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Dielectronic recombination data for dynamic finite-density plasmas

XIV. The aluminum isoelectronic sequence

Sh. A. Abdel-Naby1, D. Nikolić1,*, T. W. Gorczyca1, K. T. Korista1, and N. R. Badnell2

1 Department of Physics, Western Michigan University, Kalamazoo, MI 49008, USA
2 Department of Physics, University of Strathclyde, Glasgow G4 0NG, UK
e-mail: garczyca@wmich.edu

Received 22 June 2011 / Accepted 7 October 2011

ABSTRACT

Context. A comprehensive study of dielectronic recombination (DR) for the aluminum-like isoelectronic sequence has been completed.

Aims. Total and final-state resolved DR rate coefficients for the ground and metastable initial levels of 17 ions between Si VII and Zn XIX are presented.

Methods. Within an isolated-resonance, distorted-wave (IPIRDW) approximation, multiconfiguration Breit-Pauli (MCBP) calculations are carried out for the total and partial DR rate coefficients of Al-like ions. Both $\Delta n_e = 0$ and $\Delta n_e = 1$ core-excitations are included, using LS-coupled and intermediate-coupling (IC) schemes.

Results. The inaccuracies of earlier empirical data and/or LS-coupling calculations, particularly at lower temperatures characteristic of photoionized plasmas, is demonstrated by comparison with present, state-of-the-art IC DR rate coefficients. Fine-structure effects are found to increase the DR rate coefficient at low temperatures and decrease it at high temperatures, rendering earlier LS calculations incomplete. Good agreement is found between present IC results and experimental measurements.

Key words. plasmas – atomic processes – scattering – atomic data

1. Introduction

Cosmic gases are ionized primarily via two mechanisms: collisional ionization and photoionization. The former process dominates within, for example, stars, supernova remnants, and interstellar and intergalactic media, while the latter is predominant in H II regions, planetary nebulae, and active galactic nuclei. In collisionally ionized gas the ionization is primarily due to electron impact ionization, hence the ions are formed at temperatures $kT$ corresponding to roughly half of their ionization potential (e.g., see Bryans et al. 2006). By contrast, in photoionized plasmas the ions are formed at substantially lower temperatures $kT$ than the characteristic energies of the ionizing photons (Feerland et al. 1998; Kallman & Bautista 2001). Thus ionization balance is achieved over very different ranges in temperature in collisionally ionized and photoionized gases.

DR is the dominant electron-ion recombination process for most of the ions found in low density photoionized plasmas and low- to medium-density electron collisionally ionized plasmas (Arnaud & Raymond 1992; Arnaud & Rothenflug 1985; Kallman et al. 1996). Computer codes developed for modeling photoionized plasmas include CLOUDY (Feerland et al. 1998) and XSTAR (Kallman & Bautista 2001). For electron collisionally ionized plasmas the CHIANTI code (Landi et al. 2006), for instance, is used to model spectral emission while ADAS (Summers 2003) is used to carry-out spectral diagnostics, mainly for magnetic fusion plasmas. These modeling codes require accurate DR rate coefficients for calculating reliable ionization balance, thermal structure, and line emissions of cosmic plasmas. As an example, recent predictions of the collisional ionization equilibrium abundances of iron ions (Dere et al. 2009), using new DR rate coefficients computed by Badnell (2006b), found large differences from ionic fractions determined using the previously recommended DR data (Mazzotta et al. 1998), emphasizing the importance of using state-of-the-art results versus older, unreliable data.

In order to produce an up-to-date, reliable set of DR data for all ions relevant to the modeling of astrophysical and laboratory plasmas, Badnell et al. (2003) initiated a program to calculate accurate total and partial DR rate coefficients from both ground and metastable initial states of all ionization stages of all ions up through Zn. Partial final-state resolved rate coefficients are necessary for collisional–radiative modeling at densities found in magnetic fusion plasmas and some astrophysical sources such as the broad line region (BLR) of AGNs. Data for metastable initial states are necessary to model plasmas whose characteristic time-evolution is comparable with the lifetime of the metastables, i.e., the metastables are not in quasi-static equilibrium with the ground level. State-of-the-art MCBP calculations have been performed and data assembled for the hydrogenic (Badnell 2006a), helium-like (Bautista & Badnell 2007), lithium-like (Colgan et al. 2004), beryllium-like (Colgan et al. 2003), boron-like (Altun et al. 2004), carbon-like (Zatsarinny et al. 2004b), nitrogen-like (Mitnik & Badnell 2004), oxygen-like (Zatsarinny et al. 2003), fluorine-like (Zatsarinny et al. 2006), neon-like (Zatsarinny et al. 2004a), sodium-like

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* Present address: National Institute for Nanotechnology, Edmonton, Alberta.
Table 1. Available data for the aluminum-like isoelectronic sequence.

<table>
<thead>
<tr>
<th>Ion</th>
<th>Existing results</th>
</tr>
</thead>
<tbody>
<tr>
<td>Si$^+$</td>
<td>a b c d</td>
</tr>
<tr>
<td>P$^{2+}$</td>
<td>c</td>
</tr>
<tr>
<td>S$^{3+}$</td>
<td>a b c d</td>
</tr>
<tr>
<td>Cl$^{3+}$</td>
<td>c</td>
</tr>
<tr>
<td>Ar$^{5+}$</td>
<td>c [d]</td>
</tr>
<tr>
<td>K$^{6+}$</td>
<td>c</td>
</tr>
<tr>
<td>Ca$^{7+}$</td>
<td>b c</td>
</tr>
<tr>
<td>Ti$^{7+}$</td>
<td>c</td>
</tr>
<tr>
<td>Cr$^{11+}$</td>
<td>c</td>
</tr>
<tr>
<td>Mn$^{12+}$</td>
<td>c</td>
</tr>
<tr>
<td>Fe$^{13+}$</td>
<td>b c [d]</td>
</tr>
<tr>
<td>Co$^{14+}$</td>
<td>c</td>
</tr>
<tr>
<td>Ni$^{15+}$</td>
<td>b c</td>
</tr>
<tr>
<td>Cu$^{16+}$</td>
<td>k</td>
</tr>
<tr>
<td>Zn$^{17+}$</td>
<td>k</td>
</tr>
</tbody>
</table>


(Altun et al. 2006), and magnesium-like (Altun et al. 2007) isoelectronic sequences; for the argon-like sequence, total DR rate coefficients from the ground state have also been computed (Nikolić et al. 2010). Radiative recombination (RR) rate coefficients have also been calculated by Badnell (2006d) for all isoelectronic sequences up to magnesium-like ions. However, no systematic, state-of-the-art calculations have been performed for the aluminum-like isoelectronic sequence, and yet these ions are also abundant in astrophysical plasmas. For example, lines of Si ii, Ar vi, and Ca xvi have been observed with high-resolution by the Solar and Heliospheric Observatory (SoHO) (Curdt et al. 2001, 2004; Landi et al. 2004). Thus there is a need for an up-to-date, reliable database for this system. The purpose of the present paper is to report on a detailed investigation of DR for this sequence and the production of new, accurate DR rate coefficients for aluminum-like ions.

2. Existing aluminum-like DR data

The aluminum-like DR rate coefficients that are presently being used as input for the modeling codes such as CLOUDY, XSTAR, and CHIANTI have been taken from the recommended database of Mazzotta et al. (1998), which is a compilation of the most reliable DR data available at that time, with interpolation and/or extrapolation of data to ionization stages for which no explicit calculations existed, as summarized in Table 1. The first calculations of DR rate coefficients for aluminum-like ions were carried out by Jacobs et al. (1977a,b, 1979, 1980) for Si ii, S iv, Ca xii, Fe xiv, and Ni xvi using an uncoupled angular momentum description of DR. In this simplified model, the autoionization rates were obtained from the threshold values of the partial-wave electron-impact excitation cross sections for the corresponding ions by means of the quantum-defect theory relationship between these values. The excitation cross sections were obtained in the distorted-wave approximation and only dipole 3s$\rightarrow$3p and 3p$\rightarrow$3d transitions were included. In addition, radiative decay of autoionizing states was approximated as the ionic core radiative decay rate. A single fitting formula for all temperatures $T$ and all ionization stages $q$ was then developed by Mewe et al. (1980) in part on the computed data for Fe xiv and Si ii by Jacobs et al. and in part on the data of Ansari et al. (1970). However, this $q$-scaling is based on the Burgess formula parameterization (Burgess 1965) and fails to account for the highly non-hydrogenic behavior of the rate coefficient at low $q$. A more accurate parameterization was produced by Shull & Van Steenberg (1982) using a two-peak fit formula $a^{DR}(T) = \sum_{i=1}^{2} c_i e^{-E_i/T}$, where the $c_i$ and $E_i$ were obtained from a least-squares fit to the rate coefficients of Jacobs et al. for Si ii, S iv, Ca xii, Fe xiv, and Ni xvi, and these parameters were then interpolated to obtain similar fitting coefficients for Ar vi. Using the fits of Shull & Van Steenberg (1982), a similar parameterization was obtained by interpolation for P iii, Cl v, K vii, Ti x, Cr xii, Mn xiii, and Co xv (Landini & Monsignori Fossi 1991).

Explicit DR calculations for S iv were also performed within an LS-coupling, distorted-wave approximation by Badnell (1991), using AUTOSTRUCTURE (Badnell 1986, 1997), as is implemented in the present study, and by Al-Mulhem & Nasser (1992), using Cowan's code (Cowan 1981), considering only the 3s $\rightarrow$ 3p excitations. Then a series of LS R-matrix calculations was performed for Si ii and S iv (Nahar & Pradhan 1995; Nahar 1996), and for Ar vi, Ca xii, and Fe xiv (Nahar 2000). DR rate coefficients for Si ii and S iv were also determined by Aldrovandi & Péguinot (1973) using the Burgess formula (Burgess 1965), and a low-resonance (i.e., low-temperature) rate coefficient was obtained by Nussbaumer & Storey (1986).

Such was the status of available aluminum-like DR rate coefficients when the database of Mazzotta et al. (1998) was compiled. In most cases, that data was ultimately derived from the LS calculations of Jacobs et al. (1977a,b, 1979, 1980), which were fit by Shull & Van Steenberg (1982) for even-numbered
nuclei (and interpolated for Ar vi), and then interpolated for odd-numbered nuclei by Landini & Monsignori Fossi (1991) – see Table 1. (These data were also extrapolated to Cu xvi and Zn xvii by Mazzitelli & Mattioli 2002.) However, for Si ii and S iii, Mazzotta et al. (1998) chose to incorporate the R-matrix results of Nahar & Pradhan (1995) and Nahar (1996). All of the compiled results were thus based on simpler LS calculations that, as we will see, did not include all of the important physics required for aluminum-like ions, especially the effects of fine-structure splitting.

Since the compilation of Mazzotta et al. (1998), the only aluminum-like DR data produced has been, first, the configuration-averaged distorted-wave (CADW) results of Loch et al. (2007) for Ar vi, and, importantly, the storage ring experimental results of Schmidt et al. (2006) for Fe xiv, with accompanying calculations by Badnell (2006c). These latter calculations were performed using the multi-configuration Breit-Pauli code AUTOSTRUCTURE, including important configuration-interaction and fine-structure splitting effects, as was verified by the good agreement between experimental and theoretical DR rate coefficients. The purpose of the present study is to compute DR rate coefficients for the entire aluminum-like isoelectronic sequence using the same methodology as was implemented by Badnell (2006c), as described in the next section, and thus to create a new DR database for this isoelectronic sequence.

3. Theory

Since the more in-depth details of our calculations have already been described by Badnell et al. (2003), we only outline the main points here. DR calculations are performed with the AUTOSTRUCTURE code (Badnell 1986, 1997; Badnell & Pindzola 1989), a multi-configuration Breit-Pauli (MCBP) implementation within an independent processes and isolated resonance distorted-wave (IPIRDW) approximation. This code is based on lowest order perturbation theory, where both the electron-electron and electron-photon interactions are treated to first order. Energy levels and radiative and autoionization rates were calculated in LS- and IC-coupling (MCBP) approximations.

For the initial atomic structure, we follow the same methodology used in Badnell (2006c). A basis consisting of the 3s23p, 3s3p2, 3s23d, 3p3, 3s3p3d, 3p23d, 3s3d2, and 3p3d2 configurations was used to describe the aluminum target states. Optimized radial orbitals were determined by varying the scaling parameters, \(\lambda_{Mt}\) in model STO potentials (Burgess et al. 1989) and including the mass-velocity and Darwin corrections. The values of the radial scaling parameters for the 1s, 2s, and 2p closed-core orbitals were fixed at the default value of 1.0 whereas the \(\lambda_{Mt}\) values were optimized and yielded the values listed in Table 2. Distorted wave calculations were performed to generate the continuum \(\epsilon\ell\) and bound \(nl^m\) (\(n > 3\)) orbitals. The \((N+1)-\)electron basis configurations were then constructed by coupling an \(\epsilon\ell\) or \(nl^m\) orbital to the \(N\)-electron target configurations. Autoionization and radiative rates (electric dipole) were determined from wave functions constructed using all such \((N+1)-\)electron configurations and then used to calculate the DR cross sections and rate coefficients for the desired aluminum-like ion.

The DR process for an arbitrary aluminum-like ion \(I^+,\) with a degree of ionization \(q,\) for \(\Delta\eta_c = 0\) core excitation \((3s \rightarrow 3p, 3s \rightarrow 3d,\) and \(3p \rightarrow 3d)\) can be described as

\[
e^{-} + 1^{(+)}(3s^{2}3p^{2}P_{1/2}) \rightarrow 1^{(+)\rightarrow} \rightarrow 1^{(+)\rightarrow} + hv,
\]

where the doubly-excited intermediate resonance states \((\ell)\) include \(3s^{2}3p^{3n}, 3s3p^{2}3d^{n}, 3p^{4}3d, 3p^{3}3d^{2}, 3p^{3}3d^{2}n,\) and \(3p^{3}3d^{2}n\). Values for the principal quantum number \(n\) were included up to \(n = 55,\) and a quantum-defect approximation was used for higher values \(56 \leq n \leq 1000\) (Badnell et al. 2003), while the values for the orbital quantum number were included up to \(\ell = 13.\) For \(\Delta\eta_c = 1,\) only \(3 \rightarrow 3, 3 \rightarrow 4, 3p \rightarrow 4\ell,\) and \(3d \rightarrow 4\ell\) core-excitations were considered, and we used \(3s^{2}3f^{2}, 3s3p^{4}4f,\) and \(3p^{4}4f^2\) configurations (with \(0 \leq \ell \leq 3\)) in addition to those used for \(\Delta\eta_c = 0.\) These 20 configurations gave rise to 295 target levels. Other values included were \(\ell \leq 6\) and \(n \leq 55,\) with a quantum-defect approximation for higher \(n \leq 1000.\)

In the IPIRDW approximations, the partial DR rate coefficients \(a_{ij}^{AB}\) from an initial metastable level \(i\) into a final level \(f\) are given by

\[
a_{ij}^{AB} = \frac{4\pi\alpha_{\ell}^{2}I_{q}}{kT} \frac{3/2}{\sum_{d} g_{d}} \sum_{d} \frac{g_{d}}{2g_{i}} \exp \left( \frac{E_{c}}{kT} \right) \times \frac{\sum_{h} A_{d-hi}^{A^{m}_{\alpha=\beta,E_{h}}} A_{d-i}^{A^{m}_{\alpha=\beta,E_{h}}}}{\sum_{h} A_{d-hi}^{A^{m}_{\alpha=\beta,E_{h}}} + \sum_{m,l} A_{d-lm}^{A^{m}_{\alpha=\beta,E_{h}}}},
\]

where \(g_{d}\) is the statistical weight of the \((N + 1)-\)electron doubly-excited resonance state \(d,\) \(g_{i}\) is the statistical weight of the \(N\)-electron target state and the autoionization \(A^{A}\) and radiative \(A^{r}\) rates are in inverse seconds. Here, \(E_{c}\) is the energy of the continuum electron angular momentum \(\ell,\) which is fixed by the position of the resonances, and \(I_{q}\) is the ionization potential energy of the hydrogen atom, \(k\) is the Boltzmann constant, \(T\) is the electron temperature, and \(4\pi\alpha_{\ell}^{2}I_{q}^{3/2} = 6.6011 \times 10^{-24} \text{cm}^{2} \text{.}\) Partial DR rate coefficients from the ground and metastable states are tabulated according to the ADAS (Summers 2003) ad/09 format.

The total \((\Delta\eta_{c} = 0\) plus \(\Delta\eta_{c} = 1)\) DR rate coefficients were fitted using the formula

\[
a_{\text{DR}}(T) = \frac{1}{T^{3/2}} \sum_{i} c_{i} \exp \left( \frac{E_{c}}{T} \right),
\]
where $T$ and $E_i$ are in units of temperature (K) and the rate coefficients $a^{\text{DR}}$ are in units of cm$^3$ s$^{-1}$.

For our RR calculations, the same procedure used by Badnell (2006d) is employed here. Briefly, the aluminum-like targets were described by the eight configurations that were used in the DR calculations for the $n = 3$ complex, and capture to all $nl$ up to $n \leq 1000$ and $l \leq 200$ were included (with $f \geq 4$ treated hydrodynamically).

The total RR rate coefficients were fitted using the formula (Verner & Ferland 1996)

$$a^{\text{RR}}(T) = A \sqrt{T_0/T} \left[ \left( 1 + \sqrt{T/T_0} \right)^{1-B} \left( 1 + \sqrt{T/T_1} \right)^{1+B} \right]^{-1},$$

where, for low-charge ions, we replace $B$ by (Gu 2003)

$$B \rightarrow B + C \exp(-T_2/T).$$

Here, $T_{0,1,2}$ are in units of temperature (K), the rate coefficients $a^{\text{RR}}(T)$ are in units of cm$^3$ s$^{-1}$, $A$ has units of cm$^3$ s$^{-1}$, and $B$ and $C$ are dimensionless. Partial RR rate coefficients are tabulated according to the ADAS (Summers 2003) adj48 format.

### 4. Results

Using AUTOSTRUCTURE as described above, we computed DR rate coefficients, in both $LS$-coupled and Breit-Pauli, intermediate-coupled (IC) approximations, for the entire aluminum-like isoelectronic sequence. These results are compared to all other available data in Figs. 1–4. Also indicated in these figures are the regions of maximum abundance in both photoionized and collisionally-ionized plasmas. The photoionized zones were calculated by us using CLOUDY (v08.00; Ferland et al. 1998), whereas the collisionally ionized zones were obtained based on the calculations of Bryan et al. (2009), assuming the fractional abundance of the target ions are 10% of their peak values in each case.

We first focus on the case of Si IV, since several independent $LS$-coupled calculations have been reported for this ion. It is seen in an expanded view (see Fig. 4) that our present $LS$ results are in excellent agreement with the earlier $LS$ AUTOSTRUCTURE results of Badnell (1991), as is expected. These results are also in good agreement with those of Jacobs et al. (1979), and thus with the fitted curve of Shull & Van Steenberg (1982). We find fair agreement with the results of Al-Mulhem & Nasser (1992) up to about the peak of either rate coefficient; however, the high-temperature tail of the Al-Mulhem & Nasser (1992) results is appreciably lower than our present results, presumably due to their only including the $3s \rightarrow 3p$ core excitations and neglecting the $3p \rightarrow 3d$ excitations that are more important at higher energies.

Also shown are the $LS$ R-matrix results (Nahar & Pradhan 1995; Nahar et al. 2000) for the coherent sum of DR and RR; a DR rate coefficient was inferred from these and then used as data in the compilation of Mazzotta et al. (1998). Aside from the low-temperature difference due to their inclusion of RR (we show our present RR results for comparison), these R-matrix calculations yielded a peak rate coefficient that is significantly lower than all other $LS$ calculation peaks – their peak is only 74% of our present $LS$ peak. Although the reason for such a large discrepancy is unclear, it should be pointed out that the use of the R-matrix method for computing DR cross sections is problematic in that radiation damping effects, which were not included in the calculations of Nahar & Pradhan (1995); Nahar et al. (2000), need to be considered, and, furthermore, sufficient resolution of the resonances is required – see Gorczyca & Badnell (1997) and Gorczyca et al. (2002) for further discussions.

It can be seen that neither the Burgess formula results of Aldrovandi & Péquignot (1973) nor the parameterized Burgess-type expression of Mewe et al. (1980) correctly predict the quantitative behavior of the rate coefficient. Although the Mewe et al. (1980) results used some of the parameters in their fit from the results of Jacobs et al. (1979), other parameters in the fit were determined from Ansari et al. (1970), thereby leading to the large discrepancy seen between the Mewe et al. (1980) and Jacobs et al. (1979) results.

Also shown in Fig. 4 are the present IC results, which have taken into account additional fine-structure effects. It is seen that these results differ significantly from the present $LS$ results: at lower temperatures, the IC results are higher than the $LS$ results, whereas at higher temperatures, the IC results are lower than the $LS$ results. In order to gain a better understanding of why relativistic (mainly spin-orbit-induced, fine-structure splitting) effects are important here for a low-charged system, we study the DR resonance features in closer detail. A comparison of the present $LS$ and IC cross sections is shown in Fig. 5. In the low-energy region, it is seen that the additional fine-structure-split series $e^- + 3s^23p(^1P_{1/2}) \rightarrow 3s^23p^1P_{3/2}n\ell$, which is present in the IC calculation but not accounted for in the $LS$ calculation, gives an appreciable contribution to the DR cross section below the $3s^23p^1P_{3/2}n\ell$ threshold at 0.118 eV, thus explaining the enhancement of the IC rate coefficient at lower temperatures. Note also that these fine-structure resonances are not included in the simplified dipole model of Jacobs et al. (1977a, b, 1979, 1980).

At higher energies near the strong, dipole-allowed $3s^3p^2$ and $3s^2d^3$ thresholds, on the other hand, the IC threshold cross section is suppressed relative to the $LS$ cross section. Looking in greater detail at the $3s^3p^2(^1P_{1/2,3/2})n\ell$ Rydberg resonance behaviors as threshold is approached (see Fig. 6), it can be seen that there is a sudden drop-off in IC DR resonance strengths for $n \geq 36$ in both series. It is at this point that the resonances, after having core radiatively decayed to the $3s^23p^2(^1P_{1/2,3/2})n\ell$ states, subsequently autoionize and do not contribute to the DR process (Jacobs et al. 1977b). The entire process, dielectronic capture, radiative decay, and subsequent autoionization, can be depicted as

$$e^- + 3s^23p(^1P_{1/2}) \rightarrow 3s^23p^1P_{3/2}n\ell + \nu \rightarrow 3s^23p(^1P_{1/2}) + e^-,$$

and is responsible for the suppression of the DR rate coefficient at higher temperatures. Thus, the proper treatment of $3s^23p^2(^1P_{1/2,3/2})-3s^23p^2(^3P_{1/2})$ fine-structure splitting leads to an additional Rydberg series at lower energies, thereby increasing the low-temperature DR rate coefficient, but also leads to the subsequent autoionization of radiatively-decayed states from the core-excited resonances at higher energy, thereby decreasing the higher-temperature DR rate coefficient. We find that the higher-temperature suppression is constant for all lower ionization stages as $\alpha_{GC}/\alpha_{LS} \approx 0.8$ until about $Sc\alpha$, when the $\Delta n > 0$ core excitations become more prominent and gradually mask this $\Delta n = 0$ suppression, tending toward a reduced suppression of $\alpha_{GC}/\alpha_{LS} \approx 0.9$ at higher ionization stages.

These trends are evident in Figs. 1–4, which show our present $LS$ and IC results for the entire isoelectronic sequence. Also shown are all other available aluminum-like DR data. These comparisons emphasize, first and foremost, that essentially all of the earlier results do not account for the
Fig. 1. Present Maxwellian-averaged DR and RR rate coefficients for Si-ⅱ–Ca-ⅻ ions (excluding S-ⅳ – see Fig. 4): red solid curve, present IC; blue solid curve, present LS; green solid curve, previous recommended compilation (Mazzotta et al. 1998); gray dashed curve, present RR rate coefficient; (a) black dashed curve, Burgess formula (Aldrovandi & Péquignot 1973); (b) black squares, LS (Jacobs et al. 1979); (c) black dash dotted curve, empirical formula (Mewe et al. 1980); (d) open circles, fitted data (Shull & Van Steenberg 1982); (e) red circles, extrapolated fits (Landini & Monsignori Fossi 1991); (f) magenta solid curve, LS R-matrix, RR + DR (Nahar & Pradhan 1995; Nahar 1996, 2000); (i) black dotted curve, low temperature data (Nussbaumer & Storey 1986); and (j) pink dotted curve, configuration-average distorted-wave results (Loch et al. 2007).
Fig. 2. Present Maxwellian-averaged DR and RR rate coefficients for Sc-ix-Fe-xiv ions: red solid curve, present IC; blue solid curve, present LS; green solid curve, previous recommended compilation (Mazzotta et al. 1998); gray dashed curve, present RR rate coefficient; (b) black squares, LS (Jacobs et al. 1979); (c) black dash dotted curve, empirical formula (Mewe et al. 1980); (d) open circles, fitted data (Shull & Van Steenberg 1982); (e) red circles, extrapolated fits (Landini & Monsignori Fossi 1991); (f) magenta solid curve, LS R-matrix, RR + DR (Nahar 2000); (g) black solid curve, IC AUTOSTRUCTURE (Badnell 2006c); and (l) blue dashed curve, experimental measurements (Schmidt et al. 2006).
Fig. 3. Present Maxwellian-averaged DR and RR rate coefficients for Co XV–Zn XIX ions: red solid curve, present IC; blue solid curve, present LS; green solid curve, previous recommended compilation (Mazzotta et al. 1998); gray dashed curve, present RR rate coefficient; (b) black squares, LS (Jacobs et al. 1979); (c) black dash dotted curve, empirical formula (Mewe et al. 1980); (d) open circles, fitted data (Shull & Van Steenberg 1982); (e) red circles, extrapolated fits (Landini & Monsignori Fossi 1991); and (k) blue circles, extrapolated fit (Mazzitelli & Mattioli 2002).

Fig. 4. DR rate coefficients of S IV: red solid curve, present IC; blue solid curve, present LS; green solid curve, previous recommended compilation (Mazzotta et al. 1998); gray dashed curve, present RR rate coefficient; (a) black dashed curve, Burgess formula (Aldrovandi & Péquignot 1973); (b) black squares, LS (Jacobs et al. 1979); (c) black dash dotted curve, empirical formula (Mewe et al. 1980); (d) open circles, fitted data (Shull & Van Steenberg 1982); (f) magenta solid curve, LS R-matrix, RR + DR (Nahar & Pradhan 1995; Nahar 1996, 2000); (g) black solid curve, LS AUTOSTRUCTURE (Badnell 1991); and (h) open stars, LS (Al-Mulhem & Nasser 1992).
lower-temperature DR that is due to lower-lying resonances below the Rydberg limit. This becomes especially pronounced at the higher ionization stages. On the other hand, the high-temperature tail of the results based on the fits of Mewe et al. (1980), Shull & Van Steenberg (1982), or Landini & Monsignori Fossi (1991) tend to align more with our LS results at higher ionization stages (of course, fine-structure effects reduce this tail by about 10%, as previously discussed). It appears that the LS results of Jacobs et al. (1980) for Ca vii have included the effects of lower resonances, but the fit of Shull & Van Steenberg (1982) omitted this lower-temperature contribution. The CADW results of Loch et al. (2007) for Ar vi also predict a low-temperature rate coefficient in qualitative agreement with the present calculations; those calculations used the same IPIRDW approach, but neglected the term splitting of configurations, and, more importantly, did not include 3s → 3d contributions, hence the lower rate coefficient at high temperature.

The \( R \)-matrix calculations (Nahar & Pradhan 1995; Nahar 1996, 2000) do predict a low-temperature feature, but it is not clear how much of this is due solely to RR, which that unified method includes coherently along with DR (results from our present RR calculation are also shown for comparison). Furthermore, those \( R \)-matrix results are particularly troubling, especially at the lowest ionization stage of Si ii, for which their peak rate coefficient is almost an order of magnitude less than the present LS results (and the Burgess formula results of Aldrovandi & Péquignot 1973). Note for this lowest ionization stage, the results of Jacobs et al. (1977b) are only about one-third of the present LS results. These discrepancies could be due to the fact that, since electron correlation effects are strongest at the lowest ionization stage, it is here that the inaccuracies introduced by cruder theoretical approximations and/or implementations is expected to be most prominent.

Perhaps the most meaningful comparison of all aluminum-like ions is for Fe xiv, which not only has received considerable theoretical attention, due to its astrophysical importance, but the DR rate coefficient has also been measured experimentally at the Test Storage Ring (TSR) facility (Schmidt et al. 2006). For this ion, we see that our IC rate coefficient is in excellent agreement with the earlier IC AUTOSTRUCTURE results of Badnell (2006c), as expected, and these agree well with the experimental results at higher temperatures. Here the results of Jacobs et al. (1977a) are also in good agreement, and therefore so are the fitted results of Shull & Van Steenberg (1982); as discussed earlier, the parameterized results of Mewe et al. (1980) also are fairly reliable at higher ionization stages and higher temperatures. However, those earlier rate coefficients of Jacobs et al. (1977a), Shull & Van Steenberg (1982), and Mewe et al. (1980) do not consider low-temperature contributions. The \( R \)-matrix results (Nahar 2000) do indicate some contribution at lower temperatures, but the absolute rate coefficient, at all temperatures, is inexplicably at least a factor of three lower than our present results or experiment.

The present or earlier IC Maxwellian rate coefficients for Fe xiv are substantially lower than the experimental results at lower temperature. In order to study this discrepancy in finer detail, we compare the two rate coefficients, in Fig. 7, at the experimental electron-cooler thermal distribution resolution, characterized by a transverse temperature of \( kT_\perp = 12 \text{ meV} \) and a
Comparison of present IC (red solid curve) and experimental measurements (blue solid curve, Schmidt et al. 2006) DR rate coefficients for Fe XIV.

Fig. 7. Comparison of present IC (red solid curve) and experimental measurements (blue solid curve, Schmidt et al. 2006) DR rate coefficients for Fe XIV.

Fig. 8. Comparison between present IC results (red solid curve) and recommended compilation (green solid curve, Mazzotta et al. 1998) for the aluminum-like isoelectronic sequence.

longitudinal temperature of $kT_l = 0.09$ meV with respect to the ion beam direction (Dittner et al. 1986). Just above threshold, the theoretical rate coefficient is much lower than experiment. This is surely due to the slight inaccuracies in resonance energies; if a resonances occurs in the vicinity of threshold and the theoretical prediction for its position is in error by a small negative energy, than that resonance is erroneously not included in the DR cross section contribution – see Robicheaux et al. (2010) for a recent discussion. This is an inherent limitation in the current state of theoretical calculations for very low energies. However, there is also a theoretical underestimate in the rate coefficient at about 25 eV; this cannot be explained by slight inaccuracies in resonance positions, but might instead be due to configuration-interaction (CI) between different Rydberg series, leading to a suppressed DR contribution. The experimental Maxwellian rate coefficient shown in Fig. 7 has therefore also included an estimated addition for high Rydberg states, computed using AUTOSTRUCTURE, and this inclusion gives a modified experimental rate coefficient that is slightly higher than theory for high temperatures.

In comparing the present results to previous data, several conclusions can be reached. First and foremost, our present IC results are in good agreement with the only experimental results available – the TSR data for Fe XIV (Schmidt et al. 2006). Second, all previous LS rate coefficients for Si iv were consistent with the present LS results except, inexplicably, the $R$-matrix results (Nahar & Pradhan 1995; Nahar 1996, 2000); similar $R$-matrix results for Si ii were almost an order of magnitude less than the present LS results. Third, the recommended compilation by Mazzotta et al. (1998) was ultimately based on the simplified-model results of Jacobs et al. (1977a,b, 1979, 1980), which were then fitted by Shull & Van Steenberg (1982) and Landini & Monsignori Fossi (1991), except in the case of Si ii and S iv, for which the anomalous $R$-matrix results (Nahar & Pradhan 1995; Nahar 1996, 2000) were used. Lastly, even the accurate LS calculations did not include the physical effects of fine-structure splitting, which give rise to an additional Rydberg series near threshold, thereby increasing the low-temperature DR rate coefficient, and also allow autoionization of higher-$n$ ($n > 35$) radiatively decayed states, decreasing the high-temperature DR rate coefficient.

The net effect of including all the correct physics in our present, state-of-the-art IC calculations is shown in Fig. 8. The present IC DR rate coefficients for the entire aluminum-like sequence is shown (lower curves correspond to lower ionization stage) compared to the compiled data of Mazzotta et al. (1998) – that which had been used to date in plasma modeling codes. It is most readily seen that the earlier data do not include any of the low-temperature contributions that become increasingly important as the ionization stage is increased. At higher-temperatures, there is still a large discrepancy, especially for the lowest-charged ions, where the earlier compiled rate coefficients are significantly weaker due to the poor LS results that were
used. And even for higher ionization stages, where electron correlation becomes less important and the earlier LS results and/or scaled fits are more reliable, the high-temperature tail eventually exceeds the present results, due to the reautoionization phenomena that is not included in those LS results.

Total DR rate coefficients (Δνe = 0 or Δνe = 1) for the entire aluminum-like isoelectronic sequence are fitted using Eq. (3) and the DR fitting coefficients are listed in Table 3. These fits are accurate better than 5% for all the Al-like isoelectronic sequence in the electron temperature range $q^2(10-10^5)$ K, where $q$ is the charge of the recombining ion. The accuracy is better than 1% over the collisionally ionized range. On the other hand, our RR rate coefficients data for this isoelectronic sequence are fitted using Eqs. (4) and (5). The RR fitting coefficients are tabulated in Table 4. The fits are accurate to better than 1% over the temperature range $q^2(10-10^5)$ K.

Lastly, we have also included DR from metastable states in addition to the ground-state. Representative results for Mn xii are shown in Fig. 9 for the first five levels. Not only are there enormous difference between results for the two LS terms, but there is a significant difference between DR from the two fine-structure-split $3s^23p^3P_{1/2}$ and $3s^23p^3P_{3/2}$ levels, especially at low temperature, since the $m = 2$ series no longer has a second fine-structure-split Rydberg series enhancement near threshold.

These comparisons further emphasize the need for tabulation of DR data from ground and metastable states.

5. Summary

We have carried-out systematic calculations of DR and RR rate coefficients for the aluminum-like isoelectronic sequence in a multi-configuration intermediate coupling Breit-Pauli approximation for all ions (Si ii–Zn xviii). All previous DR data for this isoelectronic sequence were either obtained by using empirical formulas or were performed in an LS-coupling or simplified framework and did not include all of the relevant physics. We find that, most importantly, the inclusion of fine-structure effects in our calculations led to an increased low-temperature DR rate coefficient, due to the additional fine-structure-split $3s^23p^3P_{1/2}$ DR resonance series, and a decreased high-temperature DR rate coefficient, due to the subsequent reautoionization of fine-structure-excited radiative decay states, compared to all earlier LS-coupled calculations. As a result, the earlier recommended database (Mazzotta et al. 1998) contained DR rate coefficients that were unphysically low at lower-temperatures and unphysically high at higher temperatures. Furthermore, that database (Mazzotta et al. 1998) uses the
Table 4. RR fitting coefficients for the ground state of Al-like ions using Eq. 4. $Y(N)$ means $Y \times 10^N$.

<table>
<thead>
<tr>
<th>Ion</th>
<th>$A$</th>
<th>$B$</th>
<th>$T_0$</th>
<th>$T_1$</th>
<th>$C$</th>
<th>$T_2$</th>
</tr>
</thead>
<tbody>
<tr>
<td>Si$^+$</td>
<td>3.501(–11)</td>
<td>0.6344</td>
<td>1.410(+1)</td>
<td>4.343(+7)</td>
<td>0.2248</td>
<td>5.831(+4)</td>
</tr>
<tr>
<td>F$^{1+}$</td>
<td>1.348(–10)</td>
<td>0.6342</td>
<td>1.410(+1)</td>
<td>2.213(+7)</td>
<td>0.1784</td>
<td>4.692(+4)</td>
</tr>
<tr>
<td>S$^{2+}$</td>
<td>2.664(–10)</td>
<td>0.6896</td>
<td>2.107(+1)</td>
<td>2.028(+7)</td>
<td>0.0840</td>
<td>6.752(+4)</td>
</tr>
<tr>
<td>Cl$^{3+}$</td>
<td>3.996(–10)</td>
<td>0.7062</td>
<td>3.177(+1)</td>
<td>2.018(+7)</td>
<td>0.0467</td>
<td>8.299(+4)</td>
</tr>
<tr>
<td>Ar$^{4+}$</td>
<td>4.137(–10)</td>
<td>0.7064</td>
<td>6.853(+1)</td>
<td>2.108(+7)</td>
<td>0.0316</td>
<td>1.020(+5)</td>
</tr>
<tr>
<td>K$^{5+}$</td>
<td>4.328(–10)</td>
<td>0.6985</td>
<td>1.259(+2)</td>
<td>2.237(+7)</td>
<td>0.0271</td>
<td>1.033(+5)</td>
</tr>
<tr>
<td>Ca$^{6+}$</td>
<td>4.279(–10)</td>
<td>0.6860</td>
<td>2.289(+2)</td>
<td>2.459(+7)</td>
<td>0.0262</td>
<td>9.582(+4)</td>
</tr>
<tr>
<td>Sc$^{7+}$</td>
<td>4.952(–10)</td>
<td>0.6887</td>
<td>2.874(+2)</td>
<td>2.679(+7)</td>
<td>0.0192</td>
<td>1.075(+5)</td>
</tr>
<tr>
<td>Ti$^{8+}$</td>
<td>6.008(–10)</td>
<td>0.6876</td>
<td>3.176(+2)</td>
<td>2.946(+7)</td>
<td>0.0162</td>
<td>9.838(+4)</td>
</tr>
<tr>
<td>V$^{10+}$</td>
<td>4.424(–10)</td>
<td>0.6487</td>
<td>8.751(+2)</td>
<td>3.451(+7)</td>
<td>0.0285</td>
<td>8.744(+4)</td>
</tr>
<tr>
<td>Cr$^{11+}$</td>
<td>5.256(–10)</td>
<td>0.6587</td>
<td>8.457(+2)</td>
<td>3.709(+7)</td>
<td>0.0217</td>
<td>9.474(+4)</td>
</tr>
<tr>
<td>Mn$^{12+}$</td>
<td>5.330(–10)</td>
<td>0.6471</td>
<td>1.146(+3)</td>
<td>4.169(+7)</td>
<td>0.0236</td>
<td>1.013(+5)</td>
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<tr>
<td>Fe$^{13+}$</td>
<td>5.370(–10)</td>
<td>0.6338</td>
<td>1.531(+3)</td>
<td>4.632(+7)</td>
<td>0.0278</td>
<td>9.070(+4)</td>
</tr>
<tr>
<td>Co$^{14+}$</td>
<td>6.045(–10)</td>
<td>0.6412</td>
<td>1.616(+3)</td>
<td>4.963(+7)</td>
<td>0.0223</td>
<td>1.249(+5)</td>
</tr>
<tr>
<td>Ni$^{15+}$</td>
<td>6.334(–10)</td>
<td>0.6317</td>
<td>1.936(+3)</td>
<td>5.428(+7)</td>
<td>0.0256</td>
<td>1.048(+5)</td>
</tr>
<tr>
<td>Cu$^{16+}$</td>
<td>5.858(–10)</td>
<td>0.6135</td>
<td>2.836(+3)</td>
<td>6.013(+7)</td>
<td>0.0317</td>
<td>1.033(+5)</td>
</tr>
<tr>
<td>Zn$^{17+}$</td>
<td>7.187(–10)</td>
<td>0.6349</td>
<td>2.440(+3)</td>
<td>6.073(+7)</td>
<td>0.0221</td>
<td>1.534(+5)</td>
</tr>
</tbody>
</table>

Fig. 9. Maxwellian-averaged total DR (red solid curve) and RR (gray dashed curve) rate coefficients from the ground and metastable 3s$^2$3p ($^3P_{1/2,3/2}$) ($m = 1, 2$) and 3s3p$^2$ ($^3P_{1/2,3/2,5/2}$) ($m = 3–5$) initial levels.

$R$-matrix results of Nahar & Pradhan (1995) for Si$^+$ which are inexplicably almost an order of magnitude lower than any other LS results.

Our present final IC results are benchmarked to the existing experimental data (Schmidt et al. 2006) for Fe $^{14+}$, showing overall good agreement for the total DR rate coefficient. However, our present IC rate coefficient, using the experimental energy distribution, is found to be less than the experimental rate coefficient at lower temperature, which we attribute to a theoretical uncertainty in the energy positions of near-threshold resonances (whether they are predicted to be above or below threshold). There is also a noticeable difference in the two rate coefficients at about 25 eV above threshold, which may be due to interference effects between neighboring Rydberg series that are not included in our calculations. Nevertheless, our Maxwellian-averaged DR rate coefficient is found to be within the experimental uncertainty of 20% for all temperatures of interest.

Lastly, we have also considered partial recombination and metastable-state processes. All of our computed data have been tabulated in ADAS format, and total DR and RR rate coefficients have been fitted, for plasma modeling use.

Acknowledgements. We would like to thank E. W. Schmidt for providing us with the experimental data. This work was funded in part by NASA APRA, NASA SHP SR&T, and STFC grants.

References


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