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Object Detection in Optical Remote Sensing Images Based on Weakly Supervised Learning and High-level Feature Learning

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Abstract

The advance of remote sensing technology has been capable of providing abundant spatial and contextual information for object detection in optical satellite or aerial imagery, which facilitates subsequent automatic analysis and interpretation of the optical remote sensing images (RSIs). Most existing object detection approaches suffer from two limitations. First, the feature representation used is insufficiently powerful to capture the spatial and structural patterns of objects and the background regions. Second, a large number of training data with manual annotation of object bounding boxes is required in the supervised learning techniques adopted while the annotation process is generally too expensive and sometimes even unreliable. To tackle these two limitations, a novel and effective geospatial object detection framework is proposed by combining the weakly supervised learning (WSL) and high-level feature learning. First, we employ an unsupervised feature learning approach via Deep Boltzmann Machine (DBM) to infer the spatial and structural information encoded in the low-level and middle-level features, which facilitates good semantic preserving ability for effective describing objects in optical RSIs. Then, we present a novel WSL approach to object detection in optical RSIs where the training sets require only binary labels indicating whether an image contains the target object or not. Based on the learnt high-level features, it jointly integrates saliency, intra-class compactness, and inter-class separability in a Bayesian framework to initialize a set of training examples from weakly labeled images and start iterative learning of the object detector. A novel evaluation criterion is also developed to detect model drift and cease the iterative learning. Comprehensive experiments on three optical RSI datasets with large variations in terms of spatial resolution, and types of objects have demonstrated the efficacy of the proposed approach in benchmarking with several state-of-the-art supervised learning based object detection approaches.

Keywords: Weakly supervised learning, Bayesian framework, Object detection, Unsupervised feature learning, Deep Boltzmann Machine.

1. Introduction

The rapid development of remote sensing technologies has rendered many satellite and aerial sensors to provide optical imagery with high spatial resolution, facilitating a wide range of applications such as disaster control, land planning, urban monitoring, and traffic planning \(^1\)-\(^4\). In these applications, automatic detection of natural or man-made objects is a fundamental task and has received increasing research interests. The abundant spatial information and detailed structural information of
objects contained in optical RSIs has offered us the new opportunity to address this challenging task.

Early attempts [1, 4, 5] detected objects in optical RSIs in an unsupervised manner which often started from generating region of interest (ROI) by grouping pixels into clusters and then detected objects of interest based on the shape and spectral information. Afterward, many supervised learning methods have been adopted to learn the object model effectively with the help of prior information obtained from training examples [2, 6-8]. By heavily relying on the human labelled training examples which are statistically representatives of the classification problem to solve, the supervised learning methods can achieve more promising performance than the unsupervised approaches. Therefore, overwhelming object detection systems are usually based on the supervised learning techniques.

The recent advance of remote sensing technology has led to the explosive growth of satellite and aerial images in both quantity and quality. It brings about two increasingly serious problems for the object detection task in optical RSIs. First, supervised learning based object detection approaches often require a large number of training data with manual annotation of labeling a bounding box around each object to be detected. However, manual annotation of objects in large image sets is generally expensive and sometimes even unreliable. For example, for the natural objects such as landslide, the proper manual annotation generally requires considerable expertise. In addition, manual annotation is also difficult for the man-made objects such as airplane and car, where the coverage of target object appears to be very small, especially when complex textures are contained in the image background. As a result, it is difficult to achieve accurate annotation on such small regions. Moreover, the manual annotations may tend to be less accurate and unreliable when the targets are occluded or camouflaged. As a result, it is a great interest in training object detectors with weak supervision for large-scale optical satellite and aerial image datasets.

The second problem is that the rich information contained in the optical RSIs with high spatial resolution has more details of objects whereas feature descriptors used by existing object detectors are still insufficiently powerful to characterize the structural information of the objects. The limited understanding of the spatial and structural patterns of objects in optical RSIs leads to a tremendous semantic gap for the object detection task. It can be observed that man-made facilities, such as airplanes, vehicles and airports, always have intrinsic structural property with specific semantic concepts, which has obvious difference from the background areas in optical RSIs. Consequently, building of the high-level structural and semantic features is a promising way for the interpretation of the optical RSIs and object detection task.

In this paper, we tackle the manual annotation problem for object detection in optical RSIs by proposing a weakly supervised learning (WSL) framework. As one of the most cost-effective learning approach, WSL only requires a weak label for the training images to specify whether the image contains the object of interest or not. To this end, unlike conventional supervised learning approaches which rely on manually labeled bounding boxes for training object detector, accurate locations and sizes of the target objects are not needed in the WSL framework. Object detection using WSL tends to solve localization of the objects of interest in each positive training image (automatic annotation) and object detector training using automatic annotations (detector learning) simultaneously. In practice, WSL is implemented as follows. Given the weak label only indicating whether a certain category of object is contained in an image or not, an initial annotation is firstly obtained automatically, based on which, a detector is trained. The trained detector is then used as the annotator to refine the annotation, whereas the detector is iteratively trained using refined annotations until the model drift is detected. In this paper, we propose a Bayesian framework by jointly exploring saliency, intra-class compactness, and inter-class separability to initialize a training examples set. Afterwards, we propose a novel detector evaluation method which is able to cease the iterative learning process when the detector starts to drift to bad
results and thus we can obtain final object detector with satisfactory performance.

To tackle the problem of insufficiently powerful feature descriptors, we explore the spatial and structural information within image patches via high-level feature learning. Unlike existing works to extract structural features solely based on human design [9, 10], the proposed approach derives high-level features by applying unsupervised representation learning approach, where spatial and structural patterns from the low-level and middle-level features can be automatically captured. Here we adopt Deep Boltzmann Machines (DBM) to learn high-level feature because it has been demonstrated to have the potential of learning useful distributed feature representations and become a promising way in solving object and speech recognition problems [11-13].

In summary, the main contributions of this paper are threefold.

1) We propose a novel WSL framework based on Bayesian principles for detecting objects from optical RSIs, which extensively reduces human labors for annotating training data while achieving performance comparable to that of the fully supervised learning approaches;
2) We propose unsupervised feature learning via DBM to build high-level feature representation for various geospatial objects. The learned high-level features capture the structural and spatial patterns of objects in an effective and robust fashion, which leads to further improvement of object detection performance;
3) Extensive evaluations on three optical RSI datasets with different spatial resolutions and objects of interest are carried out to validate the effectiveness of the proposed methodology.

The rest of the paper is organized as follows. Section 2 gives a brief review of the related work. Section 3 introduces the proposed framework. Section 4 proposes the unsupervised feature learning. Section 5 describes the WSL framework for object detection in optical RSIs. Experimental results are presented in Section 6. Finally, conclusions are drawn in Section 7.

2. Related Work

Object or target detection in optical RSIs has been extensively studied in the past decades. For example, Li et al. [4] developed an algorithm for straight road edge detection from optical RSIs based on the ridgelet transform with the revised parallel-beam Radon transform. Ge et al. [5] detected inshore ships in optical satellite images by using shape and context information that are extracted in the segmented image. Liu et al. [1] presented robust automatic vehicle detection in QuickBird satellite images by applying morphological filters for road line removing and histogram representation for separating vehicle targets from background. All these methods are performed in an unsupervised manner. They are effective for detecting the designed object category in simple scenario.

With the advance of machine learning techniques, many approaches started to cast object detection as a classification problem. In these approaches, a set of features that can characterize the objects is extracted firstly. Then classification is performed using the extracted features and predefined classifiers. For example, Cheng et al. [2] detected landslide from RSI based on the bag-of-visual-words (BOW) representation in combination with the probabilistic latent semantic analysis (pLSA) model and the k-nearest neighbor (k-NN) classifier. Han et al. [3] proposed an efficient, simultaneous detection of multi-class geospatial objects based on visual saliency modeling and discriminative learning of sparse coding. Cheng et al. [6] extracted histogram of oriented gradients (HOG) feature of training examples and used latent Support Vector Machine (SVM) to train deformable part-based mixture models for each object category. Based on the prior information obtained from a large number of human labeled training examples, the supervised learning based approaches normally can achieve better performance. However, collection of large-scale training examples is often difficult and very time consuming.
A few efforts [14-17] have been performed to alleviate the work of human annotation. One interesting idea is to adopt semi-supervised learning model. Such methods apply a self-learning or active learning scheme where machine learning algorithms can automatically pick the most informative unlabeled examples based on a limited set of available labeled examples. Then, these picked unlabeled examples are combined with the initial labeled examples for the training of object detector or classifier. Specifically, Liao et al. [16] proposed a semi-supervised local discriminant analysis method for feature extraction in hyperspectral RSI. Dópido et al. [15] adapted active learning methods to semi-supervised learning for hyperspectral image classification. Jun et al. [18] presented a semi-supervised spatially adaptive mixture model to identify land covers from hyperspectral images.

Although semi-supervised learning methods can considerably reduce the labor of human annotation, they still inevitably require a number of precise and concrete labeled training examples where each object is manually labeled by a bounding box in positive training images. WSL is desirable to further reduce the human labor significantly, where the training set needs only binary labels indicating whether an image contains the object of interest. Although a few WSL approaches have been applied to natural scene image analysis [19-22], those existing methods cannot be directly used to the field of RSI analysis as they have insufficient capability to handle the challenges in RSIs which contain large-scale complex background and a number of target objects with arbitrary orientation. As an initial effort, in our previous work in Zhang et al. [23], WSL was adopted and heuristically combined with saliency-based self-adaptive segmentation, negative mining algorithm, and negative evaluation mechanism for target detection in RSIs. Although it introduced some new concepts for WSL based target detection, the work lacks a principled framework and ignores some important information, which thus can be largely improved. In this paper, we propose a novel principled WSL framework for detecting targets from RSIs. Compared with [23], our improvements in this paper lie in threefold: 1) we propose a powerful high-level feature learning using DBM; 2) we propose a probabilistic approach via the Bayesian rule to jointly integrate saliency, intra-class compactness, and inter-class separability to initialize the training examples; and 3) we propose a novel scheme for model drift detection using the information from both negative training images and positive training images. The experimental results reported in subsection 6.4 can fully demonstrate these improvements.

3. Overview of the Proposed Method

Given a training optical RSI set with weak label only indicating whether a certain category of object is contained in an image or not, the objective of the proposed work is to detect target objects of the same class within the testing images. Because these images generally have very large scale and contain multiple objects of interest, a straightforward way of processing is to decompose the images into small patches by sliding windows, and then predict whether each patch contains the object of interest. As suggested in [2, 3, 14], we adopt the multi-scale sliding window mechanism to handle the variational size of target objects.

The proposed object detection framework consists of two major components: unsupervised feature learning and WSL based object detection. The flowchart of the feature learning component (Section 4) is shown in Fig. 1. In order to obtain more structural and semantic representation of the image patches, we extract a group of low-level and middle-level features to capture the spatial information, and then use DBM to learn the hidden patterns of the middle-level features, which can abstract more structural and semantic information and lead to the desired high-level feature.
Based on the obtained high-level features, the component of WSL based object detection shown in Fig. 2 (Section 5) contains two stages: training and testing. The objective of the training stage is to learn an object detector. In the testing stage, the learned object detector is applied to detect objects in a given testing image. The training stage includes two major steps: training example initialization (Subsection 5.1) and iterative object detector training (Subsection 5.2). For the first step, a Bayesian approach is proposed to integrate three kinds of important information of saliency, intra-class compactness, and inter-class separability, which estimates the probability of an image patch being the object of interest. After initializing the training examples, we are inspired by the bootstrapping method [24] to train the object detector in an iterative process. In each iteration, the detector is utilized as an annotator to refine the positive training set, which is then used to re-train the object detector. Thus both the training examples and object detector could be gradually updated to be more precise and strong. Afterwards, a novel detector evaluation method is proposed to detect the model drift and stop the iterative process automatically for obtaining the final object detector.
4. High-level Feature Representation

Feature description plays an important role in the task of object detection in optical RSIs. However, the performance of the existing feature descriptions in RSI analysis is still far from satisfactory. The main issue lies in the insufficiency in extracting features using only the pixel-based spectral information, which ignores the contextual spatial information and thus fails to capture the more important structural pattern of the object. With the advance of the remote sensing technology, optical satellite and aerial imagery with high spatial resolution makes capturing spatial and structural information possible. Nowadays, accurate interpretation of optical RSI relies on effective spatial feature representation to capture the most structural and informative property of the regions in each image. A number of such approaches have started to explore the spatial information by applying some low-level descriptors (such as SIFT, HOG and GLCM in [6,25,26]) or middle-level features (such as BOW and PLSA in [2,26]) to represent image patches. Although to some extent these human designed features can improve the classification and detection accuracies in optical RSIs, they still suffer from several problems. Specifically, these low-level descriptors only catch limited local spatial geometric characteristics, which cannot be directly used to describe the structural contents of image patches. The middle-level features are usually extracted based on the statistic property of the low-level descriptors in an image patch to capture the structural information of the spatial region. However, it cannot provide enough strong description and generalization ability for object detection in complex backgrounds.

To tackle these problems, we build high-level feature representation via DBM to capture the spatial and structural patterns encoded in the low-level and middle-level features. DBM is one type of neural networks with deep architecture that learns feature representation in an unsupervised manner and has been demonstrated to be promising for building high-level feature descriptors [11,12]. We therefore use it to map the middle-level features to the high-level representation that is highly accurate in characterizing different scenes or objects in optical RSIs. Specifically, the extraction of high-level feature representation (shown in Fig. 1) is carried out in three main stages: (1) Low-level feature descriptor extraction: a collection of low-level local descriptors are calculated by using scale-invariant feature transform (SIFT) [27]. (2) Middle-level feature generation: low-level descriptor of each image patch is coded by Locality-constrained Linear Coding (LLC) model [28]. (3) High-level feature learning: DBM [13] is adopted to learn more powerful representation from the middle-level feature.

4.1 Low-level descriptor extraction

We use low-level features to characterize the local region of each key point in image patches. Due to its ability to handle variations in terms of intensity, rotation, scale, and affine projection, the SIFT descriptor [27] is adopted in the proposed algorithm as the low-level descriptor to detect and describe the key points. According to existing work [2,14,29], the SIFT descriptor has been demonstrated to outperform a set of existing descriptors and widely used in analyzing RSIs.

4.2 Middle-level feature generation

To alleviate the unrecoverable loss of discriminative information, we apply the Locality-constrained Linear Coding (LLC) model [28] to encode the local descriptors into image patch representation. Specifically, all the extracted low-level descriptors are first clustered to generate a codebook by using the K-means method. Let \( \mathbf{D} = [\mathbf{d}_1, \mathbf{d}_2, \ldots] \) denotes a set of \( N \) extracted low-level descriptors in one image patch. Given a codebook \( \mathbf{CB} = [\mathbf{cb}_1, \mathbf{cb}_2, \ldots] \) with \( M \) entries,
LLC converts each descriptor into a \( M \)-dimensional code to generate the final image representation by the following three steps. 1) For each input low-level descriptor \( d_n \), \( n \in [1, N] \), its five nearest neighbors in \( CB \) are used as the local bases \( LB_n \), \( n \in [1, N] \) to form a local coordinate system \([28]\); 2) The local code \( \tilde{c}_n \) is obtained by solving an objective function

\[
\min \sum_{n=1}^{N} ||d_n - \tilde{c}_n ||^2_2 \quad \text{s.t.} \quad \sum_{n=1}^{N} \tilde{c}_n = 1 \tag{1}
\]

Then the full code \( c_n \) is generated, which is an \( M \times 1 \) vector with five non-zero elements whose values correspond to \( \tilde{c}_n \). 3) The final middle-level image patch representation is yielded by max pooling all the generated codes within the patch.

### 4.3 High-level feature learning

A DBM \([13]\) is a neural network with deep structure constructed by stacking multiple Restricted Boltzmann Machine (RBM). In our framework, a three-layered DBM is adopted to capture structural and spatial patterns from middle-level features and learn high-level representations in an unsupervised manner. It contains a visible layer \( v \in \{0,1\}^V \) and two layers of hidden units \( h^1 \in \{0,1\}^{H_1}, \ h^2 \in \{0,1\}^{H_2} \).

Here, \( H_1 \) and \( H_2 \) indicate the numbers of units of the first hidden layer and the second hidden layer, respectively. The energy of the state \( \{v, h^1, h^2\} \) is defined as

\[
E(v, h^1, h^2; \Theta) = -v^T W^1 h^1 - h^1^T W^2 h^2 \tag{2}
\]

where \( \Theta = \{W^1, W^2\} \) are the model parameters, representing visible-to-hidden and hidden-to-hidden symmetric interaction terms. The probability that the model assigns to a visible vector \( v \) is given by the Boltzmann distribution:

\[
\Pr(v; \Theta) = \frac{1}{Z(\Theta)} \sum_{h^1, h^2} \exp(-E(v, h^1, h^2; \Theta)) \tag{3}
\]

where \( Z(\Theta) = \sum_v \sum_{h^1, h^2} \exp(-E(v, h^1, h^2; \Theta)) \) is the partition function.

The conditional distributions over the visible units and the two sets of hidden units are given by:

\[
\Pr(h^1 = 1 | v, h^2) = \text{sigm}(\sum_{m=1}^M W^1_{m, v} + \sum_{j=1}^{H_2} W^2_{j, h^2}) \tag{4}
\]

\[
\Pr(h^2 = 1 | h^1) = \text{sigm}(\sum_{i=1}^{H_1} W^2_{i, h^1}) \tag{5}
\]
\[
\Pr(v_m = 1 | h^1) = \text{sigm}\left( \sum_{i=1}^{H_1} W_{mi}h_i^1 \right)
\]  

(6)

where \( \text{sigm}(\cdot) \) is a sigmoid function.

Given a set of training data, learning of DBM is a process to determine the related model parameters \( \Theta = \{W^1, W^2\} \) in Eq. (2). Although exact maximum likelihood estimation of these parameters is intractable, efficient approximate learning of DBMs can be carried out by using mean-field inference together with the Markov Chain Monte Carlo algorithms \[13\]. Furthermore, the entire model can be efficiently pre-trained in a greedy layer-by-layer unsupervised manner by minimizing the energy function in each individual RBM model (shown in Fig. 3 (a)). Composing the RBM models afterwards forms a unified DBM model (shown in Fig. 3 (b)), which can be used to extract high-level feature representation.

In the proposed algorithm, all the middle-level features extracted from the image patches in training images are used as the input data to train DBM where the second hidden layer is used to build the final high-level feature representation for each image patch.

5. **WSL based Object Detection**

5.1 **Training example initialization**

By applying sliding windows as pre-processing, the training images are divided into many patches. Thus, the patch-level training data \( X^+ = \{x^+_p | p \in [1, P]\} \) and \( X^- = \{x^-_q | q \in [1, Q]\} \) can be generated from the positive training images and negative training images, respectively. Our first task is to select potential target object patches from \( X^+ \) to generate the initial positive training set \( X^+_0 \). Typically, three different information cues, saliency, intra-class compactness, and inter-class separability \[21\] \[22\] are used to initialize the positive training examples. Based on the assumption that the object to be detected is one kind of foreground objects in the image, saliency information ensures that the selected positive example is a foreground region. It may acquire generic knowledge about the sizes and locations
of foreground objects. The intra-class compactness enforces the selected positive examples to be visually similar to each other, whilst the inter-class separability ensures that all selected positive examples are different from negative examples. In this paper, a novel Bayesian framework is proposed to combine these three types of information simultaneously to initialize the positive example training set as follows.

Let a binary random variable $y_p^+$ denote whether or not an image patch $x_p^+$ belongs to one specified object. According to Bayes’ rule:

$$\Pr(y_p^+ = 1 | x_p^+) = \frac{\Pr(x_p^+ | y_p^+ = 1) \Pr(y_p^+ = 1)}{\Pr(x_p^+)}$$

(7)

$$\Pr(y_p^+ = 1 | x_p^+) = 1 - \Pr(y_p^+ = 0 | x_p^+) = 1 - \frac{\Pr(x_p^+ | y_p^+ = 0) \Pr(y_p^+ = 0)}{\Pr(x_p^+)}$$

(8)

After adding the above two equations and omitting the constant term, we have

$$\Pr(y_p^+ = 1 | x_p^+) \propto \left[ \frac{\Pr(x_p^+ | y_p^+ = 1) \Pr(y_p^+ = 1)}{\Pr(x_p^+)} - \frac{\Pr(x_p^+ | y_p^+ = 0) \Pr(y_p^+ = 0)}{\Pr(x_p^+)} \right]$$

(9)

In the information theory, $-\log \Pr(x_p^+)$, which is the log form of $1/\Pr(x_p^+)$, is known as the self-information of the random variable $x_p^+$ [7, 30]. Self-information increases when the probability of a patch decreases. In other words, patches that are discriminative from surrounds are more informative and thus more likely to be the foreground object. Therefore, the term of $1/\Pr(x_p^+)$ in Eq. (9) is associated with the saliency information. The term $\Pr(x_p^+ | y_p^+ = 1)$ indicates the likelihood that favors image patches sharing the similar characteristic with the class of objects of interest. Hence it can be considered as the metric of intra-class compactness. Similarly, the term $\Pr(x_p^+ | y_p^+ = 0)$ reflects the distinctness of image patches in positive images and negative images, thus it corresponds to the metric of inter-class separability. Finally, the remaining two prior probabilities $\Pr(y_p^+ = 1)$ and $\Pr(y_p^+ = 0)$ are treated as the weights of intra-class metric and inter-class metric, respectively.

5.1.1 Saliency

As we assume that objects to be detected are normally one kind of foreground objects, our objective then becomes to quantify how likely each image patch is a foreground object. Foreground objects are generally informative and salient from the surrounding background as shown in Fig. 4. In computer vision, saliency detection technique can be used to estimate the saliency for each image patch. In recent years, it is also employed for the analysis in the domain of remote sensing [31, 32]. Inspired by [31, 33], we adopt sparse coding theory to calculate saliency based on the raw pixels to reveal the structural difference between an image patch and its surrounding. For each image patch $x_p^+$ (the patch indicated by red frame in Fig. 4), it is sparsely coded with its adjacent half-overlapped surrounding
patches (patches indicated by green frames in Fig. 4) by:

$$\chi_p \approx \text{Dic}_p \alpha_p$$  \hspace{1cm} (10)$$

where $\chi_p$ is the raw pixels within $x_p^+$, while $\text{Dic}_p$ and $\alpha_p$ indicate the dictionary constructed by all surrounding patches and the sparse codes, respectively.

Fig. 4. An illustration of saliency calculation.

The rationale behind Eq. (10) is to represent $\chi_p$ approximately by its surrounding patches. According to [31, 33], the coding sparseness $||\alpha_p||_0$ and the coding residual $r_p = \chi_p - \text{Dic}_p \alpha_p$ indicates the saliency of the image patch $x_p^+$ with respect to its surrounding. Therefore, we estimate the saliency by:

$$1/\Pr(x_p^+)=||\alpha_p||_0 \cdot ||r_p||_1$$  \hspace{1cm} (11)$$

5.1.2 Intra-class compactness

The intra-class compactness metric termed as $\Pr(x_p^+ \mid y_p^+ = 1)$ in our framework aims to constrain the similarity between positive examples. As positive examples of a specific object category should be visually similar, we can use a Gaussian Mixture Model (GMM) to estimate the probability distribution of all positive examples. Then, $\Pr(x_p^+ \mid y_p^+ = 1)$ measures how likely each image patch is a positive example. Image patches with large $\Pr(x_p^+ \mid y_p^+ = 1)$ may be selected as positive examples. We use the high-level feature $f_p^+$ (described in Section 4) to represent each image patch $x_p^+$ as this feature can handle the variations in scale and orientation and capture the spatial and structural patterns of each image patch. As patterns learned using DBM are approximately independent, the joint probability is simplified to the product of probability of each hidden unit’s response:
\[
\text{Pr}(x_p^+ | y_p^+ = 1) = \prod_{j=1}^{H_2} \text{Pr}([f_p^+]_j | y_p^+ = 1)
\]

where \([f_p^+]_j\) indicates the \(j\)-th dimensional value of \(f_p^+\) and \(H_2\) indicates the dimensionality of \(f_p^+\) as defined in Section 4. The distribution of each hidden unit’s response is estimated using GMM with adaptive component \(K_{j=1,...}^+\) by:

\[
\text{Pr}([f_p^+]_j | y_p^+ = 1) = \sum_{k=1}^{K_j^+} \pi_j^+ \cdot N([f_p^+]_j | \mu_{jk}^+, \sigma_{jk}^{2+})
\]

where \(\pi_{jk}^+, \mu_{jk}^+, \sigma_{jk}^{2+}\) are parameters of the GMM in the \(k\)-th component for the \(j\)-th dimensional feature. All parameters are inferred based on object candidates in \(\tilde{J}\) by using the expectation-maximization (EM) algorithm and Bayesian inference \([34]\). Here, \(\tilde{J}\) denotes the set of object candidates and will be described in subsection 5.1.5.

5.1.3 Inter-class separability

Inter-class separability metric is to enforce the selected positive examples are dissimilar to negative examples. In WSL, the most confident information comes from the negative training images because they definitely do not contain the target. It is also reasonable to believe that the positive examples containing target objects should be different from the negative image patches in the negative images. Consequently, we can collect a large number of negative image patches to estimate the probability distribution of negative examples via a GMM. Then, we formulate the inter-class metric as the likelihood term \(\text{Pr}(x_p^+ | y_p^- = 0)\), which reflects the probability of a certain image patch appearing in negative training images. The high probability of the appearance in negative images would lead to low inter-class difference and separability. Similar to \(\text{Pr}(x_p^+ | y_p^+ = 1), \text{Pr}(x_p^+ | y_p^- = 0)\) can be decided based on the high-level feature by:

\[
\text{Pr}(x_p^+ | y_p^- = 0) = \prod_{j=1}^{H_2} \text{Pr}([f_p^-]_j | y_p^- = 0)
\]

\[
\text{Pr}([f_p^-]_j | y_p^- = 0) = \sum_{k=1}^{K_j^-} \pi_{jk}^- \cdot N([f_p^-]_j | \mu_{jk}^-, \sigma_{jk}^{2-})
\]

where parameters \(\pi_{jk}^-, \mu_{jk}^-, \sigma_{jk}^{2-}\) and \(K_j^-\) are inferred by GMM based on all the negative image patches in \(X^-\).
5.1.4 Prior probability

Pr(y_p^+ = 1) and Pr(y_p^- = 0) are two prior terms in the proposed Bayesian framework. According to [34], Bayesian methods would result in poor performance when inappropriate choices of prior are applied without any prior belief. Therefore, inspired by [35], we define the prior terms to reflect the prior belief. Our prior belief is that Pr(y_p^+ = 0) should be high when the content of certain image patch x_p^+ has small distance to the negative image patches in X^−, and Pr(y_p^- = 1) should become high when the content of x_p^- is close to the object candidates in X. Hence, we simply adopt the Nearest-Neighbor (NN) distance [36] to estimate these prior probabilities as:

\[
Pr(y_p^+ = 0) = \exp\{-||x_p^- - Nn(x_p^+)\||_1\}
\]

(16)

\[
Pr(y_p^- = 1) = \exp\{-||x_p^+ - Np(x_p^+)\||_1\}
\]

(17)

where \(||||_1\) is the \(L_1\) norm. Same as in [21, 36], Nn(x_p^+) and Np(x_p^+) refer to the nearest-neighbor of x_p^+ in X^− and X (in terms of the high-level feature described in Section 4), respectively.

Finally, these two prior terms are used as the weights of the inter-class and intra-class metrics in order to reflect the prior probability that an image patch belongs to the positive and negative training example, respectively.

5.1.5 Implementation details

In terms of Eq. (9), the post probability \(Pr(y_p^+ = 1|x_p^-)\) are estimated by integrating the saliency, intra-class and inter-class metrics. Note that before calculating the intra-class compactness metric, \(\tilde{X}\) needs to be available. The work [22] proposed an exhaustive searching strategy to generate one object candidate for each image. However, it is lack of accuracy and efficiency for the large-scale RSIs especially when it contains multiple target objects locating at quite scattered positions. To tackle this challenging problem, we in practice implement our work in two stages.

In the first stage, we calculate the post probability \(Pr(y_p^+ = 1|x_p^-)\) approximately by only using the saliency and inter-class separability metrics to generate \(\tilde{X}\). As initially \(Pr(x^+ | y_p^+ = 1)\) and \(Pr(y_p^- = 0)\) are unknown, we omit them by following [7, 30], which is equivalent to assuming a uniform likelihood distribution for the unspecified object category. The overall formulation reduces to:

\[
Pr(y_p^+ = 1|x_p^-) \propto \frac{1}{Pr(x_p^-)} [1 - Pr(x_p^+ | y_p^- = 0) Pr(y_p^+ = 0)]
\]

(18)

Hence \(\tilde{X}\) can be further determined by choosing a probability threshold \(\tau\):
Once $\hat{\mathcal{F}}$ is obtained, we fully implement the proposed Bayesian framework in the second stage, where all the three types of information are explored and integrated for calculating $\Pr(y_p^+ = 1| x_p^+)$ by Eq. (9). Similar to the first stage, a threshold $\tau$ is chosen to determine the label of each image patch and thus generate the initial positive training set $X_0^+$ by:

$$X_0^+ = \{ x_p^+ | \Pr(y_p^+ = 1| x_p^+) \geq \tau \}$$

By considering the fact that imbalanced positive and negative training data may reduce the performance of the object detector, we follow the previous work of [24] to generate the initial negative training set $X_0^-$ by randomly under-sampling of $X^-$ to the same size as $X_0^+$. Some examples in the initial training set are shown in Fig. 5.

5.2 Iterative detector training

After obtaining the initial training examples, the object detector is trained iteratively in the proposed framework (shown in Fig. 2). In each iteration, the training set generated by the previous iteration is used to train the current object detector, which in turn updates the training examples for the next iteration. The iteration process stops when a model drift is detected by a novel detector evaluation method. Then the object detector obtained before model drift is regarded as the final object detector.

5.2.1 Training example and object detector update

As can be seen in Fig. 5, although most of the examples in the initial positive training set generated by the proposed work are the objects of interest, it still contains several noise examples. Consequently, promising object detector cannot be obtained by directly using the initial training data. Inspired by [20, 22], we train the object detector in an iterative process, which can update the training set and the object detector iteratively. Linear SVM is adopted in the proposed algorithm because it has very low training costs and has been demonstrated to be both efficient and effective in RSI analysis [3, 37]. Based on the
SVM formulation, we use the below score function for object annotation and detection.

\[ \text{Score}(x_p^*) = w_i^T \Phi_p + b_i \]  \tag{21}

where the variables \( w_i \) and \( b_i \) are defined as the SVM decision plane and its bias, which are learnt from the initial training data. With the score function, binary class label \( y_p^+ \) are assigned to the image patch \( x_p^+ \) based on the sign of the function.

\[ y_p^+ = \begin{cases} 1, & \text{Score}(x_p^*) \geq 0 \\ 0, & \text{Score}(x_p^*) < 0 \end{cases} \]  \tag{22}

In order to obtain more precise object patches as the updated positive training examples, an adaptive threshold is used to determine image patches that have higher confidence to be the object of interest.

\[ X'_1 = \{ x_p^+ \mid \text{Score}(x_p^*) \geq \frac{\sum_{p=1}^{p'} y_p^+ \cdot \text{Score}(x_p^*)}{\sum_{p=1}^{p'} y_p^+} \} \]  \tag{23}

where \( X'_1 \) is the updated positive training set after the first iteration. Afterwards, the same number of negative examples randomly selected from \( X^- \) are used to generate the new negative training set \( X''^- \).

Alternating the update of object detector and training examples progressively improve their accuracy until the end of the iteration. Combination of these two stages in an iterative way is very similar to the bootstrapping [24] or active learning [14] strategy, which allows the proposed WSL based object detection in optical RSIs to achieve good performance that even superior than the traditional supervised learning methods in some cases.

5.2.2 Detector evaluation

Similar to the model drift phenomenon in adaptive object tracking, the performance of the trained object detector is improved in the first several iterations, continually, and then begins to degrade. Consequently, generating reasonable evaluation mechanism to detect the model drift is important. As the exact location of the objects of interest in each positive training image is unknown, thus it is impossible to measure directly whether a stronger object detector has been obtained after each iteration. It brings great challenge for evaluating the object model and detecting model drift in WSL.

Firstly we use a negative example based evaluation mechanism to estimate the performance of the trained object detector in each iteration. In general, a good object detector is expected to obtain detection results with high true positives and low false positives. In the WSL, we can only obtain precise negative image patches which certainly contain no object of interest. As a result, the negative evaluation mechanism is adopted here to approximately evaluate the false positive rate for the object detector. Specifically, for each iteration, the trained object detector is applied to classify each image patch with the negative training images and then calculate the false positive rate \( FR \) by:

\[ FR = \frac{|X^-_{\text{false}}|}{|X^-|} \]  \tag{24}

\[ X^-_{\text{false}} = \{ x_q^- \mid \text{Score}(x_q^-) \geq 0 \} \]  \tag{25}
where \( f_q^- \) refers to high-level features of \( x_q^- \in X^- \) and \(|\cdot|\) denotes the number of elements.

Another evaluation mechanism is based on the estimation of the object detector’s performance in positive training images. Here we define \( GMM^+ \) and \( GMM^- \) as the distributions inferred by GMM based on the positive and negative examples, respectively. As the positive training examples are updated after each iteration, the distribution of the \( j \)-th dimensional high-level feature is modified along the iteration as:

\[
GMM_j^+ = \sum_{k=1}^{K^+} \pi^+_j N(\mu^+_j, \sigma^2_j)
\]

where \( \pi^+_j, \mu^+_j, \sigma^2_j \) are inferred based on the updated positive training examples after each iteration. In contrast, \( GMM^- \) is fixed as:

\[
GMM_j^- = \sum_{k=1}^{K^-} \pi^-_j N(\mu^-_j, \sigma^2_j)
\]

where \( \pi^-_j, \mu^-_j, \sigma^2_j \) are inferred based on the constant negative image patches in \( X^- \). In the first iteration, the object detector trained on the initial training examples is not very accurate. Thus the trained object detector may work unsatisfactory and the updated positive examples generate the \( GMM^+ \) distribution having amount of overlap with the \( GMM^- \) distribution as shown in Fig. 6 (a). After several iterations, if the object detector is getting stronger, the overlap between the two distributions should become less as shown in Fig. 6 (b). Finally, when the detector starts to drift towards some noise patches without containing objects of interest, the overlap tends to large again as shown in Fig. 6 (c). Consequently, we evaluate the object detector and monitor the model drift by estimating the overlap between the two GMM distributions in each iteration. As the \( GMM^- \) distribution is fixed, the distance between the expectations of the two distributions and the variance of \( GMM^+ \) distribution are used to approximately predict the overlap area. Intuitively, the \( GMM^+ \) distribution with expectation away from that of \( GMM^- \) and small variance has small overlap with the distribution of the \( GMM^- \) and vice versa (shown in Fig. 6). According to [34], the expectation and variance of the \( GMM^+ \) for the \( j \)-th dimensional high-level feature are decided by:

\[
\text{Ex}(GMM_j^+) = \sum_{k=1}^{K^+} \pi^+_j \mu^+_j
\]
\[
\text{Var}(GMM_j^+) = \sum_{k=1}^{F} \tilde{r}_j^{(k)} \approx \left( GMM_j^+ \right)^2
\]

where \( \tilde{\mu}_j \), \( \tilde{\sigma}_j \), \( \tilde{\mu}_j \) and \( \tilde{\sigma}_j \) are inferred by the updated positive training examples after each iteration. Similarly, the expectation of the \( GMM^- \) for the \( j \)-th dimensional high-level feature is obtained by:

\[
\text{Ex}(GMM_j^-) = \sum_{k=1}^{K_j} \pi_{jk} \mu_{jk}
\]

By combining the above-mentioned two evaluation mechanisms, the final detector evaluation measure (DEM) in WSL is determined as:

\[
DEM = \sqrt{\sum_{j=1}^{H} (\text{Ex}(GMM_j^+) - \text{Ex}(GMM_j^-))^2 / (FR \times \sum_{j=1}^{H} \text{Var}(GMM_j^+))}
\]

Based on DEM, we can evaluate the object detector trained in each iteration. Higher DEM indicates better performance of the current object detector and vice versa. Being consistent with the above analysis, the DEM value of the object detector trained in the first iteration should be relatively small. Then, it increases as the detector is gradually refined in the following iterations. When the DEM value starts to decrease, the model drift is detected and the iteration process is terminated. The final object detector is determined as the one obtained before the model drift (as shown in Fig. 6 (d)).
information about the testing datasets and the experiment setup are described. Then we evaluate the 
influence of two key parameters to the proposed algorithm. Next, the effectiveness of the Bayesian 
framework and the high-level feature built by DBM are validated, respectively. Finally, the object 
detector trained by the proposed WSL approach is tested to detect the object of interest in the three 
datasets.

6.1 Datasets and experimental setup

Three optical RSI datasets with different spatial resolutions and various objects of interest were 
used in our experiments. The details of these datasets are shown in Table I. The first dataset consists of 
120 very high-resolution images from the publicly available Google Earth service. This dataset is 
adopted to train and test the airplane detector. 70 randomly selected images were weakly labeled and 
used as the training set (50 images containing airplanes as positive training images and 20 images not 
containing any airplanes as negative training images), and the remaining 50 images were used as the 
testing images. The second dataset called ISPRS data set is a very high-resolution aerial image dataset 
which contains 100 images of vehicle objects provided by the German Association of Photogrammetry 
and Remote Sensing (DGPF) [38]. We randomly selected 60 weakly labeled images as the training data 
(45 positive training images and 15 negative training images) to train vehicle detector. The remaining 40 
images were used as the testing data. The third dataset consists of 180 shortwave-infrared (SWIR) 
imageries from Landsat-7 satellite. 133 randomly selected images were weakly labeled (98 positive 
training images and 35 negative training images) and used as the training data to train the airport 
detector. The remaining 47 images were used as the testing data. For all the three datasets, we also 
manually labeled bounding box for each target object in both training data and testing data to form the 
ground truth for the following evaluations. Fig. 7 shows a number of examples for the images and 
targets of interest. As can be seen, the target objects in different datasets have different sizes, 
orientations, and colors.

![Fig. 7. Some samples from the three benchmark datasets.](image)

<table>
<thead>
<tr>
<th>Data Set</th>
<th>Scale (pixels)</th>
<th>Spatial Resolution</th>
<th>Target Area (pixels)</th>
</tr>
</thead>
<tbody>
<tr>
<td>Google Earth</td>
<td>about 1000×800</td>
<td>About 0.5m</td>
<td>700~25488</td>
</tr>
<tr>
<td>ISPRS dataset</td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>Landsat dataset</td>
<td></td>
<td></td>
<td></td>
</tr>
</tbody>
</table>
In the experiments, as suggested in [2, 3], we used square sliding windows with side lengths of \{60, 100, 135\} for airplane detection, \{60, 80\} for vehicle detection, and \{60, 100, 130\} for airport detection, respectively, where the sliding step-size was also set to be \(1/3\) of the window side length. When building the high-level feature representation for the image patches, we set the number of entries \(M\) to 1024 empirically.

In the test phase, the proposed object detector trained using our WSL framework was performed to classify each image patch in the test images generated by the multi-scale sliding window scheme. For sliding windows in different sizes, there may be significant overlap on detected targets. To solve this problem, we adopt a non-maximum suppression step as suggested in [3, 6, 14] to retain the sliding window with the highest score.

### 6.2 Key parameter analysis

In the implementation of training example initialization (subsection 5.1), several parameters may affect the performance and thus have to be set properly. These include the number of units \(H_1, H_2\) in each hidden layer of DBM and the probability threshold \(\tau\) in Eqs. (19) and (20). To show how their values affect the performance of the proposed approach, we performed experiments on all the three datasets and evaluated the F1-measure by:

\[
\text{F1-measure} = \frac{2 \cdot \text{PRE} \cdot \text{REC}}{\text{PRE} + \text{REC}}
\]

\[
\text{PRE} = \frac{TP}{TP + FP}, \quad \text{REC} = \frac{TP}{NP}
\]

where \(TP\), \(FP\) and \(NP\) denote the number of true positives (i.e. the number of correctly selected positive training examples), the number of false positives (i.e. the number of falsely selected training examples), and the number of total positives (i.e. the number of real targets in positive training images) under the threshold \(\tau\). As suggested in [3, 6], an annotation or detection is marked as a true positive when its corresponding image patch can cover more than 50% of a ground truth. \(\text{PRE}\) and \(\text{REC}\) indicate the precision and recall rate, respectively. As suggested in [38], equal number of units is used in each hidden layer (\(H_1 = H_2 = H\)) in our implementation and the experimental results are shown in Fig. 8.

We empirically set \(H = 50\) for all the datasets and \(\tau = 0.45, 0.90, \text{and } 0.95\) for the Google Earth dataset, the ISPRS dataset, and the Landsat dataset, respectively, based on which the best detection performance can be achieved. We used this set of parameter values in all subsequent experiments.
6.3 Evaluation of the Bayesian framework

In this section, we evaluated the performance of the proposed Bayesian framework by comparing it with the baseline methods. Since the proposed Bayesian framework integrates the saliency, intra-class compactness, and inter-class separability information for the positive training example initialization (indicated by the bins in red in Fig. 9), we evaluated its performance on the training sets. Here, we treat the methods that initialize positive examples by using the saliency information only, the inter-class information only, the intra-class information only, fusing the saliency and inter-class information, and fusing the saliency and intra-class information as the baseline methods. Note that the last two baseline methods were also implemented by using the proposed Bayesian framework. Based on the criterion of F1-measure, the experimental results are shown in Fig. 9.

From Fig. 9, we can observe that: 1) the impact of the three single information on the initialization
results change with the variation of the dataset and object of interest. For example, the saliency makes the biggest contribution for the initialization results on the Google Earth dataset whereas the intra-class information contributes mostly on the Landsat dataset; 2) in comparison to those using one of the three kinds of information, the performance of the fusion methods is more promising; and 3) fusion of all the three information always achieves the best results regardless to the variation of datasets and objects of interest.

6.4 Evaluation of the high-level feature

In order to demonstrate the effectiveness of the proposed high-level feature, we compared it with three state-of-the-art features, which include the bag-of-word (BOW) [26], the pyramid histograms of oriented gradients (pHOG) [6][39] and the LLC [28]. Specifically, the BOW feature characterizes each training data by using a histogram of visual words; the pHOG feature represents the shape property of the image patches by using histograms of orientation gradients while the LLC feature is described in subsection 4.2. For quantitative evaluation, we plot the precision-recall (PR) curve of the object detection results and calculated average precision (AP) value as shown in Fig. 10 for comparisons. Specifically, the PR curve is plotted based on the values of \( PRE \) and \( REC \) under different thresholds while the AP is calculated by the area under the PR curve [3][14]. The four different features were compared using the proposed WSL framework and the same sets of training and testing data. As shown in Fig. 10, the proposed high-level feature always outperforms the other three state-of-the-art features.

![Precision-recall curves on the Google Earth dataset](image1)

![Precision-recall curves on the ISPRS dataset](image2)

![Precision-recall curves on the Landsat dataset](image3)

Fig. 10. Precision-recall curves for different types of feature on the three datasets. Here DBM indicates the high-level feature learned by the proposed work.

6.5 Evaluation of the object detector

We evaluated the performance of the proposed weakly supervised object detector by comparing it
with one existing WSL based method and several supervised learning based methods. Firstly, we
compared the proposed approach with the WSL based method in [23]. For the fair comparison, in the
experiment we utilized the same experimental settings including the same feature representation build
by DBM, the same sliding window scheme, and the same testing image set. Fig. 11 gives the PR curves
of the experiment results. The corresponding AP values are shown in Table II.

![Fig. 11. Precision-recall curves for the comparisons with the weakly supervised learning method.](image)

We also compared the proposed WSL approach with several existing supervised learning based
object detection methods including a baseline method from Xu [26], and Han’s method [3]. The baseline
method was implemented by training object detector (linear SVM) based on the proposed high-level
feature in a manner of fully supervised learning where the human annotations (manually labeled
bounding box for each target in training images) are provided in the training images. The object detector
trained by Xu’s method was based on the spectral and texture local feature descriptor and SVM with
RBF kernel. Han's method trained object detector via discriminative sparse coding which has small
within-class scatter and large between-class scatter. All comparison methods were evaluated using the
same sets of training and testing data. Fig. 12 illustrates the PR curves of the experiment results. The
 corresponding AP values are shown in Table II.

![Fig. 12. Precision-recall curves for the comparisons with the supervised learning methods.](image)

From Figs.11-12 and Table II, we can observe that the proposed WSL approach can achieve
much better performance than the state-of-the-art WSL based method and comparable performance
with the state-of-the-art fully supervised learning based methods. Specifically, the object detection
accuracy of the proposed WSL approach achieves about 97.13%, 92.34% and 92.89% of what the
baseline approach does in the Google Earth dataset, the ISPRS dataset, and the Landsat dataset,
respectively. It also improves the performance of the previous WSL based approach [23] significantly,
i.e., 0.088 (8.88%), 0.1499 (14.99%), and 0.024 (2.4%) in terms of AP in the Google Earth dataset, the ISPRS dataset, and the Landsat dataset, respectively. More encouragingly, the proposed WSL approach performs even better than other two state-of-the-art fully supervised methods in some cases. Specifically, for airplane detection in the Google earth dataset, it outperforms Xu’s method and Han’s method by 0.0741 (7.41%) and 0.0595 (5.95%), respectively. In the ISPRS dataset, the proposed WSL approach outperforms Xu’s method and Han’s method by 0.0751 (7.51%) and 0.0706 (7.06%), respectively. From the overall results among the three datasets, it can be seen that due to the powerful high-level feature representation built by DBM, the supervised baseline method yields the best results on these datasets. Benefited by the Bayesian framework to generate accurate initial training examples and the iterative training scheme to gradually refine the object detector, the proposed WSL algorithm achieves detection performance that outperforms the previous WSL based target detection method [23] and approaches to the fully supervised baseline method. Furthermore, based on the combination of the high-level feature representation and the proposed WSL framework, the overall performance of weakly supervised detector apparently outperforms the other two existing state-of-the-art supervised methods.

<table>
<thead>
<tr>
<th>Objects of interest</th>
<th>WSL based object detector (ratio to the supervised baseline approach)</th>
<th>Supervised learning based object detector</th>
</tr>
</thead>
<tbody>
<tr>
<td>Airplane</td>
<td>0.6016 (97.13%)</td>
<td>0.5128 (82.79%)</td>
</tr>
<tr>
<td>Vehicle</td>
<td>0.5332 (92.34%)</td>
<td>0.3833 (66.38%)</td>
</tr>
<tr>
<td>Airport</td>
<td>0.2679 (92.89%)</td>
<td>0.2439 (84.57%)</td>
</tr>
<tr>
<td>Overall</td>
<td>0.4676 (94.45%)</td>
<td>0.3801 (76.77%)</td>
</tr>
</tbody>
</table>

Finally, some experimental results from the proposed approach for airplane detection, vehicle detection and airport detection are shown in Figs. 13-15, respectively. In these figures, the red rectangles indicate the true-positive results, while the black and yellow rectangles denote the false-positive and miss alarm results, respectively. As can be seen, the object detector trained via the proposed WSL approach can effectively detect objects of interest from all the datasets with different spatial resolution and cluttered backgrounds.

Fig. 13. Examples of airplane detection in the Google Earth dataset.
7. Conclusions

In this paper, we have proposed a novel framework to tackle the problem of object detection in optical RSIs. The novelties that distinguish the proposed work from previous works lie in two major aspects. First, instead of using traditional supervised or semi-supervised learning methodology, this paper developed a WSL framework that can substantially reduce the human labor of annotating training data while achieving the outstanding performance. Second, we developed a deep network to learn high level features in an unsupervised manner, which offers a more powerful descriptor to capture the structural information of objects in RSIs. It thus can improve the object detection performance further. Experiments on three different types of RSI datasets have demonstrated the effectiveness and robustness of the proposed work.

Our future work will focus on two directions. First, the proposed work is designed to train the object detector for detecting objects of a single category. We will extend it to the joint learning of multiple categories of object detectors. Second, the proposed work only used the spatial information.
We will combine the rich spectral information provided by RSIs with spatial information for more accurate and robust object detection.

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