Performance Prediction for Sailing Dinghies

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Abstract

This study describes the development of an approach for performance prediction for a sailing dinghy. Key modelling issues addressed include sail depowering for sailing dinghies which cannot reef; effect of crew physique on sailing performance, components of hydrodynamic and aerodynamic drag, decoupling of heel angle from heeling moment, and the importance of yaw moment equilibrium.

In order to illustrate the approaches described, a customised velocity prediction program (VPP) is developed for a Laser dinghy. Results show excellent agreement with measured data for upwind sailing, and correctly predict some phenomena observed in practice. Some discrepancies are found in downwind conditions, but it is speculated that this may be related at least in part to the sailing conditions in which the measured data was gathered.

The effect of crew weight is studied by comparing time deltas for crews of different physique relative to a baseline 80kg sailor. Results show relatively high sensitivity of the performance around a race course to the weight of the crew, with a 10kg change contributing to time deltas of more than 60 seconds relative to the baseline sailor over a race of one hour duration at the extremes of the wind speed range examined.

Keywords
sailing; dinghy; velocity prediction program; performance modelling
Performance Prediction for Sailing Dinghies

1 Introduction

1.1 Velocity Prediction Programs

Velocity Prediction Programs (VPPs) for sailing yachts were first developed more than thirty-five years ago (Kerwin (1978)) and a wide variety of commercial software is available. Whilst many commercial VPPs address generic displacement sailing yachts, customised VPPs have also been written for a wide variety of vessels from classic yachts (Oliver and Robinson (2008)) to high performance hydrofoil dinghies (e.g. Findlay & Turnock (2008)). Conventional VPPs aim at calculating steady-state solutions for boat speed and attitude over a range of true wind speeds and directions; however some attention has also been focussed on time-domain solutions which can better address performance in waves, through manoeuvres, and with unsteady wind speed (e.g. Harris et al. (2001), Day et al. (2002), Verwerft and Keuning (2008))

Standard VPPs aimed at displacement yachts typically consist of three elements: an aerodynamic model, a hydrodynamic model, and a solution algorithm. In moderate winds, when the performance in which the full power of the sail plan is exploited, the solution algorithm typically adjusts the speed in the direction of motion and the heel angle to satisfy three equations of equilibrium – force in the direction of motion, force normal to the direction of motion, and moments about the centreline of the boat. Vertical equilibrium is assumed to be satisfied implicitly for displacement yachts. As wind speeds increase, the solution algorithm typically also modifies predicted aerodynamic forces to maximise speed in a manner attempting to reflect the physical reality in which sailors depower the sails to reduce heeling moment and side force. More sophisticated VPPs solve additional equations of equilibrium to investigate impact of design parameters on performance in more detail (e.g. Guelfi (2013); for example, solution of yaw equilibrium allows the impact of rudder angle on hydrodynamic forces to be assessed.
1.2 Velocity Prediction Programs for Sailing Dinghies

For a sailing dinghy of moderate performance the basic framework for a VPP is broadly similar to that for a sailing yacht, but there are several key differences. Unlike yachts, sailing dinghies do not generally reduce sail size (or reef) in stronger winds. Hence approaches used in “standard” VPPs to reflect the reduction in sail area by reefing are not appropriate, and the models used to reflect the impact of depowering should reflect this. Furthermore, the impact of crew weight on stability is relatively small for a displacement yacht, and as a first approximation, the heel angle for a given heeling moment is essentially linked directly to the righting moment via the GZ curve. In contrast for a modern sailing dinghy, crew weight can contribute more than 50% of the total weight; the crew can move around the boat, altering the heel and trim angles of the hull substantially. Whilst the maximum righting moment generated by the crew is ultimately limited by the size and weight of the crew and the positions which can be adopted during sailing, the freedom of the crew to move around the boat essentially decouples the heel angle from the available righting moment, and hence the boat can be sailed at a range of heel angles.

A more minor difference for sailing dinghies compared to yachts is that dinghies generally race around relatively simple and well-defined courses; hence the definition of complete speed polars defining the relationship between the boat speed and the angle sailed to true wind is not required. In many cases, windward-leeward courses are adopted in which only two legs are sailed – one directly upwind and one directly downwind. In these cases, naturally, only the maximum upwind and downwind velocities made good (VMGs) are of interest.

One final difference is in the use made of VPPs for dinghies. In the case of sailing yachts, VPPs are mainly used for design; however in the case of so-called “one-design” sailing dinghies there is little scope for design changes within the tolerances allowed in the class rule describing the hull dimensions. In the case of strict one-design classes such as the Laser all of the hulls are manufactured from moulds which are, in principle, identical, and the spars and sails are made by a
common supplier. Hence there is no scope for design improvement in the boat. However there are still avenues for exploration of performance changes via changes in the crew physique, particularly in the crew weight; for example if the weather statistics are known for a particular venue, the crew weight may be optimised to maximise the speed around a race course.

1.3 Velocity Prediction Programs for the Laser Dinghy

Binns et al. (2002) describe the development of a (physical) sailing simulator based on a Laser dinghy. This utilised an unsteady VPP, which included the equations of equilibrium for longitudinal and side forces as well as heel and yaw moments. The upright resistance was based on the Delft series regression equations (Gerritsma et al. (1993)), while the lift and drag forces from dagger board and rudder were estimated using coefficients from Lewis (1989). This VPP also utilised the sail coefficients from Marchaj (1979) of the aerodynamics of Finn dinghy sails, with corrections made to them to account for aspect ratio effects. The VPP also included a number of models for the dynamics of the boat in manoeuvres, including the assessment of static and dynamic cross-coupling effects, the impact of sheeting angle, rudder dynamics (sculling), gusts, and time dependent lift build-up. Results are given in the form of speed polars for 9 and 12 knots wind speed.

Carrico (2005) developed a simple VPP for a laser dinghy. The upright resistance of the hull was based on measurements obtained by towing a full-scale dinghy from a powerboat along a canal. Side force data for the dagger board and rudder was obtained from published data for the Laser foils in conjunction with an effective span. It is not clear in the paper how the resistance components associated with the foils or the induced resistance of the underwater body were calculated. The VPP also utilised sail coefficients from Marchaj (1979) in conjunction with FLAT and TWIST variables similar to those adopted here. Carrico stated that the first version of his VPP utilised IMS sail coefficients but that these led to over-prediction of sail forces, although he does not state in which conditions this was found to be the case. It should be noted that these are presented in terms of
angle of attack of the sail, rather than the heading of the boat, so an additional step is required in the VPP to estimate the sail trim at different headings, which is not explained.

The VPP solved for longitudinal, transverse, and heel equilibrium; however it was assumed that the boat remained upright in all conditions, based on argument that this gives the fastest performance. This is approximately true for upwind sailing, but is certainly not true when sailing downwind in light winds (see section 6.3). Heel equilibrium in the upright condition was achieved by adjusting the sail depowering variables. The programme allowed for sailors of different height and weight, at least for stability purposes, but the detail of the approach adopted to address this was not explained. Some anomalies were identified in regard to stability, including a lightweight (150lb) sailor out performing a heavyweight (210lb) in strong wind conditions, apparently due to a failure to maintain heel moment equilibrium. The results generally appeared somewhat noisy, with one or two unexpected deviations. Results from these two studies are discussed in section 6.2.

1.4 Current Study: The Laser Dinghy

The current study addresses the key differences between performance prediction for sailing dinghies compared to yachts, including the effects of depowering and the importance of crew weight. A customised VPP is then developed for a Laser dinghy, and the results are used to quantify the sensitivity of the performance of the boat to crew weight, enabling the identification of the optimum crew weight for the boat to be chosen for a given wind condition to maximise the speed around a simple windward-leeward race course.

The Laser dinghy is one of the most popular single-handed sailing dinghies in the world with over 200,000 built since it was launched in 1971. The Laser is a very simple boat, with an unstayed mast and very limited sail shape controls compared to many other modern boats. The standard Laser was adopted as a men’s class in the Olympics in 1996, and a version with a smaller rig (the Laser Radial) was adopted as a women’s Olympic class in 2008. The Laser is a strict “one-design” class, with all boats, spars and sails intended to be identical.
2 Aerodynamic model for sailing dinghies

2.1 Background

Aerodynamic models in VPPs are often based on data taken from the Offshore Racing Congress (formerly IMS) VPP (Offshore Rating Congress (2013) section 5). This data consists of sets of baseline lift and drag coefficients tabulated at discrete apparent wind angles for fully powered-up sails. The interpolation for apparent wind angles between these points is carried out using a cubic spline. Two sets of data are quoted reflecting the difference between “simple” rigs with limited control on mast bend (and hence sail shape), which use the “low lift” coefficients, and more complex rigs which deploy additional rigging such as inner forestays or check stays to give greater control over mast bend and hence sail shape.

The majority of sailing dinghies have relatively simple fractional rigs, with limited control on mast bend, while some single sail boats such as the Laser have unstayed masts, and hence it seems appropriate to use the low lift coefficients, especially for dinghies without “fully-battened” rigs. However, since these coefficients are derived from wind tunnel tests of sailing yachts rather than dinghies, some further confirmation of the validity of the data in the current context is desirable.

Bossett and Mutnick (1997) measured sail forces on a full-scale Laser mounted on a stationary dynamometer in a real wind field. Results are presented for driving and heeling force coefficients (rather than lift and drag) up to wind angles of about 150 degrees. The data exhibits a large amount of scatter, and the coefficients appear to be rather high compared to other published data; furthermore it is not clear how the sail area was calculated. For these reasons the data was not utilised in the present study. Flay (1992) made wind tunnel measurements on a rig modelled on a Laser at 1/6 scale, including a model of the above-water part of the hull, though it should be noted that the sail proportions quoted do not exactly match those measured by the present author on a Laser sail. The measurements were made at apparent wind angles of 30 degrees and 60 degrees as measured in the horizontal plane. These were chosen to represent upwind and reaching conditions.
Tests were carried out in turbulent and “smooth” flow. The tests were carried out at a range of heel angles from 0-30 degrees; the apparent wind resolved in the plane of the deck varied from around 26 degrees to 30 degrees in the upwind case.

The lift coefficients quoted in the upwind condition peaked around 1.53 in turbulent flow at an apparent wind angle in the deck plane of around 28.5 degrees. In smooth flow, the value at the same angle was 1.61. These lift coefficients appear rather high in comparison with those of Table 1. However the sail area used as a reference for the calculation of the coefficients is the “triangular” area based on the luff and foot lengths. In contrast, the sail area used in conjunction with the ORC coefficients is the cloth area calculated according to the ORC formula, with a correction for additional area due to the foot curve. Correcting for this difference in area reduces the Laser sail lift coefficients in smooth and turbulent flow from Flay’s study respectively to 1.30 and 1.36. The value in the ORC table for “low lift” mainsail coefficients at an angle of 28 degrees is 1.347, which falls between these two values, suggesting that the ORC “low lift” coefficients are appropriate for a Laser, at least for upwind sailing. The full set of coefficients is given in Table 1.

The drag coefficients given by Flay (loc.cit.) relate to the total aerodynamic drag, including the effects of the spars and hull (no model crew was used). The total drag coefficient measured in the wind tunnel in turbulent flow, corrected to the cloth area of the sail, was around 0.27. It can be seen from Table 1 that little of this drag can be expected to result from the viscous drag of the sail, with the majority coming from induced drag and parasitic drag of hull and spars. In comparison, at this angle of attack, with 10 degrees of heel (corresponding to the wind tunnel tests) the predicted total drag coefficient based on the ORC coefficients and approach to parasitic drag calculation (excluding the crew) is 0.20. It is difficult to explain this discrepancy; however given that only a very small data set is available from these tests, the ORC approach is adopted here.

The Centre of Effort (CE) is calculated here according to the ORC approach, with a correction for the foot curve of the sail, resulting in a value 36.4% of the luff length above the boom. The longitudinal
position (required for the yaw balance calculation) is assumed to be 33% of the foot length aft of the
luff. It should be noted that the Laser exhibits significant mast bend when sailing upwind which has
the effect of moving the CE further aft than if the mast were straight. Analysis of photographs of
Lasers sailing upwind indicates a typical equivalent mast rake at the CE height of 11 degrees; this
value is utilised in the yaw moment calculation in the upwind condition.

2.2 Depowering models for sailing dinghies

In stronger winds, when boat speed becomes limited by the available righting moment, sailors
depower the sails to reduce heeling moment and thus heel angle. By reducing the lift and/or heeling
leverage, the heel angle is reduced and the impact of reduced hull resistance is traded off against the
reduction in drive. In the case of sailing dinghies which generally cannot reef (i.e. reduce sail area),
the modelling of this depowering process is particularly important when considering the impact of
crew weight on performance.

2.3 REEF, FLAT and TWIST

In VPPs, depowering is normally addressed by modifying sail coefficients using a semi-empirical
depowering model. A commonly adopted approach in simple yacht VPPs, as proposed originally by
Kerwin (1978), utilises the non-dimensional REEF and FLAT coefficients. These effect a rather
idealised representation of the physical processes of reefing and flattening sails, affecting lift, drag
and heeling moment from the sailplan. The fully powered up lift and drag coefficients are described
as:

\[
\begin{align*}
C_L(\beta') &= C_{L,\text{max}}(\beta') \\
C_D(\beta') &= C_{D_v}(\beta') + C_{D_p} + C_{L,\text{max}}^2 \left( \frac{1}{2} \pi AR_e + C_{D_h} \right)
\end{align*}
\]

Here \( C_{L,\text{max}} \) is the fully-powered lift coefficient at the apparent wind angle \( \beta' \) in the heeled plane,
\( C_{D_v} \) is the viscous drag coefficient, while \( C_{D_p} \) is the parasitic drag coefficient associated with hull,
mast, crew etc. The final term in the drag equation is the lift-related drag $C_{L_{max}}^2 \left( \frac{1}{\pi AR_E} + C_{Dv} \right)$.

Here the first term in the bracket is the induced drag based on the standard result from lifting line theory, using an effective aspect ratio $AR_E$. The second term $C_{Dv}$ is the separation drag coefficient reflecting the increase in viscous pressure drag with lift in 2D flow due to boundary layer thickening.

$C_{L_{max}}$ and $C_{Dv}$ are obtained by interpolation from tabulated values varying with apparent wind angle, while $C_{Dv}$ is typically treated as a constant, taken here as 0.005. The effective aspect ratio $AR_E$ is calculated from the geometric aspect ratio based on rig geometry modified using empirical coefficients. These coefficients are modified by the $REEF$ and FLAT coefficients $r$ and $f$ to give:

\[
C_L^*(r, f, \beta') = f \cdot r^2 \cdot C_{L_{max}}(\beta')
\]
\[
C_D^*(r, f, \beta') = r^2 \left( C_{Dv}(\beta') + C_{Dp} + f^2 \cdot C_{L_{max}}^2 \left( \frac{1}{\pi AR_E} + C_{Dv} \right) \right)
\]

where $C_L^*$ and $C_D^*$ are the depowered lift and drag coefficients. The effect of FLAT is to reduce the lift coefficient without affecting viscous drag. This corresponds loosely to the impact of flattening the sails. The solution algorithm for a simple VPP for a displacement yacht typically adjusts the depowering parameters $r$ and $f$ to maximise the speed whilst satisfying horizontal plane and heel equilibrium. Vertical equilibrium can be considered to be satisfied by default for a displacement vessel. Whilst this model has been remarkably successful, and has been used for many years a number of limitations have become increasingly obvious. One limitation of this model is that it implicitly assumes that the coefficient linking the lift-related drag to the square of the lift remains independent of $REEF$ and FLAT via the relation:

\[
\frac{C_{Dv}}{C_L^2} = \left( \frac{1}{\pi AR_E} \right) \quad \text{on} \quad \frac{C_{Dv}}{C_L^2} \quad k
\]

Wind tunnel tests such as those of Fossati et al. (2006) and Hansen et al. (2006) have shown that the relationship between lift and lift-induced drag is not as simple as equation (4) suggests. When sailors
are sailing upwind in moderate wind conditions, in which heel is not a limiting factor, the sails will typically be trimmed to generate maximum drive. In these conditions, wind tunnel tests suggest that some flow separation is present (Fossati et al. (2006)), and hence the drag in this condition is higher than suggested by the calculation. As the wind speed increases sailors typically reduce heeling moment when sailing upwind by increasing the twist of the sails before reefing. Adjusting the sails to generate more twist than the optimum value reduces the heeling moment by selectively depowering the upper part of the sail; however it simultaneously increases the induced drag coefficient (Hansen et. al. (2006)).

A more refined approach, originally proposed by Jackson (1996, 2001), and developed further by authors such as Hansen et al. (2006), introduces a TWIST coefficient. The idea of this coefficient is that the distribution of lift is modified so that less lift is generated higher in the sail and more lift is generated lower in the sail so that the total lift generated by the sail remains unchanged. This coefficient may be used in addition to REEF; however in the current study, since dinghies do not reef, TWIST is used in place of REEF. Using the TWIST model for a single sail boat the height of the centre of effort above the boom is calculated as:

\[
Z_{CEb} = Z_{CEb} \cdot (1 - t)
\]

Where \( t \) is the TWIST coefficient. In the results presented here, the value of the coefficient for the “baseline” crew (see section 6.3) of 0.186 in 15 knots of true wind corresponds to a centre of effort located 32% of the height of the sail above the boom. In reality as the lift distribution is modified by the sail twist to reduce the height of the centre of effort, the ratio of induced drag to the square of the lift increases: a more highly twisted sail generates more induced drag at the same lift coefficient than a less twisted sail. A typical formulation for the modified drag for a sailing dinghy (i.e. without using the REEF parameter) takes the form:
The value of $C_{\text{twist}}$ is taken here as 8.0, following Jackson (2001). Increasing twist thus has a net effect similar to reducing the effective aspect ratio. This approach to twist is rather different from that adopted in the 2013 ORC VPP (Offshore Racing Council (2013)) for a sloop-rigged yacht, which corrects the centre of effort height in relation to the $FLAT$ parameter as well as the “fractionality” of the rig, but neglects the impact of twist on induced drag.

### 2.4 Other Approaches

In the ORC model $FLAT$ cannot be reduced below 0.6, based on the recommendation of Fossati et al. (2006). This limitation is based on observation of sail flattening in wind tunnel tests and corresponds to a 40% reduction from the maximum lift coefficient. Yachts will typically start to consider reefing once this point is reached, since it can be more effective to use a smaller sail fully powered than to depower a larger sail by other means. However for sailing dinghies reefing is not an option, and hence if this limit is strictly imposed increasing $TWIST$ is the only method of further depowering once this limit is reached. This does not reflect sailing practice particularly well. In reality once dinghy sailors are overpowered with the sail flat, one part of the sailor’s natural reaction is to “spill wind” by releasing the mainsheet, whilst controlling sail twist using the vang (or kicking strap). The effect is to reduce the angle of attack of the sail, thus reducing the lift force, rather than twisting the sail to reduce the heeling lever. This has an effect on lift which is in some way similar to further flattening of the sail, if that were possible. Hence one pragmatic approach to model this behaviour is to relax the limit on $FLAT$ and regard further reductions in lift below a value of 0.6 as resulting from spilling wind rather than flattening. The disadvantage of this is that the effect on drag of spilling wind is not correctly modelled.
Many dinghies sail upwind with apparent wind angles close to the point at which lift coefficient is maximum. For angles of apparent wind from zero up to the point of maximum lift (around 34 degrees), it is likely that the mainsail sheeting angle relative to the boat for maximum lift will not change. For a single-sail dinghy sailing near to the angle of maximum lift coefficient the effect of spilling wind without adjusting the sail twist is equivalent to simply reducing the apparent wind angle on the sail as there are no sail interaction effects to consider. Thus over this range of apparent wind angles, if the sail angle is reduced by 10 degrees say, the impact on lift and drag could then be modelled by simply recalculating the sail coefficients for an apparent wind angle reduced by 10 degrees. For a sloop-rigged dinghy, a similar approach could be applied to the mainsail but not the headsails, since the headsail cannot typically be eased without affecting twist.

Table 1 shows that a reduction in the apparent wind angle from a point close to the maximum lift will lead to a small reduction in the drag coefficient between 28.0 and 12.0 degrees before a small rise is seen between 12.0 and 0.0 degrees.

In the current study therefore a further approach is examined by introducing a variable \( \text{SPILL} \) for upwind sailing only which reduces the angle of attack for which the sail coefficients are calculated. \( \text{SPILL} \) is constrained to lie between zero and the actual apparent wind angle, and is used in conjunction with \( \text{FLAT} \) and \( \text{TWIST} \). In this model the equations are thus:

\[
C'_L(t, f, s, \beta') = f \cdot C_{L_{\max}} (\beta' - s)
\]

\[
C'_D(t, f, s, \beta') = C_{D_{h}} (\beta' - s) + C_{Dp} + f^2 \cdot C_{L_{\max}}^2 (\beta' - s) \left( \frac{1 + C_{\text{min}} t^2}{\pi A R_{E}} + C_{Dn} \right)
\]

where \( s \) is the \( \text{SPILL} \) variable.

### 2.5 Parasitic Aerodynamic Drag

In addition to the viscous and induced drag of the sail plan, parasitic aerodynamic drag is relatively important for dinghies. This typically consists of the drag of the mast, rigging, topsides of the hull
and the crew. The drag area of the mast, rigging, and topsides can be estimated following an approach similar to that set out in the 2013 ORC VPP (Offshore Racing Council (2013)).

For the purposes of estimating drag in the upwind condition, the mast is divided into the “bare” part and the part inside the sail sleeve. The bare part is assumed to have a drag coefficient of 0.8 and the part to which the sail is attached has corresponding coefficient of 0.15, based on results from Hoerner (1965) for thick fairings. The centre of pressure of each part is assumed to be at its midpoint. In the downwind condition, the sail sleeve and the mast is assumed to act as part of the sail with the same drag coefficient.

The topsides of the hull can be assumed to have a frontal area equal to the freeboard multiplied by the overall beam, and a side area equal to the freeboard multiplied by the overall length. A further correction is applied to allow for the heel of the boat, based on the mean beam estimated from the waterplane area coefficient. The projected area for different apparent wind angles is estimated using a sinusoidal function varying between these values. The key equations are presented below:

\[
\begin{align*}
A_{F,\text{Hull}} &= B_{OA} \cdot FA \\
A_{S,\text{Hull}} &= L_{OA} \left( FA + 0.5B_{OA}C_{WP} \cdot \sin \phi \right) \\
A_{\text{Hull}}(\beta) &= A_{F,\text{Hull}} + \left( A_{S,\text{Hull}} - A_{F,\text{Hull}} \right) \cdot \sin \beta \\
Z_{CE,\text{Hull}} &= 0.66 \cdot \left( FA + 0.5B_{OA}C_{WP} \cdot \sin \phi \right)
\end{align*}
\]

(7)

Here \(A_{F,\text{Hull}}\) is the frontal area of the topsides of the hull, \(B_{OA}\) is the overall beam, \(FA\) is the average freeboard. \(A_{S,\text{Hull}}\) is the side area of the heeled topsides of the hull, \(L_{OA}\) is the overall length, \(C_{WP}\) is the waterplane coefficient, \(\phi\) is the heel angle. Finally \(\beta\) is the apparent wind angle, and \(Z_{CE,\text{Hull}}\) is the height of the centre of pressure of the aerodynamic drag on the topsides.

An issue not addressed in detail by the ORC IMS VPP is the aerodynamic drag of the crew. Detailed studies have been made of aerodynamic drag of athletes for sports such as cycling (e.g. García-López et al. (2008), Debraux et al (2011) and rowing (e.g. Buckmann & Harris (2014)); however the data
generated is specific to the body position adopted for these sports; similar studies have not been found by the author for sailing dinghies. Hence the aerodynamic drag of the crew is estimated here using data derived from wind tunnel studies for other purposes.

The surface area of a (nude) human can be estimated according to the formula of Dubois & Dubois (1916) as:

\[ A_{Du} = 0.0769W^{0.425}H^{0.725} \]

Where \( A_{Du} \) is the estimated Dubois surface area in square metres, \( W \) is the weight of the person in Newtons and \( H \) is the height in metres.

Penwarden et al. (1978) carried out measurements of frontal and sideways area and the drag coefficients of 331 people visiting a wind tunnel on an open day. The areas were related to the Dubois formula with a simple multiplier; the mean values were given as:

\[ A_{F,crew} = 0.326A_{Du} \]
\[ A_{S,crew} = 0.219A_{Du} \]

The drag coefficients measured were categorised by the clothes worn. The subjects were wearing normal clothing rather than sports equipment. Given that dinghy sailors typically wear hiking shorts plus lifejackets, it is assumed that they will be relatively aerodynamically efficient. For these purposes, in the absence of other data, the lowest values measured in the study (actually found for women wearing skirts) are adopted here; these are given as \( Cd =1.075 \) for frontal area and \( Cd = 0.954 \) for sideways area. In the present study these values are then reduced by 10% to take some notional account of the clothing type. The reduced values are used to compute drag areas (i.e. the product of drag coefficient and area) for the crew.
A shielding factor is then applied to account for the shielding of part of the body by the cockpit, or in two-person dinghies, by the other crew member. In the present study, the drag area is reduced by 20% to account for shielding from the cockpit.

3 Hydrodynamic model for sailing dinghies

3.1 Introduction

The hydrodynamic model in simple VPPs is very often based on the Delft series formulation (e.g. Gerritsma et al. (1981), Keuning et al. (1996), Keuning & Katgert (2008)). The model comprises a series of polynomial regression equations derived from tank tests of over fifty sailing yacht models with varying speed, heel and leeway angle. This model may be modified (as it is here) to take advantage of measured data where available.

The Delft series model, as implemented in many generic VPPs, may need to be modified or replaced in order to address particular types of vessels. The hulls tested in the development of the model were all round-bilge sailing yacht forms with principal parameters reflecting yacht design practice during the many years of testing. Hence where hulls have principal form parameters falling outside the range of hulls tested in the generation of the Delft data set, the results may not be reliable. Equally, hulls which exhibit fundamental differences in shape not captured by form parameters (such as hard chine forms) may not be well represented, while sailing vessels completely dissimilar in terms of hydrodynamics to displacement yachts, such as catamarans and hydrofoil vessels, require a different approach (see for example Findlay & Turnock (2008)). Finally issues arise for high speed planing vessels for which the range of Froude Numbers in the Delft series model may not be adequate.

In recent years sophisticated VPPs have utilised potential flow or RANS CFD calculations either directly, with the hydrodynamic solver integrated with the VPP code (such as Bohm (2014)), or indirectly, with a meta-model of the yacht hull hydrodynamics generated from hydrodynamic data.
calculated for a set of hull forms. The meta-model can take the form of polynomial-type equations (such as those used in the Delft series) or may adopt more sophisticated modelling techniques such as Artificial Neural Networks (see for example Mason (2010)).

A further possibility relevant here is to utilise data obtained directly from hydrodynamic testing. Day & Nixon (2014) investigated the resistance of a Laser dinghy, using a hull model measured using an optical measurement system. The hull form generated is shown in Figure 1 with waterline shown for an all up mass of 160kg, based on a nominal mass for the hull foils and rig of 80kg and an 80kg crew. The hull is broadly similar to some of the yachts tested in the Delft series, whilst the form parameters shown in Table 2 for three displacements varying from 150-170kg lie well within the Delft range.

Model tests on the hull in the upright condition with no appendages under normal trim angles (with transom just touching static waterline for each displacement) showed broadly reasonable agreement with the Delft model for residuary resistance (Keuning & Katgert (2008), (equation 1)):

\[
\frac{R_n}{\sqrt{c \cdot \rho g}} = a_0 + \left( a_1 \cdot \frac{LCB_{bp}}{L_{wl}} + a_2 \cdot C_p + a_3 \cdot \frac{\nabla^3}{A_w} \right) \cdot \frac{\sqrt{\text{c}}}{L_{wl}} + \left( a_4 \cdot \frac{B_{ps}}{L_{wl}} + a_5 \cdot \frac{L_{BP}}{L_{CF}} + a_6 \cdot \frac{B_{ps}}{T} + a_7 \cdot C_m \right) \cdot \frac{\sqrt{\text{c}}}{L_{wl}}
\]

However it can be seen from the comparison between the prediction and the measurements shown in Figure 2 for a displacement of 160kg that the equation under-predicts the upright resistance in the critical 3-5 knot speed range, typical of upwind sailing in a Laser, by as much as 8%.

The Delft equation also generally under-predicts sensitivity of the resistance to total weight. These results suggest that resistance regression formulae derived for sailing yachts should be treated with some caution if they are to be applied in VPPs for assessment of dinghy performance.
3.2 Hydrodynamic resistance

For the current purposes, therefore, the data from the model tests was used directly to predict the upright resistance of a Laser in the developed VPP by interpolation (and in some cases extrapolation) for weight and speed. However this is not the whole solution, since model tests were only conducted in the upright condition without appendages, and hence results were not available for other components of resistance.

The Delft framework considers eight components of hydrodynamic resistance: frictional and residuary resistance for the upright hull, viscous and residuary resistance for the keel in the upright condition, change in frictional and residuary resistance of the hull due to heel, change in residuary resistance of the keel due to heel, and induced drag of the hull/keel combination. Added to this in the current case is the resistance associated with the use of the rudder.

Of the seven components apart from the frictional and residuary upright hull resistance, three may be calculated from the boat geometry in conjunction with the fluid properties, speed and friction coefficient. The change in frictional resistance with heel angle is assumed to relate only to the change in wetted area; this may be estimated from the curve of wetted area against heel angle, calculated using the CAD model generated. The daggerboard wetted area is assumed to be independent of heel angle, and to change only due to lifting the board, whilst the rudder wetted area is assumed to be constant in all conditions. Hence the daggerboard and rudder viscous resistance components can be calculated from the friction coefficients (again using the ITTC 1957 friction line), the form factors, as proposed in the Delft model, and the wetted areas. The rudder is assumed here to generate no residuary resistance. The remaining components, the daggerboard residuary resistance, the deltas of hull residuary resistance and keel residuary resistance due to heel, are all calculated here according to the Delft model as presented in Keuning & Katgert (2008). The induced resistance is discussed further in section 3.4.
3.3 Hydrodynamic side force and yaw moment

The model as described above provides the information required for the VPP to satisfy equilibrium in the horizontal plane and also in heel. However, the impact of yaw can also usefully be considered to quantify the effect of rudder angle on speed.

In order to satisfy yaw equilibrium, the hydrodynamic and aerodynamic yawing moments must be calculated, and the sum set to zero by varying the rudder angle. This in turn requires that the leeway angle of the hull is found. The yaw moment from the hull is calculated here according to the approach proposed by Keuning & Verwerft (2009). In this approach the side force generated by the underwater body is calculated first for the daggerboard and rudder as a function of the leeway angle $\lambda$. Following Keuning and Verwerft, the lift component for the daggerboard is found as:

\[
L_k = \frac{dC_{L,k}}{d\alpha} c_{halt} c_{keel,\alpha_{eff,k}} \frac{1}{2} \rho V^2 \cdot A_{lat,k}
\]

Note that in this equation the original notation is used with subscript “k” to denote “keel”, but this should be taken here as referring to the daggerboard.

Here the lift slope is estimated as $\frac{dC_{L,k}}{d\alpha} = 5.7 AR_E \left[ 1 + \cos \Lambda \sqrt{\left( \frac{AR_E^2}{\cos^4 E} \right)^2 + 4} \right]$, with the effective aspect ratio of the daggerboard given as $AR_E = 2b_k / c_k$. The hull influence coefficient, which accounts for “lift carry-over” effects is given as $c_{halt} = 1 + 1.80 \left( T_e / b_k \right)$, while the heel influence coefficient is found as $c_{heel} = 1 - 0.382 \phi$ where the heel angle $\phi$ is expressed in radians.

The angle of attack over the daggerboard is equal to the leeway angle when the boat is upright, but is affected by the heel of the boat, as the underwater body becomes progressively more asymmetric as it heels. The effective angle is thus given as $\alpha_{eff,k} = \lambda - \lambda_0$ where $\lambda$ is the leeway angle and $\lambda_0$
is the zero-lift drift angle of the hull estimated as \( \lambda_0 = \left(0.405 \left( B_w / T_c \right) \phi \right)^2 \). Finally the inflow speed to the daggerboard \( V_{eff,k} \) is simply the boat speed. The rudder is treated in a similar manner:

\[
L_r = \frac{dC_{L,r}}{d\alpha} c_{\text{hull}} c_{\text{keel}} \alpha_{eff,r} \frac{1}{2} \rho V_{eff,r}^2 A_{\text{lat,r}}
\]

The key difference from the daggerboard is that the effective angle of attack on the rudder is affected both by downwash from the daggerboard and by the rudder angle; thus \( \alpha_{eff,r} = \lambda - \lambda_0 - \delta_r - \Phi \). The downwash is given as \( \Phi = a_0 \sqrt{C_{L,k} / AR_{eff,k}} \), while the rudder angle \( \delta_r \) is an independent variable in this equation. The inflow velocity to the rudder is assumed to be 90% of the boat speed: \( V_{eff,r} = 0.9 V_b \). The total lift of the daggerboard and rudder for a given leeway angle and rudder angle is thus obtained from the sum of the two components given in equations (11) and (12).

The hydrodynamic yaw moment from the daggerboard and rudder can be easily calculated from the moments generated by the respective lift components. Following Keuning & Vermeulen (2003) the centres of pressure of the daggerboard and rudder are each assumed to be located on the quarter chord line of the foils at 43% of the total draft of each of the foils (i.e. the vertical distance from the waterline to the lower extent of the foil). However there is a further component of yaw moment generated by the hull, related to the so-called Munk moment. Keuning & Vermeulen suggest that this may be calculated as:

\[
N = \frac{\pi}{2} \rho V_b^2 \lambda \int_{-L_b/2}^{L_b/2} h^2(x) C(x) dx
\]

Here \( h(x) \) is the local draught of the hull, and the coefficient
\[ C(x) = 3.33c_{ys}(x) - 3.05c_{ys}(x) + 1.39, \] where \( c_{ys} \) is the local sectional area coefficient. The resulting moment thus depends both on the displacement and the heel angle. In the present study the Munk moment was calculated from free-trim hydrostatics using equation (13) for three different displacements and five heel angles, and it was found that the moment could be accurately represented as:

\[ (14) \quad N = N_0 (1 - 0.00966\theta \text{deg} - 0.00134\theta^2 \text{deg}) \]

With the upright value \( N_0 = 0.0002164\Delta - 0.014572 \) where \( \Delta \) is the total displacement in kg. The total hydrodynamic yawing moment for a given leeway angle and rudder angle thus consists of the sum of the three components described above.

### 3.4 Induced Resistance

The standard Delft model (Keuning & Katgert (2008)) provides a model for the induced resistance of the hull-keel-rudder combination and with a defined speed and heeling force:

\[ R_i = \frac{F^2_{\lambda}}{\pi \cdot \frac{1}{2} \rho V^2 \cdot T^2} \]

\[ T_k = \left( A_1 \cdot \frac{T}{T} + A_2 \cdot \left( \frac{T}{T} \right)^2 + A_3 \cdot \frac{B_{\lambda}}{T} + A_4 \cdot TR \right) \cdot (B_0 + B_1 \cdot F_v) \]

The coefficients in this equation are tabulated for different heel angles. However this model equation is based on tests with zero rudder angle. As soon as the rudder angle is non-zero, the lift on the rudder will change, and since the effective aspect ratio of the rudder will be different to that of the whole underwater body, the total induced drag will also change. In the present study this is addressed as described below:

The induced drag of the rudder is assumed to be related to the lift coefficient via the widely used equation based on lifting line theory:
The lift coefficients of the rudder with rudder central and with rudder angle are determined from equation (12). The planform efficiency $e$ for a tapered swept foil where $AR_e = AR_e$ is determined following Nita & Scholz (2012) as

\begin{equation}
(17)
\quad e = 1/\left(1 + f \left(TR - \Delta TR \right)AR\right)
\end{equation}

With $\Delta TR = -0.357 + 0.45 \exp (0.0375 \Delta L)$ and

\begin{equation}
\quad f \left(TR\right) = 0.0524TR^4 - 0.1500TR^3 + 0.1659TR^2 - 0.0706TR + 0.0119
\end{equation}

Here the aspect ratio includes the image in the free surface. The heel of the boat can be considered to be equivalent to dihedral, thus modifying this value by a factor equal to $\cos^2 \phi$.

The approach described above is used to estimate the lift and associated induced drag of the rudder both on the centreline and with the given rudder angle, thus allowing the lift and induced drag deltas due to rudder angle to be estimated. The delta in the lift caused by the rudder angle is subtracted from the heeling force before applying equation (15) to estimate the hull and keel induced drag, and the delta in the rudder induced drag is then added to the total resistance.

In 10 knots of true wind with an 80kg / 1.83m sailor, the components calculated from the four Delft equations along with the delta from the rudder comprise around 20% of the total hydrodynamic drag when sailing upwind (with 14% resulting from induced drag); sailing downwind, the corresponding value is under 1%. Hence it can be seen that the majority of the resistance results from components either measured in the tank or those which can reasonably be assumed to be accurately calculated.
This model neglects the impact of waves, which will be significant in some sailing conditions, both through slowing the boat while sailing upwind, and through allowing opportunity for significant speed gains due to surfing when sailing downwind. This is discussed further in section 6.1.

4 Stability of a sailing dinghy

The hydrostatic stability of sailing dinghies is strongly dependent on the crew position, since the crew typically contributes more than 50% of the total weight. The approach adopted here is based on a calculation of the maximum available righting moment as a function of heel angle based on the height and weight of the crew.

The CG of both men and women standing upright is typically 55-57% of their height (Palmer (1944), Croskey (1922). In this study the more conservative figure of 55% is adopted. However the body position adopted by even the fittest athletes will be less straight than in the standing position due to the geometry of the side decks of the boat; hence the upper limit of righting moment will occur with a transverse offset of crew CG less than 55% of the crew height. In the present VPP it is assumed that the transverse location of the crew CG (relative to their feet) is located at a position which allows the optimum heel angle; however it is assumed that it can be no more than 95% of the CG height in the standing position from the centreline.

The maximum available righting (or heeling) moment is therefore based on the condition with the crew CG at 95% of height from the centreline, either to windward or leeward, and this maximum moment is used as one constraint to the optimisation.

In some dinghies, the crew may be offset transversely due to the location of the toe strap; in trapezing dinghies, the crews’ feet could be located on the deck edge or racks. In the case of a Laser dinghy the toe strap (or hiking strap) is located on the centreline of the boat, so that the soles of the feet will be approximately on the centreline when hiking.
The vertical position of the crew CG in this hiking position is likely to be the lowest value possible; this is estimated relative to the boat CG. The maximum righting moment available at a given heel angle is given as:

\[
RM_{\text{Max}} = W_{\text{hull}} GZ(\phi) + W_{\text{crew}} \left( GZ(\phi) + \delta YCG_{\text{crew}} \cos \phi - \delta ZCG_{\text{crew}} \sin \phi \right)
\]

where \( GZ(\phi) \) is the righting lever calculated with the crew mass located at the hull CG, and \( \delta YCG_{\text{crew}} \) and \( \delta ZCG_{\text{crew}} \) are the transverse and vertical distances from the hull CG to the crew CG when the crew is hiking to the maximum hiking potential.

For the VPP developed here, the VCG of the boat was first measured on a swing; the mast and boom were in position, but due to height restrictions, the daggerboard was placed on the deck at the correct longitudinal position, and the rudder blade was horizontal. Since the measurement was executed outdoors, the sail was not rigged in order to avoid unwanted effects due to wind. The total weight of the boat without the sail was found to be 79.5 kg, and the CG was found to be 12cm above the deck at the forward end of the cockpit. The GZ curve was then calculated for the three displacement conditions listed in Table 2, with the CG of the total system assumed to be at the CG of the boat. An estimate was then made of the position of the crew CG relative to this point when fully extended. The maximum righting moment calculated from this data is used as a constraint in the VPP solver as described in Section 5.

5 Solution procedure

The approach outlined in the previous sections was implemented in an Excel Spreadsheet. Based on input values of true wind speed and direction, boat speed, heel, leeway and rudder angles, the spreadsheet computed the aerodynamic drive and heeling force, the aerodynamic heeling moment and yawing moment, the maximum righting moment, and the hydrodynamic drag, side force and yawing moment.
The Excel “solver” was then used to solve the problem to maximise VMG both upwind and downwind. The design variables used for optimisation were speed, heel angle, true wind angle, leeway, rudder angle, TWIST, FLAT, and SPILL. The optimal solution was found subject to the constraints:

1) $\text{Abs (Total Resistance – Total Drive)} < 0.01N$
2) $\text{Min Right moment} < \text{Heeling Moment} < \text{Max Right Moment}$
3) $\text{Abs (aerodynamic heeling force – hydrodynamic heeling force)} < 0.01N$
4) $\text{Abs (aerodynamic yawing moment – hydrodynamic yawing moment)} < 0.01\text{Nm}$
5) $0.0 < \text{TWIST} < 1.0; \ 0.6 < \text{FLAT} < 1.0; \ 0.0 < \text{SPILL} < \beta$

Longitudinal equilibrium is satisfied explicitly via the first constraint. The second constraint ensures that the solution found for heel, which yields the optimal heel angle (in the sense of maximising VMG) is achievable within the range of righting moment which can be generated by a sailor of the given height and weight. Transverse force equilibrium and the associated yaw moment equilibrium are satisfied explicitly through the third and fourth constraints whilst vertical equilibrium is satisfied by equating weight and buoyancy. Trim equilibrium is assumed to be achieved by the movement of the crew longitudinally in the boat. The FLAT value is limited to a lower bound of 0.6 as discussed in section 2.2. The daggerboard was assumed to be fully down whilst sailing upwind and 50% down when sailing downwind. The only exception to the constraints described above are for the case in which yaw balance was neglected in which the third and fourth constraints were not imposed, and transverse equilibrium was imposed implicitly by equating the hydrodynamic heeling force to the corresponding aerodynamic force in the calculation of hydrodynamic induced drag.

The default Excel solver tool, using the Generalised Reduced Gradient (GRG) approach was found to converge rapidly to a solution for the speed, track, heel, leeway and rudder angles giving the best VMG which satisfies the equations of equilibrium within the available heeling moment. The solver
was run for both upwind and downwind VMG, allowing the assessment of performance in a given
wind speed for a given crew physique around a typical windward-leeward racecourse.

6 Results

6.1 Validation and comparison with measured data and previous VPP studies

The results of the VPP may be validated by comparing with full-scale measurements. Two data sets
are considered here. The first data set is presented by Binns et al. (2002), and was reported to have
been made by one of the co-authors. The data is presented in the form of polar plots of speed
against true wind angle for wind speeds of 9 and 12 knots. No information is given regarding the
height and weight of the sailor or sailors, the instrumentation used for measuring speed, track, wind
speed or angle measurements and its resulting uncertainty, or regarding the set-up or strategy
adopting in sailing the boat whilst gathering data. The authors do comment that the measurements
were made in conditions where some surfing downwind could be expected, which would lead to
higher speeds than would be achieved in calm water, particularly in broad reaching conditions. The
data set was extracted from the plots shown and is re-plotted here in Figure 3.

The second data set was presented by Clark (2014) who made measurements on an instrumented
Laser on an inland lake in Melbourne, Australia. The boat speed and track were determined from
GPS measurements, whilst an anemometer and wind vane mounted on the bow of the boat were
used to measure apparent wind speed and angle. Additional measurements were made of the mast
rotation (equal to sail trim angle on a Laser) and the rudder angle. True wind speed and angle was
derived from the measured boat and apparent wind data. The systematic uncertainty in
measurements was estimated as 0.5 knots for boat speed. The error in wind speed and direction was
estimated at +/-1.1 knots and up to +/- 3 degrees when sailing upwind. Corresponding data for
downwind is not given; however it can be seen that the anemometer and wind vane may be in the
wake of the sailor and mast when sailing downwind, which would lead to potential for underestimating the wind speed.

Data was gathered as the boat was sailed around a triangular course; the windward and leeward marks were set so that one leg was approximately dead downwind; the wing mark was set so that the true wind on the other two legs was at approximately 45 degrees from the bow. The majority of the data collected was for upwind or dead downwind sailing with very little reaching. Dagger board position was not recorded. Speed polars were presented for all true wind angles based on the data gathered. The raw data yielded fairly noisy speed polars, and a processed version was presented, which was smoothed with a moving average filter. Both sets were extracted from the presented plots and are shown in Figure 3. It appears that no attempt was made to discriminate between data gathered from steady-state sailing and that gathered during manoeuvres, hence it can be expected that some of the variations in speed with true wind angle may be caused by boat/sailor dynamics during manoeuvres (such as roll tacking and gybing). The wind speed presented was the average value obtained over the 11 laps, given as 12.53 knots; the lowest average windspeed was 10.68 knots, whilst the highest was 13.86 knots. The author comments that the wind was rather variable over the course due to the impact of surrounding buildings.

It can be seen from Figure 3 that there is a very substantial discrepancy between the two data sets for the cases of 12 knots and 12.5 knots respectively, with the second data set yielding values around half the value from the first set. It is hard to explain this level of discrepancy through issues related to boat or sailor performance, especially for upwind sailing in which surfing is extremely unlikely, and boat speed is not highly sensitive to wind speed. It seems possible that there may be a scaling or units error in the data processing. A further issue appears at both ends of the speed polars, where the smoothed data behaves differently from the raw data. It is further speculated that the moving average filter applied did not correctly account for the effects of the end of the data
record. For these reasons, this data set is not considered further here, and comparisons are focussed on the first data set.

In this study, the primary focus is on maximising VMG upwind and downwind. The comparison between the present VPP with the experiment data and with the VPPs of Binns (2002) and Carrico (2005) for upwind sailing in winds of 9.0 knots is shown in Figure 4. Since the earlier studies do not give details of the sailor physique a baseline figure of height 1.8288m and weight of 80kg has been assumed for these calculations using the present VPP. This is often suggested as close to the optimum weight for a Laser over a range of conditions – for example, in a well-known guide to Laser sailing, Goodison (2008) (an Olympic Gold Medal winner in the Laser) suggests 78-83kg as optimum. The crew is assumed to be wearing 5kg of clothing, with clothing CG located at the crew CG.

A Laser can be expected to achieve maximum VMG upwind in true wind angles in the region around 40-46 degrees in flat water. Agreement for the current VPP in this key range of true wind angles can be seen to be good, particularly around 45 degrees. VPP results are plotted for 9.0, 9.5 and 10.0 knots; it can be seen that the boat speed is relatively insensitive to the wind speed over the range of angles up to about 50 degrees, which implies that the accuracy of the wind speed measurement is not critical at these headings. The sailor is just starting to depower very slightly at 9.0 knots when sailing upwind, and so increases in wind speed require further de-powering to maintain heel angle, reducing the opportunity to gain speed. The data shows more sensitivity to wind speed above 50 degrees, since the sail is fully powered up at 60 degrees (i.e. FLAT =1, TWIST = 0, SPILL = 0), and hence the increased available power in the wind can be exploited. It can be seen that the VPP of Binns et al. displays the correct trends, but under-predicts boat speed around the key wind angle by about a knot. The VPP of Carrico, with a heavier sailor, but in 10.0 knots of wind substantially under-predicts the speed; furthermore the VPP does not display the correct trend with wind angle.

The agreement between the present VPP and the measured data for 12.0 knots true wind speed is extremely good, with predicted curves for 12.0, 13.0 and 14.0 knots all lying very close to the
measured data over the range from 42 – 60 degrees, and showing very little sensitivity to wind speed as shown in Figure 5. In this region the sail is starting to be depowered throughout the range of upwind angles. The VPP results from Binns again show under prediction of speed in the 40-50 degree range, whilst the results of Carrico, for 15.0 knots, again under-predict the speed.

The corresponding results downwind are shown in Figure 6 and Figure 7. The present VPP predicts broadly correct trends, but somewhat lower speeds than the measured data. In one sense this is surprising since the dead downwind case is arguably simpler than the upwind case – the boat is flat, with little induced drag and no sail depowering, while speeds, and hence resistance components, are comparable to the upwind case, and well within the range of test results used in the VPP. The VPPs of Binns et al. and Carrico produce similar or slightly lower results, especially dead downwind. It can clearly be seen that the downwind results are more sensitive to wind speed than the upwind results; hence it is possible that errors in wind speed measurement in the measured data are part of the cause of the discrepancy. It is hard to comment on this without more details of the equipment and set-up utilised. However it is unlikely that measurement errors could explain the whole discrepancy; it can be seen in Figure 7 that adding even two knots to the wind speed used in the VPP only partly closes the gap. It is also possible that the ORC sail coefficients used in the VPP do not adequately reflect the performance of the Laser sail downwind, in which sailors often trim the sail at angles well beyond ninety degrees to the centreline. This is possible on a boat with an unstayed rig like the Laser, but not on any typical yacht rig. However this is likely to be a small effect; in an experiment in which the drag coefficient was arbitrarily raised from 1.345 (the ORC value) to 1.500 at 180 degrees true wind angle, only just over 0.1 knots was added to the predicted speed. It should also be noted that the drag coefficient at 180 degrees from the ORC data is similar in magnitude to data presented for the Finn dinghy by Marchaj (1979). It therefore seems more likely that surfing behaviour and/or could crew kinetics contribute to a substantial part of this discrepancy, as commented by Binns et al. (2002).
An approximate prediction of the additional speed due to surfing could be undertaken by a simplified approach such as that proposed by Harris et al. (2001), although that would require knowledge of wave conditions during the measurement programme.

In summary, it can be seen that the VPP correctly predicts the trends in measured speed data in both upwind and downwind conditions, and predicts upwind speed very accurately.

6.2 Results for baseline crew

The overall VMG is calculated over a range of wind speeds by assuming a windward-leeward course with upwind and downwind legs of the same length. The times for each leg are calculated from the individual VMG values and added to give total lap time; the overall VMG is then simply the total lap length divided by total lap time. Results are shown in Figure 8, and corresponding heel and true wind angles are shown in Figure 9. Note that the downwind true wind angle is presented as the difference from 180 degrees.

The VPP results suggest that the optimum heel angle downwind is large negative for winds less than 9 knots, and then reduces in magnitude rapidly when the wind speed reaches around 9.5 knots. The explanation of this “mode shift” can be seen from Figure 10. Here the deltas due to frictional and residuary resistance are plotted against wind speed along with the heel angle. Note that the frictional resistance delta, which is negative, is plotted as positive for clarity. At 9 knots wind speed the penalty in residuary resistance of the hull is less than the benefit in frictional resistance due to reduced wetted area; however the penalty is increasing faster with wind speed. At 9.1 knots, it is still beneficial to have the boat heeled to windward, but by 9.15 knots the residuary resistance penalty exceeds the value of the frictional resistance penalty and a step change in heel angle results. It can be seen that the total delta due to heel varies smoothly.

The VPP allows the boat to heel to windward or to leeward. When sailing downwind in light to moderate winds the normal sailing practice is to heel the boat substantially to windward, a practice
known as “kiting”. Analysis of photographs of Lasers sailing downwind suggests that typical windward heel in light winds is around 20 degrees, and this is reflected in the heel angles seen in Figure 9. Goodison (2008) suggests kiting in light winds of 0-8 knots, but not in medium winds (8-16 knots); the VPP results are consistent with this.

The VPP predicts that the boat should be sailed flat upwind up to about 9 knots wind speed, and then at a small heel angle beyond that wind speed. The lowest true wind angle occurs at 9.5knots wind speed just as the sail is starting to be depowered. The apparent wind angle varies between around 27 degrees in 5 knots of wind up to around 33 degrees in 15 knots; all relatively close to the angle for which the sail generates maximum lift coefficient.

The percentage breakdown of the hull resistance components is shown for 5, 10 and 15 knot wind speeds in Figure 11. Here $R_{uh}$ is the upright hull resistance, $R_{ku}$ is the viscous resistance of the daggerboard, $R_{kr}$ is the residuary resistance of the daggerboard, $R_{ru}$ is the viscous resistance of the rudder, $dR_{fh}$ is the change in frictional resistance of the hull due to heel, $dR_{rhphi}$ is the change in residuary resistance of the hull due to heel, $dR_{rkphi}$ is the change in residuary resistance of the daggerboard due to heel, $R_{i}$ is the induced resistance of hull and daggerboard, and $dR_{i}$ is the change in induced resistance due to the use of the rudder. The change in frictional drag of the hull due to heel is negative, so the total sums to 100%. It can be seen that upright hull resistance is dominant downwind, and less so upwind, for which induced drag becomes increasingly important as wind speed increases.

The corresponding breakdown of aerodynamic drag is shown in Figure 12. When sailing upwind, the drag of the hull and crew increases in importance as the wind strength increases, contributing more than 60% of the total aerodynamic drag in 15 knots true wind. This is driven by the reduction in the induced drag coefficient of the sail as it is progressively depowered, while the hull and crew drag coefficients stay constant.
6.3 Yaw Balance

In order to examine the impact on the prediction of the boat performance of the inclusion of yaw balance, the runs described above were repeated without imposing yaw moment equilibrium; hence the boat was assumed to track in a straight line with the rudder central. The results in terms of boat speed are shown in Figure 13. It can be seen that including the yaw balance results in an increase in predicted upwind speed averaging around 1.0%. This may be expected; as suggested by Nomoto (1979) moderate weather helm can improve performance by differentially loading the rudder and unloading the hull/keel. Since the rudder is typically more efficient than the hull/keel combination this leads to a reduction in induced drag and increased speed. Downwind, there is very little impact, with an average drop in VMG due to the inclusion of yaw balance of less than 0.05%.

From an aero-hydrodynamic perspective, a reason often quoted for heeling to windward downwind is to move the centre of aerodynamic pressure of the sail over the hull, thus reducing yawing moment and in turn minimising the need to use the rudder to maintain track. By reducing the lift from the rudder the induced drag is also reduced. The results here show that the impact of the induced drag from the rudder is rather small as a proportion of total resistance, and that including a solution for yaw balance has very little impact on the magnitude of the predicted downwind heel angle as shown in Figure 14. Heeling the boat is clearly beneficial to downwind performance in light winds, largely by reducing wetted area; however that benefit could be achieved by heeling either way. Without the yaw balance included the VPP could predict the same VMG with either positive or negative heel angles. With yaw balance included, there is then a further very slight reduction in resistance due to the rudder effects which can only be achieved by heeling to windward, so with yaw balance included the VPP is guaranteed to converge to a windward heel solution. From a practical perspective, there are several additional reasons to heel to windward; large leeward heel angles will result in the boom end and/or mainsheet dragging in the water with the sail sheeted out at around 90 degrees (or more); whilst with the boom trimmed beyond 90 degrees to the centreline the weight of the boom will hold the sail forward when the boat is heeled to windward.
6.4 Impact of Sailor Physique

One of the primary goals of creating a VPP for a “one-design” sailing dinghy is to examine the effect of parameters which can be changed, such as crew physique, on performance. To this end, the VMGs for three sailors all of height 1.829m (6’ 0”), but with weights varying from 70-90kg are compared in Figure 15. As might be expected it can be seen that the lighter crew gains in all conditions downwind, and gains up to around 9.0 knots upwind, at which point the sail starts to become depowered. At that point the 90kg crew becomes fastest upwind.

The differences in speed are rather small, and in order to present the impact of these small speed changes in a meaningful manner, the results are also compared by calculating the difference in time taken over a windward-leeward course compared to a benchmark sailor who completes the course in one hour. In this calculation, no account is taken of time lost in manoeuvres or any tactical interactions between boats, nor the effects of waves or unsteady wind. Results showing the time deltas for eight sailors varying in height from 1.753m (5’9”) to 1.905 m (6’3”) and varying in weight from 70-90 kg are shown in Figure 16 for a range of true wind speeds from 5-15 knots.

It can be seen that Figure 16 can be treated broadly as being divided into three regions based on wind speed: the first “light wind” region from 5-8 knots in which the lighter sailors are always favoured, the “depowering” region above 12 knots where all sailors are starting to depower the sails, and taller heavier sailors are always favoured, and a “crossover” region between 8-12 knots, where the behaviour is rather complex as different sailors start to depower their rigs at different wind speeds. It is often quoted (e.g. Goodison (2008)) that the ideal crew weight for a Laser is around 80kg; interestingly there is only a small region (9.4-10.2 knots) for which 80kg is the fastest weight, and the benefit is presumably gained through retaining competitiveness over a wide range of wind speeds.
In the light wind region the effect of crew height is small, with only a very small penalty for taller crews due to increased aerodynamic drag; the penalty for additional 10 kg weight is around 40s in an hour, with a similar benefit for a reduction of 10 kg in weight. Above 8.5 knots, height starts to become important as well as weight, and above 11 knots some substantial gains (up to 60s in an hour) can be made by taller heavier sailors, with even larger losses made by smaller lighter sailors. It should be noted that the gains for heavier sailors in stronger winds result only from upwind performance; lighter sailors are quicker downwind in all conditions.

7 Conclusions

The key issues for performance prediction for sailing dinghies have been addressed, and illustrated through the development of a customised VPP for the Olympic Laser class dinghy. The hydrodynamic model utilises tank test data along with standard Delft series results to predict the resistance. The aerodynamic model uses standard sail coefficients along with a depowering scheme modified for sailing dinghies. The solution procedure accounts for the ability of sailors to sail boats at different heel angles to maximise speed whilst accounting for the available maximum righting moment weight of the crew.

Results are given in the form of predicted performance over a wind speed range from 5-15 knots which are qualitatively and quantitatively reasonable. The results for upwind sailing agree extremely well with published measured data at 9.0 and 12.0 knots, with somewhat larger discrepancies observed in downwind sailing. This may be partly explained by measurement errors and/or the boat surfing during the measurement programme. The sailing practice of “kiting” downwind in light winds is correctly identified by the VPP.

The VPP allows identification of the relative importance of different hydrodynamic and aerodynamic drag components, in particular the importance of aerodynamic drag of the hull and crew on the boat performance in upwind sailing. The impact of crew weight on performance over a windward-leeward
course is quantified over the range of different wind speeds in terms of time deltas relative to a baseline sailor. Results show that the impact of crew physique can be treated in terms of three regions based on wind speed: a light wind region, in which lighter sailors are always favoured, a depowered region, in which taller and heavier sailors are favoured, and a relatively narrow “crossover” region in which the benefits of being light or heavy change rapidly with wind speed. Changes of up to 60s in an hour’s racing are predicted with weight changes of +/- 10 kg. While the general effects are as expected – lighter sailors are benefitted in light winds, whilst heavier sailors benefit in stronger winds – the changeover is more rapid than might be anticipated, indicating that optimising crew weight for a given venue could be challenging if the expected wind speeds are in the intermediate range. The method can also be used to quantify the impact of other changes on the boat, such as the impact of hull and equipment weight and crew aerodynamic drag.

Whilst the use of a customised tool such as that described here offers some useful quantitative insights into the performance of this boat there are still many aspects of performance which are not modelled adequately. In particular, the effect of waves could usefully be introduced to improve the VPP. It would also be interesting to contrast the magnitudes of the gains or losses identified here with those which could be expected as a result of random variations in environmental conditions of wind speed and direction over the course of the race. The data generated from an approach such as this could be used in the context of a simplified race model, such as that deployed by Mason (2010) in order to reflect the impact of interactions with other boats. Finally, it would be of interest to gather more measured data, using more modern technology to allow more confident validation particularly for downwind sailing.
Nomenclature

\( A_{Du} \) Surface area of (nude) human
\( A_{F,\text{crew}} \) Frontal area of crew
\( A_{F,\text{Hull}} \) Frontal area of hull
\( A_{\text{Hull}} \) Area of hull
\( A_{\text{lat.k}} \) Lateral Area of keel
\( A_{\text{lat.r}} \) Lateral area of rudder
\( A_{\text{s.crew}} \) Side area of crew
\( A_{\text{s.Hull}} \) Side area of hull
\( A_w \) Waterplane area
\( AR_E \) Effective aspect ratio
\( b_k \) span of keel
\( B_{OA} \) Overall beam
\( B_{wl} \) Waterline beam
\( c_{\text{hall}} \) Hull influence coefficient
\( c_k \) Mean chord of keel
\( c_{\text{keel}} \) Heel influence coefficient
\( c_{ys} \) Local section area coefficient
\( C_D \) Drag coefficient
\( C^*_D \) Depowered drag coefficient
\( C_D^* \) Depowered drag coefficient
\( C_{Dp} \) Parasitic drag coefficient
\( C_{Ds} \) Separation drag coefficient
\( C_{Dv} \) Viscous drag coefficient
\( C_L \) Lift coefficient
\( C^*_L \) Depowered lift coefficient
\( C_{L,max} \) Maximum lift coefficient
\( C_{L,k} \) Lift coefficient of keel
\( C_{L,r} \) Lift coefficient of rudder
\( C_{m} \) Midships section coefficient
\( C_p \) Prismatic coefficient
\( C_{\text{twist}} \) Twist coefficient
\( C_{\text{wp}} \) Waterplane area coefficient
\( e \) Span efficiency factor
\( f \) FLAT variable
\( F_h \) Heeling force
\( FA \) Average freeboard
\( h \) local draught of section
\( H \) Height (of person)
\( L_k \) Lift from keel
\( L_{OA} \) Length overall
\( L_{wl} \) Waterline length
\( LCB_{fpp} \) LCB from forward perpendicular
\( LCF_{fpp} \) LCF from forward perpendicular
\( N \) Munk Moment
\( N_0 \) Munk moment at zero heel

\( R \) REEF variable

\( R_{rc} \) Residuary resistance of canoe body

\( S \) SPILL variable

\( s \) TWIST variable

\( T_c \) Canoe body draught

\( T_e \) Effective draught hull/keel

\( TR \) Taper ratio

\( V_b \) Boat speed

\( V_{\text{eff},k} \) Effective speed at keel

\( V_{\text{eff},r} \) Effective speed at rudder

\( W \) Weight of (nude) person

\( W_{\text{crew}} \) Weight of crew

\( W_{\text{Hull}} \) Weight of hull

\( Z_{CEb} \) Height of centre of effort of sails above boom

\( Z_{CE,\text{Hull}} \) Height of centre of effort of hull above WL

\( \alpha \) Angle of attack

\( \alpha_{\text{eff},k} \) Effective angle of attack of keel

\( \alpha_{\text{eff},r} \) Effective angle of attack of rudder

\( \beta \) Apparent wind angle

\( \beta' \) Apparent wind angle in plane of deck

\( \delta_r \) Rudder angle

\( \Delta \) Total displacement (kg)

\( \lambda \) Leeway angle

\( \lambda_0 \) Zero-lift drift angle

\( \rho \) Density

\( \Lambda \) Sweep angle

\( \phi \) Heel angle

\( \Phi \) Downwash angle

\( \nabla_c \) Volume displacement of canoe body
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### Table 1 ORC “Low Lift” mainsail coefficients

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<tr>
<th>beta</th>
<th>0</th>
<th>7</th>
<th>9</th>
<th>12</th>
<th>28</th>
<th>60</th>
<th>90</th>
<th>120</th>
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<th>180</th>
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<td>Lift</td>
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<tr>
<td>Coefficient</td>
<td>0.000</td>
<td>0.862</td>
<td>1.052</td>
<td>1.164</td>
<td>1.347</td>
<td>1.239</td>
<td>1.125</td>
<td>0.838</td>
<td>0.296</td>
<td>-0.112</td>
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<td>Viscous Drag</td>
<td>0.043</td>
<td>0.026</td>
<td>0.023</td>
<td>0.023</td>
<td>0.033</td>
<td>0.113</td>
<td>0.383</td>
<td>0.969</td>
<td>1.316</td>
<td>1.345</td>
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Table 2 Hull dimensions and form coefficients for Laser at three displacement variations

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<tr>
<th>Condition</th>
<th>$\frac{LCB_{sw}}{L_{sw}}$</th>
<th>$C_p$</th>
<th>$\frac{V^{2/3}}{A_w}$</th>
<th>$\frac{B_{sl}}{L_{sw}}$</th>
<th>$\frac{LCB_{sw}}{LCF_{sw}}$</th>
<th>$\frac{B_{sl}}{T_s}$</th>
<th>$C_m$</th>
<th>$\frac{V^{0.3}}{L_{sw}}$</th>
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<td>Level Trim 150 kg</td>
<td>0.535</td>
<td>0.546</td>
<td>0.100</td>
<td>0.291</td>
<td>0.946</td>
<td>12.262</td>
<td>0.755</td>
<td>0.141</td>
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<td>Level Trim 160 kg</td>
<td>0.532</td>
<td>0.552</td>
<td>0.103</td>
<td>0.291</td>
<td>0.941</td>
<td>11.755</td>
<td>0.757</td>
<td>0.143</td>
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<tr>
<td>Level Trim 170 kg</td>
<td>0.529</td>
<td>0.558</td>
<td>0.106</td>
<td>0.291</td>
<td>0.937</td>
<td>11.234</td>
<td>0.759</td>
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<td>Delft Series Min</td>
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<td>0.521</td>
<td>0.079</td>
<td>0.170</td>
<td>0.930</td>
<td>2.460</td>
<td>0.646</td>
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<td>Delft Series Max</td>
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<td>0.580</td>
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<td>0.366</td>
<td>1.002</td>
<td>19.380</td>
<td>0.790</td>
<td>0.230</td>
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</table>
Figure 1 Laser Body Plan 160 kg displacement
Figure 2 Tank data and Delft prediction for level trim 80kg crew
Figure 3 Measured data for Laser speed polars from Binns et al. (2002) and Clark (2014)
Figure 4 Upwind speed for 80kg crew: comparison with measured data and previous VPPs; 
wind speed = 9.0 knots
Figure 5 Upwind speed for 80kg crew: comparison with measured data and previous VPPs; wind speed = 12.0 knots.
Figure 6 Downwind speed for 80kg crew: comparison with measured data and previous VPPs; wind speed = 9.0 knots
Figure 7 Downwind speed for 80kg crew: comparison with measured data and previous VPPs; wind speed = 12.0 knots
Figure 8 Speed and VMG for 80kg crew
Figure 9 Heel and apparent wind angles for 80kg crew
**Figure 10** Heel deltas for 80kg crew
Figure 11 Hull resistance components for 80kg crew
Figure 12 Aerodynamic drag components for 80kg crew
Figure 13 Impact of yaw balance on predicted performance
Figure 14: Impact of yaw balance on heel angle
Figure 15 VMGs for different crew weights (1.829m tall)
Figure 16 Time deltas relative to an 80kg crew for different crew weights and heights