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Comparative Analysis of the DFB Fiber Laser and Fiber-Optic Interferometric Strain Sensors

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Abstract: The DFB fiber laser strain sensor is shown to provide an improvement in the minimum detectable length change by a factor of 275 at 2 kHz for an applied strain when compared with an interferometric sensor interrogated by an equivalent DFB laser. This corresponds to a strain resolution enhancement by a factor of 18, if the strain is applied over a 10cm length of fiber. The ability of the fiber laser sensor to operate in its thermodynamic noise limit is shown to be the primary reason for this enhanced sensitivity. Thermodynamically limited noise performance is demonstrated with three interrogation methods.

INTRODUCTION

The distributed feedback (DFB) fiber laser provides new possibilities for developing very high performance\textsuperscript{1}, small size, strain sensors. Probably the most successful, existing high-performance fiber-optic strain sensors are based on fiber-optic interferometry. Indeed, the development of the fiber laser operating in the 1550nm erbium window has permitted very high performance to be obtained from interferometric sensors interrogated by fiber laser sources \cite{1} costing considerably less than existing high-performance lasers, such as the diode-pumped Nd:YAG non-planar ring laser \cite{2}. In many types of interferometric sensor, the phase resolution is determined by laser frequency induced phase noise, which is generated in unbalanced interferometers. Balancing the optical paths thus reduces this noise source. However, in many interrogation schemes a non-zero path imbalance will exist due either to engineering constraints or the requirement of a small path imbalance in order to implement an interrogation scheme. The fiber laser sensor (FLS) offers an interesting alternative configuration to the interferometric sensor, and is implemented by simply exchanging the functions of the interferometer and laser in an interferometric sensor. In the FLS, the laser now becomes the strain sensor, where the applied strain modulates the wavelength or frequency of the laser, and the interferometer acts to decode the frequency shift of the laser. It will be shown that this configuration provides a higher sensitivity per unit length than the interferometric sensor. Thus, for any strain sensing configuration where the interaction length is limited, the FLS may either provide a performance benefit or permit equivalent sensitivity to be achieved in a smaller size transducer. Although a seemingly straightforward and beneficial exchange, the performance of the FLS is critically dependent on the laser output spectral properties. When used as a laser source, it can generally be ensured that the environmental operating conditions are carefully controlled. However, when configured as a sensor, the operating conditions are much less certain, and the laser must therefore by designed to tolerate more variation in operating conditions without significant effect on the spectral properties. What has allowed this concept to be practically useful is the significant developments that have taken place in fiber Bragg grating lasers over the last \textasciitilde 15 years. High performance strain measurement is achieved when the fiber laser operates in a single longitudinal mode, which requires a very short laser cavity. Considerable improvements in laser stability were obtained by the implementation of the distributed feedback fiber laser \cite{3}. This laser configuration consists of a single Bragg grating, a few cm in length, with a phase shift imposed to force single frequency operation. The lasing mode is now effectively locked to the resonance caused by the phase shift. This structure provides considerable resilience to environmental perturbations such as temperature gradients and bending of the fiber. These developments have yielded realistic demonstrations of sensors based on the DFB fiber laser \cite{4-6}.

The aim of the manuscript is to compare the performance of the fully optimized interferometric sensor interrogated by the DFB fiber laser with the DFB fiber laser sensor. The performance benefits of the FLS are calculated and a discussion

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\textsuperscript{1} High-performance is a relative term and in the present context refers to strain sensors capable of achieving strain resolutions approximately in the 1 to 100 f\textsuperscript{H} range. For comparison, standard fiber Bragg grating strain sensors achieve \textasciitilde 1 \mu\textsuperscript{H} resolution (dc), interferometrically interrogated FBGs achieve \textasciitilde 1 n\textsuperscript{H} resolution (ac) and interferometric sensors achieve sub p\textsuperscript{H} resolution (ac). Note that dc generally refers to frequencies less than \textasciitilde 1 Hz.
on efficient implementations of the wavelength decoding interferometer based on (i) active-homodyne, (ii) phase-generated carrier and (iii) the 3×3 interferometer is given.

STRAIN SENSORS

The output spectral properties of the fiber laser strongly influence the performance of both the interferometric sensor and the FLS. Two important properties are the relative intensity noise and frequency noise, from which the performance of most strain sensor configurations can be predicted. Two DFB fiber lasers, which exhibit similar output properties and referred to as FL1 and 2, are used in this work. The DFB fiber laser under test is pumped at ~980 nm with a grating stabilized pump diode producing up to 200mW. Both FLs exhibit single frequency and polarization mode output. The relative intensity noise (RIN) of FL1 is shown in fig. 1(i). This exhibits a strong relaxation oscillation at 210 kHz, which increases the RIN to -82 dB/Hz. Between 100Hz and 100kHz, the FL RIN is close to the pump RIN. In the case of the FLS, a significant source of excess noise due to RIN is that caused by noise aliasing, when the detected power is not sufficiently low-pass filtered to remove the relaxation oscillation peak.

![Figure 1: DFB fiber laser (i) relative intensity noise and (ii) frequency/phase noise (80m imbalance)](image)

The limiting noise source in the FLS is shown to be frequency noise, which exhibits several features. The frequency noise of the laser is measured by injecting the laser output into a fiber-optic Mach-Zehnder interferometer with an 80m fiber path imbalance and converting the interferometric phase noise into input frequency noise. This is shown in fig. 1(ii) along with the equivalent phase noise. Below 1kHz the frequency noise is strongly influenced by environmental acoustical and vibration noise. Between ~3kHz and 100kHz, the noise is limited by thermodynamic noise, first noted in [7] (spontaneous emission noise is estimated to be over an order of magnitude lower than this noise source). The theoretical thermodynamic noise, described in [8], is also plotted, for an effective cavity length of 6.5mm, yielding a frequency noise of 14.5 Hz/Hz^{1/2} or phase noise of 33 µrad/Hz^{1/2} at 2 kHz. For comparison, the phase noise due to thermodynamic noise in the measurement interferometer is 0.238 µrad/Hz^{1/2} (a factor of ~252 less than the measured phase noise @ 2 kHz). It is worth noting that although the thermodynamically induced phase noise in the interferometer is much lower, this noise floor in a practical interferometric sensor is never realized (unless the fiber lengths are > 1km), since other noise sources, typically detector or laser noise limit the phase resolution to greater than a microradian. Above 100kHz, an increase in noise due to the relaxation oscillation peak is observed. Note that the smaller peaks in the frequency noise spectrum over the range 10 kHz – 100kHz are thought to originate from the mounting.

FIBER-OPTIC INTERFEROMETRIC STRAIN SENSOR

The interferometric sensor configuration is shown in fig. 2 and utilizes the frequency-modulated phase-generated carrier (FM-PGC) interrogation method. The output of the fiber laser is frequency modulated with a fiber wrapped piezoelectric tube phase modulator, driven by a sinusoidal tone at 18.2 kHz. The modulator is used in reflection with a Faraday rotation mirror (FRM) to suppress polarization modulation. The modulated light is then injected into an imbalanced interferometer with a 1m effective fiber path imbalance and a phase carrier signal is generated on the detector. The output of the detector is sampled by an A/D converter and the processing of the PGC signal is carried out in Labview. FRMs are used in the interferometer to ensure an optimum fringe visibility of greater than 0.9. The section of fiber following the FL is a length of erbium doped fiber, which uses the remaining pump power to amplify the FL output to 10 mW. The pump is injected into this section through a bi-pass wavelength division multiplexer (WDM)
around the isolator (ISO). The interferometric phase shift, $\Delta \phi$, is related to the strain applied to the sensing fiber by the relation, 

$$\Delta \phi = 0.78 \cdot (4\pi n / \lambda) \cdot \Delta \varepsilon,$$

where $n$ is the effective refractive index of the optical fiber, $l$ is the sensing fiber length, $\lambda$ is the free space wavelength and $\Delta \varepsilon$ is the applied strain. The factor of 0.78 accounts for the elasto-optic effect [9].

$$\text{DFB FIBER LASER STRAIN SENSOR}$$

The fiber laser sensor configuration is shown in fig. 3. FL2 is used for these measurements and is also pumped by a grating stabilized pump diode at 980nm. The output of the FL is injected into one of three interferometer configurations. Configuration (i) is known as active-homodyne and uses a servo-loop to maintain the interferometer at its quadrature point. The phase signal is read from the feedback voltage applied to the PZT tube. The second configuration (ii) is known as the phase-generated carrier. Here, a sinusoidal tone is applied to the PZT, which generates a frequency carrier onto which the phase signals appear as modulation sidebands. The detected signal is then decoded in the same way as the interferometric sensor described above. Configuration (iii) is based on the 3-by-3 coupler and uses the inherent phase shift between the three outputs of the coupler to decode the phase signal. The interrogation approach described in [10] is used to decode the phase signal. The return loss of isolators (1) and (2) are 75 and 71 dB respectively, measured with a high resolution optical time domain reflectometer.

$$\text{STRAIN RESOLUTION COMPARISON AND DISCUSSION}$$

The interferometric phase shift is related to the strain applied to the fiber laser, $\Delta \varepsilon$, by the same relation as for the interferometric sensor. However, the length term, $l$, now corresponds to the imbalance in the decoding interferometer. This would be made large (10-100m) to provide significant phase gain, such that the intrinsic laser noise can be made to dominate over all other noise sources. For the interrogation configurations above the fiber length imbalances are (i) 12.5m, (ii) 32m, and (iii) 42m, corresponding to phase gains of 0.78, 2.01 and 2.64 rad/MHz respectively.
14 µrad/Hz$^{1/2}$ for all three interrogation methods (apart from small variations in environmentally induced noise due to the measurements being taken at different times). In terms of minimum detectable length change, the MI achieves 210 fm/Hz$^{1/2}$ and the FLS achieves 0.76 fm/Hz$^{1/2}$, an improvement factor of 275. It follows that the fiber laser is capable of providing an increase in strain resolution by a factor of 18, compared with a 10cm length of fiber in an interferometric sensor. The strain resolution enhancement of the FLS is reduced as the length of interaction fiber in the interferometric sensor is increased. The strain resolution of the two sensors would be matched when the fiber interaction length in the interferometric sensor is 1.8m.

### Table 1: Measurement resolutions summary @ 2 kHz

<table>
<thead>
<tr>
<th>Sensor</th>
<th>Phase resolution (µrad/Hz$^{1/2}$)</th>
<th>Strain res. (p/Hz$^{1/2}$)</th>
<th>Min. det. length change (fm/Hz$^{1/2}$)</th>
</tr>
</thead>
<tbody>
<tr>
<td>MI (0.1m)*</td>
<td>2</td>
<td>2.10</td>
<td>210</td>
</tr>
<tr>
<td>DFB FLS</td>
<td>14</td>
<td>0.118</td>
<td>0.76</td>
</tr>
<tr>
<td>Improvement factor</td>
<td></td>
<td>18</td>
<td>275</td>
</tr>
</tbody>
</table>

* Effective fiber path imbalance of 1m, interaction length = 0.1m

For applications where the interaction length is short (< 1m), the FLS provides a significant sensitivity benefit over the MI sensor (see for example [11]). The maximum sensitivity benefit is achieved if the interaction length is equal to the cavity length (approximately 5 and 6.5mm for FL1 and 2 respectively). It should be noted that the frequency noise of the fiber laser deviates from the thermodynamic noise at frequencies below ~1-2kHz depending on environmental conditions. This 1/f type noise of currently uncertain origin is often observed at lower frequencies. Thus, the benefit of the FLS may also be degraded at lower frequencies due to this excess noise.

### References: