

A low-noise transimpedance amplifier for the detection of “Violin-Mode” resonances in advanced Laser Interferometer Gravitational wave Observatory suspensions

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This paper describes the design and performance of an extremely low-noise differential transimpedance amplifier, which takes its two inputs from separate photodiodes. The amplifier was planned to serve as the front-end electronics for a highly sensitive shadow-displacement sensing system, aimed at detecting very low-level “Violin-Mode” (*VM*) oscillations in 0.4 mm diameter by 600 mm long fused-silica suspension fibres. Four such highly tensioned fibres support the 40 kg test-masses/mirrors of the Advanced Laser Interferometer Gravitational wave Observatory interferometers. This novel design of amplifier incorporates features which prevent “noise-gain peaking” arising from large area photodiode (and cable) capacitances, and which also usefully separate the *DC* and *AC* photocurrents coming from the photodiodes. In consequence, the differential amplifier was able to generate straightforwardly two *DC* outputs, one per photodiode, as well as a single high-gain output for monitoring the *VM* oscillations—this output being derived from the difference of the photodiodes’ two, naturally anti-phase, *AC* photocurrents. Following a displacement calibration, the amplifier’s final *VM* signal output was found to have an *AC* displacement responsivity at 500 Hz of (9.43 ± 1.20) MV(rms) m⁻¹(rms), and, therefore, a shot-noise limited sensitivity to such *AC* shadow- (i.e., fibre-) displacements of (69 ± 13) picometres/ $\sqrt{\text{Hz}}$ at this frequency, over a measuring span of ± 0.1 mm. © 2014 Author(s). All article content, except where otherwise noted, is licensed under a Creative Commons Attribution 3.0 Unported License. [<http://dx.doi.org/10.1063/1.4900955>]

I. INTRODUCTION

A prototype system of four shadow-sensors was designed to be retro-fitted into an Advanced LIGO (Laser Interferometer Gravitational wave Observatory) test-mass/mirror suspension, in which a 40 kg test-mass was suspended by four fused silica fibres, the dimensions of each fibre being approximately 600 mm long by 0.4 mm in diameter.^{1–6} These shadow-sensors—one per suspension fibre—each comprised an optical emitter and detector, bracketing the illuminated fibre. The emitter provided a collimated beam of illumination from a Near InfraRed (NIR: $\lambda = 890$ nm) multi-LED source,⁷ and this cast a vertical shadow of the illuminated fibre onto its facing, photodiode-based, detector. The detector was configured to monitor, with extremely high precision, any lateral displacement of the fibre’s shadow. Ultimately, each detector was in the form of a differential “synthesized split-photodiode”—this having a negligible dead-band between its pair of sensing photodiode elements.⁸ The purpose of the full shadow-sensing detection system was first to monitor any lateral “Violin-Mode” (*VM*) resonances that might be excited on these highly tensioned silica fibres, at frequencies in the range 500 Hz–5 kHz—which spanned the gravitational wave detection bandwidth;⁹ and, as a secondary task, to record any “large” amplitude “pendulum-mode” motion of the test-mass and its suspension fibres at frequencies of ~ 0.6 Hz—such that all of this unwanted oscillatory motion, which might mimic or obscure the detection of gravitational waves, then could be suppressed by active cold-damping.^{10,11} The shadow-

sensing system was required to have an overall fibre- (i.e., shadow-) displacement sensitivity of 100 picometres (rms)/ $\sqrt{\text{Hz}}$ at 500 Hz (the fundamental *VM* resonance frequency for the suspension fibres), across a ± 0.1 mm range of fibre position.

Initially, a transimpedance (photocurrent-to-voltage) amplifier was researched for use as the low-noise “front-end” electronics to a single photodiode-based shadow-sensor, with the shadow of the illuminated fibre falling over one vertically orientated edge of the rectangular sensor. In this way, a lateral vibration, or simple displacement, of the silica fibre’s shadow altered the photocurrent flowing through the photodiode (PD).

This single-PD-input amplifier, whose salient features are described in Sec. II, was developed subsequently into a differential amplifier, which was itself interfaced to the split-PD-based shadow-sensor, mentioned above. Here, the fibre’s shadow fell over the central (common vertical) edge of two adjacent rectangular elements in the detector. An additional, beneficial, side-effect of this combination of differential detector and amplifier was that proper shadow-alignment with the detector could be carried out more straightforwardly—by virtue of the natural pendulum-mode motion of the monitored fibre and its suspended test-mass. This high-performance differential amplifier is described in Sec. III.

It turned out that vibrational motion of a silica fibre and its attendant shadow at a frequency of 500 Hz, and with an amplitude of 100 pm (rms), equated to an *AC* photocurrent modulation at this frequency of approximately 4 picoamps (rms), flowing in the single PD detector, and flowing in



anti-phase in the split-photodiode detector's two elements. It was conceivable, though, that "very large" Violin-Mode vibrations with amplitudes of up to $1\ \mu\text{m}$ (rms) might be excited in the suspension fibres, and such signals clearly would have to be accommodated within the amplification chain as well—with neither distortion, nor clipping. Moreover, pendulum-mode motion of a suspended test-mass, at $\sim 0.6\ \text{Hz}$, could certainly attain excursions of $\pm 100\ \mu\text{m}$ about the monitored fibre's quiescent position. In addition, each photodiode element's standing DC photocurrent, arising from steady illumination by its NIR source, was found to be $\sim 50\ \mu\text{A}$. Therefore, ostensibly, the detection amplifier would have to be designed in such a way as to handle a very wide range indeed of photocurrents.

However, it was appreciated that this range could be reduced significantly, with other attendant benefits as described below, if the DC and $0.6\ \text{Hz}$ photocurrents were handled separately from the VM signals.

II. THE PROTOTYPE SINGLE-INPUT VIOLIN-MODE AMPLIFIER

Initially, a single-PD-input/dual output transimpedance amplifier was researched, such that the AC modulated VM photocurrent and the standing DC photocurrent—plus any very low frequency modulation—would produce separate AC and " DC " output voltages, these outputs both being proportional to their respective photocurrents, although via different resistive transduction paths.

As regards the amplifier's primary AC output, it was a requirement of the detection system that it should be able to monitor additionally a number of harmonics of the fundamental VM resonance, since these Eigenmodes also could be excited on the silica fibres—perhaps up to the tenth harmonic.

Therefore, the shadow-sensor's prototype transimpedance amplifier needed the following characteristics:

1. High gain over a VM (AC) bandwidth covering at least a frequency range of $500\ \text{Hz}$ – $5\ \text{kHz}$: a transimpedance gain of $120\ \text{M}\Omega$ would generate an acceptable $19.2\ \text{V}$ signal (peak-peak) at the maximum anticipated level of VM AC photocurrent.
2. An ultra-low-noise level at the VM (AC) output over the frequency range specified in requirement 1, above. However, "noise gain peaking" was anticipated within the above bandwidth,¹² due to the large PD plus cable capacitance, and, clearly, this effect would have to be mitigated in the amplifier's design, at the outset.
3. Very low VM (AC) signal gain at $\sim 0.6\ \text{Hz}$, so that pendulum-mode motion of the test-mass/suspension would not interfere with VM detection at frequencies of $500\ \text{Hz}$, and above.
4. A separate DC output for (ultimately, each of) the PD element(s), with a composite shadow-displacement range capability of $\pm 100\ \mu\text{m}$, say, which would be sensitive also to the anticipated $\sim 0.6\ \text{Hz}$ pendulum-mode motion of a test-mass/mirror and its suspension fibres. Here, a transimpedance gain of just $120\ \text{k}\Omega$ would give a quiescent output of magnitude $6\ \text{V}$ at the anticipated level of

DC standing photocurrent; and then, a pendulum-mode modulation at $\sim 0.6\ \text{Hz}$, and with an amplitude of $4\ \mu\text{A}$, would superimpose an easily discernible $\pm 0.48\ \text{V}$ excursion about this quiescent value.

5. In addition to the foregoing requirements, it was required that any overload of the VM (AC) amplifier should occur with essentially symmetrical clipping at the amplifier's output, such that a (cold-) damping system still could apply (e.g., electrostatic) damping forces with the correct phase.

A. The single-PD transimpedance amplifier design

A transimpedance amplifier with a single-PD input was designed to address the requirements listed 1–5 above, and its circuit diagram is shown in Figure 1(b), with a subsequent modification that was made to it shown in Figure 1(a).

Circuits similar to that shown in Figure 1(b)—if taken from the PD detector up to the node bearing the label V' —have been described previously for the purposes of "rejecting ambient light,"¹³ or for the "control of ambient light."¹⁴ In this work, however, the op-amp based circuit shown in the figure does not discard the DC photocurrent, but rather uses it in order to create a separate " DC " output channel—to be employed, ultimately,

- (i) for aligning the shadow onto a dual-PD sensor,
- (ii) for calibrating the DC , and hence AC , responsivities to fibre- (shadow-) displacement, and
- (iii) for sensing the pendulum-mode motion mentioned above—also employed in (i).

In Figure 1, I_{photo} is the full ($DC + AC$) photocurrent generated in the PD by the illuminating source, with the fibre's shadow falling over one edge of the rectangular PD. In the following discussion this current has been decomposed explicitly into its steady-state and time-varying (VM) parts, such that $I_{photo} = I_{DC} + i$.

In Figure 1(b) the "debut" (i.e., non-inverting) integrator feedback around IC3, involving IC2 and its two resistors R , and capacitors, C , forces the *mean*, steady-state, DC output of IC3 always to be close to zero volts. A zero-average input to the integrator can occur only when no DC photocurrent flows through the resistor, R_f , and under these conditions the output of IC2, labelled V_{DC} in the figure, must be frozen at whatever happened to be its existing—negative—value at the time the "zero volts average" condition was achieved at the output of IC3. Accordingly, the full DC photocurrent, I_{DC} , must flow from the anode (A) of the PD, which is a virtual Earth point (at the inverting input to IC3), down through resistor R_i , and into the output of IC2, which acts as a DC current-sink. Thus, $V_{DC} = -I_{DC} \times R_i$, as indicated in the figure: the DC transimpedance gain of the amplifier is therefore $120\ \text{k}\Omega$.

On the other hand, none of the AC photocurrent i can flow through resistor R_i , because the output of the sluggish integrator IC2 cannot follow this HF signal so as to produce a suitable driving voltage for it across resistor R_i —due the long RC time-constant of integration.

Clearly, for a truly *DC* component of photocurrent ($s = 0$) Eq. (1) reduces to the simple expression $V_{DC} = -I_{DC}R_i$, as derived above. For the component values given in Figure 1(b), the expression in Eq. (1) is effectively that of a low-pass response, with a dominant pole at 161 Hz (and a second, HF, pole at 13.1 kHz): therefore, 0.6 Hz “pendulum-mode” signals were passed without attenuation to the amplifier’s *DC* output.

In a similar fashion, the *ratio* of the amplifier’s *AC* response to a *VM* signal photocurrent, to its *DC* response to a steady quiescent photocurrent (a convenient ratio) can be found to be

$$\frac{V_{AC}}{V_{DC}(s=0)} = \frac{A(R_f/R_i)s^2CRC_2R_2}{(s^2CRC_fR_f + sCR + R_f/R_i)(sC_2R_2 + 1)(sC_3R_3 + 1)}. \quad (2)$$

Here: $A = 101$, $C_f = 10$ pF, $R_f = 1.2$ M Ω , $R_i = 120$ k Ω , $C = 100$ nF, $R = 100$ k Ω , $C_2 = 100$ nF, $R_2 = 10$ k Ω , $C_3 = 4.7$ nF, and $R_3 = 2.7$ k Ω . Equation (2) effectively expresses the relative sensitivity of the amplifier’s *AC* and *DC* outputs to changes in photocurrent due to *the same* displacement of a fibre’s shadow across (the edge of) the PD detector: in the *AC* case a change occurring at a frequency $s (= j\omega)$ for a sinusoidal modulation at angular frequency ω ; and in the *DC* case a change occurring from one steady *DC* value to another, as the fibre’s shadow made a quasi-static displacement. Practically, this relationship was used to calibrate the sensitivity to *VM* displacement of the fibre, at any given frequency $f (= \omega/2\pi)$, relative to the—straightforwardly measurable—rate of change of *DC* output voltage V_{DC} with silica fibre (shadow) position. Refer to Ref. 16.

In practice, the theoretical mid-band (~ 1.48 kHz) *AC/DC* gain ratio given by Eq. (2) did not quite peak at the anticipated value of $101 \times 10 = 1010$ but was slightly reduced by the sharply circumscribed (four poles/two zeroes) pass-band of the amplifier, as discussed below.

C. Prototype amplifier: Practical NIR gain calibration

A calibration system was built to verify that Eq. (2) properly described both the *AC* and *DC* behaviours of this amplifier. This system involved irradiating the amplifier’s single photodiode detector with a very low intensity beam derived from an OD50L NIR LED, using a pin-hole aperture, the beam consisting of a steady component of fixed intensity, plus a small sinusoidal intensity modulation on top of this at a known frequency, f .¹⁷

The results of such measurements of the *AC/DC* gain ratio as a function of the frequency f agreed with the theoretical expression given by Eq. (2) at a $\pm 1\%$ level up to ~ 100 kHz, i.e., well above the required *VM* bandwidth of 5 kHz. Consequently, as mentioned above, a bench measurement of the shadow-sensor’s quasi-static responsivity to shadow- (i.e., suspension fibre-) displacement (hereinafter called the “*DC* responsivity”), allowed the corresponding *AC* responsivity to

be inferred with a high degree of confidence from the measured *AC/DC* gain ratio at any given *VM* frequency, f . This was the technique used to calibrate the amplifier’s *AC* responsivity as a function of f .^{16,17} In practice the gain was found to be 1000 mid-band at 1.48 kHz and 990 at 1 kHz (and 976 ± 4 mid-band for the differential amplifier, described below, at 1.48 kHz).

III. THE DIFFERENTIAL VIOLIN-MODE AMPLIFIER

Following the successful performance of the prototype amplifier, connected to a single rectangular photodiode sensor, it was clear that a differential sensor would improve the signal-to-noise ratio by a factor of $\sqrt{2}$. Two closely adjacent *Hamamatsu* S2551 photodiode elements, orientated so that the fibre’s shadow fell along their common vertical edge, and sensing differentially, could in principle double the size of the available *AC* photocurrent signal, whilst offering a degree of common-mode rejection, as well.

A. The differential amplifier: From concept to construction

The outline design of the Transimpedance Amplifiers block is shown in Figure 2. It is essentially a dual version of the prototype amplifier, but with an intermediate, differential, *AC* amplification stage. For the photodiode element PDa in Figure 2, I_a represents the “*DC*” value of its photocurrent, inclusive of any pendulum-mode modulation, whilst i_a represents any HF modulation of this photocurrent due to transverse *VM* oscillation of its monitored fibre (and shadow). Similar nomenclature has been used for element PDb. Note that the modulation photocurrents i_a and i_b flowed automatically in anti-phase for the “synthesized split-photodiode” detector: if the silica-fibre’s shadow moved over the common edge of elements PDa and PDb, so as to move off PDa (by any

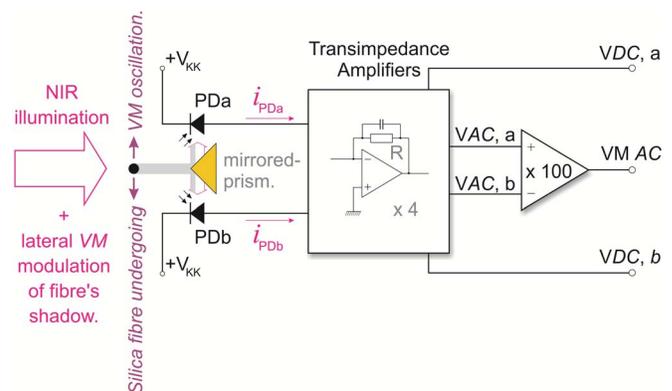


FIG. 2. Schematic diagram of the Violin-Mode shadow-sensor connected to its “Transimpedance Amplifiers” block (differential amplifier), with the “synthesized split-photodiode-” based sensor being shown in plan view. The mirrored prism split the collimated incident NIR illumination so that it, together with a variable fraction of the fibre’s shadow, fell onto each photodiode sensor element—as if the separate photodiodes formed a single split-photodiode detector, with negligible dead-band between the two elements. Here, the full photocurrents flowing in photodiode elements PDa and PDb have been designated, respectively, $i_{PDa} = I_a + i_a$ and $i_{PDb} = I_b + i_b$ (refer to the text).

amount) and onto PDb, then the illumination of PDa, and thereby its photocurrent, i_{PDa} , increased; but as the shadow moved off element PDa it moved automatically onto element PDb, thereby decreasing i_{PDb} by closely the same amount by which i_{PDa} was increased.¹⁶ The amplifier's two "DC" voltage outputs, labelled VDC,a and VDC,b in the diagram, were derived from the DC photocurrents I_a and I_b , respectively, via a transimpedance gain of $R = 120\text{ k}\Omega$. Similarly, the intermediate AC signal voltages VDC,a and VDC,b were derived from i_a and i_b , respectively, but in this case via a ten-times-larger transimpedance gain of $R = 1.2\text{ M}\Omega$. These two transimpedance signals were then differenced, and their resulting differential voltage was amplified further by a factor of $\times 100$, so as to produce the final Violin-Mode output voltage $VMAC$.

In this way, and measured from an individual photodiode element to its own respective pair of outputs, the overall AC transimpedance gain was measured to be $(976 \pm 4) \times$ the DC gain (mid-band), or approximately 1% lower than that of the single-input amplifier, as expected, given the slightly lower value of the AC gain stage in this amplifier.

The full circuit diagram of the differential amplifier is shown in Figure 3, and the realization of two such amplifiers on a pair of small Printed Circuit Boards, using surface-mount components, is shown in Figure 4. It is noteworthy that an earlier version of the differential amplifier, which was built using through-hole mounted components, gave an equally good noise performance in the pass-band, but did not conform

quite so closely to the theoretical high frequency performance as did the surface-mount amplifiers—as exemplified by Figure 5. Four differential VM amplifiers and shadow-sensors were built, one per suspension fibre of a full test-mass mirror suspension.

B. The differential amplifier: Signal and noise performance

A typical noise Power Spectral Density (PSD) of the differential amplifier, measured at its VM AC output, is shown in Figure 5. The -3 dB bandwidth was found from a fit of Eq. (2) to these noise data to lie between 226 Hz and 8.93 kHz. The theoretical pass-band is indicated by the labelled solid (blue) line in the figure and it is seen to be a very good fit to the measured noise PSD for frequencies above $\sim 50\text{ Hz}$. Moreover, the peak, mid-band, noise PSD was found to lie very close indeed to the fundamental shot-noise limit, as indicated in the figure by the horizontal (red) line. Here, this limit was calculated from the two measured DC photocurrent values by assuming that the shot noise arising from the two photodiode elements was uncorrelated. The roll-off of the amplifier's gain towards both lower and higher frequencies was at a rate of -40 dB/decade . Given the measured mid-band noise PSD of $-63.2\text{ dBV(rms)}/\sqrt{\text{Hz}}$ ($\equiv 692\text{ }\mu\text{V(rms)}/\sqrt{\text{Hz}}$), the broad-band rms noise voltage was expected to be 68 mV

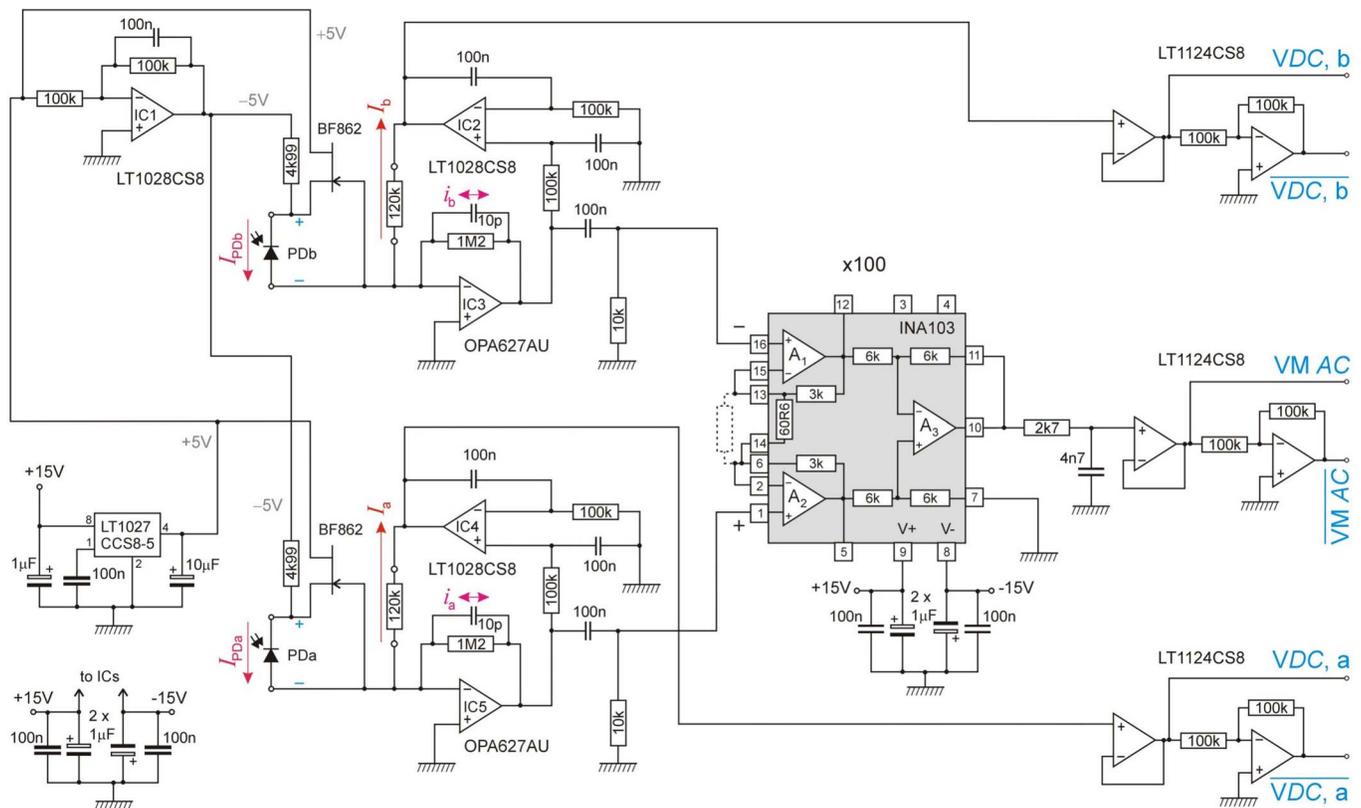


FIG. 3. Circuit diagram of the Violin-Mode differential shadow-sensing transimpedance amplifier sensor (with photodiode sensing elements PDa and PDb). Three complementary outputs were made available for driving long cables, if necessary (refer to the text). This also allowed positive versions of the two DC outputs, $\overline{VDC,a}$ and $\overline{VDC,b}$, to be used. The INA103 instrumentation amplifier is a $1\text{ nV}/\sqrt{\text{Hz}}$ device. Four such amplifiers were constructed—one per silica fibre. Two of these amplifiers are shown, as constructed, in Figure 4. For coaxial output cables $> 2.5\text{ m}$ in length, $600\text{ }\Omega$ resistors were added directly in series with the six outputs, to prevent oscillation.

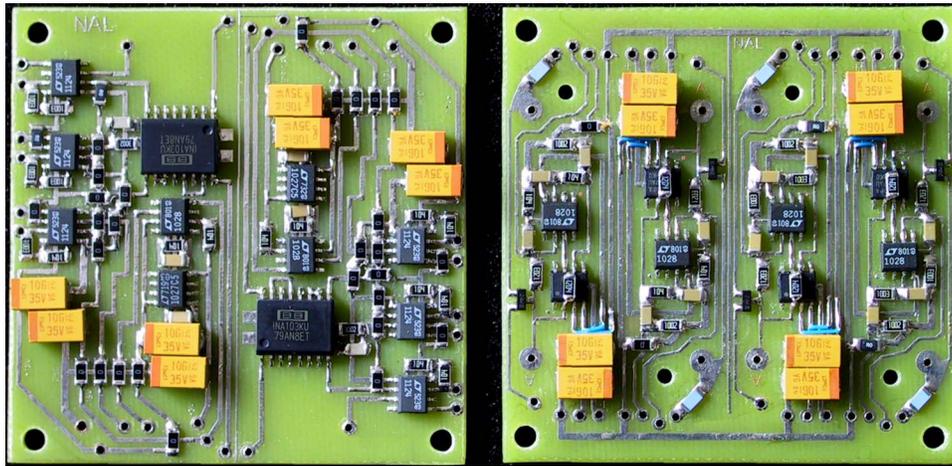


FIG. 4. Two of the four SMD-based amplifiers were constructed on the pair of PCBs shown in the figure, each amplifier being of the type shown in Figure 3. The PCBs measured $60\text{ mm} \times 60\text{ mm}$, such that they could be stacked one above the other within a compact square enclosure. Each amplifier was interfaced to a particular (differential photodiode based) shadow-sensor, a separate sensor being dedicated to each one of the four suspension fibres of a full test-mass/mirror suspension.

(rms)—very close to the measured value, as seen in Figure 6. Note that the split supply rails for the amplifiers both benefited from “noise finessing” filters, in order to reduce voltage regulator noise.¹⁸

An actual *VM* signal resulting from an approximately $1\ \mu\text{m}$ peak-peak acoustically induced fibre resonance, at a frequency of $1019.1\ \text{Hz}$, is also shown in Figure 6. Here, a single capture of the *VM* AC signal is seen to be approximately $10\ \text{V}$, peak-peak. Twenty three volts peak-peak (approx.

$2.4\ \mu\text{m}$, peak-peak) signals could have been accommodated, without clipping or distortion.

C. The differential amplifier: DC and AC responsivities

In practice, quasi-*DC* pendulum-mode signals were detected using the *DC* outputs of these amplifiers, and signals with amplitudes of up to $\pm 140\ \mu\text{m}$, peak-peak, at $0.64\ \text{Hz}$, were detected.⁹ These same *DC* outputs were used also for

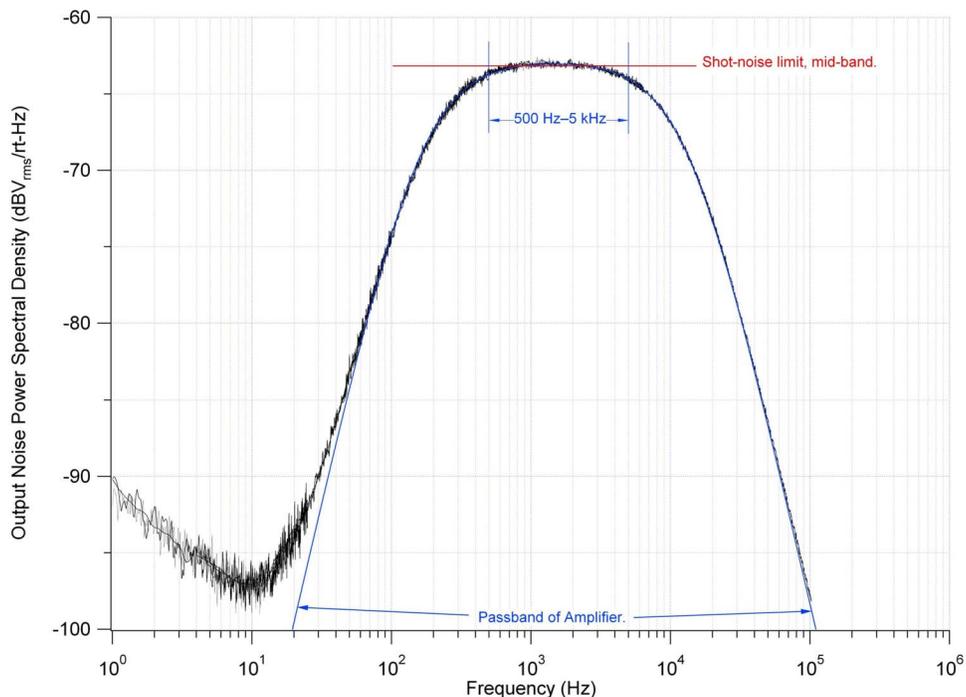


FIG. 5. Noise Power Spectral Density of the differential amplifier as a function of frequency, measured at the *VM* AC output of the amplifier. The fundamental mid-band shot noise limit is marked by the horizontal line in the figure, at $-63.2\ \text{dBV}_{\text{rms}}/\sqrt{\text{Hz}}$. The theoretical amplifier Passband, as described by Eq. (2), is indicated by the blue line. Here, the fibre’s shadow fell over neither detector element, in order to avoid *VM* and other resonant peaks, and so the noise PSD is higher in this figure at $500\ \text{Hz}$, say, than when the shadow fell over the adjacent edge of both detector elements—as it must for proper *VM* detection. The reduction in noise PSD with the shadow present was approximately $0.8\ \text{dB}$, in fact. The noise reduction was due entirely to the lower levels of *DC* photocurrent, and so shot noise, in the two partially shaded PD elements.⁷

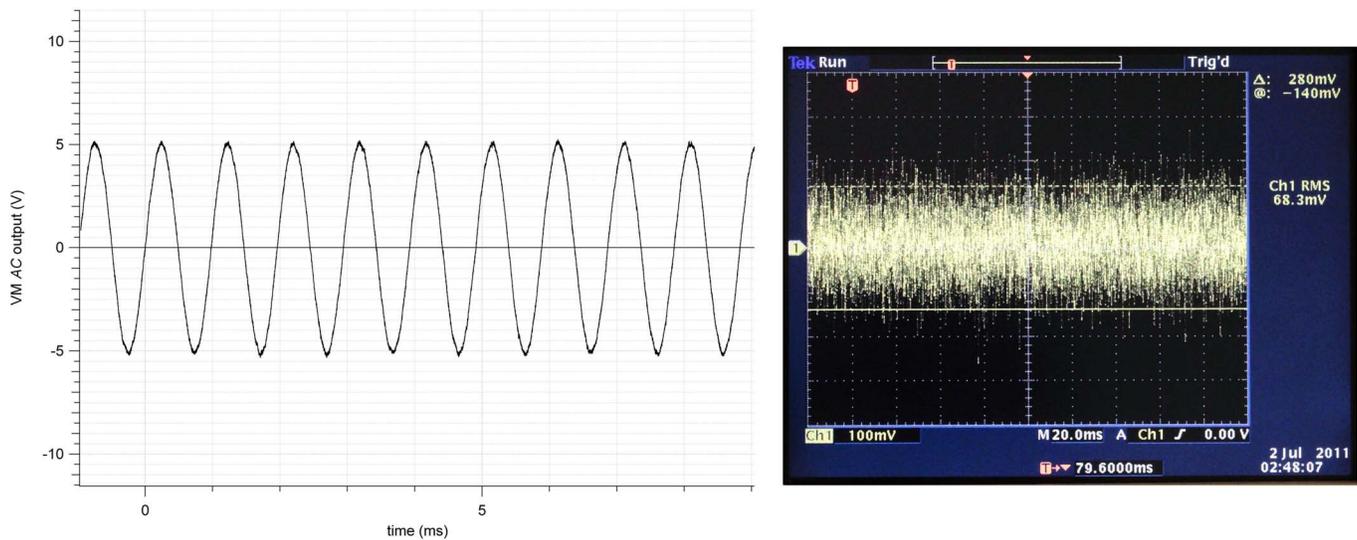


FIG. 6. (Left) The differential amplifier's *VM AC* output, showing an acoustic excitation of the fundamental Violin-Mode of a 95 mm long silica fibre sample, 0.4 mm in diameter, using a distant loudspeaker. A single capture of the resulting Violin-Mode waveform is shown, at approximately 10 V, peak-peak, and so the amplitude of the test fibre's transverse Violin-Mode motion was approximately $1 \mu\text{m}$, peak-peak. The resonant frequency was found to be 1.0191 kHz. (Right) Photo of the Tektronix TDS-3052B oscilloscope screen, showing the amplifier's typical broadband output noise level to be $\sim 68 \text{ mV}$ (rms) at the amplifier's *VM AC* output—in agreement with theory for this wide frequency band. The horizontal bars have been set approximately at the $\pm 2\sigma$ levels.

displacement calibration, and in bench tests the *DC* responsivity of each photodiode detector + amplifier was measured by translating laterally a test fibre, mounted vertically on a motorised stage, through the NIR beam of each shadow sensor. In this way, the *DC* responsivity was found.¹⁶ Taken over the four detectors and their respective amplifiers, it was measured to be 10.44 kV m^{-1} of fibre displacement. From this value, the *AC* responsivity was deduced to be $(9.43 \pm 1.20) \text{ MV(rms) m}^{-1}(\text{rms})$, when taken over the four detectors/amplifiers, since the *AC/DC* gain ratio was measured to be 904 at this frequency.

With an exceptionally low *VM AC* output noise PSD at 500 Hz of $(-64.0 \pm 0.5) \text{ dBV(rms)/}\sqrt{\text{Hz}}$, when taken over all four—partially shaded—detectors, and with the high *AC* responsivity of the detection system given above, the limiting displacement sensitivity of the full shadow sensor/amplifier system was found to be $(69 \pm 13) \text{ picometres (rms)/}\sqrt{\text{Hz}}$ at 500 Hz, over a measuring span of $\pm 0.1 \text{ mm}$ —thus exceeding its target sensitivity of $100 \text{ picometres (rms)/}\sqrt{\text{Hz}}$, at this frequency, and over this measuring range.⁷⁻⁹

IV. CONCLUSIONS

The noise level measured for the differential amplifier was little different from the fundamental limit expected from (uncorrelated) shot noise in its two photodiode detector elements. Indeed, the “white noise” region of the differential amplifier's Power Spectral Density followed its theoretical pass-band very closely over the frequency range investigated, as seen in Figure 5, only deviating above this form for frequencies below $\sim 50 \text{ Hz}$, where $1/f$ noise began to dominate. Both versions of the amplifier exhibited close-to the theoretically expected signal gain, with the *AC/DC* gain ratio mid-band (1.48 kHz) being very close to the expected value of approximately 1000. Moreover, the signal gain at the “pendulum-

mode” frequency of $\sim 0.6 \text{ Hz}$ was, by a very useful factor of $>70\,000$ (97 dB), smaller than that found mid-band—allowing Violin-Mode signals in the range 500 Hz–5 kHz to be detected, even in the presence of very much larger pendulum motion of the test mass and its supporting fibres. The differential amplifier's *AC* pass-band extended from 226 Hz to 8.93 kHz (-3 dB), and its very low noise level allowed it, in principle, to recover a 500 Hz sinusoidal Violin-Mode vibration of amplitude $(69 \pm 13) \text{ picometres (rms)}$, in one second. Yet, this amplifier output could handle, without clipping or distortion, a similar signal of amplitude $2.4 \mu\text{m}$ (or $\sim 23 \text{ V}$), peak-peak. The subsidiary “*DC*” outputs had a designed (*DC*) responsivity to quasi-static shadow displacement that was lower than the mid-band *AC* responsivity by a factor of approximately 1000. These outputs therefore exhibited a much larger detection range for shadow displacement, with a bandwidth extending from true *DC* – 160 Hz (-3 dB point). This allowed pendulum-mode signals at 0.64 Hz, and of amplitude exceeding $200 \mu\text{m}$ peak-peak, to be captured without attenuation. In summary, the differential Violin-Mode amplifier described above clearly met, or exceeded, all of its performance targets.

At the time of writing the Violin-Mode sensor system mentioned here has not been adopted for aLIGO, and, indeed, the need for *VM* damping has not yet been demonstrated. However, if it is found to be required, the current baseline solution is to use aLIGO's Arm Length Stabilisation system as a *VM* sensor.¹⁹ In fact, the issue of vacuum compatibility remains unresolved for the *VM* sensor mentioned here, because the *Hamamatsu* photodiodes used for the detector elements had been encapsulated, using an unknown epoxy. However, were it to become necessary, the issue of the epoxy for the photodiodes from this, or another, manufacturer probably could be resolved, and the LEDs and other components used are likely to prove vacuum compliant, or have

vacuum-compliant alternatives. Nevertheless, the *VM* amplifier described here may find other applications.

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