

Detection and compensation of anomalous conditions in a wind turbine

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Abstract

Anomalies in the wind field and structural anomalies can cause unbalanced loads on the components and structure of a wind turbine. For example, large unbalanced rotor loads could arise from blades sweeping through low level jets resulting in wind shear, which is an example of anomaly. The lifespan of the blades could be increased if wind shear can be detected and appropriately compensated. The work presented in this paper proposes a novel anomaly detection and compensation scheme based on the Extended Kalman Filter. Simulation results are presented demonstrating that it can successfully be used to facilitate the early detection of various anomalous conditions, including wind shear, mass imbalance, aerodynamic imbalance and extreme gusts, and also that the wind turbine controllers can subsequently be modified to take appropriate diagnostic action to compensate for such anomalous conditions.

Keywords:

Wind turbine anomaly detection, anomaly compensation, wind turbine control, Extended Kalman Filter

1. Introduction

The controller for a wind turbine has the basic objective of ensuring that the turbine operates according to its design strategy; that is, rotor torque, rotor speed and power are maintained at the appropriate values according to wind speed. In addition, for large wind turbines the controller is required to reduce various structural loads on the blades, rotor and drive-train.

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7 **Nomenclature**

8	α	severity of wind shear
9	α_c	confidence confirmation limit
10	α_d	confidence detection limit
11	β	pitch angle
12	χ^2	chi-squared distribution
13	ϵ	phase shift between θ and θ_a
14	\hat{C}_T	modified thrust coefficient for dynamic inflow model
15	\hat{V}_s	see Equation (36)
16	λ	tip-speed ratio
17	λ_R	modified tip-speed ratio for dynamic inflow model
18	$\mathbf{E}\{\cdot\}$	expected value
19	μ	see Equation (42)
20	μ_c	see Equation (44)
21	Ω	rotor speed
22	\bar{V}	mean wind speed
23	ϕ	set angle error signal
24	ρ	air density
25	σ_v	turbulence intensity
26	θ	arbitrary azimuth angle preset by the EKF
27	θ_a	actual azimuth angle of the the blade
28	θ_d	phase difference between the Mx and My BRBM measure-
29		ments
30	\tilde{R}	measurement noise covariance
31	ξ_0	Gaussian noise
32	a_1, b_1	deterministic wind speed variation across the rotor in the hor-
33		izontal and vertical directions, respectively
34	a_d, b_d	coefficients for the point wind speed model
35	A_R	rotor disc area

36	C_p	power coefficient
37	C_{mx}	in-plane blade root bending moment coefficient
38	C_{my}	out-of-plane blade root bending moment coefficient
39	e	EKF innovation error
40	g	gravity
41	g_a	signature vector of the wind anomaly
42	h	tower height
43	h_o	reference height for modelling wind shear
44	H_a	signature matrix of the wind anomaly
45	J_f	Jacobian matrix of the nonlinear function, $f(x_{k-1})$
46	J_g	Jacobian matrix of the nonlinear function, $g(x_{k-1})$
47	K	Kalman gain
48	L_t	turbulence length of the spectrum
49	M_1	see Equation (28)
50	M_2	see Equation (29)
51	M_b	blade mass
52	$M_{I/P}$	in-plane blade root bending moment
53	$M_{O/P}$	out-of-plane blade root bending moment
54	N	number of blades
55	N_{df}	degrees of freedom
56	P	estimate error covariance
57	Q	process noise covariance
58	R	rotor radius
59	S	EKF innovations error covariance
60	S_D	Dryden spectrum
61	S_v	Von Karman spectrum
62	T_f	aerodynamic torque
63	T_a	anomaly starting time

64	T_c	time interval for anomaly confirmation
65	v	process noise
66	V_0	turbulence with added mean wind speed
67	V_a, V_b	components of the effective wind speed, V_s
68	V_d	point wind speed
69	V_p, V_{a1}, V_{b1}	stochastic components of the effective wind speed
70	V_R	wind speed at rotor
71	V_s	effective wind speed
72	$V_{(anomaly)}$	wind speed affected by a given wind anomaly
73	$V_{(gust)}$	wind gust model
74	w	measurement noise
75	W_a, W_b, W_c	effective wind speed models with different parameters
76	ACT	anomaly confirmation test
77	ADT	anomaly detection test
78	BRBM	blade root bending moment
79	DNV-GL	Det Norske Veritas and Germanischer Lloyd
80	EKF	Extended Kalman Filter
81	FMM	first moment of mass
82	IBC	individual blade control
83	IEC	International Electrotechnical Commission
84	IPC	individual pitch control
85	LIDAR	light detection and ranging
86	Mx	in-plane
87	My	out-of-plane
88	O&M	operations and maintenance
89	PI control	proportional-integral control
90	Supergen	Sustainable Power Generation and Supply

91 Modern wind turbine controllers usually achieve the basic objectives very
92 well, and an anomaly detection and compensation scheme is introduced here
93 to increase the functional capability of the (baseline) controller. Operating in-
94 dependently from the baseline controller, it can detect various anomalies (or
95 anomalous conditions), including wind shear, extreme gusts, blade mass imbalance
96 and aerodynamic imbalance. By detecting and subsequently compensating
97 for anomalies, it would reduce the number of unnecessary shut-downs caused by
98 the anomalies, resulting in increased energy production, and further mitigate
99 loads on the turbine, resulting in reduced operations and maintenance (O&M)
100 costs or life-time extension.

101 The anomaly detector uses an Extended Kalman Filter (EKF) [1, 2] that is
102 primarily based on an effective wind field model [3] and a nonlinear 3 bladed
103 rotor (aerodynamic) model. It should be noted that the main contribution of
104 the work is neither in the EKF nor in the models that the EKF is based on.
105 Instead, to achieve the aforementioned novel objective, i.e. anomaly detection
106 and compensation, a standard filtering algorithm (i.e. the EKF) and existing
107 models are adapted.

108 A LIDAR (light detection and ranging) system could be utilised to achieve
109 similar results as it allows the rotor speed and other operational control param-
110 eters to be adjusted to an approaching wind field before it reaches the turbine [4].
111 However, the use of a LIDAR is costly, and the model-based anomaly detection
112 and compensation algorithm proposed here can achieve the same objective at
113 significantly reduced cost (i.e. without a LIDAR). Hence, the main contribution
114 of this work, in more detail, is that an anomaly detection and compensation al-
115 gorithm is proposed here to increase the functional capability of the existing
116 baseline controller at reduced cost; that is, without the need for an expensive
117 LIDAR.

118 Although work on anomaly detection using a LIDAR is becoming more pop-
119 ular in the literature [4, 5, 6, 7], work on this topic without the use of a LIDAR
120 is still limited [8, 9, 10]. Moreover, while the work presented in [8, 9, 10] is
121 dedicated to gust detection, the work presented here is more comprehensive
122 dealing with various types of anomalies. It is important to note that this paper
123 deals with “anomalies”, which should be separated from “faults”. Anomalies in-
124 clude anomalous wind conditions, such as wind shear and gusts, and structural
125 anomalies, such as mass imbalance and aerodynamic imbalance, while faults
126 include actuator (e.g. pitch actuator) and sensor failures. For research on fault
127 detection, readers are referred to [11, 12, 13].

128 An EKF requires that the wind field model be represented in the form of
129 a lumped parameter ordinary differential equation model. A wind field model,
130 which meets this requirement, has been developed in [3]. It outputs “effective
131 wind speeds” for each blade and the rotor such that rotor thrust, torque and
132 in-plane (M_x) and out-of-plane (M_y) blade root bending moments (BRBMs) are
133 represented reasonably accurately for frequencies up to the 1P spectral peak,
134 which is due to rotational sampling [14, 15]. More specifically the auto and
135 cross-spectral density functions for the forces and torques are accurate up to
136 and including a frequency of 1P.

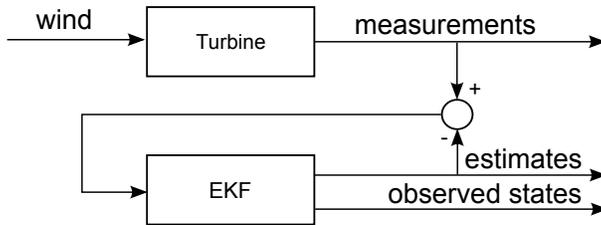


Figure 1: EKF estimates states that are not measurable or measured.

137 The wind field model is improved in this paper to include a model of dynamic
 138 inflow, hence to improve the accuracy of the EKF. To further improve the
 139 anomaly detection capabilities, this wind-field model could, if necessary, be
 140 extended to increase the accuracy to higher multiples of P at the cost of increased
 141 computational demand.

142 A nonlinear 3 bladed aerodynamic model, suitable for use with the wind
 143 field model, employs standard aerodynamic coefficient models for rotor torque
 144 and M_x and M_y BRBMs [3]. The coefficients, which are functions of wind
 145 speed, tip-speed ratio, pitch angle, etc, are derived using Det Norske Veritas
 146 and Germanischer Lloyd's (DNV-GL) Bladed. It also takes into account the
 147 gravitational loading on the blades.

148 The tower dynamics could be included in the model for designing the EKF,
 149 but in return the complexity of the EKF would increase and become more
 150 computationally demanding. In any case, it does not seem to be necessary since
 151 the EKF still performs satisfactorily without the tower dynamics included in
 152 the model, as the results throughout the paper demonstrate.

153 The EKF is designed to track measurements of aerodynamic/hub torque and
 154 M_x and M_y BRBM of each blade and, in turn, to provide estimates of the states
 155 of the wind field and the gravitational loading, etc. on the blades as depicted in
 156 Figure 1. By monitoring these estimates (which are not measured or measurable
 157 in real life), various anomalies can be detected.

158 To enable detection of gusts, the anomaly detector is extended. Detection of
 159 gusts, unlike other anomalies, cannot be achieved by directly monitoring states
 160 estimated by the EKF. Instead, the EKF innovations error is used to monitor
 161 changes in variable correlation. Such changes are matched through best fit to a
 162 modelled anomalous scenario, e.g. extreme operating gust or extreme coherent
 163 gust. A set of modelled anomalies are derived from equations provided by
 164 International Electrotechnical Commission (IEC) 61400-1 (under the section,
 165 Extreme Conditions) [16].

166 Diagnostic features are also added to the anomaly detection scheme to isolate
 167 individual anomalies, estimate their magnitudes, and compensate such anom-
 168 alies, for example using Individual Pitch Control (IPC) [17, 18], Individual Blade
 169 Control (IBC) [19] or open-loop control [20, 21]. This paper focuses more on the
 170 detection part and less on the compensation part, and therefore only wind shear

171 and gust compensation using IPC and open-loop control, respectively, following
172 the detection of wind shear and gust, is reported.

173 The EKF based anomaly detector and the models required by it are described
174 in Section 2. Simulation results on anomaly detection are presented in Section 3.
175 The extension of the anomaly detector for gust detection is reported in Section
176 4, and anomaly compensation is described in Section 5. Conclusions are drawn
177 and future work discussed in Section 6.

178 The illustrative turbine in this paper is the Supergen (Sustainable Power
179 Generation and Supply) Wind 2 MW exemplar wind turbine, which is a 3
180 bladed, horizontal-axis turbine, designed for variable-speed and pitch-regulated
181 operation.

182 Anomalies that are detected in this paper are blade mass imbalance, wind
183 shear, aerodynamic imbalance and extreme (coherent and operating) gust. Mass
184 imbalance may occur due to blade icing in cold conditions and is detected in
185 this paper by estimating each blade mass, M_b . Wind shear, variation in wind
186 speed across the rotor disc in the vertical direction, can be caused by various
187 factors including low level jets and weather front. It is detected in this paper
188 by estimating deterministic wind speed variation across the rotor in the vertical
189 direction, b_1 . Aerodynamic imbalance, which can be caused by error in blade set
190 angle, is detected in this paper by estimating set angle error signal, ϕ . Extreme
191 gust can be caused by various factors including turbulence due to friction, wind
192 shear, and solar heating of the ground. It is detected in this paper by utilising
193 the EKF innovation error, e . Sections 3 and 4 demonstrate the state estimation
194 and the anomaly detection in detail. When modelling these anomalies in Bladed,
195 we use appropriate values to ensure that the anomalies are practical and realistic
196 by consulting industrial experts.

197 **2. Anomaly Detection Scheme**

198 To facilitate early detection of anomalous operating conditions, an anomaly
199 detector is developed, which allows the wind turbine controller or operator to
200 take appropriate and timely action. It is based on an EKF, which requires
201 accurate models. An effective wind field model and a nonlinear 3 bladed aero-
202 dynamic model are utilised for designing the EKF based anomaly detector in
203 order to detect various anomalous conditions. These models, their validation
204 and the design of the EKF based on these models are described in this section.

205 As mentioned in Section 1, the main contribution of the work is neither
206 in the EKF nor in the models the EKF is based on. Instead, to achieve the
207 novel objective, i.e. anomaly detection and compensation without the use of a
208 LIDAR, a standard filtering algorithm (i.e. EKF) and existing models, both of
209 which are reported in this section, are adapted.

210 *2.1. Wind Field Model*

211 The wind field model outputs azimuthally and time varying effective wind
212 speeds, V_s , for each blade and rotor so that the rotor thrust, torque and M_x

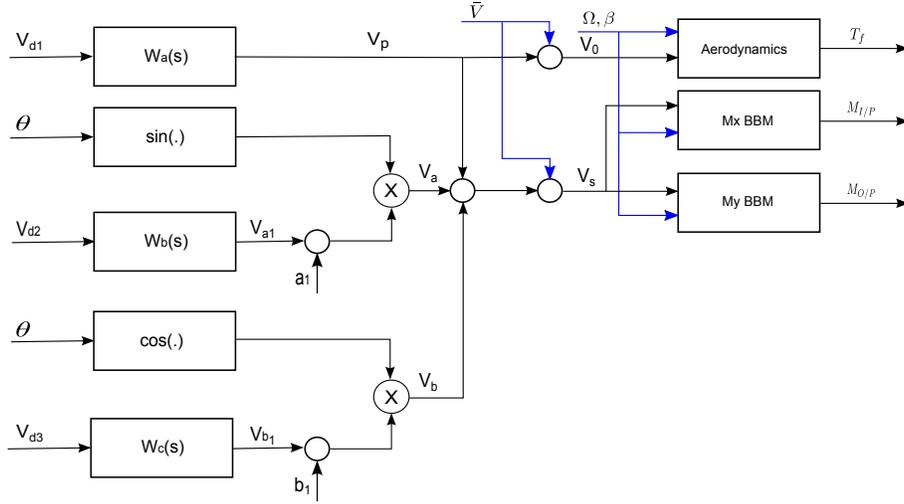


Figure 2: Wind field model and 1 of 3 blades model including frequencies up to the 1P spectral peak.

213 and My BRBMs are represented reasonably accurately at frequencies up to and
 214 including the spectral peak that corresponds to 1P. Effective wind speed, V_s ,
 215 is composed of 3 components, V_p , V_a and V_b , as shown in Figure 2. More
 216 specifically, the auto and cross-spectral density functions for the forces and
 217 torques are reasonably accurate at frequencies up to and including 1P.

218 The wind field on each blade consists of stochastic and deterministic
 219 components. Wind speed is in general measured on the nacelle by an anemometer,
 220 making unrealistic a direct correlation between the effects of the measured wind
 221 speeds and loads on the blades.

As the wind speed varies across the rotor, a blade element will experience
 different wind speeds as it rotates. The difference in wind speed across the rotor
 is caused by deterministic components, such as wind shear, tower shadow and
 blade mass imbalance, and stochastic components, such as turbulence. The wind
 field model represents separately the effects of the deterministic and stochastic
 components on the blades. The model of the wind field is depicted in Figure 2
 and has the following structure [3]:

$$V_s(\theta, t) = \bar{V} + V_p(t) + \underbrace{(a_1 + V_{a1}(t))\sin(\theta)}_{V_a} + \underbrace{(b_1 + V_{b1}(t))\cos(\theta)}_{V_b} + \dots \quad (1)$$

222 The wind speed, $V_s(\theta + \frac{2\pi(i-1)}{3}, t)$, induces the moments on blade i (for $i =$
 223 $1, \dots, N$) where N is the number of blades. \bar{V} denotes the mean wind speed,
 224 and V_p , V_{a1} and V_{b1} are coloured noise processes representing the stochastic
 225 terms. More specifically V_p is associated with turbulence (refer to [3] for further
 226 details), and V_{a1} and V_{b1} are respectively used to generate V_a and V_b that

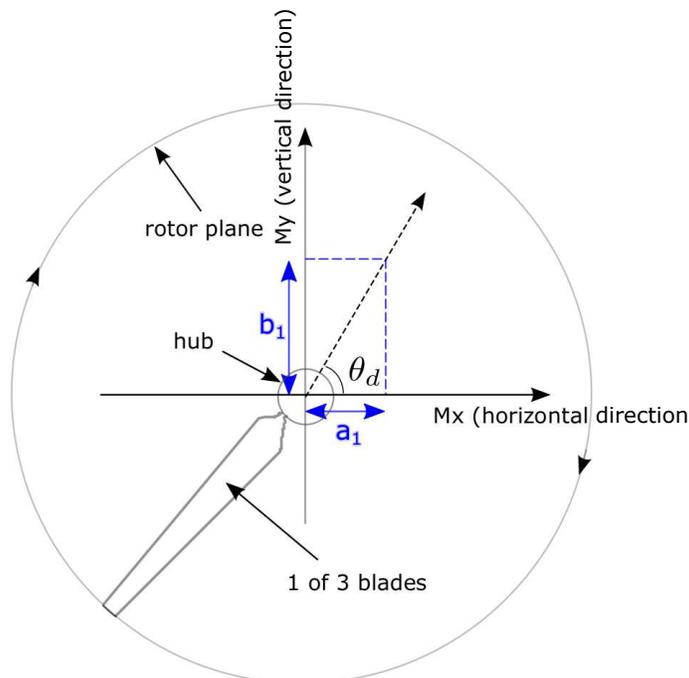


Figure 3: a_1 and b_1 ; variations in the horizontal and vertical axes.

227 eventually add the 1P spectral peak to Mx and My BRBMs.

228 As depicted in Figure 2, a_1 and b_1 denote deterministic variations in wind
 229 speed across the rotor in the horizontal and vertical directions, respectively. The
 230 transfer functions, $W_a(s)$, $W_b(s)$ and $W_c(s)$, are part of the wind field model
 231 that have point wind speed inputs, V_{di} (for $i = 1, 2, 3$), and outputs effective
 232 wind speed components [22], i.e. V_p , V_{a1} and V_{b1} . The modules (or sub-models)
 233 on the right-hand side of the figure are explained in the following sub-section.

The deterministic components on My BRBM is dominated by wind shear
 (i.e. vertical variation in wind speed), while that on Mx BRBM is dominated
 by gravity. Gravity is at its maximum value at the blade horizontal position
 while wind shear causes the wind speed to be at its maximum value at the blade
 vertical position. When the situation is free of nacelle tilting, yaw misalignment,
 etc., the phase difference between the Mx and My BRBM measurements, i.e. θ_d
 in Figure 3, should be close to 90° . However, the wind turbine always has such
 aspects, and θ_d can be calculated as

$$\tan \theta_d = \frac{b_1}{a_1} \quad (2)$$

234 As discussed later in Section 3, θ_d is an important parameter that can be mon-
 235 itored to detect various anomalies, including wind shear and wind veer, which

236 are vertical and horizontal differences in wind speed, respectively.

The point wind speeds, i.e. V_{di} (for $i = 1, 2, 3$), in Figure 2 can be described in the frequency domain by the Von Karman spectrum [22]:

$$S_v(\omega) = 0.476\sigma_v^2 \frac{\frac{L_t}{\bar{V}}}{(1 + (\frac{\omega L_t}{\bar{V}})^2)^{5/6}} \quad (3)$$

where $L_t = 6.5h$ denotes the turbulence length of the spectrum, h height and σ_v the turbulence intensity. In the anomaly detection scheme, it is approximated by the Dryden spectrum:

$$S_D(\omega) = \frac{1}{2\pi} \frac{b_d^2}{\omega^2 + a_d^2} \quad (4)$$

The values of a_d and b_d , for which the Dryden spectrum best approximates the Von Karman spectrum, are

$$a_d = 1.14 \frac{\bar{V}}{L_t} \quad (5)$$

$$b_d = \sigma_v \sqrt{2a_d} \quad (6)$$

The corresponding point wind speed model is

$$V_d = V_d(s)\xi_0 \quad (7)$$

$$= \frac{\bar{V}b_d}{s + a_d} \xi_0 \quad (8)$$

237 where ξ_0 denotes Gaussian noise.

238 2.2. Nonlinear 3 Bladed Aerodynamic Model

239 A 3 bladed aerodynamic model is used with the wind field model introduced
 240 in Section 2.1 to calculate the in-plane (Mx) and out-of-plane (My) BRBM and
 241 the contribution to torque for each blade. The model for one of the 3 blades
 242 contained in the complete model together with the wind field model is shown
 243 in Figure 2, where Ω is rotor speed and β pitch angle.

Aerodynamic torque, T_f , is estimated in the module named ‘‘Aerodynamics’’ in Figure 2 using

$$T_f = \frac{1}{2} \rho \pi V_0^2 R^3 \frac{C_p(\lambda, \beta)}{\lambda} \quad (9)$$

where β is pitch angle, and the tip-speed ratio, λ , is defined as

$$\lambda = \frac{R\Omega}{V_0} \quad (10)$$

244 R denotes the rotor radius, C_p the aerodynamic power coefficient and ρ the air
 245 density. The parameters of the 2MW Supergen exemplar turbine are used.

The resulting wind speed, V_s , is used by the the modules named “BBM Mx” and “BBM My”, respectively, in Figure 2 for estimating the Mx and My BRBM. Similar equations to Equation (9) are utilised for these modules as follows:

$$M_{I/P} = \frac{1}{2}\rho\pi V_s^2 R^3 \frac{C_{mx}(\lambda)}{3} + gM_b \cos\theta_a \quad (11)$$

$$M_{O/P} = \frac{1}{2}\rho\pi V_s^2 R^3 \frac{C_{my}(\lambda)}{3} \quad (12)$$

246 Note that these equations are valid when V_s from the wind field model described
 247 in Section 2.2 is used. C_{mx} and C_{my} are respectively in-plane and out-of-plane
 248 bending root moment coefficients [3], g gravity, M_b the first moment of mass
 249 (FMM) of each blade and θ_a the actual azimuth angle of the the blade. The
 250 second term in Equation (11) represents gravitational loading. Since gravity has
 251 little impact on My BRBM, given that the tilt angle is small, yaw misalignment
 252 is minimal, etc, it is excluded from Equation (12).

To model mass imbalance between the 3 blades, Equation (9) can simply be replaced with the sum of Equation (11) for blades 1, 2 and 3 as follows:

$$T_f = M_{I/P,1} + M_{I/P,2} + M_{I/P,3} \quad (13)$$

253 Gravitational term in Equation (11) cancels out when summed in Equation (13)
 254 only if there is no mass imbalance.

255 2.3. Validation

256 The model developed in Matlab/Simulink[®] that combines the wind field
 257 model and the 3 bladed aerodynamic model described in Sections 2.1 and 2.2,
 258 respectively, is validated against the aero-elastic Bladed model for the same
 259 turbine, the 2MW Supergen exemplar turbine. The former model is used for
 260 developing the EKF in Section 2.4.

261 Simulations are run for 400 s with a mean wind speed of 8 m/s and turbulence
 262 intensity of 10 %. The power spectra of Mx and My BRBM from the model
 263 are presented in comparison to that from the Bladed model in Figures 4 and
 264 5. Note that hub torque is the sum of Equation (11) for blade 1, 2 and 3 (see
 265 Equation (13)), and therefore the model for hub torque does not need to be
 266 validated separately. The time-series results are not very meaningful here since
 267 the Matlab/Simulink and Bladed models experience different wind speeds in
 268 time.

269 Figures 4 and 5 demonstrate that Mx and My BRBM, respectively, from the
 270 Matlab/Simulink and Bladed models have similar spectra at low frequencies
 271 especially both displaying 1P peak (around 1.8 *rad/s*). Since the model is
 272 developed to be reasonably accurate for frequencies up to 1P, they are not
 273 expected to be similar at high frequencies. The red plot in Figure 4 is discussed
 274 in the following section.

275 The EKF is designed to ensure that any remaining discrepancy is reduced
 276 even further and also that the time response (of the EKF designed on the basis
 277 of the Matlab/Simulink model) tracks the measurements from the Bladed model
 278 closely.

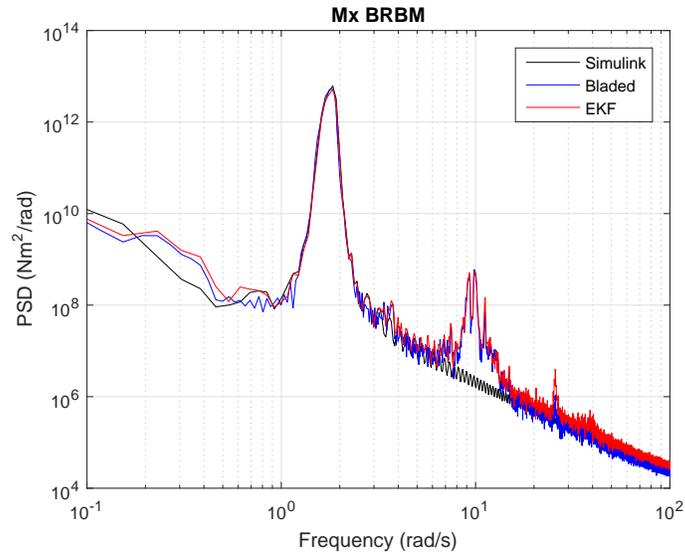


Figure 4: Power spectrum of Mx BRBM from the Matlab/Simulink model vs Bladed model vs EKF.

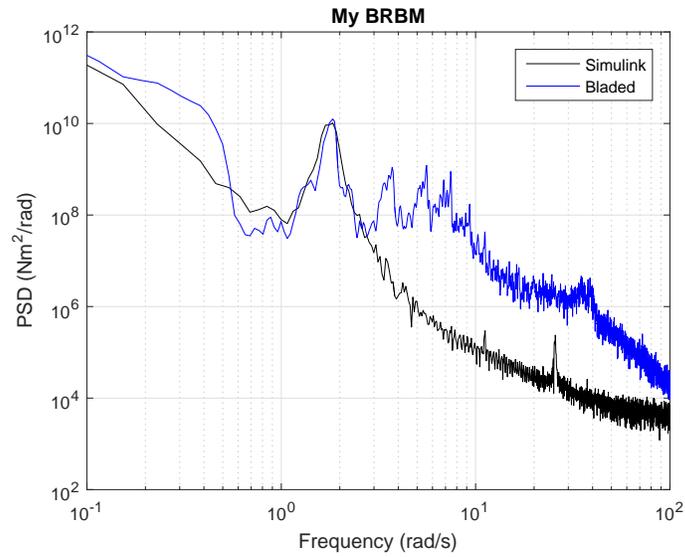


Figure 5: Power spectrum of My BRBM from the Matlab/Simulink model vs Bladed model.

The combined nonlinear models introduced in Sections 2.1 and 2.2 are rewritten in the following discrete form:

$$x_k = f(x_{k-1}) + v_{k-1} \quad (14)$$

$$y_k = g(x_k) + w_k \quad (15)$$

where $f(x_{k-1})$ and $g(x_k)$ are the nonlinear system and measurement models as described in Sections 2.1 and 2.2, respectively. For more details on the models used for $f(x_{k-1})$ and $g(x_k)$, readers are referred to Appendix A. v_{k-1} represents process noise, which is represented by Gaussian noise, ξ_0 , from Equation (7), and w_k denotes measurement noise. The measurement noise covariance, \tilde{R}_k , and the process noise covariance, Q , are given by

$$E[v_{k-1}v_{k-1}^T] = Q \quad (16)$$

$$E[w_k w_k^T] = \tilde{R}_k^T \quad (17)$$

\tilde{R}_k is updated online through the use of an online covariance algorithm, while Q is assumed to be constant.

The model forecast step or predictor uses the following equations:

$$x_k^- \approx f(x_{k-1}) \quad (18)$$

$$P_k^- = J_f(x_{k-1})P_{k-1}J_f(x_{k-1}) + Q_{k-1} \quad (19)$$

where $J_f(x_{k-1})$ denotes the Jacobian matrix of the nonlinear function, $f(x_{k-1})$. x_k^- and P_k^- denote the *a priori* state estimate and *a priori* estimate error covariance, respectively. The data assimilation step or corrector uses the following equations:

$$x_k \approx x_k^- + K_k(y_k - g(x_k)) \quad (20)$$

$$K_k = P_k^- J_g^T(x_k)(J_g(x_k)P_k^- J_g^T(x_k) + \tilde{R}_k)^{-1} \quad (21)$$

$$P_k = P_k^- - K_k J_g(x_k)P_k^- \quad (22)$$

where $J_g(x_k)$ denotes the Jacobian matrix of the nonlinear function, $g(x)$, and K_k is the Kalman gain.

Since the difference between two positive-definite matrices may result in a non positive-definite matrix, which could result in numerical instability, Equation (22) is modified as

$$P_k = (I - K_k J_g(x_k))P_k^- (I - K_k J_g(x_k))^T + K_k \tilde{R}_k K_k^T \quad (23)$$

Now, each term in the equation is positive-definite, and P_k is positive definite because the sum of two positive-definite matrices is positive-definite.

For more details on the formulation of EKF, readers are referred to [23, 24, 25].

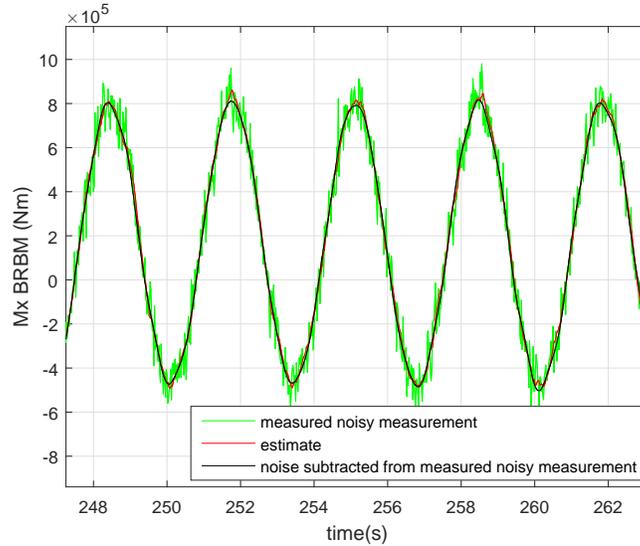


Figure 6: Noise-free tracking.

288 **3. Anomaly Detection**

289 The use of the EKF presented in Section 2 for detecting various anomalous scenarios, e.g. wind shear, mass imbalance and aerodynamic imbalance, is described with simulation results in this section. For gust detection, an extra feature needs to be incorporated into the detector, and this topic is presented in Section 4.

294 The EKF is developed in Matlab/Simulink based on the models presented in Sections 2.1 and 2.2, but the measurements required by the EKF are obtained directly from the Bladed model that represents the same turbine, i.e. 2MW Supergen exemplar turbine. The Bladed model is a high fidelity aero-elastic model that is highly detailed including all the necessary blade dynamics, tower dynamics, etc. The modelling discrepancy between the two models provides a degree of model-plant mismatch to test the robustness of design. As previously mentioned, the EKF tracks measurements of hub torque and Mx and My BRBMs from the Bladed model, and provides state estimation, such as wind field components and blade mass.

304 To make simulations more realistic, extra noise is added to the measurements throughout this paper. An example is depicted in Figure 6, in which measurement of Mx BRBM is contaminated with noise (green), which is inputted to the EKF as opposed to the original noise-free measurement (black). Despite the added noise, the estimate by the EKF (red) is almost noise-free due to computation of the measurement noise covariance, \hat{R}_k in Equation (21), online by the EKF as depicted in Figure 6. The corresponding power spectra in Figure 4 (red

311 and blue) also demonstrate similar characteristics in the frequency domain.

312 Examples of estimation of the states, the stochastic and deterministic wind
 313 speed components, V_p , V_a and V_b (see Figure 2), are depicted in Figure 7a. These
 314 wind speed components, when aggregated, become the effective wind speed V_s
 315 experienced by one of the blades as depicted in Figure 7b. When V_s is used
 316 with the blade model, i.e. Equations (11) and (12), it mimics the effect of low
 317 frequency turbulence together with 1P rotational sampling. The EKF, at the
 318 same time, estimates other important states, such as azimuth angle, mass of
 319 each blade, etc. Monitoring of these states facilitates the detection of anomalies
 320 in various situations.

321 For example, the azimuth angle (i.e. angular position) and mass of each blade
 322 can be estimated and calculated as follows. The initial condition (arbitrary value
 323 predetermined by the EKF) for the azimuth angle of blade 1 is assumed to be
 324 at the 3 o'clock position by the EKF. However, the azimuth angle of blade 1 of
 325 the Bladed model (which simulates the turbine in this paper), that the EKF is
 326 monitoring, may not be at the 3 o'clock position when the EKF starts to monitor
 327 the Bladed model. The difference (i.e. phase shift) needs to be calculated and
 328 taken into account by the EKF as follows. Note, this is paramount for correctly
 329 identifying gravitational loading, wind shear, wind veer, etc as discussed below.

The gravity term in Equation (11) is rewritten as

$$gM_{b,i}\cos\theta_a = gM_{b,i}\cos(\theta + (i - 1)2\pi/3 - \epsilon) \quad (24)$$

for $i = 1, 2, 3$ (3 being the number of blades). θ_a denotes the azimuth angle of
 the turbine being monitored, θ the arbitrary azimuth angle preset by the EKF
 (i.e. at the 3 o'clock position when the EKF starts) and ϵ the phase shift such
 that

$$\theta_a = \theta - \epsilon \quad (25)$$

For blade 1, i.e. $i = 1$, Equation (25) can be substituted into Equation (24)
 to obtain

$$gM_{b,1}\cos(\theta - \epsilon) = gM_{b,1}(\cos\epsilon \cos\theta + \sin\epsilon \sin\theta) \quad (26)$$

$$= M_1\cos\theta + M_2\sin\theta \quad (27)$$

where

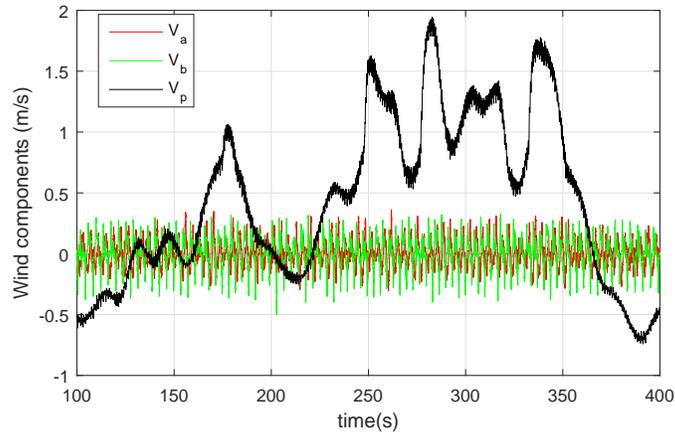
$$M_1 = gM_{b,1}\cos\epsilon \quad (28)$$

$$M_2 = gM_{b,1}\sin\epsilon \quad (29)$$

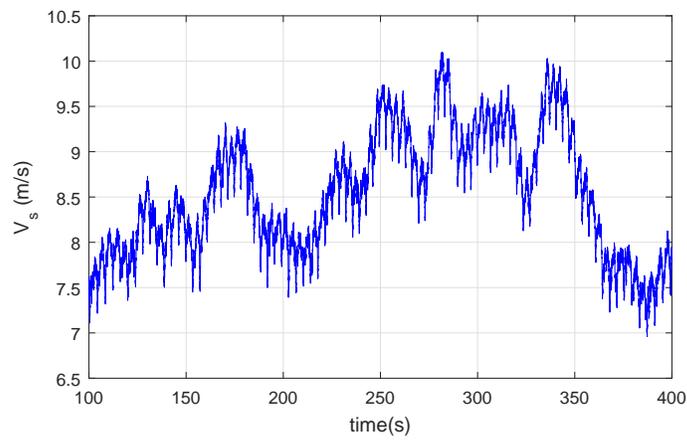
M_1 and M_2 are states estimated by the EKF. These state estimates are subse-
 quently used by the output equation, Equation (11), and also allow M_b and ϵ
 to be calculated as follows:

$$M_b = \sqrt{M_1^2 + M_2^2} \quad (30)$$

$$\epsilon = \tan^{-1}\left(\frac{M_2}{M_1}\right) \quad (31)$$



(a) Wind field components.



(b) Sum of the 3 wind field components.

Figure 7: Estimation of wind field components.

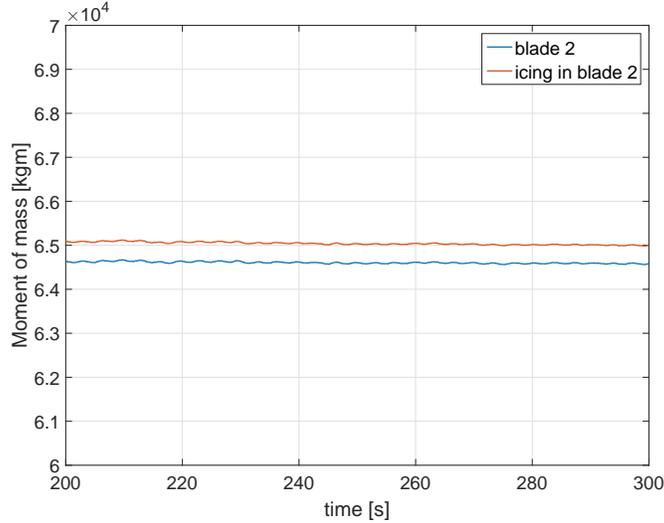


Figure 8: Mass imbalance due to blade icing.

330 The FMM of blade 2 estimated by the EKF is depicted in Figure 8. The red
 331 plot is when there is 136 kg of ice (2.55% of the blade mass and ice density of
 332 700 kg/m³) on blade 2 and the blue plot is when there is no ice on the blade.
 333 The estimates match the Bladed model parameters within 5 %. The result
 334 therefore demonstrates that the anomaly detector can be used for detecting
 335 mass imbalance, which could arise due to blade icing.

336 The phase shift, ϵ , between the arbitrary azimuth angle and the actual az-
 337 imuth angle is depicted in Figure 9. As previously mentioned, the EKF assumes
 338 that blade 1 starts at the blade horizontal position (3 o'clock). However, blade 1
 339 of the Bladed model starts at the blade vertical position (12 o'clock). The figure
 340 demonstrates that ϵ is correctly estimated, $\epsilon = 90^\circ$. This estimate updates the
 341 EKF, which can now be used to correctly identify gravitational loading, wind
 342 shear, wind veer, etc.

343 Deviations in a_1 , b_1 and θ_d (in Equation (2)) from typical values can indi-
 344 cate anomalies in wind speed across the rotor, e.g. vertically (wind shear) and
 345 horizontally. As mentioned in Section 2.1, θ_d would never in reality be 90° due
 346 to tilt angle, blade dynamics and so on. Note that the nacelle tilt angle is 4°
 347 for the turbine considered here. θ_d , varies with mean wind speed as depicted in
 348 Figure 10. When θ_d deviates from the plot in the figure, anomalies such as an
 349 increase in wind shear, wind veer or yaw misalignment can be suspected. More
 350 specifically, b_1 can be used for detecting wind shear and a_1 for detecting wind
 351 veer or yaw misalignment. An example of detecting wind shear by monitoring
 352 b_1 is given below.

As discussed in the context of Figure 3, the state b_1 represents variation in

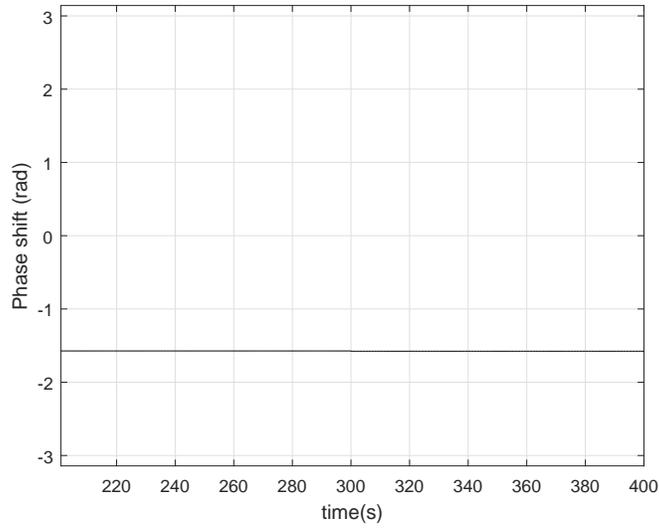


Figure 9: Phase shift.

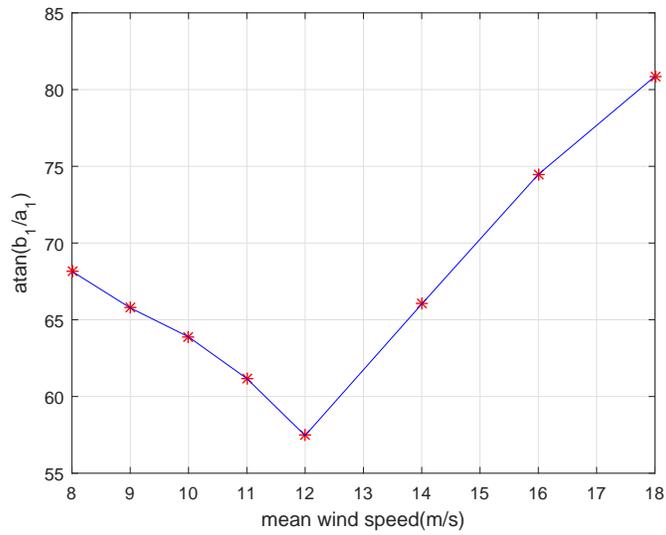


Figure 10: θ_d at different wind speeds with tilt angle of 4α and wind shear with ground roughness height of 0.02m.

wind speed in the vertical direction, e.g. wind shear. Bladed models wind shear

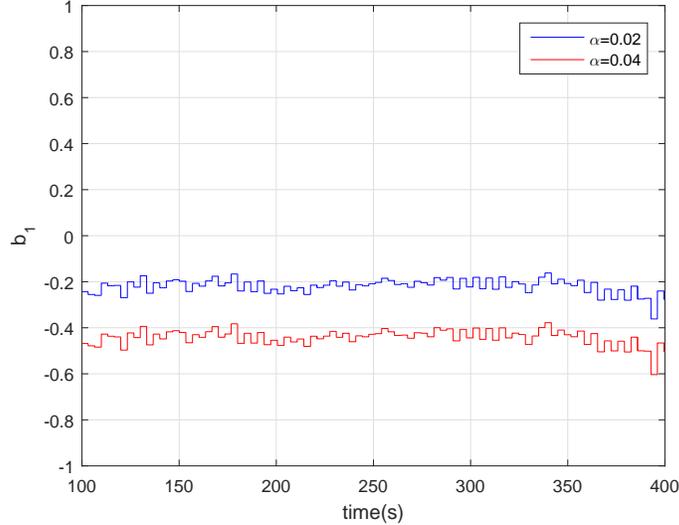


Figure 11: Wind shear.

using the following equation:

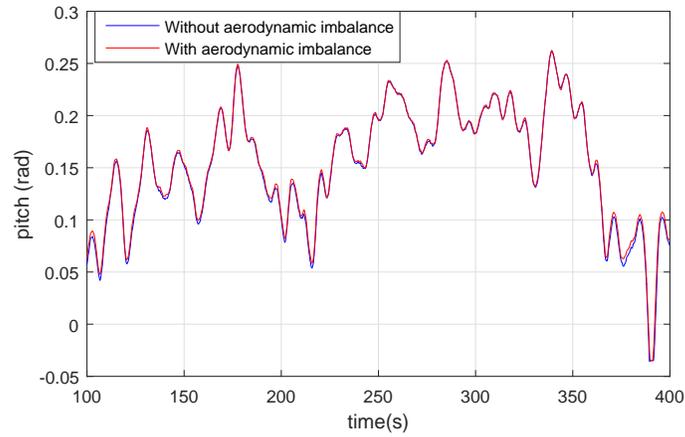
$$V(h) = V(h_o) \left(\frac{h}{h_o} \right)^\alpha \quad (32)$$

353 where h denotes height above the ground and h_o a reference height. α determines
 354 severity of wind shear.

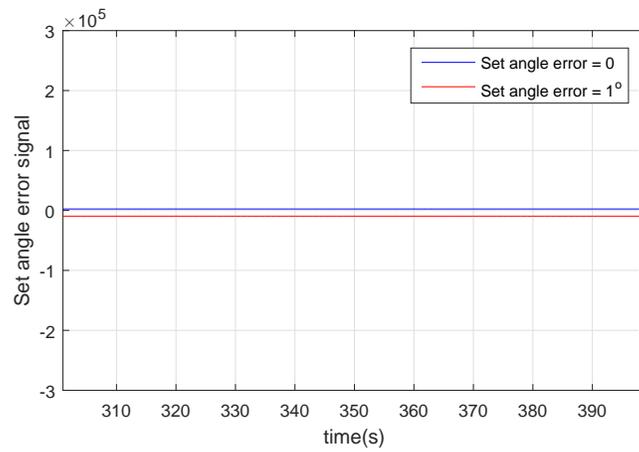
355 Two simulations identical except for severity of wind shear are depicted in
 356 Figure 11. α from Equation (32) is increased by 2 times from the blue to
 357 red plots. The figure shows that monitoring b_1 , estimated by the EKF, could
 358 successfully be used to detect wind shear.

359 The anomaly detector can also be used for detecting aerodynamic imbalance.
 360 For instance, when there is a set angle error, ϕ , of 1° in blade 2, such that
 361 the collective pitch angle (the baseline controller acts through collective pitch
 362 angle) is slightly increased overall as depicted in Figure 12a, the magnitude of
 363 the error signal (set angle error signal) between the measurement and estimate
 364 of My BRBM is increased as depicted in Figure 12b. This offset can therefore
 365 be used to detect aerodynamic imbalance, i.e. a blade set angle error in this
 366 example.

367 Dynamic inflow, i.e. the fractional decrease in wind speed between the free
 368 stream wind (what the wind speed would be without the turbine present) and
 369 the wind speed interacting with the turbine, continuously changes with the
 370 operating conditions. The models introduced in Section 2.1 is improved to
 371 include this effect. The following dynamic inflow model is used [26]:



(a) Pitch with and without set angle error.



(b) Set angle error signal.

Figure 12: Aerodynamic imbalance.

$$\dot{V}_R = \frac{3}{4}(A_R(V - V_R)V_R - \frac{1}{4}A_RV_R^2\hat{C}_T(\lambda_R, \beta))/R^3 \quad (33)$$

where V_R denotes wind speed at rotor, A_R rotor disc area, V wind speed from Equation (1), R rotor radius and \hat{C}_T a modified C_T table from [26]. Equations (11) and (12) are modified as follows:

$$M_{I/P} = \frac{1}{2}\rho\pi\hat{V}_s^2R^3\frac{C_{mx}(\lambda)}{3} + gM_b\cos\theta_a \quad (34)$$

$$M_{O/P} = \frac{1}{2}\rho\pi\hat{V}_s^2R^3\frac{C_{my}(\lambda)}{3} \quad (35)$$

where

$$\hat{V}_s = V_R(1 + \frac{1}{4}\hat{C}_T(\lambda_R, \beta)) \quad (36)$$

372 The incorporation of the dynamic inflow model improves the accuracy of the
 373 EKF. For instance, when the turbine switches from operating below rated to
 374 above rated, a large peak is produced on the estimate of V_a (green) at around
 375 390 s in Figure 13. This is because the effect of dynamic inflow becomes more
 376 significant when switching from operating below rated to above rated. With
 377 the dynamic inflow model properly modelled and included, the EKF now takes
 378 into account the effect of dynamic inflow, and the estimation is improved; that
 379 is, the peak is now removed (black).

380 4. Extension of the Anomaly Detector for Gust Detection

The wind field model described in Section 2.1 does not include the effects of wind gust-like events and therefore a model mismatch (between the events and the model used by the EKF) occurs in the EKF when a gust happens. Consider a model for extreme wind gusts as follows:

$$V_{(anomaly)} = \begin{cases} V_s(\theta, t) & t < T_a \\ V_s(\theta, t) \pm V_{(gust)} & t \geq T_a \end{cases} \quad (37)$$

When a gust occurs, that is, after the anomaly starting time, T_a , the effective wind speed is affected by the magnitude and duration of the gust. These changes in variable correlation can be quantified by taking the expectation ($\mathbf{E}\{\cdot\}$) of the EKF innovations error, e_k , given by

$$e_k = y_k - g(x_k) \quad (38)$$

Expanding Equation (38) in Taylor series about x_{k-1} , the expectation of the innovations error is given by

$$E\{e_k|y_k\} = J_g(x_{k-1})J_f(x_{k-1})E\{\tilde{x}_{k|k-1}|y_{k-1}\} \quad (39)$$

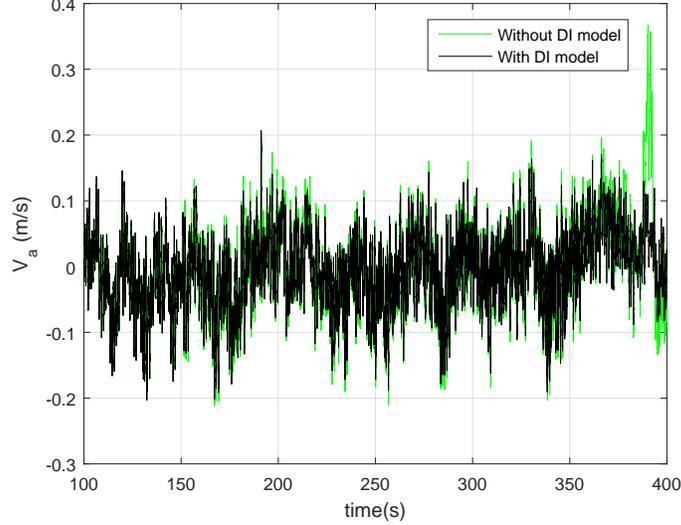


Figure 13: Dynamic inflow model.

where $\tilde{x}_{k|k-1}$ is the error in state estimates due to the anomaly prior to the measurement update (i.e. Equations (20), (21) and (22)) of the EKF. The calculation of state estimates posterior to the EKF measurement update can be obtained with a similar approach as follows:

$$E \{ \tilde{x}_{k|k} | y_k \} = J_f(x_{k-1}) E \{ \tilde{x}_{k|k-1} | y_{k-1} \} + K_k E \{ e_k | y_k \} \quad (40)$$

It is therefore possible to define linear dependence of $E \{ \tilde{x}_{k|k} | y_k \}$ on the anomaly as follow [27]:

$$E \{ \tilde{x}_{k|k} | y_k \} = H_a(k, T_a) g_a, \quad k \geq T_a \quad (41)$$

In Equation (41), the anomaly is described by signature matrix of the anomaly magnitude, $H_a(k, T_a)$, affecting the EKF outputs, state estimates and signature vector of its behaviour, g_a . The signature matrix is time-varying allowing the magnitude of the wind gust to evolve in time. The measurement of the drift in standard deviation produced by the anomaly is determined by the Mahalanobis distance of the innovations error as follows:

$$\mu_k = e_k^T S_k^{-1} e_k \quad (42)$$

where S_k is the EKF innovations error covariance given by

$$S_k = J_g(x_k) P_k J_g^T(x_k) + \tilde{R}_k \quad (43)$$

Equation (42) is used to detect unmodelled anomalies, and this process is referred to as anomaly detection test (ADT) here. The ADT follows the central

χ^2 distribution with N_{df} degrees of freedom and α_d confidence detection limit. To avoid false alarms caused by noise, a positive ADT is followed by an anomaly confirmation test (ACT):

$$\mu_{c,k} = \sum_{k=T_a}^{T_a+T_c} e_k^T S_k^{-1} e_k \quad (44)$$

The ACT follows the same distribution but has $N_{df} (T_c + 1)$ degrees of freedom, a suitable interval time for anomaly confirmation, T_c , and α_c confidence confirmation limit. The following stopping rules need to be defined:

$$ADT_{(alarm)} = \{k > 0, \mu_k > \chi_{N,\alpha_d}^2\} \quad (45)$$

$$ACT_{(alarm)} = \left\{k > 0, \mu_k > \chi_{N \times (T_c+1),\alpha_c}^2\right\} \quad (46)$$

Practical considerations for the detection parameters are: $\alpha_c > \alpha_d$ and T_c longer than half the EKF convergence time. To implement a diagnostic action upon detection and confirmation of a wind gust, the signature matrix has to be estimated; that is, in order to calculate the maximum likelihood ratio in Equation (44), the signature matrix estimate is given by

$$H_a(k, T_a) = [g_a^T J_f^T(x_{k-1}) J_g^T(x_{k-1}) S_k^{-1} J_g(x_{k-1}) J_f(x_{k-1})]^{-1} \times [g_a^T J_f^T(x_{k-1}) J_g^T(x_{k-1}) S_k^{-1}] g_a^{-1} \quad (47)$$

381 The estimation of the signature matrix allows the detection of a wind gust at any
 382 mean wind speed. The signature vector is modelled *a priori* using the design
 383 standards described in [16]. Goodness of fit is used to match the unknown
 384 detected anomaly to a modelled signature vector, e.g. operating wind gust
 385 or coherent wind gust. In practice, gust-like events can have any shape and
 386 magnitude. The detection begins with low goodness of fit and increases as
 387 soon as the estimated signature matrix adapts to the anomaly. The signature
 388 matrix is updated until the anomaly has passed. If the detector cannot isolate
 389 the anomaly as neither operating nor coherent gust, the anomalous data is
 390 stored and classified as unknown anomaly, thus providing the detector with an
 391 adaptability feature.

392 Both extreme operating gusts and extreme coherent gusts are generated in
 393 Bladed. An extreme operating gust is modelled at a mean wind speed of 14 m/s.
 394 It has the Mexican hat shape with a recurrence period of 50 year as reported in
 395 [16].

396 The detection of an operating gust is demonstrated in Figure 14, in which
 397 the operating gust starts at 120s. The confirmation threshold for blade 1, V_{b1}
 398 (wind speed estimate for blade 1), and $\mu_{c,k}$ are included in the figure. The hub
 399 wind speed that the Bladed model experiences is also included as a reference
 400 (the Bladed model does not provide wind speed equivalent to V_{b1}). Confidence
 401 limits for the ADT and ACT are set to 0.75 and 0.92, respectively. Several
 402 positive alarms are triggered by noise during the ADT, and two positive alarms

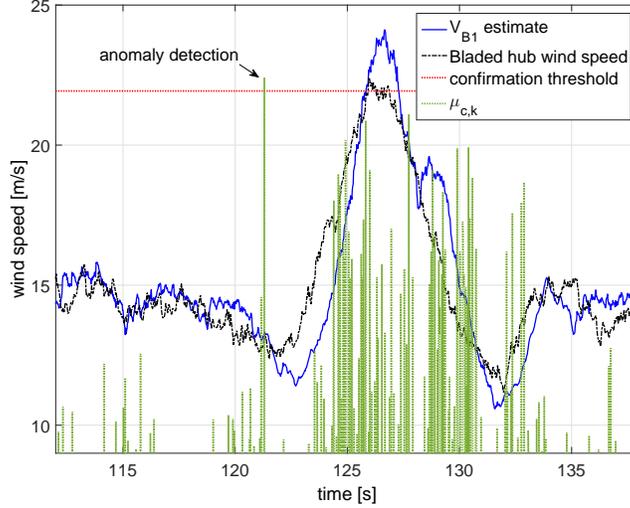


Figure 14: Extreme operating wind gust detection.

403 during the ACT at 64.9s and 121.3s. The first ACT alarm does not remain to
 404 reach T_c , hence the detector rules it out as false. The second alarm remains to
 405 reach T_c , and thus the detector isolates it as an operating gust with a 19.8%
 406 model fit. A diagnostic action, i.e. open-loop control in this paper, can be
 407 applied at this point as described later in Section 5. Once the signature matrix
 408 is estimated, the model fit reaches 89%. This value of model fit is acceptable
 409 considering that turbulence intensity of 10% is not taken into account in the
 410 modelled wind gust.

411 An extreme coherent gust is modelled as a sudden cosine-shaped increase
 412 from a mean wind speed of 14 m/s to 24 m/s, and the increase is subsequently
 413 sustained as depicted in Figure 15, in which the coherent gust starts at 73s. As
 414 with the operating gust depicted in Figure 14, the confirmation threshold for
 415 blade 1, V_{b1} , and $\mu_{c,k}$ are included in the figure, in addition to the hub wind
 416 speed that the Bladed model experiences as a reference. A positive ACT alarm
 417 is triggered at 74.88s and negative ACT alarms at 43.48s, 74.22s and 74.48s. A
 418 model fit of 5.86% is initially achieved and, in turn, increases reaching 82.3%.
 419 The detector can not improve the model fit further since the wind field model
 420 in the EKF is dependent on the mean wind speed, but the mean wind speed has
 421 not been updated; that is, the mean wind speed before and after the onset of the
 422 gust is different. The same diagnostic action as the one used for the operating
 423 wind gust, i.e. open-loop control, can be applied.

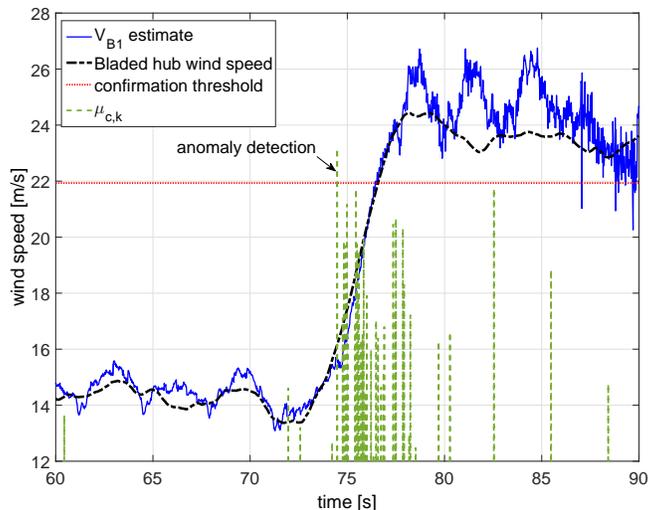


Figure 15: Extreme coherent wind gust detection.

424 **5. Anomaly Compensation**

425 Once an anomaly is detected, a remedial action (compensation) can be ap-
 426 plied directly to the baseline controller to counteract the effects of the anomaly.
 427 The baseline controller used here is a standard commercial controller based
 428 on proportional-integral (PI) control (with modifications to incorporate fatigue
 429 reduction, anti-windup, etc.). It causes the turbine to track its design operat-
 430 ing curve defined on the torque/speed plane [28]; that is, a constant generator
 431 speed (i.e. 89 rad/s) is maintained in the lowest wind speeds; the C_{pmax} curve
 432 is tracked to maximise the aerodynamic efficiency in intermediate wind speeds;
 433 another constant generator speed (i.e. 157 rad/s) is maintained in higher wind
 434 speeds; and in above rated wind speed, the rated power of 2 MW is maintained
 435 by active pitching. Readers are referred to [15, 29] for further details on the
 436 baseline controller.

437 The remedial action reported here is for wind shear and extreme operating
 438 gust. For wind shear, the baseline controller is modified to switch on IPC, which
 439 is a control technique for alleviating unbalanced rotor loads through pitching
 440 each blade separately. Additive corrections to the demanded pitch angle for each
 441 blade are determined by the controller acting on measurements of the BRBMs.
 442 This remedial action is only invoked when the anomalous behavior is detected,
 443 thus avoiding an excess of pitch activity; that is, without the anomaly detector,
 444 the IPC would need to be enabled at all times greatly increasing pitch activity
 445 and wear of the pitch actuator. For an operating gust, when the anomaly
 446 is detected, the baseline controller is modified to operate open-loop to apply
 447 maximum control actions.

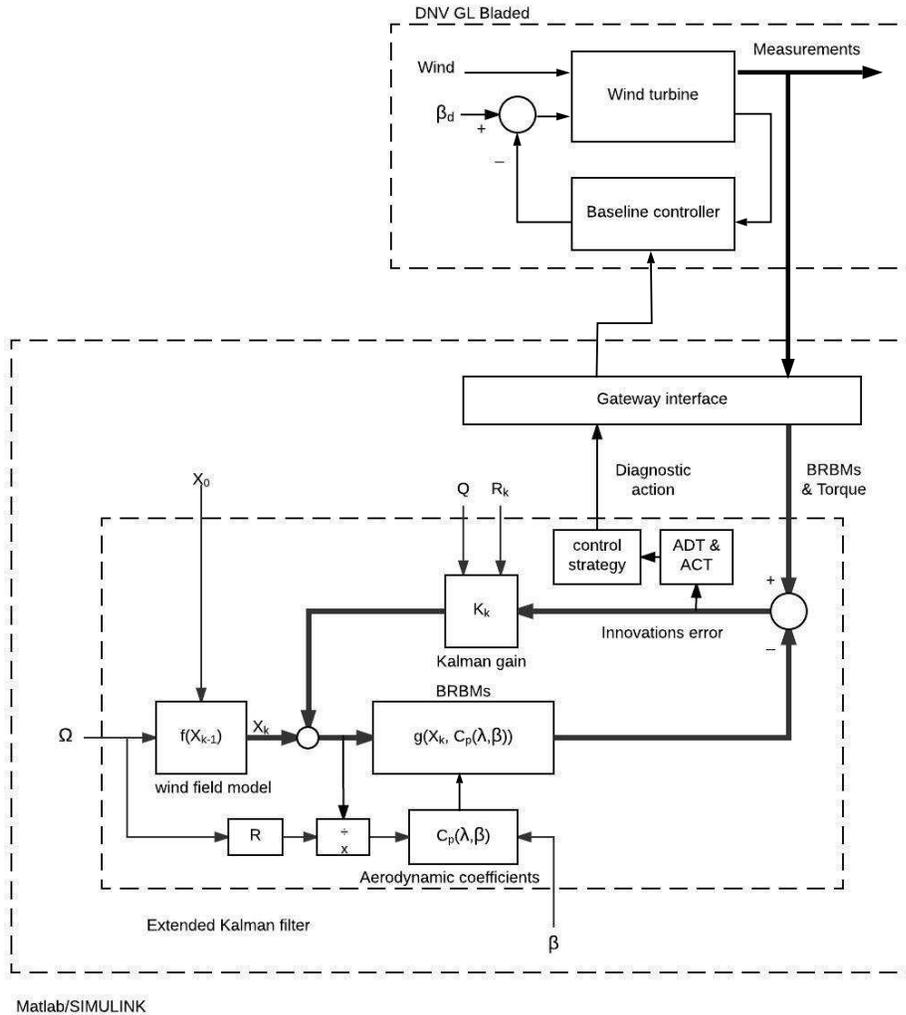
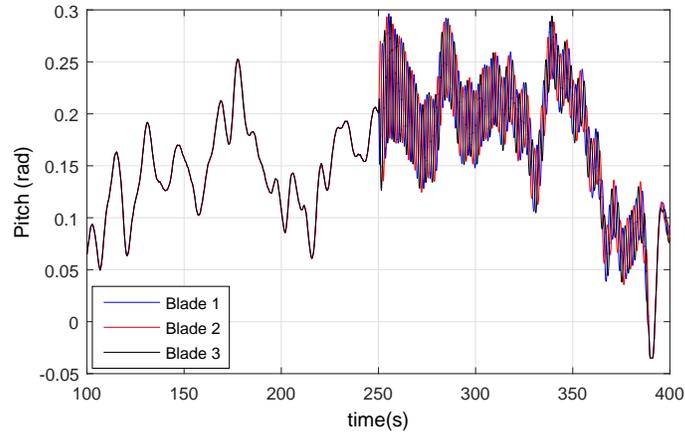


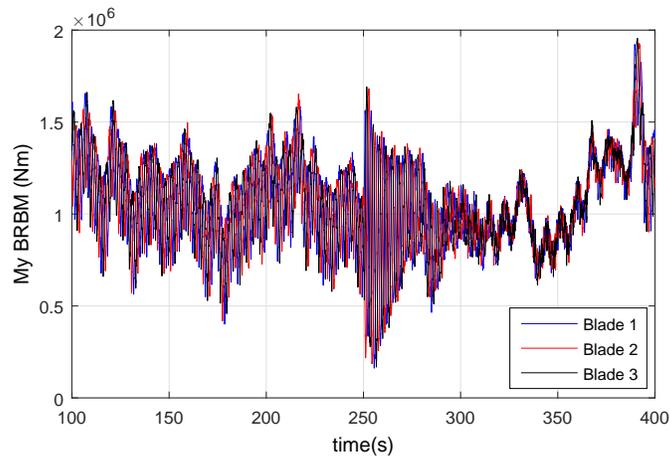
Figure 16: Anomaly detection and compensation scheme.

448 To apply these remedial actions on the Bladed simulation, the anomaly de-
 449 tector and the Bladed model are run in parallel through a commercial gateway
 450 software interface. The gateway interface allows co-simulation between Bladed
 451 and Matlab/Simulink. The simulation set-up for control compensation is pre-
 452 sented in Figure 16. In this figure, the overall anomaly detection and compen-
 453 sation scheme reported throughout this paper is illustrated.

454 In Figure 17 from 100 to 250s, wind shear causes increased loads on the



(a) IPC from 250s.



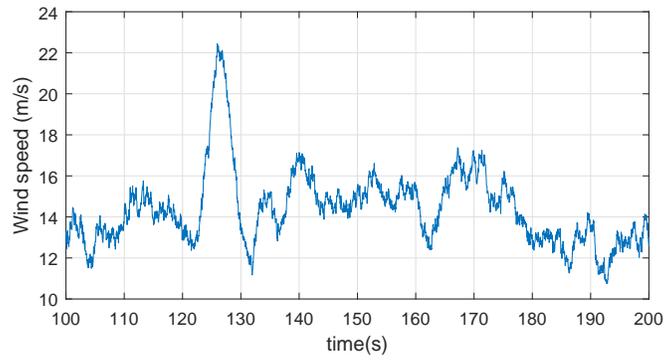
(b) My BRBM.

Figure 17: IPC compensating for wind shear.

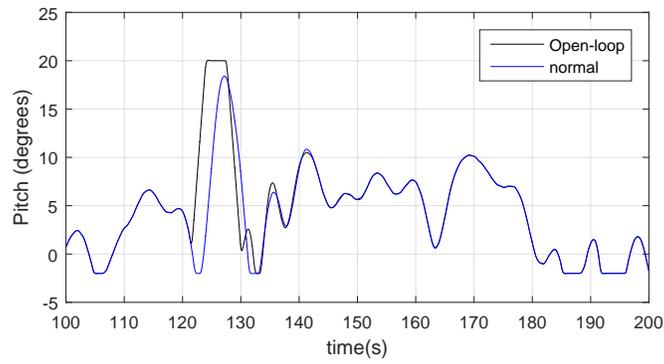
455 blades, i.e. My BRBM in Figure 17. At 250s, the anomaly detector detects an
456 anomaly, i.e. wind shear, and thus switches on the IPC through the gateway
457 interface as depicted in Figure 17a. Consequently, the magnitude of the oscillation
458 on each blade is significantly decreased, resulting in reduced loads on the
459 blades, as demonstrated in Figure 17b. The lifespan of the blades would thus be
460 increased as a result of the wind shear being detected in time and appropriately
461 compensated.

462 In the previous section, i.e. in Figure 14, the detection of an operating gust
463 by the anomaly detector is described. Subsequent compensation of the gust is
464 demonstrated in Figure 18 in this section. In Figure 14, the operating gust is
465 detected at 121.3s. This allows the baseline controller to change from the normal
466 control mode to open-loop control mode. It starts pitching at the maximum
467 pitch rate until it is capped at 20° as demonstrated (in black) in Figure 18b in
468 comparison to the situation in the normal control mode (in blue). Note that in
469 the normal control mode, the open-loop control mode is not activated and the
470 controller persists in following the standard control strategy described in [29];
471 that is, the standard commercial controller is not modified. It is shown that
472 the baseline controller can be modified (from normal control mode to open-
473 loop control mode) in time to compensate for the anomaly. When the wind
474 speed starts to decrease, the controller returns to the normal control mode,
475 and as a result, rotor speed remains below the 12 % threshold as shown (in
476 black) in Figure 18c, preventing the turbine from shutting down. Without the
477 anomaly detection and compensation scheme, rotor speed exceeds the threshold
478 as shown (in blue) in the figure. The individual turbine shut-downs not only
479 cause reduction in the power production but also cascading shut-downs of nearby
480 turbines, which needs to be avoided to protect the grid.

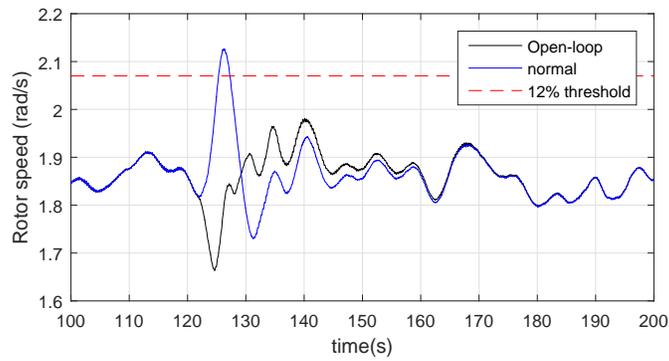
481 The transition from the open-loop control back to the normal control mode
482 can significantly be improved using appropriate techniques such as the one re-
483 ported in [30], but this topic is beyond the scope of this paper.



(a) Gust, the Mexican hat.



(b) Pitch.



(c) Rotor speed.

Figure 18: Open-loop control compensating for gust (the Mexican hat).

484 6. Conclusion and future work

485 An anomaly detection and compensation scheme for a wind turbine is re-
486 ported. By detecting anomalies and taking appropriate remedial actions in time,
487 unnecessary shut-downs can be avoided, thereby improving energy production,
488 and structural loads can be reduced, thus improving O&M costs.

489 The detection approach is to create a map of the wind field at the rotor disc
490 using an EKF that is primarily based on a wind field model and a 3 bladed
491 aerodynamic model. The wind field model is modified to include the effect of
492 dynamic inflow. The EKF developed in Matlab/Simulink, using the parameters
493 of the 2MW exemplar Supergen wind turbine, accepts measurements, i.e. aero-
494 dynamic torque and M_x and M_y BRBM, from the Bladed model of the same
495 turbine. The modelling discrepancy between the two models provides a degree
496 of model-plant mismatch to test the robustness of design. The EKF estimates
497 states that are not measured or measurable. Simulation results demonstrate
498 that the EKF closely tracks the measurements, coping with noise contamina-
499 tion, and that the state estimates can successfully be observed for detecting
500 various anomalies, including wind shear, mass imbalance and aerodynamic im-
501 balance.

502 The anomaly detector is further extended to detect extreme gusts prevent-
503 ing the turbine from shutting down, which would have a number of adverse
504 consequences. The detection is made by exploiting the EKF innovations error.

505 Diagnostic features are added to the anomaly detector to isolate and compen-
506 sate for some anomalies, i.e. wind shear and operating gust. Simulation
507 results demonstrate that once wind shear or operating gust is detected, reme-
508 dial action is successfully applied by IPC or open-loop control, respectively.

509 The mitigation of the impact of anomalies by means of other control strate-
510 gies is being investigated. To date, the model used in the EKF is accurate up
511 to a frequency of 1P, but it could be extended to higher frequency to improve
512 detection of additional anomalous scenarios, including yaw misalignment and
513 wind veer.

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520 bine.

521 A. Models for the Extended Kalman Filter

522 The EKF requires a discrete state space equation as described in Equations
523 (14) and (15), and the models or equations used for the state equations, $f(x_{k-1})$,
524 and the output equations, $g(x_k)$, are described here.

525 Equations used to constitute $f(x_{k-1})$ and their derivation are summarised
 526 as follows.

1. The point wind speed model, $V_d(s)$, used to produce V_{d1} , is combined with $W_a(s)$ as follows (refer to Equation (7) and Figure 2):

$$F_1(s) = V_d(s)W_a(s) \quad (\text{A.1})$$

$$V_p = F_1(s)\xi_0 \quad (\text{A.2})$$

527 V_p is one of the states, x_k , to be estimated. Now the input for the model
 528 $F_1(s)$ is Gaussian noise, which is also the required input for the EKF as
 529 shown in Equation (14).

- 530 2. $F_1(s)$ is converted into the state space form and subsequently discretised,
 531 becoming $F_1(z^{-1})$ (order of 4), to be in the suitable format for the EKF.
 532 Using this model, the EKF estimates V_p .
- 533 3. Steps 1 and 2 are repeated for $W_b(s)$ and $W_c(s)$ to give $F_2(z^{-1})$ and
 534 $F_3(z^{-1})$ (both order of 7), respectively. Using these models, the EKF
 535 estimates V_{a1} and V_{b1} .
- 536 4. The terms, $(a_1 + V_{a1})\sin(\theta)$ and $(b_1 + V_{b1})\cos(\theta)$, in Equation (1) are used
 537 to estimate the states, V_a and V_b (see Figure 2). V_{a1} and V_{b1} are estimated
 538 in Step 3 above, and θ , a_1 and b_1 are also states estimated by the EKF
 539 as reported in Section 3. These equations are used for each blade.
- 540 5. The dynamic inflow model (Equation (33)) is discretised and subsequently
 541 used by the EKF to estimate V_R .
- 542 6. Equation (36) (which is a function of V_R from Step 4) is used to estimate
 543 \hat{V}_s .

544 Equations (11), (12) and (13) constitute the output equations, $g(x_k)$. Equa-
 545 tions (11) and (12) are used for each blade, hence the number output equations
 546 used by the EKF is 7.

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