

Commuting effects in Okun's Law among British areas: evidence from spatial panel econometrics

JEL classification: R11, C31, J64

Key words: unemployment, output growth, commuting, spatial econometrics, panel data

1 Introduction

The linear, negative association linking real output growth to unemployment rate changes over the business cycle has been widely investigated since Arthur Okun's (1962; 1970) seminal work, which analyzed it using data for the U.S. in the years 1947-1960. The association in question, relating transitory movements in output and unemployment as measured by their year-on-year variations, is consistent with Okun's Difference Model, where first-differences represent the deviations of actual production and joblessness from their equilibrium trends. Another way of seeing the output-unemployment relationship, also studied by Okun (1962; 1970) and known as the Gap Model, is between the divergence of economic output from its potential or long-run level and the divergence of the joblessness rate from its non-inflationary or full-employment (NAIRU) level. The first-differences approach provides the base for the specification adopted in this paper.

Okun's finding of a 3:1 trade-off between economic growth and unemployment, often referred to as Okun's Law, has emerged as an

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empirical regularity predicting the magnitude of the reduction in unemployment from real GDP gains (or the costs in terms of higher unemployment of real GDP loss), and also how much demand stimulus is necessary to stabilise the joblessness rate. Specifically, the law envisages that for every 3% fall in output below its potential or long-term path the unemployment rate tends to rise by one percentage point (above its "natural", or NAIRU, level). This corresponds to a point estimate of around -0.3, i.e. a 1% fall in output from its trend yields an approximate 0.3 percentage point rise in the unemployment rate from its trend level. The less-than-proportionate increase in unemployment following an economic contraction, or equally the predicted slow employment response to an expansion in GDP, is due to labour market stickiness. Firms tend to invest considerably in company-specific human capital and certain skills are in limited supply, meaning that they have more to lose by dismissing workers when faced with temporary downturns than by utilising labour less intensely in the short term. Equally, during upturns, firms may prefer to raise output via productivity gains instead of taking on new workers, which can result in sluggish labour market adjustments to positive demand shocks. It should be noted that the relationship can be, and indeed has been, explored in either causal direction depending on the empirical problem or policy question at hand; this paper analyses the responsiveness of unemployment to GDP performance, in line with models of unemployment typical of labour market research (for a survey, see Elhorst 2003).

While several tests of Okun's Law exist which are based on cross-country evidence (Knoester 1984; Paldam 1987; Moosa 1997; Attfield and Silverstone 1997; Attfield and Silverstone 1998; Lee

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2000; Freeman 2001; Harris and Silverstone 2001; Crespo-Cuaresma 2003; Perman and Tavéra 2005; Moazzami and Dadgostar 2009), only recently have empirical studies started to estimate it using geographically disaggregated data. The regional Okun's Law literature, mainly concerned with the responsiveness of output volume growth to unemployment, points to the existence of noticeable interregional differences in the size of the coefficient. Christopoulos (2004), one of the main contributions, looks at thirteen Greek regions over the period 1971-1993; he reports slope values ranging from -0.37 to -1.70 in the areas where the empirical law holds, which tend to be areas with low long-term unemployment. Adanu (2005) investigates Okun's Law for ten Canadian provinces during the period 1981-2001; his parameters vary from -0.30 to -2.14, with more negative values seen in areas with larger concentrations of skilled workers. Using 1980-2004 data for seventeen Spanish regions, Villaverde and Maza (2007; 2009) obtain regional estimates in the range of -0.32 to -1.55, and show that the law is stronger in areas where productivity growth rates are lower. The consensus is therefore that the output gains/costs of lower/higher unemployment are larger in some regions and smaller or even negligible in others. Two exceptions are the earlier studies by Freeman (2000) and Apergis and Rezitis (2003) who, focussing on eight regional economies respectively in the U.S. for the years 1958 to 1998 and in Greece over a similar time span 1960-1997, do not find clear evidence of spatial variability in the magnitude of Okun's coefficients.

While looking at the problem from a regional perspective, this body of work ignores the importance of controlling for spatial interactions

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3 and spillovers, and the implications for the strength and validity of
4 Okun's relationship. To some extent, Kangasharju et al. (2012)
5 represents an exception; the authors deal with the problem of cross-
6 section dependence in their Okun's Law study of Finnish regions,
7 however they do not treat it as the central theme of their paper but
8 wash it out by taking output and unemployment series in deviation
9 from their time means. By contrast, in labour market research,
10 attempts have been made to rigorously apply a spatial
11 economic/econometrics perspective to wage curve studies (Buettner
12 1999; Longhi et al. 2006; Morrison et al. 2006; Elhorst et al. 2007),
13 and have led to the conclusion that spatial effects matter and improve
14 the explanatory power of the wage curve.

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17 The present paper addresses this gap in the Okun's Law literature by
18 exploring the question as to whether and to what extent there are
19 spatial mechanisms involved in Okun's Law dynamics. For this
20 purpose, we use data for the 128 NUTS3 regions of Great Britain
21 over the period 1985-2011. The paper is organized as follows:
22 Section 2 describes the model and data; Section 3 is concerned with
23 aspects of estimation; Section 4 provides a discussion of results and,
24 finally, Section 5 summarises and concludes.

26 27 28 29 30 31 32 33 34 35 36 37 38 39 40 41 42 43 44 45 46 **2 Model and data**

47 48 *2.1 Traditional Okun's Law specification*

49 Okun (1962; 1970) suggested two alternative forms of Okun's Law
50 relationship, namely a gap model and a first-differences model. The
51 former connects the deviation of actual output from its equilibrium or
52 potential level to the unemployment rate gap; it therefore needs
53 information about unemployment and output trends. Trend series are
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not directly observable, and there is no universal agreement on the optimal technique to estimate them, but any construction of these entails judgement. Moreover, the gap model should be preferred when the researcher is interested in inferences on time-series behaviour over the business cycle (Lee 2000). By contrast the latter, relating real output growth to unemployment rate changes, has the advantage of not relying on approximations of the size of the gap. Thus, as is common practice in applied Okun's Law studies, and because our aim is not to document estimates under different approaches to trend estimation as in purely econometric exercises, we adopt the first-differences method of Okun's Law analysis.

The short-run relationship between output and unemployment as in Okun's (1962; 1970) first-differences version (see also Knoester 1986) is given by the following expression

$$\Delta UN_{i,t} = \alpha + \beta \Delta GDP_{i,t} + e_{i,t}, \quad GDP = \log \text{output} \quad (1)$$

where $\Delta UN_{i,t}$ is the percentage point change in the local unemployment rate in region i at time t ($i=1, \dots, n$ with $n=128$ British NUTS3 areas, $t=1985, \dots, 2011$ so that $T=27$), as constructed from claimant counts and working-age population data published by the United Kingdom's Office for National Statistics; $GDP_{i,t}$ is expressed as the natural logarithm of output (not in absolute terms), so that $\Delta GDP_{i,t}$ is the percent real growth rate of local economic activity, using Gross Value Added in basic constant (2006) prices as economic volume measure; and $e_{i,t}$ is the error term, which in cross-sectional or panel-data (non-spatial) Okun's Law studies is commonly modelled as satisfying the **ordinary least squares**

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assumptions of homoscedasticity and lack of autocorrelation. With regards to the structural parameters, α is the intercept, β ($\beta < 0$) is Okun's Law coefficient capturing the extent of the contemporaneous labour market reaction to short-term GDP fluctuations (estimated in the range -0.30 to -0.50), and the ratio α/β indicates how fast economic activity has to grow in order to keep the unemployment rate stable. This basic regression equation can be augmented with other control variables which are commonly considered in the Okun's Law literature and justified on theoretical or empirical grounds.

In line with the dynamic version of Okun's Law (e.g. Chamberlin 2011), we start by adding $\Delta UN_{i,t-1}$ to the right-hand-side of Equation (1) in order to test whether current unemployment depends on its recent history. A significant influence of the unemployment rate in the preceding period would indicate the presence of rigidities and inertia in labour markets, causing delayed adjustments to workforce levels; it would also suggest the importance of path dependency and negative hysteresis (as discussed in Blanchard and Summers 1987; Cross 1993), thus reflecting persistent changes to the unemployment rate due to jobless workers permanently losing their skills or becoming inactive.

The extended specification, reflecting an unemployment-output relationship which is both contemporaneous and time-lagged, thus takes the form

$$\Delta UN_{i,t} = \alpha + \beta \Delta GDP_{i,t} + \gamma \Delta UN_{i,t-1} + e_{i,t} \quad (2)$$

As outlined in subsequent sections, our panel-data framework allows for unobserved or unmeasured region-specific time-invariant

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3 characteristics by means of fixed effects or of a composite error term
4 structure incorporating random effects. These fixed-effects or
5 random-effects vectors act as a catch-all for any causes of spatial
6 heterogeneity. They include differences across regions in the sectoral
7 composition of the local economic base, which can affect their
8 relative ability to absorb demand shocks. For instance, output from
9 the manufacturing and construction sectors is particularly sensitive to
10 cyclical fluctuations. Moreover, employment in these industries
11 consists in large part of temporary and contractual workers, who are
12 easier to lay off when demand falters. Another way industrial
13 structure can have supply-side effects on local unemployment is
14 through the effectiveness of the skills-jobs matching process, which
15 tends to be lower in regions specialized in agriculture and
16 manufacturing (Taylor and Bradley 1997; Elhorst 2003).

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18 It is worth mentioning that existing papers (Sögner and Stiassny
19 2002; Knotek 2007; Chamberlin 2011) have also shown a relevant
20 effect of real GDP growth in the previous year ($\Delta GDP_{i,t-1}$). The
21 time-lagged impact of demand shocks on the labour market can be
22 explained by the fact that hiring and firing workers depends on the
23 long-term state of the economy, since employers face costs in
24 changing the size of the workforce. Therefore uncertainty over the
25 extent and duration of output movements means the transmission
26 from output to unemployment is likely to occur gradually, as
27 businesses adjust their labour force while expectations are formed
28 about the true economic outlook.

2.2 Labour market interactions

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3 While the role of spatial effects in Okun's Law is largely unexplored,
4 the literature on regional unemployment disparities suggests that the
5 geography of and interaction among regional economies are
6 important drivers of labour market outcomes. One of the first
7 empirical papers to consider spatial variables in a model of
8 unemployment determination is Molho (1995), who looks at the
9 geographical distribution of the joblessness rate across labour market
10 areas within Great Britain in 1991. Starting from a standard
11 regression of local unemployment on current and time-lagged local
12 employment growth, he includes spatially lagged employment
13 variables measuring demand changes in surrounding areas. He finds
14 strong evidence of spillover effects from demand shocks both
15 contemporaneously and after a lag, the former reflecting interregional
16 trade links and the latter pointing to labour migration. The author
17 also tests for the impact of each area's unemployment rate on that in
18 neighbouring areas by incorporating the spatial lag of the dependent
19 variable. His results, indicating a significant presence of localised
20 spillovers, are consistent with the transmission mechanism
21 hypothesized by Burridge and Gordon (1981) and Taylor and
22 Bradley (1983). These authors propose a balancing identity which
23 relates regional unemployment changes to employment growth,
24 labour force participation, migration and commuting, demonstrating
25 the equilibrating effect of labour mobility on unemployment
26 differentials. Such outcome arises because, as workers move from
27 locations with spare capacity to locations with a surplus of demand
28 for labour, local unemployment rates shift towards a new long-run
29 steady state. A corollary to this is that labour market developments
30 are not confined to the local area but spill over to other areas as well,
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3 implying that regional unemployment will exhibit spatial
4 autocorrelation. For instance, in a slack labour market, employers
5 will find it less necessary to advertise vacancies outside their area
6 and fewer workers from nearby regions will look to this area for jobs;
7 thus, inward commuting flows will fall and labour market conditions
8 in contiguous areas will also tighten (see also Elhorst 2003). This
9 explains why a region's unemployment rate tends to be higher/lower
10 when surrounded by high-/low-unemployment regions.

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13 Niebuhr (2003) follows this strand of analysis, looking at a sample of
14 EU countries between 1986 and 2000. By means of spatial
15 econometric techniques, she uncovers a strong degree of spatial
16 linkages among regional labour markets in Europe. In particular, the
17 paper demonstrates that the evolution of a region's unemployment is
18 considerably influenced by labour market developments in
19 surrounding regions, which lends further support to the commuting
20 hypothesis of Burridge and Gordon (1981) and other authors. She
21 also tests for spatial dependence in the error term, and shows that
22 accounting for omitted spatial effects eliminates significant spatial
23 residual autocorrelation thus removing sources of misspecification.

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25 Building on this body of work, we introduce spatial effects in
26 Equation (2), the dynamic counterpart of the standard Okun's Law
27 relationship as given by Equation (1). Failure to account for labour
28 market interdependencies can have serious consequences for the
29 reliability of econometric results, as well as lead to an incorrect
30 representation and understanding of the true causal forces at work.
31 Specifically, neglecting spatial correlation in the variables of interest
32 would cause biased and possibly inconsistent coefficient estimates,
33 while leaving unobserved common factors (positive spatial
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correlation in the error term) unmodelled would lead to reduced standard errors, inflated t -ratios and incorrect inference (Le Sage and Pace 2009).

In the most complex of our specifications, spatial effects are in the form of spatial lags as well as spatially autoregressive error components, with regional heterogeneity modelled via random effects. In the spatial econometrics literature (e.g. Elhorst 2014), this is referred to as General Nesting Spatial (GNS) Model. The various spatial processes considered in this paper are summarized in the following regression equation; all of our estimated models are nested within this

$$\begin{aligned}\Delta UN_{i,t} &= \alpha + \rho \sum_{j=1}^N W_{ij} \Delta UN_{j,t} + \beta \Delta GDP_{i,t} + \\ &+ \theta \sum_{j=1}^N W_{ij} \Delta GDP_{j,t} + \delta \Delta GDP_{i,t-1} + \gamma \Delta UN_{i,t-1} + e_{i,t} \\ e_{i,t} &= \lambda \sum_{j=1}^N M_{ij} e_{j,t} + \xi_{i,t} \\ \xi_{i,t} &= \mu_i + v_{i,t}\end{aligned}\quad (3.a)$$

where the $n \times 1$ vector $e_{i,t}$ is the spatially dependent error term, and this is a function of $\xi_{i,t}$ which combines a (unobserved or unmeasured) time-invariant region-specific component $\mu_i \sim iid(0, \sigma_\mu^2)$ and a time-varying component $v_{i,t} \sim iid(0, \sigma_v^2)$, respectively a random-effects vector and a disturbances vector (Kapoor et al. 2007). Time dependency is introduced in the innovations $\xi_{i,t}$ by specifying the permanent error component μ_i together with the transient error component $v_{i,t}$ (Fingleton 2008).

Also, $\sigma_1^2 = \sigma_v^2 + T\sigma_\mu^2$.

The fixed-effects counterpart to Equation (3.a) can be formally expressed as

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$$\begin{aligned} \Delta UN_{i,t} &= \alpha + \rho \sum_{j=1}^N W_{ij} \Delta UN_{j,t} + \beta \Delta GDP_{i,t} + \\ &+ \theta \sum_{j=1}^N W_{ij} \Delta GDP_{j,t} + \delta \Delta GDP_{i,t-1} + \gamma \Delta UN_{i,t-1} + \mu_i + e_{i,t} \\ e_{i,t} &= \lambda \sum_{j=1}^N M_{ij} e_{j,t} + v_{i,t} \end{aligned} \quad (3.b)$$

2.3 Testing for spatial effects in Okun's variables

The aim of this section is to verify the existence of spatial correlation in the variables of interest – unemployment and Gross Value Added, both in levels (UN and GDP) and in first differences (ΔUN) or growth rates (ΔGDP) – using the Cross-section Dependence statistic for panel time series data due to Pesaran (2004)¹. It is worth noting that, as the test is applied to the model's variables, it does not require the assumptions regarding the panel model specification and error term structure which are necessary when the testing problem involves estimated residuals, thus its properties are reliable.

TABLE 1 AROUND HERE

Pesaran's (2004) Cross-section Dependence (CD) statistic is given by

$$CD = \sqrt{\left(\frac{2}{N(N-1)}\right)} \left(\sum_{i=1}^{N-1} \sum_{j=i+1}^N \sqrt{T_{ij}} \hat{\omega}_{ij}\right) \quad CD_{H_0: indep} \sim N(0,1)$$

which is based on an average of the pairwise correlation coefficients between all cross-sectional series ($\hat{\omega}_{ij}$), with T_{ij} being the joint sample for regions i and j for each correlation coefficient estimate. Results are illustrated in Table 1 and show that, for every variable,

¹ Another available testing device is the space-time Moran's I (STMI) statistic (Mitze 2012), a straightforward extension to a panel-data framework of the ordinary Moran coefficient for cross-sectional data (Anselin 2001). Results (unreported) from the STMI test are equivalent to those from the CD test and are available from the authors upon request.

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there is strong evidence against the null hypothesis of no cross-section dependence in the model's variables. The test statistics are significantly large, and the associated P -values are very small, which leads us to reject the null and conclude in favour of the presence of significant spatial correlation in the panel. These findings confirm the discussion in Section 2.2 which suggested the importance of controlling for interactions among labour markets.

2.4 Definition of Spatial Weight Matrices

The $n \times n$ (standardized) spatial weights matrix \mathbf{W} in Equation (3.a) takes the following form

$$\begin{aligned} W_{ij}^* &= \exp(-\hat{\tau}_i d_{ij}) \text{ for } i \neq j \\ W_{ij}^* &= 0 \quad \text{for } i = j \\ W_{ij}^* &= 0 \quad \text{for } d_{ij} > 100\text{km} \end{aligned} \quad (4)$$

$$W_{ij} = \frac{W_{ij}^*}{\sum_{j=1}^N W_{ij}^*}$$

Regarding the distance threshold of 100km, we have taken this value from existing and well-established studies in the empirical regional economics literature; for example, Fingleton (2003) uses a similar specification of the \mathbf{W} matrix (for Britain's local authority districts rather than NUTS3 areas) to explore the significance of increasing returns to labour productivity from employment density. Similarly, Lerbs and Oberst (2012) use a distance threshold of 90km in a four nearest neighbour inverse distance matrix.

In Equation (4), $\hat{\tau}_i$ is specific to each area and calibrated on commuting flows (as explained in Fingleton 2003, to which we refer for details), with travel-to-work data taken from the UK's 2001

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Census and converted from district to NUTS3 level, and d_{ij} denotes the straight-line distance between any two areas i and j .

The \mathbf{W} matrix is used to construct spatial lags $(\mathbf{I}_T \otimes \mathbf{W})\Delta UN$ and $(\mathbf{I}_T \otimes \mathbf{W})\Delta GDP$, which allow testing for the significance of spillover effects in labour-market and economic outcomes arising from workforce mobility and interregional proximity.

The $n \times n$ (standardized) spatial weights matrix \mathbf{M} for the error process is based on a canonical contiguity specification, given by

$$\begin{aligned} M_{ij}^* &= 1 \text{ if } i \text{ and } j \text{ share a border} \\ M_{ij}^* &= 0 \text{ otherwise} \end{aligned} \quad (5)$$

$$M_{ij} = \frac{M_{ij}^*}{\sum_{j=1}^N M_{ij}^*}$$

The use of different spatial weights matrices (\mathbf{W} for the model's variables and \mathbf{M} for the error process) is common practice in empirical spatial econometrics work, and is thoroughly motivated in a recent publication by Corrado and Fingleton (2012). With reference to the case at hand, the \mathbf{W} matrix is constructed on commuting data because the main aim of our study is to explore the existence and significance of spatial effects due to workers mobility (labour market linkages), and a commuting-based spatial weights matrix enables us to explicitly test this proposition. For the error term, a spatial structure is typically imposed in order to capture the transmission of shocks across regions as well as spatial correlation in unobserved/unmeasured causes of interregional heterogeneity (the fact that similar regions are typically close to each other); regarding \mathbf{M} , a contiguity-based spatial weights matrix is a standard choice in

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spatial econometrics, and our preference for this functional form conforms to such custom.

3 Methodology

3.1 Instrumentation strategy

It is important to observe that some of the regressors, namely ΔGDP and $(\mathbf{I}_T \otimes \mathbf{W})\Delta GDP$, may be jointly determined. The former may be affected by two-way causation involving ΔUN , an aspect that has been neglected in the relevant Okun's Law literature to date, since unemployment is likely to cause (as well as be caused by) variations in demand. Similarly, the construction of \mathbf{W} , which is based on commuting flows from the 2001 Census and thus postdates the dependent variable in some years, may introduce simultaneity bias and lead to inconsistent parameter estimates. We address these concerns using appropriate instruments to eliminate any correlation of Okun's variables with residuals, thus ensuring that estimation results are accurate and reliable.

One of the elements of originality in this paper is the use of instrumental variables (IV) to correctly identify ΔGDP and $(\mathbf{I}_T \otimes \mathbf{W})\Delta GDP$.

The instruments adopted here are widely accepted and well established. Our strategy follows the approach as discussed in Drukker, Egger and Prucha (2013), who build on the econometric theory developed in Kelejian and Prucha (1998, 1999, 2004, 2010).

As in Drukker, Egger and Prucha (2013), we define $\mathbf{X}_f = [\mathbf{X}; \mathbf{X}_e]$ as the set of included exogenous variables and excluded exogenous variables, respectively \mathbf{X} and \mathbf{X}_e . Here \mathbf{X}_f consists of $\Delta UN_{i,t-1}$

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and $\Delta GVA_{i,t-1}$, both of which are pre-determined - i.e. pre-date the dependent variable, being lagged by one year - and can thus be treated as exogenous, although this property will be explicitly tested using appropriate diagnostics.

The instruments are given by the linearly independent columns of

$$\mathbf{Z} = [\mathbf{X}_f; (\mathbf{I}_T \otimes \mathbf{W})\mathbf{X}_f; \dots; (\mathbf{I}_T \otimes \mathbf{W})^q \mathbf{X}_f; (\mathbf{I}_T \otimes \mathbf{M})\mathbf{X}_f; (\mathbf{I}_T \otimes \mathbf{W})(\mathbf{I}_T \otimes \mathbf{M})\mathbf{X}_f; \dots; (\mathbf{I}_T \otimes \mathbf{W})^q (\mathbf{I}_T \otimes \mathbf{M})\mathbf{X}_f].$$

The above-cited literature has highlighted that these instruments are a good approximation of the ideal instruments under reasonable assumptions; with regard to spatial lag order, $q=1$ is a common choice while a value of two also worked well in Monte Carlo experiments.

Thus, in its extended specification and standard formulation with $q=1$, our instruments set contains the linearly independent columns of

$$\begin{aligned} & [\mathbf{X}_f; (\mathbf{I}_T \otimes \mathbf{W})\mathbf{X}_f; (\mathbf{I}_T \otimes \mathbf{M})\mathbf{X}_f; (\mathbf{I}_T \otimes \mathbf{W})(\mathbf{I}_T \otimes \mathbf{M})\mathbf{X}_f] \\ \mathbf{X}_f &= [\Delta GDP_{i,t-1}; \Delta UN_{i,t-1}] \end{aligned} \quad (6)$$

At a minimum, in our case the instruments should be a sub-set of \mathbf{Z} containing the linearly independent columns of Equation (7) below (with spatial lags up to second order ($q=2$) as required to fulfil the rank condition for model over-identification)

$$\begin{aligned} & [\mathbf{X}_f; (\mathbf{I}_T \otimes \mathbf{W})\mathbf{X}_f; (\mathbf{I}_T \otimes \mathbf{W})^2 \mathbf{X}_f] \\ \mathbf{X}_f &= [\Delta GDP_{i,t-1}; \Delta UN_{i,t-1}] \end{aligned} \quad (7)$$

We provide results both for this minimal representation of the IV set and for the extended expression.

3.2 Fixed effects or random effects

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3 Panel data estimation necessitates the selection between fixed effects
4 and random effects. The relative merits of each method are
5 extensively discussed in the available literature (e.g. Arbia, Basile
6 and Piras 2005; Elhorst 2014), to which we refer for details. We
7 make this choice on the basis of results from both specifications,
8 taking into account theoretical coherence and empirical robustness,
9 but our decision is also informed by the appropriate statistical
10 devices which are available for this purpose; for instance, the
11 Hausman statistics for random-effects consistency is normally used
12 to this end, and the Sargan-Hansen instruments exogeneity test can
13 help detecting misspecification and distinguishing between models.
14 Therefore, while acknowledging the advantage of consistency for
15 fixed effects, we look for evidence in the data as to whether this is
16 also the case for random effects, and whether a random-effects model
17 actually outperforms a fixed-effects model in this application.
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33 It is worth discussing the adequacy of random effects when the
34 spatial units cover the whole population, as in the case at hand; it
35 should be noted that while our dataset does not comprise a sample it
36 is possible to consider the data to be one of many realisations from a
37 super-population, since the spatial partitions giving the areal units are
38 just one of an infinite number of possible sets that could have
39 occurred (see also Fingleton 2010, p. 5, note 12) - in other words, the
40 spatial units within the study area are such that inference about the
41 population is not conditional on the observed units, even if these
42 cover the whole population.
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55 **3.3 Estimation**

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3 All of our estimates are derived from an instrumental-variables
4 approach to satisfy orthogonality conditions and to achieve
5 consistency, in contrast to existing spatial panel evidence on Okun's
6 Law which is based on Maximum Likelihood and thus obtained
7 under the assumption that all variables are exogenous.
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10 Precisely, we carry out Two-Stage Least Squares (2SLS) estimation
11 of Spatial Durbin Models (without spatially autoregressive errors)
12 and Feasible Generalised Spatial Two-Stage Least
13 Squares/Generalised Method of Moments (FGS2SLS/GMM)
14 estimation of General Nesting Spatial Models (as defined in
15 Equations (3.a) and (3.b)).
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17 The 2SLS technique is well known. With regard to the
18 FGS2SLS/GMM procedure, the main difference between the present
19 model and that of Kapoor et al. (2007) is that we include endogenous
20 regressors other than the spatial lag of the dependent variable,
21 namely ΔGDP and $(\mathbf{I}_T \otimes \mathbf{W})\Delta GDP$, following Fingleton (2008).
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23 The methodology for estimating a random effects panel model with
24 an endogenous spatial lag, additional endogenous regressors and
25 spatially autoregressive error components is described in detail in the
26 cited references, so we do not include technical specifics here.
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28 To summarize, however, the estimation procedure has three stages. In
29 the first step, the model is estimated via Two-Stage Least Squares
30 (2SLS) to obtain consistent residuals. In the second step, these
31 residuals are used to estimate, via GMM, the model parameters
32 relating to the error term, namely the spatially autoregressive error
33 process parameter λ and the error components variances σ_μ^2 and
34 σ_ν^2 . Finally, given these, we find estimates of the spatial
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3 autoregressive parameter ρ and of the regression coefficients;
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5 precisely, the $\hat{\lambda}$ estimate allows the variables to be purged of spatial
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7 dependence by means of a Cochrane–Orcutt transformation, with
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9 inference in the third stage based on a robust approach for IV
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11 estimation with non-spherical disturbances (Bowden and Turkington
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13 1984; Greene 2003).
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3.4 Measurement of direct, spillover and total impacts

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18 Le Sage and Pace (2009) point out that, when the spatial lags of the
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20 regressand and regressor are present in a model, the true total effect
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22 on a dependent variable, here ΔUN , of a unit change in an
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24 explanatory variable, here ΔGDP , (i.e. the true partial derivative
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26 $\partial \Delta UN / \partial \Delta GDP$) is not the same as the estimated regression
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28 coefficient $\hat{\beta}$; it also captures spatial linkages and simultaneous
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30 feedbacks passing through the dependence system, thus leading to a
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32 total effect which typically differs from $\hat{\beta}$ and which can be
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34 separated into a direct (own-region) effect and an indirect (spatial,
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36 spillover) effect.
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41 Equation (3.a), which has both $(\mathbf{I}_T \otimes \mathbf{W})\Delta UN$ and
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43 $(\mathbf{I}_T \otimes \mathbf{W})\Delta GDP$ as determinants of ΔUN (plus spatially
44
45 autoregressive error components), accommodates regional
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47 interdependencies up and down the spatial network, thus expanding
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49 the information set for the i th region to include observations on the
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51 dependent and explanatory variables in other regions. The
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53 implication of including these spatial lags is that a unit change in
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55 $\Delta GDP_{i,t}$ within a given area i will directly affect $\Delta UN_{i,t}$ in area i
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Spatial effects in Okun's Law among British areas

itself, but will also have an indirect effect on $\Delta UN_{i,t}$ in all other areas which eventually impacts back to i . This is different from non-spatial linear regressions (based on the assumption of independence among cross-sectional units), where $\partial \Delta UN_{i,t} / \partial \Delta GDP_{i,t} = \beta$ for all i while $\partial \Delta UN_{i,t} / \partial \Delta GDP_{j,t} = 0$ for $i \neq j$.

The proper interpretation of the marginal effects of ΔGDP is derived from rearranging the following model, which is identical to Equation (3.a) but expressed in terms of individual cross-sections, and assuming $|\rho| < 1$

$$\Delta UN_t = \alpha + \rho \mathbf{W} \Delta UN_t + \beta \Delta GDP_t + \theta \mathbf{W} \Delta GDP_t + \delta \Delta GDP_{t-1} + \gamma \Delta UN_{t-1} + e_t \quad (8)$$

$$\Delta UN_t = (\mathbf{I}_n - \rho \mathbf{W})^{-1} \alpha + (\mathbf{I}_n - \rho \mathbf{W})^{-1} (\beta \Delta GDP_t + \theta \mathbf{W} \Delta GDP_t) + (\mathbf{I}_n - \rho \mathbf{W})^{-1} \delta \Delta GDP_{t-1} + (\mathbf{I}_n - \rho \mathbf{W})^{-1} \gamma \Delta UN_{t-1} + (\mathbf{I}_n - \rho \mathbf{W})^{-1} e_t$$

where \mathbf{I}_n is an $n \times n$ identity matrix and the Leontief Expansion

$(\mathbf{I}_n - \rho \mathbf{W})^{-1}$ is equal to

$$(\mathbf{I}_n - \rho \mathbf{W})^{-1} = \mathbf{I}_n + \rho \mathbf{W} + \rho^2 \mathbf{W}^2 + \rho^3 \mathbf{W}^3 + \dots \quad (9)$$

It follows that, in a given year t , the $n \times n$ matrix of partial derivatives of ΔUN in all regions (ΔUN_i for $i=1, \dots, n$) with respect to ΔGDP in all regions (ΔGDP_i for $i=1, \dots, n$) varies over i and is

$$\begin{bmatrix} \frac{\partial \Delta UN_1}{\partial \Delta GDP_1} & \dots & \frac{\partial \Delta UN_1}{\partial \Delta GDP_n} \\ \vdots & \ddots & \vdots \\ \frac{\partial \Delta UN_n}{\partial \Delta GDP_1} & \dots & \frac{\partial \Delta UN_n}{\partial \Delta GDP_n} \end{bmatrix} = (\mathbf{I}_n - \rho \mathbf{W})^{-1} \begin{bmatrix} \beta_k & w_{12} \theta_k & \dots & w_{1n} \theta_k \\ w_{21} \theta_k & \beta_k & \dots & w_{2n} \theta_k \\ \vdots & \vdots & \beta_k & \vdots \\ w_{n1} \theta_k & w_{n2} \theta_k & \dots & \beta_k \end{bmatrix}$$

This matrix can be denoted by

$\mathbf{S} = \partial \Delta UN / \partial \Delta GDP = (\mathbf{I}_n - \rho \mathbf{W})^{-1} \mathbf{C}$. Therefore, the *average total*

effect on ΔUN of a unit change in ΔGDP can be summarized by

Spatial effects in Okun's Law among British areas

computing the row (or column) sum of partial derivatives contained in matrix \mathbf{S} and then averaging over the n regions, as in

$$n^{-1} \sum_{ij} \frac{\partial \Delta UN_i}{\partial \Delta GDP_j} = n^{-1} \mathbf{1}' [(\mathbf{I}_n - \rho \mathbf{W})^{-1} \mathbf{C}] \mathbf{1} \quad (10)$$

This average total effect can be partitioned into a direct component and an indirect component. The *average direct effect* is a scalar summary of the own-partial derivatives, each of these measuring the impact of a unit change in region i 's ΔGDP on region i 's ΔUN . It is calculated as the average of the elements on the main diagonal of the \mathbf{S} matrix, as in

$$n^{-1} \sum_j \frac{\partial \Delta UN_j}{\partial \Delta GDP_j} = n^{-1} \text{trace} [(\mathbf{I}_n - \rho \mathbf{W})^{-1} \mathbf{I}_n \beta] \quad (11)$$

The *average indirect effect* is a scalar summary that corresponds to the cross-partial derivatives, each of these representing the response of region i 's ΔUN to a unit change in ΔGDP in all other regions. It is equal to the difference between the average total effect and the average direct effect, and is computed as the average of either the row sums or the column sums of the off-diagonal elements of \mathbf{S} . Results on the true Okun's Law coefficient, as obtained from the implementation of Le Sage and Pace's (2009) method, are presented in Section 4.2.

4 Estimation results

4.1 Initial estimates

This section presents results from our panel data analysis of Okun's Law for the 128 NUTS3 regions of Great Britain. Outcomes from various modelling solutions are provided in order to document biases

Spatial effects in Okun's Law among British areas

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3 due to model misspecification and to the omission of spatial patterns
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5 in space-time unemployment rate variations.
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TABLE 2 AROUND HERE

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12 We start with fixed-effects (FE) and random-effects (RE) IV
13 estimates from panel models with spatial lags of the dependent and
14 independent variables but without interactions among errors, namely
15 Spatial Durbin Models. **Table 2** illustrates initial estimates from
16 baseline regressions, using an instruments set in its minimal
17 specification (Equation (6)). **Model 1** and **Model 2** are the closest
18 approximations to a dynamic Okun's Law relationship with spatial
19 effects, where joblessness rate changes are explained by time-lagged
20 (local) unemployment rate changes, real GDP growth both locally
21 and within commuting distance, and spatially-lagged
22 (contemporaneous) unemployment rate changes. The $\hat{\beta}$ coefficient
23 of -0.05 (FE model) or -0.06 (RE model) is lower in absolute terms
24 than Okun's value of -0.32, or than point estimates found elsewhere
25 e.g. ranging from -0.17 to -0.24 in Crespo-Cuaresma (2003).
26 Particularly, it is smaller than shown for the UK by studies which
27 have investigated Okun's Law over various time periods using
28 national data². Nonetheless, with a *t*-ratio of -2.58 (FE model) or -
29 2.46 (RE model), Okun's coefficient is highly significant, supporting
30 the existence of a negative association between economic growth and
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54 ² For example, -0.34 in Knoester (1986), -0.36 in Paldam (1987), -
55 0.38 in Moosa (1997), -0.69 in Attfield and Silverstone (1998), -0.77 in
56 Freeman (2001) (see also Lee 2000). For comparability with our result,
57 these are the reciprocals of coefficients obtained from models with
58 unemployment as right-hand-side variable.
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Spatial effects in Okun's Law among British areas

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3 unemployment among the British regions. Previous studies of
4 regional data, for instance Kangasharju et al. (2012), also found a
5 smaller $\hat{\beta}$ coefficient than typically estimated from macro time-
6 series data, and related this result to workers mobility and spatial
7 linkages being more important across regions than across countries.
8
9 The incorporation of spatial effects in the form of spatial lags of the
10 dependent variable, $(\mathbf{I}_T \otimes \mathbf{W})\Delta UN$, and of the explanatory
11 variable, $(\mathbf{I}_T \otimes \mathbf{W})\Delta GDP$, allows to explicitly test this hypothesis;
12 given the definition of \mathbf{W} , the strength of spillovers between any
13 two areas is inversely related to geographical distance and directly
14 proportional to the intensity of the commuting links between them.
15 We find a statistically significant and negatively signed between-area
16 impact of real output changes on ΔUN , with the parameter on
17 $(\mathbf{I}_T \otimes \mathbf{W})\Delta GDP$ equal to -0.07 in both models and with an
18 associated t -ratio of -2.33 (FE model) or -1.98 (RE model). This
19 validates the prediction that economic growth effects on ΔUN are
20 also due to real GDP performance in adjacent areas within
21 commuting distance, rather than confined to the local area; therefore,
22 Okun's Law papers should not focus only on the labour market
23 responsiveness to output volume growth in a given location, but
24 attention should be paid to how localised demand policies might
25 influence workforce mobility and have employment effects outside
26 administrative borders. Also for $(\mathbf{I}_T \otimes \mathbf{W})\Delta UN$, we find highly
27 significant (direct) effects from nearby commuting areas, which
28 corroborates the existence of interregional labour market linkages.
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Spatial effects in Okun's Law among British areas

Moreover we see strong relevance of the one-year lag of the dependent variable; in particular, the negative sign of the $\hat{\gamma}$ coefficient provides evidence of delayed adjustments to workforce levels and suggests the presence of negative hysteretic effects. Higher-order time lags are either insignificant or wrongly signed (compared to theoretical expectations as outlined in Section 2.1), or both, and eliminating these does not modify our regression coefficient estimates, which implies that dynamic effects only accrue to the first period³.

We next turn to the diagnostics. For the fixed-effects model (Model 1), the overidentifying restrictions test gives a Hansen-Sargan test statistic equal to 4.75, which when referred to the relevant χ^2_2 distribution has an exceedence probability of 0.09; this P -value is large enough to allow non-rejection of the null that instruments are exogenous, although only at the 1% level. With regard to Model 2, the Hansen-Sargan test statistic is 2.93, with an associated P -value of 0.23, which indicates that orthogonality conditions hold strongly for the random-effects model. Also, in both cases, the joint F statistics from the first-stage regressions of 2SLS estimation are 19.71 for ΔGDP and 41.47 for $(\mathbf{I}_T \otimes \mathbf{W})\Delta GDP$, all of which are extreme observations in the reference $F_{6,3449}$ distribution, which demonstrates that we do not have weak instruments.

Moreover, the Hausman test of regressors endogeneity causes us to reject the null that ΔGDP and $(\mathbf{I}_T \otimes \mathbf{W})\Delta GDP$ are correlated to

³ Results with higher-order time lags are not reported in the paper but are available from the authors upon request.

Spatial effects in Okun's Law among British areas

residuals, however it is worth noting that later estimations will actually produce test results which are in favour of this hypothesis.

Finally, we implement the Hausman consistency test which is a useful statistical tool to assess whether the difference in coefficients between the consistent fixed-effects model and the relatively more efficient random-effects model is significant; it uses the test statistic $\hat{H} = (\hat{\beta}_{RE} - \hat{\beta}_{FE})'(\hat{\Sigma}_{RE} - \hat{\Sigma}_{FE})^{-1}(\hat{\beta}_{RE} - \hat{\beta}_{FE})$, where the $\hat{\beta}_s$ are the vectors of estimates from Model 1 and Model 2 and the $\hat{\Sigma}_s$ are the respective covariance matrices. We find that \hat{H} is not an extreme value with reference to the relevant χ^2 distribution under the null, as the test statistic is equal to 10.35 which has a P -value of 0.0350; this implies that, at a conventional (though more liberal) 1% level, we cannot reject the null that random effects are uncorrelated to the explanatory variables – in other words, statistical evidence is not enough to completely dismiss the estimates from Model 2.

At this point in our analysis it seems that the fixed-effects model fits the data well and gives plausible results, but the random-effects model cannot be discarded because it produces equally satisfactory outcomes. Diagnostic evidence also suggests that the random-effects model should be retained: the Hausman FE vs. RE test indicates that random-effects estimates are consistent, as well as efficient; in addition, the Sargan-Hansen test shows that the instruments orthogonality conditions are strongly satisfied when random effects are used but notably less so under fixed effects, a possible consequence of some misspecification in the latter case. In order to shed further light on which model should be the preferred one, we next carry out robustness checks on our initial regressions.

Spatial effects in Okun's Law among British areas

TABLE 3a AROUND HERE

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Model 3a and **Model 4a** in **Table 3a** are obtained by applying an extended instruments set (Equation (7)). Looking across Table 3, it is apparent that the evidence points to the superiority of a random-effects model. Results from the fixed-effects model (Model 3a) become somewhat worse, with the $\hat{\theta}$ coefficient unexpectedly turning insignificant, while results from the random-effects model (Model 4a) remain statistically relevant. It should be noted that the Hausman regressors endogeneity test now confirms that the instrumented variables are not orthogonal to the error term, thus justifying the use of 2SLS estimation to guarantee consistency. Meanwhile, the first-stage F statistic still leads us to conclude that instruments are relevant (i.e. jointly significant in identifying our endogenous regressors). With regard to the Hansen-Sargan overidentifying restrictions test, in both cases the test statistic is sufficiently small to infer that instruments are exogenous but, with the P -value just exceeding the 1% rate, hints at potential issues with these regressions. For the sensitivity checks in Table 3b, we thus use the minimal IV set, which proved to be valid according to diagnostics in Table 2, and we verify the robustness of estimates to the inclusion of dummy variables for the 1991-92 and 2008-09 recessions (similarly to Oberst and Oelgemöller, 2013).

TABLE 3b AROUND HERE

Spatial effects in Okun's Law among British areas

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3 From a comparison of **Model 3b** and **Model 4b** in **Table 3b** it
4 emerges that results from a random-effects specification (Model 4b)
5 are statistically relevant and economically meaningful while, in the
6 fixed-effects specification (Model 3b), the real GDP growth rate and
7 its spatial lag are both statistically insignificant and well below
8 theoretical expectations with regard to coefficient sizes. Importantly,
9 the Sargan-Hansen test fails under fixed effects, suggesting
10 instruments invalidity or other causes of model misspecification,
11 whereas the overidentifying restrictions clearly hold in the context of
12 IV estimation with random effects. The Hausman consistency test
13 now gives a test statistic of 6.09, with a P -value of 0.73 which is well
14 above a 10% significance level, strongly suggesting that random
15 effects are uncorrelated to the explanatory variables.
16
17 All in all, estimation results from baseline and additional regressions
18 support the adoption of a random-effects model, with a minimal form
19 of the IV set fully satisfying the validity requirements (and
20 noticeably outperforming its extended form on the basis of results
21 from the Hansen-Sargan test). We thus select random effects because
22 these worked well over various estimations, offering theoretically
23 coherent and empirically solid outcomes, in contrast to fixed-effects
24 evidence which proved less systematic and less acceptable than one
25 would anticipate; available statistical tests such as the Hausman
26 consistency test also support this decision. The final aspect in our
27 spatial analysis is concerned with further developing our econometric
28 model by allowing for spatially autoregressive (SAR) error
29 components in a random-effects specification, estimated via
30 FGS2SLS/GMM.
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Spatial effects in Okun's Law among British areas

TABLE 4 AROUND HERE

In **Table 4 (Model 5 and Model 6)**, Okun's coefficient remains negative and significant, confirming the inverse response of unemployment rate changes to real output growth, and there is a statistically relevant estimate for the spatial autoregressive parameter λ , which indicates significant 'nuisance' spatial dependence due to shock spillovers and omitted (positively) spatially autocorrelated explanatory variables.

Importantly, the inclusion of spatial dependence in the error term appears to improve the estimates. To begin with, results are more in line with expectations as the regression coefficient of own region's output growth is now lower, in absolute terms, than that of output growth in other regions within commuting distance; the theoretical argument for this is the presence of regional dependence in labour markets from *systematic/substantive linkages*, here taking the form of commuting flows which cause labour-market outcomes in one place to depend partly on labour-market or business conditions elsewhere, and *non-systematic linkages* which arise from inappropriate geographical delineation (non-systematic linkages mean that available spatial units, i.e. formal areas, virtually never coincide with functional labour market areas, in other words output growth within commuting distance is a better approximation of the true extent of economic activity).

Additionally, compared to the counterpart model without SAR errors (Model 4b), we find that ΔGDP and $(\mathbf{I}_T \otimes \mathbf{W})\Delta GDP$ become more strongly significant as t -ratios are higher; the likely reason is

Spatial effects in Okun's Law among British areas

that the fit of the model is better when SAR errors are a component of the equation and thus standard errors are smaller. For $(\mathbf{I}_T \otimes \mathbf{W})\Delta UN$, we see that the absolute value of coefficient $\hat{\rho}$ is now lower, possibly because if \mathbf{M} -based interactions should be in the model and they are not then one will have omitted-variables bias in the parameter estimates and this may be distorting $\hat{\rho}$.

Models 5 and 6 give almost identical outcomes; however, since Model 5 has a slightly better fit, we take this as our final preferred specification. In the next section we use Model 5 as the point of departure to give a comprehensive and precise account of the validity and strength of Okun's Law, by capturing spatial effects in their full extent.

4.2 True Okun's Law coefficient: direct, spillover and total impacts

TABLE 5 AROUND HERE

Table 5 displays the true marginal effects relating to ΔGDP , i.e. the average total impact, and their average direct and indirect components. It should be noted that the direct and indirect effects associated with ΔGDP are different from the values of, respectively, $\hat{\beta}$ and $\hat{\theta}$ obtained from Model 5 because they incorporate feedback loop effects, as implied by the Leontief Expansion in Equation (9); these arise because any given area is considered a neighbour to its neighbour, so that the spatial transmission mechanism is such that shocks to the system propagate

Spatial effects in Okun's Law among British areas

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3 across neighbouring areas and eventually come back to the area they
4 originated from.

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7 The substantive result that emerges from this analysis is that our true
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9 Okun's Law coefficient amounts to -0.2798, which in absolute terms
10 is very close to the 'empirical law', and this is primarily attributable
11 to indirect effects. This means that, while the average direct impact
12 coefficient of -0.0756 in Table 5 is statistically significant, what
13 really counts for local labour market performance is real GDP growth
14 in nearby areas within commuting distance, with a large part of the
15 actual marginal effect of ΔGDP on ΔUN being due to spatial
16 spillovers from workforce mobility and geographical proximity –
17 around 73%.

18
19 Our conclusions regarding the validity and strength of Okun's Law
20 for the British regions, based on the average total impact coefficient
21 of -0.2798, are more in accord with existing evidence, as opposed to
22 inference drawn from estimated regression coefficients $\hat{\beta} = -0.0609$
23 and $\hat{\theta} = -0.1119$ given by Model 5 (interpreted individually and
24 without considering feedback loops). Spatial effects thus matter, and
25 are responsible for the seemingly low impact of economic growth on
26 unemployment which is apparent from Model 5.

27
28 For an explanation of why the regression coefficient of own region's
29 output growth is lower in absolute terms than that of output growth in
30 other regions within commuting distance, we refer the reader to the
31 discussion of results from Table 4 in the previous sub-section.
32
33 Moreover, our result is not exceptional, as authors who have
34 undertaken similar analyses of direct, spillover and total effects have
35 reached analogous conclusions. Lerbs and Oberst (2012) investigate
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Spatial effects in Okun's Law among British areas

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3 the influence of house prices on homeownership rates among
4 German regions and see a total effect of -5.3 percentage points, of
5 which only -1.7 points are due to own-region variations while -3.6
6 points correspond to the average cumulative indirect effect (68% of
7 the overall impact). In a regional Okun's Law context, Oberst and
8 Oelgemöller (2013) find that the magnitude of the total growth effect
9 can be attributed to output variations in neighbouring areas for a
10 proportion of almost 60%. In both cases, results are robust to
11 alternative weighting matrices – namely a contiguity matrix and a
12 four nearest neighbour inverse distance matrix with no distance
13 threshold or with a threshold of 90km. While this evidence may be
14 less striking than our estimate of 73%, it indicates a prominent role of
15 interregional linkages, with spatial effects accounting for more than
16 half of the total effect in both papers.

17
18 In order to show the robustness of results to specifications of \mathbf{W} , we
19 vary the distance threshold, which is a discretionary parameter
20 though motivated by existing literature as explained in Section 2.4.
21 Results in Table 5 show that threshold values of 100km, 150km and
22 50km give broadly the same estimates of direct, indirect and total
23 effects, which demonstrates that outcomes are robust to the use of
24 different forms of the commuting-based \mathbf{W} matrix; obviously, with a
25 threshold of 50km, the spatial weight matrix is relatively more sparse
26 (more of its elements are zero), so spillover and total effects become
27 somewhat less significant.

54 **5 Conclusions**

55
56 This paper has been the first to analyze Okun's Law using a spatial
57 panel approach on NUTS3 data for Great Britain. The relationship,
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Spatial effects in Okun's Law among British areas

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3 expressing unemployment rate changes as an inverse function of real
4 GDP growth as in Okun's seminal work, is adapted to properly
5 control for regional heterogeneity, spatial spillovers between
6 neighbouring areas within commuting distance involving both
7 variables, and cross-section dependence in error components. We
8 find that the predicted negative relationship is corroborated by our
9 data, and that the statistical significance of output volume growth is
10 maintained under different model specifications and estimation
11 methods, which demonstrates the robustness of our results.

12
13 The main conclusion we reach from estimating Okun's Law in a
14 regional context is that the regression coefficient is lower than
15 previously shown by cross-country evidence, and this is largely
16 attributable to the spatial mechanisms which are at work in a small-
17 distance, small-area scenario. Firstly, the inclusion of the spatial lags
18 to absorb interactions and linkages reveals that commuting and other
19 spatial effects (as embodied in the \mathbf{W} and \mathbf{M} matrices, respectively)
20 are relevant to a proper understanding of Okun's Law dynamics.
21 Moreover, although Model 5 provided us with a satisfactory set of
22 outcomes, our final preferred estimate (-0.28) is one which is
23 obtained from taking full account of spatial effects, including the
24 additional impact on any given area from changes cascading through
25 the entire spatial hierarchy, and which points to a stronger Okun's
26 relationship than inferred from the $\hat{\beta}$ and $\hat{\theta}$ parameters of Model 5.
27 This provides further support for the important role of interregional
28 dependencies in the context of Okun's Law.
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Table 1. Pesaran's Cross-section dependence (CD) test statistic (H_0 : no cross-section dependence)

	UN	Δ UN	GDP	Δ GDP
CD test stat	426.01	397.06	420.69	134.63
[<i>P</i> -value]	[0.000]***	[0.000]***	[0.000]***	[0.000]***
Average $\hat{\rho}_{ij}$	0.927	0.864	0.915	0.293

*** means significance at 1% level (strong rejection of the null hypothesis of no cross-section dependence)

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Table 2. Baseline regressions: Spatial Durbin Models with minimal IV set (Eq. 6).

Estimation Method	1	2
	Fixed-Effects IV	Random-Effects IV
<i>Regressors</i>		
Endogenous Spatial Lag	0.5770	0.4774
(s.e. ρ)	(5.29)***	(4.14)***
Real GDP growth rate (Δ GDP)	-0.0499	-0.0614
(s.e. β)	(-2.58)***	(-2.46)***
Spatial lag of Δ GDP	-0.0748	-0.0747
(s.e. θ)	(-2.33)**	(-1.98)**
One-year lag of UN rate change	0.1104	0.1480
(s.e. γ)	(4.03)***	(4.63)***
Constant		0.2370
(s.e.)		(3.76)***
<i>Diagnostics</i>		
Hausman test of regressors endogeneity ^a		
Chi-sq(2) statistic [P-value]	14.07 [0.00]	14.07 [0.00]
First-stage F test of instruments relevance ^b		
F(6,3449) statistic [P-value] (Δ GDP)	19.71 [0.00]***	19.71 [0.00]***
F(6,3449) statistic [P-value] (Spatial lag of Δ GDP)	41.47 [0.00]***	41.47 [0.00]***
Sargan-Hansen test of instruments orthogonality		
Chi-sq(2) statistic [P-value]	4.75 [0.09]**	2.93 [0.23]***
R ²	0.7671	0.7126
No. regions	128	128
No. years (1985-2011)	27	27

Notes: regressand is Δ UN.

^a^b These diagnostics are common to both models.

Table 3a. Robustness checks: Spatial Durbin Models with extended IV set (Eq. 7).

Estimation Method	3a	4a
	Fixed-Effects IV	Random-Effects IV
<i>Regressors</i>		
Endogenous Spatial Lag (s.e. ρ)	0.7741 (14.19)***	0.6478 (9.69)***
Real GDP growth rate (Δ GDP) (s.e. β)	-0.0189 (-1.72)*	-0.0288 (-1.96)**
Spatial lag of Δ GDP (s.e. θ)	-0.0219 (-1.31)	-0.0388 (-1.80)*
One-year lag of UN rate change (s.e. γ)	0.0731 (4.38)***	0.1133 (5.48)***
Constant (s.e.)		0.1108 (3.78)***
<i>Diagnostics</i>		
Hausman test of regressors endogeneity^a		
Chi-sq(2) statistic [P-value]	2.29 [0.32]***	2.29 [0.32]***
First-stage F test of instruments relevance^b		
F(8,3447) statistic [P-value] (Δ GDP)	26.02 [0.00]***	26.02 [0.00]***
F(8,3447) statistic [P-value] (Spatial lag of Δ GDP)	49.96 [0.00]***	49.96 [0.00]***
Sargan-Hansen test of instruments orthogonality		
Chi-sq(4) statistic [P-value]	14.69 [0.01]*	14.82 [0.01]*
R ²	0.8611	0.8318
No. regions	128	128
No. years (1985-2011)	27	27

Notes: regressand is Δ UN.

^{a,b} These diagnostics are common to both models.

Table 3b. Robustness checks: Spatial Durbin Models with crises dummies (Eq. 6 for IVs).

Estimation Method	3b	4b
	Fixed-Effects IV	Random-Effects IV
<i>Regressors</i>		
Endogenous Spatial Lag (s.e. ρ)	0.8571 (11.33)***	0.5345 (3.26)***
Real GDP growth rate (Δ GDP) (s.e. β)	-0.0266 (-1.11)	-0.1068 (-2.34)***
Spatial lag of Δ GDP (s.e. θ)	-0.0135 (-0.35)	-0.1207 (-1.63)*
One-year lag of UN rate change (s.e. γ)	0.0562 (3.60)***	0.1149 (3.26)***
1991-92 Recession (s.e.)	-0.0049 (-0.05)	-0.2681 (-1.60)*
2008-09 Recession (s.e.)	-0.1052 (-0.63)	-0.6228 (-2.15)***
Constant (s.e.)		0.5361 (2.21)**
<i>Diagnostics</i>		
Hausman test of regressors endogeneity ^a Chi-sq(2) statistic [P-value]	1.22 [0.54]***	1.22 [0.54]***
First-stage F test of instruments relevance ^b F(6,3449) statistic [P-value] (Δ GDP)	19.71 [0.00]***	19.71 [0.00]***
F(6,3449) statistic [P-value] (Spatial lag of Δ GDP)	41.47 [0.00]***	41.47 [0.00]***
Sargan-Hansen test of instruments orthogonality Chi-sq(2) statistic [P-value]	17.62 [0.00]	3.70 [0.16]***
R ²	0.8647	0.6260
No. regions	128	128
No. years (1985-2011)	27	27

Notes: regressand is Δ UN.

^{a,b} These diagnostics are common to both models.

Table 4. Random-Effects FGS2SLS/GMM estimation of General Nesting Spatial (GNS) Models.

Instrumental-Variables set	5	6
	Minimal (Eq. 6)	Minimal (Eq. 6)
<i>Regressors</i>		
Endogenous Spatial Lag (s.e. ρ)	0.3824 (3.44)***	0.3319 (2.59)***
Real GDP growth rate (Δ GDP) (s.e. β)	-0.0609 (-2.66)***	-0.0652 (-2.64)***
Spatial lag of Δ GDP (s.e. θ)	-0.1119 (-3.00)***	-0.1232 (-2.96)***
One-year lag of UN rate change (s.e. γ)	0.1615 (6.36)***	0.1584 (6.23)***
1991-92 Recession (s.e.)		-0.1990 (-1.54)*
2008-09 Recession (s.e.)		-0.4203 (-2.56)***
Constant (s.e.)	0.3009 (3.33)***	0.3482 (3.14)*
<i>Spatial Error process</i>		
λ	0.5816***	0.6016***
σ_v^2	01686	0.1728
$\sigma_1^2 = \sigma_v^2 + T\sigma_u^2$	0.1519	0.1594
R^2 ^a	0.8002	0.7782
No. regions	128	128
No. years (1985-2011)	27	27

Notes: regressand is Δ UN.

^a Correlation between fitted values and observed values of the dependent variable.

Table 5. Direct, Indirect and Total Effects of Δ GDP (Model 5)

W Matrix with distance threshold of 100	Okun's Law Coefficient
AVG DIRECT (OWN-REGION) EFFECTS	-0.0756
(bootstrapped <i>t</i> -ratio)	(-3.19)***
AVG INDIRECT (SPATIAL, SPILLOVER) EFFECTS	-0.2042
(bootstrapped <i>t</i> -ratio)	(-5.18)***
AVG TOTAL EFFECTS	-0.2798
(bootstrapped <i>t</i> -ratio)	(-5.69)***
W Matrix with distance threshold of 150	Okun's Law Coefficient
AVG DIRECT (OWN-REGION) EFFECTS	-0.0754
(bootstrapped <i>t</i> -ratio)	(-3.55)***
AVG INDIRECT (SPATIAL, SPILLOVER) EFFECTS	-0.2039
(bootstrapped <i>t</i> -ratio)	(-5.16)***
AVG TOTAL EFFECTS	-0.2793
(bootstrapped <i>t</i> -ratio)	(-6.14)***
W Matrix with distance threshold of 50	Okun's Law Coefficient
AVG DIRECT (OWN-REGION) EFFECTS	-0.0763
(bootstrapped <i>t</i> -ratio)	(-3.47)***
AVG INDIRECT (SPATIAL, SPILLOVER) EFFECTS	-0.2056
(bootstrapped <i>t</i> -ratio)	(-4.71)***
AVG TOTAL EFFECTS	-0.2819
(bootstrapped <i>t</i> -ratio)	(-5.38)***

References

- Adanu K (2005) A cross-province comparison of Okun's coefficient for Canada. *Applied Economics* 37: 561–570.
- Anselin L (2001) Spatial Econometrics. In: Baltagi BH (eds.) *A Companion to Theoretical Econometrics*. Blackwell Publishers, Massachusetts 310-330.
- Apergis N, Rezitis A (2003) An examination of Okun's law: evidence from regional areas in Greece. *Applied Economics* 35: 1147–1151.
- Arbia G, Basile R, Piras G (2005), Using Spatial Panel Data in Modelling Regional Growth and Convergence. Working Paper No. 55, Istituto di Studi e Analisi Economica (ISAE).
- Attfield C, Silverstone B (1997) Okun's coefficient: a comment. *Review of Economics and Statistics* 79: 326-329.
- Attfield C, Silverstone B (1998) Okun's law cointegration and gap variables. *Journal of Macroeconomics* 20: 626-637.
- Baltagi BH (2005) *Econometric analysis of panel data*. Wiley, Chichester.
- Barro R (1997) *Macroeconomics*. 5th Edition, The MIT Press.
- Blanchard OJ, Summers LH (1984) Hysteresis in unemployment. *European Economic Review* 31: 288-295.
- Bowden RJ, Turkington DA (1984) *Instrumental Variables*. Cambridge University Press, Cambridge.
- Buettner T (1999) The effect of unemployment, aggregate wages, and spatial contiguity on local wages: an investigation with German district level data. *Papers in Regional Science* 78: 47–67.
- Burridge P, Gordon I (1981) Unemployment in the British metropolitan labour areas. *Oxford Economic Papers* 33: 274-297.

Chamberlin G (2011) Okun's law revisited. *Economic and Labour Market Review* 5: 104-132.

Corrado L, Fingleton B (2012) Where is the economics in spatial econometrics?. *Journal of Regional Science* 52: 210-239.

Christopoulos DK (2004) The relationship between output and unemployment: evidence from Greek regions. *Papers in Regional Science* 83: 611–620.

Crespo-Cuaresma J (2003) Okun's law revisited. *Oxford Bulletin of Economics and Statistics* 65: 439-451.

Cross R (1993) On the foundations of hysteresis in economic systems. *Economics and Philosophy* 9: 53-74.

Drukker DM, Egger P, Prucha IR (2013) On two-step estimation of a spatial autoregressive model with autoregressive disturbances and endogenous regressors. *Econometric Reviews* 32: 686–733.

Egger P, Larch M, Pfaffermayr M, Walde J (2009) Small sample properties of maximum likelihood versus generalized method of moments based tests for spatially autocorrelated errors. *Regional Science and Urban Economics* 39: 670-678.

Elhorst P (2003) The mystery of regional unemployment differentials; a survey of theoretical and empirical explanations. *Journal of Economic Surveys* 17: 709-748.

Elhorst P (2010) Spatial panel data models, chapter C2. In: Fischer M, Getis A (eds) *Handbook of Applied Spatial Analysis*. Springer-Verlag, Berlin.

Elhorst, JP (2012) Dynamic spatial panels: models, methods, and inferences. *Journal of Geographical Systems* 14: 5-28.

Elhorst JP (2014) Spatial econometrics: from cross-sectional data to spatial panels. Springer, Heidelberg New York Dordrecht London.

Spatial effects in Okun's Law among British areas

Elhorst P, Blien U, Wolf K (2007) New evidence on the wage curve: a spatial panel approach. *International Regional Science Review* 30: 173-191.

Fingleton B (2003) Increasing returns: evidence from local wage rates in Great Britain. *Oxford Economic Papers* 55: 716-739.

Fingleton B (2008) A Generalized Method of Moments Estimator for a Spatial Panel Model with an Endogenous Spatial Lag and Spatial Moving Average Errors. *Spatial Economic Analysis* 3: 27-44.

Fingleton B (2010) Predicting the Geography of House Prices. SERC Discussion Paper No. 45.

Freeman DG (2000) Regional tests of Okun's law. *International Advances in Economic Research* 6: 557-570.

Freeman DG (2001) Panel tests of Okun's law for ten industrial countries. *Economic Inquiry* 39: 511-523.

Greene WH (2003) *Econometric Analysis*. Prentice Hall, New Jersey.

Harris R, Silverstone B (2001) Testing for asymmetry in Okun's law: a cross-country comparison. *Economics Bulletin* 5: 1-13.

Kangasharju A, Tavéra C, Nijkamp P (2012) Regional growth and unemployment: the validity of Okun's law for the Finnish regions. *Spatial Economic Analysis* 7: 381-395.

Kapoor M, Kelejian HH, Prucha IR (2007) Panel data models with spatially correlated error components. *Journal of Econometrics* 140: 97-130.

Kelejian HH, Prucha IR (1998) A generalized spatial two-stage least squares procedure for estimating a spatial autoregressive model with autoregressive disturbances. *Journal of Real Estate Finance and Economics* 17: 99-121.

Spatial effects in Okun's Law among British areas

- Kelejjan HH, Prucha IR (1999) A generalised moments estimator for the autoregressive parameter in a spatial model. *International Economic Review* 40: 509-533.
- Kelejjan HH, Prucha IR (2004) Estimation of simultaneous systems of spatially interrelated cross sectional equations. *Journal of Econometrics* 118: 27-50.
- Kelejjan HH, Prucha IR (2010) Specification and estimation of spatial autoregressive models with autoregressive and heteroskedastic disturbances. *Journal of Econometrics* 157: 53-67.
- Knoester A (1986) Okun's law revisited. *Weltwirtschaftliches Archiv* 122: 657-666.
- Lee J (2000) The robustness of Okun's law: evidence from OECD countries. *Journal of Macroeconomics* 22: 331-356.
- Leibs OW and Oberst CA (2012) Explaining the Spatial Variation in Homeownership Rates: Results for German Regions. *Regional Studies* 1: 1-22.
- Le Sage J, Pace KR (2009) *Introduction to Spatial Econometrics*. CRC Press, Boca Raton, FL.
- Longhi S, Nijkamp P, Poot J (2006) Spatial heterogeneity and the wage curve revisited. *Journal of Regional Science* 46: 707-731.
- Mitze T (2012) *Empirical Modelling in Regional Science*. Springer.
- Moazzami B, Dadgostar B (2009) Okun's law revisited: evidence from OECD countries. *International Business and Economics Research Journal* 8: 21-24.
- Molho I (1995) Spatial autocorrelation in British unemployment. *Journal of Regional Science* 35: 641-658.

Spatial effects in Okun's Law among British areas

Morrison PS, Papps K, Poot J (2006) Wages, employment, labour turnover and the accessibility of local labour markets *Labour Economics* 13: 639-663.

Moosa IA (1997) A cross-country comparison of Okun's coefficient. *Journal of Comparative Economics* 34: 335–356.

Niebuhr A (2003) Spatial interaction and regional unemployment in Europe. *European Journal of Spatial Development* 5: 1-26.

Oberst CA, Oelgemöller J (2013) Economic Growth and Regional Labour Market Development in German Regions: Okun's Law in a Spatial Context. FCN Working Paper No. 5/2013.

Okun A (1962) Potential GNP: its measurement and significance. *American Statistical Association, Proceedings of the Business and Economics Section* 98–103.

Okun A (1970) *The Economics of Prosperity*. Brookings Institution, Washington, DC.

Paldam M (1987) How much does one percent of growth change the unemployment rate?. *European Economic Review* 31: 306-313.

Partridge MD (2005) Does income distribution affect U.S. state economic growth?. *Journal of Regional Science* 45: 363–394.

Perman R, Tavera C (2005) A cross-country analysis of the Okun's law coefficient convergence in Europe. *Applied Economics* 37: 2501-2513.

Pesaran H (2004) General diagnostic tests for cross section dependence in panels. Working Paper No. 0435, University of Cambridge, Department of Economics.

Taylor J, Bradley S (1983) Spatial variations in the unemployment rate; a case study of North West England. *Regional Studies* 17: 113-124.

Spatial effects in Okun's Law among British areas

Taylor J, Bradley S (1997) Unemployment in Europe: a comparative analysis of regional disparities in Germany, Italy and the UK. *Kyklos* 50: 221-245.

Villaverde J, Maza A (2007) Okun's law in the Spanish regions. *Economics Bulletin* 18: 1-11.

Villaverde J, Maza A (2009) The robustness of Okun's law in Spain, 1980-2004: regional evidence. *Journal of Policy Modelling* 31: 289-297.