

1 **Passive flow control for aerodynamic performance enhancement of airfoil**
2 **with its application in Wells turbine – under oscillating flow condition**

3
4 **Ahmed S. Shehata^{1,2*}, Qing Xiao¹, Khalid M. Saqr³, Ahmed Naguib², Day Alexander¹**
5

6 *1) Department of Naval Architecture, Ocean and Marine Engineering, University of*
7 *Strathclyde, Glasgow G4 0LZ, U.K*

8 *2) Marine Engineering Department, College of Engineering and Technology,*
9 *Arab Academy for Science Technology and Maritime Transport, P.O. 1029 AbuQir,*
10 *Alexandria, EGYPT*

11 *3) Mechanical Engineering Department, College of Engineering and Technology,*
12 *Arab Academy for Science Technology and Maritime Transport, P.O. 1029 AbuQir,*
13 *Alexandria, EGYPT*

14 ** Corresponding Author: Ahmed S. Shehata,*

15 *E-mail address: ahmed.mohamed-ahmed-shehata@strath.ac.uk*
16

17 **ABSTRACT**

18 In this work, the passive flow control method was applied to improve the performance
19 of symmetrical airfoil section in the stall regime. In addition to the commonly used first
20 law analysis, the present study utilized an entropy generation minimization method to
21 examine the impact of the flow control method on the entropy generation characteristics
22 around the turbine blade. This work is performed using a time-dependent CFD model of
23 isolated NACA airfoil, which refers to the turbine blade, under sinusoidal flow
24 boundary conditions, which emulates the actual operating conditions. Wells turbine is
25 one of the most proper applications that can be applied by passive flow control method
26 because it is subjected to early stall. Additionally, it consists of a number of blades that
27 have a symmetrical airfoil section subject to the wave condition. It is deduced that with
28 the use of passive flow control, torque coefficient of blade increases by more than 40%
29 within stall regime and by more than 17% before the stall happens. A significantly
30 delayed stall is also observed.

- 1 **Keywords:** Sinusoidal flow; Wells turbine; Passive flow control method; Entropy generation;
- 2 Stall regime; Large Eddy Simulation.

3 **Nomenclature**

A	The total blade area (m ²)
c	Blade chord (m)
C_D	Drag force coefficient
C_L	Lift force coefficient
C_T	Torque coefficient
D	The fluid domain
D_{ss}	Suction slot diameter (m)
f	Cycle frequency (Hz)
F_D	In-line force acting on cylinder (N)
G	The filter function
KE	Kinetic Energy (J)
L_{ss}	Suction slot location from leading edge in chord percentage %
K	Turbulent kinetic energy (J/kg)
Δp	Pressure difference across the turbine (N/m ²)
R_m	Mean rotor radius (m)
S_{gen}	Local entropy generation rate (W/m ² K)
S_G	Global entropy generation rate (W/K)
S_{ij}	Mean strain rate (1/s)
S_t	Thermal entropy generation rate (W/m ² K)
S_v	Viscous entropy generation rate (W/m ² K)
T_o	Reservoir temperature (K)

U	Moving frame velocity (m/s)
\bar{u}_i	Reynolds Averaged velocity component in i direction (m/s)
V	Volume of a computation cell (m ³)
V_a	Instantaneous Velocity (m/s)
V_{am}	Highest speed of axial direction (m/s)
V_o	Initial velocity for computation (m/s)
V_r	Relative velocity (m/s)
\dot{W}	The net-work transfer rate (W/s)
\dot{W}_{rev}	Reversible work transfer rate (W/s)
η_F	The efficiency in first law of thermodynamics
η_S	The second law efficiency
μ	Viscosity (kg/ms)
μ_t	Turbulent viscosity (N.s/m ²)
ρ	Density (kg/m ³)
$\bar{\phi}$	Flow coefficient
ω	Rotor angular speed (rad/s)
$(-\overline{\rho u'_i u'_j})$	Reynolds stress tensor

1

List of Abbreviations	
CFD	Computational Fluid Dynamics
NACA	National Advisory Committee for Aeronautics
OWC	Oscillating Water Column
2D	Two Dimensional
3D	Three Dimensional

2

3

1. Introduction

The techniques developed to maneuver the boundary layer, either for the purpose of increasing the lift or decreasing the drag, are classified under the general heading of boundary layer control or flow control. In order to achieve separation postponement, methods of flow control lift enhancement and drag reduction have been considered. It is important to note that flow control can be defined as a process used to alter a natural flow state or development path (transient between states) into a more desired state (or development path; e.g. laminar, smoother, faster transients) [1]. Moreover, it could be more precisely defined as modifying the flow field around the airfoil to increase lift and decrease drag. This could be achieved by using different flow control techniques such as blowing and suction, morphing wing, plasma actuators, and changing the shape of the airfoil [2]. All the techniques essentially do the same job, i.e. reduce flow separation so that the flow is attached to the airfoil and, thus, reduce drag and increase lift. In regards to flow control techniques, they can be broadly classified as active and passive flow control which can be further classified into more specific techniques [3]. The terms “active” or “passive” do not have any clearly accepted definitions, but nonetheless are frequently used. Typically, the classification is based on energy addition, either on the possibility of finding parameters and modifying them after the system is built, or on the steadiness of the control system; whether it is steady or unsteady. Such studies have demonstrated that suction slot can modify the pressure distribution over an airfoil surface and have a substantial effect on lift and drag coefficients [4-9]. A wide variety of different studies have been conducted on flow control techniques. In actual fact, in 1904, Prandtl [10] was the first scientist who employed boundary layer suction on a cylindrical surface to delay boundary layer separation. The earliest known experimental works on boundary layer suction for wings were conducted in the late 1930s and the 1940s [11-13]. Huang et al. [14] studied the suction and blowing flow control techniques on a NACA0012 airfoil. The combination of jet location and angle of attack showed a remarkable difference concerning lift coefficient as perpendicular suction at the leading edge increased in comparison to the case in other suction situations. Moreover, the tangential blowing at downstream locations was found to lead to the maximum increase in the lift coefficient value. Rosas in [15] numerically studied flow separation control

1 through oscillatory fluid injection, in which lift coefficient increased. The authors in [16]
2 examined the optimization of synthetic jet parameters on a NACA0015 airfoil in different
3 angles of attack to increase the lift to drag ratio. Their results revealed that the optimum jet
4 location moved toward the leading edge and the optimum jet angle incremented as the angle of
5 attack increased. The CFD method has been increasingly used to investigate boundary layer
6 control. Many flow control studies by CFD approaches [17-20] have been conducted to
7 investigate the effects of blowing and suction jets on the aerodynamic performance of airfoils.

8 The major challenge facing oscillating water column ocean energy extraction systems is to find
9 an efficient and economical means of converting flow kinetic energy to unidirectional rotary
10 motion for driving electrical generators [21-25], as seen in Figure 1. The energy conversion
11 from the oscillating air column [26, 27] can be achieved by using a self-rectifying air turbine
12 such as Wells turbine which was invented by A. A. Wells in 1976, see Figure 2 [28-33]. Wells
13 turbine consists of a number of blades that have symmetrical airfoil section. This airfoil section
14 under different conditions with various geometric parameters was investigated by other
15 researchers in consideration of improving the overall system performance. In order to achieve
16 this purpose, different methods were used, such as experimental, analytical and numerical
17 simulation. The main disadvantage of Wells turbine is the stall condition [34]. Aerodynamic
18 bodies subjected to pitching motions or oscillations exhibit a stalling behavior different from
19 that observed when the flow over a wing at a fixed angle of attack separates. The latter
20 phenomenon is referred to as static stall, since the angle of attack is fixed. In the case of a
21 dynamically pitching body, such as an airfoil with large flow rates and a large angle of attack,
22 the shear layer near the leading edge rolls up to form a leading-edge vortex which provides
23 additional suction over the upper airfoil surface as it convects downstream. This increased
24 suction leads to performance gains in lift and stall delay, but the leading-edge vortex quickly
25 becomes unstable and detaches from the airfoil. As soon as it passes behind the trailing edge,
26 however, the leading-edge vortex detachment is accompanied by a dramatic decrease in lift and
27 a significant increase in drag. This phenomenon is called dynamic stall. From Figure 3 it can be
28 noted that Wells turbine can extract power at low air flow rate, when other turbines would be
29 inefficient[35, 36]. Also, the aerodynamic efficiency increases with the increase of the flow

1 coefficient (angle of attack) up to a certain value, after which it decreases. Thus, most of the
2 past studies aimed to 1) improve the torque coefficient (the turbine output) and 2) improve the
3 turbine behavior under the stall condition. In a number of previous studies [37-39], it was
4 concluded that the delay of stall onset contributes to improving Wells turbine performance.
5 This delay can be achieved by setting guide vanes on the rotor's hub [37, 40, 41]. It was found
6 that a multi-plane turbine without guide vanes was less efficient (approximately 20%) than the
7 one with guide vanes. A comparison between Wells turbines having 2D guide vanes and 3D
8 guide vanes was investigated [42, 43] by testing a Wells turbine model under steady flow
9 conditions, and using the computer simulation (quasi-steady analysis. It demonstrated that, the
10 3D case has superior characteristics in the running and starting characteristics. Concerning
11 Wells turbine systems which operate at high pressure values, a multi plane (usually tow stage)
12 turbine configuration can be used. Such a concept avoids the use of guide vanes and, therefore,
13 the turbine would require less maintenance and repairs [37]. The performance of a biplane
14 Wells turbine is dependent on the gap between the planes as it is shown in [37]. A gap-to-chord
15 ratio between the planes of 1.0 was recommended. Experimental results in [44] showed that
16 the use of two twin rotors rotating in the opposite direction to each other was an efficient means
17 of recovering the swirl kinetic energy without the use of guide vanes. The overall performance
18 of several types of Wells turbine design have been investigated in [45] and, a semi-empirical
19 method for predicting the performance has been used in [46]. Similar comparisons were
20 undertaken using experimental measurement in [47]. It can be observed that the contra-rotating
21 turbine had an operational range which was similar to that of the monoplane turbine with guide
22 vanes and it achieved similar peak efficiency as well. However, the flow performed was better
23 than the latter in the post-stall regime. In order to improve the performance of the Wells
24 turbine, the effect of end plate on the turbine characteristics has been investigated in [48, 49].
25 Using an experimental model and a CFD method it was shown that the optimum plate position
26 was a forward type. The peak efficiency increases approximately 4% as compared to the Wells
27 turbine without an endplate. The calculations of the blade sweeps for the Wells turbine with a
28 numerical code by [50] and experimentally with quasi-steady analysis in [51]. As a result, it
29 was concluded that the performance of the Wells turbines was influenced by the blade sweep
30 area.

1 Exergy analysis is performed using the numerical simulation for steady state biplane Wells
2 turbines [52] where the upstream rotor has a design point second law efficiency of 82.3%
3 although the downstream rotor second law efficiency equals 60.7%. The entropy generation,
4 due to viscous dissipation, around different 2D airfoil sections for Wells turbine was recently
5 examined by the authors in [53, 54]. When Reynolds number was increased from 6×10^4 to
6 1×10^5 the total entropy generation increased more than two folds for both airfoils
7 correspondingly. However, when Reynolds number was increased further to 2×10^5 , the total
8 entropy generation exhibited unintuitive values ranging from 25% less to 20% higher than the
9 corresponding value at Reynolds number = 1×10^5 . The efficiency for four different airfoils in
10 the compression cycle is higher than the suction cycle at 2 degree angle of attack. Although,
11 when the angle of attack increases, the efficiency for the suction cycle increases much more
12 than the compression one. This study suggested that a possible existence of critical Reynolds
13 number for the operating condition at which viscous irreversibilities takes minimum values. A
14 comparison between total entropy generation of a suggested design (with variable chord) and a
15 constant chord of Wells turbine was presented in [55]. The detailed results demonstrate an
16 increase in static pressure difference around a new blade and a 26.02 % average decrease in
17 total entropy generation throughout the full operating range. Most of the researchers studied the
18 performance of different airfoils design and different operational conditions where analyzing
19 the problem was only based on the parameter of first law of thermodynamics. In order to form a
20 deeper understanding, it is necessary to look at the second law of thermodynamics since it has
21 shown very promising result in many applications, such as wind turbine in [56-61], and gas
22 turbine in [62-67].

23 Wells turbine consists of a number of blades that have symmetrical airfoil section. This airfoil
24 section under different conditions with various geometric parameters was investigated by other
25 researchers to improve the overall system performance. Different methods were used to achieve
26 this purpose, such as experimental, analytical and numerical simulation. In this work the CFD
27 analysis is used to investigate and analyze the flow around the isolated NACA airfoil, which
28 refers to the turbine blade, under sinusoidal flow boundary conditions, which emulates the
29 actual operating conditions. The force coefficients, such as torque coefficient and the entropy

1 generation value, are calculated and compared under different conditions with various design
2 parameters by analyzing the flow around the airfoil section using CFD software, where the
3 force coefficients are referring to the first law analysis and the entropy generation value is
4 referring to the second law analysis. The objective of the present work is to demonstrate that
5 the performance of airfoil section, which refers to the Wells turbine blade at stall and near-stall
6 conditions, can be radically improved by using passive flow control method such as suction or
7 blowing slot. Therefore, a typical slot is created in the airfoil section, normal to the chord, and
8 due to the pressure difference between the two surfaces. Consequently, a suction effect occurs
9 which delays the stall. Accordingly, there is no need to generate any specific active suction or
10 blowing within the airfoil or the slot. Along with this design, there are two new aspects here.
11 The first is improving the performance of airfoil section for Wells turbine in near-stall
12 conditions. The second is to study the effect of slot in oscillating (i.e. sinusoidal) flow, which is
13 newly compared to the unidirectional flow as in aerodynamics applications. Apart from that, an
14 entropy generation minimization method is used to conduct the second-law analysis as recently
15 reported by the authors in [53, 54]. An investigation on the entropy generation, due to viscous
16 dissipation, around turbine airfoils in two-dimensional unsteady flow configurations, will be
17 carried out. In reference to the literature, no specific unsteady CFD study of the slot effect with
18 sinusoidal flow on the entropy generation rate has been performed for airfoil section of Wells
19 turbine.

20 **2. Mathematical Model and Numerical Approach**

21 The governing equations employed for Large Eddy Simulation (LES) are obtained by filtering
22 the time-dependent Navier-Stokes equations. The filtering process effectively filters out eddies
23 whose scales are smaller than the filter width or grid spacing used in the computations. The
24 resulting equations thus govern the dynamics of large eddies. A filtered variable (denoted by an
25 over-bar) is defined by [68]:

$$26 \quad \overline{\phi}(x) = \int_D \phi(x')G(x, x')dx' \quad (1)$$

1 where D is the fluid domain, and G is the filter function that determines the scale of the
 2 resolved eddies. In FLUENT, the finite-volume discretization itself implicitly provides the
 3 filtering operation[69]:

$$4 \quad \bar{\phi}(x) = \frac{1}{V} \int_V \phi(x') dx', \quad x' \in V \quad (2)$$

5 where V is the volume of a computational cell. The filter function, $G(x, x')$, implied here is
 6 then

$$7 \quad G(x, x') = \begin{cases} 1/V & \text{for } x' \in V \\ 0 & \text{otherwise} \end{cases} \quad (3)$$

8

9 The LES model will be applied to essentially incompressible (but not necessarily constant-
 10 density) flows. By filtering the incompressible Navier-Stokes equations, one obtains [70]

$$11 \quad \frac{\partial \rho}{\partial t} + \frac{\partial \rho \bar{u}_i}{\partial x_i} = 0 \quad (4)$$

$$12 \quad \frac{\partial}{\partial t} (\rho \bar{u}_i) + \frac{\partial}{\partial x_j} (\rho \bar{u}_i \bar{u}_j) = \frac{\partial}{\partial x_j} \left(\mu \frac{\partial \bar{u}_i}{\partial x_j} \right) - \frac{\partial \bar{p}}{\partial x_i} - \frac{\partial \tau_{ij}}{\partial x_j} \quad (5)$$

13 Where τ_{ij} is the sub-grid-scale stress defined by

$$14 \quad \tau_{ij} = \rho \overline{u_i u_j} - \rho \bar{u}_i \bar{u}_j \quad (6)$$

15 The sub-grid-scale stresses resulting from the filtering operation are unidentified, and require
 16 modeling. The majority of sub-grid-scale models are eddy viscosity models of the following
 17 form [71]:

$$18 \quad \tau_{ij} - \frac{1}{3} \tau_{kk} \sigma_{ij} = -2\mu_t \bar{S}_{ij} \quad (7)$$

19 Where \bar{S}_{ij} is the rate-of-strain tensor for the resolved scale defined by:

$$20 \quad \bar{S}_{ij} = \frac{1}{2} \left(\frac{\partial \bar{u}_i}{\partial x_j} + \frac{\partial \bar{u}_j}{\partial x_i} \right) \quad (8)$$

21 and μ_t is the sub-grid-scale turbulent viscosity, which the Smagorinsky-Lilly model is used for
 22 it [72]. The most basic of sub-grid-scale models for ‘‘Smagorinsky-Lilly model’’ was proposed
 23 by Smagorinsky [73] and was further developed by Lilly [74]. In the Smagorinsky-Lilly model,
 24 the eddy viscosity is modeled by:

$$25 \quad \mu_t = \rho L_s^2 |\bar{S}| \quad (9)$$

1 where L_s is the mixing length for sub-grid-scale models and $|\bar{S}| = \sqrt{2\bar{S}_{ij}\bar{S}_{ij}}$. The L_s is
 2 computed using:

$$3 \quad L_s = \min(kd, C_s V^{1/3}) \quad (10)$$

4 Where C_s is the Smagorinsky constant, $k = 0.42$, d is the distance to the closest wall, and V is
 5 the volume of the computational cell. Lilly derived a value of 0.23 for C_s from homogeneous
 6 isotropic turbulence. However, this value was found to cause excessive damping of large-scale
 7 fluctuations in the presence of mean shear or in transitional flows. $C_s = 0.1$ has been found to
 8 yield the best results for a wide range of flows.

9
 10 For the first law of thermodynamics, the lift and drag coefficient C_L and C_D are computed from
 11 the post processing software. The average value for lift and drag coefficient was used to
 12 calculate one value for torque coefficient for each angle of attack. Afterwards, the torque
 13 coefficient can then be expressed as [39, 46, 75]:

$$14 \quad C_T = (C_L \sin \alpha - C_D \cos \alpha) \quad (11)$$

15 The flow coefficient $\bar{\phi}$ relating tangential and axial velocities of the rotor is defined as

$$16 \quad \bar{\phi} = \frac{V_a}{\omega * R_m} \quad (12)$$

17 where the α angle of attack equal to

$$18 \quad \alpha = \tan^{-1} \frac{V_a}{\omega R_m} \quad (13)$$

19 and the torque as:

$$20 \quad Torque = \frac{1}{2} \rho (V_a^2 + (\omega R_m)^2) A R_m C_T \quad (14)$$

21 the efficiency in the first law of thermodynamics (η_F) is defined as:

$$22 \quad \eta_F = \frac{Torque * \omega}{\Delta P * Q} \quad (15)$$

23 The transport equations of such models can be found in turbulence modeling texts such as [76].

24 The second law of thermodynamic defines the network transfer rate \dot{W} as [77]:

$$25 \quad \dot{W}_{rev} - \dot{W} = T_o S_{gen} \quad (16)$$

1

2 Which has been known for most of this century in engineering as the Gouy–Stodola
3 theorem[78].

4 It is possible to express the irreversible entropy generation in terms of the derivatives of
5 local flow quantities in the absence of phase changes and chemical reactions. The two
6 dissipative mechanisms in viscous flow are the strain-originated dissipation and the thermal
7 dissipation which correspond to a viscous and a thermal entropy generation respectively [79].
8 Thus, it can be written,

$$9 \quad S_{gen} = S_V + S_{th} \quad (17)$$

10 In incompressible isothermal flow, such as the case in hand, the thermal dissipation
11 term vanishes. The local viscous irreversibilities therefore can be expressed as:

$$12 \quad S_V = \frac{\mu}{T_o} \phi \quad (18)$$

13 where ϕ is the viscous dissipation term, that is expressed in two dimensional Cartesian
14 coordinates as [79]:

$$15 \quad \phi = 2 \left[\left(\frac{\partial u}{\partial x} \right)^2 + \left(\frac{\partial v}{\partial y} \right)^2 \right] + \left(\frac{\partial u}{\partial y} + \frac{\partial v}{\partial x} \right)^2 \quad (19)$$

16 Equations 18 and 19 were used to create the UDF file, which is used to calculate the local
17 entropy form the FLUENT software. Then, the global entropy generation rate is hence
18 expressed as:

$$19 \quad S_G = \iint_{xy} S_V dydx \quad (20)$$

20 Which is also calculated from the FLUENT software by integral the global value,

21 The next equation is defining the exergy value, which can be written as [80]:

$$22 \quad Exergy = KE + S_G \quad (21)$$

23 and finally the second law efficiency is defined as [56]:

$$24 \quad \eta_s = \frac{KE}{Exergy} \quad (22)$$

1 Where $KE = \frac{1}{2}V^2$

2 From the above equation we can come up with a number of conclusions. On the one hand, that
3 the torque coefficient indicates to the first law efficiency and the global entropy generation rate
4 indicates to the second law and efficiency, in which the increase in torque coefficient leads to
5 increase in the first law efficiency. On the other hand, the decrease in the global entropy
6 generation rate leads to an increase in the second law efficiency.

7 **3. CFD Approach**

8 **3.1. Computational model, solver details and boundary conditions**

9 Two-dimensional numerical models for NACA0015 airfoils were built and validated
10 against experimental measurements under unsteady flow conditions with both non-oscillating
11 velocity, and sinusoidal inlet velocity. The computational domain is discretized to Cartesian
12 structured finite volume cells using GAMBIT code. The application of such boundary
13 condition types [81-84] matches the Green-Gauss cell based evaluation method for the gradient
14 terms used in the solver (ANSYS FLUENT). Numerous tests accounting for different
15 interpolation schemes were used to compute cell face values of the flow field variables. The
16 variables of governing equation which are velocity and pressure, as well as convergence tests
17 have been undertaken. The second order upwind [85] interpolation scheme was used in this
18 work in which it yields results which are approximately similar to such yielded by third order
19 MUSCL scheme in the present situation. In addition, in some cases of the third order MUSCL
20 scheme was given high oscillatory residual during the solution. Figure 4 demonstrates the
21 dimensions of the whole computational domain and the location of airfoil, and it also shows the
22 grid distribution near the wall of the airfoil. Furthermore, the near views of slot mesh can be
23 determined from Figure 5 for different slot diameter. The Quad-Pave meshing scheme
24 (Structured Grid) is used in this work. It was also detected that the solution reaches
25 convergence when the scaled residuals approaches 1×10^{-5} . See Figure 6 for the convergence
26 criteria in the non-oscillating flow and sinusoidal flow inlet velocity. At such limit, the flow
27 field variables holds constant values with the application of consecutive iterations.

1 The axial flow of Wells Turbine is modeled as a sinusoidal wave in this simulation.
2 Therefore, Inlet boundary conditions are set to change as time. In order to apply the inlet
3 boundary condition, inlet velocity with periodic function (see Figure 7) is generated as follows.

$$4 \quad V_a = V_o + V_{am} \sin(\sin 2\pi ft) \quad (23)$$

5 Where t is time period, 6 seconds are set as one period in this simulation considering to
6 the literature survey [84, 86-88]. Time step is set as 0.000296721 seconds in order to satisfy
7 CFL (Courant Friedrichs Lewy) [89] condition equal to 1. The sinusoidal wave condition create
8 various Reynolds number up to 2×10^4 according to the reference [83].

9

10 **3.2. Grid sensitivity test**

11 In order to ensure that the numerical produces results are minimally dependent on the grid size,
12 several grids were tested to estimate the number of grid cells required to establish a reliable
13 model. The grid sensitivity test is performed where 4 grids with different mesh sizes ranging
14 from 112603 up to 446889 cells are investigated. This test shows that for grids with mesh sizes
15 of 312951 cells, gives good result within reasonable computation time (more details about this
16 result in [53]). Therefore, it was selected to conduct the analysis presented hereafter.

17 Figure 8 show the grid sensitivity analysis with respect to cell number across the slot section
18 for one, two, four and eight cells in the transversal direction. It can be noted that the results for
19 the four grids A, B, C and D are approximately the same. On the other hand, by increase the
20 number of cells in the transversal direction, the cells number for the total domain is increase for
21 the four grids A, B, C and D by 312951, 350662, 388637 and 413665 respectively. Therefore,
22 the grid A was selected in order to immunize the solution time of the different cases without
23 impacting on the quality and accuracy of the results.

24 **3.3. LES resolution quality assessment**

25 In the most common practice, in LES, the filter length depends on the resolution of spatial
26 discretization (i.e. grid) in a specified problem. The implication of the filtering technique,
27 which is the backbone of LES, is the question about the resolution of the resolved scales in

1 comparison with the total turbulence spectrum in the flow. An assortment of several attempts
 2 were made to propose and index of LES quality [90, 91]. The most established index of LES
 3 quality was proposed by Pope [92]. Such quality index can be expressed mathematically as a
 4 function $M(x, t)$ of space and time [93] as:

$$5 \quad M(x, t) = \frac{K_{Res}}{K_{Res} + K_{SGS}}$$

6 where K_{Res} and K_{SGS} are the resolved and subgrid modeled turbulent kinetic energy scalars,
 7 respectively. In the present work, K_{Res} can be calculated as: $K_{Res} = \frac{1}{2}(\tilde{u}^2 + \tilde{v}^2)$ and K_{SGS} can
 8 be calculated as $K_{SGS} = \frac{\nu_t^2}{(C\Delta)^2}$ where ν_t is the subgrid modeled turbulent kinematic viscosity as
 9 calculated in the Smagorinsky model as: $\nu_t = L_s^2 |\bar{S}|$, where L_s is the mixing length for subgrid
 10 scales as calculated in equation (10) and Δ is the filter length [94]. Pope [92] has evidently
 11 shown that when $M(x, t) \geq 80\%$ the LES is sufficiently resolved and the flow field is properly
 12 resolved. Literature records support Pope's proposition in numerous and variant flows as
 13 reported in [95-98]. In the present work, the quality index $M(x, t)$ was calculated for the
 14 computational domain and plotted against LES filter length as in Figure (9). It is shown that
 15 $M(x, t) \geq 80\%$ for filter lengths in the range $\Delta \geq 0.01$. In Figure (10) a histogram of the filter
 16 length shows that approximately 98% of the grid has values of $M(x, t)$ larger than 90% which
 17 satisfies Pope's criteria for fully resolved LES.

18 Since one of the work main objectives is to study the stall regime, therefore, an accurate
 19 simulation for the stall must be done. The following Figure (Figure 11) illustrates that a
 20 comparison between different models to simulate two dimensional NACA0015 in an unsteady
 21 flow with stall angle (13.6 degrees) for NACA0015 with Reynolds number equals to 2×10^5
 22 from experimental data [83, 99] was presented. The comparison uses only the stall angle to
 23 identify which model can present it. The Large Eddy Simulation model (LES) gives good
 24 results for the torque coefficient value, while, other models cannot predict the stall angle. The
 25 LES model has shown high disturbance for the path line of the flow stream and the pressure
 26 distribution at the upper surface, which leads to the stall condition. The larger turbulent
 27 separated zone of the LES may be a reason for the lower value of the lift force [100]. The LES

1 has shown that some vortexes were formed and caused to appear a fluctuation behavior of
2 pressure distribution on the upper surface of the airfoil, whereas other models were not able to
3 predict it [101]. On the other hand, the unsteady RANS turbulence modeling has shown a quite
4 dissipative character that attenuates the instabilities and the vortex structures related to the
5 dynamic stall [102]. Therefore, the LES model will be used to investigate the stall behavior.

6 Large Eddy Simulation model was used to model the flow around NACA0015 airfoil in order
7 to give the best agreement with experimental data adopted from [83, 99] and [103]. The Large
8 Eddy Simulation model gives excellent results when they are used to simulate the airfoil in stall
9 condition, according to literature survey [70, 100, 104-110].

10 Although LES is a 3D model by definition, there have been numerous successful attempts to
11 use it in 2D applications. For example, flow over obstacles [111], hump [112], block [113],
12 airfoils [109, 114, 115] and Hills [116]. Other two dimension model applications include the
13 problems dealing with, dam-break [117], mechanism of pollutant [118, 119], heat transfer [120,
14 121], turbulent Convection [122] and Parallel Blade Vortex [123]. The flow under investigation
15 occurs due to sinusoidal velocity signal in the XY plane, with no other velocity signals in other
16 domains. Hence, all the main flow phenomena of interest occurs in the XY plane except for the
17 vortex stretching and secondary shedding which occur in the XZ and YZ planes. The authors
18 have reviewed the 2D assumption of the flow under consideration in their recent extensive
19 review paper [34] and concluded that the 2D assumptions are not influential in the flow
20 structure nor the aerodynamic performance of the airfoil under oscillating flow. Hence, the
21 governing equations were reduced to two dimensional form, and solved accordingly.
22 Consequently, and given the fact that this reduction is physically valid, the method of solution
23 of the governing equation (i.e. LES) must follow the coordinate formalism of the governing
24 equations, hence it was solved as two-dimensional problem. In this work two sets of
25 experimental data were used to validate the numerical model from references. First,
26 experimental data from references [83, 99, 124] are used to simulate and validate the stall
27 condition. Details of the first validation case, where Wells turbine prototype are under
28 investigation, is characterized by the following parameters: hub radius, is equal to 101 mm; tip
29 radius, equal to 155 mm; NACA0015 blade profile with constant chord length, equal to 74 mm;

1 and number of blades, equal to 7. Therefore, the hub-to-tip ratio, and the solidity, is equal to
2 0.65 and 0.64, respectively. The uncertainty in the measurements is 5%. The blades have been
3 produced with composite material reinforced by carbon fiber with suited attachment. Second,
4 experimental data from reference [103] is adopted to simulate and validate the unsteady
5 sinusoidal wave inlet velocity. Details of the second validation case, where experimental data
6 for unsteady forces (F_D) acting on a square cylinder in oscillating flow with nonzero mean
7 velocity are measured. The oscillating air flows are generated by a unique AC servomotor wind
8 tunnel. The generated velocity histories are almost exact sinusoidal waves.

9 For unsteady flow with non-oscillating velocity, Figure 12 shows a very good agreement
10 between the measured torque coefficient from reference [83, 99] and the calculated torque
11 coefficient from CFD result at Reynolds number of 200000. It can be noted that the
12 computational model has approximately the same stall condition value as the reference. The
13 comparison between those results and the percentage of error are listed in Table 1.
14 Furthermore, for an unsteady flow with sinusoidal inlet velocity, Figure 13 and 14 show a good
15 agreement between measured drag force from reference [103] and predicted drag force from
16 CFD at two different frequencies (2 Hz and 1 Hz). It can be shown from Figure 13 and 14 that
17 the computational model has almost the same behavior of oscillating flow condition as the
18 reference; see also the error percentage in Table 2 for the two frequencies. Finally, Figure 15
19 displays the results of computational model under sinusoidal inlet flow velocity with
20 experimental data from [83, 99] and an excellent agreement is achieved. The comparison of
21 these results and the percentage of error are summarized in Table 3. The Large Eddy
22 Simulation computational model has approximately the same stall condition value as the
23 reference.

24 **4. Results and Discussion**

25 A slot with certain diameter at various locations from the leading edge was created with a
26 shape of NACA0015 from reference [83, 99], see Figure 16. The diameter and location for
27 the slot were changed in order to obtain an optimum value. During the compression cycle,
28 this slot suctions the flow from lower surface (high pressure) and blows it to the upper

1 surface (low pressure), see Figure 17. Where, Figure 17 A is for the accelerating flow at 1.3
2 second and B is for the decelerating flow at 1.65 second with Reynolds number equal to
3 190000. Furthermore, this pressure difference affecting on the velocity vector direction, as
4 it can be noted in Figure 17 for the velocity vector of the velocity magnitude. On the other
5 hand, during the suction cycle in Figure 17 C (4.35 second) and D (4.6 second), the slot
6 suctions the flow from the upper surface (high pressure) and blows it to the lower surface
7 (low pressure) in both the accelerating and decelerating flow at Reynolds number equal to
8 190000. It can be also noted that the pressure difference affecting on the velocity vector
9 direction, which it refer to the flow direction. Therefore, it can be concluded that the factor
10 affecting determination of the slot velocity direction is the pressure difference. The slot will
11 be defined as a suction slot in the analysis and results which were presented henceforth. The
12 test cases investigated are under 1) unsteady flow with non-oscillating velocity and 2)
13 sinusoidal wave condition.

14 **4.1. Unsteady flow with non-oscillating velocity**

15 The effect of suction slots in the airfoils behavior will be shown in the following three sections.

16 **4.1.1. Torque coefficient and Stall angle**

17 Figure 18 demonstrates the effect of varying D_{SS} on the torque coefficient at the stall angle
18 (13.6 Degree) from Figure 11 for reference [83, 99]. All suction slots have L_{SS} up to 65%. It
19 can be remarked that the suction slot with D_{SS} of 0.001 m gives a higher torque coefficient than
20 others. The torque coefficient increases about 26% than the airfoil without suction slot.

21 Figure 19 exemplifies the effect of L_{SS} on the torque coefficient at the stall angle (13.6 Degree)
22 with D_{SS} equal to 0.001 m. It can be discerned that, the L_{SS} equal to 45%, gives a higher torque
23 coefficient than other L_{SS} . Where, the torque coefficient increases about 42% than the airfoil
24 without suction slot.

25 Figure 20 reveals the effect of suction slot with optimum L_{SS} and optimum D_{SS} on the torque
26 coefficient at different angles. It is clearly noted that the improvement of torque coefficient at
27 different angles (from 7% to 19%), especially at stall regime (from 44% to 45%), which is

1 caused by the delay in stall angle. For more details about the value of improvement in torque
2 coefficient, see Table 4.

3 **4.1.2. Flow field around the airfoil section**

4 Figure 21 shows path lines colored by mean velocity magnitude at maximum value of torque
5 coefficient and stall condition. In addition, it also shows the effect of suction slot on the
6 boundary layer and flow field around the airfoil. Also, it highlights the amount of the difference
7 between the effects of suction slot before and after the stall condition. This difference is clearly
8 indicated between Figures a, b for 12.3 (Degree) and Figures c, d for 13.6 (Degree). The effect
9 of suction slot on the separation layer at the end of blade in Figures a, b was small. This is due
10 to the fact that the tow Figures did not have the stall condition yet. On the other hand, the effect
11 of suction slot on the separation layer in Figures c and d is significant because Figure c
12 represents the data in the stall condition however, Figure d does not. As for Figures e and f, the
13 two airfoils are in stall regime. Figures 22 and 23 clarify the pressure distribution around the
14 upper and lower surface of airfoil at maximum velocity (2.92 m/s) with different angles of
15 attack. It can be shown that the low pressure area at the trailing edge was increased with the
16 increase in angle of attack for the airfoil without slots. From Figure 23 A), C) and E) it can be
17 noted that the low pressure zones and disturbances at the trailing edge for the upper surface was
18 created the layer separation at the trailing edge and it was also increased by the increase in
19 angle of attack. The effect of the suction slot was very clear at the pressure distribution around
20 the airfoil, where it was more significant after the stall angles (13.6 and 14.4 degrees) than that
21 before the stall (12.3 degrees). The difference between the pressure value for the upper and
22 lower surface at the trailing edge was decreased by adding suction slot to the airfoil especially
23 at the stall angles.

24 **4.1.3. Second law analysis**

25 Figure 24 shows that the suction slot has a negative effect on the second law efficiency, where
26 the global entropy generation rate increases at all angles from (14% to 41%). The 10.6 degree
27 angle of attack (before the stall) has the highest difference in global entropy generation rate by
28 41% due to suction slot. On the other hand, 8.7 (before the stall) and 13.6 (after the stall)

1 degree angle of attack have the lowest difference in global entropy generation rate by 14 % due
2 to suction slot. Otherwise, the 10.1, 11.27, 11.74 and 12.3 (before the stall) degree have the
3 same difference in global entropy generation rate by 21.5% due to suction slot. Also, the 14.4
4 (after the stall) degree has a difference in the global entropy generation rate by 30%. This
5 phenomenon suggests that the change in velocity gradient due to the suction slot has a direct
6 impact on the entropy generation.

7 **4.2. Sinusoidal wave**

8 **4.2.1. Torque coefficient and Stall angle**

9 Figure 25 a) clarifies the instantaneous torque coefficient at compression cycle for different L_{SS} ,
10 while Figure 25 b) shows the average value of torque coefficient. These values are at citrine
11 angle of attack of 13.6 (Degree) and citrine D_{SS} equal to 0.001 m. The L_{SS} equal to 45%, gives a
12 higher torque coefficient value than other L_{SS} . This result is consistent with the result from
13 previous section. Figure 26 shows the effect of L_{SS} with 45% and D_{SS} equal to 0.001 m, on
14 torque coefficient at different angles. The improvement of torque coefficient is clearly noted
15 before the stall regime (from 11% to 26%) and at stall regime (from 32% to 53%). Table 5
16 shows more details about the value of improvement in torque coefficient.

17 Figure 27 explains the hysteretic behavior due to the reciprocating flow, the performance of the
18 Wells turbine has a hysteretic loop in which the values of torque coefficient in the accelerating
19 flow is smaller than in the decelerating flow. The hysteretic behavior was studied
20 experimentally and numerically in the references of [51, 69, 84, 86-88, 125-129]. By a
21 numerical simulation using a quasi-steady analysis, it can be that the only study which
22 simulated the hysteretic behavior after the stall is [51]. Moreover, Figure 27 highlights the
23 hysteretic behavior after adding the suction slot to the airfoil which has the same behavior.
24 Furthermore, it delays the stall regime in addition the torque coefficient. The torque
25 coefficients at compression cycle for different angles of attack are shown in Figure 28. It can be
26 observed that for all angles, the suction slot increases the torque coefficient. Figures d) and e)
27 have the highest increase value in comparison to other Figures. Whereas, the torque coefficient
28 was increased by (approximately) 26% in Figure 28 a), 16% in Figure 28 b) and 11% in Figure

1 28 c). The stall regime was delayed in Figure 28 d), in addition, the torque coefficient was
2 increased by (approximately) 53% and by (approximately) 32% in Figure 28 e). Furthermore,
3 the behavior of torque coefficient with the suction slot curve was more stable than that without
4 suction slot which is increased from the amount of highest value, as it see in Figure d) and e).

5

6 **4.2.2. Flow field around the airfoil section**

7 The flow structures over the NACA0015 airfoil in oscillating flow was shown in Figure 29 and
8 Figure 30. Figure 29 accentuates the contour of velocity magnitude at maximum velocity and
9 angle of attack equal to 12.3 degree (before the stall). The improvement effect of the suction
10 slot on flow structures is clear when compared between Figure a) and b), especially in, the
11 separated layer regime at the end of airfoil. The same behavior occurs in Figure 30 a) and b) for
12 the contour of velocity magnitude, and also in Figure c) and d) for mean velocity magnitude
13 from unsteady statistics. Figure 30 emphasize the improvement effect of the suction slot on
14 flow structures at maximum velocity and angle of attack equal to 13.6 degree (after the stall).
15 The suction slot has a direct effect on the flow structures at the end of blade, which leads to an
16 improvement in the separation regime.

17 The path-lien colored by means of velocity magnitude highlight the improvement effect of the
18 suction slot on the separation layers in Figures 31 and 32. It can be noted that by adding the
19 suction slot in the airfoil, this suction slot was decreased from the separation layer at the end of
20 airfoil. By comparing Figure 31 (before the stall) and Figure 32 (after the stall), it can be also
21 noted that, the improvement effect of suction slot on separation layers was increased in the stall
22 regime. The pressure distribution around the upper and lower surface at 12.3 degrees before the
23 stall (Figure 33) and 13.6 degrees after the stall (Figure 34) were presented. The effect of the
24 suction slot on the trailing edge area was appearing through the decrease from the low pressure
25 area that cause disturbances in the path line at the trailing edge area and it extends to the area
26 beyond the trailing edge. The pressure distribution after suction slot location ($L_{SS} = 45\%$) at
27 the upper surface has a direct effect in its value before and after the stall. The difference in
28 pressure value between the upper and lower surface after the slot location (Figure 34) was

1 decreased due to the slot effect. This decrease made the pressure distribution behavior similar
2 to the pressure distribution for the upper surface of the airfoil before the stall (Figure 33) which
3 led to a delay on the stall condition.

4 **4.2.3. Second law analysis**

5 The numerical simulations are used to obtain local entropy viscosity predictions of the different
6 angle of attack. Figure 35 and 36 highlight the suction slot effect in the entropy behavior when
7 a flow is accelerating and decelerating in compression cycle. Consequently, the entropy
8 generations rate varies with the Reynolds number. The change of Reynolds number values
9 results as a consequence to using sinusoidal wave boundary conditions. Suction slot have
10 negative effect on the entropy behavior in both accelerating and decelerating flow. Otherwise,
11 at some Reynolds numbers, the suction slot decreased from the entropy generation. As an
12 illustration, Figure 35 e) at Reynolds number is less than 100000 in accelerating flow. Also,
13 Figure 36 a) at Reynolds number is equal to 160000 in decelerating flow. The airfoil with the
14 suction slot at 11.3 degree has an average increase in the entropy generation rate by 22% than
15 that without the suction slot for the accelerating flow. Whereas, on the one hand, the maximum
16 difference in the entropy generation rate was found at Reynolds number to be equal to 193000
17 and 200000 by 36% than that without the suction slot. On the other hand, the minimum
18 difference in the entropy generation rate was found at Reynolds number from 50000 to 100000
19 by 11% than that without the suction slot; see Figure 35 a). For decelerating flow at 11.3
20 degree, it can be noted that the maximum increase in the entropy generation rate due to the
21 suction slot was 35% at Reynolds number equal to 55000. Additionally, on one hand, the
22 entropy generation rate was decreased than that without the suction slot by -23% at 160000
23 Reynolds number. This increase and decrease in the entropy generation rate for the airfoil with
24 the suction slot gives an average value equal to 0% at decelerating flow, see Figure 36 a). From
25 Figure 35 b), it can be noted that the maximum increase in the entropy generation rate is 39%
26 due to the suction slot for accelerating flow at 198000 Reynolds number. On the other hand, the
27 minimum increase in the entropy generation rate is 11% at Reynolds number from 78000 to
28 100000, with an average percentage 22% for the 11.7 degree. For decelerating flow at 11.7
29 degree, the maximum increase in the entropy generation rate is 31% at 30000 Reynolds number

1 and the minimum value is -14% at 175000 Reynolds number, due to the decrease of the entropy
2 generation rate than that without the suction slot. This increase and decrease in the entropy
3 generation rate for the airfoil with the suction slot gives an average value equal to 14% at
4 decelerating flow, see Figure 36 b). The 12.3 degree at accelerating flow gives maximum
5 increase by 35% at 200000 Reynolds number and minimum increase by 6% Reynolds number
6 from 78000 to 100000 with an average percentage 21%, see Figure 35 c). Otherwise, Figure 36
7 c) shows the maximum increase by 34% at 80000 Reynolds number and minimum increase by
8 3% 160000 Reynolds number with an average percentage 18%.

9 The airfoil with the suction slot at 13.6 degree has an average increase in the entropy
10 generation rate by 51% than that without the suction slot for the accelerating flow. Whereas,
11 the maximum different in the entropy generation rate was found at Reynolds number to be
12 equal to 28400 by 152% than that without suction slot. On the other hand, the minimum
13 difference in the entropy generation rate was found at 160000 Reynolds number by 17% than
14 that without the suction slot, see Figure 35 d). For decelerating flow at 13.6 degree, the
15 maximum increase in the entropy generation rate is 36% at 160000 Reynolds number and the
16 minimum value is -5% at 80000 Reynolds number, due to the decrease of the entropy
17 generation rate than that without the suction slot. This increase and decrease in the entropy
18 generation rate for the airfoil with the suction slot gives an average value equal to 19% at
19 decelerating flow, see Figure 36 d). The 14.4 degree at accelerating flow gives maximum
20 increase by 26% at 185000 and 198000 Reynolds number, and minimum increase by -30%
21 Reynolds number from 54000 to 80000 due to the decrease of the entropy generation rate than
22 that without suction slot. This increase and decrease in the entropy generation rate for the
23 airfoil with the suction slot gives an average value equal to 3% at accelerating flow, see Figure
24 35 e). Otherwise, Figure 36 e) shows the maximum increase by 46% at 80000 and 143000
25 Reynolds number, and minimum increase by 0% 100000 Reynolds number with an average
26 percentage 21%.

27 Furthermore, as an average value for the compression cycle, the suction slot was increased
28 from the global entropy generation rate, see Figure 37. This led to a decrease in the second law
29 efficiency, see Figure 38. From Figure 37 and 38, it is deducted that the minimum value for the

1 global entropy generation rate and maximum second law efficiency occurs at 11.7 degree for
2 airfoil without the suction slot. On the other hand, the minimum value for the global entropy
3 generation rate and maximum second law efficiency occurs at 11.3 degree for airfoil with the
4 suction slot.

5 **5. Conclusions**

6 A two-dimensional incompressible unsteady flow is simulated for airfoil under different
7 conditions to investigate the effect of airfoil with a suction slot on the torque coefficient and a
8 stall condition as well as the entropy generation due to viscous dissipation. The modeling
9 results show that D_{SS} and L_{SS} have different effects on the torque coefficient and stall
10 condition. Therefore, not all the parameters tested in the present study achieve a positive effect
11 in terms of improved blade torque. In general, it can be concluded that the decrease in D_{SS}
12 comes with an increase in torque coefficient. The smallest tested D_{SS} is 0.001 m, since any
13 smaller value would not be practical in real industries. Also, the best L_{SS} is locating
14 (approximately) at 45 % from the leading edge (at 13.6 Degree). By applying these conditions
15 we can achieve a 53% increase in the torque coefficient at stall regime (13.6 Degree). The
16 increase in torque coefficient, due to the suction slot, ranges from 11% to 26% before the stall
17 regime. Hence, the regime after the stall increases in torque coefficient varying from 32% to
18 53%. The main reason behind this observation is due to the delay of the stall condition. The
19 suction slot increases the torque coefficient and delays the stall angle which further leads to an
20 increase of first law efficiency. On the other hand, it decreases the second law efficiency. Thus,
21 if the turbine operates under high flow coefficient (angle of attack), it is strongly suggested to
22 use the suction slot to improve the performance at the stall condition. Otherwise, it may not be
23 effective. Future research should focus on improving the first law efficiency with a minimize
24 entropy generation, by using numerical algorithm and experimental test, in order to enhance the
25 overall Wells turbine performance under flow control method. Furthermore, it should
26 investigate the suction slot and its location in the third direction (Z axis) via three-dimensional
27 simulation.

6. Acknowledgements

The authors would like to acknowledge the support provided by the Department of Naval Architecture, Ocean and Marine Engineering at Strathclyde University, UK and the Department of Marine Engineering at Arab Academy for Science, Technology and Maritime Transport.

7. References

1. Collis, S., et al., Issues in active flow control: theory, control, simulation and experiment. *Progress in Aerospace Sciences*, 2004. 40(4-5): p. 237-289.
2. Katam, V., Simulation of low-Re flow over a modified NACA 4415 airfoil with oscillating camber. 2005, University of Kentucky: Master's thesis.
3. Gad-el-Hak, Pollard, and Bonnet, *Flow Control: Fundamentals and Practices*. 1998: Springer-Verlag Berlin Heidelberg.
4. Yousefi, K., R. Saleh, and P. Zahedi, Numerical study of blowing and suction slot geometry optimization on NACA 0012 airfoil. *Journal of Mechanical Science and Technology*, 2014. 28(4): p. 1297-1310.
5. Chapin, V.G. and E. Benard, Active Control of a Stalled Airfoil Through Steady or Unsteady Actuation Jets. *Journal of Fluids Engineering*, 2015. 137(9): p. 091103.
6. Schatz, M., B. Günther, and F. Thiele, Computational Investigation of Separation Control for High-Lift Airfoil Flows. *Active Flow Control*, ed. P.D.R. King. Vol. 95. 2007, Berlin, Germany. 173–189.
7. Chawla, J.S., et al., Efficiency improvement study for small wind turbines through flow control. *Sustainable Energy Technologies and Assessments*, 2014. 7: p. 195-208.
8. Fernandez, E., R. Kumar, and F. Alvi, Separation Control on a Low-Pressure Turbine Blade using Microjets. *Journal of Propulsion and Power*, 2013. 29(4): p. 867-881.
9. Volino, R.J., O. Kartuzova, and M.B. Ibrahim, Separation Control on a Very High Lift Low Pressure Turbine Airfoil Using Pulsed Vortex Generator Jets. *Journal of Turbomachinery*, 2011. 133(4): p. 041021.
10. Schlichting, H., *Boundary layer theory*. McGraw-Hill, New York, USA, 1968: p. 347-362.

- 1 11. Richards, E.J. and C.H. Burge, An airfoil designed to give laminar flow over the surface
2 with boundary layer suction. Aeronautical Research Council, R&M 2263, 1943.
- 3 12. Walker, S.W. and W.G. Raymer, Wind tunnel test on the 30 percent symmetrical griffth
4 aerofoil with ejection of air. Aeronautical Research Council, R&M 2475, 1946.
- 5 13. Braslow, A.L., A history of suction type laminar flow control with emphasis on flight
6 research, NASA History Division. Monograph in Aerospace History, 1999. 13.
- 7 14. Huang, L., P.G. Huang, and R.P. LeBeau, Numerical study of blowing and suction
8 control mechanism on NACA0012 airfoil. Journal of Aircraft, 2004. 41(5): p. 1005-
9 1013.
- 10 15. C. R. Rosas, Numerical simulation of flow separation control by oscillatort fluid
11 injection. 2005, A&M University: Texas
- 12 16. Akcayoz, E. and I.H. Tuncer, Numerical investigation of flow control over an airfoil
13 using synthetic jets and its optimization. International Aerospace Conference, Turkey,
14 2009.
- 15 17. Kim, S.H. and C. Kim, Separation control on NACA23012 using synthetic jet.
16 Aerospace Science and Technology, 2009. 13(4): p. 172-182.
- 17 18. Genc, M.S., U. Keynak, and H. Yapici, Performance of transition model for predicting
18 low re aerofoil flows without/with single and simultaneous blowing and suction.
19 European Journal of Mechanics B/Fluids, 2011. 30(2): p. 218-235.
- 20 19. Rumsey, C.L. and T. Nishino, Numerical study comparing RANS and LES approaches
21 on a circulation control airfoil. International Journal of Heat and Fluid Flow, 2011.
22 32(5): p. 847-864.
- 23 20. B. Yagiz, O. Kandil, and Y.V. Pehlivanoglu, Drag minimization using active and
24 passive flow control techniques. Aerospace Science and Technology, 2012. 17(1): p.
25 21-31.
- 26 21. Rosa, A.V.d., Fundamentals of Renewable Energy Processes. Third Edition ed. 2012,
27 United States of America: Elsevier Academic Press. 908.
- 28 22. Curran, R. and M. Folley Air turbine design for OWCs, in Ocean Wave Energy, i.J.
29 Cruz, Editor. 2008: Springer, Berlin. . p. 189-219.

- 1 23. Falcao, A.F.d.O.J., P.A.P., OWC wave energy devices with air flow control. *Ocean*
2 *Engineering*, 1999. 26(12): p. 1275-1295.
- 3 24. Falcao, A.F.d., Stochastic Modelling in wave power-equipment optimisation: maximum
4 energy production versus maximum profit. *Ocean Engineering*, 2004. 31(2004): p.
5 1407-1421.
- 6 25. Torres, F.R., P.R.F. Teixeira, and E. Didier, Study of the turbine power output of an
7 oscillating water column device by using a hydrodynamic – Aerodynamic coupled
8 model. *Ocean Engineering*, 2016. 125: p. 147-154.
- 9 26. Boccotti, P., Comparison between a U-OWC and a conventional OWC. *Ocean*
10 *Engineering*, 2007. 34: p. 799–805.
- 11 27. Boccotti, P., Caisson breakwaters embodying an OWC with a small opening—Part I:
12 Theory. *Ocean Engineering*, 2007. 34(5-6): p. 806-819.
- 13 28. Raghunathan, S., Theory and Performance of Wells Turbine. Queen's University of
14 Belfast, 1980. Rept. WE/80/13R.
- 15 29. Hitoshi Hotta, Y.W., V-5 A study on the matching between the air turbine and phase
16 control for the OWC wave power generator. *Ocean Engineering*, 1985. 12(6): p. 585-
17 586.
- 18 30. Masahiro Inoue, K.K., Toshiaki Setoguchi, Katsumi Shimamoto, II-2 On the starting
19 and quasi-steady characteristics of wells turbine under oscillating flow condition. *Ocean*
20 *Engineering*, 1985. 12(6): p. 563.
- 21 31. Masami Suzuki, C.A., Tetsuo Tagori, II-4 Fundamental studies on oscillating water
22 column wave power generator with wells turbine. *Ocean Engineering*, 1985. 12(6): p.
23 565.
- 24 32. Yukihiwa Washio, H.H., Takeaki Miyazaki, Yoshio Masuda, II-3 Full-scale
25 performance tests on tandem wells turbine. *Ocean Engineering*, 1985. 12(6): p. 564.
- 26 33. Folley, M., R. Curran, and T. Whittaker, Comparison of LIMPET Contra-rotating Wells
27 Turbine with Theoretical and Model Test Predictions. *Ocean Engineering*, 2006. 33(8-
28 9): p. 1056-1069.
- 29 34. Shehata, A.S., et al., Wells turbine for wave energy conversion: a review. *International*
30 *journal of energy research*, 2017. 41(1): p. 6-38.

- 1 35. Liu, Z., et al., Numerical study on a modified impulse turbine for OWC wave energy
2 conversion. *Ocean Engineering*, 2016. 111: p. 533-542.
- 3 36. Okuhara, S., et al., Wells Turbine for Wave Energy Conversion —Improvement of the
4 Performance by Means of Impulse Turbine for Bi-Directional Flow. *Open Journal of*
5 *Fluid Dynamics*, 2013. 03(02): p. 36-41.
- 6 37. Raghunathan, S., The Wells Air Turbine for Wave Energy Conversion. *Progress*
7 *Aerospace Sciences*, 1995. 31: p. 335-386.
- 8 38. Dixon, S.L., *Fluid Mechanics, Thermodynamics of Turbomachinery*. 1998: Pergamon
9 Press Ltd.
- 10 39. Sheldahl, R.E. and P.C. Klimas, Aerodynamic Characteristics of Seven Symmetrical
11 Airfoil Sections Through 180-Degree Angle of Attack for Use in Aerodynamic
12 Analysis of Vertical Axis Wind Turbines, in Sandia National Laboratories energy
13 report. 1981: the United States of America. p. 118.
- 14 40. Raghunathan, S., A methodology for Wells turbine design for wave energy conversion.
15 ARCHIVE: *Proceedings of the Institution of Mechanical Engineers, Part A: Journal of*
16 *Power and Energy 1990-1996 (vols 204-210)*, 1995. 209(31): p. 221-232.
- 17 41. Brito-Melo, A., L.M.C. Gato, and A.J.N.A. Sarmento, Analysis of Wells turbine design
18 parameters by numerical simulation of the OWC performance. *Ocean Engineering*,
19 2002. 29: p. 1463–1477.
- 20 42. Setoguchi, T., et al., Effect of Guide Vane Shape on the Performance of a Wells
21 Turbine. *Renewable Energy*, 2001. 23: p. 1-15.
- 22 43. Takao, M., et al., The Performance of a Wells Turbine with 3D Guide Vanes.
23 *International Journal of Offshore and Polar Engineering*, 2001. 11(1): p. 72-76.
- 24 44. Gato, L.M.C. and R. Curran, Performance of the Contrarotating Wells Turbine.
25 *International Journal of Offshore and Polar Engineering*, 1996. 6(1): p. 68-75.
- 26 45. Raghunathan, S. and W.C. Beattie, Aerodynamic performance of contra-rotating Wells
27 turbine for wave energy conversion. ARCHIVE: *Proceedings of the Institution of*
28 *Mechanical Engineers, Part A: Journal of Power and Energy 1990-1996 (vols 204-210)*,
29 1996. 210(61): p. 431-447.

- 1 46. Curran, R., et al., Performance Prediction of Contrarotating Wells Turbines for Wave
2 Energy Converter Design. *Journal of Energy Engineering*, 1998. 124(2): p. 35-53.
- 3 47. Gato, L.M.C. and R. Curran, The Energy Conversion Performance of Several Types of
4 Wells Turbine Designs. *Proceedings of the Institution of Mechanical Engineers, Part A:
5 Journal of Power and Energy*, 1997. 211(2): p. 133-145.
- 6 48. Mamun, M., et al., Improvement of the Performance of the Wells Turbine by using a
7 Very Thin Elongated Endplate at the Blade Tip, in the 3rd BSME-ASME International
8 Conference on Thermal Engineering. 2006, ASME: Dhaka, Bangladesh.
- 9 49. Takao, M., et al., Wells Turbine with End Plates for Wave Energy Conversion. *Ocean
10 Engineering*, 2007. 34(11-12): p. 1790-1795.
- 11 50. Kim, T.H., et al., Numerical investigation on the effect of blade sweep on the
12 performance of Wells turbine. *Renewable Energy*, 2002. 25: p. 235-248.
- 13 51. Setoguchi, T., et al., Effect of Rotor Geometry on the Performance of Wells Turbine, in
14 The Thirteenth International Offshore and Polar Engineering Conference. 2003, The
15 International Society of Offshore and Polar Engineers: Honolulu, Hawaii, USA. p. 374-
16 381.
- 17 52. Shaaban, S., Insight Analysis of Biplane Wells Turbine Performance. *Energy
18 Conversion and Management*, 2012. 59: p. 50-57.
- 19 53. Shehata, A.S., et al., Entropy Generation Due to Viscous Dissipation around a Wells
20 Turbine Blade: A Preliminary Numerical Study. *Energy Procedia*, 2014. 50: p. 808-816.
- 21 54. Shehata, A.S., et al., Performance Analysis of Wells Turbine Blades Using the Entropy
22 Generation Minimization Method. *Renewable Energy*, 2016. 86: p. 1123-1133.
- 23 55. Soltanmohamadi, R. and E. Lakzian, Improved design of Wells turbine for wave energy
24 conversion using entropy generation. *Meccanica*, Springer Netherlands., 2015. 51(8): p.
25 1713-1722.
- 26 56. Pope, K., I. Dincer, and G.F. Naterer, Energy and Exergy Efficiency Comparison of
27 Horizontal and Vertical Axis Wind Turbines. *Renewable Energy*, 2010. 35(9): p. 2102-
28 2113.

- 1 57. Baskut, O., O. Ozgener, and L. Ozgener, Effects of Meteorological Variables on
2 Exergetic Efficiency of Wind Turbine Power Plants. *Renewable and Sustainable Energy*
3 *Reviews*, 2010. 14(9): p. 3237-3241.
- 4 58. Redha, A.M., I. Dincer, and M. Gadalla, Thermodynamic Performance Assessment of
5 Wind Energy Systems: An Application. *Energy*, 2011. 36(7): p. 4002-4010.
- 6 59. Ozgener, O. and L. Ozgener, Exergy and Reliability Analysis of Wind Turbine
7 Systems: A Case Study. *Renewable and Sustainable Energy Reviews*, 2007. 11(8): p.
8 1811-1826.
- 9 60. Baskut, O., O. Ozgener, and L. Ozgener, Second Law Analysis of Wind Turbine Power
10 Plants: Cesme, Izmir Example. *Energy*, 2011. 36(5): p. 2535-2542.
- 11 61. Mortazavi, S.M., M.R. Soltani, and H. Motieyan, A Pareto optimal multi-objective
12 optimization for a horizontal axis wind turbine blade airfoil sections utilizing exergy
13 analysis and neural networks. *Journal of Wind Engineering and Industrial*
14 *Aerodynamics*, 2015. 136: p. 62-72.
- 15 62. Şöhret, Y., et al., Advanced exergy analysis of an aircraft gas turbine engine: Splitting
16 exergy destructions into parts. *Energy*, 2015. 90: p. 1219-1228.
- 17 63. Ghazikhani, M., I. Khazaei, and E. Abdekhodaie, Exergy analysis of gas turbine with
18 air bottoming cycle. *Energy*, 2014. 72: p. 599-607.
- 19 64. Sue, D.-C. and C.-C. Chuang, Engineering design and exergy analyses for combustion
20 gas turbine based power generation system. *Energy*, 2004. 29(8): p. 1183-1205.
- 21 65. Kim, K.H. and K. Kim, Exergy Analysis of Overspray Process in Gas Turbine Systems.
22 *Energies*, 2012. 5(12): p. 2745-2758.
- 23 66. Jubeh, N.M., Exergy Analysis and Second Law Efficiency of a Regenerative Brayton
24 Cycle with Isothermal Heat Addition. *Entropy*, 2005. 7(3): p. 172.
- 25 67. Lugo-Leyte, R., et al., Parametric Analysis of a Two-Shaft Aeroderivate Gas Turbine of
26 11.86 MW. *Entropy*, 2015. 17(8): p. 5829-5847.
- 27 68. SB., P., *Turbulent flows*. Cambridge University Press, 2000.
- 28 69. Mamun, M., The Study on the Hysteretic Characteristics of the Wells Turbine in a Deep
29 Stall Condition, in *Energy and Material Science Graduate School of Science and*
30 *Engineering*. 2006, Saga University: Japan. p. 141.

- 1 70. DAHLSTROM, S., LARGE EDDY SIMULATION OF THE FLOW AROUND A
2 HIGH-LIFT AIRFOIL, in Department of Thermo and Fluid Dynamics. 2003,
3 CHALMERS UNIVERSITY OF TECHNOLOGY: Goteborg, Sweden. p. 62.
- 4 71. Moin P, S.K., Cabot W, Lee S., A dynamic subgrid-scale model for compressible
5 turbulence and scalar transport. *Physics Fluids A*, 1991. 3(11): p. 2746–57.
- 6 72. DK., L., A proposed modification of the Germano subgrid-scale closure method.
7 *Physics Fluids A*, 1992. 4(3): p. 633–5.
- 8 73. Hinze, J.O., *Turbulence*. 1975, New York: McGraw-Hill Publishing Co.
- 9 74. Launder, B.E. and D.B. Spalding, *Lectures in Mathematical Models of Turbulence*.
10 1972, London, England: Academic Press.
- 11 75. Whittaker, T.J.T., T.P. Stewart, and R. Curran, Design synthesis of oscillating water
12 column wave energy converters: performance matching. *Proceedings of the Institution*
13 *of Mechanical Engineers, Part A: Journal of Power and Energy*, 1997. 211(6): p. 489-
14 505.
- 15 76. Hirsch, C., *Numerical Computation of Internal and External Flows: The Fundamentals*
16 *of Computational Fluid Dynamics*. 2007: Elsevier Science.
- 17 77. Bejan, A., *Entropy Generation Minimization- The New Thermodynamics of Finite-Size*
18 *Devices and Finite-Time Processes*. *Applied Physics Reviews*, 1996. 79(3): p. 1191-
19 1218.
- 20 78. A. Stodola, *Steam and Gas Turbines* (McGraw-Hill, New York). 1910.
- 21 79. Iandoli, C.L., 3-D Numerical Calculation of the Local Entropy Generation Rates in a
22 Radial Compressor Stage. *International journal of thermodynamics*, 2005. 8: p. 83-94.
- 23 80. Bejan, A., *Entropy Generation Minimization: The Method of Thermodynamic*
24 *Optimization of Finite-Size Systems and Finite-Time Processes*. 1995: Taylor &
25 Francis.
- 26 81. Starzmann, R. and T. Carolus, Model-Based Selection of Full-Scale Wells Turbines for
27 Ocean Wave Energy Conversion and Prediction of their Aerodynamic and Acoustic
28 Performances. *Proceedings of the Institution of Mechanical Engineers, Part A: Journal*
29 *of Power and Energy*, 2013. 228(1): p. 2-16.

- 1 82. Mohamed, M.H. and S. Shaaban, Optimization of Blade Pitch Angle of an Axial
2 Turbine Used for Wave Energy Conversion. *Energy*, 2013. 56: p. 229-239.
- 3 83. Torresi, M., S.M. Camporeale, and G. Pascazio, Detailed CFD Analysis of the Steady
4 Flow in a Wells Turbine Under Incipient and Deep Stall Conditions. *Journal of Fluids*
5 *Engineering*, 2009. 131(7): p. 071103.
- 6 84. Mamun, M., et al., Hysteretic Flow Characteristics of Biplane Wells Turbine. *Ocean*
7 *Engineering*, 2004. 31(11-12): p. 1423-1435.
- 8 85. Smagorinsky, J., General Circulation Experiments with the Primitive Equations. I. The
9 Basic Experiment. *Month. Wea. Rev.*, 1963. 91: p. pp.99-164.
- 10 86. Setoguchi, T., et al., Hysteretic Characteristics of Wells Turbine for Wave Power
11 Conversion. *Renewable Energy*, 2003. 28(13): p. 2113-2127.
- 12 87. Kinoue, Y., et al., Mechanism of Hysteretic Characteristics of Wells Turbine for Wave
13 Power Conversion. *Journal of Fluids Engineering*, 2003. 125(2): p. 302.
- 14 88. Kinoue, Y., et al., Hysteretic Characteristics of Monoplane and Biplane Wells Turbine
15 for Wave Power Conversion. *Energy Conversion and Management*, 2004. 45(9-10): p.
16 1617-1629.
- 17 89. DE Moura, C.A.K., Carlos S., *The Courant–Friedrichs–Lewy (CFL) Condition: 80*
18 *Years After Its Discovery*. 1 ed. 2013, Boston: Birkhäuser Basel.
- 19 90. Saqr, K., Large eddy simulation: the demand for a universal measure of resolution. *CFD*
20 *Letters*. 2010: issres.net.
- 21 91. Celik, I., Z. Cehreli, and I. Yavuz, Index of resolution quality for large eddy
22 simulations. *Journal of fluids engineering*, 2005. 127(5): p. 949-958.
- 23 92. Pope, S.B., Ten questions concerning the large-eddy simulation of turbulent flows. *New*
24 *journal of Physics*, 2004. 6(1): p. 35.
- 25 93. Saqr, K.M., M. Wahid, and M.M. Sies. Highly-resolved large eddy simulation of the
26 nonreacting flow in an asymmetric vortex combustor. in *THE 4TH INTERNATIONAL*
27 *MEETING OF ADVANCES IN THERMOFLUIDS (IMAT 2011)*. 2012. AIP
28 Publishing.

- 1 94. Eldrainy, Y., et al., Large eddy simulation and preliminary modeling of the flow
2 downstream a variable geometry swirler for gas turbine combustors. ...
3 Communications in Heat ..., 2011.
- 4 95. Mazzei, L., et al., Impact of Swirl Flow on Combustor Liner Heat Transfer and
5 Cooling: A Numerical Investigation With Hybrid Reynolds-Averaged Navier–Stokes
6 Large Eddy Simulation Models. Journal of Engineering for Gas Turbines and Power,
7 2016. 138(5): p. 051504.
- 8 96. Fureby, C., Challenges for Large Eddy Simulation of Engineering Flows, in Whither
9 Turbulence and Big Data in the 21st Century? 2017, Springer. p. 375-400.
- 10 97. Georgiadis, N.J., D.P. Rizzetta, and C. Fureby, Large-eddy simulation: current
11 capabilities, recommended practices, and future research. AIAA journal, 2010. 48(8): p.
12 1772-1784.
- 13 98. Eldrainy, Y.A., et al., Large eddy simulation and preliminary modeling of the flow
14 downstream a variable geometry swirler for gas turbine combustors. International
15 Communications in Heat and Mass Transfer, 2011. 38(8): p. 1104-1109.
- 16 99. Torresi, M., S. Camporeale, and G. Pascazio, Experimental and Numerical Investigation
17 on the Performance of a Wells Turbine Prototype, in Seventh European Wave and Tidal
18 Energy Conference. 2007: Porto, Portugal
- 19 100. Richez, F., et al., Zonal RANS/LES coupling simulation of a transitional and separated
20 flow around an airfoil near stall. Theoretical and Computational Fluid Dynamics, 2007.
21 22(3-4): p. 305-315.
- 22 101. Rezaei, F., E. Roohi, and M. Pasandideh-Fard, Stall simulation of flow around an airfoil
23 using LES model and comparison of RANS models at low angles of attack, in 15th
24 Conference on Fluid Dynamics. 2013: The University of Hormozgan, Bandar Abbas,
25 Iran. p. 1-10.
- 26 102. Martinat, G., et al., Turbulence modeling of the flow past a pitching NACA0012 airfoil
27 at 10^5 and 10^6 Reynolds number, . Journal of Fluids and Structures, 2008. 24: p. 1294-
28 1303.

- 1 103. Nomura, T., et al., Aerodynamic Forces on a Square Cylinder in Oscillating Flow with
2 Mean Velocity. *Journal of Wind Engineering and Industrial Aerodynamics*, 2003. 91: p.
3 199–208.
- 4 104. Kawai, S. and K. Asada, Wall-modeled large-eddy simulation of high Reynolds number
5 flow around an airfoil near stall condition. *Computers & Fluids*, 2013. 85: p. 105-113.
- 6 105. Alferez, N., I. Mary, and E. Lamballais, Study of Stall Development Around an Airfoil
7 by Means of High Fidelity Large Eddy Simulation. *Flow, Turbulence and Combustion*,
8 2013. 91(3): p. 623-641.
- 9 106. Kim, Y., I.P. Castro, and Z.T. Xie, Large-Eddy Simulations for Wind Turbine Blade:
10 Dynamic Stall and Rotational Augmentation. 2015. 20: p. 369-375.
- 11 107. AlMutairi, J., I. AlQadi, and E. ElJack, Large Eddy Simulation of a NACA-0012 Airfoil
12 Near Stall. 2015. 20: p. 389-395.
- 13 108. Armenio, V., B. Geurts, and J. Fröhlich, Large Eddy Simulation of Flow Around an
14 Airfoil Near Stall. 2010. 13: p. 541-545.
- 15 109. Hitiwadi, M., et al., Large Eddy Simulations of 2D and Open-tip Airfoils Using Voxel
16 Meshes. *Procedia Engineering*, 2013. 61: p. 32-39.
- 17 110. Bromby, D.Y.a.W., Large-Eddy Simulation of Unsteady Separation Over a Pitching
18 Airfoil at High Reynolds Number, in *Seventh International Conference on
19 Computational Fluid Dynamics (ICCFD7)*. 2012: Big Island, Hawaii.
- 20 111. SKYLLINGSTAD, E.D. and H.W. WIJESKERA, Large-Eddy Simulation of Flow
21 over Two-Dimensional Obstacles: High Drag States and Mixing. *Journal of physical
22 oceanography*, 2004. 34: p. 94-112.
- 23 112. Avdis, A., S. Lardeau, and M. Leschziner, Large Eddy Simulation of Separated Flow
24 over a Two-dimensional Hump with and without Control by Means of a Synthetic Slot-
25 jet. *Flow, Turbulence and Combustion*, 2009. 83(3): p. 343-370.
- 26 113. Cheng, W.-C. and F. Porté-Agel, Evaluation of subgrid-scale models in large-eddy
27 simulation of flow past a two-dimensional block. *International Journal of Heat and
28 Fluid Flow*, 2013. 44: p. 301-311.

- 1 114. Christian Tenaud and L.T. Phuoc, Large eddy simulation of unsteady, compressible,
2 separated flow around NACA 0012 airfoil, in Fifteenth International Conference on
3 Numerical Methods in Fluid Dynamics. 1997. p. pp 424-429.
- 4 115. Shehata, A.S., et al., Comparative analysis of different wave turbine designs based on
5 conditions relevant to northern coast of Egypt. Energy, 2016.
6 <http://dx.doi.org/10.1016/j.energy.2016.11.091>.
- 7 116. Ashvinkumar Chaudhari, et al., Large Eddy Simulation of Boundary-Layer Flows over
8 Two-Dimensional Hills, in Industrial Mathematics at ECMI 2012. 2012, Springer
9 International Publishing Switzerland 2014. p. 211-218.
- 10 117. Özgökmen, T.M., et al., Large eddy simulation of stratified mixing in two-dimensional
11 dam-break problem in a rectangular enclosed domain. Ocean Modelling, 2007. 16(1-2):
12 p. 106-140.
- 13 118. Michioka, T., et al., Large-Eddy Simulation for the Mechanism of Pollutant Removal
14 from a Two-Dimensional Street Canyon. Boundary-Layer Meteorology, 2010. 138(2):
15 p. 195-213.
- 16 119. Chung, T.N.H. and C.-H. Liu, On the Mechanism of Air Pollutant Removal in Two-
17 Dimensional Idealized Street Canyons: A Large-Eddy Simulation Approach. Boundary-
18 Layer Meteorology, 2013. 148(1): p. 241-253.
- 19 120. Andrej Horvata, I.K., Jure Marnb, Two dimensional large eddy simulation of turbulent
20 natural convection due to internal heat generation. international journal of heat and
21 mass transfer, 2001. 44(21): p. 3985–3995.
- 22 121. Matos, A.d., F.A.A. Pinho, and A. Silveira!Neto, Large-eddy simulation of turbulent
23 ~ow over a two! dimensional cavity with temperature ~uctuations. International Journal
24 of Heat and Mass Transfer, 1999. 42: p. 3848.
- 25 122. Chen, Q. and G.A. Glatzmaier, Large eddy simulations of two-dimensional turbulent
26 convection in a density-stratified fluid. Geophysical & Astrophysical Fluid Dynamics,
27 2005. 99(5): p. 355-375.
- 28 123. Liu, Y., et al., Numerical Simulation of Two-Dimensional Parallel Blade-Vortex
29 Interactions Using Large Eddy Simulation. Procedia Engineering, 2012. 31: p. 703-707.

- 1 124. Torresi, M., S. Camporeale, and G. Pascazio, Performance of a Small Prototype of a
2 High Solidity Wells Turbine, in Seventh European Conference on Turbomachinery
3 Fluid Dynamics and Thermodynamics. 2007: Athens, Greece
- 4 125. Kim, T.H., et al., Hysteretic Characteristics of Wells Turbine for Wave Power
5 Conversion, in The Twelfth International Offshore and Polar Engineering Conference.
6 2002, The International Society of Offshore and Polar Engineers: Kitakyushu, Japan. p.
7 687-693.
- 8 126. Kinoue, Y., et al., Comparison of Performances of Turbines for Wave Energy
9 Conversion. *Journal of Thermal Science*, 2003. 12(4): p. 323-328.
- 10 127. Setoguchi T, T.M., Kaneko K., Hysteresis on Wells Turbine Characteristics in
11 Reciprocating Flow. *International Journal of Rotating Machinery*, 1998. 4(1): p. 17-24.
- 12 128. Thakker, A. and R. Abdulhadi, The Performance of Wells Turbine Under Bi-
13 Directional Airflow. *Renewable Energy*, 2008. 33(11): p. 2467-2474.
- 14 129. Thakker, A. and R. Abdulhadi, Effect of Blade Profile on the Performance of Wells
15 Turbine under Unidirectional Sinusoidal and Real Sea Flow Conditions. *International
16 Journal of Rotating Machinery*, 2007. 2007: p. 1-9.
- 17

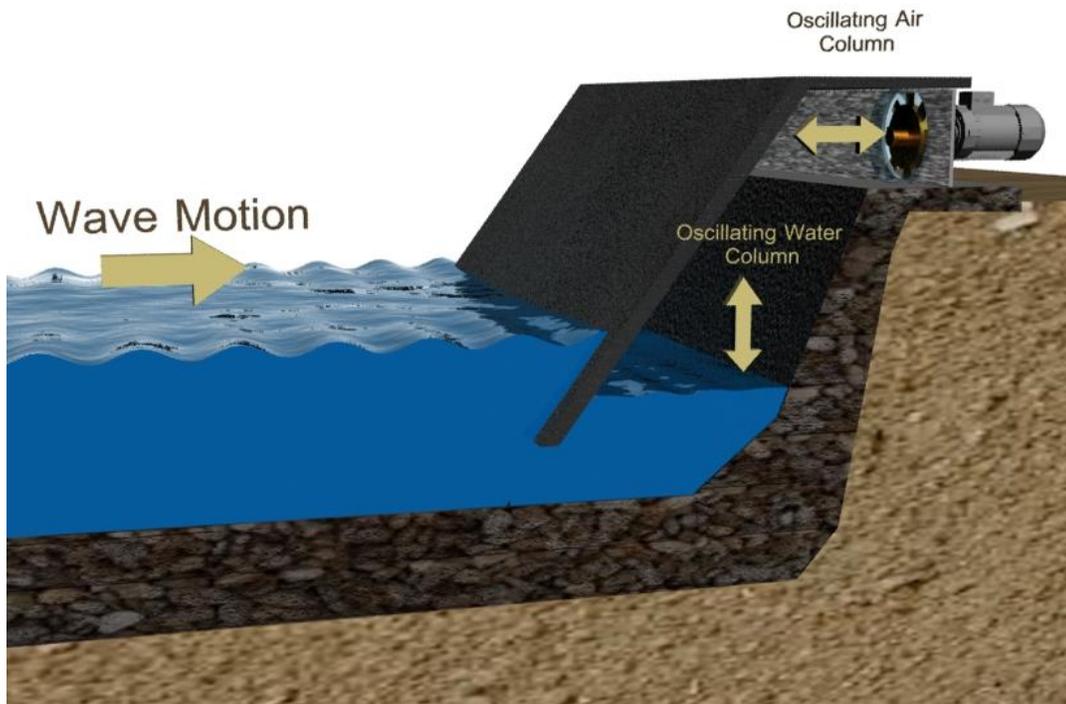


Figure 1 An illustration of the principle of operation of OWC system, where the wave motion is used to drive a turbine through the oscillation of air column [43].

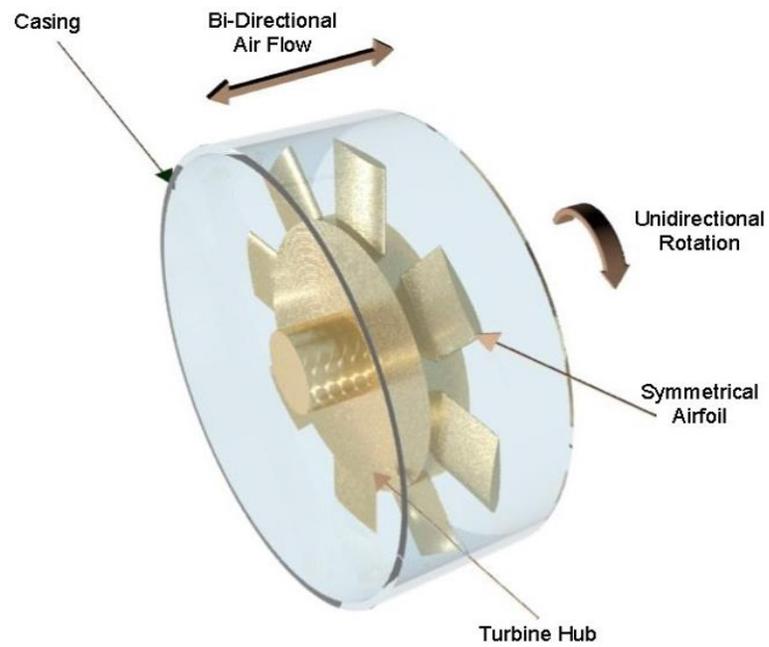


Figure 2 Typical structure of Wells turbine rotor [43].

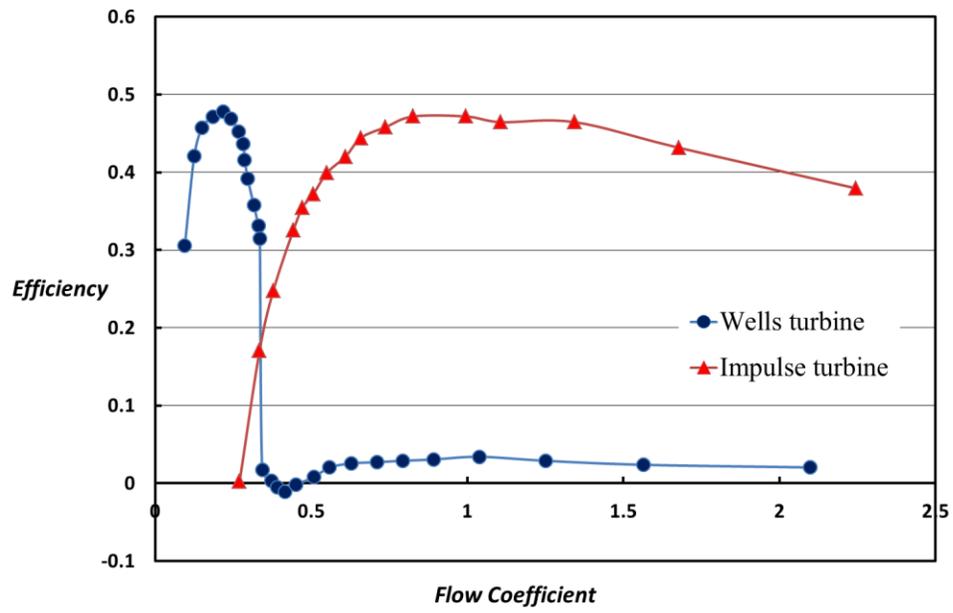


Figure 3 Turbines characteristic under steady flow conditions: Flow coefficient variation with the efficiency [16].

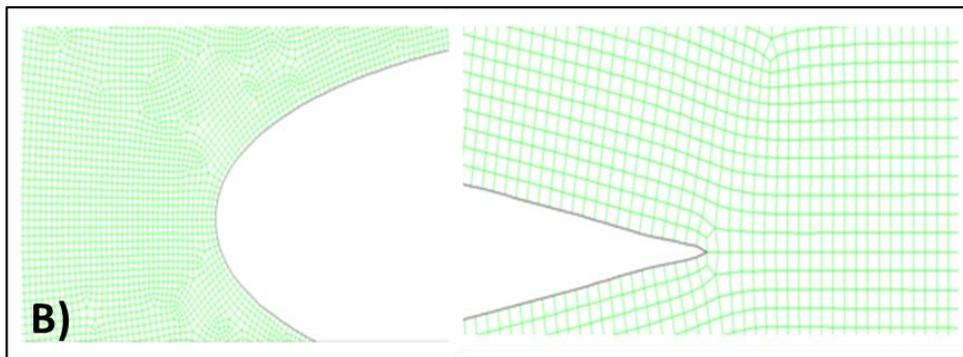
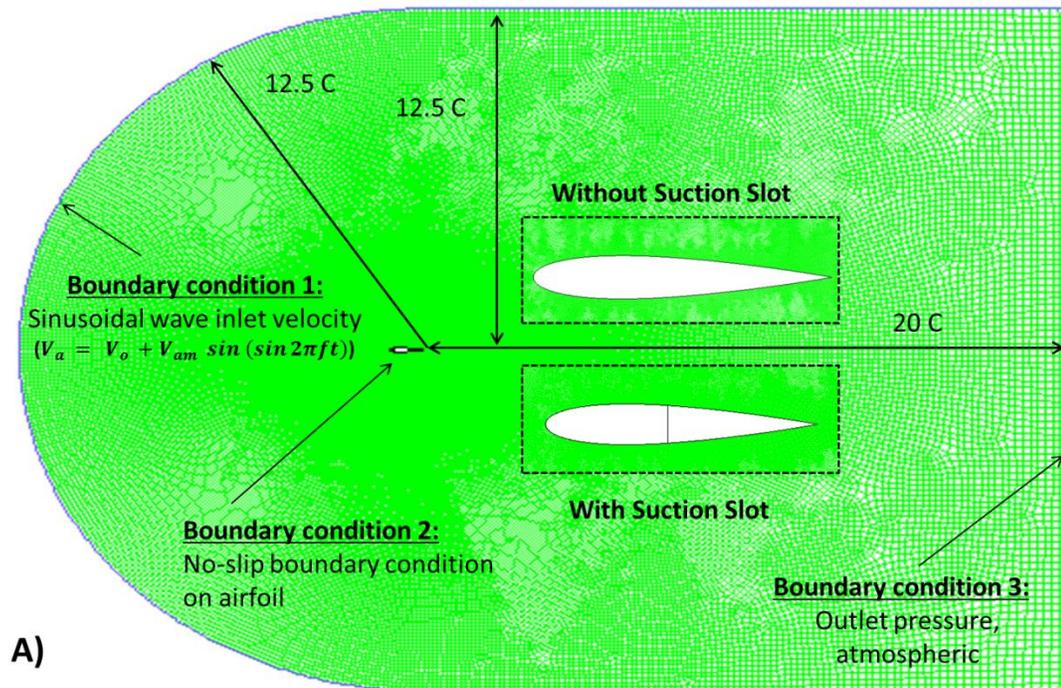


Figure 4 Computational model and boundary conditions A) Dimensions of whole computational domain and location of airfoil B) Computational grid near the wall of the airfoil

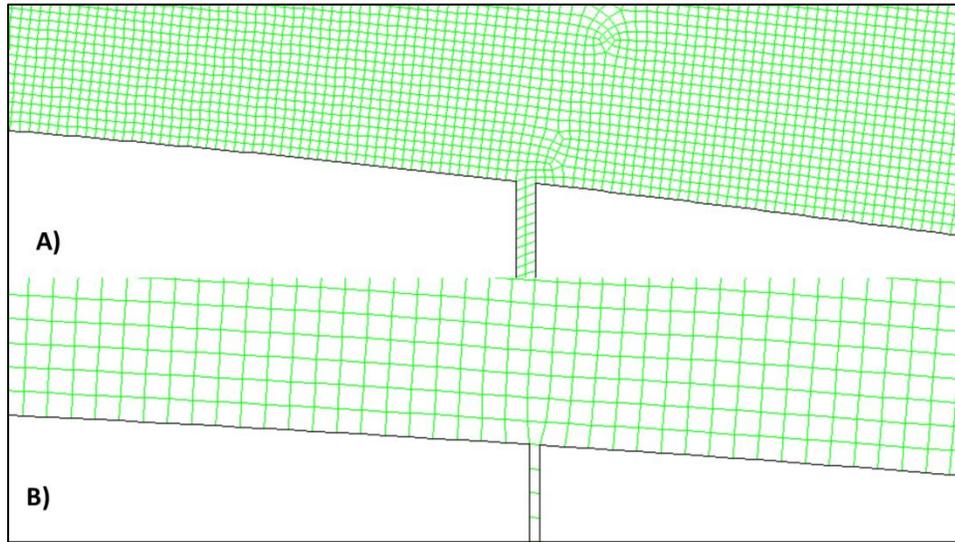
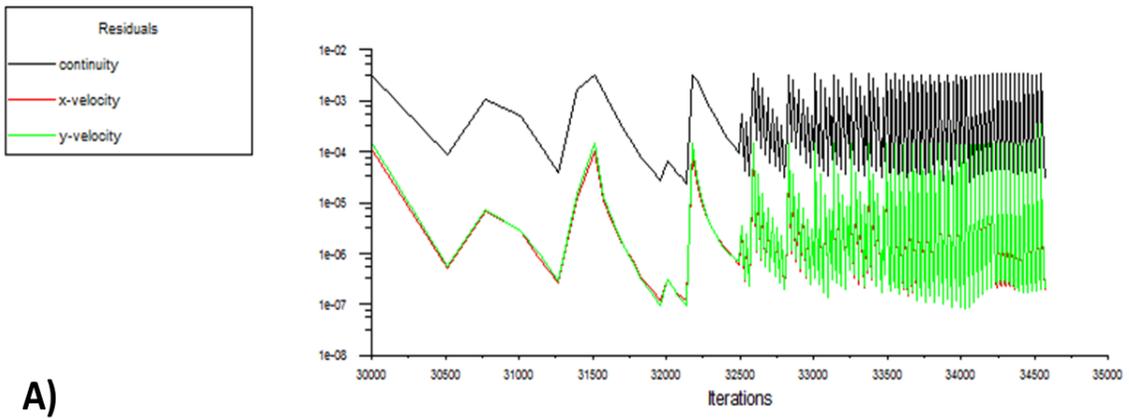
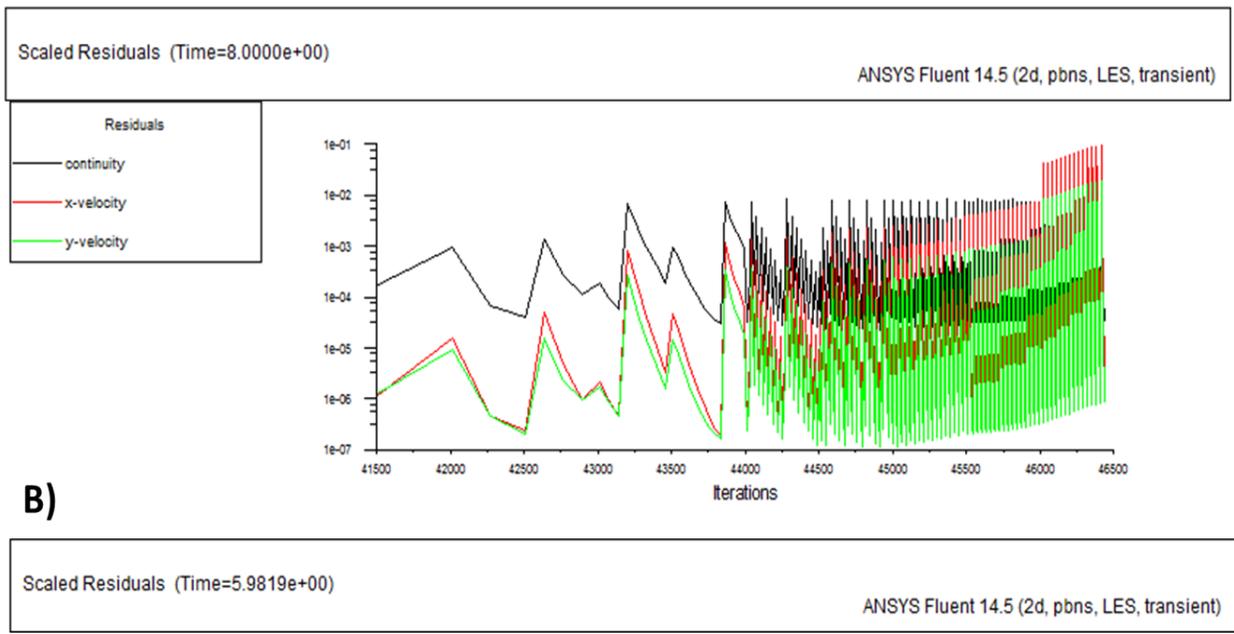


Figure 5 The near views of slot mesh A) $D_{SS} = 0.005$ m B) $D_{SS} = 0.001$ m



A)



B)

Figure 6 Convergence criteria A) non-oscillating flow B) sinusoidal flow

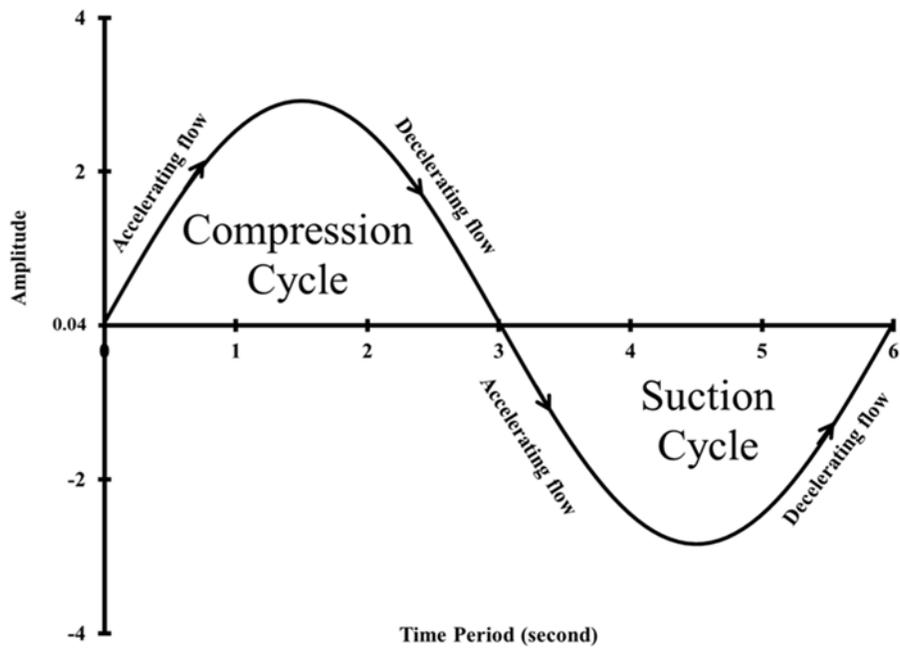
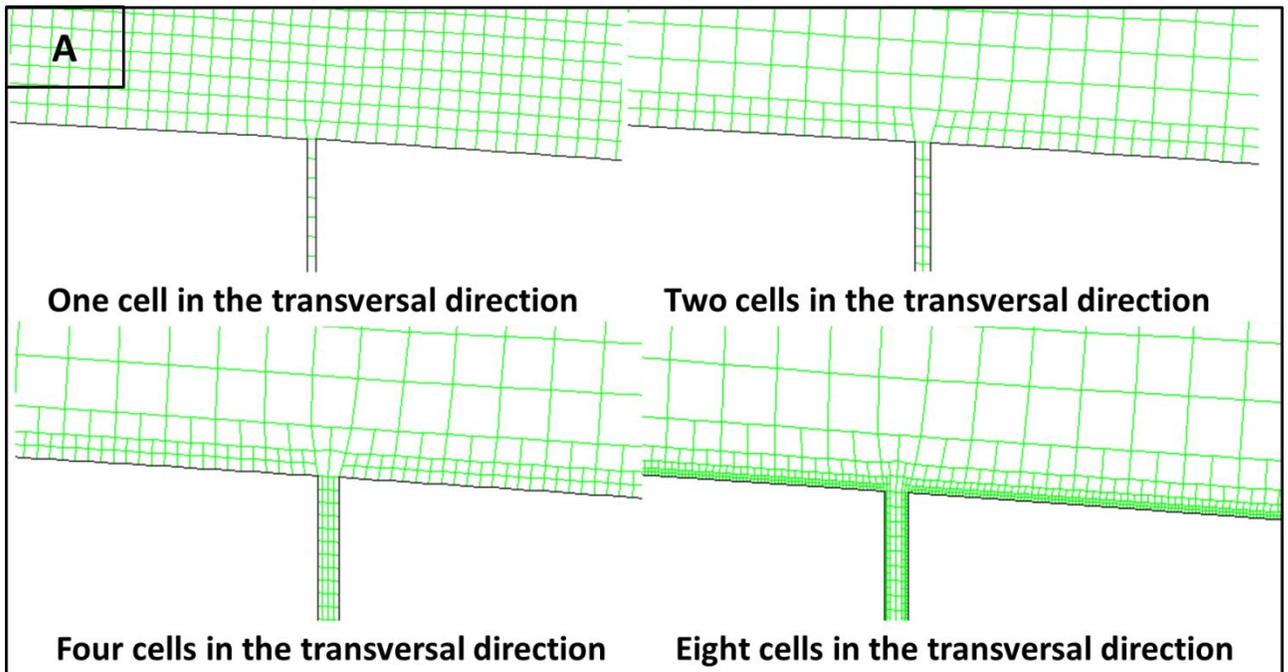


Figure 7 The sinusoidal wave boundary condition, which represents a regular oscillating water column



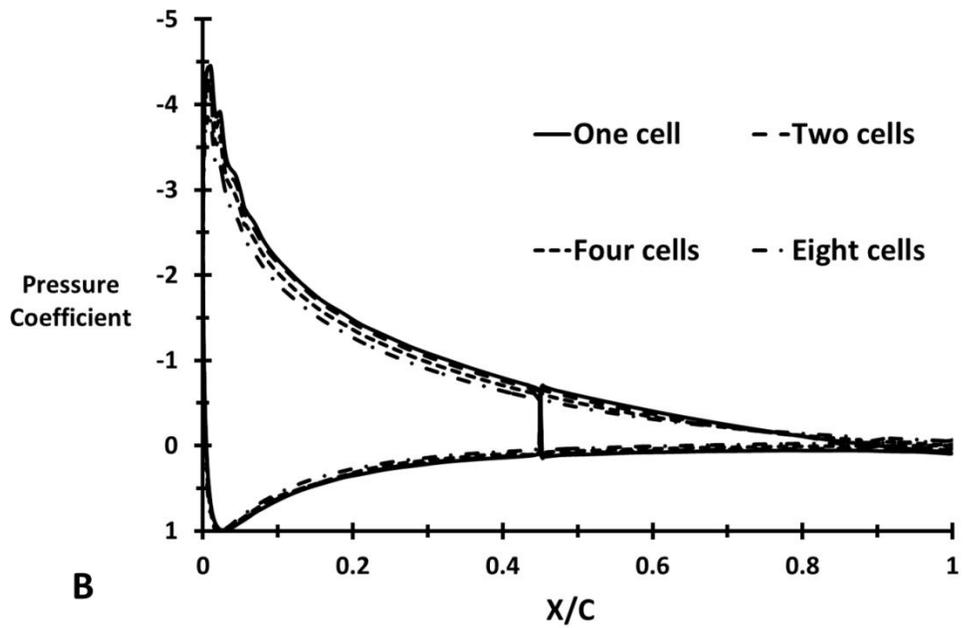


Figure 8 A) grid sensitivity analysis with respect to cell number across the slot section B) Pressure coefficient plotted on the normalized aerofoil cord at different grid resolutions

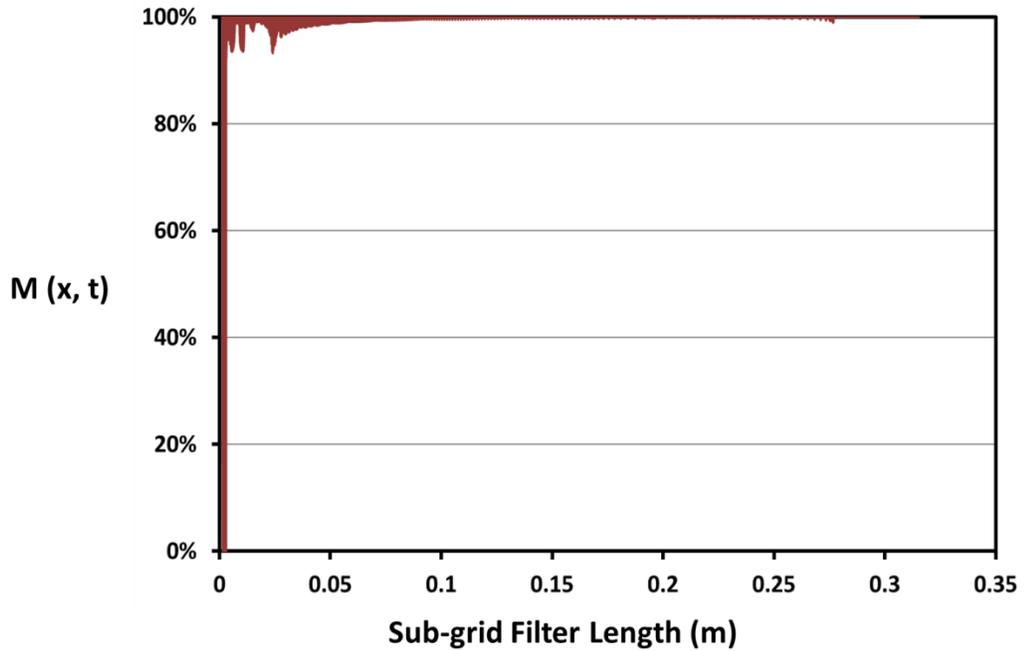


Figure 9 The measure of LES quality by $M(x, t)$ with the Sub-grid Filter Length

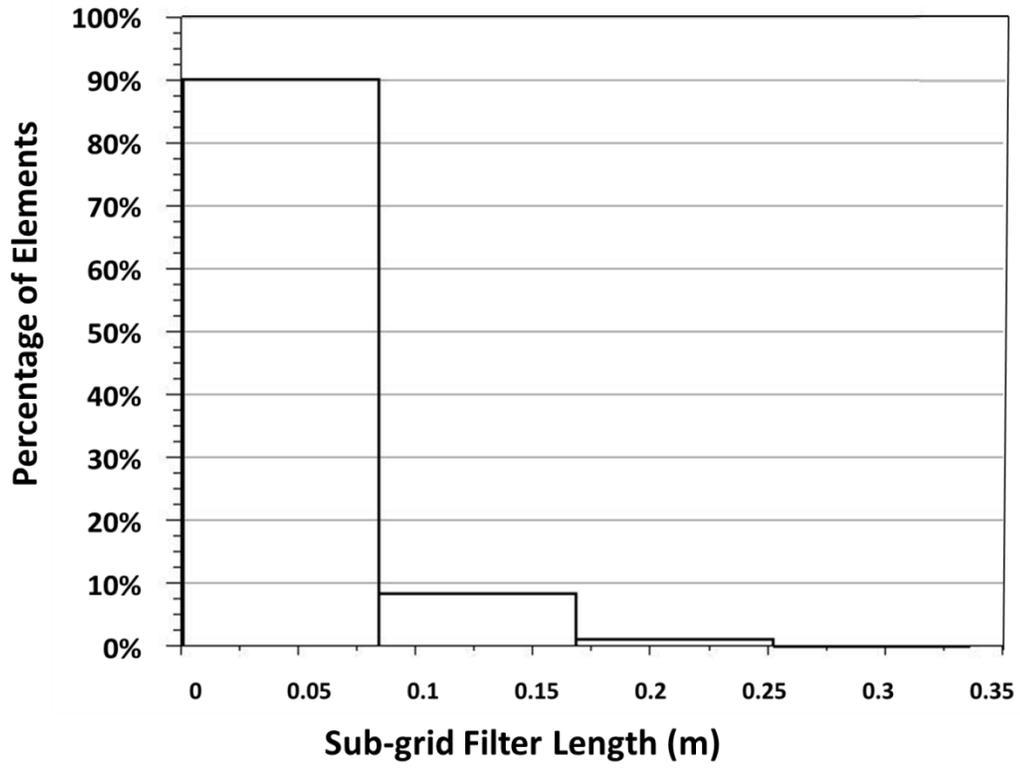
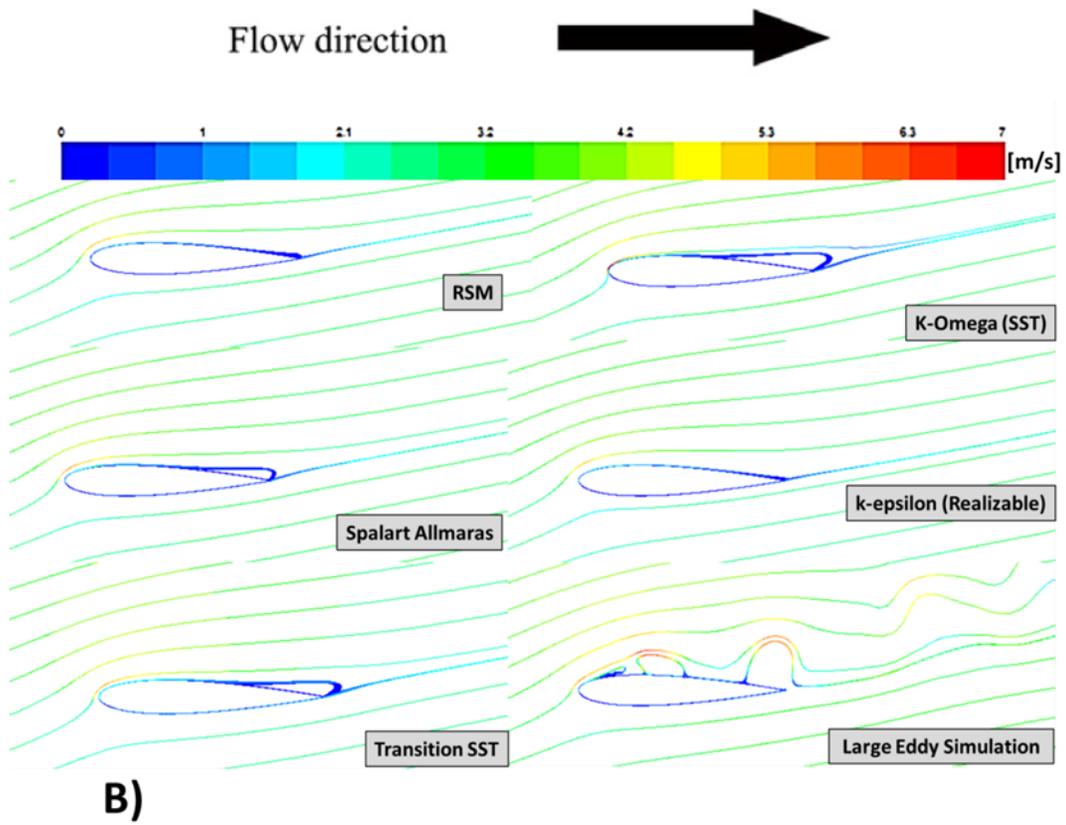
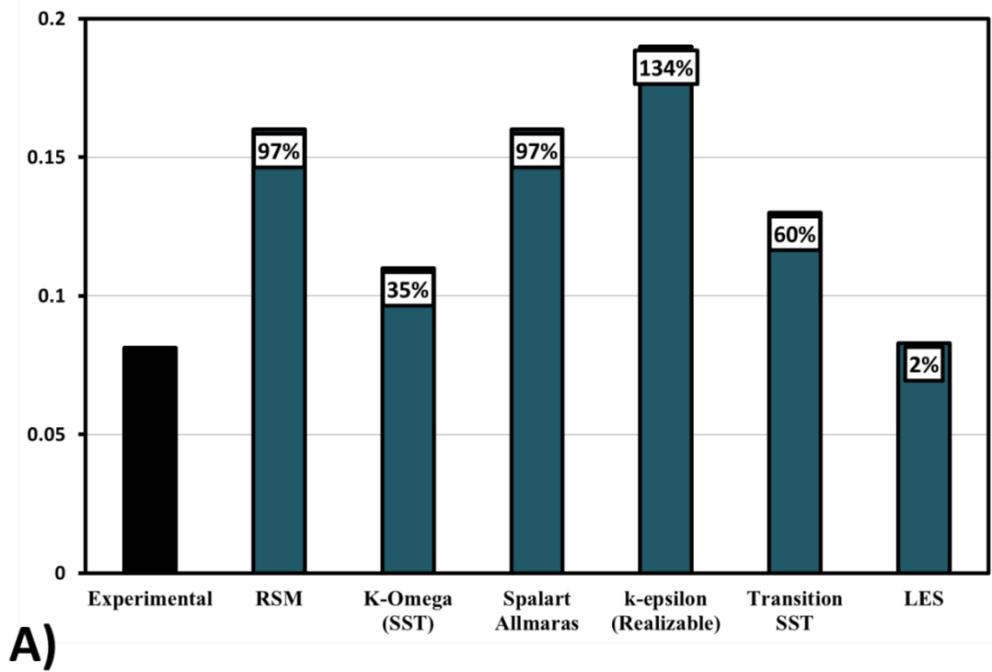
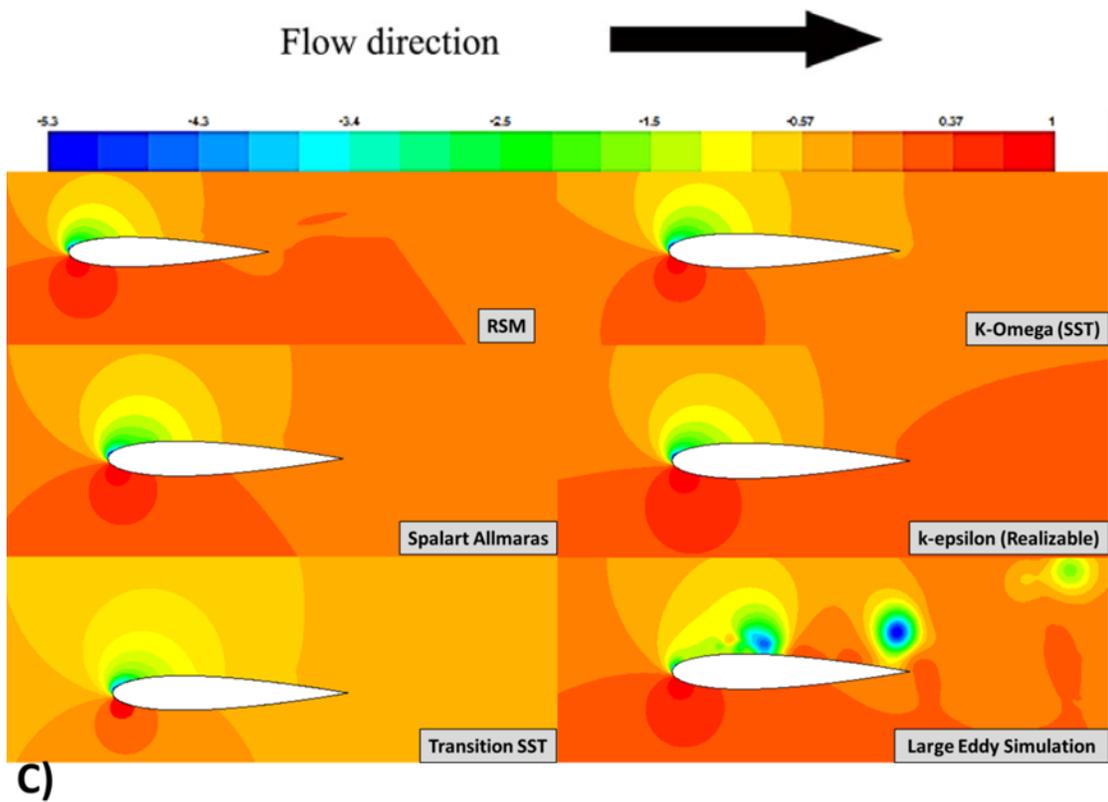


Figure 10 A histogram of Number of Elements for the Sub-grid Filter Length





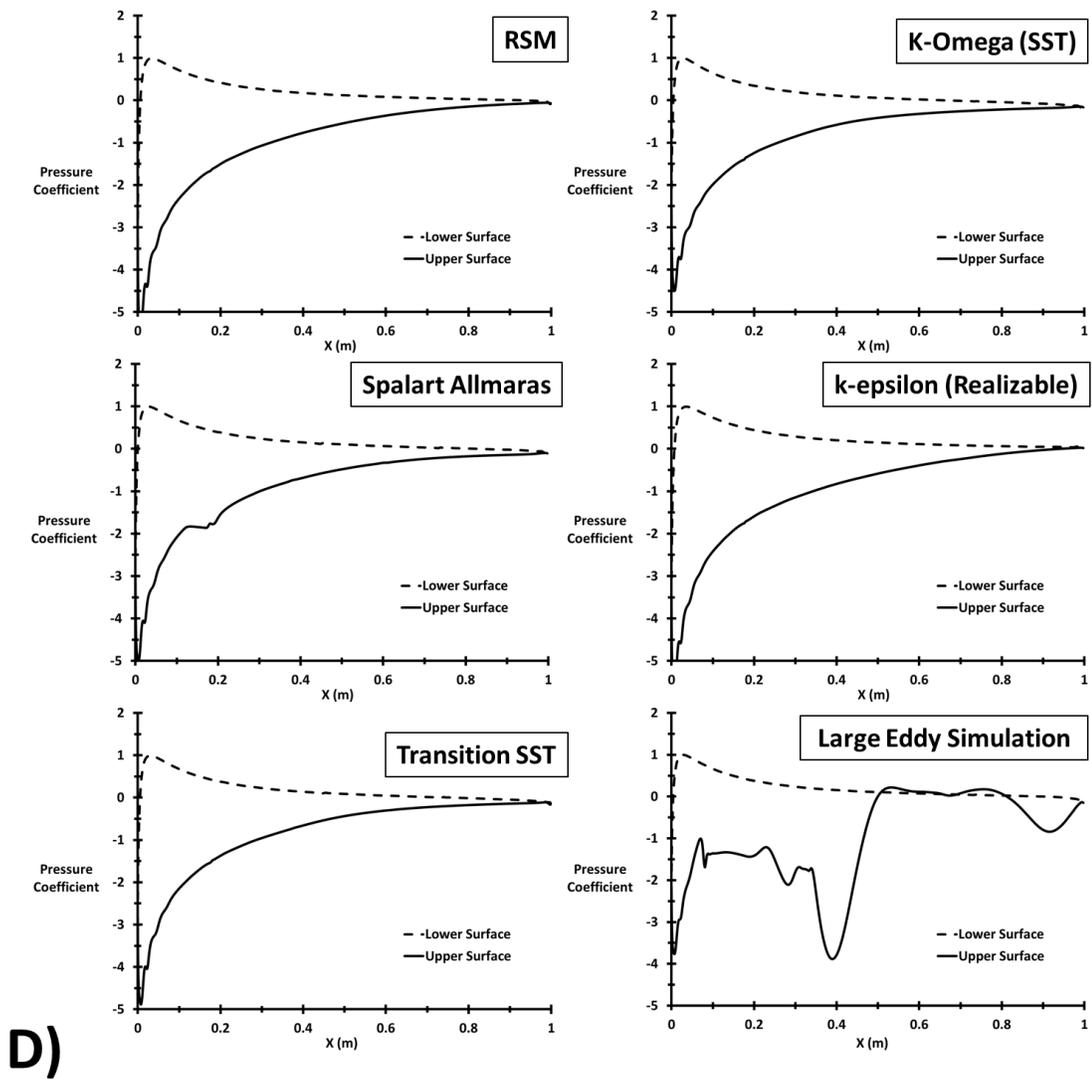


Figure 11 Comparison between different models to simulate the stall angle from experimental data A) Torque coefficient B) Path-line colored by the velocity magnitude C) Contours of pressure distribution D) Pressure distribution at upper and lower surface

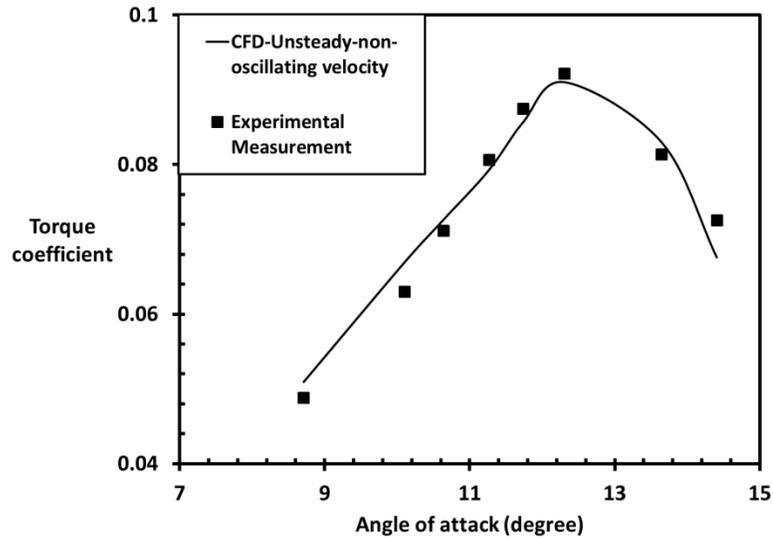


Figure 12 Measured torque coefficient from reference (Torresi, Camporeale et al. 2007, Torresi, Camporeale et al. 2007, Torresi, Camporeale et al. 2009) and calculated torque coefficient from present CFD unsteady flow with non-oscillating velocity

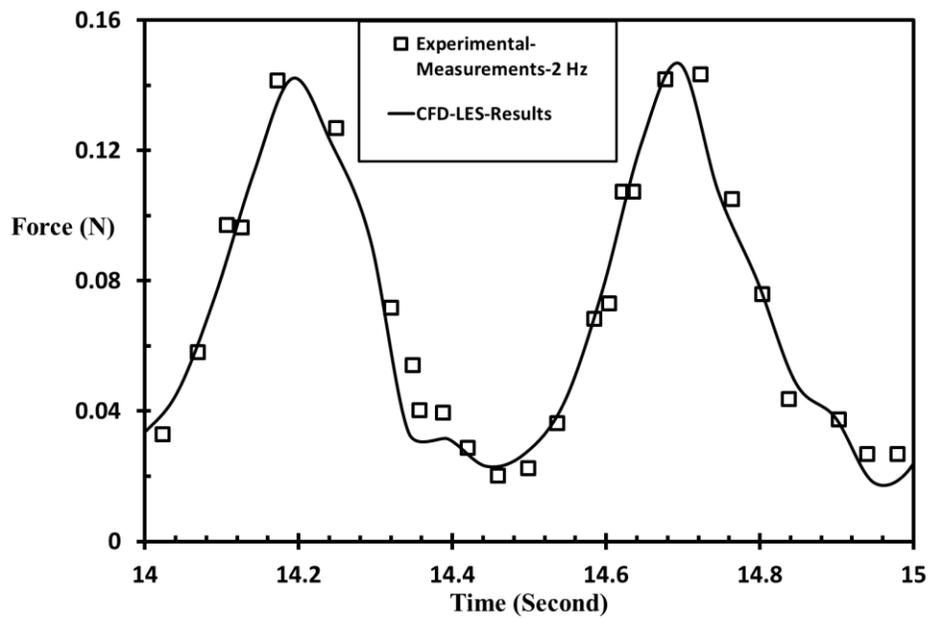


Figure 13 Measured unsteady in-line force F_D from reference ((Nomura, Suzuki et al. 2003), (angle of attack= 0 degree) and F_D calculated from the present CFD for frequency 2 Hz

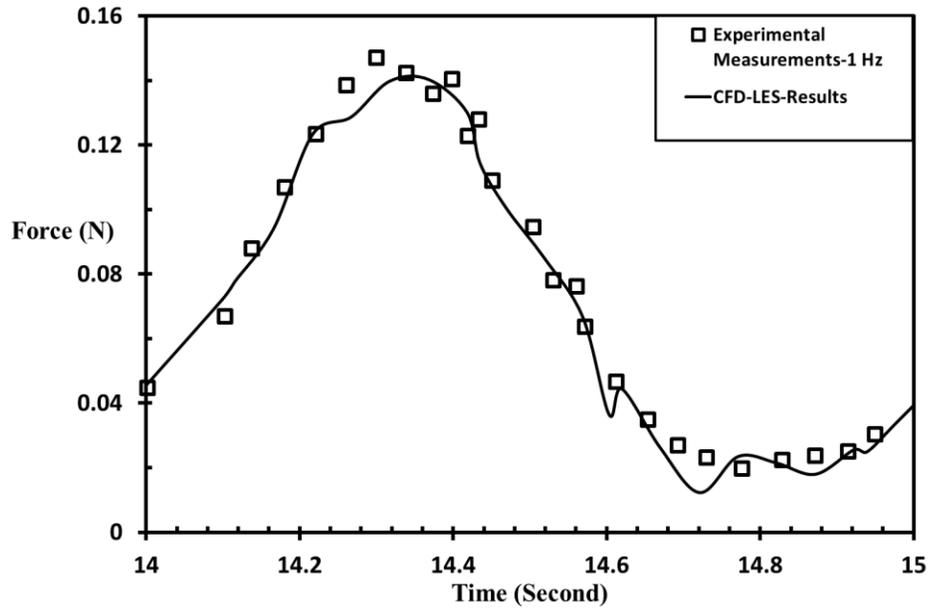


Figure 14 Measured unsteady in-line force F_D from reference ((Nomura, Suzuki et al. 2003), (angle of attack= 0 degree) and F_D calculated from the present CFD for frequency 1 Hz.

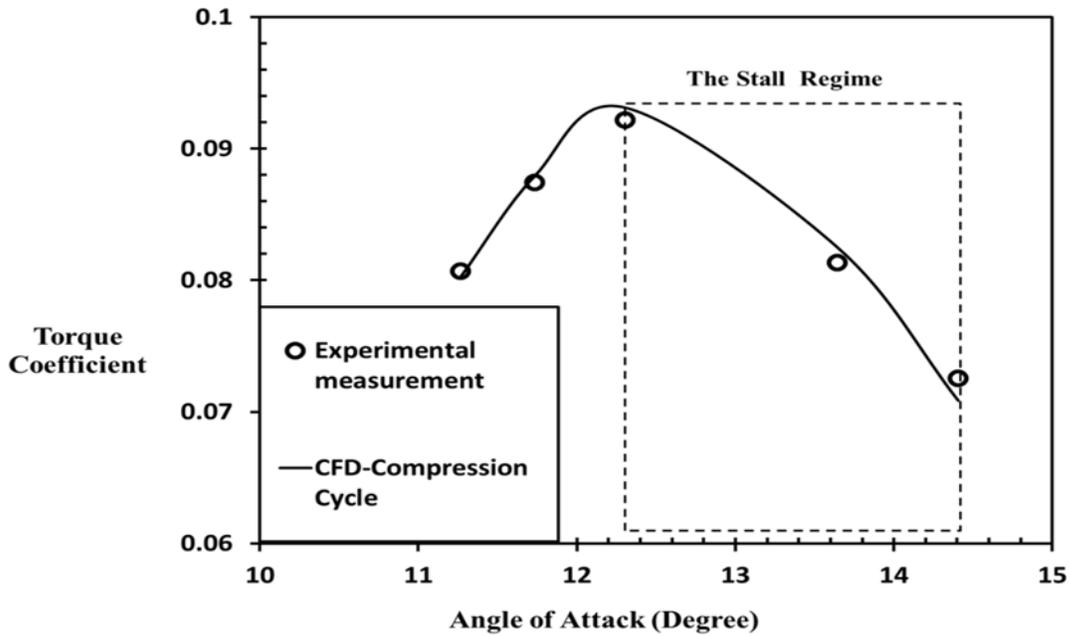


Figure 15 Measured torque coefficient from reference (Torresi, Camporeale et al. 2007, Torresi, Camporeale et al. 2007, Torresi, Camporeale et al. 2009) and calculated torque coefficient from CFD unsteady flow with sinusoidal inlet velocity

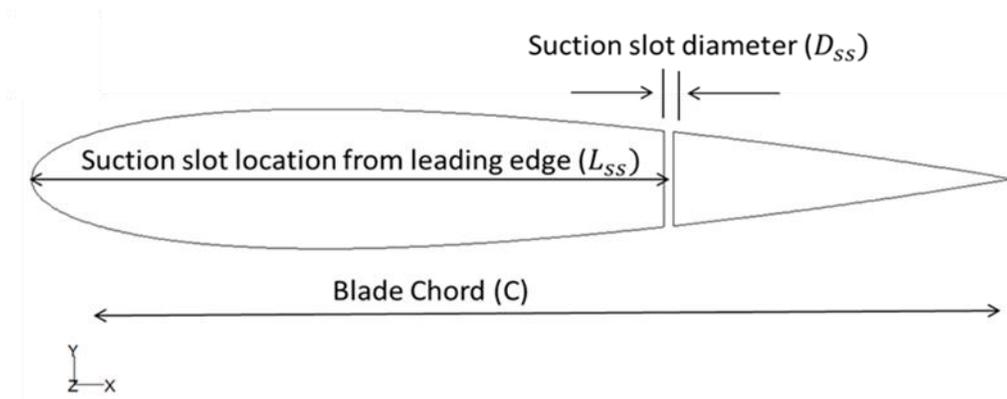
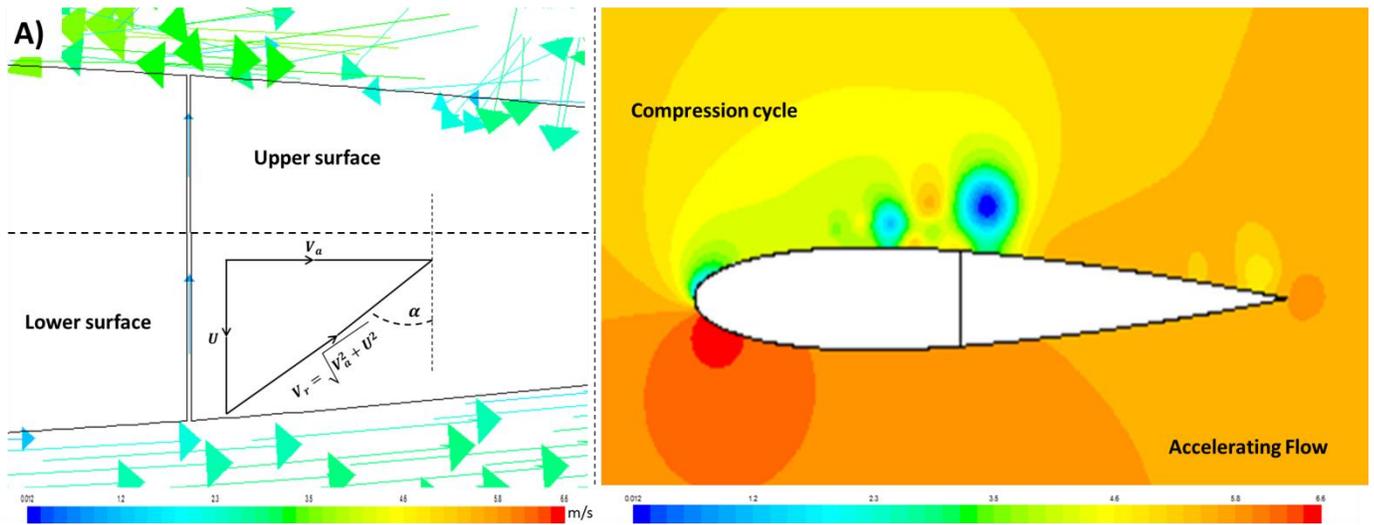
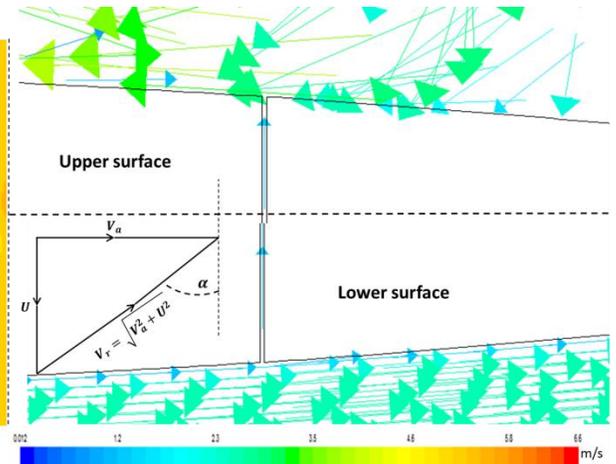
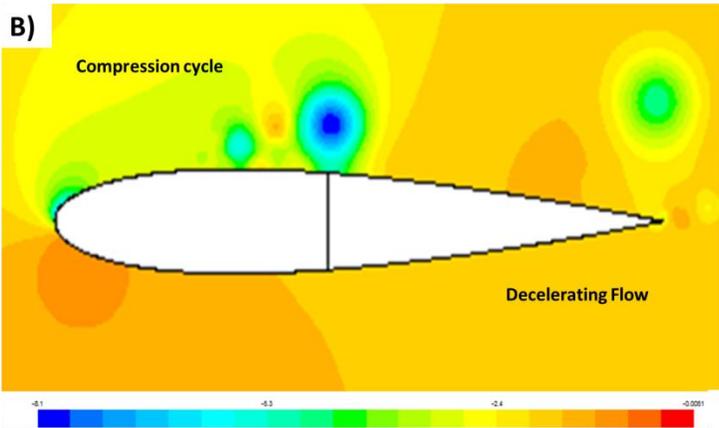


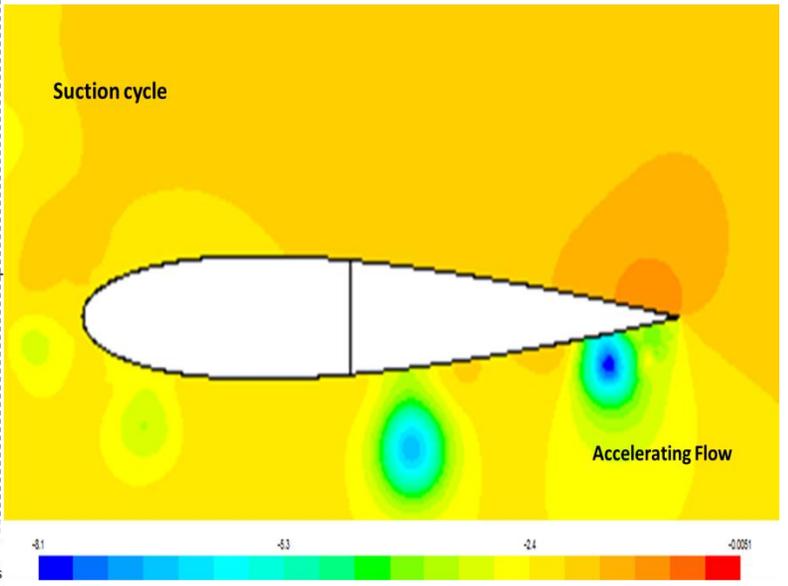
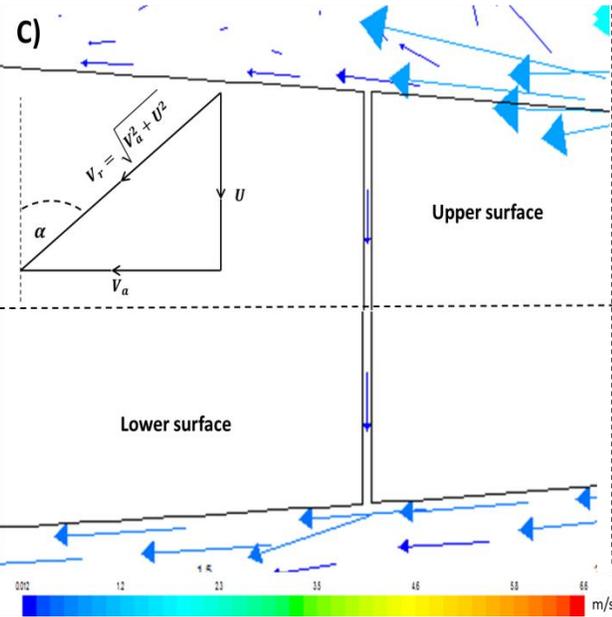
Figure 16 2D airfoil diagram with a slot



B)



C)



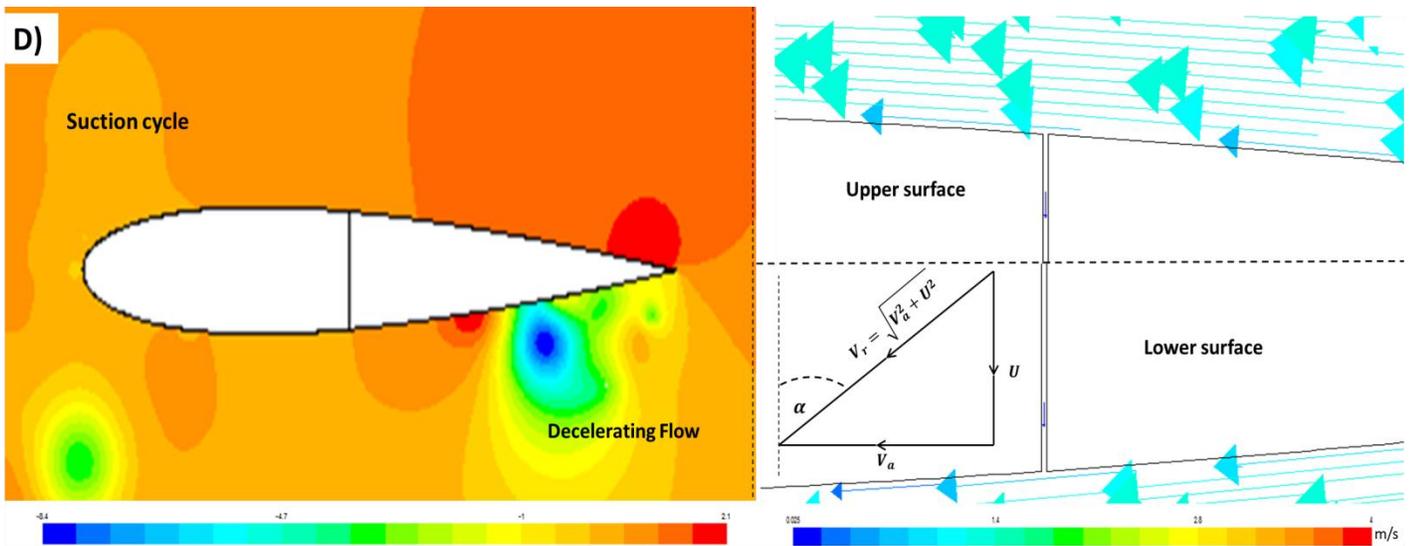


Figure 17 Factors affecting determination of the slot velocity direction for the Pressure distribution and Velocity vector direction A) Accelerating flow at compression cycle B) Decelerating flow at compression cycle C) Accelerating flow at suction cycle D) Decelerating flow at suction cycle

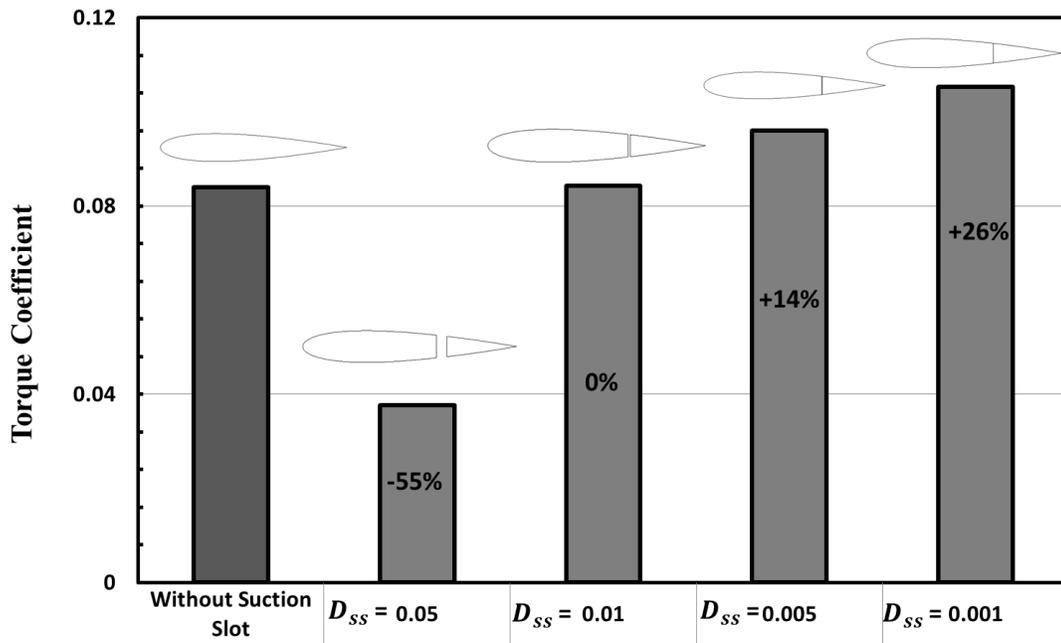


Figure 18 Torque coefficient for different D_{ss} at stall angle

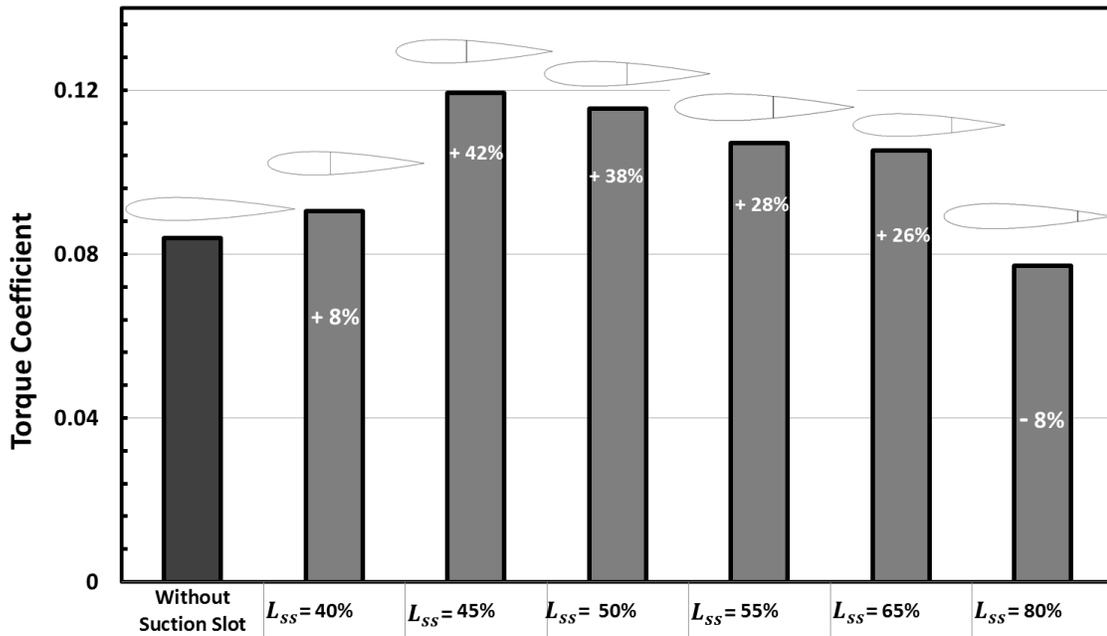


Figure 19 Torque coefficient for suction slots at different L_{ss} at 13.64 degree

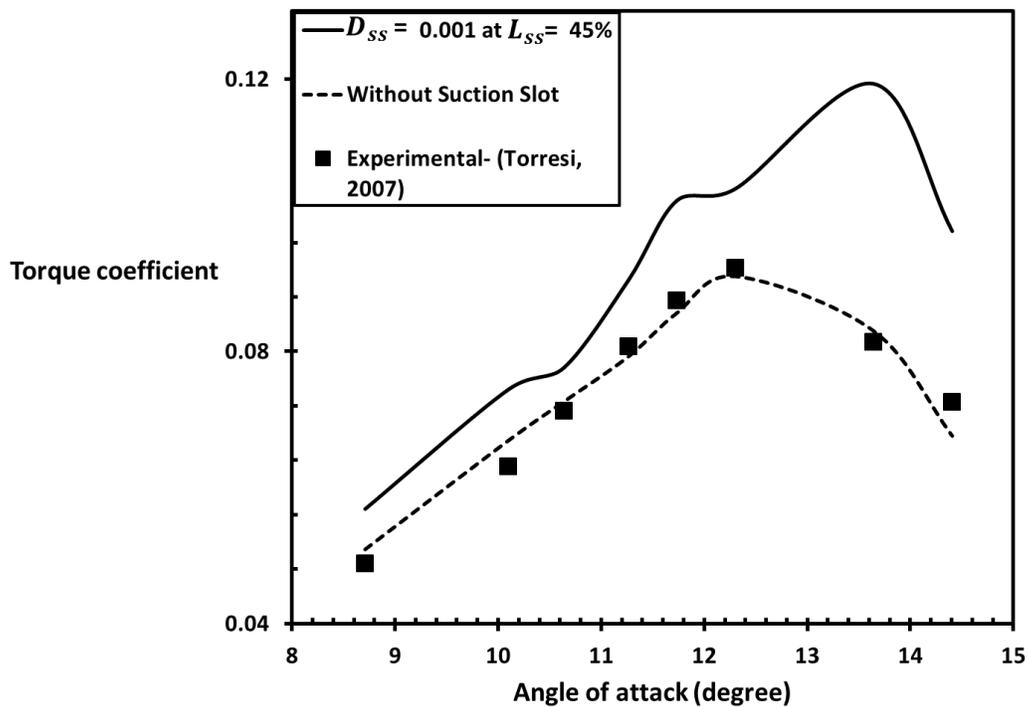


Figure 20 Suction slot with optimum L_{ss} (45%) and optimum D_{ss} (0.001 m) at different angles of attack

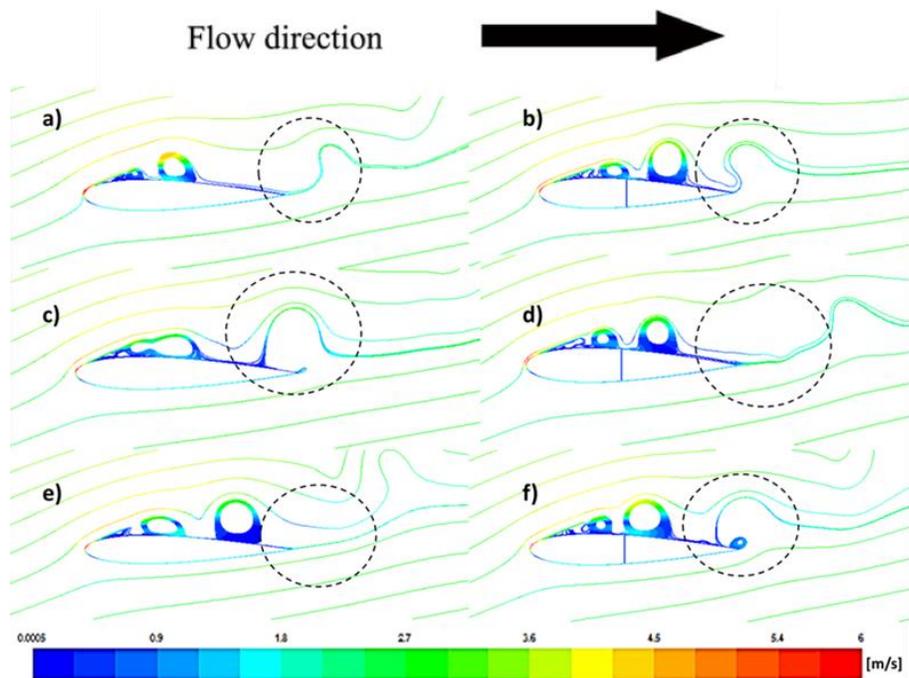


Figure 21 The Path-line for mean velocity magnitude at certain velocity equal to 2.92m/s unsteady input flow with non-oscillating velocity, a) and b) 12.3 degree, c) and d) 13.6 degree, e) and f) 14.4 degree

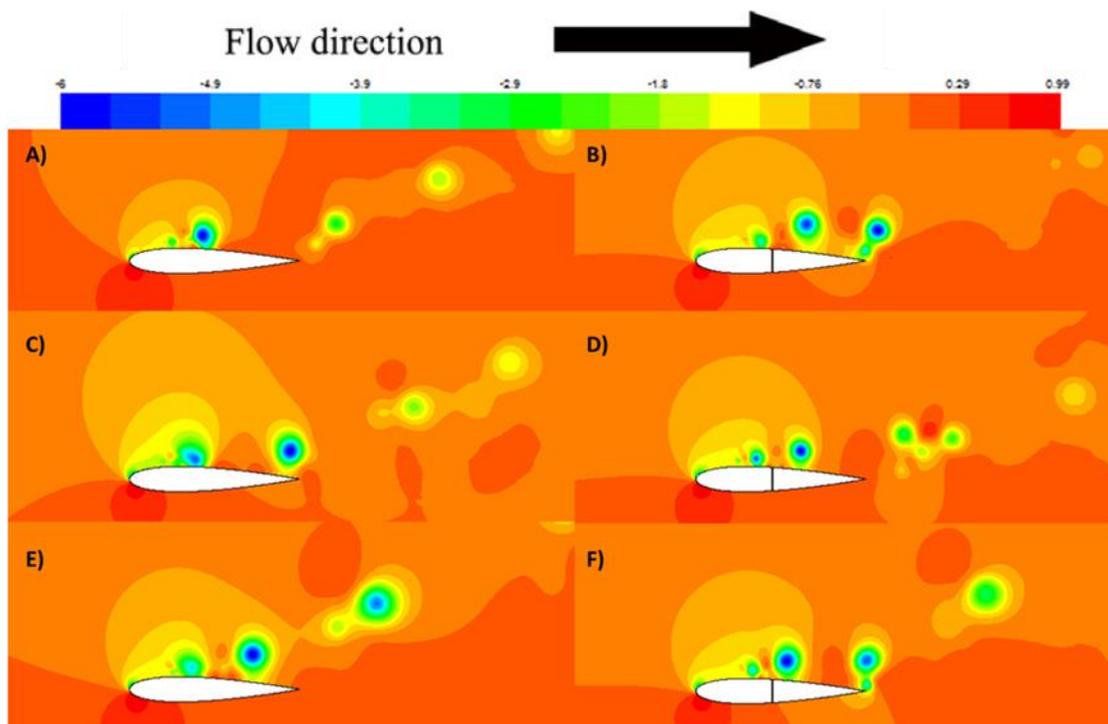


Figure 22 The pressure coefficient around the airfoil, unsteady input flow with non-oscillating velocity, A) and B) 12.3 degree, C) and D) 13.6 degree, E) and F) 14.4 degree

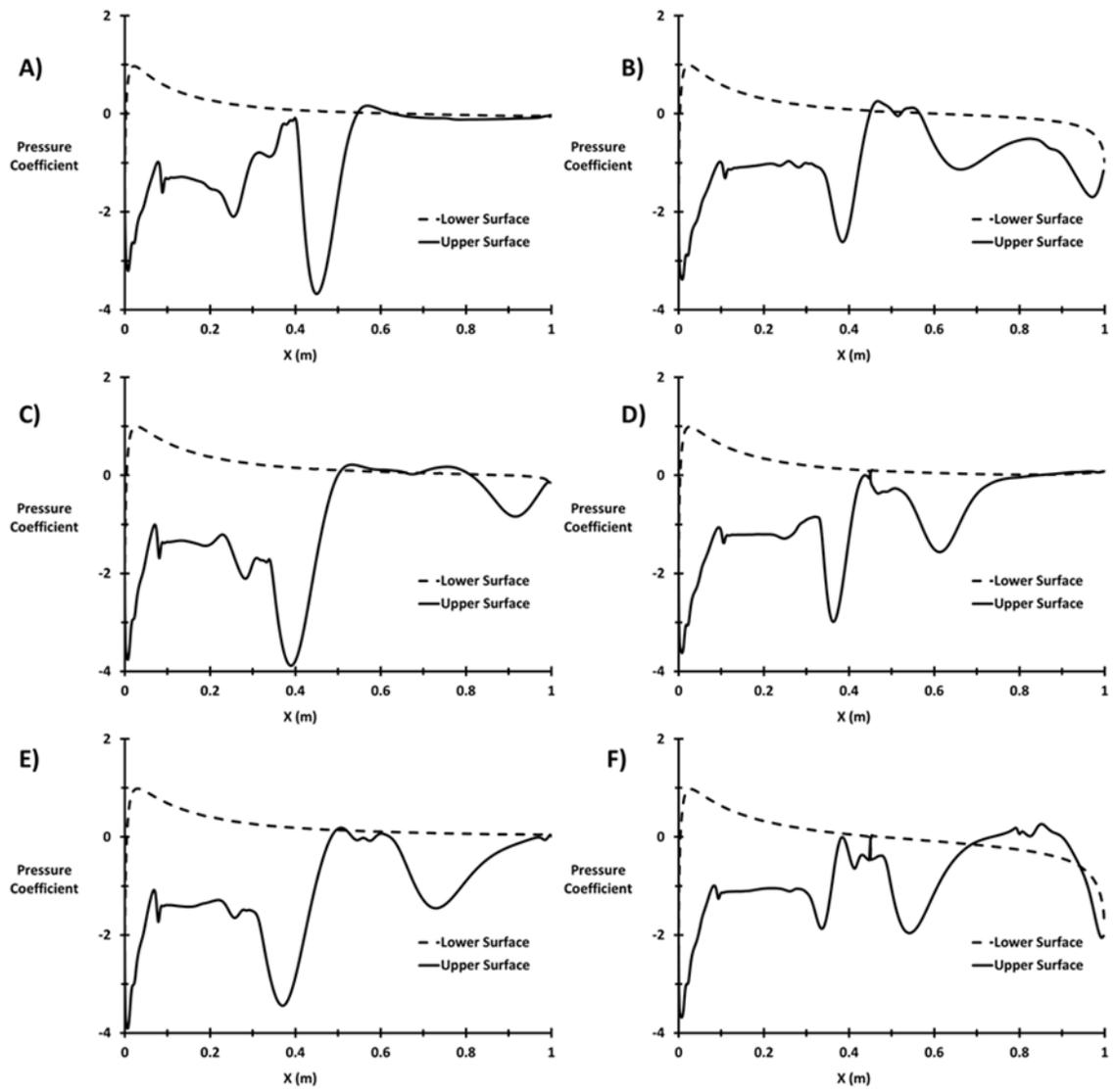


Figure 23 Pressure coefficient distribution on the upper and lower surface of the airfoil, A) and B) 12.3 degree, C) and D) 13.6 degree, E) and F) 14.4 degree

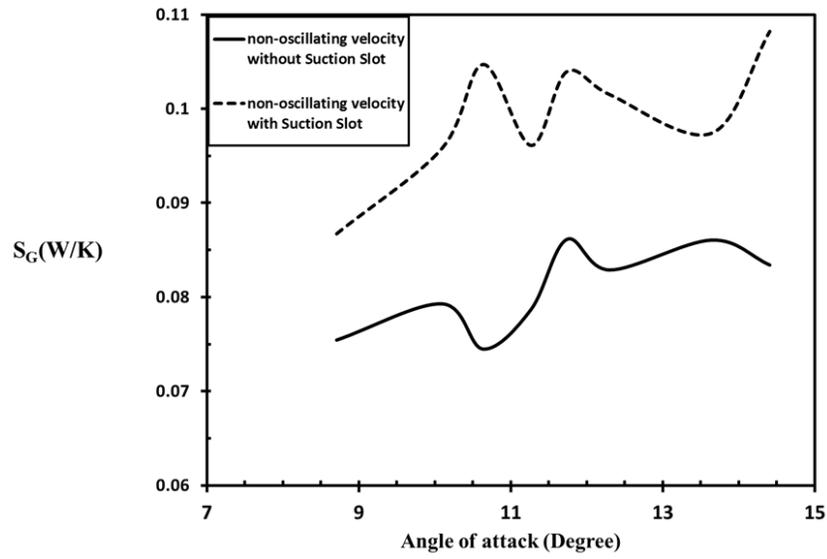


Figure 24 The effect of suction slot on the global entropy generation rate with different angle of attack

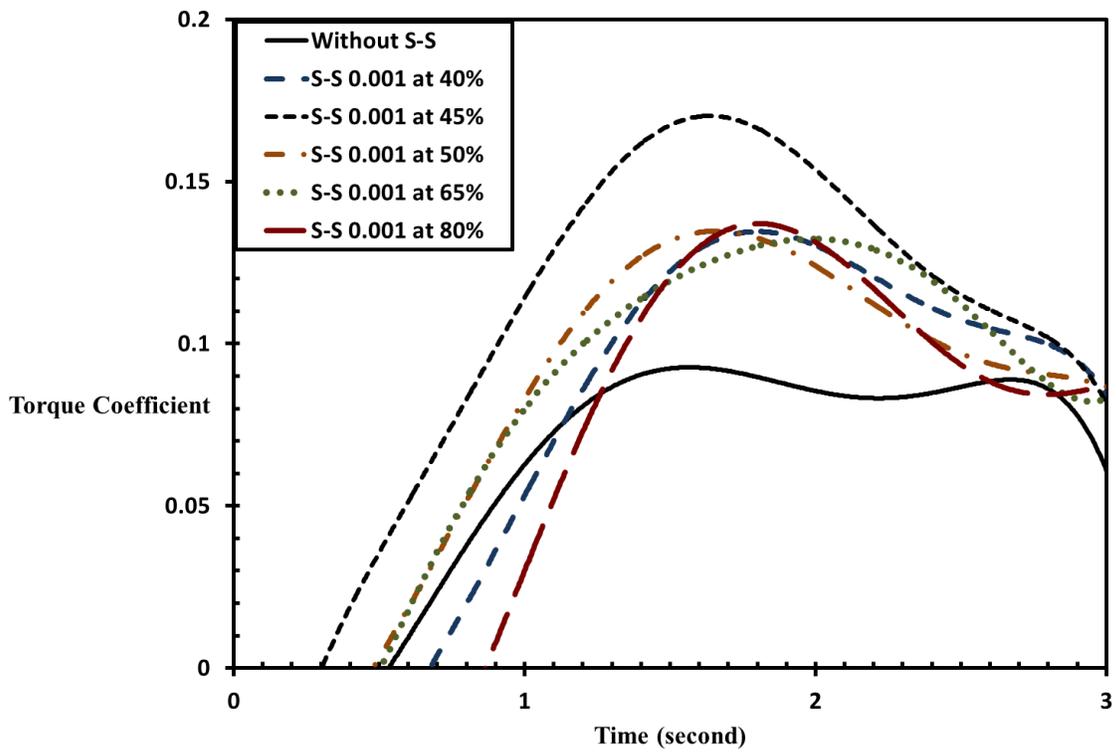


Figure 25 a) Suction slot with D_{ss} equal to 0.001 m at different L_{ss} for instantaneous torque coefficient at 13.6 degree under unsteady flow with sinusoidal inlet velocity

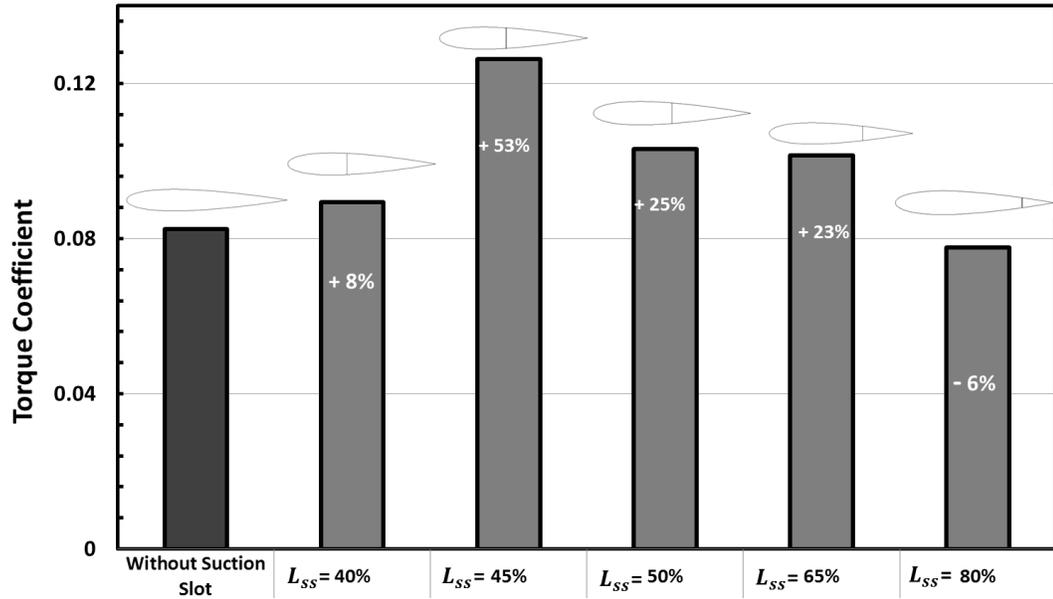


Figure 25 b) Suction slot with D_{ss} equal to 0.001 m at different L_{ss} for average torque coefficient at 13.6 degree under unsteady flow with sinusoidal inlet velocity

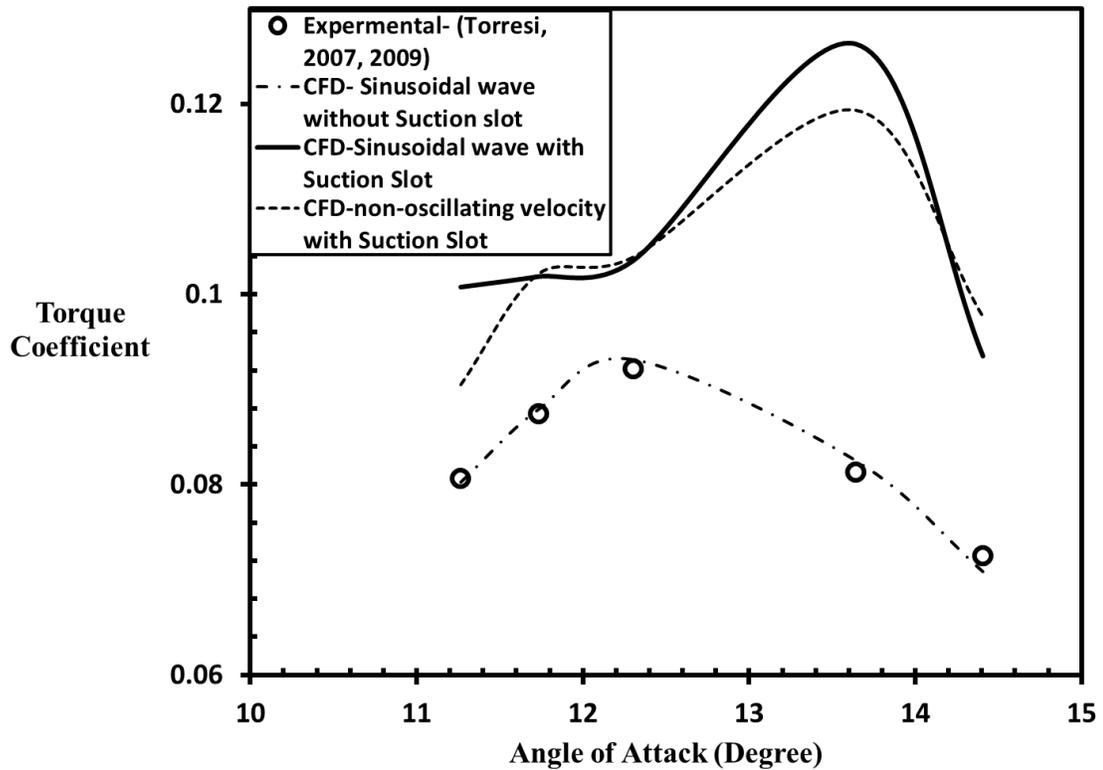


Figure 26 Suction slot with optimum L_{ss} (45%) and optimum D_{ss} (0.001 m) at different angles of attack under unsteady flow with sinusoidal inlet velocity

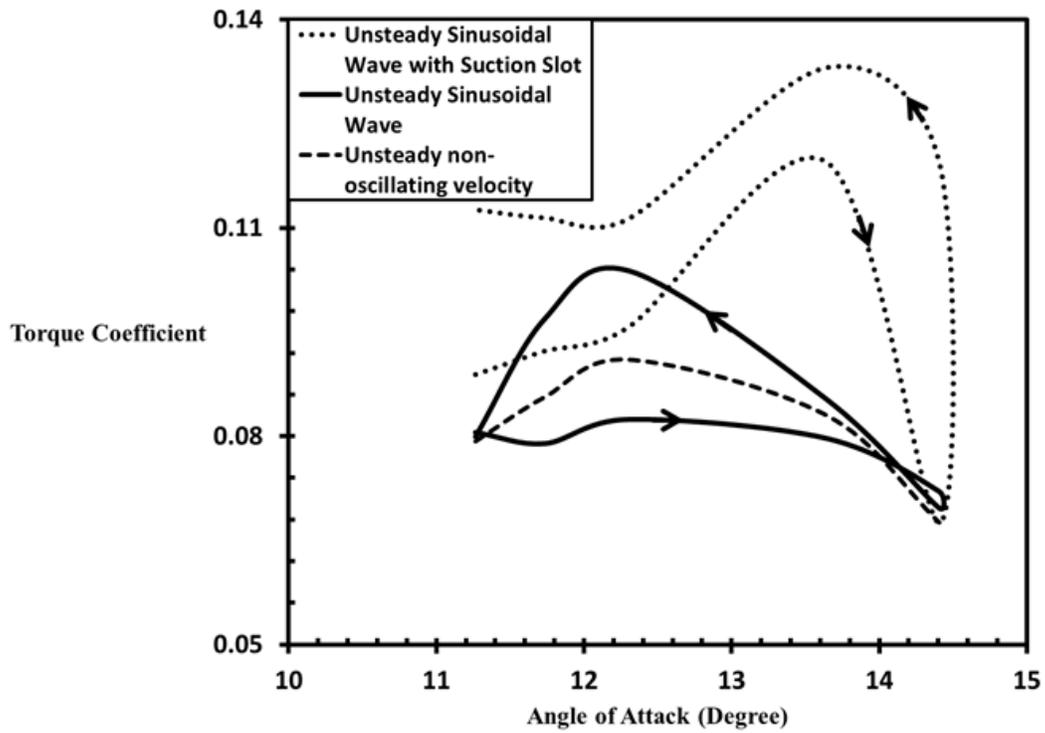


Figure 27 The hysteretic behavior due to unsteady flow with sinusoidal inlet velocity at different angles of attack with optimum L_{ss} (45%) and optimum D_{ss} (0.001 m)

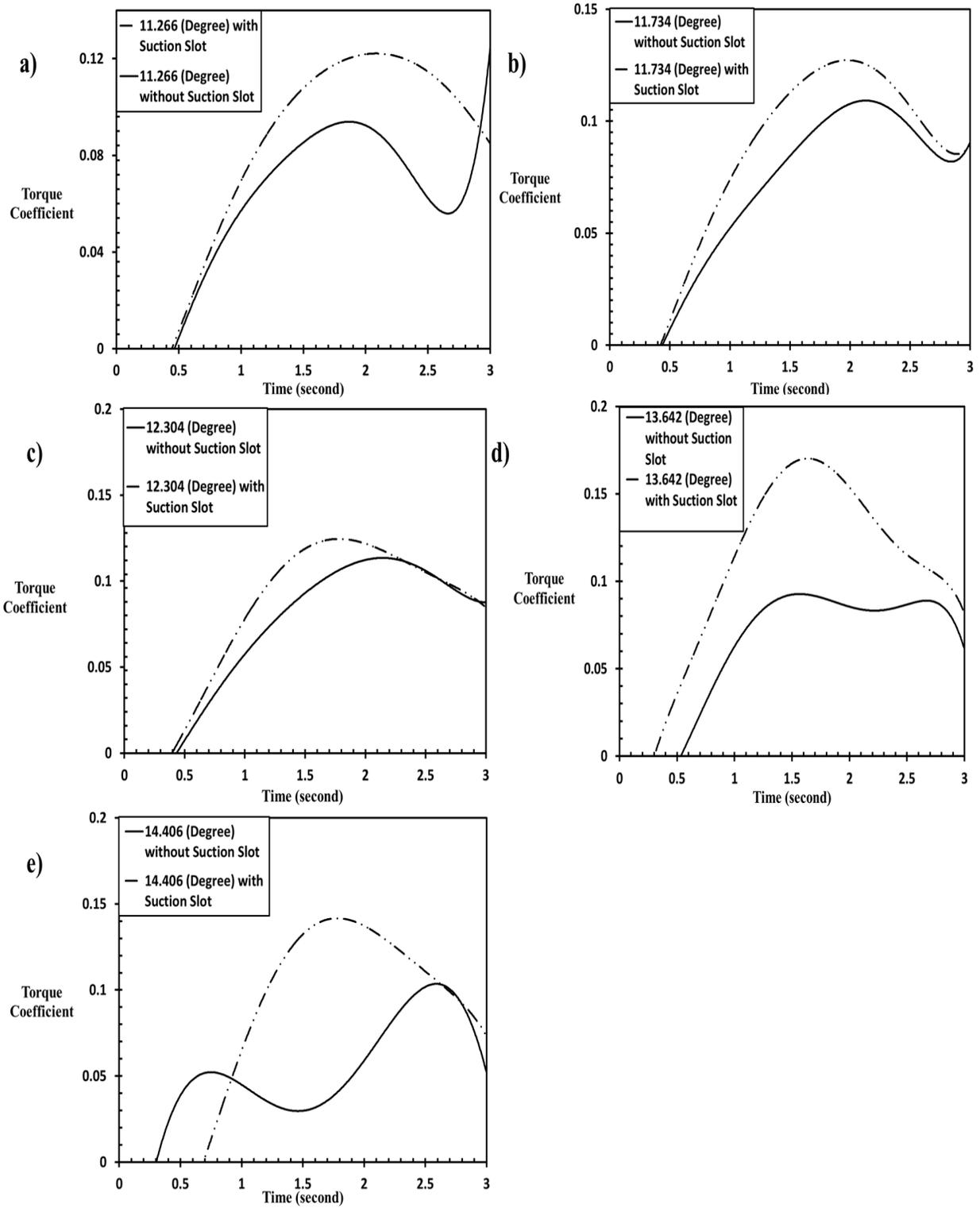


Figure 28 Torque coefficients at compression cycle for different angles of attack under unsteady flow with sinusoidal inlet velocity with optimum L_{ss} (45%) and optimum D_{ss} (0.001 m), a) 11.3 degree, b) 11.7 degree, c) 12.3 degree, d) 13.6 degree, e) 14.4 degree

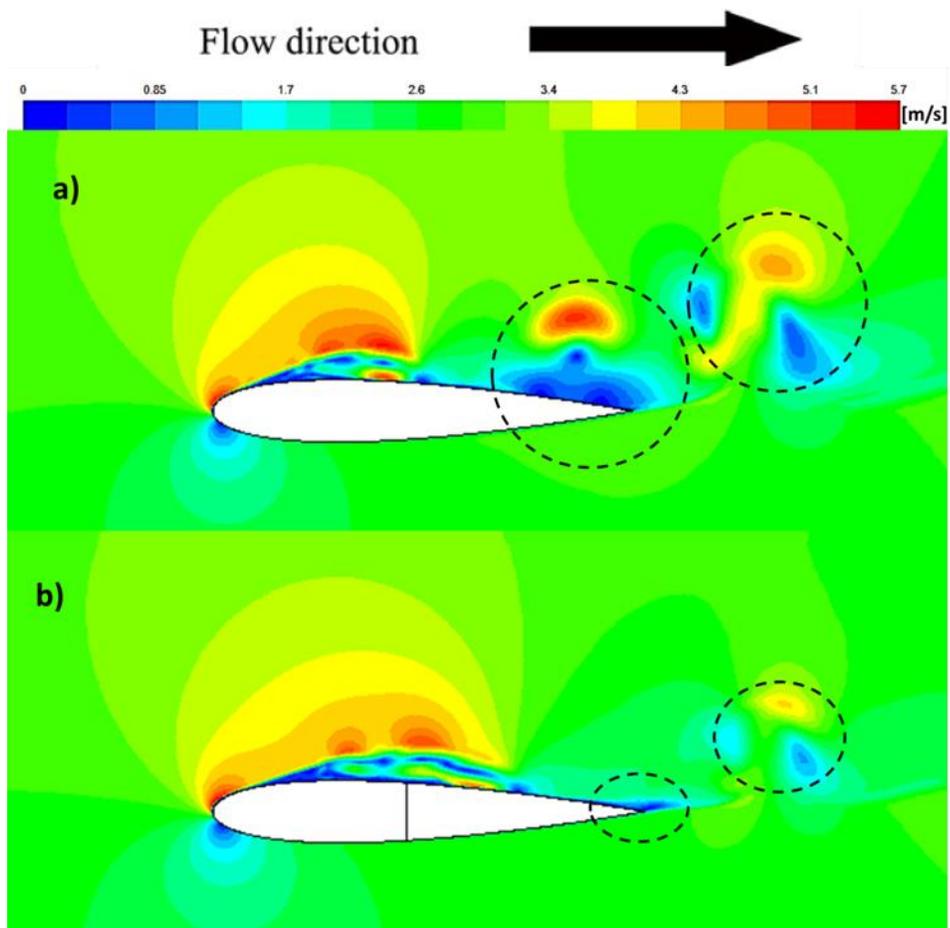


Figure 29 Velocity magnitude contours at maximum velocity equal to 2.92 (m/s) for sinusoidal input flow, at 12.3 (Degree), Before the Stall

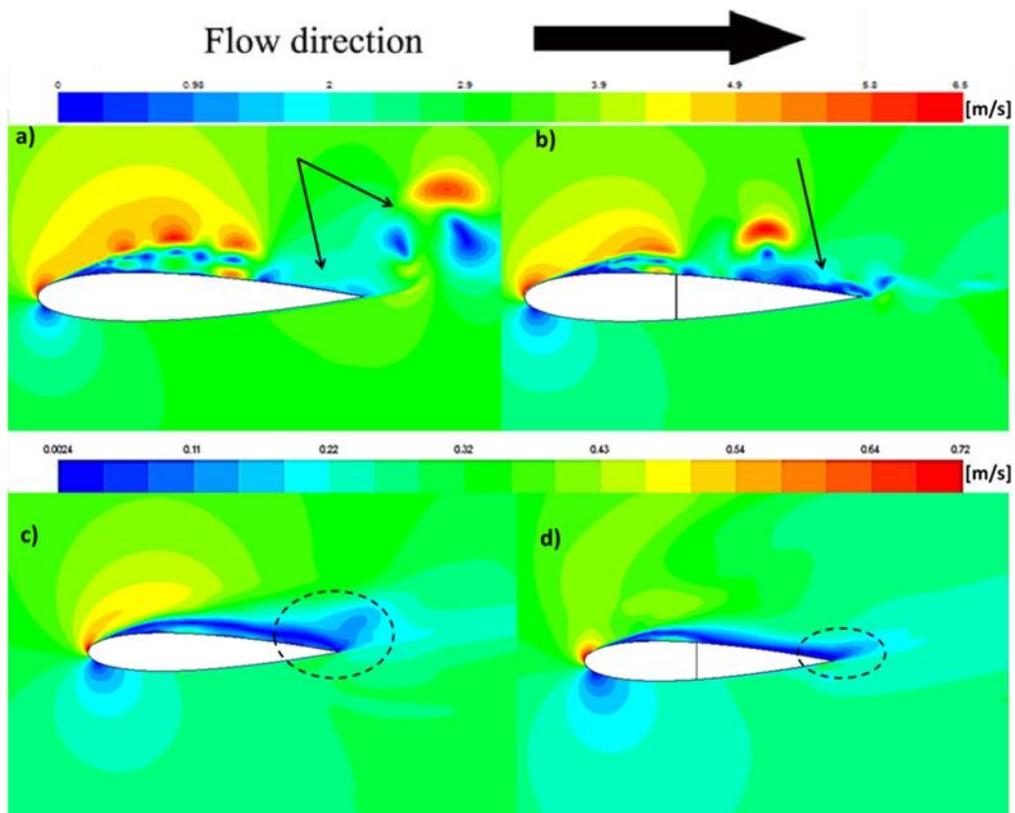


Figure 30 a) and b) velocity magnitude contours, c) and d) mean velocity magnitude contours, at maximum velocity equal to 2.92 (m/s) for sinusoidal input flow, at 13.6 (Degree), After the Stall

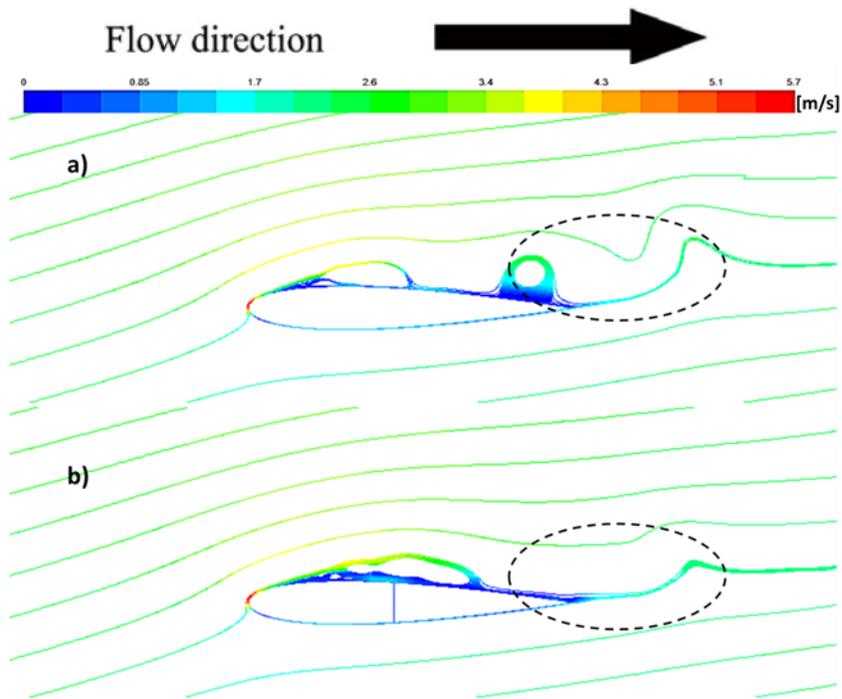


Figure 31 Path-line colored by mean velocity magnitude at maximum velocity equal to 2.92 (m/s) for sinusoidal input flow, at 12.3 (Degree), Before the Stall

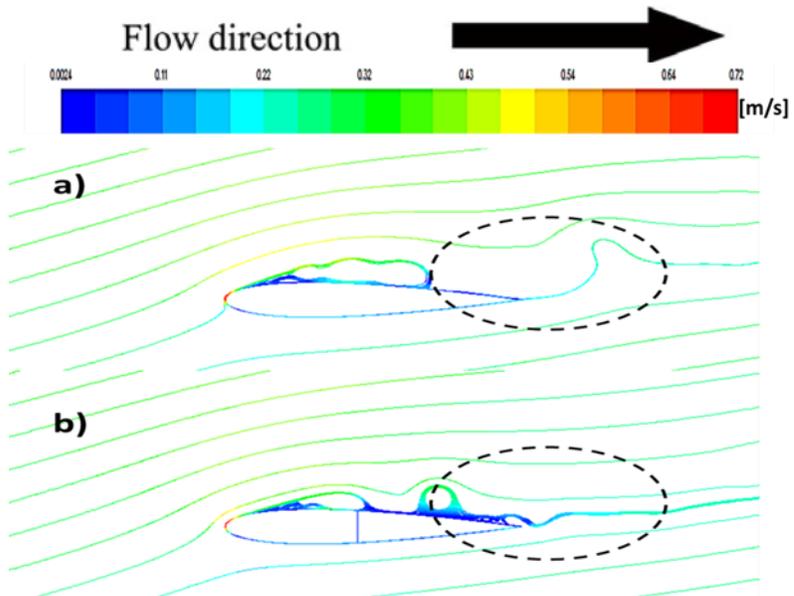


Figure 32 Path-line colored by mean velocity magnitude at maximum velocity equal to 2.92 (m/s) for sinusoidal input flow, at 13.6 (Degree), After the Stall

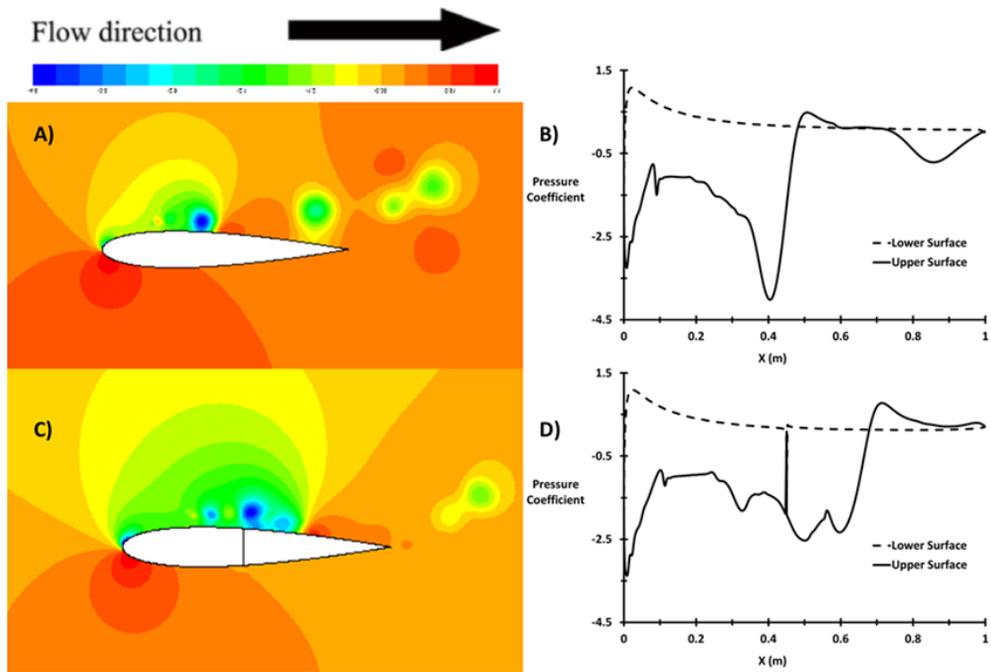


Figure 33 The pressure distribution at maximum velocity equal to 2.92 (m/s) for sinusoidal input flow, at 12.3 (Degree), Before the Stall

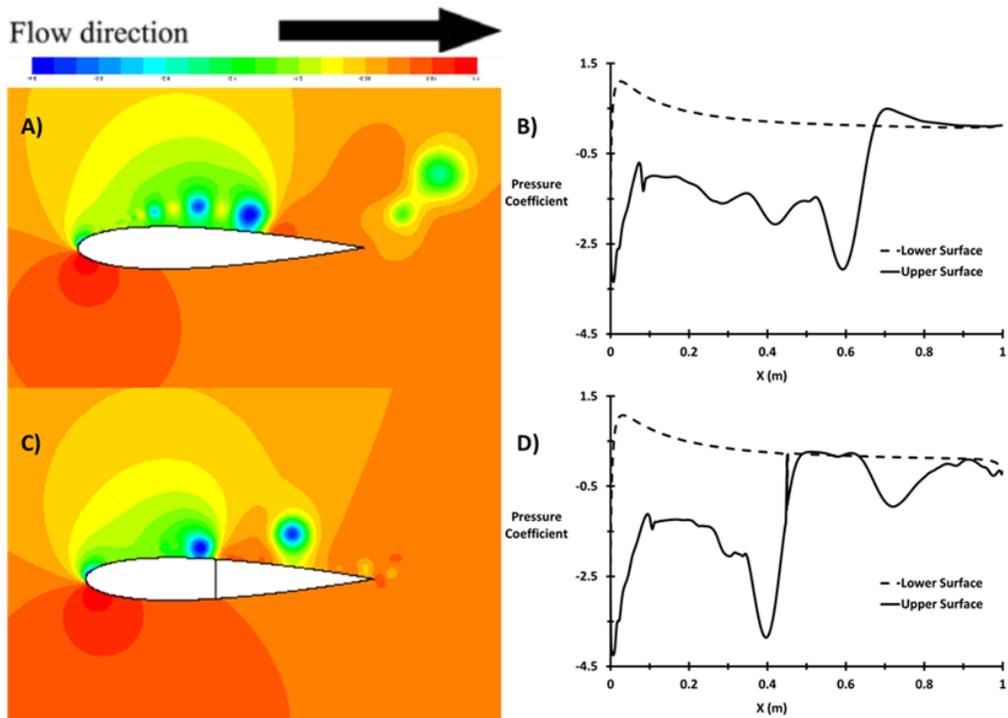


Figure 34 The pressure distribution at maximum velocity equal to 2.92 (m/s) for sinusoidal input flow, at 13.6 (Degree), After the Stall

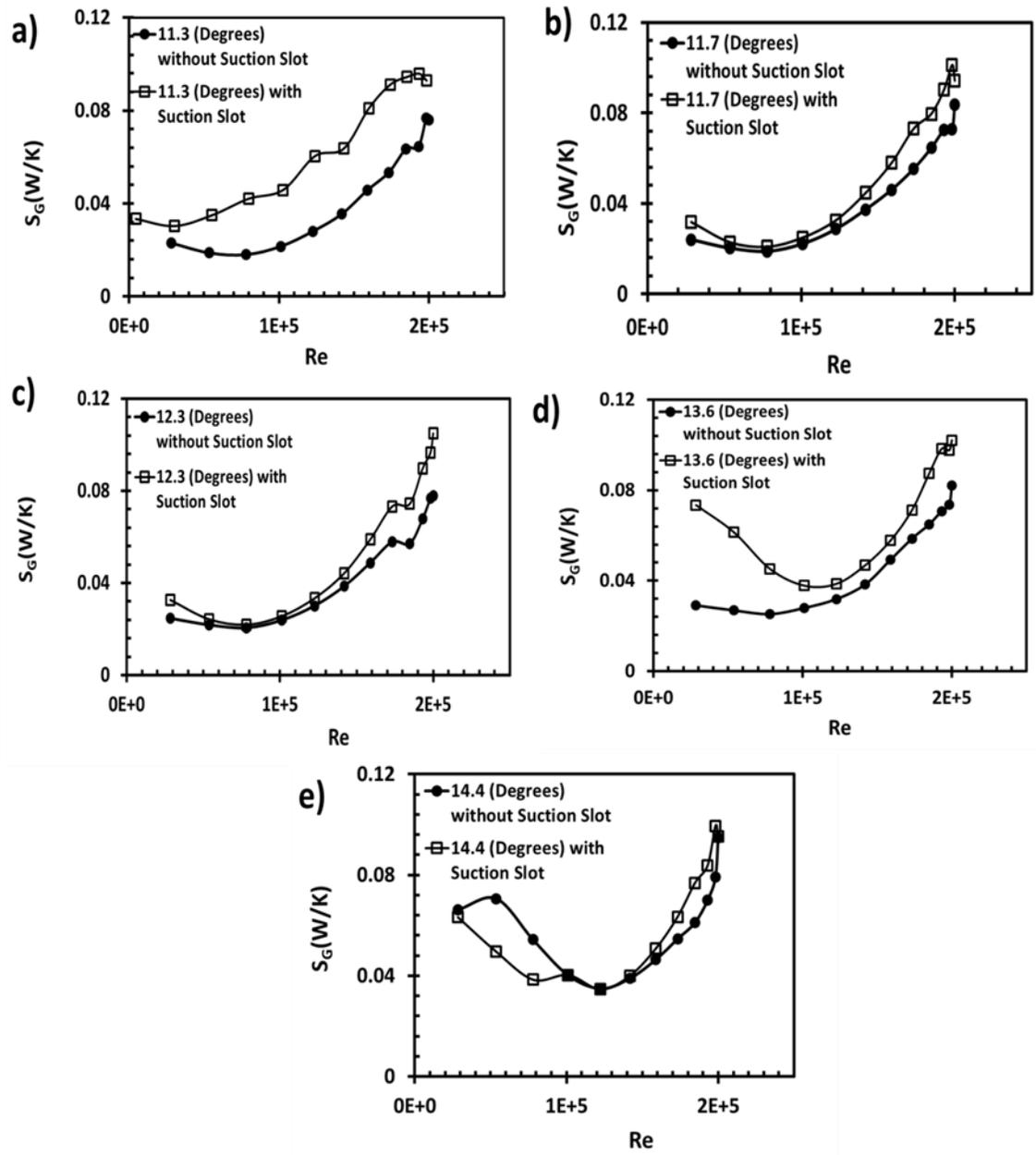


Figure 35 The global entropy generation rate variation with different Reynolds number at accelerating flow in compression cycle for different angles of attack with optimum L_{ss} (45%) and optimum D_{ss} (0.001 m)

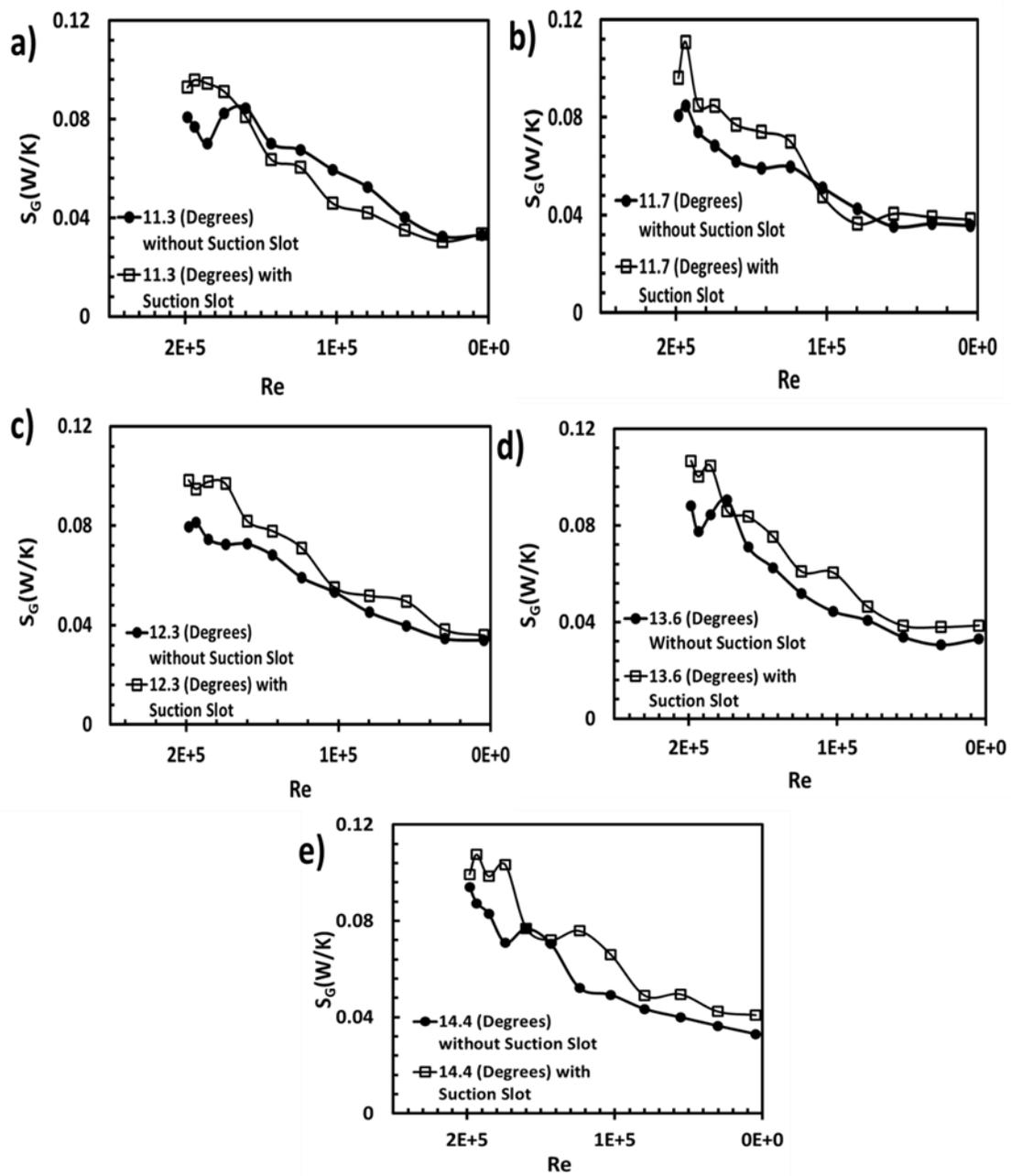


Figure 36 The global entropy generation rate variation with different Reynolds number at decelerating flow in compression cycle for different angles of attack with optimum L_{ss} (45%) and optimum D_{ss} (0.001 m)

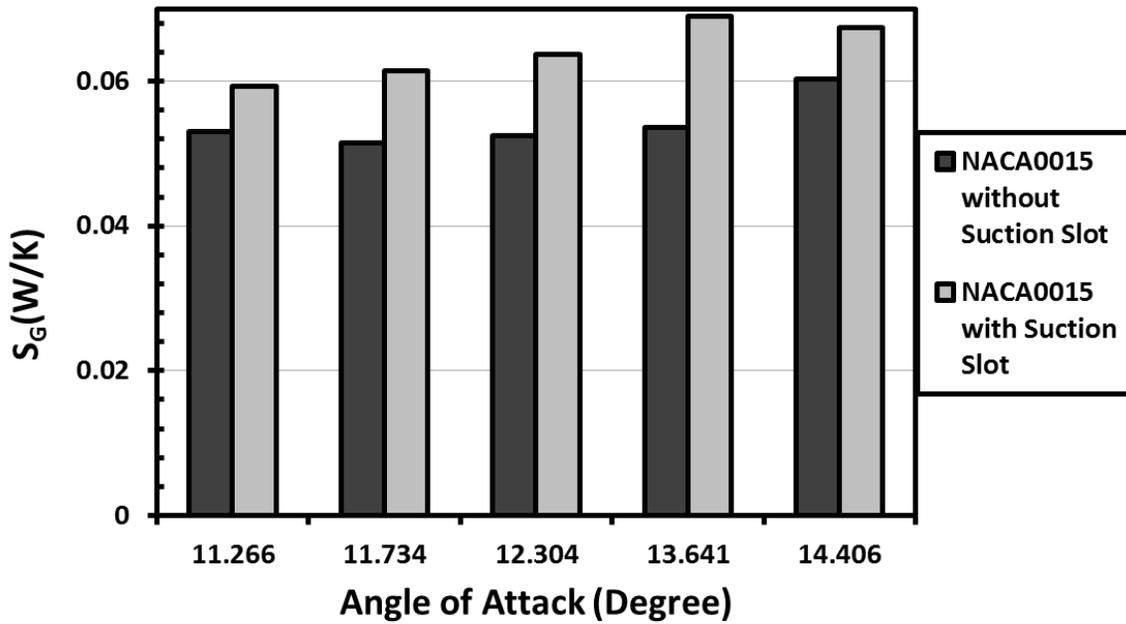


Figure 37 The global entropy generation rate in compression cycle for different angles of attack with optimum L_{ss} (45%) and optimum D_{ss} (0.001 m)

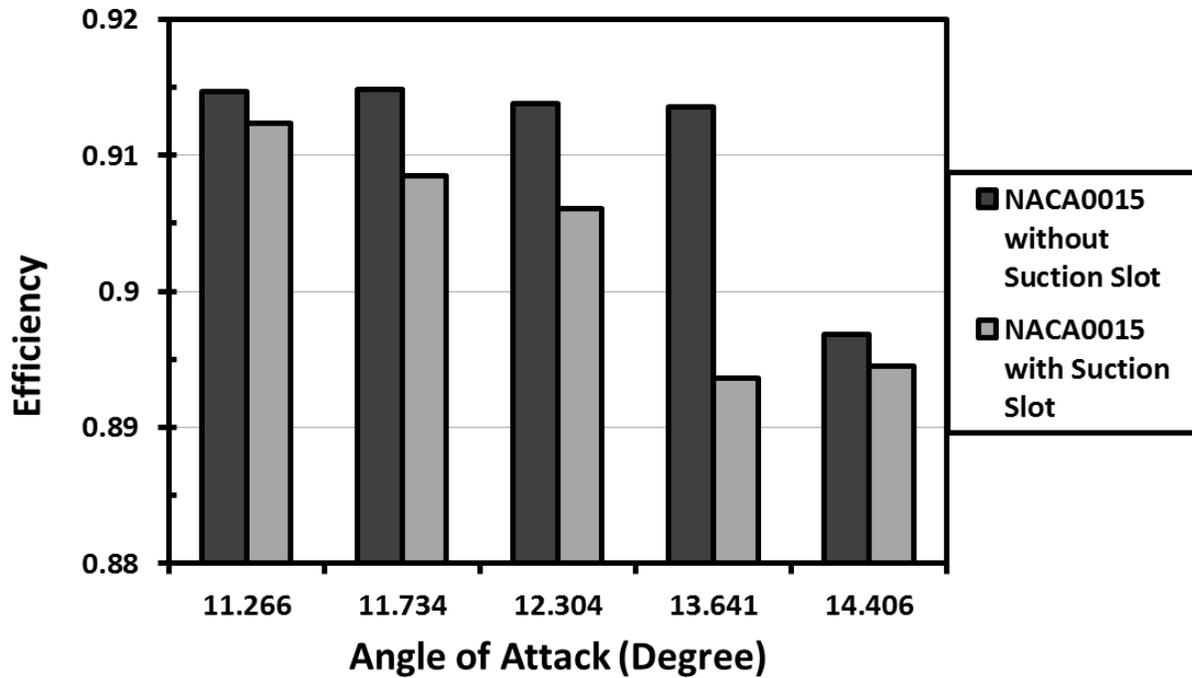


Figure 38 The second law efficiency in compression cycle for different angles of attack with optimum L_{ss} (45%) and optimum D_{ss} (0.001 m)

Table 1 The error percentage between measured torque coefficient from reference (Torresi, Camporeale et al. 2007, Torresi, Camporeale et al. 2007, Torresi, Camporeale et al. 2009) and calculated torque coefficient from CFD under unsteady flow with non-oscillating velocity

Torque Coefficient	Angle of attack (Degree)							
	8.709	10.097	10.639	11.266	11.734	12.304	13.642	14.406
Experimental	0.0488	0.0631	0.0712	0.0807	0.0875	0.0922	0.0814	0.0725
CFD	0.05092	0.06689	0.0726	0.0793	0.0856	0.091	0.083	0.0676
Error %	4	6	2	-2	-2	-1	2	-7

Table 2 The error percentage between measured F_D from reference ((Nomura, Suzuki et al. 2003) and calculated F_D from CFD under unsteady flow with sinusoidal inlet velocity

Frequency 2 Hz													
$F_D * 10^{-2}$ (N)	Time (Second)												
	14.02	14.1	14.12	14.2	14.3	14.34	14.4	14.5	14.6	14.7	14.8	14.9	15
Experimental	3.3	7.6	9.7	14.1	12.7	3.3	4	2.3	7.4	14.4	10.5	3.8	2.6
CFD	3.7	7.6	9.6	14.2	12.3	3.4	3.3	2.6	7.6	14.6	10.7	3.7	2.4
Error %	11	1	-1	1	-4	1	-17	17	4	1	2	-2	-11
Frequency 1 Hz													
Experimental	4.4	6.8	12.4	13.8	14	12.7	10	7.6	4.6	2.7	2.3	2.5	2.9
CFD	4.5	7.1	12.4	12.9	14	12.9	10.1	8.4	4.4	2.6	2.2	2.6	3.2
Error %	2	4	0	-7	0	1	1	10	-4	1	-4	4	10

Table 3 The error percentage between measured torque coefficient from reference (Torresi, Camporeale et al. 2007, Torresi, Camporeale et al. 2007, Torresi, Camporeale et al. 2009) and calculated torque coefficient from CFD under unsteady flow with sinusoidal inlet velocity

Torque Coefficient	Angle of attack (Degree)				
	11.266	11.734	12.304	13.642	14.406
Experimental	0.0807	0.0875	0.092	0.0814	0.0725
CFD	0.0803	0.0879	0.0931	0.0825	0.0709
Error %	-1	1	1	1	-2

Table 4 The improvement percentage between NACA0015 without suction slot and with suction slot at optimum L_{ss} and D_{ss} under unsteady flow with non-oscillating velocity

Torque Coefficient	Angle of attack (Degree)							
	8.709	10.097	10.639	11.266	11.734	12.304	13.642	14.406
Without Suction Slot	0.0509	0.0669	0.0726	0.0793	0.0856	0.091	0.083	0.0676
$D_{ss} = 0.001$ m at $L_{ss} = 45\%$	0.0568	0.0744	0.0776	0.091	0.1022	0.104	0.119	0.0977
Improvement %	12	11	7	14	19	14	44	45

Table 5 The improvement percentage between NACA0015 without suction slot and with suction slot at optimum L_{ss} and D_{ss} under unsteady flow with sinusoidal inlet velocity

Torque Coefficient	Angle of attack (Degree)				
	11.266	11.734	12.304	13.642	14.406
Without Suction Slot	0.0803	0.0879	0.0931	0.0825	0.0709
$D_{ss} = 0.001$ m at $L_{ss} = 45\%$	0.1008	0.1019	0.104	0.126	0.094
Improvement %	26	16	11	53	32