

# Active Power Sharing in Input-Series-Input-Parallel Output-Series Connected DC/DC Converters

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**Abstract**—A high-capacity DC/DC converter with novel input-series-input-parallel output-series connection and with autonomous power sharing between modules is proposed. The proposed scheme is well suited for large-scale wind farm DC collection networks, as it avoids the charging current issues associated with its AC counterpart, and offers lower losses and reduced size and weight when a medium- or high-frequency transformer is used. Small-signal analysis is used to derive the control structures for the converter input and output stages. The proposed control scheme is validated through simulation and experimentation, including demonstration of autonomous power sharing between modules under several operating conditions.

**Keywords**—DC/DC converter, ISIPOS connection, Power sharing

## I. INTRODUCTION

Large offshore wind farms require substantial sub-sea power network to provide internal interconnection. Present solutions are based around conventional medium-voltage AC architectures. Recent studies have highlighted the potential benefits of DC collection networks. Such DC architectures depend on DC/DC conversion to step up the wind-generator output to a voltage compatible with efficient interconnection. Achieving DC/DC conversion at the required voltage and power levels presents a significant challenge for wind-turbine generator's power electronics. Since voltage levels in medium- and high-voltage systems exceed individual semiconductor device voltage ratings, high-capacity converters often require series connection of power devices.

In this paper, a high-power modular structure DC/DC converter which is realized by input-series-input-parallel output-series (ISIPOS) connection of modules is proposed. Parallel-series architectures can be classified into four categories based on their connection. These categories are input parallel output parallel (IPOP), input parallel output series (IPOS), input series output parallel (ISOP) and input series output series (ISOS) [1]. Currently, the open literature contains no publication in the field of the ISIPOS converter and its control strategy. This structure enables generation of high output voltage with reduced voltage and current stresses at the input side. Moreover, the use of high-frequency (HF)

or medium-frequency (MF) for galvanic isolation [2, 3], allows the heavy line-frequency transformer in an AC grid to be eliminated, leading to significant weight and size savings and much less investment in copper and core material. For example, the estimated mass of a 1MVA medium-frequency (4kHz) transformer is 150kg, whereas that of a 1MVA 50Hz transformer is 3 tons [4]. With series-output connection, the turns-ratio of the isolation transformer can be reduced, leading to a reduction in leakage inductance. Additionally, modular DC/DC converters offer more compact and lighter designs in situations where a single high-voltage converter with series connection of switches can be replaced with a set of low-voltage converter modules as being discussed in this paper. It will also solve the problem of additional snubber component and more complex gate drive units caused by the series connection of switches [5]. Compared to DC/DC converter based modular multilevel converter (MMC), re-configurability and potential for interleaved control may make the ISIPOS DC/DC converter an attractive choice in medium-voltage applications. ISIPOS connection of multiple low-voltage modules provides an excellent solution for scalability of DC/DC converters, with improved robustness and possibility of fault-tolerant operation. Modular architectures offer further advantages, including internal fault management and module reconfiguration as a result of ' $n+k$ ' designed redundancy and the use of power electronic building blocks (PEBB) to reduce production [6-8].

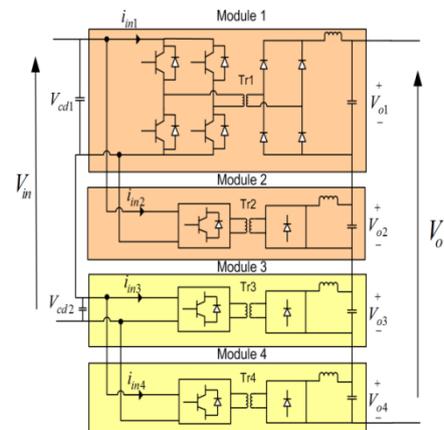


Fig. 1. Four-module ISIPOS DC/DC converter

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Fig.1 shows an illustrative schematic diagram of four-module ISIPOS DC/DC converter that forms the basis of the study. Reliable operation of the ISIPOS modular DC/DC converter requires a control mechanism that ensures equal power sharing among the individual modules, with ability to compensate for any mismatch in the passive components and active switching devices. In this paper, an active input side control scheme for converter power sharing is addressed. Also, the linearized control scheme offered by the Lyapunov control law is applied to provide an improved transient response.

The paper is organized as follows: power sharing in the ISIPOS DC/DC converter is presented in Section 2. In Section 3, the power sharing control strategy for this topology is discussed and the small-signal analyses necessary for controller design are presented. Section 4 presents the simulation and experimental results, and the conclusions are presented in Section 5.

## II. POWER SHARING

Assuming all four modules in Fig.1 are lossless, the relationships between the input and output powers of each module can be expressed as (1):

$$\begin{cases} V_{cd1} I_{in1} = V_{o1} I_o \\ V_{cd1} I_{in2} = V_{o2} I_o \\ V_{cd2} I_{in3} = V_{o3} I_o \\ V_{cd2} I_{in4} = V_{o4} I_o \end{cases} \quad (1)$$

where  $V_{cd1}$  is the DC input voltage for Modules 1 and 2 due to the parallel connection;  $V_{cd2}$  is similarly the DC input voltage for Modules 3 and 4;  $I_{in1}, I_{in2}, \dots, I_{in4}$  are the input currents to Modules 1 to 4,  $V_{o1}, V_{o2}, \dots, V_{o4}$  are the output voltages from Modules 1 to 4, and  $I_o$  is the load current. In steady-state condition, the average filter capacitor current is zero, and therefore only a very small filter inductor current ripple is assumed. If output voltage sharing (OVS) is achieved, then  $V_{o1}=V_{o2}=V_{o3}=V_{o4}$ . Substituting this result into (1) yields (2):

$$V_{cd1} I_{in1} = V_{cd1} I_{in2} = V_{cd2} I_{in3} = V_{cd2} I_{in4} \quad (2)$$

Since  $I_{in1}=I_{in3}$  due to the series connection, (2) leads to  $I_{in1}=I_{in3}=I_{in2}=I_{in4}$  and  $V_{cd1}=V_{cd2}$ . It should be noted that input power balancing can be achieved as long as OVS is achieved. Alternatively, if all modules share the same input power, which means Modules 1 and 2 (similarly for Modules 3 and 4) share the same input current and Modules 1 and 3 share the same input voltage, output voltage sharing is achieved.

The common feature revealed for an ISOS system [8-11] is the indispensability of input voltage sharing control. Fig.2 (a) illustrates the equivalent schematic diagram of the output side control strategies for the ISIPOS DC/DC converter. Assuming that OVS is achieved through output side control, modules behave as a constant power sink seen from the input side, with constant output current and equally shared output voltages. Thus, any increase of  $V_{cd1}$  leads to a decrease of  $i_{cin1}$  and drives the system from equilibrium

operating point A to B, as shown in Fig.2 (b). Fig.2 (b) also shows that  $i_{cin1}$  at point B is smaller than input current  $i_{in}$  and that input filter capacitor current  $i_{cd1}$  becomes positive, which will further increase  $V_{in1}$ . Thus, the equilibrium point cannot be resumed. An increase in input voltage  $V_{in1}$  leads to further increase of itself, eventually leading to a runaway condition between  $V_{in1}$  and  $V_{in2}$ . This means that any input disturbance may result in an inversely proportional current-voltage relationship. OVS cannot therefore provide input power sharing for the ISIPOS system.

Fig.3 (a) and (b) highlight the consequences of input side control. Modules behave as constant power source seen from the output side, with equally shared input voltage and current. Thus, an increase in  $V_{o1}$  leads to a decrease in  $i_{yf1}$  which drives the system from the equilibrium operating point A to B, as shown in Fig.3 (b). Now,  $i_{yf1}$  is smaller than the load current  $i_o$ , current  $i_{cf1}$  becomes negative, discharging the capacitor and driving the operating point back to A. Therefore, a dedicated input control loop is indispensable for ISIPOS DC/DC converter stable operation.

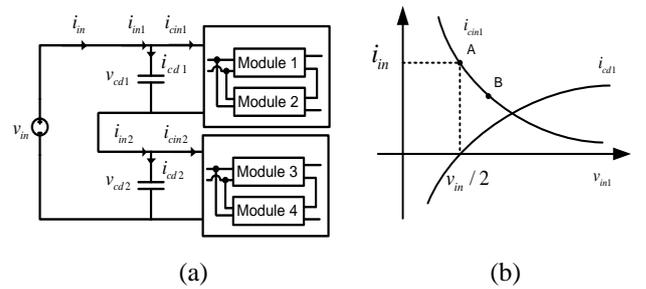


Fig. 2. ISIPOS DC/DC converter (a) output side control and (b) operating point

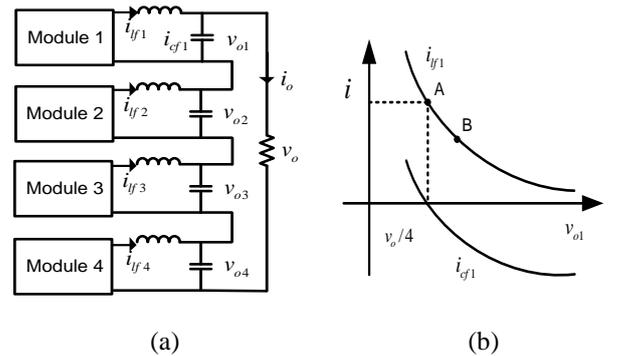


Fig. 3. ISIPOS DC/DC converter (a) input side control and (b) operating point

## III. CONTROLLER DESIGN

Converter output voltage control is normally achieved by a linear control technique such as PI control. In comparison, some non-linear techniques can provide improved transient response which is robust to load, input and parameter variations [12]. Most of the non-linear control laws are complex, which makes them difficult to apply, but the linearization schemes have the advantage of reducing the converter model to an equivalent output filter model which

significantly simplifies the control design process, without significant compromise to its robustness. A novel linearized equivalent model of the ISIPOS DC/DC converter incorporating closed-loop output voltage control is presented in Fig.4 [13] which provides a linear representation of converter behavior under large-signal variation which is suitable for faster control response and estimation of the converter state variables. This study applies a large signal Lyapunov controller, with the objective of controlling output voltage error for the ISIPOS DC/DC converter:

$$e = v_o^* - v_o \quad (3)$$

The first order Lyapunov control function  $v(x)$  and its derivative are given in (4) and (5), where  $\alpha$  is a proportionality constant and  $\beta$  is strictly a positive proportionality constant [13]:

$$v = \frac{1}{2}(\dot{e} + \alpha e)^2 \quad (3)$$

$$\dot{v} = (\dot{e} + \alpha e)(\ddot{e} + \alpha \dot{e}) = -\beta v < 0 \quad (4)$$

$$(\ddot{e} + \alpha \dot{e}) = -\frac{1}{2}\beta(\dot{e} + \alpha e) \quad (5)$$

From Fig.4, (6) and (7) can be derived. Control variable  $v_c$  can then be explicitly included in the second order transfer function of the output voltage (8).

$$\frac{di_{lf}}{dt} = \frac{1}{L_f} \left( \frac{1}{\pi} v_c - \frac{1}{4} v_o \right) \quad (6)$$

$$\frac{dv_o}{dt} = \frac{4}{C_f} (i_{lf} - i_o) = \frac{4}{C_f} \left( i_{lf} - \frac{v_o}{R_o} \right) \quad (7)$$

$$\ddot{v}_o = \frac{4}{C_f} \left( -\frac{v_o}{4L_f} + \frac{v_c}{\pi L_f} - \frac{\dot{v}_o}{R_o} \right) \quad (8)$$

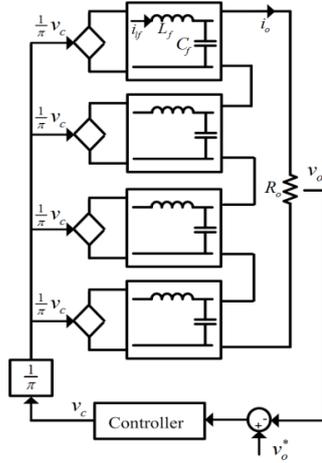


Fig. 4. Simplified large signal control for ISIPOS DC/DC converter

Assuming  $v_o^*$  to be constant,  $\dot{e} = -\dot{v}_o$  and  $\ddot{e} = -\ddot{v}_o$ . Based on Fig.4, (9) is deduced. This, in turn, yields (10).

$$\ddot{v}_o = \frac{\alpha\beta}{2}(v_o^* - v_o) - \frac{\beta}{2}\dot{v}_o - \alpha v_o = \frac{4}{C_f} \left( \frac{v_c}{L_f \pi} - \frac{v_o}{4L_f} - \frac{\dot{v}_o}{R_o} \right) \quad (9)$$

$$v_c = \frac{\alpha\beta C_f L_f \pi}{8} e + \frac{C_f L_f \pi}{4} \left( \frac{\beta}{2} + \alpha - \frac{1}{R_o C_f} \right) \dot{e} + \frac{\pi}{4} v_o \quad (10)$$

The first and second terms of (10) represent a PD controller, where 'e' will decay to 0 as the system output voltage  $v_o$  converges to its reference value.  $\pi v_o/4$  is a feed-forward term to speed start-up and to help stabilise the controller. Therefore, (10) can be rewritten as (11):

$$v_c = k_p e + k_d \dot{e} + \frac{\pi}{4} v_o \quad (11)$$

The transfer function between the output voltage and the adjusted output from the load voltage controller can be obtained from Fig.4 and expressed as (12):

$$G_{oc} = \frac{4}{\pi} \frac{1}{L_f C_f s^2 + 1} \quad (12)$$

The resulting closed-loop Lyapunov output voltage controller is shown in Fig.5. The Routh-Hurwitz stability criterion shows that if proportional and derivative gains  $k_p$  and  $k_d$  are both positive, the system is stable. Thus, by designing the damping ratio and natural frequency from the system characteristic equation, the required closed-loop performance can be achieved.

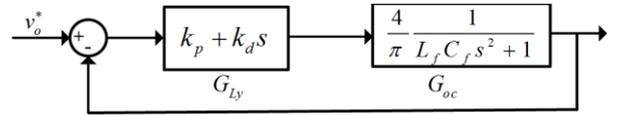


Fig. 5. Lyapunov closed-loop controller

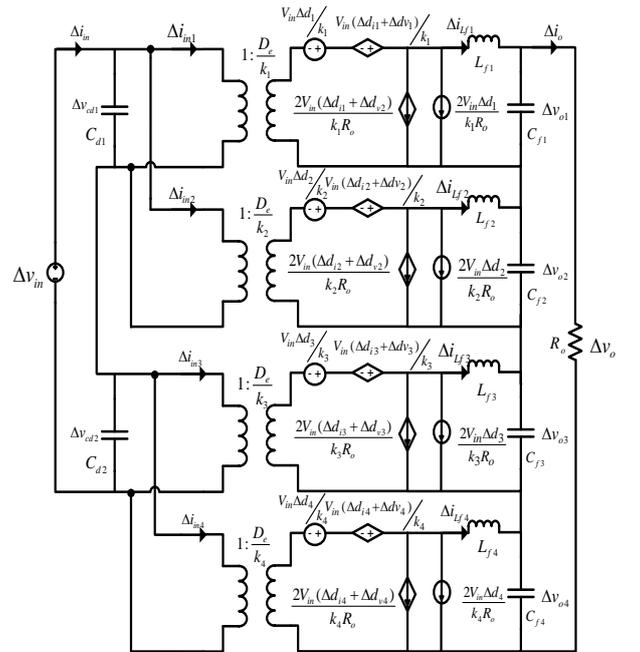


Fig. 6. ISIPOS converter small signal model

The small signal model of four ISIPOS connected DC/DC modules is shown in Fig.6 [7], where  $k_1, k_2, k_3, k_4$  are transformer turns ratios,  $L_r$  is the transformer leakage inductance,  $D_e$  is the effective duty ratio per module [7],  $L_{f1}, L_{f2}, L_{f3}, L_{f4}, C_{f1}, C_{f2}, C_{f3}$  and  $C_{f4}$  are filter inductances and capacitances for the four modules. Input voltage perturbation is represented by  $\Delta v_{in}$ , input voltage perturbation components for Modules 1 and 2, and for Modules 3 and 4 are  $\Delta v_{cd1}$  and  $\Delta v_{cd2}$  respectively, input current perturbations for the four modules are  $\Delta i_{in1}, \Delta i_{in2}, \Delta i_{in3}$  and  $\Delta i_{in4}$  respectively, and filter inductor current and capacitor voltage perturbations are represented by  $\Delta i_{lf1}, \Delta i_{lf2}, \Delta i_{lf3}, \Delta i_{lf4}$ , and  $\Delta v_{o1}, \Delta v_{o2}, \Delta v_{o3}$  and  $\Delta v_{o4}$  respectively.  $\Delta d_1, \Delta d_2, \Delta d_3$  and  $\Delta d_4$  are the duty ratio perturbations, and  $\Delta d_{v1}, \Delta d_{v2}, \Delta d_{v3}, \Delta d_{v4}, \Delta d_{i1}, \Delta d_{i2}, \Delta d_{i3}$ , and  $\Delta d_{i4}$  respectively represent perturbations of the duty ratio due to the input voltage and output current, and are defined in (13) [7].

$$\begin{cases} \Delta d_{v1} = \Delta d_{v2} = \frac{32L_r D_e f_s}{k^2 V_{in} R_o} \Delta v_{cd1} \\ \Delta d_{v3} = \Delta d_{v4} = \frac{32L_r D_e f_s}{k^2 V_{in} R_o} \Delta v_{cd2} \\ \Delta d_{ij} = -\frac{8L_r f_s}{k V_{in}} \Delta i_{lfj} \end{cases} \quad (13)$$

It is assumed that four modules have the same effective duty ratio, transformer turns ratios, and capacitor and inductor values. From Fig.6, equations (14-16) are obtained:

$$\begin{cases} \frac{D_e \Delta v_{cd1}}{k} + \frac{V_{in}}{2k} (\Delta d_1 + \Delta d_{v1} + \Delta d_{i1}) = sL_f \Delta i_{lf1} + \Delta v_{o1} \\ \frac{D_e \Delta v_{cd1}}{k} + \frac{V_{in}}{2k} (\Delta d_2 + \Delta d_{v2} + \Delta d_{i2}) = sL_f \Delta i_{lf2} + \Delta v_{o2} \\ \frac{D_e \Delta v_{cd2}}{k} + \frac{V_{in}}{2k} (\Delta d_3 + \Delta d_{v3} + \Delta d_{i3}) = sL_f \Delta i_{lf3} + \Delta v_{o3} \\ \frac{D_e \Delta v_{cd2}}{k} + \frac{V_{in}}{2k} (\Delta d_4 + \Delta d_{v4} + \Delta d_{i4}) = sL_f \Delta i_{lf4} + \Delta v_{o3} \end{cases} \quad (14)$$

$$\begin{cases} \Delta i_{lf1} = sC_f \Delta v_{o1} + \frac{\Delta v_o}{R_o} - \Delta i_o \\ \Delta i_{lf2} = sC_f \Delta v_{o2} + \frac{\Delta v_o}{R_o} - \Delta i_o \\ \Delta i_{lf3} = sC_f \Delta v_{o3} + \frac{\Delta v_o}{R_o} - \Delta i_o \\ \Delta i_{lf4} = sC_f \Delta v_{o4} + \frac{\Delta v_o}{R_o} - \Delta i_o \end{cases} \quad (15)$$

Considering the series pair Modules 1 and 3,

$$\begin{cases} \frac{k}{D_e} (\Delta i_{in} - sC_d \Delta v_{d1}) = \frac{2v_{in}}{kR_o} (\Delta d_1 + \Delta d_{v1} + \Delta d_{i1}) + \Delta i_{lf1} \\ \frac{k}{D_e} (\Delta i_{in} - sC_d \Delta v_{d3}) = \frac{2v_{in}}{kR_o} (\Delta d_3 + \Delta d_{v3} + \Delta d_{i3}) + \Delta i_{lf3} \end{cases} \quad (16)$$

Based on (16), neglecting duty ratio perturbations due to input voltage and output current, subtraction of the two equations leads to (17). Subtraction of the first and third equations of (14) leads to (18), and from (15) the modular voltage and current relationship can be obtained as (19):

$$\frac{k}{D_e} sC_d (\Delta v_{cd2} - \Delta v_{cd1}) = \frac{2v_{in}}{kR_o} (\Delta d_1 - \Delta d_3) + \Delta i_{lf1} - \Delta i_{lf3} \quad (17)$$

$$\frac{D_e}{k} (\Delta v_{cd2} - \Delta v_{cd1}) + \frac{V_{in}}{2k} (\Delta d_3 - \Delta d_1) = sL_f (\Delta i_{lf3} - \Delta i_{lf1}) + \Delta v_{o3} - \Delta v_{o1} \quad (18)$$

$$\begin{cases} \Delta v_{o1} = \frac{1}{sC_f} \left( \Delta i_{lf1} - \frac{\Delta v_{o1} + \Delta v_{o2} + \Delta v_{o3} + \Delta v_{o4}}{R_o} \right) \\ \Delta v_{o2} = \frac{1}{sC_f} \left( \Delta i_{lf2} - \frac{\Delta v_{o1} + \Delta v_{o2} + \Delta v_{o3} + \Delta v_{o4}}{R_o} \right) \\ \Delta v_{o3} = \frac{1}{sC_f} \left( \Delta i_{lf3} - \frac{\Delta v_{o1} + \Delta v_{o2} + \Delta v_{o3} + \Delta v_{o4}}{R_o} \right) \\ \Delta v_{o4} = \frac{1}{sC_f} \left( \Delta i_{lf4} - \frac{\Delta v_{o1} + \Delta v_{o2} + \Delta v_{o3} + \Delta v_{o4}}{R_o} \right) \end{cases} \quad (19)$$

Rearranging (19), the relationship between modular voltage output and inductor current can be represented as (20):

$$\begin{cases} \Delta v_{o1} = g_1 \Delta i_{lf1} - g_2 (\Delta i_{lf2} + \Delta i_{lf3} + \Delta i_{lf4}) \\ \Delta v_{o2} = g_1 \Delta i_{lf2} - g_2 (\Delta i_{lf1} + \Delta i_{lf3} + \Delta i_{lf4}) \\ \Delta v_{o3} = g_1 \Delta i_{lf3} - g_2 (\Delta i_{lf1} + \Delta i_{lf2} + \Delta i_{lf4}) \\ \Delta v_{o4} = g_1 \Delta i_{lf4} - g_2 (\Delta i_{lf1} + \Delta i_{lf2} + \Delta i_{lf3}) \end{cases} \quad (20)$$

where,

$$\begin{cases} g_1 = \frac{R_o + 3}{sC_f (R_o + 4)} \\ g_2 = \frac{1}{sC_f (R_o + 4)} \end{cases} \quad (21)$$

Substituting (21) into (18) yields (22):

$$\begin{aligned} \frac{D_e}{k} (\Delta v_{cd2} - \Delta v_{cd1}) + \frac{V_{in}}{2k} (\Delta d_3 - \Delta d_1) \\ = (sL_f + g_1 + g_2) (\Delta i_{lf3} - \Delta i_{lf1}) + \Delta v_{o3} - \Delta v_{o1} \end{aligned} \quad (22)$$

Substituting (22) into (21) yields (23):

$$\frac{\Delta v_{cd1} - \Delta v_{cd2}}{\Delta d_1 - \Delta d_3} = \frac{-\frac{2V_{in}}{kR_o} (g_2 + g_1 + sL_f) - \frac{V_{in}}{2k}}{\frac{D_e}{k} + sC_d \frac{k}{D_e} (g_1 + sL_f + g_2)} \quad (23)$$

which can be rewritten as (24):

$$\Delta v_{cd2} = \Delta v_{cd1} + A(s)(\Delta d_3 - \Delta d_1) \quad (24)$$

where,

$$A(s) = -\frac{\frac{2V_{in}}{kR_o}(g_2 + g_1 + sL_f) + \frac{V_{in}}{2k}}{\frac{D_e}{k} + sCd \frac{k}{D_e}(g_1 + sL_f + g_2)} \quad (25)$$

Assuming that  $\Delta v_{in}=0$ , and  $\Delta v_{cd1}=-\Delta v_{cd2}$ , the relationship between input capacitor voltage and duty ratio is obtained as (26):

$$\begin{bmatrix} \Delta v_{cd1} \\ \Delta v_{cd2} \end{bmatrix} = \begin{bmatrix} \frac{A(s)}{2} & -\frac{A(s)}{2} \\ -\frac{A(s)}{2} & \frac{A(s)}{2} \end{bmatrix} \begin{bmatrix} \Delta d_1 \\ \Delta d_3 \end{bmatrix} \quad (26)$$

The relationship between input current and duty ratio shown in (27) can be obtained by using a similar procedure.

$$\begin{bmatrix} \Delta i_{in1} \\ \Delta i_{in2} \end{bmatrix} = \begin{bmatrix} \frac{B(s)}{2} & -\frac{B(s)}{2} \\ -\frac{B(s)}{2} & \frac{B(s)}{2} \end{bmatrix} \begin{bmatrix} \Delta d_1 \\ \Delta d_2 \end{bmatrix} \quad (27)$$

$$\begin{bmatrix} \Delta i_{in3} \\ \Delta i_{in4} \end{bmatrix} = \begin{bmatrix} \frac{B(s)}{2} & -\frac{B(s)}{2} \\ -\frac{B(s)}{2} & \frac{B(s)}{2} \end{bmatrix} \begin{bmatrix} \Delta d_3 \\ \Delta d_4 \end{bmatrix}$$

where,

$$B(s) = D_e \left( \frac{2V_{in}}{R_o} + g_3 - g_4 \right)$$

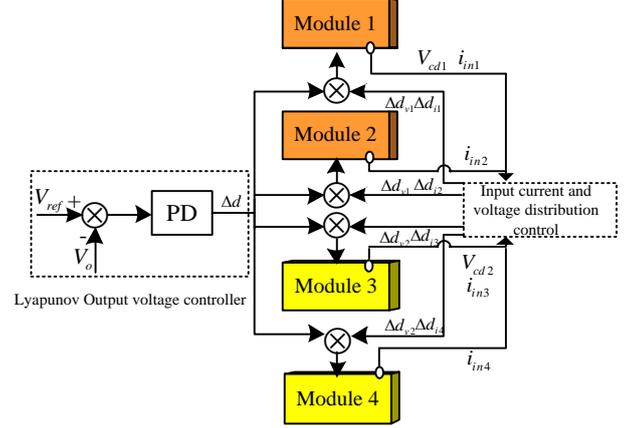
$$\begin{cases} g_3 = \frac{ac - 2bc}{(a+b)(a-3b)} \\ g_4 = \frac{bc}{(a+b)(a-3b)} \end{cases} \quad (28)$$

$$\begin{cases} a = sL_f + \frac{3 + R_o}{sC_f R_o + 4sC_f} + \frac{4L_r f_s}{k^2} \\ b = -\frac{1}{sC_f R_o + 4sC_f} \\ c = \frac{V_{in}}{2k} \end{cases}$$

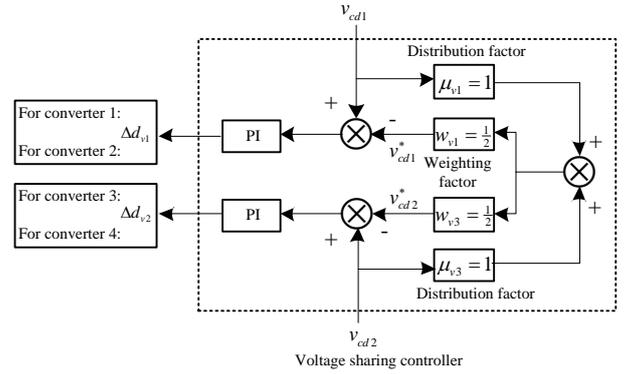
The input-series connection requires input voltage balanced while the input-parallel connection requires input current balance. Individual module input voltages and currents are sensed, and average sharing is used to produce correcting error signals to ensure input power sharing.

As shown in Fig.7, the proposed scheme consists of three loops to ensure input voltage and current sharing among the modules. The Lyapunov controller accordingly contributes the main duty ratio signal  $\Delta d$  to all modules, which is then

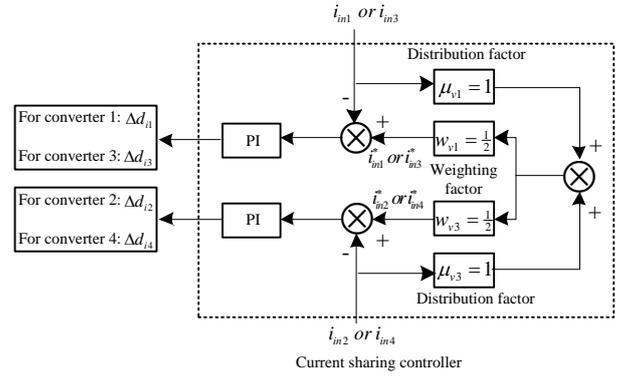
modified by the input current and voltage sharing loops. Average voltage sharing between the two series-connected modules is implemented by correcting the voltage difference signals to generate the duty cycle contributions  $\Delta d_{v1}$  and  $\Delta d_{v2}$  based on (26).



(a)



(b)



(c)

Fig. 7. Three-loop control for ISIPDS DC/DC converter (a) output voltage loop structure (b) voltage sharing controller (c) current sharing controller

The voltage reference signals for Modules 1 and 3 are generated using distribution factor  $\mu_{v1}$  and  $\mu_{v3}$ , and weighting functions  $W_{v1}$  and  $W_{v3}$ , as shown in Fig.7 (b). Average active sharing is used, therefore  $\mu_{v1}=\mu_{v3}=1$  and  $W_{v1}=W_{v3}=1/2$ .

Master-slave active sharing could also be used, but this is not discussed here. The voltage reference for Modules 1 and 3 is therefore given by (29):

$$v_{ref} = \frac{v_{cd1} + v_{cd2}}{2} \quad (29)$$

Alternatively, a fixed voltage reference of  $v_{in}/2$  could be used. The main advantages of using the dynamic input voltage reference in (29) rather than a fixed voltage reference are that it minimizes the interaction among the different control loops and results in better transient performance [1]. Referring to Fig.7, taking Module 1 as an example, the duty ratio contribution of the voltage sharing loop is:

$$\Delta d_{v1} = k_p(v_{cd1} - v_{cd1}^*) + k_i(v_{cd1} - v_{cd1}^*) \quad (30)$$

The current sharing loop corrects differences in input current between the parallel-connected modules, i.e. Modules 1 and 2, and Modules 3 and 4. Similar to the voltage sharing loop, dynamic current sharing is applied to generate the other duty ratio components  $\Delta d_{i1}$ ,  $\Delta d_{i2}$ ,  $\Delta d_{i3}$  and  $\Delta d_{i4}$  based on (27). Due to its discontinuity, high-cost current transducer is required to provide the high bandwidth. The duty ratios for each module are, therefore:

$$\begin{cases} d_1 = \Delta d + \Delta d_{v1} + \Delta d_{i1} \\ d_2 = \Delta d + \Delta d_{v1} + \Delta d_{i2} \\ d_3 = \Delta d + \Delta d_{v2} + \Delta d_{i3} \\ d_4 = \Delta d + \Delta d_{v2} + \Delta d_{i4} \end{cases} \quad (31)$$

#### IV. RESULTS

The proposed control strategy is assessed by considering the impact of mismatches among modules, and transient operating conditions in the ISIPPOS DC/DC converter. To assess the performance improvement offered when the converter is regulated using the proposed three-loop control scheme, simulation results are compared with those obtained from the widely used common duty-cycle control scheme shown in Fig.8 [14, 15].

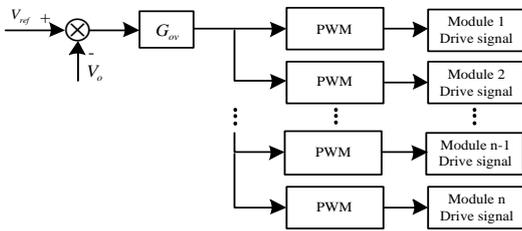


Fig. 8. Common duty-cycle control

The test system, shown in Fig.1, consists of an ISIPPOS DC/DC converter with rated output power of 1MW. Mismatched parameters, including input capacitance, transformer turns ratio, output inductance and capacitance, as specified in Table 1, are introduced to test the effectiveness of the power balancing function.

TABLE I. SIMULATION AND EXPERIMENTAL SYSTEM PARAMETERS

Parameter	Values	
	Simulation	Experiment
DC/DC Converter Rated Power	1MW	100W
Input DC Voltage	2200V	40V
Number of Modules	4	4
Input Capacitance	$C_{d1} = 50\mu\text{F}$ $C_{d2} = 80\mu\text{F}$	$C_{d1} = 40\mu\text{F}$ $C_{d2} = 10\mu\text{F}$
Transformer Turns Ratio	$T_1 = 1:6.8$ $T_2 = 1:6.4$ $T_3 = 1:6$ $T_4 = 1:6.4$	$T_1 = 1:1.4$ $T_2 = 1:1.2$ $T_3 = 1:1.3$ $T_4 = 1:1.2$
Output Inductance	$L_1 = 0.05\text{H}$ $L_2 = 0.06\text{H}$ $L_3 = 0.06\text{H}$ $L_4 = 0.05\text{H}$	$L_1 = 6.8\text{mH}$ $L_2 = 5.0\text{mH}$ $L_3 = 5.9\text{mH}$ $L_4 = 6.3\text{mH}$
Output Capacitance	$C_1 = 300\mu\text{F}$ $C_2 = 350\mu\text{F}$ $C_3 = 300\mu\text{F}$ $C_4 = 330\mu\text{F}$	$C_1 = 160\mu\text{F}$ $C_2 = 160\mu\text{F}$ $C_3 = 200\mu\text{F}$ $C_4 = 200\mu\text{F}$
PWM Carrier Frequency	2.5kHz	2.5kHz

For the simulation validation, the control schemes are tested by applying a step change in load voltage reference from 21.2kV to 22.5kV at  $t=0.2\text{ms}$  and back to 21.2kV at  $t=0.4\text{ms}$ , with system parameter mismatch conditions summarized in Table I. Fig.9 (a) shows the load voltage and individual module output voltages ( $v_{o1}$ ,  $v_{o2}$ ,  $v_{o3}$  and  $v_{o4}$ ) under the common duty-cycle control scheme, and Fig.9 (b) shows the performance of the proposed control scheme. The simulation results show that the performance of the common duty-cycle control strategy is significantly affected by the mismatches. With this control scheme the output voltages of all modules exhibit significant voltage ripple, with a worst-case peak voltage ripple value of approximately 14.7% of the average load voltage. Conversely, the proposed control scheme is able to compensate the mismatch, since the sharing loop enables adjustment of the duty ratio of each individual module so that each module can achieve the same output voltage. Output performances can be further improved by interleaving the modules' control systems. These results have demonstrated that with the proposed input power balancing control scheme is able to compensate for any negative influences of system parameters mismatch.

A scaled-down experimental rig of ISIPPOS with four modules is built to validate the proposed control scheme. Fig.11 shows the two output voltage being regulated at the desired reference value of 60V with common duty-cycle control and proposed control scheme respectively. It indicates that without the dedicated input voltage and current control, each module operates at different voltages  $V_{o1}=16.1\text{V}$ ,  $V_{o2}=16.9\text{V}$ ,  $V_{o3}=12.8\text{V}$  and  $V_{o4}=14.2\text{V}$ . By virtue of the proposed control loops, it compensates for the mismatch in the module transformer turns ratios and input capacitances by adjustment the phase shift angle of individual module in order to ensure that output voltages are equally shared, see Fig.11 (b). Fig.12 shows that the proposed control the system is able to ensure OVS during start-up transient and load changing transient.

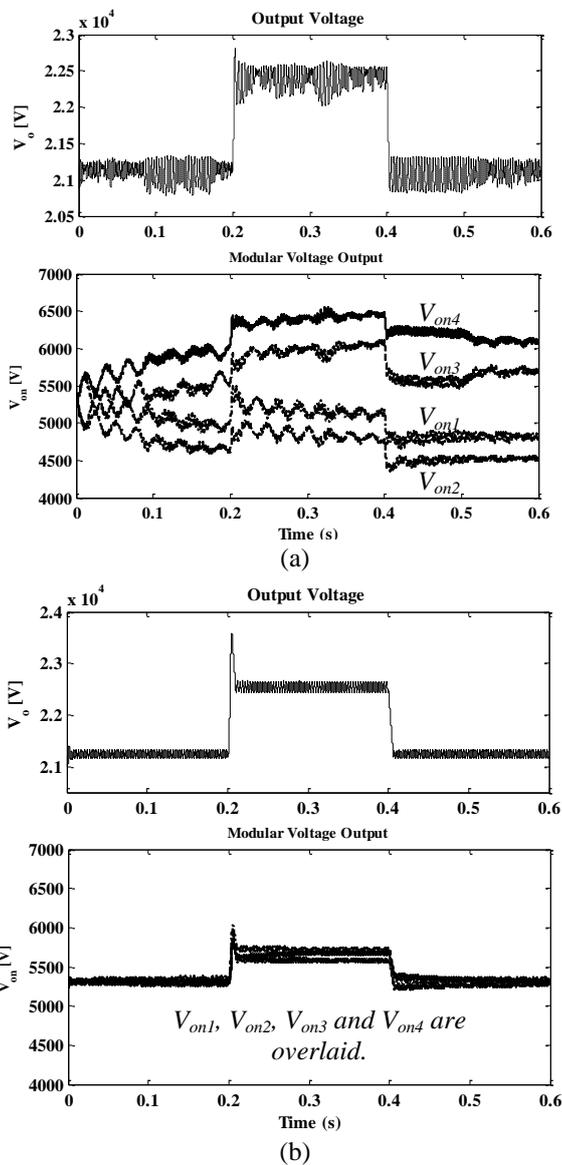


Fig. 9. Simulated response to a step change in load voltage, with mismatched parameters (a) common duty-cycle control (b) proposed control



Fig. 10. ISIPOS connected full-bridge DC/DC converter test rig

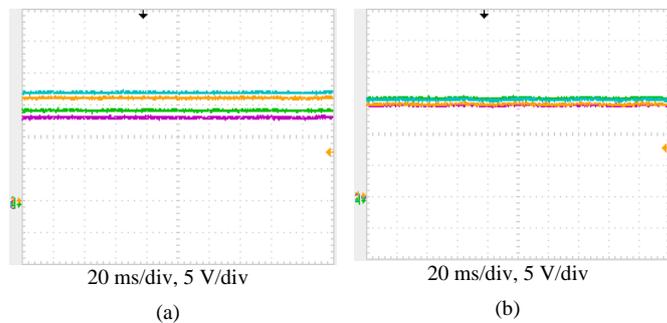


Fig. 11. Experiment result (a) with common duty-cycle control and (b) with proposed control

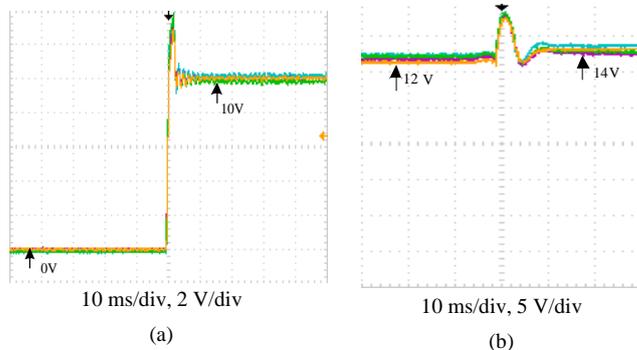


Fig. 12. Experiment result with proposed control (a) closed loop start-up transient and open loop load step-up transient

## V. CONCLUSIONS

A new modular DC/DC converter with ISIPOS connection is proposed with ability to further expand the benefits of parallel-series connection of low power rating modules. Primarily, an active input side control scheme for converter power sharing is addressed. For the load voltage control, the linearized control scheme offered by the Lyapunov control law reduces complexity and ensures improved transient response which is robust to load and input and parameter variations when compared to a linear control technique. The power sharing loops ensure input current sharing among the series connected modules, and input voltage sharing among the parallel connected modules. System-level simulation and scaled-down experimental validation are performed to verify the modeling and control schemes. It is verified that the proposed control, in ISIPOS DC/DC converter, is reliable for stable control and uniform sharing.

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