 - \gamma^*)$$

$$+ J f_0 x_3^2 + \frac{1}{2 \beta} \left((1-x_3)(1+x_4) - x_3 - x_4\right)^2,$$

(16)

with the droop gain overestimation factor $\gamma^* = \gamma_c (1 + \epsilon) \geq 1$, the ratio of uncontrolled to controlled primary resources $\gamma_{\text{sec}} = \frac{k_c}{\hat{k}_c} \geq 0$, as well as the placeholders $\alpha = \frac{f_0}{k_c}$, $\beta = T_c f_s \in (0,1)$.

The total time derivative of (16) is

$$\dot{V}(x) = - (1 + \gamma_{\text{sec}})^2 x_1^2 - x_2^2 - \gamma^* x_3^2 - x_4^2$$

$$+ x_1 (x_2 - x_3 + x_4) + 2 x_3 x_4.$$  

(17)

For $\gamma_{\text{sec}} \geq 0$ and $\gamma^* \geq 1$, (17) fulfills

$$\dot{V}(x) \leq -\frac{x_1^2 + (x_1 + x_3 - x_4)^2 + (x_1 - x_2)^2 + (x_4 - x_3)^2}{2}\leq 0.$$  

(18)

3) **Stability Assessment:** An investigation of (16) reveals that either for perfect knowledge of the droop gain of controllable resources ($\gamma^* = 1$) or total observability ($\gamma_{\text{obs}} = 1$), the Lyapunov function is decoupled from the power disturbance $P^p$ and stable for $\forall x_1 \geq -\frac{1}{2} f_0$, which is always fulfilled. Otherwise, the minimal stability range for arbitrary power disturbances is

$$|P^p (1 - \gamma_{\text{obs}}) (1 - \gamma^*)| \leq |k_c (\gamma^* - \gamma_{\text{sec}}) (1 - \gamma^*)| f_0|.$$  

(19)

$^1$Applying the bilinear transform would require the incorporation of fast system dynamics and slow controller intervals in an intricate multi-rate model. Transforming the discrete controller into a continuous state space simplifies analytical stability studies while retaining important properties (e.g., only inertial response at the time of transient load steps, steady-state values).
for $|z_1| \ll f_0$. Because the droop of typical power systems ranges from 1% to 10%, $k_f f_0$ is much larger than the total installed power and $|P^e|$ is therefore always within the stability range during normal operation.

A closer examination of the proof reveals an advantageous property of the DLFC regarding nonlinearities: Ramp limitations of the primary devices participating in the secondary control result in temporarily decreased effective droop gains. Since we showed before that overestimation of the gains increases the stability margin, ramp limitations contribute to the stability of the DLFC, unlike the case of the AGC, where the integrator winds up.

### IV. System Characteristics

The applicability of the proposed DLFC has been verified both in simulations and in a laboratory grid featuring industrial power and metering devices. In the following, the experimental setup and implementation aspects are described.

#### A. Experimental Setup

The experimental facility SYSLAB, located at the Risø campus of the Technical University of Denmark, is a 400 V three-phase grid designed for studying advanced grid control and communication concepts. It has 16 busbars and 116 automated coupling points, as shown in Fig. 2, spread across an area with a diameter of about 1 km. A wide range of DERs (wind turbines, solar panels, a Diesel generator, controllable loads) can be remotely operated in various topological configurations over a distributed monitoring and control platform.

The system configuration used in Fig. 2 is made up of three Cells in meshed topology. Connected parts are marked in red and emphasized in the corresponding single-line diagram underneath, followed by the location of the Cell controllers as well as the communication links between them and the devices. The properties of the components are listed in Table I, where $P_{nom}$ is the nominal device power, $P_{min}$ and $P_{max}$ are the lower and upper limits of the operating range, and $P_b$ is the base operating point, where applicable. Devices providing the primary response are marked with 1, and II indicates participation in the secondary control. The diesel operates at a fixed droop of 5% as the grid-forming unit in island mode, and is the only component with a rotating mass. It covers, together with the four-quadrant inverter of the vanadium redox fuel battery, the reactive power flows caused by cables and thyristors.

#### B. DLFC Implementation

##### a) Controller Settings: The secondary control is executed at intervals of $T_{sec} = 1$ s in all scenarios. The low-pass cutoff frequency is $\omega_{LP} = \frac{1}{2} T_{sec}$ according to (13).

##### b) Frequency Control: Remote adjustment of the reference frequency $f_r$ on selected primary resources during operation is required by the DLFC. The diesel supports this feature via its off-the-shelf governor, as does the battery via a custom-built controller.

##### c) Secondary Dispatch: Cell 1 uses the dumpload for secondary control because the diesel’s base power is immutable in islanding mode. The battery conducts both primary and secondary control in Cell 2, making Mobile Load 1 available for triggering unobserved disturbances. Mobile Load 3 is used in Cell 3 for secondary control.
TABLE II
CELL PROPERTIES FOR THE CONSIDERED SIMULATION SCENAROIS

<table>
<thead>
<tr>
<th>Scenario</th>
<th>( J_{hi} )</th>
<th>( J_{lo} )</th>
</tr>
</thead>
<tbody>
<tr>
<td>Cell 1</td>
<td>1 2 3</td>
<td>1 2 3</td>
</tr>
</tbody>
</table>

- Inertial constant \( H (s) \) @ \( S_{max} = 60 \text{kVA} \): 4.112 4.112 0.411 0.411 0.411 0.041
- Ramp limit \( P_{ramp} \) (kW s\(^{-1}\)): 2 5 10 20 50 10
- Secondary delay \( T_{sec} \) (s): 5 2.5 1 0.5 0.25 0.1
- Primary regulating capacity (kW): 48 30 0 48 30 0
- Primary drop gain \( k^p \) (kW Hz\(^{-1}\)): 19.2 9.6 0.0 19.2 9.6 0.0
- Primary drop (%): 5.00 6.25 0.0 5.00 6.25 0.0
- AGC proportional gain \( k^P \) (1): 0.065 0.09 0.1 0.065 0.09 0.1
- AGC integral time constant \( T_i \) (s): 12.5 9.091 7.691 12.5 9.091 7.691
- Secondary control interval \( T_{sec} \) (s): 1
- DLFC low-pass filter cutoff \( \omega_{LP} \) (rad/s): 0.333 (see Section IV-B)

TABLE III
SIMULATION EVENTS

<table>
<thead>
<tr>
<th>Event</th>
<th>Time (s)</th>
<th>Parameter</th>
<th>Parameter change</th>
<th>Description</th>
</tr>
</thead>
<tbody>
<tr>
<td>1</td>
<td>10</td>
<td>( \Delta P_{ramp} ) (kW)</td>
<td>0 \rightarrow -5</td>
<td>Load in Cell 1 increased</td>
</tr>
<tr>
<td>2</td>
<td>80</td>
<td>( \Delta P_{ramp} ) (kW)</td>
<td>-5 \rightarrow 0</td>
<td>Load in Cell 1 decreased</td>
</tr>
<tr>
<td>3</td>
<td>90</td>
<td>( \Delta P_{ramp} ) (kW)</td>
<td>0 \rightarrow 5</td>
<td>Load in Cell 3 increased</td>
</tr>
<tr>
<td>4</td>
<td>180</td>
<td>( \Delta P_{ramp} ) (kW)</td>
<td>0 \rightarrow 5</td>
<td>Load in Cell 2 decreased; unobs. by DLFC</td>
</tr>
<tr>
<td>5</td>
<td>170</td>
<td>( \Delta P_{ramp} ) (kW)</td>
<td>0 \rightarrow 5</td>
<td>Load in Cell 2 increased; unobs. by DLFC</td>
</tr>
<tr>
<td>6</td>
<td>210</td>
<td>( \delta_{12} )</td>
<td>1 \rightarrow 0</td>
<td>Tie-line 1-2 opens, tie-line setpoint sums for Cells adjust according to (7)</td>
</tr>
<tr>
<td>7</td>
<td>280</td>
<td>( \Delta P_{ramp} ) (kW)</td>
<td>5 \rightarrow 0</td>
<td>Load in Cell 3 increased</td>
</tr>
</tbody>
</table>

V. RESULTS & DISCUSSION

A. Simulation

The simulation model of SYSLAB in Section IV-A was developed in MATLAB/Simulink. Each Cell is modeled using one swing equation and the physical resources in Section III-A, incorporating the following constraints: Output saturations, ramping rate \( P_{ramp} \) limiting the change of primary and secondary power, and the reaction time \( T_{sec} \) of secondary resources. Tie-lines are modeled as serial admittances as described in [31] without the parallel susceptances.

The DLFC is compared with the AGC for a range of Cell inertias, ramp rates, and control delays. Table II lists the parameters for two scenarios: (i) The high inertia scenario \( J_{hi} \) with long delay times and comparatively low ramp rates of primary and secondary resources, representing mechanical fuel-driven generators; and (ii) the low inertia scenario \( J_{lo} \) resembling SYSLAB setup with fast, inverter-based devices. Cell 3 offers in both scenarios only secondary power control, as it lacks primary resources. Despite Cells 2 and 3 having only inverter-coupled devices in the laboratory, a small inertia value is necessary for simulations.

The frequency deviation \( \Delta f_{5\%} = \frac{1}{20} |P_{step}|(\sum_{k} b_k)^{-1} \), which is 5% of the primary system response to \( P_{step} \) in steady-state, serves as a threshold to assess the settling time \( T_{set} \) for the controllers. \( T_{set} \) is the interval between a load step and the point when \( |\Delta f| = |f - f_0| \) remains smaller than \( \Delta f_{5\%} \) for all times, formally \( T_{set} = \{ T_{set} \in \mathbb{R} \mid \forall t \geq T_{set} : |\Delta f| \leq \Delta f_{5\%} \} \).

We measure overshooting by the deviation of the relative frequency \( \Delta f_{rel} = \frac{|f_{max} - f_0|}{f_{max} - f_0} \), where \( f_{max} \) is the maximum and \( f_{min} \) is the minimum frequency after the load event. This ratio indicates how much the system frequency rises above its nominal value in relation to the minimum detected value, which is predominantly determined by the primary response.

1) Event Response Evaluation: The series of events listed in Table III is applied in each scenario to the system for a simulation period of 300 s. Observed load steps; load steps unobserved by the DLFC; and breaking the meshed topology into a radial configuration by opening tie-line 1-2. All load steps are \( \pm 5 \text{kW} \), to which the parameters of the AGC's PI-controller are tuned in the \( J_{hi} \) scenario so as to deliver a fast and smooth response under the nonlinearities.

Fig. 3a shows the system frequency response for both scenarios and controllers. In scenario \( J_{hi} \), the frequency approaches \( 50 \pm 0.1 \text{Hz} \) after the initial inertia response due to the large secondary control delays. As the AGC was tuned for \( \pm 5 \text{kW} \) steps for optimal performance and no overshooting, its performance is similar for all events, with a settling time of around 20.02 s. The DLFC with a 26.08 s settling time is about 25% slower in comparison, and exhibits around 40% overshooting due to the two concurrent control actions for the observed load events 1 to 4. Both controllers’ responses are bounded by exponentially decaying functions (“trumpet-curves”) defined by \( H(t) = f_0 + Ae^{-t/T} \) in [32]. For the case of the slowest DLFC responses (events 1 and 2), the trumpet parameters are \( A = 0.21 \text{Hz} \) and \( T = 14.5 \text{s} \). This results in a decay time of 34 s to cross the \( \pm 20 \text{mHz} \) margin around the nominal frequency \( f_0 \) after the event, which is well under the 900 s restoration time demanded by the ENTSO-E.

The primary reference frequencies \( f_r \), necessary for frequency control under partial observability, are depicted in Fig. 3b. Changes in the reference signals follow the primary
responses immediately after the load events. As the secondary balancing resources start acting, \( f_r \) returns to \( f_0 \) as the primary powers approach their nominal operating points \( P_{\text{nom}} \). No overshooting occurs for unobserved events 5 and 6 because no direct power balancing takes place, and \( f_r \) differs from \( f_0 \) as long as the unobserved power persists. The overall reaction time is decreased in this case. Opening the tieline at event 7 makes Cell 3, which does not participate in primary control, the only physical neighbor of Cells 1 and 2. Hence, the reference frequencies start to diverge because of the different local ramp rates. Load sharing between the Cells is no longer proportional, but stable frequency control is maintained.

The situation between the controllers turns in the \( J_{lo} \) scenario where the DLFC only needs 16.2 s to settle, approaching the 95\% settling time of 9 s for a first-order low-pass filter with a cutoff of \( \omega_{LP} = 3 \text{ rad s}^{-1} \). Overshooting drops to around 14\%. The AGC does not benefit from the faster system response and its performance gets even worse, causing even longer frequency excursions.

The powers in Fig. 4 reveal the fundamentally different behavior of AGC and DLFC. Fig. 4a shows the active involvement of the primary resources in frequency control, as opposed to the normal droop response with AGC. In the case of the secondary power response in Fig. 4b, AGC responds to all deviations in frequency or tieline during transients, causing secondary resource activations in Cells 1 and 2 (but not Cell 3, which lacks frequency dependent resources) regardless of the location of the event. The DLFC, on the other hand, only activates secondary resources if the event happened in its corresponding Cell, with the primary resources catching unobserved events. Consequently, the tieline power deviations

caused by observed events and topological changes are mitigated faster than by the AGC.

Events not directly captured by the system, however, cause deviations in the primary devices and tielines that need to be addressed with dedicated observers over the auxiliary hook in (6). It has to be noted that events 5 and 6 are merely meant to demonstrate the DLFC’s frequency control capability even when significant load changes are not captured by the measurement system. Under normal operation, entirely unobserved load events in the magnitude of the rated generation are highly unlikely to occur. Thus, tieline deviations would be considerably smaller in practice.

2) Sensitivity Analysis: That the DLFC is tuningless, unlike the AGC, is quantified by analyzing the system response to a single load step in Cell 1 for parameter variations between the two extremal cases of Table II. The multiplier \( \mu_{\text{step}} \) scales the step’s magnitude by \( P_{\text{step}} = \mu_{\text{step}} P_0 \). In Cells 1 and 2 the multiplier \( \mu_{\text{speed}} \) scales the Cells’ inertias and ramp rates by \( J = \mu_{\text{speed}} J \) and \( P_{\text{ramp}} = \mu_{\text{speed}} P_{\text{ramp,hi}} \), respectively. The secondary response times vary with \( P_{\text{delay,hi}} = \mu_{\text{speed}}^{-1} P_{\text{delay,hi}} \).

Fig. 5 shows the settling times \( T_{\text{set}} \) for variations of \( \mu_{\text{step}} \) and \( \mu_{\text{speed}} \). The AGC naturally exhibits good performance around the operating point for which they were tuned. However, moving away from that point reveals peculiarities of applying PI-controllers to nonlinear systems. First, the AGC’s settling time does not necessarily decrease with smaller load steps, and second, neither does it benefit from faster systems. Instead, its performance gets even worse because of the fundamentally changing system response. The DLFC on the other hand has a slightly worse performance than the AGC in the considered high inertia scenario but responds much more predictably to
changing environmental conditions. Smaller load steps and/or faster system responses lead to short settling times in virtually all considered cases, without the need for tuning.

The overshooting characteristic of the DLFC for variations of $\mu_{\text{step}}$ and $\mu_{\text{speed}}$ is depicted in Fig. 6. As demonstrated before in Fig. 3, the maximum peak recedes with faster system parameters. Variations of the step size reveal that the relative overshooting decreases with bigger steps. Thus, ramp limitations dampen the control response and increase the stability margins, as predicted by the stability proof in Section III-C. In contrast, the AGC requires careful tuning to prevent the controller’s integral term from winding up.

3) Small-Signal Analysis: A small-signal analysis has been conducted on the three-area system to study the frequency response of the two simulation scenarios described in Section V-A. The system is analytically linearized around $f_0$ in steady-state and includes secondary response delays, which are a degrading performance factor particularly in the high inertia case. System input is the load disturbance in Cell 1, and the output is the system frequency. The magnitude of the frequency response is normalized to the combined droop gain of the three Cells, for which the parameters of Table II apply.

Fig. 7 shows the response for the AGC and DLFC in the high and low inertia cases. Both controllers behave similarly in the natural system frequency range between 0.1 Hz to 1 Hz determined by the inertia constants and primary response. There, the response magnitude is mainly determined by the total droop capability of the three-area system. The AGC was optimally tuned for the high inertia case and consequently exhibits a smoother response than the DLFC in the considered range. Inertia dominates the suppression of higher frequency disturbances, resulting in a $-20\,\text{dB}$ falloff in all investigated cases. The performance gain of the DLFC over the AGC is apparent for lower frequencies. Whereas the AGC shows a $-20\,\text{dB}$ falloff towards lower frequencies due to its integrator, the DLFC has $-40\,\text{dB}$ because of the concurrent power matching and reference frequency control mechanisms. Additionally, the DLFC takes advantage of the faster system dynamics in the low inertia case, confirming the findings of Fig. 3 and Fig. 5. The DLFC’s speed manifests in a higher initial phase compared to the AGC, but both controllers remain between $-90^\circ$ to $180^\circ$ and operate stably.

B. Experiment

Experimental verification of the DLFC’s practical applicability was conducted on the setup described in Fig. 2 and Table I. In contrast to the simulations, the SYSLAB environment exhibits parameter uncertainties and unmodeled dynamics such voltage dependencies. The DLFC was implemented in Java and executed on SYSLAB’s headless computer nodes, which provide access to the devices via Java RMI calls. Inter-Cell communication was realized with JeroMQ, an open-source library of the ZeroMQ (ØMQ) protocol stack.

Fig. 8 shows the system and reference frequencies resulting from the events in Table IV. A running mean filter with a width of $\pm 10\,\text{s}$ was used to obtain $f$ from the measured frequency $f$. Wind turbines, solar panels, and the randomly charging and discharging EV created additional disturbances on the islanded system. Cloudy and gusty weather during the experiment caused low PV output and highly fluctuating power production on the part of the wind turbines.

Starting with primary control only, imbalances caused deviations from $f_0 = 50\,\text{Hz}$ that are particularly clear after event 1, when Mobile Load 1 in Cell 2 was turned on. Following the activation of the secondary control at event 2, the system frequency immediately moved towards $f_0$, with
the primary resources covering the unobserved Mobile Load 1 and the missing balancing power of Cell 2 (discussed later). Commencing state publishing of $P_{\text{pri,uo}}$ and $k^c$ between the Cells at event 3 enabled load sharing due to the alignment of the reference frequency setpoints, which returned towards $f_0$ after turning off Mobile Load 1 at event 4. As in the simulations, opening the tieline 1-2 at event 5 appears like turning off state publishing because Cell 3 does have primary resources. The frequency references diverge based on the resources’ response speeds and only realign again after closing the line at event 6. Averaging the frequency between 215 s to 750 s yields exactly $f = 50.0$ Hz.

The primary power responses in Fig. 9a show that the primary resources operate around their base setpoints $F_{\text{pri,c}}^0$ in times of high observability (between events 4 and 5 and after 6). Having virtually no solar production, the power balancing stage of Cell 2 reacts only to the topological changes, while Cells 1 and 3 meet their respective local demands as the secondary powers in Fig. 9b illustrate. Cell 3, also lacking PV support, is only partly able to match its power demand, as mentioned earlier. This mismatch appears like yet another unobserved load to Cells 1 and 2 and is consequently accounted for by their primary resources. While the frequency control of the DLFC works under partial observability, Fig. 9c confirms that tieline balancing requires high observability if no auxiliary observer is employed. The primary power deviations in Fig. 9d hold the necessary information for indirect frequency observation in each Cell (see (10)) and are exchanged between Cells along with the Cells’ droop capabilities (which are constant and therefore not depicted) for load sharing purposes. The observed powers used in the secondary power balancing are shown in Fig. 9e, and finally Fig. 9f features the output of unobserved (i.e., not directly measured by the DLFC) devices.

VI. CONCLUSIONS AND FUTURE RESEARCH

The analytical and experimental assessments in this research demonstrate the aptness of the proposed LFC approach for dynamically changing power systems. Given the inexorable advances in monitoring and communication infrastructure, using primary resources for secondary control is both feasible and reasonable for managing low-inertia systems. Direct secondary power regulation allows harnessing the benefits of fast-acting flexibility resources while reducing the number of activations. Consideration of the resources’ capabilities in real time promotes the notion of “plug-and-play,” while scalability is ensured by the neighborhood interaction scheme, which is independent of the network’s total extent. As only power balances are considered, hierarchical structures involving DSOs and aggregators (whose resources may be obfuscated for policy or privacy reasons) can be maintained. While the AGC will remain the secondary control method of choice when only tieline measurements are available, the prospect of a significantly higher degree of observability in future power systems enables all the described advantages of the DLFC.

Future research will address the functional gap between DLFC and AGC. First, deviations of scheduled tieline flows in the wake of unobserved power events must be properly handled. This requires a tieline observer which does not impair the advantages of the proposed approach (i.e., tuningless control, decoupled Cell balancing). Second, the ENTSO-E demands from secondary control that the ACE must not overshoot [32]. This can currently not be guaranteed in the proposed approach, e.g., after unobserved events, for which reason the DLFC’s concurrent control actions need to be systematically dampened to comply with regulations.

REFERENCES


