1 Stress accumulation in the Marmara Sea estimated through ground-
2 motion simulations from dynamic rupture scenarios

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17 Keypoints

- 18 • Earthquake ground motions are simulated in the Marmara Sea region based on
19 dynamic rupture scenarios.
- 20 • Ground motion prediction equations (GMPEs) allow the revision of the probabilities
21 of model parameters used in a logic tree framework.
- 22 • The revised probabilities thereby support the hypothesis of the low stress conditions
23 for this part of the North Anatolian fault.

ABSTRACT

We compare ground motions simulated from dynamic rupture scenarios, for the seismic gap along the North Anatolian Fault under the Marmara Sea (Turkey), to estimates from empirical ground motion prediction equations (GMPEs). Ground motions are simulated using a finite difference method and a 3D model of the local crustal structure. They are analyzed at more than a thousand locations in terms of horizontal peak ground velocity. Characteristics of probable earthquake scenarios are strongly dependent on the hypothesized level of accumulated stress, in terms of a normalized stress parameter T (Aochi and Ulrich, 2015). With respect to the GMPEs, it is found that simulations for many scenarios systematically overestimate the ground motions at all distances. Simulations for only some scenarios, corresponding to moderate stress accumulation, match the estimates from the GMPEs. The difference between the simulations and the GMPEs is used to quantify the relative probabilities of each scenario and, therefore, to revise the probability of the stress field. A magnitude $M_w 7+$ operating at moderate prestress field ($0.6 < T \leq 0.7$) is statistically more probable, as previously assumed in the logic tree of probabilistic assessment of rupture scenarios. This approach of revising the mechanical hypothesis by means of comparison to an empirical statistical model (e.g. a GMPE) is useful not only for practical seismic hazard assessments but also to understand crustal dynamics.

1. INTRODUCTION

The part of the North Anatolian Fault under the Marmara Sea (Turkey) is recognized as a major seismic gap, where a large earthquake of magnitude larger than 7 is expected in the coming years (Atakan et al., 2002; Erdik et al., 2004; Parsons 2004). Seismic risk mitigation plans have been developed around this gap, in particular for the megacity of Istanbul, in terms of, for example, early warning systems using dense observation networks and structural retrofitting. Regardless of the high seismic hazard/risk, the description of the potential source area remains imprecise, principally because: the faults are running under the Marmara Sea; the largest earthquakes were not recorded instrumentally as they occurred in the 18th century or earlier (e.g. Ergintav et al., 2014 and references therein); and the current seismicity rate is relatively low. Many studies have been carried out to assess potential earthquake scenarios in this area (e.g. Erdik et al., 2004; Pulido et al., 2004; Oglesby et al., 2008; Oglesby and Mai, 2012). Among them, Aochi and Ulrich (2015), hereafter referred as AU15, have discussed

statistically the occurrence probability of various earthquake scenarios, which are dynamically simulated along different non-planar fault systems for various levels of hypothesized stress accumulation and hypocentral locations. Although each model parameter is assigned a probability, this process is based on expert judgement through a logic-tree approach. It is found that some scenarios correspond to extreme conditions, such as a very fast rupture velocity (super-shear rupture), which leads to high-amplitude ground motions (e.g. Akinci et al., 2016). The purpose of this article is to quantify the ground-motion variations as a function of the hypotheses, especially with respect to stress accumulation, through comparisons with empirical ground motion prediction equations (GMPEs) (e.g. Douglas, 2003), which are simple models used extensively in engineering seismology to estimate ground motions at a site given the occurrence of an earthquake of a particular magnitude and location.

There have been several attempts to validate numerical simulations of earthquake ground motions using GMPEs (e.x. SCEC broadband platform validation exercise; Goulet et al., 2015), which had been previously derived from curve fitting to observations. Aochi and Douglas (2006) compare ground motions that were dynamically simulated from simple earthquake scenarios (double-couple sources) to GMPEs for various intensity measures: peak ground acceleration (PGA), peak ground velocity (PGV), response spectral acceleration, Arias intensity and duration. Although there were no complex propagation or site effects in the simulations, the results implied a strong dispersion of the ground motion due only to source effects. Baumann and Dalguer (2014) show more systematically the consistency of ground-motion simulations from dynamic rupture modelling with GMPEs for frequencies up to 1 Hz, in particular for intermediate distances (between 10 and 45 km). They also observed supersaturation (a large variation both in positive and negative senses) very close (less than 1 km) to the source. Although most of the studies are for planar faults, ground motion from dynamic rupture simulations based on non-planar fault systems can also be coherent in terms of different metrics such as PGV, duration and response spectral ordinates (Aochi and Yoshimi, 2016).

In the following sections, we first explain the procedure of our analysis, in which model parameters are “inverted” from the difference between the ground motion simulated for different dynamic rupture scenarios and those predicted by GMPEs. Then we introduce the simulations both in terms of the earthquake source and the 3D regional structure, such that the calculated ground motions are comparable with available observations for this region. Finally, we discuss the implications of our analysis for this area and more generally for future seismic hazard assessments.

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93 2. METHOD AND MODEL

94 In this section we present the method followed in this article and the models used to make the
95 calculations.

96 2.1 METHOD

97 Figure 1 illustrates schematically the forward modelling of earthquake scenarios and
98 ground-motion simulations in a logic-tree formulation (top) and an inversion with respect to
99 the GMPE for calibrating the model-parameter probabilities (bottom), from steps (1) to (4).
100 Each forward modelling is a deterministic process based on fracture mechanics and elasto-
101 dynamics under given conditions. Various model parameters are considered together with a
102 weighting probability based on expert judgment, as in many recent probabilistic seismic
103 hazard assessments (e.g. Douglas et al., 2014). In the forward modelling of AU15, three
104 variable model parameters are considered and for each of which three branches are given:
105 namely $3 \times 3 \times 3 = 27$ simulations are carried out, with probabilities between 0.5 % and 7.5
106 %. The model parameters are: (1) fault geometry, (2) stress accumulation level and (3)
107 hypocentral location. This study focuses only on the variation in stress accumulation level,
108 which strongly affects the simulated ground motions. Previously the three increasing levels of
109 stress accumulation were attributed decreasing probabilities, i.e. higher probability for a lower
110 stress accumulation. This assumption is reasonable in the sense that a characteristic
111 earthquake may be triggered once the regional accumulated stress is just sufficient, without
112 requiring a high and unstable stress. The assigned probabilities, however, remain uncertain.
113 We previously remarked that some simulated scenarios show severe or extreme features, such
114 as very large slip velocity and/or very fast rupture propagation (i.e. super-shear rupture), and,
115 thus, lead to extreme ground motions (AU15). Such scenarios are most commonly associated
116 to a high accumulated stress and are given a low probability. However, they appear quite
117 frequently so that, in the sum, they become statistically important. The motivation of this
118 study is to quantify the resultant ground motions so as to better constrain the probabilities of
119 different stress accumulation levels.

120 For convenience, we briefly explain the stress conditions and friction that are essential
121 in dynamic rupture simulations. AU15 introduced a stress parameter T indicating the

closeness of a given Mohr circle to Coulomb friction stick threshold in a Mohr-Coulomb diagram (Figure 2). Parameter T is a global, non-dimensional parameter that describes the externally loaded principal stresses, namely the initial level of stress loading, and the frictional parameters, and is uniform everywhere in a simulation. The condition of $T = 1$ means that the Mohr circle tangentially meets the static friction threshold τ_p :

$$\tau_p = \sigma_0 + \mu_s \cdot \sigma_n \quad (1)$$

where σ_0 is the cohesive force, μ_s the static frictional coefficient, and σ_n the applied normal stress. Following simulations of the 1999 Izmit earthquake (Aochi and Madariaga, 2003), these parameters are set as $\sigma_0 = 5$ MPa and $\mu_s = 0.3$. Mapping the regional stress tensor on the complex fault leads to spatially heterogeneous shear and normal stress acting on the fault. In the simulations, the external principal stress direction is set according to the tectonic movement (Le Pichon et al., 2003), and its absolute level varies with depth. The condition of $T = 0$ means, in contrast, that the Mohr circle tangentially meets the dynamic friction threshold τ_r :

$$\tau_r = \mu_d \cdot \sigma_n \quad (2)$$

where the dynamic frictional coefficient μ_d is set equal to 0.24, 20 % less than μ_s , which allows modeling the released fracture energy during the earthquake (e.g. McGarr, 1999) (thus, always $\tau_p > \tau_r$). T is given by:

$$T \equiv \frac{\tau_0 - \tau_r}{\tau_p - \tau_r} \text{ for an optimal fault orientation } (\Phi = 36.7^\circ; \text{ see Figure 2}). \quad (3)$$

We assume that the seismogenic zone extends down to 12 km depth and that its shallow part is less favorable to rupture propagation. As a consequence, we introduce a depth-dependent critical displacement [D_c of the slip weakening law (Figure 2c)], identical to the depth dependent D_c used by Aochi and Madariaga (2003) to simulate the 1999 Izmit earthquake. For a positive stress drop during an earthquake, T must be between 0 and 1. If a planar fault is ideally oriented with respect to the external principal stress, the condition $T = 0.5$ easily allows spontaneous rupture propagation (this corresponds to $S = 2$ of Das and Aki, 1977); however this is not the case for a non-planar fault system. Figure 3 shows the principal stresses as a function of stress parameter. Although the rupture process is sensitive to the parameter T (or S), the external principal stress does not change significantly. Note that S is only defined for a planar fault, while stress parameter T is defined in a Mohr-Coulomb diagram such that stress conditions can be calculated for faults of any orientation. It should

also be noted that S is strongly variable along the fault traces for a given T . In this study, we vary T when discussing in detail the probability distribution.

The purpose of this study is to constrain the probable stress levels by analyzing statistically the calculated ground motions of various scenarios by comparing them to estimates from GMPEs (final step of Figure 1). GMPEs are generally obtained by regression analysis on intensity measures, such as PGA and PGV, computed from observed strong-motion data. GMPEs are usually simple functions of earthquake magnitude, faulting mechanism, source-to-site distance and local site conditions. The equations provide a median value as well as its associated standard deviation. Therefore, the deviation of the simulated ground motions with respect to the GMPEs indicates a likelihood of each case, and the degree of this deviation can be used to update the probabilities of model parameters of interest among the bins.

Scherbaum et al. (2009) and Delavaud et al. (2012) propose and demonstrate the model selection of GMPEs using an information-theoretic approach. For every sampling point ($x_i (i=1, \dots, N)$), function $g(x)$ evaluates the likelihood of observing x (ground-motion estimate) for a given reference model (GMPE, here). Negative average sample log-likelihood (LLH) is, therefore, defined as

$$LLH(g) = -\frac{1}{N} \sum_{i=1}^N \log_2(g(x_i)), \quad (4)$$

which is a good estimate of the relative distance between a model and a given reference. A small LLH means a close match between the model and the observation. Then, for residuals from different models $g_k(x), k=1, \dots, K$, the likely weight of each model p_j is given as

$$p_j = \frac{2^{-LLH(g_j)}}{\sum_{k=1}^K 2^{-LLH(g_k)}} \quad (5)$$

This criterion provides a simple expression to rank the models statistically. Hence, this can be regarded as a probabilistic inversion process. Equation (5) provides a relative probability among all the bins, which is used in logic tree (Figure 1). The bins may be biased for some reasons but the probability provided by Equation (5) is valid in the framework of a logic tree.

In this study, we calculate the ground motions in the 3D structure using a finite difference method (Aochi and Madariaga, 2003; Aochi et al., 2013) according to different finite source scenarios dynamically simulated. For the purpose mentioned above, we adopt PGV as the primary intensity measure as we find that our tests on moderate earthquakes (M of about 5) show a consistency among the simulation, the observations and the GMPEs (section

2.3) and also because PGV is sensible at lower frequencies (around 1 Hz) which we calculate than PGA. Below we also demonstrate that other metrics lead to similar findings.

2.2 MODELS

Various earthquake scenarios along the North Anatolian Fault under the Marmara Sea were dynamically simulated using the 3D boundary integral equation method (AU15). Each of the 27 simulated scenarios has a probability between 0.5 and 7.5 % and results in earthquakes with moment magnitudes (M_w) between 5.49 and 7.56. Each scenario is given a weight corresponding to the selected model parameters for fault geometry, stress accumulation level and hypocentral location in a logic-tree formulation as explained in the previous section. The assigned probabilities remain, however, qualitative and uncertain, in particular, for the stress accumulation level, which significantly controls the consequent ground motions. Figure 4 presents three examples of dynamic rupture simulations based on three different stress levels ($T = 0.66, 0.75$ and 0.97) along the same fault geometry and assuming the same hypocenter (AU15). After forcing rupture on an initial crack in the same way, the subsequent dynamic rupture propagation is controlled by energy balance due to the static and dynamic stress field and a frictional law. The external principal stress determined by parameter T is assumed homogeneous along the tectonic rotational movement of the Marmara block, but the applied normal/shear stress field along the fault trace is heterogeneous with respect to the strike direction. Irregularity in fault geometry perturbs the stress field. If the assumed accumulated stress (T) is high enough, the rupture propagation overcomes the stress heterogeneity to become a large earthquake. This tendency is what we generally observe in similar numerical simulations of dynamic rupture process along non-planar faults such as the 1999 Izmit earthquake nearby, for example (Harris et al., 2002; Aochi and Madariaga, 2003). As a result, the ruptured area, the amount of slip and the magnitude of an earthquake, hence, become larger (M_w 7.04, 7.27 and 7.46) as T increases (Figure 4) and these changes should influence the ground motions (AU15).

The ground-motion simulations are carried out in a 3D structural model using a finite difference method, as in AU15. The finite difference is based on approximations that are fourth order in space and second order in time for a staggered grid scheme (Aochi and Madariaga, 2003; Aochi et al., 2013, and references therein). In the model domain of 200 km (EW) by 120 km (NS) by 40 km (UD), the 3D structural model combines a 3D tomographic model (Bayrakci et al., 2013), bathymetry from the General Bathymetric Chart of the Ocean

and a 1D layered model (Karabulut, personal communication; See Figure 5). The 3D model describes the basin structure of the Marmara Sea but it assumes a flat surface. The sea layer is given by $V_p = 1.5$ km/s, $V_s = 0$ km/s and $\rho = 1000$ kg/m³. The 3D model of Bayrakci et al. (2013) gives only the structure of V_p , so we define V_s and the material density ρ simply by the following equations: $V_s = V_p / \sqrt{3}$ and $\rho = 1000 \times (-0.045 V_s^2 + 0.432 V_s + 1.711)$, where V_s is in km/s and ρ is in kg/m³ (Ludwig et al., 1970; Horikawa et al., 2009). Figure 5 shows a 1D profile extracted from the constructed 3D model. The basin structure is pronounced down to about 12 km. The minimum velocity ($V_{\min}$) included is about 0.8 km/s (V_s beneath the sea floor). We set the grid size of the finite difference scheme as $\Delta s = 160$ m. The maximum frequency $f_{\max}$ that is reliable numerically in the fourth order approximation is estimated as $f_{\max} = V_{\min} / (5 \cdot \Delta s) = 1.0$ Hz. Our simulations do not take into account any site effects beyond those accounted for directly by the simulations. However, we can assume that at the relatively low frequencies considered, site effects may have minimal impact on the ground motions. The maximum velocity included in this model is $V_{\max} = 7.94$ km/s (V_p). Therefore, a time step of the finite difference should be $\Delta t \leq 0.5 \cdot \Delta s / V_{\max} = 0.010$ s to ensure stability; and, hence, we fix $\Delta t = 0.008$ s. Each calculation is run for a duration of 120 s. The quality factor Q for anelastic attenuation is introduced as a damping term in the finite difference formulation (Graves, 1996) with central frequency about 1 Hz. There are other methods to take Q into account in visco-elastic (e.g. Day and Bradley, 2001; Kristek and Moczo, 2003) or viscoplastic (e.g. Roten et al., 2014) formulations. However, as shown in the next section, our current knowledge of this region is still limited, even in terms of velocity structure, and a detailed description of attenuation would not be useful yet.

2.3. CURRENT MODEL PERFORMANCE

We first simulate a moderate earthquake to check the reliability of the 3D model and the accuracy of the ground-motion simulations. Figure 6 shows maps of the 2011/07/25 M_L 5.2 earthquake (40.823°N, 27.743°E, 10.8 km depth) and the 2012/06/07 M_L 5.1 earthquake (40.853°N, 27.920°E, 7.1 km depth) (Karabulut, personal communication; who also provided their focal mechanisms) and available seismograph stations (Broadband stations from Kandilli Observatory of Earthquake Research Institute, Turkey). For the comparison, we calculate the ground motions using the 1D layered model with a fixed $Q = 300$ and the 3D model assuming $Q = V_s/10$ (Figure 5). Moment magnitude M_w of 4.85 and 4.9 are given to obtain the best fit to

the spectral accelerations at 20 seconds. The source time function is assumed as a spline function of durations of 2.0 s and 1.8 s, respectively. Figure 7 shows the waveforms filtered up to 1 Hz at the common stations for the two earthquakes, aligned at the origin time ($t = 0$). The arrivals of the waves are generally good except for SLVT where the observed wave arrives slightly later than the simulated one. The peak values of the waveforms (here, PGV) are mostly caused by the direct S-wave, but they are associated with the later phases at station SLVT. In our models, no 3D structure exists beneath SLVT. This indicates that the model could be further improved locally to reflect the geological context. As well as considering a single ground-motion parameter, such as PGV, we also calculate the Goodness-of-Fit (GoF) score between simulations and observations based on several metrics from each time series (Olsen and Mayhew, 2010; Aochi and Yoshimi, 2016): averaged over long-period SA (10, 20 and 50 s), short-period SA (1, 2 and 5 s) and duration defined as interval between 5 and 95% of Arias Intensity. GoF for two positive values (x, y) to compare is calculated with

$$GoF = \operatorname{erfc}\left(\frac{2|x-y|}{x+y}\right) \quad (6)$$

where erfc is the complementary error function. Figure 8 shows the scores averaged over the defined metrics for each component for the two earthquakes. We do not aim to discuss the scores of any particular station; we intend to show that the 3D model is better than the 1D-layered model in this area. In general, GoF scores larger than 0.8 and 0.6 are considered “excellent” and “good”, respectively, so that the current 3D model could be further improved. Note that a factor-of-two difference between values leads to $GoF = 0.35$, although it would be better to compare spectra not by its linear amplitude but by its logarithm. Hereafter we use the 3D model assuming $Q = Vs/10$ for ground motion simulations of large scenario earthquakes. Assumption of much stronger attenuation of $Q = Vs/20$ does not give a better result in terms of GoF, as the duration becomes very short.

We also compare the horizontal PGVs with GMPEs in Figure 9. The selected GMPEs are Bindi et al. (2014), Akkar et al. (2014a, b), Boore et al. (2014) and Cauzzi et al. (2015). We show the non-filtered values of PGV from both simulations and observations because the duration of the source time function of a smooth B-spline function is given for 1 s in the simulations. The comparisons show a good coherency between the simulations and the observations for both the moderate earthquakes. Although the used source parameter is simple (a smooth source time function at a point source) in these tests, this agreement is supportive of applying any of these GMPEs at a frequency of around 1 Hz for large scenario earthquakes for which no observations exist. For the nearby 1999 Izmit earthquake, Bouchon et al. (2002)

showed the near-field ground velocities with no filtering and used them directly for seismological analyses. The waveforms were dominated by low frequency content: strong pulses of about a few seconds are visible and are closely related to the earthquake source process (e.g. Aochi et al., 2011). In the following section, we use the GMPE of Bindi et al. (2014), which is found roughly in the middle of the considered GMPEs and the simulations and was found by Douglas and Aochi (2016) to be suitable for ground-motion simulations from moderate earthquakes in this region. Similar results would be found for any of the other three GMPEs as they also predict similar ground motions.

3. Results

Let us first explore the PGV maps simulated for an $M_w 7.27$ earthquake scenario (central hypocenter position with $T = 0.75$, shown in Figure 4B). We calculate the ground motions assuming a constant $Q = 300$ or a variable $Q = V_s/10$. Figure 10 shows the PGV maps and PGVs as a function of distance, evaluated at 2851 distributed receivers. Both the calculations tend to overestimate the ground motion levels predicted by the GMPE of Bindi et al. (2014). For comparison, the three other recent GMPEs considered above are also shown. Although some differences are found at distances shorter than 5 km, all these GMPEs show similar overall features. The simulated PGVs are high particularly in the near field compared with the predictions of GMPEs, but we find that strong attenuation ($Q = V_s/10$) shows a smaller average residual (in terms of common logarithms): 0.402 compared to 0.467. Hereafter, our discussion is based on the calculations assuming $Q = V_s/10$. Ground motions at very short distances of a few numerical grids of FDM should not be taken into account because each fault element of 500 m size within the BIEM simulation is represented as point source in the ground-motion simulations, namely seismic moment release on a finite sub-element of finite surface is concentrated at a point. The residuals are calculated for distances larger than 1 km. For further distances, the receiver coverage is no longer azimuthally uniform as our physical model dimension is $200 \text{ km} \times 120 \text{ km}$. Thus we use distances up to 60 km, which is roughly the distance from the fault to the outer model boundary. We recall that the purpose of this study is not to adjust the model parameters to fit the GMPEs but to assess the probabilities of the model parameters using the relative discrepancy between the simulations and the GMPEs.

We keep the same fault geometry as in Figure 4 [Model LP, based on the fault trace mapping of Le Pichon et al. (2003)] and the three hypocentral locations (West, Center and

East, approximatively at 28.2°E, 28.5°E and 28.8°E, respectively). Since only six simulations, featuring three different stress levels, are available for $M_w \sim 7$ events from AU15 for the selected fault geometry, we carry out supplementary simulations for various stress levels. Figure 11 shows the simulated magnitudes of earthquakes with respect to the stress parameter T . It is found that the simulated magnitudes do not always depend linearly on T . Each increase in magnitude corresponds to the activation of a farther segment after a geometrical irregularity. It is also confirmed that the position of the hypocenter changes the possible progress of rupture propagation even under the same stress conditions, as inferred in previous studies (e.g. Oglesby et al., 2008). Finally, the magnitude converges when the stress is extremely high ($T \geq 0.8$), as the ruptured area becomes identical in such cases. In the simulations, as already pointed out in AU15, the earthquakes can be divided into two groups: those that have succeeded in progressing to a large event of magnitude 7 or larger; and those that arrest soon, thereby leading to a magnitude of about 6 or less. Here we are interested in the former group of larger events.

The results of 13 simulations are summarized in Table 1 and Figure 12 (see also Supporting Information, Figure S1), and also plotted as a function of the stress parameter T in Figure 13. The average residual is small for small T , and it increases with T wherever the hypocenter. The simulations overestimate the ground motions for high T . This is mechanically understandable because a high T facilitates the rupture propagation. In Table 1, we also change the distances used for the residuals to 20 – 60 km, as it was thought that the ground motions in the near field (< 10 km) and at the regional scale (a few tenths kilometers) could show different tendencies. The residuals and bias become smaller, i.e. the ground motions are closer to the reference GMPE. This is expected, as the used fault models do not have any smaller scale heterogeneities. In fact, a smooth rupture model is likely to exaggerate the rupture directivity and tends to generate extreme ground motions coherently. On the other hand, when small-scale inhomogeneities are considered on a fault, high slip rate may still exist but do not contribute to the ground motions coherently, avoiding this extreme ground-motions problem. In addition, the fact that the receivers near the source are all located on the sedimentary ocean bottom, while the receivers at distance are on land where the rock from the assumed 1D structure ($V_s = 1780$ m/s) is harder, although all are regarded as hard rock sites in the GMPEs, may explain the smaller residual in the far field. However, we still obtain similar results for the revised probability p . This confirms that the formulation based on Equations (4) and (5) reattributes the probabilities among the bins appropriately. We recall the hypothesis given in AU15, assigning three levels of the stress parameter T (0.66, 0.75 and 0.97), with

associated probabilities of 50 % ($T=0.66$), 35 % ($T=0.75$) and 15 % ($T=0.97$), independently of the other model parameters. To evaluate the revised probabilities, we simply summarize them for three bands: $0.6 < T \leq 0.7$, $0.7 < T \leq 0.8$ and $T > 0.8$, which are shown as a gray surface in Figure 13 (c). Indeed this revision is consistent with AU15's hypothesis. The probability of low T is slightly higher (55.0%) than its estimate in AU15, and consequently extremely high T is less probable (6.2%).

We also compare the SAs at two different periods (1 and 2s) at the available KOERI station locations (but where there are no data) in Figure 14. Bindi et al. (2014) provide the coefficients for the prediction of SAs up to 3 s. Results for three different values of T are compared. The tendency that the residuals are smaller for small T is the same as we observe in the comparison of PGV, so that we can quantify them in the same way. The choice of the PGV as a metric is sufficient to quantify the impact of stress parameter T on the ground motions and to adjust its probability in the logic tree. Nevertheless, the models might not be the best with respect to the GMPE. Some stations with large residuals are strongly affected by the given 3D structure through which the seismic waves propagate. As discussed in the previous chapter for the moderate earthquakes, it would be necessary to improving further the 3D structure and/or take into account a more detailed local structure. The simulations might be biased due to any model parameters and assumption explicitly or implicitly existing in the given logic tree. We discuss this further in the following section.

This revision not only validates the framework of probabilistic seismic hazard assessment previously carried out, but also infers the possible crustal strengths. The fault system might be ruptured by low T without waiting for the extremely high accumulation of stress. According to our results, the stress level at which could operate a reasonable Mw7+ earthquake is likely (with a probability of more than 50%) to be in the range of T between 0.6 and 0.7, as previously indicated in Figures 3 and 4. This roughly corresponds to S between 0.67 and 0.43 on an ideally-oriented fault (36.65° inclined from the σ_1 axis). This insight needs to be scrutinized from different points of view of current tectonic movement and (a) seismic activity along the North Anatolian fault.

4. Discussion

We have revised the hypothesis on the stress level based on the expected ground motions with respect to GMPEs. Although the different stress conditions are clear in terms of parameter T from the mechanical point of view, it would still be a challenge to estimate the

probability of a given state of regional stress from observations. Thus, we have briefly carried out a statistical analysis on T with a rough resolution width of 0.1. However, the simulations show that the results are sensitive to a small increase of T . Furthermore, we find that the values of T and the hypocenter locations may not be independent. The simulations starting from the central or eastern hypocenters are presented by low T ($0.6 < T \leq 0.7$), while western hypocenters are common for high T ($0.7 < T \leq 0.8$). In other words, within a seismic cycle, a large event will start most probably from the central or eastern parts. However, if the recurrence time was longer (higher T) due to reasons ignored in this study, a large event nucleating from the western hypocenter would become more likely. This is the feature also inferred from AU15 in the given probabilistic framework, but the current study confirms it statistically. This finding is important for further seismic hazard studies in this region and should be carefully considered in future studies (Spagnuolo et al., 2016).

In the formulation of Equations (4) and (5) (Scherbaum et al., 2009), the probability is revised relatively among the available bins as a function of LLH. Even if none of the bins is suitable (= a zero residual to a given reference), the probability is assigned accordingly such that the bins of smaller LLH are considered more probable and the summation of the revised probabilities of all bins is equal to unity. Therefore, the probability shown in Figure 13 can be interpreted by the tendency of the ground motions to be stronger for larger T . The dynamic rupture scenarios and 3D geological structure used in this study might not yet be close enough to reality. On the other hand, the model settings for the rupture scenarios may be biased somehow from the fact that they are positioned as part of a logic tree, and there may be other factors that are not explicitly modeled. For example, earthquake source process could be more complex than the simulations presented here due to small-scale inhomogeneity (e.g. Mikumo and Miyatake, 1978; Day, 1982; Aochi et al., 2003; Ripperger et al., 2008; Schmedes et al., 2010; Shi and Day, 2013; Mai and Thingbaijan, 2014 and many other studies). Such aspects are important for reproducing and generating ground motions over a large band of frequencies required for engineering applications (e.g. Mai et al., 2010; Graves and Pitarka, 2010; Song et al., 2013; Goulet et al., 2015). Akinci et al. (2016) also propose a hybrid ground motion simulation method combining non-planar dynamic rupture simulations (AU15), kinematic fractal sum of asperities (Ruiz et al., 2011) and stochastic Green's functions based on a finite source (Boore, 2009). The relatively smooth slip models might have led to large ground motions in all cases, as the calculated residuals (and consequently σ) are quite large in this study, because of ignored factors such as fault heterogeneity (see above) or off-plane damaging (e.g. Andrews, 2005; Roten et al., 2014). Yet, our discussion is still valid. Although

the presented simulations are still limited (with only a single variable T), this is the simplest way to evaluate the probability of the given model parameters by fixing all the other parameters. The process adopted in this study can be useful when scrutinizing dynamically-simulated earthquake scenarios and to assign them a priority to communicate to engineers which scenarios are the most probable.

As a simple example of model bias, let us carry out ground-motion simulations assuming $Q = V_s/20$, although this was not better in our tests for the two moderate earthquakes than assuming a constant Q or $Q = V_s/10$. Under such a strong attenuation condition, the wave propagation is significantly changed and the simulated PGVs get closer to the GMPE, i.e. smaller residuals, for the same earthquake scenarios (Figure 15). This changes the values of LLH, and the probabilities are revised accordingly. Nevertheless, the revised probabilities are relative among the bins and the tendency of the role of stress parameter T on the ground motions is similar. This leads to the same conclusion that lower levels of T are preferred and an extreme level of high T is less probable, supporting the hypothesis taken in AU15.

5. Summary

We have carried out ground-motion simulations in the Marmara Sea (Turkey) region using a 3D finite difference method taking into account the 3D geological structure of this region. First, two moderate earthquakes of about magnitude 5 have been simulated and the goodness-of-fit of the simulated ground motion parameters to the observations have been evaluated. The 3D structure assuming a quality factor $Q = V_s/10$ lead to a better match among our tests.

Second, we have attempted to constrain the regional stress levels that allow a future large earthquake of magnitude of about 7 or larger, focusing on the stress parameter T . Several hypotheses for this mechanical parameter and their associated likelihoods were introduced by a logic-tree approach in Aochi and Ulrich (2015) to estimate the likelihood of the earthquake scenarios. We have proposed a strategy for re-evaluating these hypotheses by making use of published ground motion prediction equations (GMPEs) for engineering strong-motion parameters. The simulations being valid up to frequencies of about 1 Hz, we were able to compare the simulated horizontal peak ground velocity (PGV) with the PGVs predicted by various GMPEs. It was shown that high stress conditions (high T) leads to large earthquakes as well as high resulting ground motions. By quantifying the overall difference between

simulated PGV and estimates from GMPEs, we were able to estimate the probability of each scenario. Namely a high absolute residual means a less probable scenario. Finally, we are able to revise the probability of the stress field in terms of T . A moderate T ($0.6 < T \leq 0.7$) has a probability of more than 50 % and an extremely high T (>0.8) is unlikely (probability less than 10%). These results are coherent with our previous hypotheses based on expert judgment. This constraint from comparisons with GMPEs is important not only for further quantitative seismic hazard assessments and for investigating the likelihood of probable and extremes of dynamic rupture scenarios for ground-motion estimations but also to understand dynamic rupture processes along non-planar fault systems and the crustal strength in geodynamic processes. The same model parameterization could be used for other earthquake scenario of analogous fault geometric complexity and the fault maturity as this part of the North Anatolian fault.

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Table and Figure captions

Table 1: Results from the 13 simulations characterized by a moment magnitude greater than 6.8. The regressions (mean residual μ and variance σ) with respect to GMPE of Bindi et al. (2014) are calculated for distances between 1 and 60 km, and between 20 and 60 km, respectively. The former is also shown in Figure 12. Negative average sample log-likelihood (LLH) and the revised probability p are calculated from Equations (4) and (5), respectively. The model is represented by different T and hypocenters (H1, H2 and H3 correspond to longitude 28.5°E (center), 28.2°E (east) and 28.8°E (west).

Model	Regression (1-60 km): See also Figures 12 and 13				Regression (20-60 km)			
	μ	σ	LLH	p	μ	μ	LLH	p
T=0.64 H1	0.568	0.904	2.148	0.161	0.492	0.880	2.059	0.154
T=0.66 H1	0.846	1.062	2.655	0.113	0.762	1.044	2.530	0.111
T=0.68 H1	1.170	1.154	3.273	0.074	1.092	1.137	3.117	0.074
T=0.68 H2	1.211	1.134	3.312	0.072	1.114	1.036	2.994	0.081
T=0.70 H1	1.206	1.037	3.151	0.080	1.136	1.035	3.029	0.079
T=0.70 H2	1.485	1.199	3.846	0.050	1.335	1.098	3.480	0.058
T=0.75 H1	1.533	0.911	3.618	0.058	1.451	0.918	3.451	0.059
T=0.75 H2	1.795	1.185	4.665	0.028	1.688	1.093	4.243	0.034
T=0.78 H3	0.166	0.784	1.789	0.207	0.089	0.742	1.729	0.194
T=0.80 H3	0.805	1.251	2.921	0.094	0.805	1.216	2.860	0.088
T=0.97 H1	1.945	0.892	4.627	0.029	1.873	0.854	4.381	0.031
T=0.97 H2	2.322	1.216	6.281	0.009	2.209	1.147	5.79-	0.012
T=0.97 H3	1.815	1.292	4.906	0.024	1.723	1.266	4.623	0.026

Figure 1: Schematic illustration of forward modeling of earthquake scenarios and inversion process to calibrate the model parameters initially given. Top panel shows simulation steps in a logic tree with three branch levels (parameters 1, 2 and 3). Each set of choices of model parameters has a probability $P(a_1)P(a_2)P(a_3)$, such that the simulation results can be discussed statistically as demonstrated in AU15. Bottom: (1) Each earthquake scenario leads to a ground motion simulation. (2) The ground motion of different scenarios (different color circles) can be compared with GMPE (red curve as mean with a log-normal distribution). (3) Position of simulated ground motions within a log-normal distribution of GMPE is calculated for each scenario. (4) This derivative may infer the likelihood of each scenario so as to revise the probabilities of model parameters of interest.

Figure 2: Model parameters used in AU15. (a) A Mohr-Coulomb diagram for the case of $T = 0.66$ and 7.25 km depth. Stress parameter T constrains the position of Mohr circle, defined by principal stresses σ_1, σ_2 and σ_3 , between static and dynamic friction lines defined by σ_0 , μ_s and μ_d . The optimal direction of σ_1 is set to 36.7° from the tectonic rotation of Marmara block. (b) Maximum and minimum principal stress (σ_1 and σ_3) ranges for $T = (0.6, 0.7)$ as a function of depth (the curves for the two values of T overlap, but their variations are small). $\Delta\sigma = \sigma_1 - \sigma_3$ is also shown. Initial normal and shear stress on each portion of the fault system is given in a function of $\Delta\sigma$. (c) Assumed variation of D_c with depth of a linear slip-weakening friction. In the shallow crust and below 12 km depth, a relatively stable frictional regime is assumed. More details are given in AU15.

Figure 3: (a) Variation of σ_1 , σ_3 and $\Delta\sigma$ as a function of stress parameter T . (b) Relation between parameter S of Das and Aki (1977) and stress parameter T . S here is calculated for the optimal fault orientation with respect to the external principal stresses. In the simulations, S varies along the fault strike in each simulation. The vertical dotted lines correspond to the three different levels of T studied in AU15 ($T = 0.66, 0.75$ and 0.97).

Figure 4: Snapshot of three representative dynamic rupture simulations along the North Anatolian fault in the Marmara Sea (redrawn from AU15). Fault geometry and hypocenter locations are similar, only the stress conditions are different: (A) sufficient ($T = 0.66$), (B) high ($T = 0.75$) and (C) extremely high ($T = 0.97$), controlled by one single parameter T . The bottom panels show the final slip distribution. The resultant magnitudes M_w are $7.04, 7.27$ and 7.46 , respectively.

Figure 5: P- and S-wave velocity structures used in the simulations. Black lines represent the 1D layered base model (Karabulut, pers. comm., 2012). Red lines show a profile extracted from the constructed 3D model based on the 3D tomography results of Bayrakci et al. (2013) in the middle of the Marmara sea, at the location of 2012/06/07 earthquake (see Figure 6).

Figure 6: Maps of two moderate earthquakes and the available seismic stations from the broadband network of the Kandilli Observatory of Earthquake Research Institute. (A) M_L 5.2 2011/07/25, and (B) M_L 5.1 2011/06/07 earthquakes.

Figure 7: Comparison between simulated ground motions and observations at five common stations for (A) 2011/07/25 and (B) 2012/06/07 earthquakes. All the waveforms are filtered between 0.01 and 1 Hz. Two synthetics correspond to the simulations in a 3D structure with $Q = V_s/10$ (black) and a 1D layered model with fixed $Q = 300$, respectively.

Figure 8: GoF scores between simulations and observations for (A) 2011/07/25 and (B) 2012/06/07 earthquakes (See also Figures 6 and 7). The scores are based on SA at various short and long periods and on duration metrics. We tested 1D structure and 3D structure assuming $Q = V_s/10$. The scores are calculated for each component at each station. The average over all the components and stations are shown by bold horizontal lines (3D: black and 1D: blue).

Figure 9: Comparison of the horizontal geometric-mean Peak Ground Velocities (PGVs) for: (A) the 2011/07/25 earthquake, and (B) the 2012/06/07 earthquake. The grey points represent the simulations (3D structure with $Q = V_s/10$) at the 2851 receivers distributed on the ground surface (about every 3 km). The red points show particularly the simulations at the receiver positions corresponding to the KOERI network, and the crosses are the observations available from the KOERI network for each earthquake. No filter is applied. Note that a duration of the source time function of 1 s is given in the simulations. Four GMPEs are compared, as listed in the legend. The standard deviation of Bindi et al. (2014)'s GMPE is shown by broken lines.

Figure 10: Comparison of the horizontal PGV map from the M_w 7.27 earthquake scenario shown in Figure 4(B). The ground motions are calculated assuming: (a) $Q = 300$ (constant) or (b) $Q = V_s/10$. Small triangles show the grid of receivers composed of 2851 points. The hypocenter position is shown by a cross, and the ruptured fault portion by a bold white line. On the right, the simulated PGVs are compared with those predicted by the empirical GMPEs

of Bindi et al. (2014), Cauzzi et al. (2015), Akkar et al. (2014) and Boore et al. (2014). The curve of Bindi et al. (2014) is overlapping almost perfectly that of Boore et al. (2014).

Figure 11: Simulated earthquake magnitudes as a function of the stress parameter T . We test the same three hypocentral positions as AU15. Previously only the three levels ($T = 0.66, 0.75$ and 0.97 , indicated as dotted lines) were simulated by AU15.

Figure 12: Comparison of the selected three scenarios (shown in Figure 4) of simulated ground motions in terms of PGV with the prediction from the GMPE by Bindi et al. (2014) (red line). The simulated values are illustrated as points, among which the gray represents the receivers of $V_S = 1780$ m/s (1D structure), located on land, far from the source area. The dashed and dash-dotted lines show the median PGV plus or minus one and two standard deviations of the GMPE. The calculated mean normalized residual (μ), normalized standard deviation (σ), LLH value and the revised weight (p) are shown in each panel and summarized in Table 1. The blue lines are regressions for an equation : $PGV = a + b \ln(\sqrt{r^2 + h^2})$, where a , b and h are constants and r is source-receiver distance. This logarithm relation is typically used in GMPE for modeling the decay of ground motion with distance. Thus, the blue line allows comparing the distance decay of the simulated data with the plotted GMPE. All the comparisons of 13 scenarios are shown in the Supporting Information (Figure S1).

Figure 13: (a) Mean normalized residual between the simulated PGVs and the prediction from the GMPE (Bindi et al., 2014) for each scenario as function of different hypocenter positions and stress parameter T . (b) The calculated normalized σ from Figure 11. Vertical lines show the three levels of T used in AU15. (c) The revised probability of each scenario by lines and the averaged probability for three levels by gray shadow. For reference, a black line represents the initial probability assumed in the logic tree of AU15.

Figure 14: A: Ruptured fault position and PGV map for a scenario with $T = 0.66$ and central hypocenter position (cross mark). Receiver positions used for the calculation of SA are shown by triangles. B: Residuals for SA (1 s) between the simulations and the GMPE of Bindi et al. (2014) are shown for the three scenarios of $T = 0.66$ (panel A), 0.75 and 0.97 featuring the same hypocenter location. The horizontal axis represent a distance between the rupture fault and receiver. C: Residuals for SA (2 s). Also shown on the right-hand side are histograms of the residuals for the different values of T .

Figure 15: A: Mean normalized residual between the simulated PGVs and the prediction from the GMPE (Bindi et al., 2014). The residual is defined as $\varepsilon = \log_{10}(y_{GMPE}) - \log_{10}(y_{simulation})$

for ground-motion parameter y . The simulations are carried out assuming $Q = V_s/20$. Although this assumption give worse GoF than the assumption $Q=V_s/10$ when considering the two moderate earthquakes of Figure 6, the normalized residual are lower. B: The revised probability of each scenario is shown by the red, blue and green lines. The averaged probability for three stress levels is displayed as a gray shadow. For reference, the orange line shows the probability obtained in Figure 13 for the case of $Q = V_s/10$. Despite the bias introduce by the assumption $Q=V_s/20$, the obtained probabilities are relatively similar.

Figure 1.

Figure 2.

Figure 3.

Figure 4.

Slip Velocity

(A) Stress = sufficient

(B) Stress = high

(C) Stress = extremely high

t = 2 s

t = 2 s

Z (km) t = 2 s

t = 7 s

t = 7 s

t = 7 s

t = 12 s

t = 12 s

t = 12 s

Slip Velocity m/s

t = 17 s

Final Slip

Figure 5.

Figure 6.

Figure 7.

Figure 8.

Figure 9.

Figure 10.

(A) $Q = 300$ (const.)

(B) $Q = V_s/10$

Figure 11.

Figure 12.

Figure 13.

Figure 14.

Figure 15.