

# Multi-scale surface simulation of the KDP crystal fly cutting machining

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**Abstract:** The paper presents a novel approach for modelling and simulation of the surface generation in the potassium dihydrogen phosphate (KDP) crystal fly cutting machining process in the macro, micro and nano scales, in order for the evaluation specifications in different spatial frequency region. The main influential factors of surface topography in different scales are discussed and modeled by different methods. The simulations take into account all the intricate aspects of the machining process affecting the surface topography and texture formation, such as the straightness of the slide, the dynamic performance of the machine tool, the cutter profile. This method can realize the machine tool performance and machining parameters optimization by the surface prediction and detection. The numerical calculation (NC) and the finite element (FE) method are used in the macro and micro scales. Molecular dynamics (MD) simulation is used in the nano scale. Furthermore, the proposed systematic modelling approach is verified by cutting trials, which provide the coincident results of the simulated surface topography.

**Keywords:** Multi-scale simulation; dynamic performance; surface simulation; precision machining

## 1.Introduction:

The energy plays an irreplaceable role in the development and progress of society, especially

the fossil fuels, such as coal, petroleum, natural gas. These non-renewable energy promote the rapid development of society, nevertheless, they have caused the unsustainable energy crisis. Renewable sources such as solar, photovoltaic, and wind, will play an essential role in meeting this challenge, but most countries do not have the storage capacity or available land to meet the majority baseload power requirements. Therefore, finding new energy sources is imperative to human survival and development. Scientists have been recognized that fusion energy can provide a highly attractive solution to society's demand for safe and environmentally sustainable energy, at a scale that meets our long-term need. Many countries have carried out the research of the Laser Inertial Fusion (LIF), such as America, France, Britain, Japan, China.

Figure 1 shows the principle of the LIF: the low-energy beam is amplified in the preamplifier module and then in the power amplifier, the main amplifier, and again in the power amplifier before the beam run through the switchyard and into the target chamber to achieve nuclear fusion [1-3]. The KDP crystal is the key optical element in this system, which is used as harmonic frequency converters in the optical path, and can make frequency multiplication and optical switching. However, the current low laser induced damage threshold (LIDT) of the KDP crystal has become a bottleneck, which restricts the application and development of LIF system [4,5]. In addition to the material qualities of KDP crystal, the topographic properties of surface especially machined surface also affects the LIDT obviously [6]. Therefore, during the KDP crystal machining, enough attention must be paid to the surface topographic generation. In the spatial frequency region from  $3.0 \times 10^{-2}$  to  $8.3 \text{ mm}^{-1}$ , we define a maximum “waviness” in terms of a power spectral density (PSD). The PSD simply represents the square of the phase noise amplitude ( $\text{nm}^2$ ) over a certain spatial frequency ( $\text{mm}^{-1}$ ) and thus has the unusual set of units  $\text{nm}^2 \text{mm}$ . The

KDP crystal in LIF system has extremely harsh requirements of the topography. In this study, the specific indexes for the KDP crystal are as follows: It requires roughness values of less than 3 nm in 0.01~0.12 mm; a root mean square (RMS) no more than 4.2 nm, and a PSD2 better than 15 nm<sup>2</sup>/mm in 0.12~2.5mm; a RMS of less than 6.4 nm and PSD1 better than 15 nm<sup>2</sup>/mm in 2.5~33 mm; and a gradient root mean square (GRMS) better than 11 nm/cm in the range over 33 mm [7]. In addition, the sub-surface damage will affect the light transmittance, so low sub-surface damage is also needed. The KDP crystal is hygroscopic and heat-sensitive, so that traditional lapping and polishing methods are not applicable for processing this material [8-10]. Therefore, the final surface quality can only be achieved by fly cutting. High frequency roughness can cause beam divergence and reduce the surface thermal damage resistance, medium and low spatial frequency will lead to nonlinear self-focusing and reduce the laser damage threshold of the element. In order to investigate the influence of machine tool performance and processing parameters on the surface generation, a multi-scale simulation model of the fly cutting machining is urgently needed.

The process of surface generation has attracted a lot of research interest. Luo et al. presented a surface generation model, containing the dynamic cutting process and the effects of machining process variables and tooling characteristics [11]. Lee et al. proposed an ultra-precision cutting surface modelling and simulation method based on machine tool kinematics and cutting theory [12]. Zhou et al. established a dynamic cutting force model and studied its impact on the generation of surface topography and texture in nano/micro cutting [13]. Sun et al. proposed a quasi-continuum based multi-scale simulation method to investigate the nano-metric cutting of single crystal aluminum [14]. Wang et al. presented a novel solution to the simulation of the KDP crystal 3D topography surface that achieved by single point diamond turning operation by using

wavelet analysis and orthogonal design methods [15]. All of them did outstanding works. However, the ultra-precision machining differs from conventional machining as it deals with physical phenomenon from the micro-scale of dislocations to the macro-scale of a cutting tool [16], and most of the works to date focused on a particular aspect of the technology, and seldom of which link up the different length scales which affect the quality of machined surface at the macro-, micro- and nano-levels. Especially, for the KDP crystal used in the LIF, it has harsh requirements of not only the roughness, but also the waviness and the profile accuracy, so it needs the full scale simulation of the surface topography generation. Therefore, a multi-scale simulation is presented in this paper based on the machine tool performance and processing parameters.

## **2.Multi-scale surface simulation of the fly cutting machining**

The ultra-precision fly cutting machine tool used for KDP crystal machining is illustrated in Fig. 2. A bridge supports a vertical-axis spindle and flycutter over a horizontal-axis slide. Mounted to the horizontal slide is a vacuum chuck that fixing the workpiece by vacuum power. The surface to be machined lies in a horizontal plane [17]. The influence of the processing parameters and the machine tool performance on the surface morphology, such as flatness, waveness, roughness and subsurface damage is given in Fig.2, respectively. That is to say, while the prediction model is established, the influential factors can be controlled intentionally in terms of the desired surface topography. The following text will discuss the influential factors and simulate the surface in the macro, micro and nano scales, separately.

### **2.1 The macro scale surface simulation**

Taking into account the structure type and kinematic chain of the machine tool, it can be noted that the profile accuracy of the machined surface is affected by the straightness of the slide,

the dynamic stiffness of the machine tool, the rotation speed of the spindle, squareness error between the spindle and the slide, and the chucking deformation of the workpiece. In this study the squareness error between the spindle and the slide is excellent after testing, and chucking deformation of the workpiece is small due to the vacuum adsorption. Therefore, only the first three major factors are considered in the profile accuracy simulation. The straightness of the slide is 0.8  $\mu\text{m}$  in the 415 mm processing length as shown in Fig.3. The cutter will cut more on the peaks of straightness, forming the valleys on the workpiece surface, and the cutter will cut less on the valleys of the straightness, forming the peaks on the workpiece surface. The profile caused by the straightness combining with the large-period waviness together, affecting the GRMS of the machined surface. The waviness caused by the dynamic performance of the machine tool will be discussed in the following.

In order to gain the dynamic performance of the machine tool, an accurate FE model is built according to the real machine model, as shown in Fig.4. The input is the periodically interrupted cutting force and the output is the vibration of the tool which will form the waviness on the surface. Fig.5 shows the dynamic performance of the machine tool. The relationship between the period of the waviness and dynamic performance can be expressed by Eq. (1), which is shown below:

$$T_D = \frac{\pi d \times n_0 \times \cos \theta}{60 \omega_n} \quad (1)$$

Where,  $d$  denotes the diameter of the flyhead ( $d=630$  mm),  $n_0$  denotes the rotation speed of spindle ( $n_0=300$  rpm),  $\theta$  denotes the maximum angle of the tangent direction in cutting process ( $\theta=0^\circ$ ), and  $T_D$  denotes the period of the vertical stripes ( $T_D=17.3$  mm). According to Eq. (1), the low-level frequency (less than 300 Hz) will cause the large-period waviness ( $>33$  mm) which

affects the GRMS, while the high-level frequency (larger than 300 Hz) will cause the small period waveness ( $<33 \text{ mm}$ ) which affects the PSD1.

Fig. 6 shows the low and high levels frequency response of the tool tip under the cutting force. The 3D surface is generated by combining the straightness with the dynamic response factors as shown in Fig. 7. In order to test the simulation surface by the test software Zygo, the simulation surface results are changed into the format which can be read by Zygo. To test the flatness index GRMS, which with only tip, tilt, and piston removed, the low pass filter is used and the high-pass frequency is  $0.0303 \text{ mm}^{-1}$ , the test result shows GRMS is  $0.0153 \text{ wv/cm}$  ( $9.685 \text{ nm/cm}$ ), as shown in Fig.8. And in order to get the PSD1 index, the band pass filter is used, the high-pass frequency is  $0.4 \text{ mm}^{-1}$  and the low-pass frequency is  $0.0303 \text{ mm}^{-1}$ , the test result in this frequency region shows the RMS is  $3.251 \text{ nm}$  in Fig.9. Fig.10 shows that the PSD1 in this region are all bellow the not-to-exceed line for the PSD.

## **2.2.The micro scale surface simulation**

As shown in Fig.11, when the spindle is rotating, it has runout in axial and radial directions. The runout in radial direction will affect the cutting depth, and when the feed is small, it will cause cutting interference phenomenon [18], leading to different residual height. While the runout in radial direction will affect the cutting area and feed per revolution. The runout of the spindle both in axial and radial directions is tested by spindle error analyzer (Lion Precision, Automated Quality Technologies, USA), as shown in Fig.12, the spindle runout in axial direction is  $20 \text{ nm}$ , the spindle runout in radial direction is  $30 \text{ nm}$ . In the roughness simulation model, the spindle runout in both axial and radial directions are considered.

The simulation roughness surface is obtained as shown in Fig.13, the simulation parameters

are: the feed is 75  $\mu\text{m/s}$ , the spindle rotation speed is 300 r/min and the nose of the cutter tool is 5 mm. The simulation result shows that the roughness of the surface is 3nm.

### **2.3.The nano scale surface simulation**

In order to study the influence of the tool geometry on sub-surface damage of the machined surface, the MD simulation is carried out in nano scale. In this simulation model, two cutter tools are compared, one is straight edge, the other is circular blade. As shown in Fig.14, it can be noted that under the same cutting parameters, such as the cutter depth and the cutting speed, the cutter tool with circular blade will cause smaller sub-surface damage thickness, with 18 layers of atoms compared with 20 layers of atoms caused by the cutter tool with straight edge. Although the simulation scale is very small compared with the real situation, it can give that the cutter tool with circular blade is qualitatively better than the cutter tool with straight edge from the sub-surface damage point of view. Therefore, in order to get the smaller sub-surface damage, the cut tool with circular blade should be used.

### **3. Experimental verification**

Machining trials are carried out on the ultra precision fly cutting machine tool whose performance is used in the simulation model to validate the model and simulation. The same machining parameters as in the simulation are used in the processing experiments. The experimental results are examined by a 3D rough surface tester, Wyko RST-plus (Veeco Metrology Group, Santa Barbara, CA, USA), which has a 500mm vertical measurement range and 3 nm vertical resolution. The test result is read by the software Zygo. The measurement results with only tip, tilt, and piston removed, are shown in Figure 15-18. It shows that the GRMS of the machined surface is 0.017 wv/cm (10.76 nm/cm), the PSD1 is bellow the not-to-exceed line, the

RMS is 3.8 nm, the roughness is 2 nm. The test results are in good agreement with the analytical and simulation results, which verifies the validity and reliability of the simulation model.

#### **4.Conclusion:**

To bridge the gap between the surface topography generation and the machine tool performance, a multi-scale modelling method of the fly cutting process is presented in the macro, micro and nano scales, with the comprehensive consideration of the machining parameters and the performance of the machine tool. The following conclusions can be drawn.

1.The multi-scale modelling method contributes to more comprehensive and better understanding of the relationship between the surface generation and the machine tool performance, and realizes the prediction of the surface morphology in different scales, which is more efficient and economical.

2.The influential factors for different scales are discussed and used in the surface modelling. The influence of the machining parameters on the surface in different scales is discussed. By modelling the surface with different machining parameters, we can get different surfaces, and the test software shows the results of the modelling surface morphology. Through this method, the optimization of the parameters such as the spindle rotation speed and the feed speed can be achieved.

3. The successful development of the model-based system realizes the prediction of the influence of the machine tool performance on the surface. It can help to quantitatively analyze the influence of machine performance indicators such as the straightness, dynamic stiffness and natural frequency on the surface morphology, and lead us to a better understanding of the ultra-precision machine performance.



4. These experimental tests evaluate and validate that the proposed simulation approach is effective and efficient in multi scale surface prediction. It indicates that the proposed simulation approach can be used as a powerful tool for the machine tool performance and machining parameters optimization, which also enables the machining results meet the machining requirements.

## **5. Acknowledgment**

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## Figure captions:

Fig.1 The principle of the LIF.

Fig.2 The influence of the machine tool parameters on the surface morphology.

Fig.3 The straightness of the slide.

Fig.4 The dynamic response of the machine tool.

Fig.5 The dynamic performance of the machine tool.

Fig.6 The low and high level frequency response under the cutting force.

Fig.7 The 3D simulation surface of the workpiece.

Fig.8 The simulation GRMS test result.

Fig.9 The simulation RMS test in PSD1 region.

Fig.10 The simulation PSD test in PSD1 region.

Fig.11 The spindle runout and the generation of the surface.

Fig.12 The test spindle runout in axial and radial directions.

Fig.13 The simulation result of the roughness.

Fig.14 The MD simulation for different cutter profile.

Fig.15 The test result of GRMS.

Fig.16 The test RMS result in PSD1 region.

Fig.17 The test PSD result in PSD1 region.

Fig.18 The test result of the roughness.

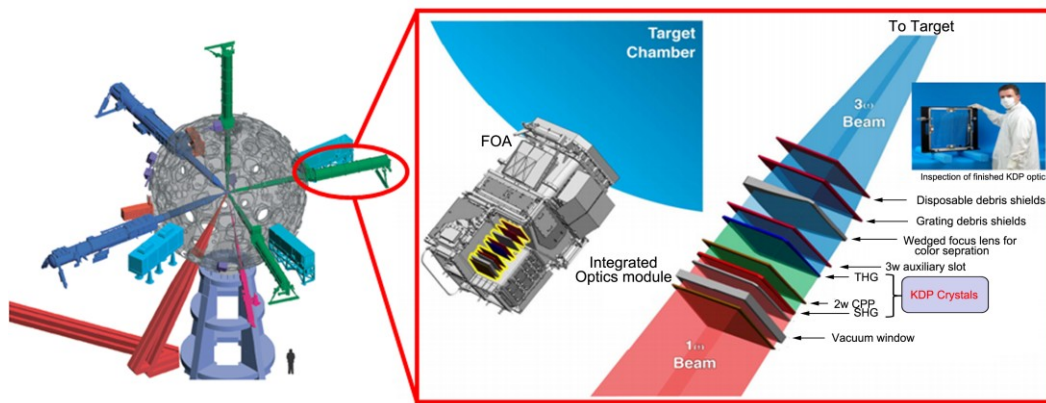


Fig.1 The principle of the LIF.

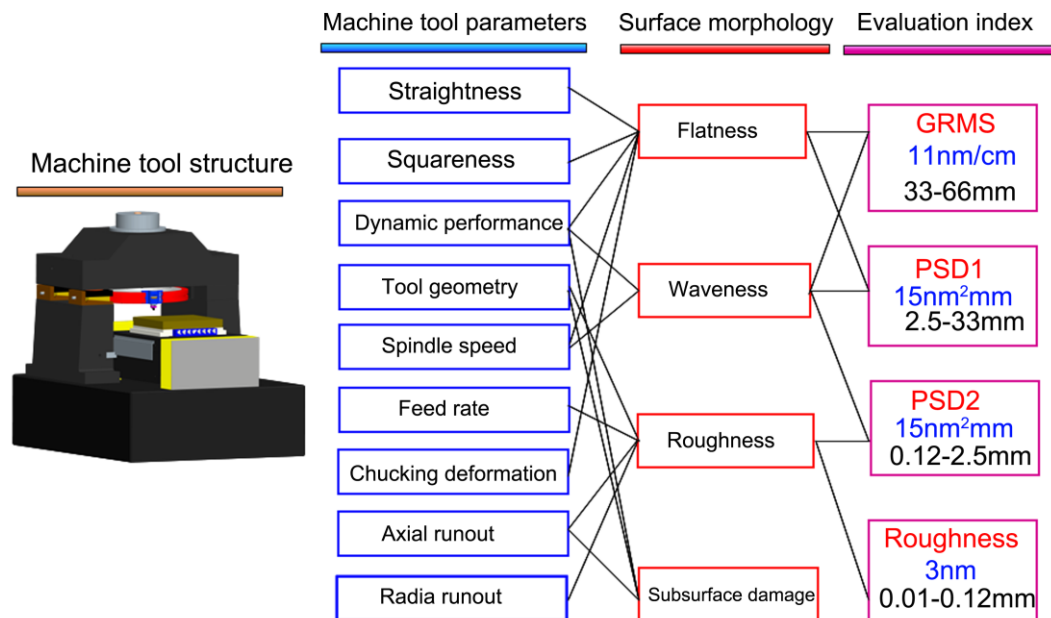


Fig.2 The influence of the machine tool parameters on the surface morphology.

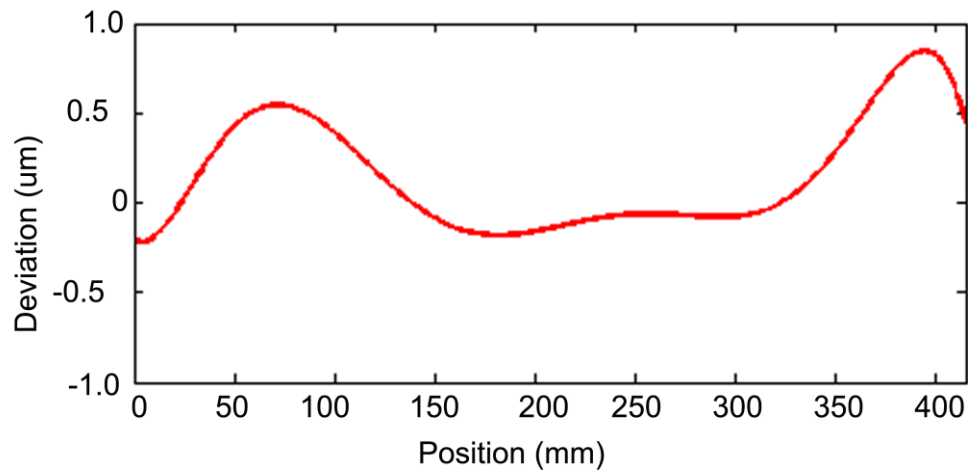


Fig.3 The straightness of the slide.

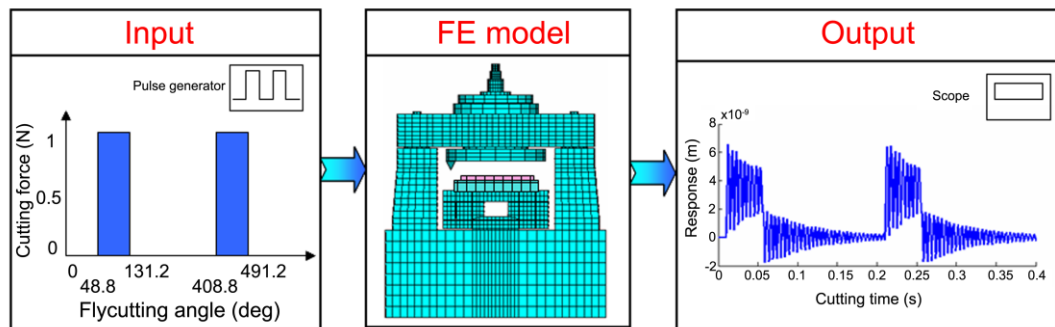


Fig.4 The dynamic response of the machine tool.

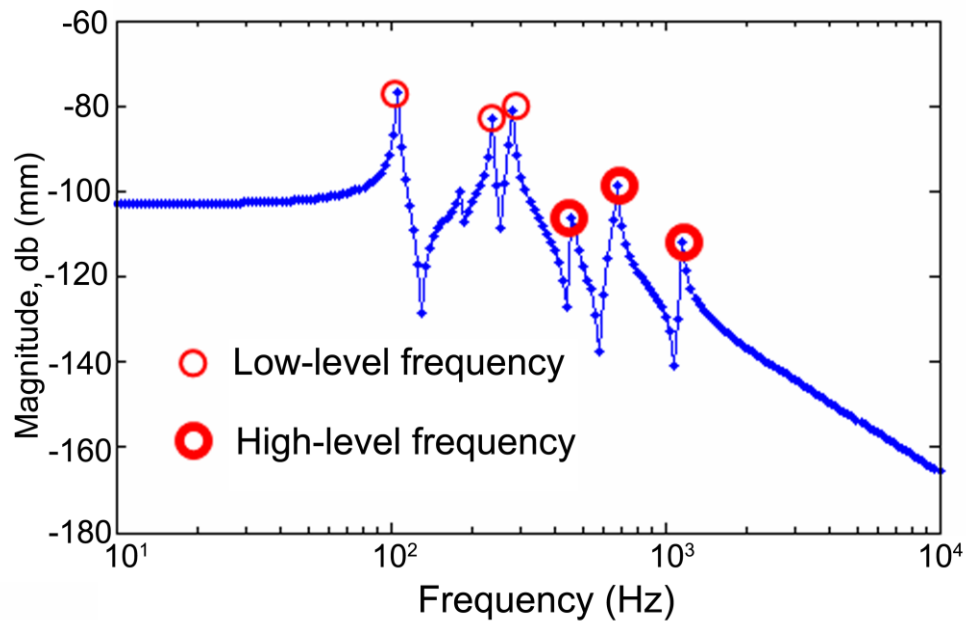


Fig.5 The dynamic performance of the machine tool.

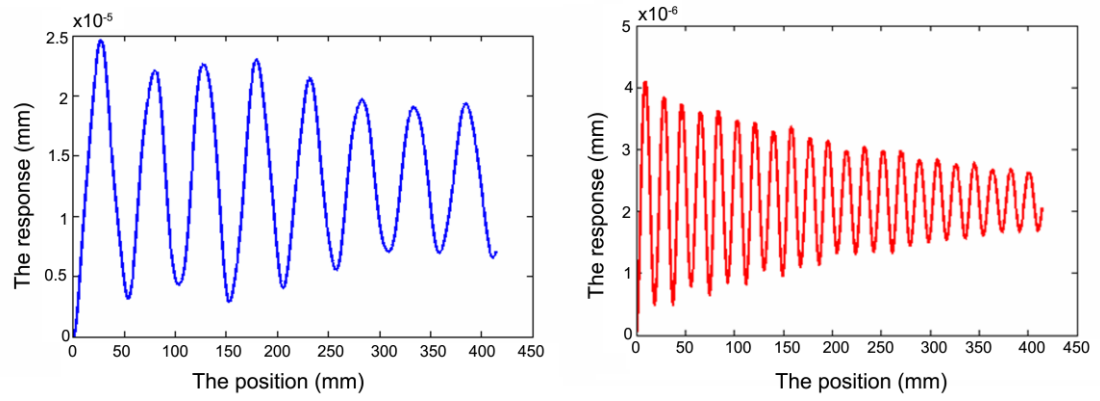


Fig.6 The low and high level frequency response under the cutting force.

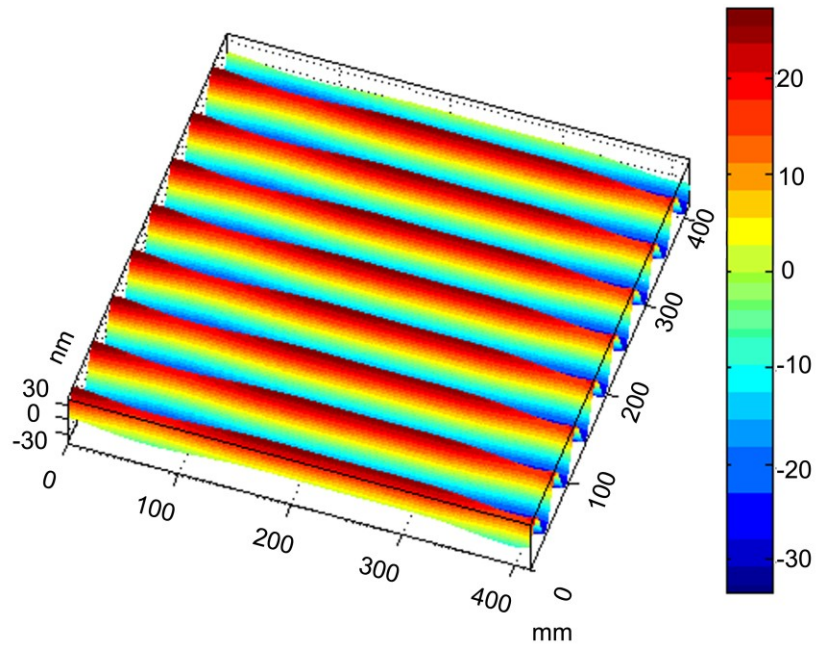


Fig.7 The 3D simulation surface of the workpiece.

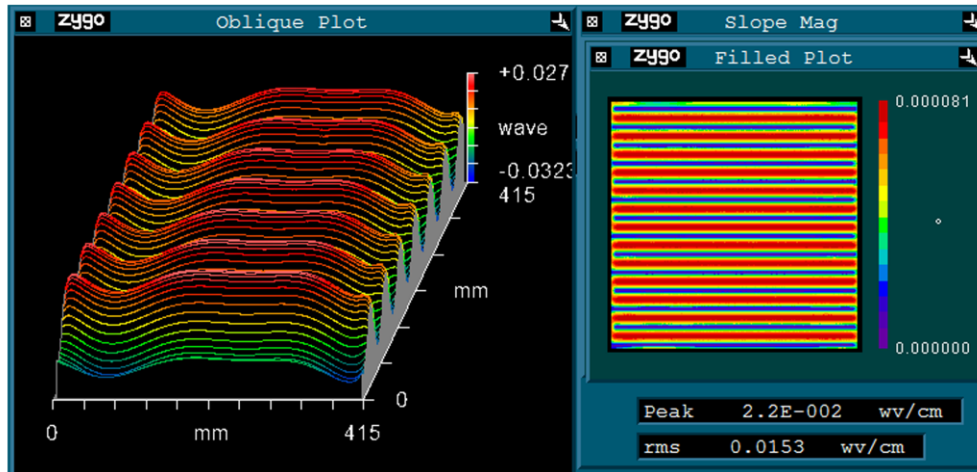


Fig.8 The simulation GRMS test result.

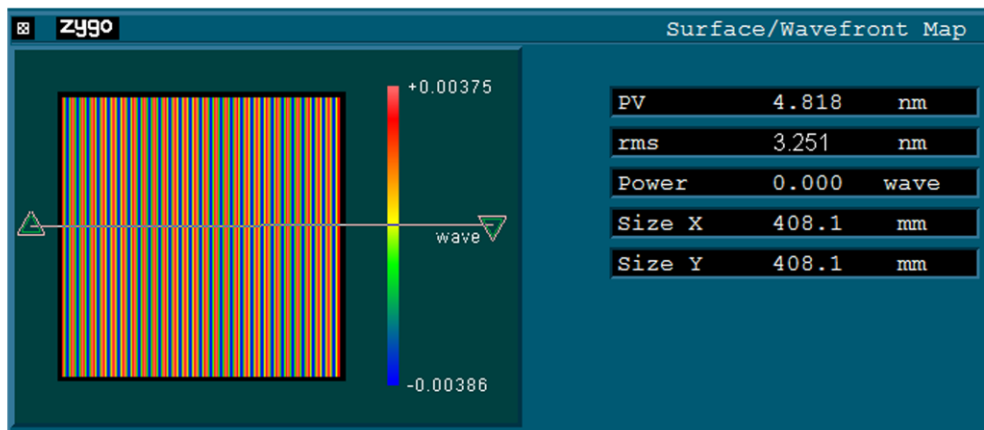


Fig.9 The simulation RMS test in PSD1 region.



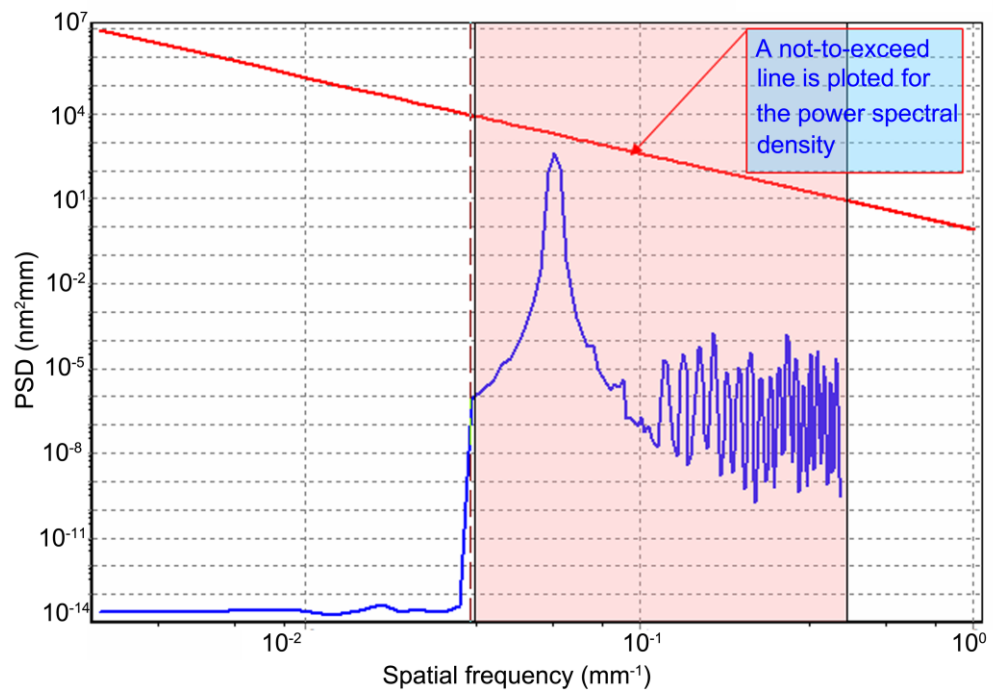


Fig.10 The simulation PSD test in PSD1 region.

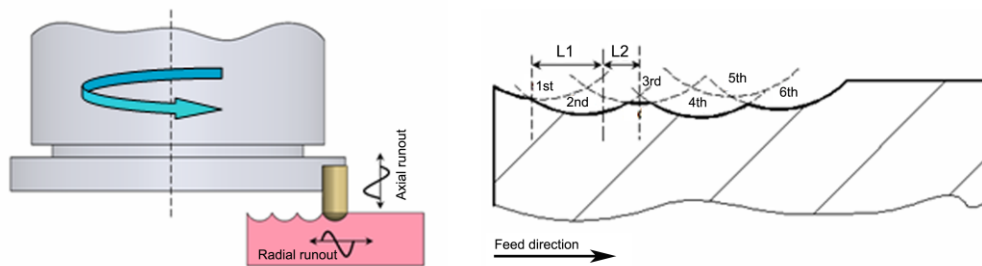


Fig.11 The spindle runout and the generation of the surface.

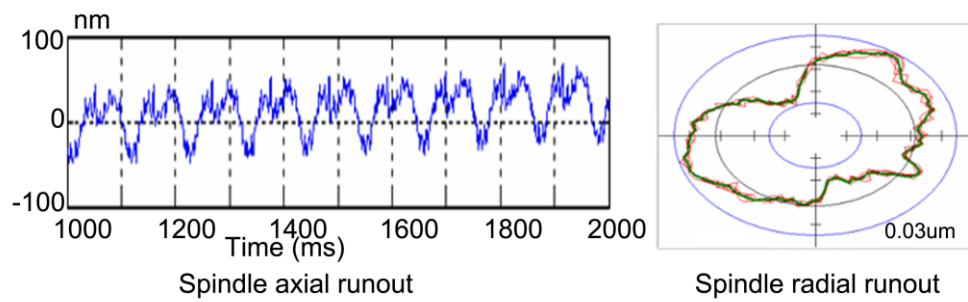


Fig.12 The test spindle runout in axial and radial directions.

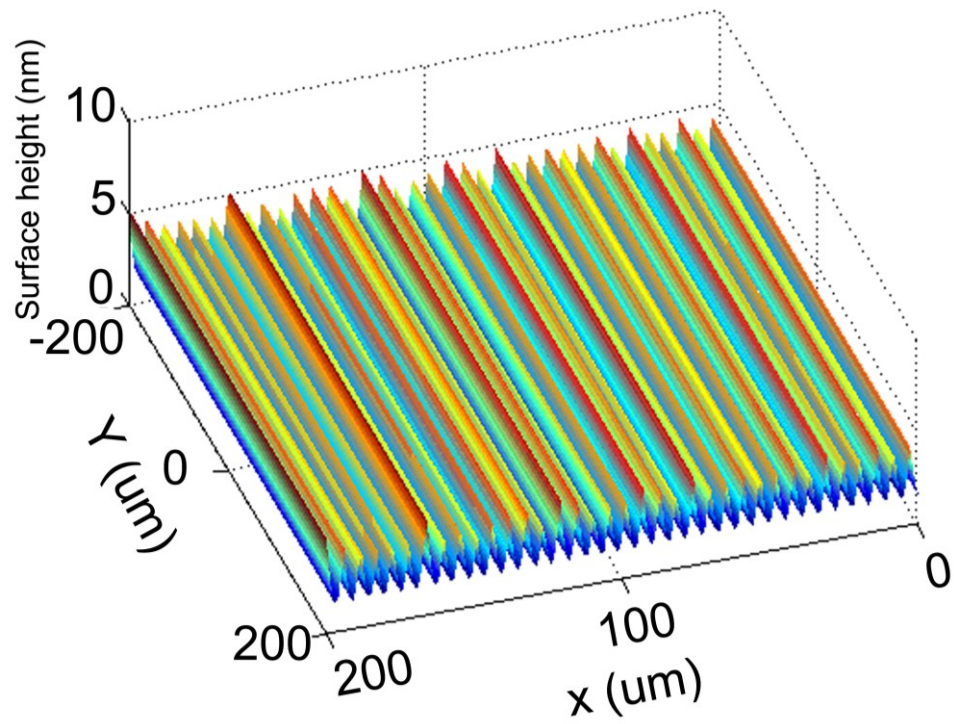


Fig.13 The simulation result of the roughness.

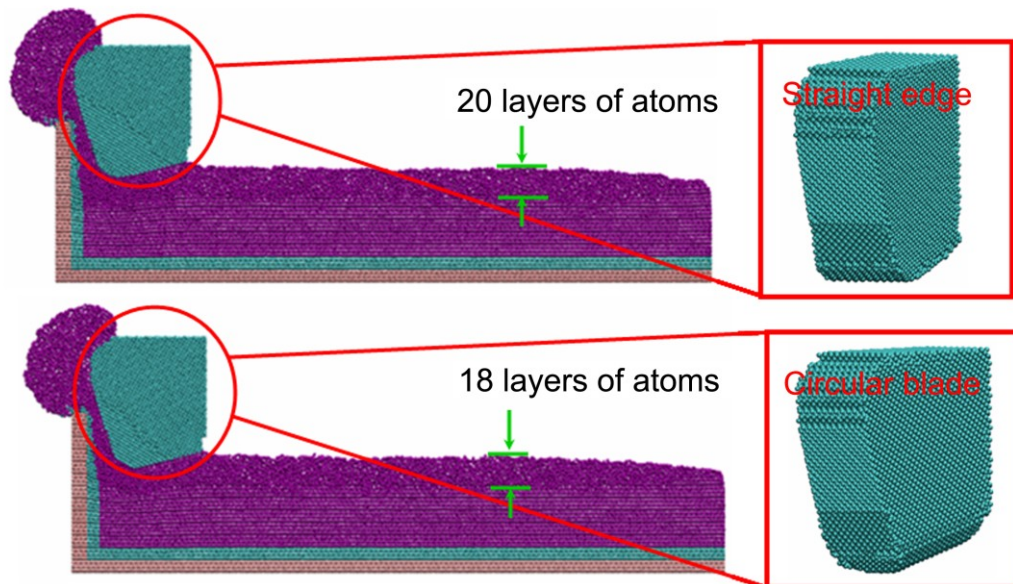


Fig.14 The MD simulation for different cutter profile.

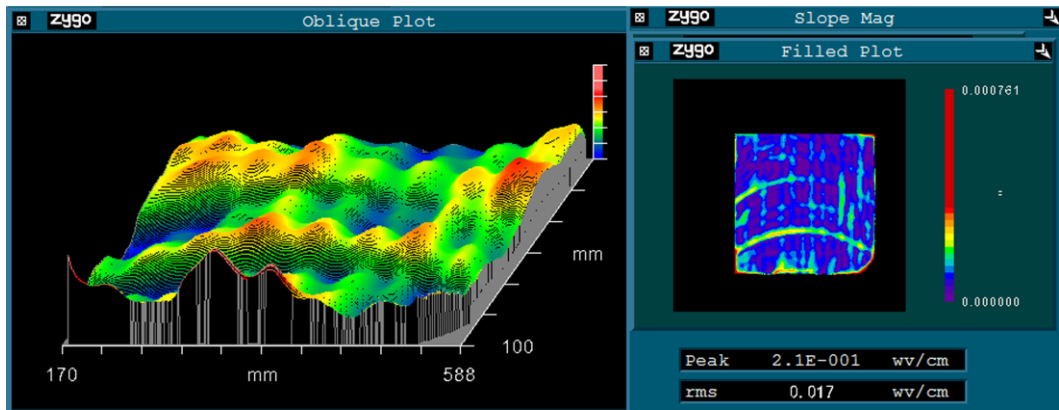


Fig.15 The test result of GRMS.

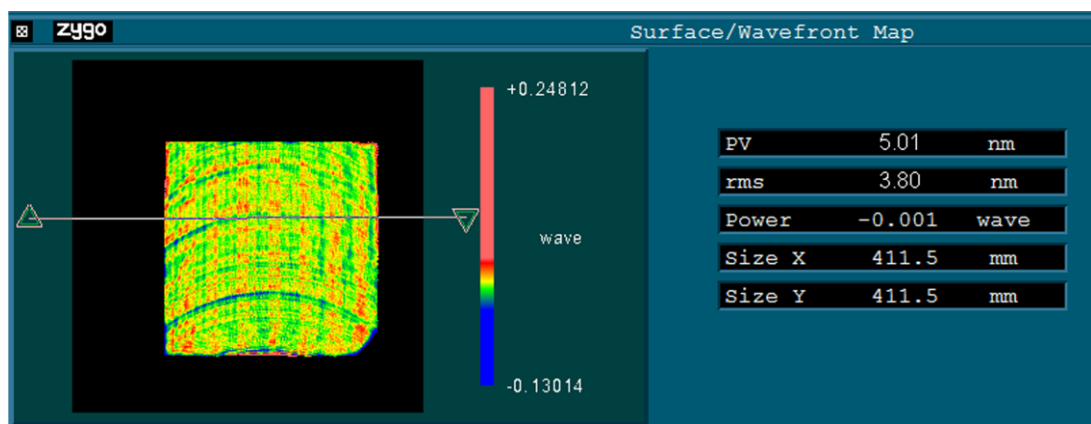


Fig.16 The test RMS result in PSD1 region.

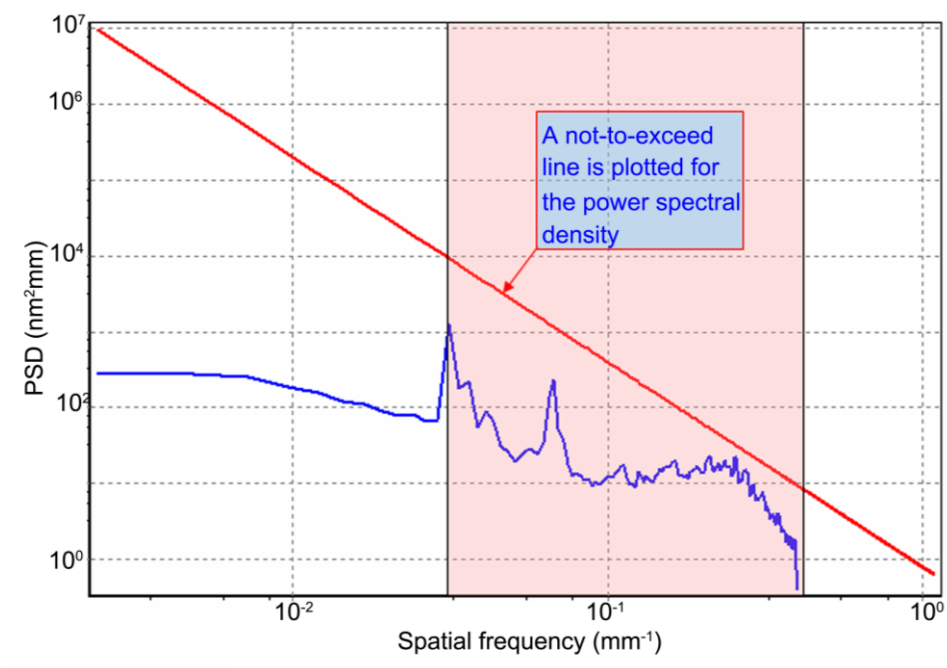


Fig.17 The test PSD result in PSD1 region.

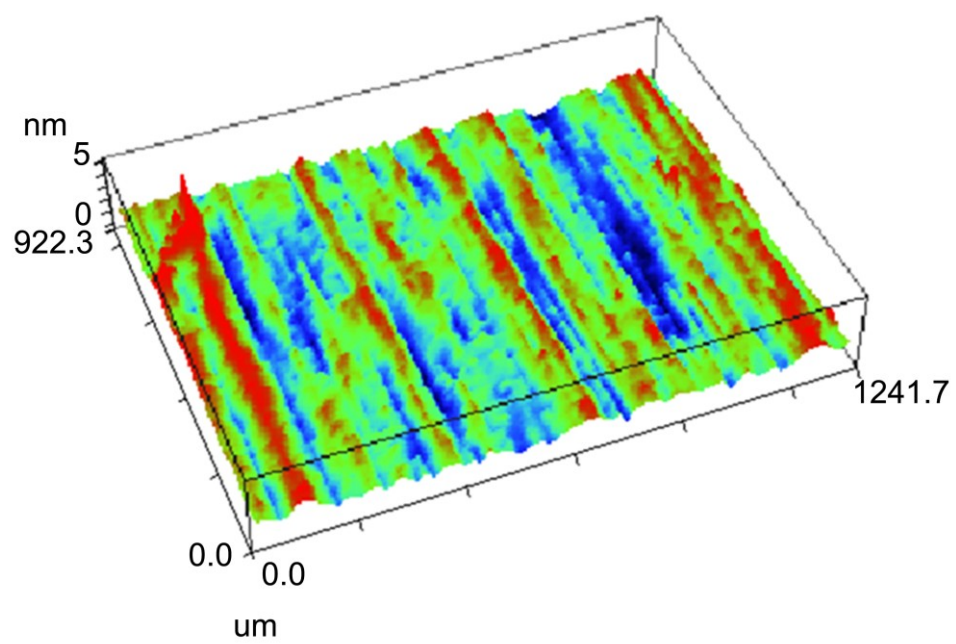


Fig.18 The test result of the roughness.