# Web crippling strength of cold-formed stainless steel lipped channels with web perforations under end-two-flange loading

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(Received: ; Revised: ; Accepted: )

Abstract: This paper presents a finite element investigation into the web crippling strength of cold-formed stainless steel lipped channels with circular web perforations under end-two-flange (ETF) loading. The cases of web openings located both centred and offset to the load bearing plates, are considered. In order to take into account the influence of the circular web openings, a parametric study involving 2,190 finite element analyses was performed, covering duplex EN1.4462, austenitic EN1.4404 and ferretic EN1.4003 stainless steel grades; from the results of the parametric study, strength reduction factor equations are determined. The strength reduction factor equations are first compared to equations recently proposed for cold-formed carbon steel lipped channels. It is demonstrated that the strength reduction factor equations proposed for cold-formed carbon steel are conservative for the stainless steel grades by up to 10%. New coefficients for web crippling strength reduction factor equations are then proposed that can be applied to all three stainless steel grades.

Keywords: Cold-formed stainless steel; Finite element analysis; Lipped channel; Stainless

steel material grades; Strength reduction factor; Web crippling; Web perforation.

### Nomenclature

А	Web opening ratio;
a	Diameter of circular web opening;
$b_f$	Overall flange width of section;
bı	Overall lip width of section;
COV	Coefficient of variation;
d	Overall web depth of section;
Ε	Young's modulus of elasticity;
h	Depth of the flat portion of web;
L	Length of the specimen;
N	Length of the bearing plate;
$P_{\text{ASCE}}$	Nominal web crippling strength obtained from American Code;
Pas/NZS	Nominal web crippling strength obtained from Australian/New Zealand Code;
$P_{\mathrm{FEA}}$	Web crippling strength per web predicted from finite element (FEA);
$P_{\rm BS}$	Nominal web crippling strength obtained from British Code;
$P_{ m Euro}$	Nominal web crippling strength obtained from Euro Code;
$P_m$	Mean value of analysed-to-predicted load ratio;
R	Reduction factor;
Rp	Proposed reduction factor;
<i>r</i> <sub>1</sub>	Inside corner radius of section;
θ	Angle between web and bearing surface
t	Thickness of section;
$V_P$	Coefficient of variation of Analysed-to-predicted load ratio;
x	Horizontal clear distance of the web openings to the near edge of the bearing plate;
β	Reliability index;

#### **1** Introduction

Cold-formed stainless steel sections are most often used for both architectural and structural applications in conditions characterised by high corrosion aggressiveness; not only because they are aesthetically pleasing, but they also have favourable characteristics in terms of strength, durability and formability (Zhao *et al.* 2016; Nethercot *et. al.* 2011; Rosi *et al.* 2009). To provide ease of access for services, the use of web openings for such sections are also becoming popular in industry (Lawson *et al.* 2015) (see Fig. 1). Such web openings, however, result in the sections being more susceptible to web crippling, especially under concentrated loads in the vicinity of the openings.

The authors have recently proposed unified strength reduction factor equations for the web crippling strength of cold-formed stainless steel lipped channel-sections with circular web openings under the one and two flange loading conditions (Yousefi *et al.* 2016a, b, c, d). The equations covered three stainless steel grades: duplex grade EN 1.4462; austenitic grade EN 1.4404 and ferritic grade EN 1.4003. Similar equations for cold-formed carbon steel under end-one-flange loading condition have previously been proposed by Lian *et al.* (2016a, b), which was a continuation of the work of Uzzaman *et al.* (2012a, b, c, 2013) who had considered the two-flange loading conditions. When applied to the stainless steel grades, Yousefi *et al.* (2016b) showed that the equations proposed by Lian *et al.* (2016b) for the end-one-flange (EOF) loading condition were unconservative by up to 7%. Also, Yousefi *et al.* (2016d) showed that the equations proposed by Uzzaman *et al.* (2012a, c) for the interior-two-flange (ITF) loading condition were unconservative by up to 17%.

In the literature, for cold-formed stainless steel lipped channel-sections, only Krovink *et al.* (1995) has considered web crippling strength, but limited to sections without openings. Zhou and Young (2006, 2007, 2008, 2013) have considered the web crippling strength of cold-formed stainless steel tubular sections, again without openings. Research by Lawson *et* 

*al.* (2015), while concerned with circular web openings, focussed on the bending strength of the sections and not on the web crippling strength under concentrated loads (see Fig. 1).

In terms of cold-formed carbon steel, Keerthan and Mahendran (2012) and Keerthan *et al.* (2014) considered the web crippling strength of hollow flange channel beams, again without openings. Sundararajah *et al.* (2016) and Gunalan and Mahendran (2015) have also considered a Direct Strength Method approach for the web crippling strength of channel sections, again without openings. For cold-formed carbon steel lipped channel-sections, recent work has included Natario *et al.* (2014); Chen *et al.* (2015) and Gunalan and Mahendran (2015), all without openings.

This paper considers the case of the web crippling strength of cold-formed stainless steel lipped channels with circular web perforations under the end-two-flange (ETF) loading condition (see Figs. 2 and 3), and applicability of the proposed equations by Uzzaman *et al.* (2012c, 2013) to the same three stainless steel grades, namely the duplex grade EN 1.4462; austenitic grade 1.4404 and ferritic grade 1.4003. Similar to previous investigations, typical stress-strain curves for the three grades were taken from Chen and Young (2006) and Arrayago *et. al.* (2015).

#### 2 Experimental Investigation

For cold-formed carbon steel, Uzzaman *et al.* (2012b, 2013) conducted 100 end-twoflange (ETF) laboratory tests on lipped channel-sections with circular web openings subjected to web crippling (see Fig. 3). The size of the circular web openings was varied in order to investigate the effect of the web openings on the web crippling strength. All the test specimens were fabricated with web openings located at the mid-depth of the webs with centred and offset to the bearing plates. The laboratory test results were used to validate a non-linear geometry elasto-plastic finite element model (details of the model can be found in Uzzaman *et al.* (2012b, 2013)), which was then used for a parametric study to investigate the web crippling strength of cold-formed stainless steel lipped channel-sections with circular web openings under the end-two-flange (ETF) loading condition. Recommendations were proposed in the form of strength reduction factor equations, relating the loss of strength due to the web openings to the strength of the web without openings. The size of the circular web openings was varied in order to investigate the effect of the web opening size on the web crippling strength. Full details of both the laboratory tests can be found in Uzzaman *et al.* (2012b, 2013).

#### **3** Numerical Investigation

#### 3.1 General

In this study, the non-linear elasto-plastic general purpose finite element program ABAQUS (2014) was used to simulate the cold-formed stainless steel lipped channels with and without circular web perforations subjected to web crippling. The bearing plates, the lipped channel-section with circular web perforations and the interfaces between the bearing plates and the lipped-channel section were modelled. In the finite element model, the model was based on the centreline dimensions of the cross-sections. Details of the finite element models in ABAQUS (2014) are summarised below.

#### 3.2 Specimens labelling

The dimensions of the lipped channel-section modelled are given in Table 1. Fig. 4 shows the definition of the symbols used to describe the dimensions of the cold-formed carbon steel lipped channel-sections considered in the test programme. The same definitions were used in this numerical investigation; the models have been coded such the nominal dimension of the model and the length of the bearing plates as well as the ratio of the diameter of the circular web perforations to the depth of the flat portion of the webs (a/h) can be determined from the coding system. As an example, the label "142-N100-A0.2-FR" means the following. The first notation is the nominal depth of the models in millimeters. The notation "*N100*" indicates the length of bearing in millimeters (i.e. 100 mm). The notation "*A0.2*" indicates the ratio of the diameter of the holes to the depth of the flat portion of the webs (a/h) and are one of 0.2, 0.4, 0.6 and 0.8 (i.e. *A0.2* means a/h = 0.2; *A0.4* means a/h = 0.4 etc). Channel-sections without circular web perforations are denoted by "*A0*". The flanges unfastened and fastened cases are identified as "*FR*" and "*FX*", respectively.

#### 3.3 Geometry and material properties

In the finite element model, full model of the test set-up of Uzzaman *et al.* (2012b, 2013) was modelled, as shown in Fig 5. The stress-strain curves for duplex grade EN 1.4462; austenitic grade 1.4404 and ferritic grade 1.4003 were obtained from Chen and Young (2006) and Arrayago *et al.* (2015). The stress-strain curves were converted into true stress- strain curves as per the equations described in the ABAQUS manual (2014).

#### 3.4 Element type and mesh sensitivity

Fig. 5 shows details of a typical finite element mesh of the channel section and the bearing plates. The effect of different element sizes in the cross-section of the channel section was investigated to provide both accurate results and reduced computation time. Finite element mesh sizes were 5 mm  $\times$  5 mm for the cold-formed steel channel sections and 10 mm  $\times$  10 mm for the bearing plates.

Cold-formed steel lipped channels with and without web perforations were modelled using S4R shell element. The S4R is a four-node double curved thin or thick shell element with reduced integration and finite membrane strains. It is stated in the ABAQUS Manual (2014)

that the S4R element is suitable for complex buckling behaviour. The S4R has six degrees of freedom per node and provides accurate solutions to most applications. The bearing plates and load transfer block were modelled using analytical rigid plates and C3D8R element, which is suitable for three-dimensional modelling of structures with plasticity, stress stiffening, large deflection, and large strain capabilities. The solid element is defined by eight nodes having three translational degrees of freedom at each node.

#### 3.5 Loading and boundary conditions

Contact between the bearing plates and the cold-formed stainless steel section was modelled in ABAQUS using the *contact pairs* option. The interface between the bearing plates and the cold-formed stainless steel section were modelled using the surface-to-surface contact option. The bearing plates were the master surface, while the flange of the cross-section of stainless steel section was the slave surface extended up to the corners. Since the web-flange rounded transition will contact the bearing plates due to undergoing heavy deformation, the contact surfaces must include the corner elements and the flange. The two contact surfaces were not allowed to penetrate each other. The vertical load applied to the channel sections in the laboratory tests was modelled using displacement control method; an imposed displacement is applied to the nodes of the top bearing plate where the vertical load is applied. The top bearing plate was restrained against all degrees of freedom, except for the translational degree of freedom in the Y-direction. In the flanges fastened condition, the connector was used in the region where the flanges connected to the bearing plates. The nodes were prevented from translating in all degrees of freedom except in the y direction. Cartesian connectors were used to simulate the bolts instead of physically modelling bolts and holes. "CONN3D2" connector elements were used to model the in-plane translational stiffness i.e. x- and zdirections. The stiffness of the connectors element was 10 kN/mm, which Lim and Nethercot (2004a, b) suggestion would be suitable. In the y direction, the nodes were prevented from translating.

#### 3.6 Verification of finite element model

In order to verify the finite element model, the results of experimental study on lipped carbon steel channel sections 142×60×13-t1.3-N30 and 202×65×13-t1.4-N120 (flanges unfastened and fastened to the bearing plates) for the cases of web holes located centred and offset to the bearing plates under ETF loading condition conducted by Uzzaman *et al.* (2012b, 2013) (see Fig. 3) were compared to the results obtained from the finite element analyses (Figs. 6 and 7) using the same material as developed for stainless steel materials in this study. As can be seen, there is good agreement between the failure loads of the tested specimens and the finite element results. For cold-formed stainless steel lipped channel-sections, the numerical failure loads with and without circular web perforations were then determined for the three stainless steel grades: duplex grade EN 1.4462; austenitic grade 1.4404 and ferritic grade 1.4003 (see Table 1). These results were compared with the failure loads calculated in accordance with ASCE 8-02 (2002), BS 5950-5 (1998), Eurocode-3 (2006), NAS (2007) and AS/NZS 4600 (2005) (see Table 2). The failure loads predicted from the finite element results are generally similar to the standard codified failure loads of the sections.

#### 4 Parametric study for stainless steel grades

In this study, in order to investigate the effect of circular web perforations on the web crippling strength of cold-formed stainless steel lipped channels, a total of 2,190 finite element analyses of lipped channels with various dimensions and thicknesses were considered for the three stainless steel grades: duplex EN1.4462, austenitic EN1.4404 and ferritic EN1.4003. The web crippling strength predicted was influenced primarily by the ratio of the circular web opening depth to the flat portion of the web, the ratio of the bearing length to the flat portion

of the web and the location of the web hole as defined by the distance of the web perforation from the edge of the bearing divided by the flat portion of the web (Uzzaman et al. (2012a,b,c, 2013)). In order to find the effect of a/h, N/h and x/h on the web crippling strength of channel sections with circular web perforations, parametric studies were carried out considering the circular web perforations, different bearing plate lengths, the cross-section sizes and location of the circular web perforations. The cases of both flanges fastened and flanges unfastened to the bearing plates were considered.

The specimens consisted of three different section sizes, having thicknesses (t) ranging from 1.23 mm to 6.0 mm and web slenderness (h/t) values ranging from 111.7 to 157.8. The ratios of the diameter of the circular web perforations (a) to the depth of the flat portion of the webs (h) were 0.2, 0.4, 0.6 and 0.8. The ratios of the distance of the web perforations (x) to the depth of the flat portion of the web (h) were 0.2, 0.4 and 0.6. Bearing plates of lengths (N) equal to 100 mm, 120 mm and 150 mm are considered. For each series of specimens, the web crippling strengths of the sections without the web perforations were obtained. Thus, the ratio of the web crippling strengths for sections with web perforations divided by the sections without web perforations, which is the strength reduction factor (R), was used to quantify the degrading influence of the web perforations on the web crippling strengths.

The parametric study investigated the effect of the ratios of a/h, N/h and x/h. The web crippling strengths (PFEA) per web predicted from the FEA are summarised in Tables 3 to 5 for the duplex grade EN 1.4462. As can be seen from Tables 3 to 5, the failure load of the cold-formed stainless steel sections reduces as web perforations are present and continues to reduce with increase in the size of web perforations. The results demonstrate that the failure load obtained from the cold-formed stainless steel sections with the case of flanges fastened to bearing plates is in average 25% higher than the case of flanges unfastened to bearing plates for the sections with and without web perforations. In addition, for the case of web

perforations with a horizontal clear distance to the near edge of the bearing plates, the web crippling strength of the sections is higher than the case of web holes located centred above the bearing plates. Moreover, for the same section with different span and bearing plates, the failure loads were found to be different among the results. Based on the results, it was found that the failure load increases as the length of the bearing plates increases and as the length of the sections increases. The effect of the ratios of a/h, N/h and x/h on the reduction factor of the web crippling strength is shown in Fig. 8 for the C142 specimen.

Fig. 8(a) shows the ratio of the circular web perforation depth to the flat portion of the web (a/h) versus the strength reduction factor, for the three stainless steel grades. As can be seen, the reduction in strength increases as the parameter a/h increases for all three stainless steels, in particular for the ferritic grade with lower thickness (1.3mm). The reduction in strength of the ferritic grade 6 mm thick section is smallest and the reduction in strength increases from 0.2 to 0.6, the reduction in strength for the ferritic grade increases by 28%.

Fig. 8(b) shows the ratio of the bearing length to the flat portion of the web (N/h) versus the strength reduction factor, for the three stainless steel grades. As can be seen, the reduction in strength is not sensitive to the ratio N/h and the 6 mm thick sections have the smallest reduction in strength or the highest strength reduction factor.

Fig. 8(c) shows the ratio of the circular web hole location to the flat portion of the web (x/h) versus the strength reduction factor, for the three stainless steel grades. As can be seen, the reduction in strength is sensitive to the horizontal distance of the web perforations to the bearing plates. As the ratio of x/h decreases from 0.6 to 0.2, the strength reduction factor decreases by 7%. Also, it can again be seen that the reduction in strength is less for the austenitic grade compared to that of the other two stainless steel grades.

#### 5 Reduction factor comparison with Uzzaman et al. (2012c, 2013)

For ease of reference, the reduction factor equations proposed by Uzzaman *et al.* (2012c, 2013) are summarised below:

*For centered web opening:* 

Free case 
$$R_p = 0.90 - 0.60(\frac{a}{h}) + 0.12(\frac{N}{h}) \le 1$$
 (1)

Fixed case 
$$R_p = 0.95 - 0.50(\frac{a}{h}) + 0.08(\frac{N}{h}) \le 1$$
 (2)

For offset web opening:

Free case 
$$R_p = 0.95 - 0.49(\frac{a}{h}) + 0.17(\frac{x}{h}) \le 1$$
 (3)

Fixed case: 
$$R_p = 0.96 - 0.36(\frac{a}{h}) + 0.14(\frac{x}{h}) \le 1$$
 (4)

where the limits for the reduction factor in Eqs. (1)-(4) are  $h/t \le 156$ ,  $N/t \le 84$ ,  $N/h \le 0.63$ ,  $a/h \le 0.8$ , and  $\theta = 90^{\circ}$ .

In order to evaluate the applicability of the proposed equations to cold-formed stainless steel grades, an extensive statistical analysis was performed on all four proposed equations. Table 6 compares the reduction factors determined from the finite element models to Eqs. (1)-(4) for cases of centred and offset web perforation where the flanges are unfastened to the bearing plates.

As can be seen from Table 6, the four equations proposed by Uzzaman *et al.* (2012c, 2013) for carbon steel are conservative for the stainless steel grades, especially for the ferritic stainless steel grade which are conservative by up to 10%. As an example, for the ferritic stainless steel grade, for the centred web perforation case, the mean value of the web crippling reduction factors are 1.10 and 1.00 for the cases of flanges unfastened and fastened to the bearing plates, respectively; the corresponding values of COV are 0.05 and 0.10, respectively.

Similar values nearly are reported for the case of the duplex stainless steel grade. In the next section, new equations are proposed for each of the three stainless steel grades.

#### 6 Proposed strength reduction factors

Tables 3 to 5 show the dimensions considered and web crippling strengths of the stainless steel sections predicted from the finite element analysis. Using bivariate linear regression analysis, two unified strength reduction factor equations ( $R_p$ ) for three stainless steel grades with web openings are proposed. The equations are as follows:

Centred web opening: 
$$R_p = \alpha - \gamma(\frac{a}{h}) + \lambda(\frac{N}{h}) \le 1$$
 (5)

Offset web opening: 
$$R_p = \rho - \mu(\frac{a}{h}) - \zeta(\frac{x}{h}) \le 1$$
 (6)

The limits for the reduction factor Eqs. (5)-(6) are  $h/t \le 157.68$ ,  $N/t \le 120.97$ ,  $N/h \le 1.15$ ,  $a/h \le 0.8$ , and  $\theta = 90^{\circ}$ . The coefficients  $\alpha$ ,  $\gamma$ ,  $\lambda$ ,  $\rho$ ,  $\mu$  and  $\zeta$  of the equations are calibrated with the stainless steel finite element analysis results, and the coefficients are presented in Table 7.

#### 7 Comparison of numerical results with proposed reduction factors

For the three stainless steels grades, the values of the strength reduction factor (*R*) obtained from the numerical results are compared with the values of the proposed strength reduction factor (*R<sub>p</sub>*) calculated using Eqs. (5) and (6). The results for C142, C202 and C302 are shown in Figs. 9 to 12. In order to evaluate the accuracy of proposed equations, extensive statistical reliability analyses are performed. The results are summarized in Table 8. It should be noted, in calculating the reliability index, the resistance factor of  $\phi$ =0.85 was used, corresponding to the reliability index  $\beta$  from the North American Specification (NAS, 2007). The load combination of 1.2DL + 1.6LL as specified in the NAS specification was used in the

reliability analysis, where DL is the dead load and LL is the live load. In this study,  $M_m$ = 1.10 and  $V_M$ = 0.10, which are the mean and coefficients of variation for the material properties factors,  $F_m$ = 1.00 and  $V_F$ = 0.05, which are the mean and coefficients of variation for the fabrication factors, and  $V_q$ = 0.21, which is the coefficient of variation of load effect were used. According to the NAS specification, design rules are reliable if the reliability index is more than 2.5. As can be seen in Table 8, the proposed reduction factors are a good match with the numerical results for the both cases of flanges unfastened and flanges fastened to the bearing plates.

For example, for the centred circular web perforation, the mean value of the web crippling reduction factor ratios are 1.00 and 1.00 for the cases of flanges unfastened and flanges fastened to the bearing plates, respectively. The corresponding values of COV are 0.10 and 0.13, respectively. Similarly, the reliability index values ( $\beta$ ) are 2.62 and 2.51, respectively. For the offset circular web perforation, the mean value of the web crippling reduction factor ratios are 1.00 and 1.00 for the cases of flanges unfastened and flanges fastened to the bearing plates, respectively. The corresponding values of COV are 0.02 and 0.01, respectively. Similarly, the reliability index values ( $\beta$ ) are 2.84 and 2.85, respectively. Therefore, the proposed strength reduction factor equations are able to reliably predict the influence of the circular web perforations on the web crippling strengths of cold-formed stainless steel lipped channels under end-two-flange (ETF) loading.

#### 8 Conclusions

In this paper, an investigation into the effect of circular web perforations on the web crippling strength of cold-formed stainless steel lipped channels has been conducted. For this purpose, a parametric study comprising 2,190 lipped channels with various dimensions, thicknesses were considered for the three stainless steel grades, namely the duplex EN1.4462,

austenitic EN1.4404 and ferretic EN1.4003. Cases with and without circular web perforations under the end-two-flange (ETF) loading were considered with web holes located centred and offset to the bearing plates.

In order to take into account the influence of the circular web perforations, strength reduction factor equations were determined. The strength reduction factor equations were then compared to equations proposed by Uzzaman *et al.* (2012c, 2013) for cold-formed carbon steel. It was observed that the strength reduction factor equations proposed for cold-formed carbon steel are conservative for the stainless steel grades by up to 10%.

Based on the finite element results obtained from this study, new coefficients for web crippling strength reduction factor equations considering different web hole diameter and location in the web were proposed for both cases of flanges unfastened and flanges fastened to the bearing plates under end-two-flange (ETF) loading. Reliability analyses were performed in order to evaluate the reliability of the proposed strength reduction factors. It was demonstrated that the proposed strength reduction factors are generally conservative and agree well with the finite element results. The proposed new unified strength reduction factors are capable to produce reliable and safe yet not too conservative design values when calibrated with the resistance factor of 0.85 ( $\varphi = 0.85$ ) for end-two-flange (ETF) loading.

#### Acknowledgement

The University of Auckland Doctoral Scholarship is greatly acknowledged.

## **Declaration of Conflicting Interests**

The author(s) declared no potential conflicts of interest with respect to the research, authorship and/or publication of this article.

## Funding

The author(s) received no financial support for the research, authorship and/or publication of this article.

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**Table 1** Dimensions and web crippling strengths predicted from finite element analysis of cold-formed stainless steel lipped channels

Specimen	Web	Flange	Lip	Thickness	Length	Web		Duplex			Ferritic			Austenitic	
	d (mm)	b <sub>f</sub> (mm)	b <sub>l</sub> (mm)	t (mm)	L (mm)	a (mm)	P(A0) (kN)	P(Opening) (kN)	P(Opening) (kN)	P(A0) (kN)	P(Opening) (kN)	P(Opening) (kN)	P(A0) (kN)	P(Opening) (kN)	P(Opening) (kN)
								Offset	Centred		Offset	Centred		Offset	Centred
142-N100-MA0.6-FR	141.82	60.63	13.66	1.27	720.0	139.27	3.34	3.25	2.28	3.03	2.95	2.05	2.75	2.68	1.88
142-N120-MA0.6-FR	142.24	60.37	13.90	1.27	740.0	139.70	3.61	3.53	2.47	3.02	3.19	2.21	2.95	2.89	2.04
142-N150-MA0.4-FR	142.40	59.79	13.28	1.28	770.0	139.84	4.03	3.99	3.18	3.35	3.56	2.84	3.29	3.27	2.30
202-N100-MA0.4-FR	202.04	64.79	14.78	1.38	899.2	199.28	3.05	2.98	2.33	2.82	2.76	2.16	2.61	2.54	2.02
202-N100-MA0.6-FR	202.04	64.79	14.78	1.38	899.2	199.28	3.05	2.89	2.02	2.82	2.66	2.02	2.61	2.46	1.80
202-N120-MA0.4-FR	202.00	65.00	14.73	1.38	920.0	199.24	3.23	3.17	2.49	2.98	2.92	2.3	2.74	2.69	2.14
202-N120-MA0.6-FR	202.00	65.00	14.73	1.38	920.0	199.24	3.23	3.07	2.06	2.98	2.83	2.06	2.74	2.62	1.82
202-N150-MA0.4-FR	202.01	65.04	14.98	1.38	950.0	199.24	3.49	3.41	2.73	3.2	3.12	2.49	2.74	2.9	2.31
302-N100-MA0.6-FR	303.18	87.91	18.83	1.90	1200.0	299.37	5.40	5.1	3.66	5.09	4.79	3.49	5.53	4.55	3.68
302-N120-MA0.6-FR	303.07	87.95	18.26	1.90	1221.0	299.26	5.66	5.25	3.69	5.66	5.11	3.51	5.77	4.76	3.70
302-N150-MA0.6-FR	303.03	88.54	18.97	1.90	1249.0	299.23	6.04	5.93	3.79	5.67	5.36	3.79	6.19	5.11	3.80

(a) For the case of flanges unfastened to the bearing plates

(b) For the case of flanges fastened to the bearing plates

Specimen	Web	Flange	Lip	Thickness	Length	Web		Duplex			Ferritic			Austeniti	2
	d (mm)	b <sub>f</sub> (mm)	b <sub>l</sub> (mm)	t (mm)	L (mm)	a (mm)	P(A0) (kN)	P(Opening) (kN)	P(Opening) (kN)	P(A0) (kN)	P(Opening) (kN)	P(Opening) (kN)	P(A0) (kN)	P(Opening) (kN)	P(Opening) (kN)
								Offset	Centred		Offset	Centred		Offset	Centred
142-N100-MA0.6-FX	142.49	60.33	13.79	1.29	720.0	139.27	5.58	5.55	4.13	4.73	4.69	3.56	4.35	4.27	3.28
142-N120-MA0.6-FX	142.38	60.21	13.68	1.29	740.0	139.70	6.19	6.16	4.65	6.18	5.20	3.96	4.84	4.76	3.68
142-N150-MA0.4-FX	142.18	60.12	13.19	1.28	770.0	139.84	7.12	7.10	6.08	8.05	6.04	4.77	5.61	5.58	4.85
202-N100-MA0.4-FX	201.99	64.87	14.76	1.37	900.0	199.28	5.27	5.24	4.29	4.58	4.57	3.75	4.30	4.28	3.53
202-N100-MA0.6-FX	201.99	64.87	14.76	1.37	900.0	199.28	5.27	5.18	3.52	4.58	4.55	3.52	4.30	4.24	2.98
202-N120-MA0.4-FX	202.05	64.99	14.82	1.41	920.0	199.24	5.72	5.69	4.69	4.96	4.94	4.09	4.64	4.62	3.83
202-N120-MA0.6-FX	202.05	64.99	14.82	1.41	920.0	199.24	5.72	5.64	3.63	4.96	4.92	3.29	4.64	4.59	3.06
202-N150-MA0.4-FX	202.00	64.93	15.00	1.41	950.0	199.24	6.43	6.38	5.33	5.57	5.55	4.67	5.43	5.20	4.33
302-N100-MA0.6-FX	303.20	88.24	18.66	1.96	1199.0	299.37	9.56	9.30	6.55	8.40	8.21	6.02	7.99	7.83	5.68
302-N120-MA0.6-FX	303.50	88.53	18.36	1.93	1219.0	299.26	10.17	3.52	6.71	8.93	8.78	6.16	8.47	8.40	5.21
302-N150-MA0.6-FX	303.85	88.71	18.41	1.90	1248.3	299.23	11.14	10.98	6.94	9.80	9.74	6.35	9.31	9.26	6.20

Specimen	Web slenderness	Bearing length to thickness ratio	Bearing length to web height ratio	Inside bend radius ratio	Failure load per web	Web crippling strength per web predicted from current design codes						Comparison					
	h/t	N/t	N/h	$r_i/t$	P <sub>FEA</sub>	$P_{\rm NAS}$	$P_{ASCE}$	P <sub>BS</sub>	P <sub>Euro</sub>	P <sub>AS/NZS</sub>	$P/P_{\rm NAS}$	P/P <sub>ASCE</sub>	P/ P <sub>AS/NZS</sub>	$P/P_{BS}$	$P/P_{Euro}$		
					(KN)	(KIN)	(KN)	(KN)	(KN)								
142-N100-A0	114.01	81.30	0.71	3.90	2.94	3.12	2.56	2.37	2.54	3.12	0.94	1.15	0.94	1.24	1.16		
142-N120-A0	111.67	96.01	0.86	3.84	3.05	3.24	2.73	2.52	2.78	3.24	0.94	1.12	0.94	1.21	1.10		
142-N150-A0	112.64	120.97	1.07	3.87	3.37	3.44	3.06	2.82	3.26	3.44	0.98	1.10	0.98	1.20	1.03		
202-N100-A0	147.62	74.07	0.50	3.70	3.17	2.94	2.52	2.49	2.62	2.94	1.08	1.26	1.08	1.27	1.21		
202-N120-A0	147.68	88.89	0.60	3.70	3.41	3.27	2.97	2.93	3.19	3.27	1.04	1.15	1.04	1.16	1.07		
202-N150-A0	147.72	111.11	0.75	3.70	3.76	3.48	3.32	3.27	3.71	3.48	1.08	1.13	1.08	1.15	1.01		
302-N100-A0	157.69	52.63	0.33	2.63	5.62	5.40	5.28	5.34	5.34	5.40	1.04	1.07	1.04	1.05	1.05		
302-N120-A0	157.13	63.16	0.40	2.63	6.02	5.47	5.43	5.49	5.58	5.47	1.10	1.11	1.10	1.10	1.08		
302-N150-A0	157.67	78.95	0.50	2.63	6.64	5.59	5.71	5.76	6.12	5.59	1.19	1.16	1.19	1.15	1.09		
Mean, Pm								-			1.04	1.14	1.04	1.17	1.09		
Coefficient of varia	tion										0.15	0.05	0.05	0.08	0.06		

 Table 2 Comparison of numerical results with design strengths for the case of flanges fastened to bearing plates without web hole

Specimen	Thickness	Unfaste	ened FEA	load per	web, P <sub>FI</sub>	ĒA	Fastened FEA load per web, $P_{\rm FEA}$					
	t	A(0)	A(0.2)	A(0.4)	A(0.6)	A(0.8)	A(0)	A(0.2)	A(0.4)	A(0.6)	A(0.8)	
	(mm)	(kN)	(kN)	(kN)	(kN)	(kN)	(kN)	(kN)	(kN)	(kN)	(kN)	
142-N100	1.27	3.34	3.01	2.62	2.27	2.01	5.57	5.16	4.66	4.13	2.98	
142-N100	4.00	46.82	40.39	33.83	27.62	20.82	74.15	67.29	58.58	48.78	25.39	
142-N100	6.00	114.74	99.47	83.03	51.75	40.15	169.62	154.59	133.85	106.70	46.40	
142-N120	1.27	3.60	3.26	2.84	2.46	2.52	6.18	5.74	5.20	4.65	3.60	
142-N120	4.00	51.20	44.74	37.81	31.30	24.73	84.10	77.00	67.97	58.16	33.89	
142-N120	6.00	125.16	109.72	92.97	76.91	55.31	194.88	176.45	155.14	130.30	69.02	
142-N150	1.28	4.02	3.66	3.18	2.78	2.40	7.11	6.66	6.08	5.46	4.64	
142-N150	4.00	57.70	51.29	43.94	37.26	30.43	97.98	90.89	81.73	71.58	55.16	
142-N150	6.00	140.18	124.51	106.81	91.07	73.48	227.83	208.56	186.57	162.23	116.43	
202-N100	1.39	3.04	2.75	2.33	2.01	1.82	5.27	4.84	4.29	3.52	2.93	
202-N100	4.00	37.72	31.90	26.13	22.25	19.60	62.08	55.33	46.59	36.25	25.35	
202-N100	6.00	96.81	81.88	64.30	53.00	40.75	151.34	132.80	111.58	79.65	47.52	
202-N120	1.39	3.23	2.92	2.48	2.05	1.86	5.72	5.28	4.69	3.63	3.02	
202-N120	4.00	40.61	34.56	28.34	22.71	19.95	69.47	62.50	52.26	37.39	26.13	
202-N120	6.00	105.25	89.91	70.91	54.34	41.67	169.64	149.80	127.15	82.16	48.80	
202-N150	1.39	3.48	3.17	2.72	2.28	1.90	6.41	5.96	5.33	4.64	3.14	
202-N150	4.00	45.22	39.37	31.99	25.88	20.46	80.39	70.52	63.51	52.42	27.24	
202-N150	6.00	117.65	102.26	82.37	64.36	42.96	196.97	176.28	151.83	123.27	50.82	
302-N100	1.98	5.39	4.84	4.08	3.65	3.22	9.56	8.65	7.54	6.55	5.43	
302-N100	4.00	30.04	27.10	21.89	19.76	17.51	48.94	43.60	37.03	31.95	24.49	
302-N100	6.00	74.39	65.16	54.03	48.56	41.97	124.84	108.66	92.01	77.88	52.93	
302-N120	1.98	5.65	5.05	4.11	3.69	3.28	10.17	9.25	7.78	6.71	5.55	
302-N120	4.00	31.77	27.10	22.14	19.99	17.72	53.45	47.87	38.59	32.72	24.99	
302-N120	6.00	83.43	69.47	55.29	49.37	42.81	139.05	121.14	96.43	79.90	54.08	
302-N150	1.99	6.04	5.43	4.48	3.79	3.47	11.14	10.23	8.88	6.94	5.73	
302-N150	4.00	34.26	29.30	23.89	20.43	18.14	60.53	54.77	45.38	33.87	25.73	
302-N150	6.00	91.23	76.74	60.97	50.51	43.66	156.18	139.21	114.85	82.77	55.61	

**Table 3** Web crippling strengths of duplex stainless steel sections predicted from finite elementanalysis: a/h for centred circular web perforation

Specimen	Thickness	Unfaste	ened FEA	load per v	veb, P <sub>FEA</sub>	Faster	ned FEA l	oad per w	eb, P <sub>FEA</sub>
	t	A(0)	A(0.2)	A(0.4)	A(0.6)	A(0)	A(0.2)	A(0.4)	A(0.6)
	(mm)	(kN)	(kN)	(kN)	(kN)	(kN)	(kN)	(kN)	(kN)
142-N100	1.27	3.34	3.31	3.27	3.25	5.58	5.57	5.56	5.55
142-N100	4.00	46.82	46.80	46.73	46.62	74.15	74.13	74.12	74.11
142-N100	6.00	114.74	114.69	114.58	114.37	171.90	171.89	171.88	171.85
142-N120	1.27	3.62	3.60	3.58	3.53	6.19	6.18	6.17	6.16
142-N120	4.00	51.21	51.18	51.11	50.99	84.10	84.08	84.07	84.05
142-N120	6.00	125.16	125.11	124.98	124.76	194.88	194.85	194.84	194.80
142-N150	1.28	4.03	4.02	3.99	3.95	7.12	7.11	7.10	7.09
142-N150	4.00	57.70	57.67	57.60	57.48	98.28	98.27	98.26	98.23
142-N150	6.00	140.18	140.13	139.99	139.77	227.83	227.81	227.80	227.76
202-N100	1.39	3.05	3.04	2.98	2.89	5.27	5.26	5.24	5.18
202-N100	4.00	37.72	37.69	37.63	37.50	62.08	62.06	62.05	62.03
202-N100	6.00	96.81	96.76	96.68	96.51	151.35	151.31	151.29	151.26
202-N120	1.39	3.23	3.22	3.17	3.07	5.72	5.71	5.69	5.64
202-N120	4.00	40.61	40.58	40.52	40.40	69.47	69.45	69.43	69.42
202-N120	6.00	105.25	105.19	104.93	104.93	169.64	169.63	169.60	169.56
202-N150	1.39	3.49	3.47	3.41	3.30	6.43	6.41	6.38	6.33
202-N150	4.00	45.23	45.18	45.09	44.62	80.39	80.36	80.35	80.32
202-N150	6.00	117.65	117.57	117.42	117.13	196.97	196.93	196.91	196.85
302-N100	1.98	5.40	5.38	5.28	5.10	9.56	9.55	9.48	9.30
302-N100	2.00	30.04	29.99	29.82	29.44	48.96	48.93	48.91	48.85
302-N100	4.00	78.33	78.26	78.13	77.84	65.08	57.86	44.18	43.35
302-N120	1.98	5.66	5.63	5.28	5.25	5.32	4.72	3.91	3.52
302-N120	2.00	31.77	31.73	31.62	31.35	28.89	24.42	20.10	18.27
302-N120	4.00	83.43	82.34	82.20	81.90	75.69	62.55	49.29	44.31
302-N150	1.99	6.04	6.02	5.93	5.75	11.14	11.12	11.07	10.98
302-N150	2.00	34.27	34.22	34.12	33.88	31.02	26.31	21.63	18.63
302-N150	4.00	91.23	91.14	91.03	90.80	82.88	69.35	53.65	45.33

**Table 4** Web crippling strengths of duplex stainless steel sections predicted from finite elementanalysis: a/h for offset circular web perforation

Specimen	Thickness	Unfast	ened FEA	load per w	eb, P(FEA)	Faste	ned FEA 1	oad per we	eb, P <sub>FEA</sub>
	t	X(0)	X(0.2)	X(0.4)	X(0.6)	X(0)	X(0.2)	X(0.4)	X(0.6)
	(mm)	(kN)	(kN)	(kN)	(kN)	(kN)	(kN)	(kN)	(kN)
142-N100-A0	1.27	3.34	3.34	3.34	3.34	5.58	5.58	5.58	5.58
142-N100-A0.2	1.27	3.15	3.18	3.22	3.24	5.39	5.43	5.47	5.51
142-N100-A0.4	1.27	2.86	2.96	3.03	3.09	5.12	5.21	5.30	5.38
142-N100-A0.6	1.27	2.59	2.72	2.83	2.93	4.87	5.01	5.13	5.24
142-N120-A0	1.27	3.61	3.61	3.61	3.61	6.18	6.18	6.18	6.18
142-N120-A0.2	1.27	3.43	3.47	3.49	3.52	6.01	6.04	6.08	6.12
142-N120-A0.4	1.27	3.16	3.24	3.31	3.37	5.75	5.84	5.92	6.00
142-N120-A0.6	1.27	2.91	3.03	3.12	3.22	5.54	5.68	5.79	5.89
142-N150-A0	1.28	4.03	4.03	4.03	4.03	7.11	7.11	7.11	7.11
142-N150-A0.2	1.28	3.87	3.89	3.92	3.94	6.95	6.98	7.02	7.05
142-N150-A0.4	1.28	3.62	3.67	3.75	3.81	6.70	6.79	6.87	6.95
142-N150-A0.6	1.28	3.40	3.50	3.59	3.68	6.49	6.64	6.75	6.85
202-N100-A0	1.39	3.05	3.05	3.05	3.05	5.27	5.27	5.27	5.27
202-N100-A0.2	1.39	2.86	2.90	2.92	2.95	5.04	5.07	5.11	5.14
202-N100-A0.4	1.39	2.56	2.66	2.72	2.78	4.71	4.79	4.87	4.94
202-N100-A0.6	1.39	2.26	2.39	2.48	2.53	4.36	4.47	4.57	4.66
202-N120-A0	1.39	3.23	3.23	3.23	3.23	5.72	5.72	5.72	5.72
202-N120-A0.2	1.39	3.05	3.09	3.11	3.13	5.50	5.53	5.56	5.60
202-N120-A0.4	1.39	2.75	2.85	2.91	2.97	5.18	5.25	5.33	5.40
202-N120-A0.6	1.39	2.46	2.58	2.68	2.77	4.88	4.99	5.08	5.17
202-N150-A0	1.45	3.49	3.49	3.49	3.49	6.41	6.41	6.41	6.41
202-N150-A0.2	1.45	3.32	3.35	3.37	3.39	6.21	6.23	6.27	6.30
202-N150-A0.4	1.45	3.04	3.11	3.18	3.24	5.90	5.97	6.05	6.15
202-N150-A0.6	1.45	2.75	2.86	2.96	3.05	5.64	5.75	5.84	5.92
302-N100-A0	1.98	5.40	5.40	5.40	5.40	9.56	9.56	9.56	9.56
302-N100-A0.2	1.98	5.03	5.09	5.15	5.22	8.99	9.07	9.12	9.18
302-N120-A0	1.96	5.66	5.66	5.66	5.66	10.00	10.00	10.00	10.00
302-N120-A0.2	1.96	5.27	5.33	5.40	5.47	9.64	9.70	9.75	9.81
302-N120-A0.4	1.96	4.83	4.87	5.00	5.15	9.11	9.19	9.24	9.36
302-N150-A0	1.99	6.04	6.04	6.04	6.04	11.14	11.14	11.14	11.14
302-N150-A0.2	1.99	5.67	5.73	5.80	5.87	10.68	10.74	10.80	10.84
302-N150-A0.4	1.99	5.07	5.24	5.40	5.55	10.04	10.19	10.31	10.42

**Table 5** Web crippling strengths of duplex stainless steel sections predicted from finite elementanalysis: x/h for offset circular web perforation

 Table 6 Comparison of web crippling strength reduction factor for cold-formed stainless steel lipped channels with reduction factors equations proposed by Uzzaman *et al.* (2012c, 2013)

 (a) Flanges unfastened to the bearing plates

Specimen	Factored resistance (Eq. 1)	Factored resistance (Eq. 3)			Reduction factor				Compariso	n with resistanc $R/R_{Uzza}$	e from Uz	zaman <i>et a</i>	l
			Duplex		Ferritic		Austenitic	Duplex		Ferritic		Austenitic	
			R=P(Opening)/P(A)	))	R=P(Opening)/P(A0)	)	R=P(Opening)/P(A0)						
	Centred	Offset	Centred	Offset	Centred	Offset	Centred Offse	et Centred	1 Offset	Centred	Offset	Centred	Offset
142-N100-MA0.6-FR	0.63	0.92	0.68	0.92	0.68	0.99	0.69 0.9	8 1.09	1.08	1.08	1.07	1.09	1.06
142-N120-MA0.6-FR	0.63	0.92	0.68	0.93	0.73	0.99	0.69 0.9	8 1.08	1.07	1.16	1.07	1.10	1.07
142-N150-MA0.4-FR	0.75	1.03	0.79	0.96	0.78	0.99	0.79 0.9	9 1.05	0.96	1.04	0.96	1.05	0.96
202-N100-MA0.4-FR	0.73	1.02	0.77	0.93	0.77	0.98	0.78 0.9	3 1.05	0.96	1.05	0.96	1.06	0.96
202-N100-MA0.6-FR	0.63	0.90	0.66	0.98	0.72	0.95	0.69 0.9	5 1.05	1.05	1.14	1.05	1.10	1.05
202-N120-MA0.4-FR	0.73	1.02	0.77	0.93	0.77	0.98	0.78 0.9	8 1.05	0.96	1.05	0.96	1.06	0.96
202-N120-MA0.6-FR	0.63	0.91	0.64	0.88	0.69	0.95	0.66 0.9	6 1.01	1.06	1.09	1.05	1.05	1.06
202-N150-MA0.4-FR	0.74	1.02	0.78	0.95	0.78	0.98	0.78 0.9	8 1.06	0.96	1.06	0.96	1.07	0.97
302-N100-MA0.6-FR	0.58	0.96	0.68	0.98	0.69	0.94	0.66 0.9	4 1.17	0.98	1.19	0.98	1.15	0.97
302-N120-MA0.4-FR	0.58	0.97	0.65	0.95	0.62	0.96	0.64 0.9	4 1.12	0.95	1.07	0.99	1.10	0.97
302-N150-MA0.4-FR	0.58	0.99	0.63	0.99	0.67	0.95	0.61 0.9	5 1.08	0.96	1.15	0.96	1.05	0.96
Mean, Pm	# #	#	#	#	#	#		1.07#	1.00	1.10	1.00	1.08	1.00
Coefficient of	#		#	#	#	#							
variation, Vp	#	#						0.04#	0.06	0.05	0.05	0.03	0.05

## (b) Flanges fastened to the bearing plates

Specimen	Factored resistance (Eq. 2)	Factored resistance (Eq. 4)		Reduction factor					Comparison with resistance from Uzzaman <i>et al</i> $R/R_{Uzaman}$					
			Duplex		Ferritic		Austenitic		Duplex		Ferritic		Austenitic	
			R=P(Hole)/P(A0)		R=P(Hole)/P(A0)		R=P(Hole)/P(A0)	)						
	Centred	Offset	Centred	Offset	Centred	Offset	Centred	Offset	Centred	Offset	Centred	Offset	Centred	Offset
142-N100-MA0.6-FX	0.71	0.96	0.74	1.00	0.75	0.99	0.75	0.98	1.05	1.03	1.06	1.03	1.07	1.02
142-N120-MA0.6-FX	0.71	0.96	0.75	0.99	0.64	0.99	0.76	0.99	1.06	1.03	0.90	1.03	1.07	1.02
142-N150-MA0.4-FX	0.81	1.05	0.86	1.00	0.59	0.99	0.86	0.99	1.05	0.95	0.73	0.95	1.07	0.95
202-N100-MA0.4-FX	0.80	1.03	0.81	1.00	0.82	0.99	0.78	1.00	1.02	0.97	1.03	0.96	0.97	0.96
202-N100-MA0.6-FX	0.71	0.95	0.67	0.98	0.77	0.99	0.69	0.99	0.94	1.03	1.08	1.05	0.97	1.04
202-N120-MA0.4-FX	0.80	1.04	0.82	1.00	0.82	1.00	0.78	1.00	1.03	0.97	1.03	0.97	0.98	0.96
202-N120-MA0.6-FX	0.71	0.95	0.64	0.99	0.66	0.99	0.66	0.99	0.90	1.04	0.93	1.04	0.93	1.04
202-N150-MA0.4-FX	0.80	1.03	0.83	0.99	0.84	0.99	0.78	0.96	1.04	0.96	1.05	0.96	0.98	0.93
302-N100-MA0.6-FX	0.68	1.00	0.68	0.97	0.72	0.98	0.66	0.98	1.01	0.98	1.06	0.98	0.98	0.98
302-N120-MA0.4-FX	0.78	1.01	0.76	0.98	0.79	0.98	0.78	0.99	0.98	0.66	1.01	0.99	1.00	0.98
302-N150-MA0.4-FX	0.79	1.03	0.80	0.99	0.81	0.99	0.80	1.00	1.01	0.97	1.02	1.00	1.01	0.97
Mean, Pm	#	#	#	#	#	#	#		1.01	1.00	1.00	1.01	1.00	1.01
Coefficient of		#	#	#	#	#	#							
variation, Vp	#								0.05	0.04	0.10	0.04	0.05	0.04

	Stainlass staal grada	Coofficient	Unfastened to	Fastened to
	Stanness steel grade	Coefficient	bearing plates	bearing plates
		α	0.97	1.02
		γ	0.59	0.76
	$FN \pm 4462$ (Duplay)	λ	0.01	0.09
	EN 1.4402 (Duplex)	ρ	0.93	0.98
		$\mu$	0.03	0.02
		ζ	0.05	0.01
		α	0.91	0.98
		γ	0.57	0.64
Steen -th as heating for the East (5. ()	EN 1.4404	λ	0.09	0.06
Strength reduction factor Eqs. (3-6)	(Austenitic)	ρ	0.94	1.01
		$\mu$	0.03	0.04
		ζ	0.04	0.06
		α	0.97	1.04
		γ	0.62	0.73
	EN 1 4002 (Equitio)	λ	0.04	0.07
		ρ	0.94	0.99
		$\mu$	0.03	0.07
		ζ	0.04	0.05

## Table 7 Coefficients of the proposed strength reduction factor equations

		Centred circula $R_{(FEA)}$	ar web opening $\frac{1}{R_p}$	Offset circular web opening $R_{(FEA)}/R_p$			
Stainless steel grade	Statistical parameters	Unfastened to bearing plates	Fastened to bearing plates	Unfastened to bearing plates	Fastened to bearing plates		
	Number of data	108	108	81	81		
	Mean, $P_m$	1.00	1.00	1.00	1.00		
EN 1.4462 (Duplex)	Coefficient of variation, $V_p$	0.10	0.13	0.02	0.01		
	Reliability index, $\beta$	2.62	2.51	2.84	2.85		
	Resistance factor, $\phi$	0.85	0.85	0.85	0.85		
	Number of data	105	105	81	81		
	Mean, $P_m$	1.00	1.00	1.00	1.00		
EN 1.4404 (Austenitic)	Coefficient of variation, $V_p$	0.09	0.11	0.02	0.02		
	Reliability index, $\beta$	2.66	2.54	2.84	2.84		
	Resistance factor, $\phi$	0.85	0.85	0.85	0.85		
	Number of data	108	108	81	81		
	Mean, $P_m$	1.00	1.00	1.00	1.00		
EN 1.4003 (Ferritic)	Coefficient of variation, $V_p$	0.12	0.12	0.01	0.01		
	Reliability index, $\beta$	2.54	2.52	2.85	2.85		
	Resistance factor, $\phi$	0.85	0.85	0.85	0.85		

### **Figure Captions**

Fig. 1. Photograph of cold-formed stainless steel lipped channel-sections with circular web openings after Lawson *et. al.* (2015)

Fig. 2. End-two-flange (ETF) loading condition after Uzzaman et al. (2012b, 2013)

(a) With circular web opening centred from bearing plates

(b) With circular web openings offset from bearing plates

**Fig. 3.** Experimental analysis of cold-formed steel lipped channel-sections under end-two-flange (ETF) loading condition for the case of flanges unfastened and fastened to bearing plates after Uzzaman *et al.* (2012b, 2013);

(a) Centred circular web opening

(b) Offset circular web opening

Fig. 4. Definition of symbols

**Fig. 5.** Deformed shape predicted from finite element analysis of cold-formed steel lipped channels under end-two-flange (ETF) loading condition for case of flanges unfastened and fastened to bearing plates;

(a) Centred circular web perforation

(b) Offset circular web perforation

Fig. 6. Comparison of finite element results and experimental results by Uzzaman *et al.* (2012b) for sections with centred circular web opening

(a) For the case of flanges unfastened to bearing plates

(b) For the case of flanges fastened to bearing plates

Fig. 7. Comparison of finite element results and experimental results by Uzzaman *et al.* (2013) for sections with offset circular web opening

(a) For the case of flanges unfastened to bearing plates

(b) For the case of flanges fastened to bearing plates

Fig. 8. Variation in reduction factors for C142 section for the case of flanges unfastened to bearing plates

(a) with a/h for centered circular web perforation

(b) with N/h for centered circular web perforation

(c) with x/h for offset circular web perforation

Fig. 9. Comparison of strength reduction factor for C142 section with centered circular web perforation

(a) For the case of flanges unfastened to bearing plates

(b) For the case of flanges fastened to bearing plates

Fig. 10. Comparison of strength reduction factor for C142 section with offset circular web perforation

- (a) For the case of flanges unfastened to bearing plates
- (b) For the case of flanges fastened to bearing plates
- Fig. 11 Comparison of strength reduction factor for sections with centered circular web perforation
- (a) For the case of flanges unfastened to bearing plates
- (b) For the case of flanges fastened to bearing plates
- Fig. 12. Comparison of strength reduction factor for sections with offset circular web perforation
- (a) For the case of flanges unfastened to bearing plates
- (b) For the case of flanges fastened to bearing plates



Fig. 1 Photograph of cold-formed stainless steel lipped channel-sections with circular web openings after Lawson *et. al.* (2015)



(a) With circular web opening centred from bearing plates



(b) With circular web openings offset from bearing plates

Fig. 2. End-two-flange (ETF) loading condition after Uzzaman et al. (2012b, 2013)



(a) Centred circular web opening



(b) Offset circular web opening

**Fig. 3.** Experimental analysis of cold-formed steel lipped channel-sections under end-two-flange (ETF) loading condition for the case of flanges unfastened and fastened to bearing plates after Uzzaman *et al.* (2012b, 2013)



Fig. 4. Definition of symbols



(a) Centred circular web perforation



(b) Offset circular web perforation

**Fig. 5.** Deformed shape predicted from finite element analysis of cold-formed steel lipped channels under end-two-flange (ETF) loading condition for case of flanges unfastened and fastened to bearing plates







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b) For the case of flanges fastened to bearing plates

Fig. 6. Comparison of finite element results and experimental results by Uzzaman *et al.* (2012b) for sections with centred circular web opening





b) For the case of flanges fastened to bearing plates

Fig. 7. Comparison of finite element results and experimental results by Uzzaman *et al.* (2013) for sections with offset circular web opening



(a) with a/h for centered circular web perforation



(b) with N/h for centered circular web perforation



(c) with x/h for offset circular web perforation

Fig. 8. Variation in reduction factors for C142 section for the case of flanges unfastened to bearing plates



(a) For the case of flanges unfastened to bearing plates



(b) For the case of flanges fastened to bearing plates





(a) the case of flanges unfastened to bearing plates



(b) the case of flanges fastened to bearing plates

Fig. 10. Comparison of strength reduction factor for C142 section with offset circular web perforation



(a) For the case of flanges unfastened to bearing plates



(b) For the case of flanges fastened to bearing plates

Fig. 11. Comparison of strength reduction factor for sections with centered circular web perforation



(a) For the case of flanges unfastened to bearing plates



(b) For the case of flanges fastened to bearing plates

Fig. 12. Comparison of strength reduction factor for sections with offset circular web perforation