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MULTI-DISCIPLINARY SHAPE OPTIMIZATION OF A
ENTRY CAPSULE INTEGRATED WITH CUSTOM NEU-RAL NETWORK APPROXIMATION AND MULTI-FIDELITY
APPROACH

Claudio Cavallero
Exemplar s.r.l.
C.so Vittorio Emanuele II, 161
10139, Turin, Italy
Email: claudio.cavallero@exemplar.com

Alessio Davite
DIASP, Politecnico di Torino
C.so Duca degli Abruzzi, 29
10129, Turin, Italy
Email: alessio.davite@polito.it

Cosimo Chiarelli,
Vincenzo Mareschi,
Martins Sudars
Thales Alenia Space Italia s.p.a.
Strada Antica di Collegno, 253
10146, Turin, Italy
Email: {cosimo.chiarelli, vincenzo.mareschi, martins.sudars}@thalesaleniaspace.com

Federico Gallizio,
Optimad engineering s.r.l.
via Giacinto Collegno, 18
10143, Turin, Italy
Email: federico.gallizio@optimad.it

Edmondo Minisci
School of Engineering
University of Glasgow
G128QQ, Glasgow, UK
Email: edmondo.minisci@glasgow.ac.uk

Abstract. This paper describes a new integrated approach for the multi-disciplinary optimization of a entry capsule’s shape. Aerothermodynamics, Flight Mechanics and Thermal Protection System behaviors of a reference spaceship when crossing Martian atmosphere are considered, and several analytical, semi-empirical and numerical models are used. The multi-objective and multi-disciplinary optimization process implemented in Isight software environment allows finding a Pareto front of best shapes. The optimization process is integrated with a set of artificial neural networks, trained and updated by a multi-fidelity evolution control approach, to approximate the objective and constraint functions. Results obtained by means of the integrated approach with neural networks approximators are described and compared to the results obtained by a different optimization process, not using the approximators. The comparison highlights advantages and possible drawbacks of the proposed method, mainly in terms of calls to the true model and precision of the obtained Pareto front.
Key words: spacecraft shape optimization, multi-disciplinary optimization, meta-modelling, artificial neural networks, Isight.

1 INTRODUCTION

For future Mars exploration missions the most suitable protection from the high temperatures involved for both Mars entry modules and Earth reentry capsules is represented by ablative systems. Ablative materials are in fact characterized by a higher reliability than non-ablative protections (i.e., ceramics) and simpler process of manufacturing and assembly, hence leading to more contained costs. Furthermore, ablative systems have applications ranging a broader scale of applications, being potentially used in those zones (i.e., nose, stagnation points) exposed to high flux levels exceeding temperature limits of ceramic protections.

In the last years several European and US exploration and commercial space programs need ablative Thermal Protection System (TPS); see for instance the ESA project IXV, the NASA project COTS and the EU-US jointed initiatives ExoMars and Mars Sample Return Mission.

Through the funding support of Regione Piemonte - P.O.R./F.E.S.R. 2007/2013, the STEPS Program intended to produce a series of technological demonstrators (both virtual and physical) finalized to the development of systems for soft landing (lander) and surface mobility (rover) applicable for both robotic and human mission. This program envisages the realization and utilization of a set of laboratories equipped for tele-operations, of tools devoted to the concurrent design, simulation and virtual reality and of Moon and Mars simulated environments.

The Ablative Materials and Aerothermodynamics work package within STEPS Program involves some partners from industrial and academic institutions deeply rooted in Turin area. Partners are: Thales Alenia Space Italia, Politecnico di Torino, Università di Torino and two SMEs (Exemplar S.r.l. and Optimad engineering S.r.l.). Two are the main objectives of the Ablative Materials and Aerothermodynamics research team: a) development of an advanced composite material as core of the ablative TPS for Mars entry missions; b) development of an integrated code simulating the material behavior during an entry path through the Martian atmosphere and the shape optimization of ablative TPS shields. Basically such a code has to provide two main capabilities: a) to simulate the interaction between the external thermo-fluid dynamic and the ablative behavior, in terms of ablation, thermal conduction and surface recession; and b) to implement some optimization techniques relative to the shield shape and indeed to devise a general design procedure aimed to the pre-project of an entry vehicle optimizing a set of cost functionals.

In this framework, the shape optimization task addressed in the present work is to develop an efficient software tool that can be easily integrated within the design workflow of a capsule intended for a Martian mission and equipped with an ablative TPS. Such a kind of shape optimization has to take into account of several aspects of physics complexity where the accuracy of the physical models (hypersonic flow, chemical non-equilibrium, detailed kinetics, heat transfer, ablation) is often related to a large computational effort.
By means of different approaches and models, a wide and recent literature shows the application of the multi-disciplinary optimization techniques for designing the shape and the heat shield of an entry capsule.

In Brooks and Powers [1] and Shimoyama et al. [2] some reduced order models are used to evaluate the functional forms with saving computational resources. The first one implements a Proper Orthogonal Decomposition in order to approximate the quantities depending on the aerodynamics (lift, drag,...), with a drastic reduction of degrees of freedom. The authors remark that some difficulties are expected in the multiple-shock fitting and in the 3D extension. The second paper shows the shape optimization of a Mars exploratory airplane through an approach based on the improvement of the design for six sigma conventional algorithm, with a fine result in terms of robustness. In several papers of Johnson et al. (for instance [3] and [4]) some different multi-disciplinary strategies (a Differential Evolutionary Scheme and a Gradient-based algorithm) were adopted for the optimization of entry heat shield of vehicles devoted to trajectories through martian or terrestrial atmospheres. In Theisinger and Braun [5] an hypersonic entry aeroshell is optimized within the Isight environment by taking into account of the ballistic properties, the static stability and the volumetric efficiency evaluated with simple analytical and semi-empirical correlations. In Gogu et al. [6] an optimal mass tradeoff for an aeroassisted orbital transfer vehicle including both fuel mass and TPS mass for an optimized trajectory is presented. In this paper both reusable and ablative TPSs are considered. At last, Minisci et al. [7] present the robust multi-disciplinary design of a small scale unmanned space vehicle for reentry operations. In this paper the aerodynamic forces, thermal flux and TPS properties are evaluated by taking into account of uncertainties through a Monte-Carlo sampling procedure.

In this paper the first instance of the optimization procedure for the shield shape design is presented. An evolutionary algorithm is modified and hybridized with a multi-fidelity evolution control technique for the treatment of complex and expensive models. During the optimization process, individuals of the population are evaluated (in terms of objectives and constraints) by means of a set of approximated models, whose computing time can be considered much smaller than the one required by the true models. The approximators are initially trained on the basis of sampling of the search space, whose dimension must be limited to save computational time. Then, if the search landscape is not trivial, it is not possible to have an initial set of approximators which are globally correct. This means that, in order to avoid converging towards false optima, the database of solutions used to train the approximators must be integrated in due course, and the approximators updated. Here the evolution control approach is adopted for the on-line updating of the surrogate models.

Moreover, in order to further increase the saving of computational time, true models of different fidelity levels are considered here for each required functional. Models at lowest fidelity level are used to train the initial approximator and to update it at the early phases of the optimization process, while higher fidelity models are used at latter stages, when the optimizer is exploiting the optimal region of the search space.

The whole process is implemented in Isight. The used approximators are Artificial Neural Networks (ANNs), while the adopted evolutionary algorithm is the NSGA-
II[8] which is implemented in Isight.

The structure of this paper is as follows. In section 2 the reference shape of the capsule is illustrated and it is parameterized through some direct analytical formulas. In section 3 the physical models involved within the shape design are collected; a map of the relationships among cost functionals is provided. The section 4 is focused on a description of the multi-fidelity evolution control approach and on the integration within Isight software environment; here the implemented algorithms are in detail presented and discussed. The results and the values of the parameters used in the optimization are then described and discussed in section 6. A final conclusion sections ends the paper with a summary of the work and a note on the work that should be done in the immediate future.

2 PARAMETERIZATION

A reference shape of the capsule is here presented and parameterized. It is a classical Viking 3D axialsymmetrical geometry defined by two conical elements connected by two spherical junctions (see figure 1). A set of five design parameters describes such a shape: the nose and the corner radius \( R_n, R_c \), the forebody cone angle \( \theta_1 \), the rear cone angle \( \theta_2 \) and the capsule length \( L \). The base of the capsule is enforced to be \( r_b = 0.425 \text{ m} \). The capsule diameter \( D \) is defined as reference length, then all the length quantities are prescribed as non-dimensional values \( r_b/D, R_n/D, R_c/D, L/D \). In figure 1 the axial coordinates of the junction points between conical and spherical elements are shown \( F_1, N_1, M_1 \). The centers of curvature are \( O_c, O_n \). As the five design variables are chosen the junction points and the centers of curvature are univocally prescribed.

The parameterization of the shape is defined by a set of analytical expressions obtained by enforcing the continuity and the tangency at the boundary of each conical and spherical segment. Since the geometry is axialsymmetric, it can be described through the radius with respect to the axial coordinate. The function is defined piecewise as follows:
\[ r(x) = \begin{cases} r_b & \text{for } x = 0 \\ r_b + x \tan \theta_2 & \text{for } 0 < x \leq M_1O \\ \sqrt{R_c^2 - (S_O - x)^2} + S_Oc & \text{for } M_1O < x \leq N_1O \\ r(N_1O) - (x - N_1O) \tan \theta_1 & \text{for } N_1O < x \leq F_1O \\ \sqrt{R_n^2 - (x - O_nO)^2} & \text{for } F_1O < x \leq L \end{cases} \]  

(1)

where:

\[ SO = \left[ \frac{R_b}{\tan \theta_2} + L - R_n \left( 1 - \frac{1}{\sin \theta_1} \right) \right] \frac{\tan \theta_1}{\tan \theta_2 + \tan \theta_1} - \frac{R_b}{\tan \theta_2} \]

\[ S_cO = SO - \frac{R_c}{\sin \alpha_2} \cos \left( \theta_2 + \alpha_2 \right) \]

\[ S_cO_c = \left[ \frac{R_b}{\tan \theta_2} + L + R_n \left( \frac{1}{\sin \theta_1} - 1 \right) \right] \frac{\tan \theta_1 \tan \theta_2}{\tan \theta_1 + \tan \theta_2} - \frac{R_c \sin \left( \theta_2 + \alpha_2 \right)}{\sin \alpha_2} \]

\[ M_1O = SO - \left[ R_c \sin \theta_2 + \frac{R_c \cos \left( \theta_2 + \alpha_2 \right)}{\sin \alpha_2} \right] \]

\[ N_1O = SO + \left[ R_c \sin \theta_2 + \frac{R_c \cos \left( \theta_2 + \alpha_2 \right)}{\sin \alpha_2} \right] \]

\[ O_nO = L - R_n \]

and with \( \alpha_2 = (\pi - \theta_1 - \theta_2) / 2 \).

3 \textbf{AEROTHERMODYNAMICS AND FLIGHT MODELS}

Several physical models are integrated within the multi-disciplinary optimization loop in order to take into account effects of the hypersonic aerodynamics, ballistic trajectory, choice of ablative TPS.

A general framework on the relationships among the different physical models is summarized in figure 2. The flow diagram on the left shows the connections among the functionals involved during the optimization loop and the input dataset. On the top of the flow chart the parameterization of the geometry and the initial state of the mission represent the input values needed. The boxes point out the modules evaluating the functionals: from each module a dashed-line indicates the output dataset evaluated by the related functional. The solid-lines show the explicit dependencies existing among the functionals.

Given a set of design parameters (see the previous section) and the initial (at time \( t_0 \)) conditions of mission, the ballistic coefficient, the volume and the mass (the density of the capsule is assumed constant) are evaluated by the first functional module (‘BC’). The ballistic coefficient and the initial state dataset provide the input values to the second module (‘trajectory’) computing the history in time of the entry path. By knowing the shape of the capsule and the trajectory output dataset, the third module (‘stagnation heat flux’) and the fourth module (‘heat flux distribution’) compute the aerothermal response of the capsule for each position along the entry path. The last module (‘TPS recession’) requires the heat flux data.
and the geometry in order to estimate the recession of a TPS ablative layer along the frontal surface of the vehicle.

Figure 2: Map of the functionals and dependencies involved in the present multi-disciplinary optimization. On the right side the dashed-lines indicate for each functional which are the output yielded.

In the following paragraphs the physical models adopted to solve these functionals are described.

3.1 Modified Newtonian model

The classical expression of the ballistic coefficient is \( BC = \frac{M}{C_D A} \), where \( M \), \( C_D \), \( A \) represent the mass of the capsule, the drag coefficient and the frontal area respectively. The drag force depends on the hypersonic aerothermal field experienced by the blunt-body through the entry path. The Modified Newtonian Flow model (see [9]) is a well-known approach to a first approximation of the drag experienced by a capsule in hypersonic regime. The newtonian model theorized a stream of particles in rectilinear motion impacting a surface will lose all normal momentum but conserve all tangential momentum. This model provides an estimation of the pressure coefficient \( c_p = c_{p,\text{max}} \sin \left( \frac{V}{V_\infty} \cdot \mathbf{n} \right) \) where \( c_{p,\text{max}} \) is given by the Rayleigh’s Pitot tube formula:

\[
    c_{p,\text{max}} = \frac{2}{\gamma M_\infty^2} \left\{ \frac{(\gamma + 1)^2 + M_\infty^2}{4\gamma M_\infty^2 - 2(\gamma - 1)} \right\} \left[ \frac{1 - \gamma + 2\gamma M_\infty^2}{\gamma + 1} - 1 \right] \quad (2)
\]

Let us define a cartesian orthogonal frame of reference \( X, Y, Z \) with the origin 0 on the intersection between the nose and the axis of simmetry (figure 3). The nose and the cone surfaces can be defined through the following implicit formulation:

\[
    F(X, Y, Z) = (X - R_n)^2 + Y^2 + Z^2 - R_n^2 = 0 \quad \text{where} \quad 0 < X \leq F_1
\]

\[
    G(X, Y, Z) = \frac{Y^2}{\tan^2 \theta_1} + \frac{Z^2}{\tan^2 \theta_1} - \left[ X - R_n \left( \frac{1}{\sin \theta_1} - 1 \right) \right]^2 = 0 \quad \text{where} \quad F_1 < X \leq N_1
\]
For instance, the normal to the surface of the nose is computed by:

\[
\mathbf{n} = \frac{\nabla F}{|\nabla F|} = n_x \mathbf{i} + n_y \mathbf{j} + n_z \mathbf{k}
\]  

(4)

where \( \mathbf{i}, \mathbf{j}, \mathbf{k} \) are the Cartesian orthogonal unit vectors. By replacing the equations (2), (3) and (4) into \( c_p \) expression, the pressure distribution on the frontal surface of the capsule is evaluated. Therefore the drag \( D \) is computed by means of a numerical integration of the pressure on the frontal surface of the blunt body projected onto the far-field direction.

![Figure 3: Sphere and cone are described within a frame of reference at the nose’s center](image)

3.2 'Euler + boundary layer' model

Continuum aerodynamic characteristics are determined within an inviscid code with a time-dependent Euler calculation. Furthermore, an integral boundary layer code has been coupled to the Euler solver to obtain the viscous components of the forces and moments and the aerodynamic heating distribution on the body.

The approach followed is first to map the vehicle surface geometries onto a nearly horizontal surface, thus producing a coordinate grid closely aligned with the body geometry (see [10], [11]). This mapping is then used to generate the three-dimensional inviscid time-dependent equations of fluid motion written in terms of the new coordinates. A final transformation maps the transformed shock layer onto a regular, equally spaced grid.

For the solution of this steady inviscid flow problem is followed a time-asymptotic relaxation method. In this approach, the steady flow solution is sought as the limit of a time-dependent flow with time invariant boundary conditions as \( t \to \infty \). Because the time-dependent equations are hyperbolic, this method allows solution of the steady flow problem, which is a boundary value problem, as a mixed initial-boundary value problem with a forward-marching (in time) numerical technique.

For the solution of the Integral Boundary Layer a quasi-three-dimensional coverage of the entry body is provided by a series of 2D integral boundary layer calculations along inviscid surface streamlines. Equations are formulated in a streamline/surface normal coordinates. Along each streamline, ordinary differential equations for momentum and energy conservation are solved using an iterative implicit
algorithm. The integral equations use the momentum and energy thicknesses as the dependent variables, and include the effects of streamline curvature, pressure gradient, surface mass addition and the surface thermal condition. Closure of the equation set is provided by correlations relating skin friction coefficient, heat transfer coefficient, and displacement thickness to the dependent variables. Boundary layer edge conditions are determined as part of the solution by a mass balance procedure between the inviscid and boundary layer solutions.

An application of the 'Euler + boundary layer' code for a bi-conical hypersonic entry vehicle at incidence is displayed in figure 4. On the left picture the iso-lines of the pressure field normalized with the stagnation pressure are shown. On the right picture the streamlines are marked with a color gradient according to the wall heat flux.

3.3 Flight Dynamics model description and heat flux computation

A direct integration of the entry path is fine when large number of vehicles and mission parameters are being optimized or a closed loop guidance is present. Running the trajectory integration at each optimization iteration may slow down the whole loop unless other processes are numerically much more consuming than the trajectory integrator.

Two possible ways to deal with the speed requirements in the optimization environment are: a) pre-production of performance maps, or b) simplification of the trajectory propagator in order to run quicker under the optimization environment. The approach of performance maps generally works fine if the number of input parameters is small (usually less than four) and output results do not show sharp peaks or discontinuities. The results are prepared by a high-fidelity optimization tool and then saved in a database. The tool used in the present work to create the performance maps is FMST (Flight Management System Trainers\(^1\)), an in-house flight mechanics simulation tool developed by and sued internally by Thales Alenia Space Italia. Spherical planet assumption is applied over elliptic shape in order to

\(^1\)for more information see the web resource http://www.thalesalenia.com/Portfolio/Security/091006_D3S_ThalesFormation_Systems_Trainer/
maintain simple and rapid trajectory propagation approach for the ballistic entry. A custom-made Mars atmosphere model has been utilized.

The entry maximum heat fluxes profiles and load values can be either computed directly by empiric formulas or by numerical integration of the equations of motion and the applying some empiric methodology for heat flux computations. In general, when the flow is laminar (usually it is or can be assumed to be), the correlation between nose cap parameters, flight conditions and the convective heating rate at stagnation is described by the classical Detra, Kemp & Riddel formula (see [12]):

\[ \dot{q} = \frac{K_1}{\sqrt{R_N}} \left( \frac{\rho_\infty}{\rho_0} \right)^n \left( \frac{\nu}{\nu_0} \right)^m \]  

The coefficient \( K_1 \), \( m \) and \( n \) describe the correlation of the equation and its parameters with experimental heating rate. For \( \dot{q} \) expressed in \( W/m^2 \), according to [12], the coefficients are: \( K_1 = 113.5 \cdot 10^6 \), \( n = 0.5 \), \( m = 3.15 \), \( \rho_0 = 1.225 \ Kg/m^3 \) and \( \nu_0 = 7908 \ m/s \). For entry velocity below 9 km/s the radiative effects are negligible and hence not included in the evaluation.

In the present work, given the geometrical parameters described in section 2, the initial state of the mission and the related ballistic coefficient (as computed in section 3.1), the FMST estimates the time history of heat flux at stagnation and the heat load experienced by the capsule through the entry operation.

The Lees’ formulas [13] compute the convective heat flux distribution over an hemisphere and a blunt cone during a ballistic hypersonic entry. These expressions depend on some geometrical parameters (\( R_n \), \( \theta_1 \)), the undisturbed Mach number \( M_\infty \) and the specific heat ratio \( \gamma_\infty \). These formulas are valid in high hypersonic flight regime and in the limiting case of thermodynamic equilibrium where the heat transfer at the wall is achieved by conduction. The convective heat flux distribution was computed for the Mars Pathfinder test case reported in [14] and a first approximation accordance was encountered².

### 3.4 Ablation model

A complete modeling of the ablation process requires a conjugate heat transfer analysis, coupling a CFD solver for the external flux to a material response solver for the TPS, and possibly a detailed model to calculate the energy absorbed by the ablation process [15].

Being shape optimization the main scope of this study, an engineering correlation permitting a fast evaluation of surface recession is needed. The ‘heat of ablation’ (or \( Q^* \)) model assumes that ablation occurs at a fixed temperature and that there is a fixed amount of energy consumed per unit mass of material ablated [16]. This permits to relate the heat flux coming form the boundary layer, to the TPS density and recession rate:

\[ \dot{q}_{hw} = Q^* \cdot \rho_{TPS} \cdot \dot{s} \]  

²less than 10% error for the stagnation heat flux and less than 20% for the heat flux along the first 40% of curvilinear abscissa starting from the stagnation point.
where $\dot{q}_{hw}$ is the 'hot-wall' heat flux and $\dot{s}$ is the normal recession velocity. As reported in [16], the 'hot-wall' heat flux can be computed as a correction of the 'cold-wall' heat flux $\dot{q}_{cw}$ obtained as shown in section 3.3. The relationship between the 'hot-wall' and the 'cold-wall' yields $\dot{q}_{hw} = \dot{q}_{cw} \left(1 - \frac{H_w}{H_r}\right)$, where $H_w$ is the wall enthalpy and $H_r$ is the recovery enthalpy.

Given the heat flow distribution over the frontal surface of the capsule (as computed in section 3.3), the amount of shield recession can be calculated at every point of the entry trajectory\(^3\).

![Figure 5: The ablative TPS is modeled as a thin layer deposited on the frontal surface of the capsule (left picture). An example of surface recession at the end of the entry mission computed by the $Q^*$ model.](image)

In the present model the TPS is defined by a variable length layer with a maximum value at stagnation $\delta_{TPS}$, a linear percent decrease along the spherical segment $m_{\delta_{TPS}}$ and a constant thickness on the conical surface. At present $\delta_{TPS}$ and $m_{\delta_{TPS}}$ are not considered as design parameters but as constants within the optimization process ($\delta_{TPS}/D = 0.005$ and $m_{\delta_{TPS}} = 0\%$). In figure 5 the ablative TPS modeling is represented. On the left picture the dotted line marks the external boundary of the ablative at the start of entry. On the right picture the recession of the ablative layer close to the stagnation point at the nose is shown. The maximum recessed surface is computed as the maximum variation of ablative thickness between the start and the end of the mission.

4 Integrated Optimization Process

The integrated optimization process is implemented into Isight environment, which efficiently manages and integrates all the models pertinent to the involved disciplines. Moreover, within several Isight optimization methods are already implemented.

As previously introduced, the integrated method utilizes a multi-fidelity evolution control approach to evolve an initial random population of solutions towards the optimal region. The basic idea of evolution control (EC) approaches is to use,\(^3\)

\(^3\)Values of $Q^*$ can be evaluated experimentally, and have been published for the most used materials in [17] and [18]. The SLA-561S is the ablator considered in the present computation. It is a silicone based ablator used as the heatshield for the Mars Viking Missions (see [19]).
throughout the optimization process, both the true and the surrogated models in a way that reduces the total computational time, without loosing too much in precision. Due to the necessity to limit the number of training samples, if the search landscape is not trivial (linear or quadratic functions), it is almost impossible to construct a globally correct initial approximated model. Most likely, the approximation will bring the optimization algorithm to false optima, i.e. solutions that are optimal for the approximated model but are suboptimal for the true functions. This is the reason why model management or evolution control techniques have been formalized.

Jin et al. [20] propose two different approaches for the evolution control of the model: a) individual-based control and b) generation-based control. In the first approach, \( n_v \) individuals in the current population are chosen and evaluated with the true model at each generation. In the latter, the whole population is evaluated with the real model, every \( n_{geyc} \) generations, for \( n_{gv} \) generations, where \( n_{gv} < n_{geyc} \). The individuals evaluated with the true model are then introduced into the dataset in order to locally improve the surrogated model in the promising regions.

Here, in order to further increase the efficiency of the process, multi-fidelity approach is combined with EC. This means that during the process the adopted approximator is updated with outputs of models having different fidelity levels. In particular, low fidelity models are used to fill the first database, used to build the first instance of the approximator, then, during the optimization process, higher fidelity models are adopted to integrate the database and improve the precision of the approximated model within the optimal region.

For this work, a mixed individual-generation based EC is adopted and the general algorithm, whose main part is described in figure 6, is as follows:

1. set a) fidelity level, \( F_l \), to 0, b) predefined values for \( N_g, N_u^u, N_u^l, d_{sl}, d_{ll}, n_{c,max} \)
2. exploration of parameters space, performed with a Design Of Experiment (DOE)
3. initialization of first approximator
4. start of optimization process: generation of initial population
5. application of search heuristics to generate new population
6. if a cycle of \( N_u^u \) iteration is completed
   (a) explore new population to find individuals to upgrade the database;
   (b) if a cycle of \( N_u^l \) updates is completed, increase fidelity level, \( F_l = F_l + 1 \)
   (c) update the approximator with new database
   (d) re-evaluate the new population by means of the updated approximated model
7. if iteration = \( N_g \) STOP; else go to 5

Some more details are needed to explain the point 6.a. In order to update the database the entire new population is explored and individuals are inserted into the database if their distance from other solutions computed with the same fidelity level is \( \geq d_{ul} \) and if the number of currently sampled individuals is \(< n_{c,max} \). On the other hand, all the solutions of the database which were evaluated with a lower fidelity model and whose distance from last level solutions is \( \leq d_{ll} \) are discarded.
4.1 Artificial Neural Network

Evolution control does not depend on any specific approximation technique but the approximation approach strongly affects the outcome of any EC strategy. Here Artificial Neural Networks are used and, in particular, of MultiLayer Perceptron (MLP) type.

When dealing with ANNs, usually radial basis NNs are preferred due to the modest computational effort required to train them [21, 22], but in this case the generic MLP with one hidden layer was used, due to the expected better generalization in regions far for the training data.

The training process is based on a Bayesian regularization back-propagation [23], which is slow, but limits any overfitting problem. With the idea that the computational costs of initial training and online update are negligible if compared to the calls to the high-fidelity model, the additional computational efforts required by the Bayesian regularisation back-propagation can be neglected.

5 Problem settings

The optimization process is set as a multi objective one, with 3 objective functions:

\[
\min_{x \in X} M ; \min_{x \in X} S_R ; \max_{x \in X} V
\]  

and three constraint functions:

\[
q_{\text{max}} \leq 100[W/cm^2] ; \quad S_{R,\text{max}} \leq 70\% ; \quad D_A \leq 4[m]
\]  

where, \( M [kg] \) is the total mass of the vehicle, \( S_R [%] \) is the percentage of recessed surface for the TPS material, \( V [m^3] \) is the volume of the vehicle, \( q_{\text{max}} [W/cm^2] \), is the maximum heat flux experienced during the mission, \( S_{R,\text{max}} \), is maximum recession for the TPS surface, and \( D_A, [m] \), is the actual diameter.

Design parameters and their bounds are summarized in table 1, whilst table 2 summarizes the fidelity levels adopted for this test case.
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<table>
<thead>
<tr>
<th>description</th>
<th>name and bounds</th>
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<td>radius of ship’s nose [m]</td>
<td>$0.2 \leq R_n/D \leq 0.4$</td>
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<tr>
<td>radius of ship’s corner [m]</td>
<td>$0.02 \leq R_c/D \leq 0.04$</td>
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<td>front edge angle [°]</td>
<td>$55 \leq \theta_1 \leq 70$</td>
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<td>back edge angle [°]</td>
<td>$25 \leq \theta_2 \leq 55$</td>
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Table 1: Design parameters

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<th>model</th>
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<td>modified newtonian</td>
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Table 2: Table of levels of fidelity

6 Optimization setting and results

The process described in section 4 was performed by using NSGA-II code, already implemented into the Isight environment. A population of 32 individuals was evolved for 50 generations ($N_g = 50$). The initial DOE with models at 0 level ($F_l = 0$), required 50 solutions, while additional 27 evaluations of models at level 1 and 2, allowed the updating of the ANN approximators. All the ANNs were trained and updated considering a mean square error of 5%, while characteristic parameters for the ANN update were: $N_u^u = 4$, $N_u^l = 4$, $d_s = 0.2$, $d_l = 0.2$ (note that distances are computed on non-dimensional search space, with all variables $\in [0,1]$).

In figure 7 the obtained Pareto front is shown (front A) and compared with the results of a second optimization process, which does not use any approximator, but all the objective functions are computed by calling the models at fidelity level 2 (front B). Note that in figure the solutions of the original process (the one using the ANN approximators) are also shown recomputed by means of models at fidelity level 2 (front C). An analysis of the results shows that the differences between two fronts are close to 5%, which is congruent with the allowed error in the ANN training.

The second optimization process evolved a population of 12 individuals for 32 generations, requiring then to call the models 384 times. This means that the use of approximator in this case allowed to save 80% of the model calls. Moreover, the gain in computational time is even bigger, because most of the model calls to generate and update the approximators involved models at fidelity levels 0 and 1.
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Figure 7: Comparison of Pareto fronts with level 2 and integrated process. The solid-line circle and the dotted-line circle indicate the 'large volume' capsule and the 'small volume' capsule reported in figure 8.

Figure 8: Solutions with largest and smallest volume extracted from the Pareto front.

Characteristic shapes representing solutions at the extremes of the Pareto front are shown in figure 8.

7 Conclusions

In this paper a multi disciplinary design technique and its application to the shape optimization of a entry capsule is presented. The resulting routine integrates a modelling coupling several aerodynamic elements (ballistic coefficient, entry trajectory,...) with CFD and thermal analyses and structural models at different fidelity levels. The optimization process is implemented in the Isight environment and hybridizes a standard evolutionary algorithm with a multi-fidelity evolution control technique for the training and the online updating of a set of ANN approximators.

Although the considered test case, as demonstrated, could have been handled without the sophisticated multi-fidelity evolution control technique, nonetheless the
work allowed to set up and test with good results the new approach, which will be
adopted in the future as main design tool for advanced concepts.

Next immediate steps will be devoted to challenging and testing the proposed
approach with a more real case. The aim would be to reproduce with this new tool
preliminary design phases of already finished space projects, in order to compare
real/frozen results with the ones provided by the automated procedure.

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